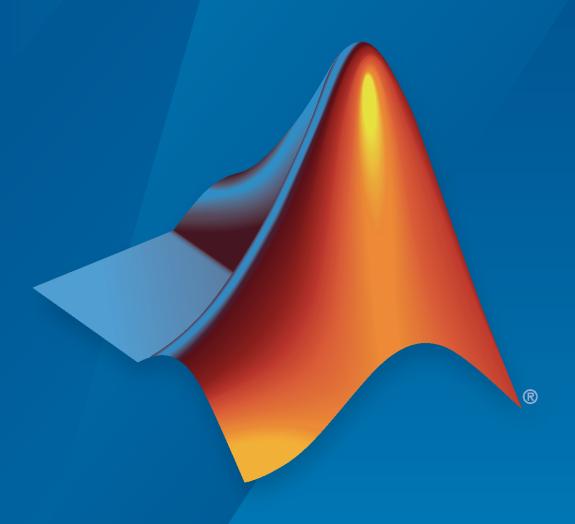
Navigation Toolbox™

Reference



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Contents

	Functions
1	
2	Classes
3	Methods
4	Blocks
	
	Apps
5	

Functions

allanvar

Allan variance

Syntax

```
[avar,tau] = allanvar(Omega)
[avar,tau] = allanvar(Omega,m)
[avar,tau] = allanvar(Omega,ptStr)
[avar,tau] = allanvar(____,fs)
```

Description

Allan variance is used to measure the frequency stability of oscillation for a sequence of data in the time domain. It can also be used to determine the intrinsic noise in a system as a function of the averaging time. The averaging time series τ can be specified as $\tau = m/fs$. Here fs is the sampling frequency of data, and fs is a list of ascending averaging factors (such as 1, 2, 4, 8, ...).

[avar,tau] = allanvar(Omega) returns the Allan variance avar as a function of averaging time tau. The default averaging time tau is an octave sequence given as $(1, 2, ..., 2^{\text{floor}\{\log_2[(N-1)/2]\}})$, where N is the number of samples in Omega. If Omega is specified as a matrix, allanvar operates over the columns of omega.

[avar,tau] = allanvar(Omega,m) returns the Allan variance avar for specific values of tau defined by m. Since the default frequency fs is assumed to be 1, the output tau is exactly same with m

[avar,tau] = allanvar(Omega,ptStr) sets averaging factor m to the specified point specification, ptStr. Since the default frequency fs is 1, the output tau is exactly equal to the specified m. ptStr can be specified as 'octave' or 'decade'.

[avar,tau] = allanvar(____,fs) also allows you to provide the sampling frequency fs of the input data omega in Hz. This input parameter can be used with any of the previous syntaxes.

Examples

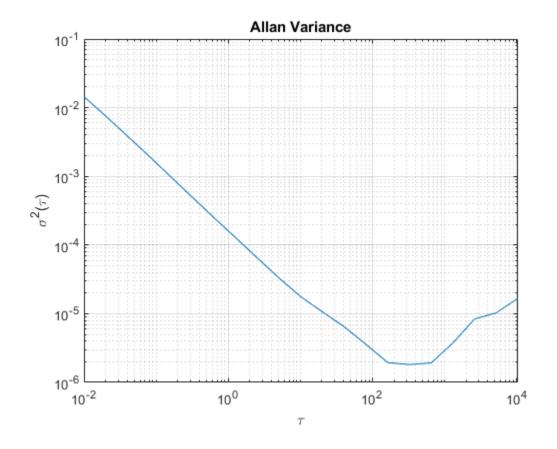
Determine Allan Variance of Single Axis Gyroscope

Load gyroscope data from a MAT file, including the sample rate of the data in Hz. Calculate the Allan variance.

```
load('LoggedSingleAxisGyroscope','omega','Fs')
[avar,tau] = allanvar(omega,'octave',Fs);

Plot the Allan variance on a loglog plot.

loglog(tau,avar)
xlabel('\tau')
ylabel('\sigma^2(\tau)')
title('Allan Variance')
grid on
```



Determine Allan Deviation at Specific Values of au

Generate sample gyroscope noise, including angle random walk and rate random walk.

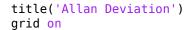
```
numSamples = 1e6;
Fs = 100;
nStd = 1e-3;
kStd = 1e-7;
nNoise = nStd.*randn(numSamples,1);
kNoise = kStd.*cumsum(randn(numSamples,1));
omega = nNoise+kNoise;
```

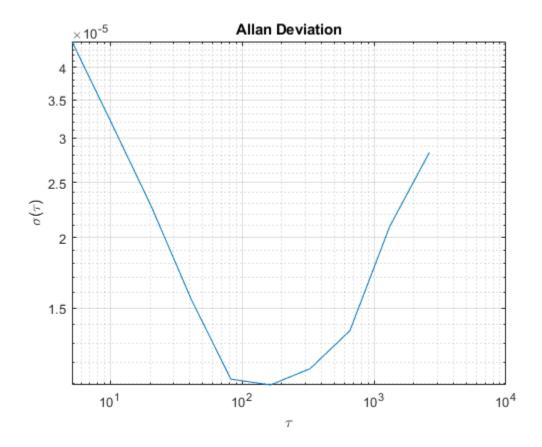
Calculate the Allan deviation at specific values of $m = \tau$. The Allan deviation is the square root of the Allan variance.

```
m = 2.^(9:18);
[avar,tau] = allanvar(omega,m,Fs);
adev = sqrt(avar);
```

Plot the Allan deviation on a loglog plot.

```
loglog(tau,adev)
xlabel('\tau')
ylabel('\sigma(\tau)')
```





Input Arguments

0mega — Input data

N-by-1 vector | *N*-by-*M* matrix

Input data specified as an N-by-1 vector or an N-by-M matrix. N is the number of samples, and M is the number of sample sets. If specified as a matrix, allanvar operates over the columns of Omega.

Data Types: single | double

m — Averaging factor

scalar | vector

Averaging factor, specified as a scalar or vector with ascending integer values less than (N-1)/2, where N is the number of samples in Omega.

Data Types: single | double

ptStr — Point specification of m

'octave' (default) | 'decade'

Point specification of m, specified as 'octave' or 'decade'. Based on the value of ptStr, m is specified as following:

• If ptStr is specified as 'octave', m is:

$$\left[2^0, 2^1 \dots 2 \left| \log_2 \left(\frac{N-1}{2} \right) \right| \right]$$

• If ptStr is specified as 'decade', m is:

$$\left[10^{0}, 10^{1}...10 \left| \log_{10} \left(\frac{N-1}{2} \right) \right| \right]$$

N is the number of samples in Omega.

fs — Basic frequency of input data in Hz

scalar

Basic frequency of the input data, Omega, in Hz, specified as a positive scalar.

Data Types: single | double

Output Arguments

avar — Allan variance of input data

vector | matrix

Allan variance of input data at tau, returned as a vector or matrix.

tau — Averaging time of Allan variance

vector | matrix

Averaging time of Allan variance, returned as a vector, or a matrix.

See Also

gyroparams | imuSensor

Introduced in R2019a

angdiff

Difference between two angles

Syntax

```
delta = angdiff(alpha,beta)
delta = angdiff(alpha)
```

Description

delta = angdiff(alpha,beta) calculates the difference between the angles alpha and beta. This function subtracts alpha from beta with the result wrapped on the interval [-pi,pi]. You can specify the input angles as single values or as arrays of angles that have the same number of values.

delta = angdiff(alpha) returns the angular difference between adjacent elements of alpha along the first dimension whose size does not equal 1. If alpha is a vector of length n, the first entry is subtracted from the second, the second from the third, etc. The output, delta, is a vector of length n-1. If alpha is an m-by-n matrix with m greater than 1, the output, delta, will be a matrix of size m-1-by-n.

Examples

Calculate Difference Between Two Angles

```
d = angdiff(pi,2*pi)
d = 3.1416
```

Calculate Difference Between Two Angle Arrays

```
d = angdiff([pi/2 3*pi/4 0],[pi pi/2 -pi])
d = 1\times3
1.5708 -0.7854 -3.1416
```

Calculate Angle Differences of Adjacent Elements

```
angles = [pi pi/2 pi/4 pi/2];
d = angdiff(angles)
d = 1 \times 3
```

-1.5708 -0.7854 0.7854

Input Arguments

alpha — Angle in radians

scalar | vector | matrix | multidimensional array

Angle in radians, specified as a scalar, vector, matrix, or multidimensional array. This is the angle that is subtracted from beta when specified.

Example: pi/2

beta — Angle in radians

scalar | vector | matrix | multidimensional array

Angle in radians, specified as a scalar, vector, matrix, or multidimensional array of the same size as alpha. This is the angle that alpha is subtracted from when specified.

Example: pi/2

Output Arguments

delta — Difference between two angles

scalar | vector | matrix | multidimensional array

Angular difference between two angles, returned as a scalar, vector, or array. delta is wrapped to the interval [-pi,pi].

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder $^{\text{\tiny TM}}$.

Introduced in R2015a

axang2quat

Convert axis-angle rotation to quaternion

Syntax

```
quat = axang2quat(axang)
```

Description

quat = axang2quat(axang) converts a rotation given in axis-angle form, axang, to quaternion,
quat.

Examples

Convert Axis-Angle Rotation to Quaternion

```
axang = [1 0 0 pi/2];
quat = axang2quat(axang)
quat = 1×4
    0.7071    0.7071    0    0
```

Input Arguments

axang — Rotation given in axis-angle form

```
n-by-4 matrix
```

Rotation given in axis-angle form, specified as an n-by-4 matrix of n axis-angle rotations. The first three elements of every row specify the rotation axis, and the last element defines the rotation angle (in radians).

```
Example: [1 0 0 pi/2]
```

Output Arguments

quat — Unit quaternion

```
n-by-4 matrix
```

Unit quaternion, returned as an n-by-4 matrix containing n quaternions. Each quaternion, one per row, is of the form $q = [w \times y \ z]$, with w as the scalar number.

```
Example: [0.7071 0.7071 0 0]
```

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder $^{\text{\tiny TM}}$.

See Also

quat2axang

Introduced in R2015a

axang2rotm

Convert axis-angle rotation to rotation matrix

Syntax

```
rotm = axang2rotm(axang)
```

Description

rotm = axang2rotm(axang) converts a rotation given in axis-angle form, axang, to an
orthonormal rotation matrix, rotm. When using the rotation matrix, premultiply it with the
coordinates to be rotated (as opposed to postmultiplying).

Examples

Convert Axis-Angle Rotation to Rotation Matrix

Input Arguments

axang — Rotation given in axis-angle form

```
n-by-4 matrix
```

Rotation given in axis-angle form, specified as an n-by-4 matrix of n axis-angle rotations. The first three elements of every row specify the rotation axis, and the last element defines the rotation angle (in radians).

```
Example: [1 0 0 pi/2]
```

Output Arguments

rotm — Rotation matrix

```
3-by-3-by-n matrix
```

Rotation matrix, returned as a 3-by-3-by-n matrix containing n rotation matrices. Each rotation matrix has a size of 3-by-3 and is orthonormal. When using the rotation matrix, premultiply it with the coordinates to be rotated (as opposed to postmultiplying).

```
Example: [0 0 1; 0 1 0; -1 0 0]
```

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder $^{\text{\tiny TM}}$.

See Also

rotm2axang

Introduced in R2015a

axang2tform

Convert axis-angle rotation to homogeneous transformation

Syntax

```
tform = axang2tform(axang)
```

Description

tform = axang2tform(axang) converts a rotation given in axis-angle form, axang, to a homogeneous transformation matrix, tform. When using the transformation matrix, premultiply it with the coordinates to be transformed (as opposed to postmultiplying).

Examples

Convert Axis-Angle Rotation to Homogeneous Transformation

Input Arguments

axang — Rotation given in axis-angle form

```
n-by-4 matrix
```

Rotation given in axis-angle form, specified as an n-by-4 matrix of n axis-angle rotations. The first three elements of every row specify the rotation axis, and the last element defines the rotation angle (in radians).

```
Example: [1 0 0 pi/2]
```

Output Arguments

tform — Homogeneous transformation

```
4-by-4-by-n matrix
```

Homogeneous transformation matrix, specified by a 4-by-4-by-n matrix of n homogeneous transformations. When using the transformation matrix, premultiply it with the coordinates to be formed (as opposed to postmultiplying).

```
Example: [0 0 1 0; 0 1 0 0; -1 0 0 0; 0 0 0 1]
```

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder $^{\text{\tiny TM}}$.

See Also

tform2axang

Introduced in R2015a

buildMap

Build occupancy map from lidar scans

Syntax

```
map = buildMap(scans,poses,mapResolution,maxRange)
```

Description

map = buildMap(scans, poses, mapResolution, maxRange) creates a occupancyMap map by
inserting lidar scans at the given poses. Specify the resolution of the resulting map,
mapResolution, and the maximum range of the lidar sensor, maxRange.

Examples

Build Occupancy Map from Lidar Scans and Poses

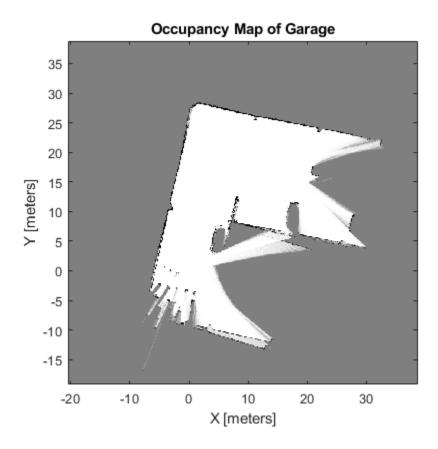
The buildMap function takes in lidar scan readings and associated poses to build an occupancy grid as lidarScan objects and associated [x y theta] poses to build an occupancyMap.

Load scan and pose estimates collected from sensors on a robot in a parking garage. The data collected is correlated using a lidarSLAM algorithm, which performs scan matching to associate scans and adjust poses over the full robot trajectory. Check to make sure scans and poses are the same length.

```
load scansAndPoses.mat
length(scans) == length(poses)
ans = logical
1
```

Build the map. Specify the scans and poses in the buildMap function and include the desired map resolution (10 cells per meter) and the max range of the lidar (19.2 meters). Each scan is added at the associated poses and probability values in the occupancy grid are updated.

```
occMap = buildMap(scans,poses,10,19.2);
figure
show(occMap)
title('Occupancy Map of Garage')
```



Perform SLAM Using Lidar Scans

Use a lidarSLAM object to iteratively add and compare lidar scans and build an optimized pose graph of the robot trajectory. To get an occupancy map from the associated poses and scans, use the buildMap function.

Load Data and Set Up SLAM Algorithm

Load a cell array of lidarScan objects. The lidar scans were collected in a parking garage on a Husky® robot from ClearPath Robotics®. Typically, lidar scans are taken at a high frequency and each scan is not needed for SLAM. Therefore, down sample the scans by selecting only every 40th scan.

```
load garage_fll_southend.mat scans
scans = scans(1:40:end);
```

To set up the SLAM algorithm, specify the lidar range, map resolution, loop closure threshold, and search radius. Tune these parameters for your specific robot and environment. Create the lidarSLAM object with these parameters.

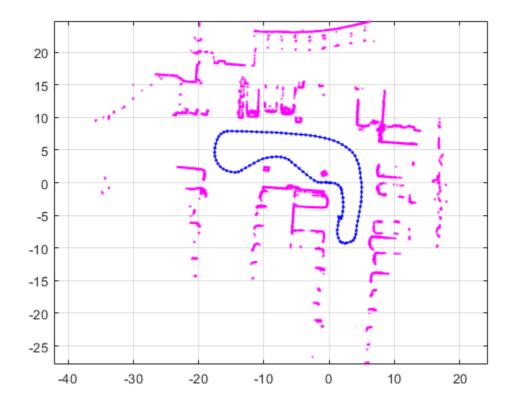
```
maxRange = 19.2; % meters
resolution = 10; % cells per meter

slamObj = lidarSLAM(resolution, maxRange);
slamObj.LoopClosureThreshold = 360;
slamObj.LoopClosureSearchRadius = 8;
```

Add Scans Iteratively

Using a for loop, add scans to the SLAM object. The object uses scan matching to compare each added scan to previously added ones. To improve the map, the object optimizes the pose graph whenever it detects a loop closure. Every 10 scans, display the stored poses and scans.

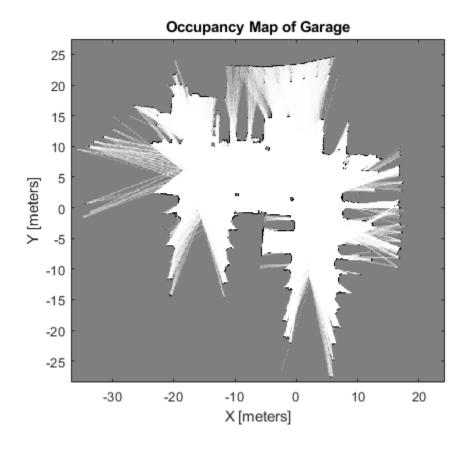
```
for i = 1:numel(scans)
    addScan(slamObj,scans{i});
    if rem(i,10) == 0
        show(slamObj);
    end
end
```



View Occupancy Map

After adding all the scans to the SLAM object, build an occupancyMap map by calling buildMap with the scans and poses. Use the same map resolution and max range you used with the SLAM object.

```
[scansSLAM,poses] = scansAndPoses(slamObj);
occMap = buildMap(scansSLAM,poses,resolution,maxRange);
figure
show(occMap)
title('Occupancy Map of Garage')
```



Input Arguments

scans — Lidar scans

cell array of lidarScan objects

Lidar scans used to build the map, specified as a cell array of lidarScan objects.

poses — Poses of lidar scans

n-by-3 matrix

Poses of lidar scans, specified as an n-by-3 matrix. Each row is an [x y theta] vector representing the xy-position and orientation angle of a scan.

mapResolution — Resolution of occupancy grid

positive integer

Resolution of the output occupancyMap map, specified as a positive integer in cells per meter.

maxRange — Maximum range of lidar sensor

positive scalar

Maximum range of lidar sensor, specified as a positive scalar in meters. Points in the scans outside this range are ignored.

Name-Value Pair Arguments

Specify optional comma-separated pairs of Name, Value arguments. Name is the argument name and Value is the corresponding value. Name must appear inside quotes. You can specify several name and value pair arguments in any order as Name1, Value1, . . . , NameN, ValueN.

Example: ['MapWidth',10]

MapWidth — Width of occupancy grid

positive scalar

Width of the occupancy grid, specified as the comma-separated pair consisting of 'MapWidth' and a positive scalar. If this value is not specified, the map is automatically scaled to fit all laser scans.

MapHeight — Height of occupancy grid

positive scalar

Height of occupancy grid, specified as the comma-separated pair consisting of 'MapHeight' and a positive scalar. If this value is not specified, the map is automatically scaled to fit all laser scans.

Output Arguments

map — Occupancy Map

occupancyMap object

Occupancy map, returned as a occupancyMap object.

See Also

Functions

lidarScan | matchScans | matchScansGrid | transformScan

Classes

lidarSLAM | occupancyMap

Topics

"Implement Simultaneous Localization And Mapping (SLAM) with Lidar Scans"

"Implement Online Simultaneous Localization And Mapping (SLAM) with Lidar Scans"

Introduced in R2019b

cart2hom

Convert Cartesian coordinates to homogeneous coordinates

Syntax

```
hom = cart2hom(cart)
```

Description

hom = cart2hom(cart) converts a set of points in Cartesian coordinates to homogeneous
coordinates.

Examples

Convert 3-D Cartesian Points to Homogeneous Coordinates

```
c = [0.8147 \ 0.1270 \ 0.6324; \ 0.9058 \ 0.9134 \ 0.0975];
h = cart2hom(c)
h = 2\times4
0.8147 \ 0.1270 \ 0.6324 \ 1.0000 \ 0.9058 \ 0.9134 \ 0.0975 \ 1.0000
```

Input Arguments

cart — Cartesian coordinates

```
n-by-(k-1) matrix
```

Cartesian coordinates, specified as an n-by-(k-1) matrix, containing n points. Each row of cart represents a point in (k-1)-dimensional space. k must be greater than or equal to 2.

```
Example: [0.8147 0.1270 0.6324; 0.9058 0.9134 0.0975]
```

Output Arguments

hom — Homogeneous points

n-by-k matrix

Homogeneous points, returned as an n-by-k matrix, containing n points. k must be greater than or equal to 2.

```
Example: [0.2785 0.9575 0.1576 0.5; 0.5469 0.9649 0.9706 0.5]
```

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder $^{\text{\tiny TM}}$.

See Also

hom2cart

Introduced in R2015a

connect

Connect poses for given connection type

Syntax

```
[pathSegments,pathCosts] = connect(connectionObj,start,goal)
[pathSegments,pathCosts] = connect(connectionObj,start,
goal,'PathSegments','all')
```

Description

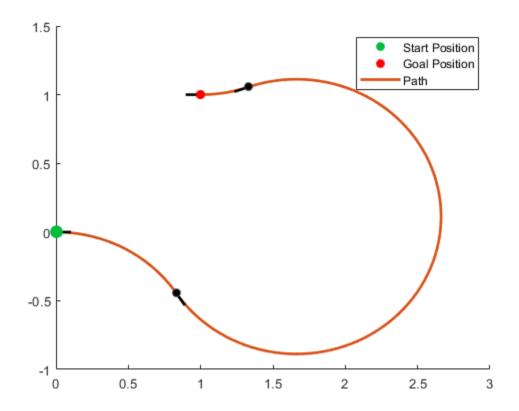
[pathSegments,pathCosts] = connect(connectionObj,start,goal) connects the start and goal poses using the specified dubinsConnection object. The path segment object with the lowest cost is returned.

```
[pathSegments,pathCosts] = connect(connectionObj,start,
goal,'PathSegments','all') returns all possible path segments as a cell array with their
associated costs.
```

Examples

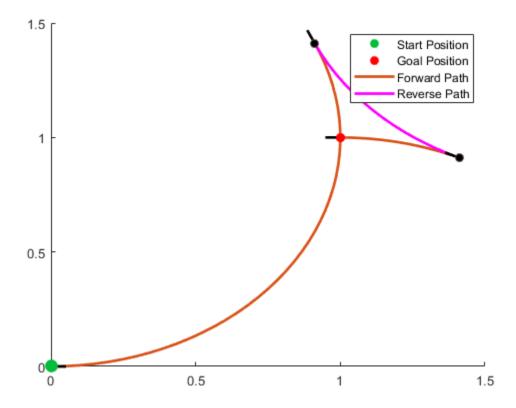
Connect Poses Using Dubins Connection Path

```
Create a dubinsConnection object.
dubConnObj = dubinsConnection;
Define start and goal poses as [x y theta] vectors.
startPose = [0 0 0];
goalPose = [1 1 pi];
Calculate a valid path segment to connect the poses.
[pathSegObj, pathCosts] = connect(dubConnObj,startPose,goalPose);
Show the generated path.
show(pathSegObj{1})
```



Connect Poses Using ReedsShepp Connection Path

```
Create a reedsSheppConnection object.
reedsConnObj = reedsSheppConnection;
Define start and goal poses as [x y theta] vectors.
startPose = [0 0 0];
goalPose = [1 1 pi];
Calculate a valid path segment to connect the poses.
[pathSegObj,pathCosts] = connect(reedsConnObj,startPose,goalPose);
Show the generated path.
show(pathSegObj{1})
```



Input Arguments

connectionObj — Path connection type

dubinsPathSegment object | reedsSheppPathSegment object

Path connection type, specified as a dubinsConnection or reedsSheppConnection object. This object defines the parameters of the connection, including the minimum turning radius of the robot and the valid motion types.

start — Initial pose of robot

 $[x, y, \Theta]$ vector or matrix

This property is read-only.

Initial pose of the robot at the start of the path segment, specified as an $[x, y, \Theta]$ vector or matrix. Each row of the matrix corresponds to a different start pose.

x and y are in meters. Θ is in radians.

The connect function supports:

- Singular start pose with singular goal pose.
- Multiple start pose with singular goal pose.

- Singular start pose with multiple goal pose.
- Multiple start pose with multiple goal pose.

The output pathSegments cell array size reflects the singular or multiple pose options.

goal — Goal pose of robot

[x, v, Θ] vector or matrix

This property is read-only.

Goal pose of the robot at the end of the path segment, specified as an $[x, y, \Theta]$ vector or matrix. Each row of the matrix corresponds to a different goal pose.

x and y are in meters. Θ is in radians.

The connect function supports:

- Singular start pose with singular goal pose.
- · Multiple start pose with singular goal pose.
- Singular start pose with multiple goal pose.
- Multiple start pose with multiple goal pose.

The output pathSegments cell array size reflects the singular or multiple pose options.

Output Arguments

pathSegments — Path segments

cell array of objects

Path segments, specified as a cell array of objects. The type of object depends on the input connectionObj. The size of the cell array depends on whether you use singular or multiple start and goal poses. By default, the function returns the path with the lowest cost for each start and goal pose. When call connect using the 'PathSegments', 'all' name-value pair, the cell array contains all valid path segments between the specified start and goal poses.

pathCosts — Cost of path segment

positive numeric scalar | positive numeric vector | positive numeric matrix

Cost of path segments, specified as a positive numeric scalar, vector, or matrix. Each element of the cost vector or matrix corresponds to a path segment in pathSegment. By default, the function returns the path with the lowest cost for each start and goal pose.

Example: [7.6484,7.5122]

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

Functions

interpolate | show

Objects

dubinsConnection | dubinsPathSegment | reedsSheppConnection |
reedsSheppPathSegment

Introduced in R2019b

createPlanningTemplate

Create sample implementation for path planning interface

Syntax

```
createPlanningTemplate
createPlanningTemplate("StateValidator")
```

Description

createPlanningTemplate creates a planning template for a subclass of the nav.StateSpace class. The function opens a file in the MATLAB® Editor. Save your custom implementation and ensure the file is available on the MATLAB path. Alternative syntax: createPlanningTemplate("StateSpace")

createPlanningTemplate("StateValidator") creates a template for a subclass of the
nav.StateValidator class.

Examples

Create Custom State Space for Path Planning

This example shows how to use the createPlanningTemplate function to generate a template for customizing your own state space definition and sampler to use with path planning algorithms. A simple implementation is provided with the template.

Call the create template function. This function generates a class definition file for you to modify for your own implementation.

createPlanningTemplate

Class and Property Definition

The first part of the template specifies the class definition and any properties for the class. Derive from the nav.StateSpace class. For this example, create a property for the uniform and normal distributions. You can specify any additional user-defined properties here.

Save your custom state space class and ensure your file name matches the class name.

Class Constructor

Use the constructor to set the name of the state space, the number of state variables, and define its boundaries. Alternatively, you can add input arguments to the function and pass the variables in when you create an object.

- For each state variable, define the [min max] values for the state bounds.
- Call the constructor of the base class.
- For this example, you specify the normal and uniform distribution property values using predefined NormalDistribution and UniformDistribution classes.
- Specify any other user-defined property values here.

```
methods
```

Copy Semantics

Specify the copy method definition. Copy all the values of your user-defined variables into a new object, so copyObj is a deep copy. The default behavior given in this example creates a new copy of the object with the same name, state bounds, and distributions.

```
function copyObj = copy(obj)
   copyObj = feval(class(obj));
   copyObj.StateBounds = obj.StateBounds;
   copyObj.UniformDistribution = obj.UniformDistribution.copy;
   copyObj.NormalDistribution = obj.NormalDistribution.copy;
end
```

Enforce State Bounds

Specify how to ensure states are always within the state bounds. For this example, the state values get saturated at the minimum or maximum values for the state bounds.

```
function boundedState = enforceStateBounds(obj, state)
    nav.internal.validation.validateStateMatrix(state, nan, obj.NumStateVariables, "enfo
    boundedState = state;
    boundedState = min(max(boundedState, obj.StateBounds(:,1)'), ...
        obj.StateBounds(:,2)');
end
```

Sample Uniformly

Specify the behavior for sampling across a uniform distribution. support multiple syntaxes to constrain the uniform distribution to a nearby state within a certain distance and sample multiple states.

```
STATE = sampleUniform(OBJ)
STATE = sampleUniform(OBJ, NUMSAMPLES)
STATE = sampleUniform(OBJ, NEARSTATE, DIST)
STATE = sampleUniform(OBJ, NEARSTATE, DIST, NUMSAMPLES)
```

For this example, use a validation function to process a varargin input that handles the varying input arguments.

```
function state = sampleUniform(obj, varargin)
  narginchk(1,4);
  [numSamples, stateBounds] = obj.validateSampleUniformInput(varargin{:});
  obj.UniformDistribution.RandomVariableLimits = stateBounds;
  state = obj.UniformDistribution.sample(numSamples);
end
```

Sample from Gaussian Distribution

Specify the behavior for sampling across a Gaussian distribution. Support multiple syntaxes for sampling a single state or multiple states.

Interpolate Between States

Define how to interpolate between two states in your state space. Use an input, fraction, to determine how to sample along the path between two states. For this example, define a basic linear interpolation method using the difference between states.

```
function interpState = interpolate(obj, state1, state2, fraction)
    narginchk(4,4);
    [state1, state2, fraction] = obj.validateInterpolateInput(state1, state2, fraction);
    stateDiff = state2 - state1;
    interpState = state1 + fraction' * stateDiff;
end
```

Calculate Distance Between States

Specify how to calculate the distance between two states in your state space. Use the state1 and state2 inputs to define the start and end positions. Both inputs can be a single state (row vector) or multiple states (matrix of row vectors). For this example, calculate the distance based on the Euclidean distance between each pair of state positions.

Terminate the methods and class sections.

```
end
end
```

Save your state space class definition. You can now use the class constructor to create an object for your state space.

Create Custom State Space Validator for Path Planning

This example shows how to use the createPlanningTemplate function to generate a template for customizing your own state validation class. State validation is used with path planning algorithms to ensure valid paths. The template function provides a basic implementation for example purposes.

Call the create template function. This function generates a class definition file for you to modify for your own implementation. Save this file.

```
createPlanningTemplate("StateValidator")
```

Class and Property Definition

The first part of the template specifies the class definition and any properties for the class. Derive from the nav.StateValidator class. You can specify any additional user-defined properties here.

```
classdef MyCustomStateValidator < nav.StateValidator & ...
    matlabshared.planning.internal.EnforceScalarHandle
    properties
        % User-defined properties
    end</pre>
```

Save your custom state validator class and ensure your file name matches the class name.

Class Constructor

Use the constructor to set the name of the state space validator and specify the state space object. Set a default value for the state space if one is not provided. Call the constructor of the base class. Initialize any other user-defined properties.

```
methods
    function obj = MyCustomStateValidator(space)
        narginchk(0,1)

    if nargin == 0
        space = stateSpaceSE2;
    end

    obj@nav.StateValidator(space);

% Initialize user-defined properties
end
```

Copy Semantics

Specify the copy method definition. Copy all the values of your user-defined variables into a new object, so copyObj is a deep copy. The default behavior given in this example creates a new copy of the object with the same type.

```
function copyObj = copy(obj)
    copyObj = feval(class(obj), obj.StateSpace);
end
```

Check State Validity

Define how a given state is validated. The state input can either be a single row vector, or a matrix of row vectors for multiple states. Customize this function for any special validation behavior for your state space like collision checking against obstacles.

```
function isValid = isStateValid(obj, state)
    narginchk(2,2);
    nav.internal.validation.validateStateMatrix(state, nan, obj.StateSpace.NumStateVarial
        "isStateValid", "state");

bounds = obj.StateSpace.StateBounds';
    inBounds = state >= bounds(1,:) & state <= bounds(2,:);
    isValid = all(inBounds, 2);</pre>
```

Check Motion Validity

end

Define how to generate the motion between states and determine if it is valid. For this example, use linspace to evenly interpolate between states and check if these states are valid using isStateValid. Customize this function to sample between states or consider other analytical methods for determining if a vehicle can move between given states.

```
function [isValid, lastValid] = isMotionValid(obj, state1, state2)
    narginchk(3,3);
    state1 = nav.internal.validation.validateStateVector(state1, ...
        obj.StateSpace.NumStateVariables, "isMotionValid", "state1");
    state2 = nav.internal.validation.validateStateVector(state2, ...
        obj.StateSpace.NumStateVariables, "isMotionValid", "state2");

if (~obj.isStateValid(state1))
        error("statevalidator:StartStateInvalid", "The start state of the motion is invalend
```

```
% Interpolate at a fixed interval between states and check state validity
numInterpPoints = 100;
interpStates = obj.StateSpace.interpolate(state1, state2, linspace(0,1,numInterpPointinterpValid = obj.isStateValid(interpStates);

% Look for invalid states. Set lastValid state to index-1.
firstInvalidIdx = find(~interpValid, 1);
if isempty(firstInvalidIdx)
    isValid = true;
    lastValid = state2;
else
    isValid = false;
    lastValid = interpStates(firstInvalidIdx-1,:);
end
```

Terminate the methods and class sections.

```
end
end
```

Save your state space validator class definition. You can now use the class constructor to create an object for validation of states for a given state space.

See Also

nav.StateSpace|nav.StateValidator|stateSpaceSE2|validatorOccupancyMap

Introduced in R2019b

ecompass

Orientation from magnetometer and accelerometer readings

Syntax

```
orientation = ecompass(accelerometerReading, magnetometerReading)
orientation = ecompass(accelerometerReading, magnetometerReading,
orientationFormat)
orientation = ecompass(accelerometerReading, magnetometerReading,
orientationFormat, 'ReferenceFrame', RF)
```

Description

orientation = ecompass(accelerometerReading, magnetometerReading) returns a quaternion that can rotate quantities from a parent (NED) frame to a child (sensor) frame.

orientation = ecompass(accelerometerReading, magnetometerReading,
orientationFormat) specifies the orientation format as quaternion or rotation matrix.

orientation = ecompass(accelerometerReading, magnetometerReading, orientationFormat, 'ReferenceFrame', RF) also allows you to specify the reference frame RF of the orientation output. Specify RF as 'NED' (North-East-Down) or 'ENU' (East-North-Up). The default value is 'NED'.

Examples

Determine Declination of Boston

Use the known magnetic field strength and proper acceleration of a device pointed true north in Boston to determine the magnetic declination of Boston.

Define the known acceleration and magnetic field strength in Boston.

```
magneticFieldStrength = [19.535 -5.109 47.930];
properAcceleration = [0 0 9.8];
```

Pass the magnetic field strength and acceleration to the ecompass function. The ecompass function returns a quaternion rotation operator. Convert the quaternion to Euler angles in degrees.

```
q = ecompass(properAcceleration,magneticFieldStrength);
e = eulerd(q,'ZYX','frame');
```

The angle, e, represents the angle between true north and magnetic north in Boston. By convention, magnetic declination is negative when magnetic north is west of true north. Negate the angle to determine the magnetic declination.

```
magneticDeclinationOfBoston = -e(1)
magneticDeclinationOfBoston = -14.6563
```

Return Rotation Matrix

The ecompass function fuses magnetometer and accelerometer data to return a quaternion that, when used within a quaternion rotation operator, can rotate quantities from a parent (NED) frame to a child frame. The ecompass function can also return rotation matrices that perform equivalent rotations as the quaternion operator.

Define a rotation that can take a parent frame pointing to magnetic north to a child frame pointing to geographic north. Define the rotation as both a quaternion and a rotation matrix. Then, convert the quaternion and rotation matrix to Euler angles in degrees for comparison.

Define the magnetic field strength in microteslas in Boston, MA, when pointed true north.

```
m = [19.535 -5.109 47.930];

a = [0 0 9.8];
```

Determine the quaternion and rotation matrix that is capable of rotating a frame from magnetic north to true north. Display the results for comparison.

Determine Gravity Vector

Use ecompass to determine the gravity vector based on data from a rotating IMU.

Load the inertial measurement unit (IMU) data.

```
load 'rpy_9axis.mat' sensorData Fs
```

Determine the orientation of the sensor body relative to the local NED frame over time.

```
orientation = ecompass(sensorData.Acceleration,sensorData.MagneticField);
```

To estimate the gravity vector, first rotate the accelerometer readings from the sensor body frame to the NED frame using the orientation quaternion vector.

```
gravityVectors = rotatepoint(orientation,sensorData.Acceleration);
```

Determine the gravity vector as an average of the recovered gravity vectors over time.

```
gravityVectorEstimate = mean(gravityVectors,1)
gravityVectorEstimate = 1 \times 3
0.0000 -0.0000 10.2102
```

Track Spinning Platform

Fuse modeled accelerometer and gyroscope data to track a spinning platform using both idealized and realistic data.

Generate Ground-Truth Trajectory

Describe the ground-truth orientation of the platform over time. Use the kinematicTrajectory on page 2-423 System object^m to create a trajectory for a platform that has no translation and spins about its z-axis.

```
duration = 12;
fs = 100;
numSamples = fs*duration;
accelerationBody = zeros(numSamples,3);
angularVelocityBody = zeros(numSamples,3);
zAxisAngularVelocity = [linspace(0,4*pi,4*fs),4*pi*ones(1,4*fs),linspace(4*pi,0,4*fs)]';
angularVelocityBody(:,3) = zAxisAngularVelocity;
trajectory = kinematicTrajectory('SampleRate',fs);
[~,orientationNED,~,accelerationNED,angularVelocityNED] = trajectory(accelerationBody,angularVelocityNED)
```

Model Receiving IMU Data

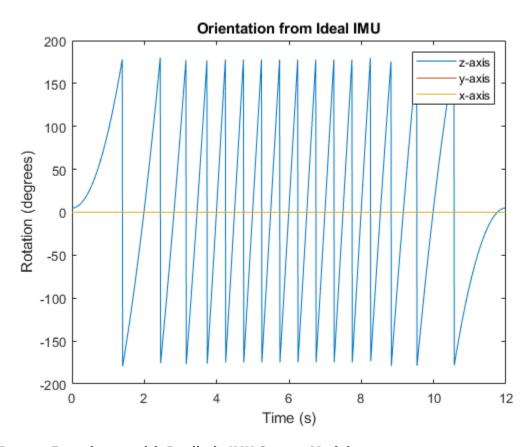
Use an imuSensor on page 2-381 System object to mimic data received from an IMU that contains an ideal magnetometer and an ideal accelerometer.

Fuse IMU Data to Estimate Orientation

Pass the accelerometer data and magnetometer data to the ecompass function to estimate orientation over time. Convert the orientation to Euler angles in degrees and plot the result.

```
orientation = ecompass(accelerometerData, magnetometerData);
orientationEuler = eulerd(orientation, 'ZYX', 'frame');
timeVector = (0:numSamples-1).'/fs;
```

```
figure(1)
plot(timeVector,orientationEuler)
legend('z-axis','y-axis','x-axis')
xlabel('Time (s)')
ylabel('Rotation (degrees)')
title('Orientation from Ideal IMU')
```



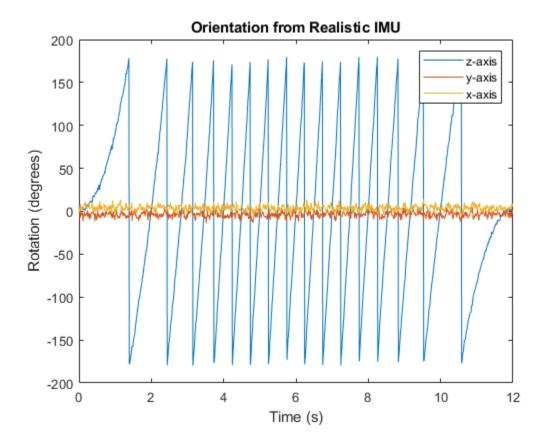
Repeat Experiment with Realistic IMU Sensor Model

Modify parameters of the IMU System object to approximate realistic IMU sensor data. Reset the IMU and then call it with the same ground-truth acceleration, angular velocity, and orientation. Use ecompass to fuse the IMU data and plot the results.

```
IMU.Accelerometer = accelparams( ...
    'MeasurementRange',20, ...
    'Resolution',0.0006, ...
    'ConstantBias',0.5, ...
    'AxesMisalignment',2, ...
    'NoiseDensity',0.004, ...
    'BiasInstability',0.5);
IMU.Magnetometer = magparams( ...
    'MeasurementRange',200, ...
    'Resolution',0.01);
reset(IMU)
```

[accelerometerData,magnetometerData] = IMU(accelerationNED,angularVelocityNED,orientationNED);

```
orientation = ecompass(accelerometerData, magnetometerData);
orientationEuler = eulerd(orientation, 'ZYX', 'frame');
figure(2)
plot(timeVector, orientationEuler)
legend('z-axis', 'y-axis', 'x-axis')
xlabel('Time (s)')
ylabel('Rotation (degrees)')
title('Orientation from Realistic IMU')
```



Input Arguments

accelerometerReading — Accelerometer readings in sensor body coordinate system (m/s²) N-by-3 matrix

Accelerometer readings in sensor body coordinate system in m/s^2 , specified as an N-by-3 matrix. The columns of the matrix correspond to the x-, y-, and z-axes of the sensor body. The rows in the matrix, N, correspond to individual samples. The accelerometer readings are normalized before use in the function.

Data Types: single | double

magnetometerReading — Magnetometer readings in sensor body coordinate system (μT) N-by-3 matrix

Magnetometer readings in sensor body coordinate system in μ T, specified as an *N*-by-3 matrix. The columns of the matrix correspond to the *x*-, *y*-, and *z*-axes of the sensor body. The rows in the matrix,

N, correspond to individual samples. The magnetometer readings are normalized before use in the function.

Data Types: single | double

orientationFormat — Format used to describe orientation

'quaternion' (default) | 'rotmat'

Format used to describe orientation, specified as 'quaternion' or 'rotmat'.

Data Types: char | string

Output Arguments

orientation — Orientation that rotates quantities from global coordinate system to sensor body coordinate system

N-by-1 vector of quaternions (default) | 3-by-3-by-N array

Orientation that can rotate quantities from a global coordinate system to a body coordinate system, returned as a vector of quaternions or an array. The size and type of the orientation depends on the format used to describe orientation:

- 'quaternion' -- N-by-1 vector of quaternions with the same underlying data type as the input
- 'rotmat' -- 3-by-3-by-N array the same data type as the input

Data Types: quaternion | single | double

Algorithms

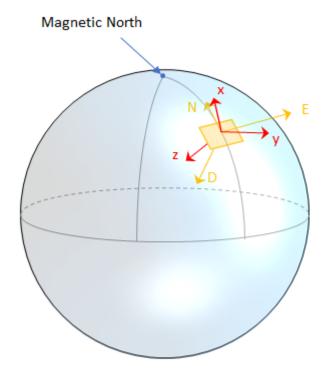
The ecompass function returns a quaternion or rotation matrix that can rotate quantities from a parent (NED for example) frame to a child (sensor) frame. For both output orientation formats, the rotation operator is determined by computing the rotation matrix.

The rotation matrix is first calculated with an intermediary:

$$R = \left[(a \times m) \times a \ a \times m \ a \right]$$

and then normalized column-wise. a and m are the accelerometerReading input and the magnetometerReading input, respectively.

To understand the rotation matrix calculation, consider an arbitrary point on the Earth and its corresponding local NED frame. Assume a sensor body frame, [x,y,z], with the same origin.



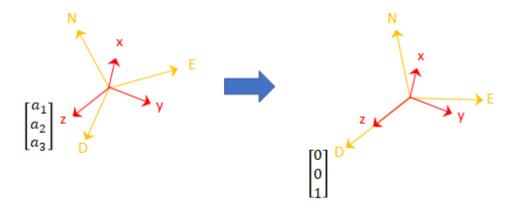
Recall that orientation of a sensor body is defined as the rotation operator (rotation matrix or quaternion) required to rotate a quantity from a parent (NED) frame to a child (sensor body) frame:

$$\begin{bmatrix} R \end{bmatrix} \begin{bmatrix} p_{\text{parent}} \end{bmatrix} = \begin{bmatrix} p_{\text{child}} \end{bmatrix}$$

where

- *R* is a 3-by-3 rotation matrix, which can be interpreted as the orientation of the child frame.
- p_{parent} is a 3-by-1 vector in the parent frame.
- p_{child} is a 3-by-1 vector in the child frame.

For a stable sensor body, an accelerometer returns the acceleration due to gravity. If the sensor body is perfectly aligned with the NED coordinate system, all acceleration due to gravity is along the z-axis, and the accelerometer reads [0 0 1]. Consider the rotation matrix required to rotate a quantity from the NED coordinate system to a quantity indicated by the accelerometer.

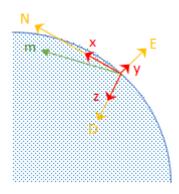


$$\begin{bmatrix} r_{11} & r_{21} & r_{31} \\ r_{12} & r_{22} & r_{32} \\ r_{13} & r_{23} & r_{33} \end{bmatrix} \begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix} = \begin{bmatrix} a_1 \\ a_2 \\ a_3 \end{bmatrix}$$

The third column of the rotation matrix corresponds to the accelerometer reading:

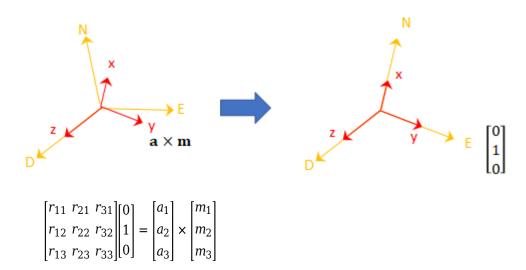
$$\begin{bmatrix} r_{31} \\ r_{32} \\ r_{33} \end{bmatrix} = \begin{bmatrix} a_1 \\ a_2 \\ a_3 \end{bmatrix}$$

A magnetometer reading points toward magnetic north and is in the N-D plane. Again, consider a sensor body frame aligned with the NED coordinate system.



By definition, the E-axis is perpendicular to the N-D plane, therefore $N \times D = E$, within some amplitude scaling. If the sensor body frame is aligned with NED, both the acceleration vector from the accelerometer and the magnetic field vector from the magnetometer lie in the N-D plane. Therefore $m \times a = y$, again with some amplitude scaling.

Consider the rotation matrix required to rotate NED to the child frame, $[x \ y \ z]$.



The second column of the rotation matrix corresponds to the cross product of the accelerometer reading and the magnetometer reading:

$$\begin{vmatrix} r_{21} \\ r_{22} \\ r_{23} \end{vmatrix} = \begin{vmatrix} a_1 \\ a_2 \\ a_3 \end{vmatrix} \times \begin{vmatrix} m_1 \\ m_2 \\ m_3 \end{vmatrix}$$

By definition of a rotation matrix, column 1 is the cross product of columns 2 and 3:

$$\begin{bmatrix} r_{11} \\ r_{12} \\ r_{13} \end{bmatrix} = \begin{bmatrix} r_{21} \\ r_{22} \\ r_{23} \end{bmatrix} \times \begin{bmatrix} r_{31} \\ r_{32} \\ r_{33} \end{bmatrix}$$
$$= (a \times m) \times a$$

Finally, the rotation matrix is normalized column-wise:

$$R_{ij} = \frac{R_{ij}}{\sqrt{\sum_{i=1}^{3} R_{ij}^2}} \quad , \ \forall j$$

Note The ecompass algorithm uses magnetic north, not true north, for the NED coordinate system.

References

[1] Open Source Sensor Fusion. https://github.com/memsindustrygroup/Open-Source-Sensor-Fusion/tree/master/docs

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder $^{\scriptscriptstyle\mathsf{TM}}$.

See Also

ahrsfilter|imufilter

Introduced in R2018b

enu2lla

Transform local east-north-up coordinates to geodetic coordinates

Syntax

```
lla = enu2lla(xyzENU,lla0,method)
```

Description

lla = enu2lla(xyzENU,lla0,method) transforms the local east-north-up (ENU) Cartesian
coordinates xyzENU to geodetic coordinates lla. Specify the origin of the local ENU system as the
geodetic coordinates lla0.

Note

- The latitude and longitude values in the geodetic coordinate system use the World Geodetic System of 1984 (WGS84) standard.
- Specify altitude as height in meters above the WGS84 reference ellipsoid.

Examples

Transform ENU Coordinates to Geodetic Coordinates

Specify the geodetic coordinates of the local origin in Zermatt, Switzerland.

```
lla0 = [46.017 7.750 1673]; % [lat0 lon0 alt0]
```

Specify the ENU coordinates of a point of interest, in meters. In this case, the point of interest is the Matterhorn.

```
xyzENU = [-7134.8 - 4556.3 2852.4]; % [xEast yNorth zUp]
```

Transform the local ENU coordinates to geodetic coordinates using flat earth approximation.

Input Arguments

xyzENU — Local ENU Cartesian coordinates

three-element row vector | *n*-by-3 matrix

Local ENU Cartesian coordinates, specified as a three-element row vector or an n-by-3 matrix. n is the number of points to transform. Specify each point in the form [$xEast\ yNorth\ zUp$]. $xEast\ yNorth$, and zUp are the respective x-, y-, and z-coordinates, in meters, of the point in the local ENU system.

Data Types: double

11a0 — Origin of local ENU system in geodetic coordinates

three-element row vector | *n*-by-3 matrix

Origin of the local ENU system in the geodetic coordinates, specified as a three-element row vector or an n-by-3 matrix. n is the number of origin points. Specify each point in the form [lat0 lon0 alt0]. lat0 and lon0 specify the latitude and longitude of the origin, respectively, in degrees. alt0 specifies the altitude of the origin in meters.

Data Types: double

method — Transformation method

'flat'|'ellipsoid'

Transformation method, specified as 'flat' or 'ellipsoid'. This argument specifies whether the function assumes the planet is flat or ellipsoidal.

The flat Earth transformation method has these limitations:

- · Assumes that the flight path and bank angle are zero.
- Assumes that the flat Earth *z*-axis is normal to the Earth at only the initial geodetic latitude and longitude. This method has higher accuracy over small distances from the initial geodetic latitude and longitude, and closer to the equator. The method calculates a longitude with higher accuracy when the variation in latitude is smaller.
- Latitude values of +90 and -90 may return unexpected values because of singularity at the poles.

Data Types: char | string

Output Arguments

lla — Geodetic coordinates

three-element row vector | *n*-by-3 matrix

Geodetic coordinates, returned as a three-element row vector or an *n*-by-3 matrix. *n* is the number of transformed points. Each point is in the form [lat lon alt]. lat and lon specify the latitude and longitude, respectively, in degrees. alt specifies the altitude in meters.

Data Types: double

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

Functions

lla2enu | lla2ned | ned2lla

Introduced in R2021a

eul2quat

Convert Euler angles to quaternion

Syntax

```
quat = eul2quat(eul)
quat = eul2quat(eul,sequence)
```

Description

quat = eul2quat(eul) converts a given set of Euler angles, eul, to the corresponding quaternion,
quat. The default order for Euler angle rotations is "ZYX".

quat = eul2quat(eul, sequence) converts a set of Euler angles into a quaternion. The Euler angles are specified in the axis rotation sequence, sequence. The default order for Euler angle rotations is "ZYX".

Examples

Convert Euler Angles to Quaternion

Convert Euler Angles to Quaternion Using Default ZYZ Axis Order

Input Arguments

eul — Euler rotation angles

```
n-by-3 matrix
```

Euler rotation angles in radians, specified as an n-by-3 array of Euler rotation angles. Each row represents one Euler angle set.

Example: [0 0 1.5708]

sequence — Axis rotation sequence

"ZYX" (default) | "ZYZ" | "XYZ"

Axis rotation sequence for the Euler angles, specified as one of these string scalars:

- "ZYX" (default) The order of rotation angles is *z*-axis, *y*-axis, *x*-axis.
- "ZYZ" The order of rotation angles is *z*-axis, *y*-axis, *z*-axis.
- "XYZ" The order of rotation angles is *x*-axis, *y*-axis, *z*-axis.

Data Types: string | char

Output Arguments

quat — Unit quaternion

n-by-4 matrix

Unit quaternion, returned as an *n*-by-4 matrix containing *n* quaternions. Each quaternion, one per row, is of the form $q = [w \times y \ z]$, with *w* as the scalar number.

Example: [0.7071 0.7071 0 0]

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

quat2eul | quaternion

Introduced in R2015a

eul2rotm

Convert Euler angles to rotation matrix

Syntax

```
rotm = eul2rotm(eul)
rotm = eul2rotm(eul,sequence)
```

Description

rotm = eul2rotm(eul) converts a set of Euler angles, eul, to the corresponding rotation matrix,
rotm. When using the rotation matrix, premultiply it with the coordinates to be rotated (as opposed
to postmultiplying). The default order for Euler angle rotations is "ZYX".

rotm = eul2rotm(eul, sequence) converts Euler angles to a rotation matrix, rotm. The Euler
angles are specified in the axis rotation sequence, sequence. The default order for Euler angle
rotations is "ZYX".

Examples

Convert Euler Angles to Rotation Matrix

Convert Euler Angles to Rotation Matrix Using ZYZ Axis Order

Input Arguments

eul — Euler rotation angles

n-by-3 matrix

Euler rotation angles in radians, specified as an *n*-by-3 array of Euler rotation angles. Each row represents one Euler angle set.

Example: [0 0 1.5708]

sequence — Axis rotation sequence

"ZYX" (default) | "ZYZ" | "XYZ"

Axis rotation sequence for the Euler angles, specified as one of these string scalars:

- "ZYX" (default) The order of rotation angles is z-axis, y-axis, x-axis.
- "ZYZ" The order of rotation angles is *z*-axis, *y*-axis, *z*-axis.
- "XYZ" The order of rotation angles is *x*-axis, *y*-axis, *z*-axis.

Data Types: string | char

Output Arguments

rotm — Rotation matrix

3-by-3-by-*n* matrix

Rotation matrix, returned as a 3-by-3-by-n matrix containing n rotation matrices. Each rotation matrix has a size of 3-by-3 and is orthonormal. When using the rotation matrix, premultiply it with the coordinates to be rotated (as opposed to postmultiplying).

Example: [0 0 1; 0 1 0; -1 0 0]

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

rotm2eul

Introduced in R2015a

eul2tform

Convert Euler angles to homogeneous transformation

Syntax

```
eul = eul2tform(eul)
tform = eul2tform(eul,sequence)
```

Description

eul = eul2tform(eul) converts a set of Euler angles, eul, into a homogeneous transformation
matrix, tform. When using the transformation matrix, premultiply it with the coordinates to be
transformed (as opposed to postmultiplying). The default order for Euler angle rotations is "ZYX".

tform = eul2tform(eul, sequence) converts Euler angles to a homogeneous transformation. The Euler angles are specified in the axis rotation sequence, sequence. The default order for Euler angle rotations is "ZYX".

Examples

Convert Euler Angles to Homogeneous Transformation Matrix

Convert Euler Angles to Homogeneous Transformation Matrix Using ZYZ Axis Order

```
eul = [0 pi/2 pi/2];
tformZYZ = eul2tform(eul, 'ZYZ')
tformZYZ = 4 \times 4
   0.0000 -0.0000
                    1.0000
                                  0
   1.0000
          0.0000
                    0
                                  0
         1.0000 0.0000
  -0.0000
                                  (-)
       0
            (-)
                    0 1.0000
```

Input Arguments

eul — Euler rotation angles

n-by-3 matrix

Euler rotation angles in radians, specified as an *n*-by-3 array of Euler rotation angles. Each row represents one Euler angle set.

Example: [0 0 1.5708]

sequence — Axis rotation sequence

"ZYX" (default) | "ZYZ" | "XYZ"

Axis rotation sequence for the Euler angles, specified as one of these string scalars:

- "ZYX" (default) The order of rotation angles is z-axis, y-axis, x-axis.
- "ZYZ" The order of rotation angles is *z*-axis, *y*-axis, *z*-axis.
- "XYZ" The order of rotation angles is *x*-axis, *y*-axis, *z*-axis.

Data Types: string | char

Output Arguments

tform — Homogeneous transformation

4-by-4-by-*n* matrix

Homogeneous transformation matrix, specified by a 4-by-4-by-n matrix of n homogeneous transformations. When using the rotation matrix, premultiply it with the coordinates to be rotated (as opposed to postmultiplying).

Example: [0 0 1 0; 0 1 0 0; -1 0 0 0; 0 0 0 1]

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

tform2eul

Introduced in R2015a

exportOccupancyMap3D

Import an octree file as 3D occupancy map

Syntax

exportOccupancyMap3D(map3D,filename)

Description

exportOccupancyMap3D(map3D,filename) serializes the 3D occupancy map, map3D, into either
an octree or binary tree file (.ot/bt) specified at the file location and name, filename

Input Arguments

map3D — 3-D occupancy map

occupancyMap3D object

3-D occupancy map, specified as a occupancyMap3D object.

filename — Absolute or relative path to octree file

string scalar | character vector

Absolute or relative path to octree file (.ot/bt), specified as a string scalar or character vector.

Example: "path/to/file/map.ot"

Data Types: char | string

See Also

Classes

lidarSLAM | occupancyMap | occupancyMap3D

Functions

inflate | insertPointCloud | setOccupancy | show

Introduced in R2020a

flush

Flush all GPS data accumulated in the buffers and reset properties

Syntax

flush(gpsdev0bj)

Description

flush(gpsdev0bj) clears the buffers and resets SamplesRead and SamplesAvailable.

Input Arguments

gpsdev0bj — GPS sensor object

The GPS sensor object with the default or specified properties.

See Also

Objects

Introduced in R2020b

gnssconstellation

Satellite locations at specified time

Syntax

```
[satPos,satVel] = gnssconstellation(t)
```

Description

[satPos,satVel] = gnssconstellation(t) returns the satellite positions and velocities at the datetime t. The function returns positions and velocities in the Earth-centered Earth-fixed (ECEF) coordinate system in meters and meters per second, respectively.

Examples

Get Current Satellite Positions and Velocities

Get the current satellite positions and velocities from the GNSS constellations. Access the orbital parameters from IS-GPS-200K Interface Specification and calculate the position and velocities in ECEF coordinates for the given time. Display the satellite positions.

```
t = datetime('now', 'TimeZone', 'Local');
[satPos,satVel] = gnssconstellation(t);
disp(satPos)
   1.0e+07 *
   -1.5334
              0.7843
                        2.0219
    0.6522
              2.1986
                       -1.3398
    0.1356
             -2.6346
                        0.3074
    0.8926
             -2.3649
                       -0.8153
    1.1912
             1.1018
                       -2.1027
    2.1098
              0.3277
                       -1.5797
   -1.9403
              1.5328
                       -0.9695
   0.3029
             -1.6710
                        2.0421
   -2.4945
              0.8953
                        0.1737
                       -2.1742
   -1.0057
              1.1470
   2.2126
              1.4377
                        0.3028
   2.2078
              0.4620
                        1.4023
   -0.9498
             -2.0131
                        1.4490
             -1.3129
                       -1.9649
   -1.2123
             -0.1258
                        2.1589
    1.5420
             -1.2163
                        1.8486
    1.4688
   -0.7398
              2.4849
                       -0.5762
   -0.5125
             -2.3301
                       -1.1671
    2.4254
             -1.0775
                       -0.1044
    0.0214
              1.5977
                        2.1216
   -2.1168
                       -1.5721
             -0.3190
   -1.2847
              1.7161
                        1.5680
                        1.3718
    1.0463
              2.0193
   -2.2929
             -1.1303
                         0.7206
```

```
-2.1336 -0.2661 1.5592
0.7587 -1.3325 -2.1687
1.7463 -0.3893 -1.9629
```

Get Satellite Look Angles for Receiver Position

Use the lookangles function to get the azimuth and elevation angles of satellites for given satellite and receiver positions. Specify a mask angle of 5 degrees. Get the satellite positions using the gnssconstellation function.

Specify a receiver position in geodetic coordinates (latitude, longitude, altitude).

```
recPos = [42 -71 50];
```

Get the satellite positions for the current time.

```
t = datetime('now');
gpsSatPos = gnssconstellation(t);
```

Specify a mask angle of 5 degrees.

```
maskAngle = 5;
```

Get the azimuth and elevation look angles for the satellite positions. The vis output indicates which satellites are visible. Get the total using nnz.

```
[az,el,vis] = lookangles(recPos,gpsSatPos,maskAngle);
fprintf('%d satellites visible at %s.\n',nnz(vis),t);
9 satellites visible at 25-Feb-2021 12:29:41.
```

Input Arguments

t — Current time for satellite simulation

scalar datetime array

Current time for the satellite simulation, specified as a scalar datetime array.

The default time zone for a dateTtime array is UTC. For information on specifying a different time zone, see datetime.

GPS start time is Jan 6, 1980 midnight, UTC. Specifying any datetime prior to this time will use the GPS start time.

```
Example: datetime('now', 'TimeZone', 'Local');
Data Types: datetime
```

Output Arguments

```
satPos — Satellite positions
```

N-by-3 matrix of scalars

Satellite positions in the Earth-centered Earth-fixed (ECEF) coordinate system in meters, returned as an *N*-by-3 matrix of scalars. *N* is the number of satellites in the constellation.

Data Types: single | double

satVel — Velocity readings in local navigation coordinate system (m/s)

N-by-3 matrix of scalar

Velocity readings of the GNSS receiver in the local navigation coordinate system in meters per second, returned as an *N*-by-3 matrix of scalars. *N* is the number of satellites in the constellation.

Data Types: single | double

More About

Orbital Parameters

The satellite positions and velocities are defined by orbital parameters from IS-GPS-200K Interface Specification, and are given in Earth-centered Earth-fixed (ECEF) coordinates.

Position calculations use equations from Table 30-II in the same IS-GPS-200K Interface Specification.

Velocity calculations use equations 8.21-8.27 in [1].

References

[1] Groves, Paul D. *Principles of GNSS, Inertial, and Multisensor Integrated Navigation Systems*. Boston: Artech House, 2013.

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

Only MEX functions are supported for code generation.

See Also

Objects

gnssSensor|gpsSensor|imuSensor

Functions

lookangles | pseudoranges | receiverposition | skyplot

Topics

"Estimate GNSS Receiver Position with Simulated Satellite Constellations"

Introduced in R2021a

hom2cart

Convert homogeneous coordinates to Cartesian coordinates

Syntax

```
cart = hom2cart(hom)
```

Description

cart = hom2cart(hom) converts a set of homogeneous points to Cartesian coordinates.

Examples

Convert Homogeneous Points to 3-D Cartesian Points

```
h = [0.2785 0.9575 0.1576 0.5; 0.5469 0.9649 0.9706 0.5];
c = hom2cart(h)
c = 2×3
0.5570 1.9150 0.3152
1.0938 1.9298 1.9412
```

Input Arguments

hom — Homogeneous points

n-by-*k* matrix

Homogeneous points, specified as an n-by-k matrix, containing n points. k must be greater than or equal to 2.

```
Example: [0.2785 0.9575 0.1576 0.5; 0.5469 0.9649 0.9706 0.5]
```

Output Arguments

cart — Cartesian coordinates

```
n-by-(k-1) matrix
```

Cartesian coordinates, returned as an n-by-(k-1) matrix, containing n points. Each row of cart represents a point in (k-1)-dimensional space. k must be greater than or equal to 2.

```
Example: [0.8147 0.1270 0.6324; 0.9058 0.9134 0.0975]
```

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

cart2hom

Introduced in R2015a

importOccupancyMap3D

Import an octree file as 3D occupancy map

Syntax

map3D = importOccupancyMap3D(mapPath)

Description

map3D = importOccupancyMap3D(mapPath) imports the octree file (.ot/bt) specified at the
relative or absolute file path, mapPath

Input Arguments

mapPath — Absolute or relative path to octree file

string scalar | character vector

Absolute or relative path to octree file (.ot/bt), specified as a string scalar or character vector.

Example: "path/to/file/map.ot"

Data Types: char | string

Output Arguments

map3D — 3-D occupancy map

occupancyMap3D object

3-D occupancy map, specified as a occupancyMap3D object.

See Also

Classes

lidarSLAM | occupancyMap | occupancyMap3D

Functions

inflate|insertPointCloud|setOccupancy|show

Introduced in R2020a

info

Read Update Rate, GPS Lock information and number of satellites in View for the GPS receiver

Syntax

gpsInfo = info(gps0bj)

Description

gpsInfo = info(gps0bj) returns the update rate of the GPS receiver, GPS lock information and number of satellites from which the GPS can read signals. info gets updated after every execution of read command.

Input Arguments

gps0bj — GPS object

gpsdev object

The GPS object with the default or specified properties.

Output Arguments

gpsInfo — GPS module information

GPS module information such as update rate, and number of satellites. The output has three fields:

- UpdateRate Update Rate of the GPS Module in Hz. Update Rate of GPS receiver is estimated from the difference in time at which two RMC sentences are obtained. This value might be slightly varying from actual Update Rate of the module.
- GPSLocked This property specifies if GPS has enough information to get valid data. GPS signals are acquired easily in locations that have a clear view of the sky. It can be either a 0 or 1 (logical). If GPSLocked is 0, the GPS does not have the lock to compute location or time information. If GPSLocked is 1, GPS module has enough data to compute location or time information.
- NumberOfSatellitesInView Number of satellites from which the GPS module can read the signals.

Data Types: struct

See Also

Introduced in R2020b

insfilter

Create inertial navigation filter

Syntax

```
filter = insfilter
filter = insfilter('ReferenceFrame',RF)
```

Description

filter = insfilter returns an insfilterMARG inertial navigation filter object that estimates pose based on accelerometer, gyroscope, GPS, and magnetometer measurements. See insfilterMARG for more details.

filter = insfilter('ReferenceFrame',RF) returns an insfilterMARG inertial navigation filter object that estimates pose relative to a reference frame specified by RF. Specify RF as 'NED' (North-East-Down) or 'ENU' (East-North-Up). The default value is 'NED'. See insfilterMARG for more details.

Examples

Create Default INS Filter

The default INS filter is the insfilterMARG object. Call insfilter with no input arguments to create the default INS filter.

```
filter = insfilter
filter =
 insfilterMARG with properties:
        IMUSampleRate: 100
                                         Hz
   ReferenceLocation: [0 0 0]
                                         [deg deg m]
                State: [22x1 double]
      StateCovariance: [22x22 double]
  Multiplicative Process Noise Variances
            GyroscopeNoise: [1e-09 1e-09 1e-09]
                                                      (rad/s)^2
        AccelerometerNoise: [0.0001 0.0001 0.0001]
                                                      (m/s^2)^2
        GyroscopeBiasNoise: [1e-10 1e-10]
                                                      (rad/s)^2
   AccelerometerBiasNoise: [0.0001 0.0001 0.0001]
                                                      (m/s^2)^2
  Additive Process Noise Variances
   GeomagneticVectorNoise: [1e-06 1e-06]
                                                   uT^2
    MagnetometerBiasNoise: [0.1 0.1 0.1]
                                                   uT^2
```

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder $^{\scriptscriptstyle\mathsf{TM}}.$

See Also

ahrsfilter|imufilter|insfilterAsync|insfilterErrorState|insfilterMARG| insfilterNonholonomic

Introduced in R2018b

interpolate

Interpolate poses along path segment

Syntax

```
poses = interpolate(pathSeg)
poses = interpolate(pathSeg,lengths)
[poses,directions] = interpolate(____)
```

Description

poses = interpolate(pathSeg) interpolates along the path segment at the transitions between
motion types.

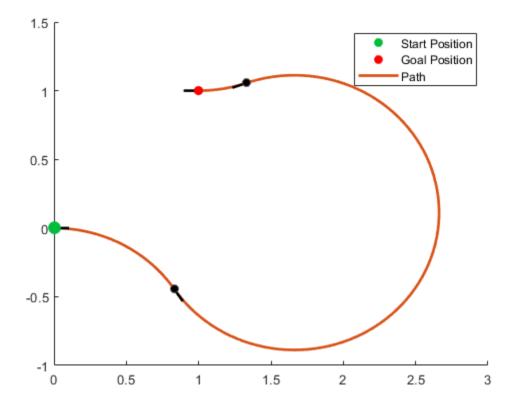
poses = interpolate(pathSeg,lengths) interpolates along the path segment at the specified
lengths along the path. Transitions between motion types are always included.

[poses, directions] = interpolate(____) also returns the direction of motion along the path for each section as a vector of 1s (forward) and -1s (reverse) using the previous inputs.

Examples

Interpolate Poses For Dubins Path

```
Create a dubinsConnection object.
dubConnObj = dubinsConnection;
Define start and goal poses as [x y theta] vectors.
startPose = [0 0 0];
goalPose = [1 1 pi];
Calculate a valid path segment to connect the poses.
[pathSegObj,pathCosts] = connect(dubConnObj,startPose,goalPose);
Show the generated path.
show(pathSegObj{1})
```

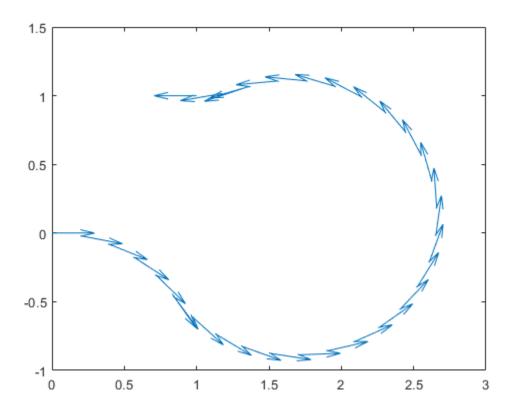


Interpolate poses along the path. Get a pose every 0.2 meters, including the transitions between turns.

```
length = pathSegObj{1}.Length;
poses = interpolate(pathSegObj{1},0:0.2:length)
poses = 32 \times 3
         0
                    0
                               0
    0.1987
              -0.0199
                         6.0832
    0.3894
              -0.0789
                         5.8832
    0.5646
              -0.1747
                         5.6832
    0.7174
              -0.3033
                         5.4832
    0.8309
             -0.4436
                         5.3024
    0.8418
              -0.4595
                         5.3216
    0.9718
              -0.6110
                         5.5216
    1.1293
             -0.7337
                         5.7216
    1.3081
             -0.8226
                         5.9216
```

Use the quiver function to plot these poses.

```
quiver(poses(:,1),poses(:,2),cos(poses(:,3)),sin(poses(:,3)),0.5)
```



Input Arguments

pathSeg — Path segment

dubinsPathSegment object | reedsSheppPathSegment object

Path segment, specified as a dubinsPathSegment or reedsSheppPathSegment object.

lengths — Lengths along path to interpolate at

positive numeric vector

Lengths along path to interpolate at, specified as a positive numeric vector. For example, specify [0:0.1:pathSeg0bj{1}.Length] to interpolate at every 0.1 meters along the path. Transitions between motion types are always included.

Output Arguments

poses — Interpolated poses

 $[x, y, \Theta]$ matrix

This property is read-only.

Interpolated poses along the path segment, specified as an $[x, y, \Theta]$ matrix. Each row of the matrix corresponds to a different interpolated pose along the path.

x and y are in meters. Θ is in radians.

directions — Directions of motion

vector of 1s (forward) and -1s (reverse)

Directions of motion for each segment of the interpolated path, specified as a vector of 1s (forward) and -1s (reverse).

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

Functions

connect | show

Objects

dubinsConnection | dubinsPathSegment | reedsSheppConnection | reedsSheppPathSegment

Introduced in R2019b

lla2enu

Transform geodetic coordinates to local east-north-up coordinates

Syntax

```
xyzENU = lla2enu(lla,lla0,method)
```

Description

xyzENU = lla2enu(lla,lla0,method) transforms the geodetic coordinates lla to local east-north-up (ENU) Cartesian coordinates xyzENU. Specify the origin of the local ENU system as the geodetic coordinates lla0.

Note

- The latitude and longitude values in the geodetic coordinate system use the World Geodetic System of 1984 (WGS84) standard.
- Specify altitude as height in meters above the WGS84 reference ellipsoid.

Examples

Transform Geodetic Coordinates to ENU Coordinates

Specify the geodetic coordinates of the local origin in Zermatt, Switzerland.

```
lla0 = [46.017 7.750 1673]; % [lat0 lon0 alt0]
```

Specify the geodetic coordinates of a point of interest. In this case, the point of interest is the Matterhorn.

```
lla = [45.976 \ 7.658 \ 4531]; % [lat lon alt]
```

Transform the geodetic coordinates to local ENU coordinates using flat earth approximation.

```
xyzENU = lla2enu(lla,lla0,'flat')

xyzENU = 1 \times 3

10^3 \times -7.1244 -4.5572 2.8580
```

Input Arguments

lla — Geodetic coordinates

three-element row vector | *n*-by-3 matrix

Geodetic coordinates, specified as a three-element row vector or an *n*-by-3 matrix. *n* is the number of points to transform. Specify each point in the form [lat lon alt]. lat and lon specify the latitude and longitude respectively in degrees. alt specifies the altitude in meters.

Data Types: double

11a0 — Origin of local ENU system in geodetic coordinates

three-element row vector | *n*-by-3 matrix

Origin of the local ENU system in the geodetic coordinates, specified as a three-element row vector or an n-by-3 matrix. n is the number of origin points. Specify each point in the form [lat0 lon0 alt0]. lat0 and lon0 specify the latitude and longitude of the origin, respectively, in degrees. alt0 specifies the altitude of the origin in meters.

Data Types: double

method — Transformation method

'flat'|'ellipsoid'

Transformation method, specified as 'flat' or 'ellipsoid'. This argument specifies whether the function assumes the planet is flat or ellipsoidal.

The flat Earth transformation method has these limitations:

- · Assumes that the flight path and bank angle are zero.
- Assumes that the flat Earth *z*-axis is normal to the Earth at only the initial geodetic latitude and longitude. This method has higher accuracy over small distances from the initial geodetic latitude and longitude, and closer to the equator. The method calculates a longitude with higher accuracy when the variation in latitude is smaller.
- Latitude values of +90 and -90 may return unexpected values because of singularity at the poles.

Data Types: char | string

Output Arguments

xyzENU — Local ENU Cartesian coordinates

three-element row vector | *n*-by-3 matrix

Local ENU Cartesian coordinates, returned as a three-element row vector or an n-by-3 matrix. n is the number of transformed points. Each point is in the form [$xEast\ yNorth\ zUp$]. $xEast\ yNorth$, and zUp are the respective x-, y-, and z-coordinates, in meters, of the point in the local ENU system.

Data Types: double

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

Functions

enu2lla | lla2ned | ned2lla

Introduced in R2021a

lla2ned

Transform geodetic coordinates to local north-east-down coordinates

Syntax

```
xyzNED = lla2ned(lla,lla0,method)
```

Description

xyzNED = lla2ned(lla,lla0,method) transforms the geodetic coordinates lla to local northeast-down (NED) Cartesian coordinates xyzNED. Specify the origin of the local NED system as the geodetic coordinates lla0.

Note

- The latitude and longitude values in the geodetic coordinate system use the World Geodetic System of 1984 (WGS84) standard.
- Specify altitude as height in meters above the WGS84 reference ellipsoid.

Examples

Transform Geodetic Coordinates to NED Coordinates

Specify the geodetic coordinates of the local origin in Zermatt, Switzerland.

```
lla0 = [46.017 7.750 1673]; % [lat0 lon0 alt0]
```

Specify the geodetic coordinates of a point of interest. In this case, the point of interest is the Matterhorn.

```
lla = [45.976 7.658 4531]; % [lat lon alt]
```

Transform the geodetic coordinates to local NED coordinates using flat earth approximation.

```
xyzNED = lla2ned(lla,lla0,'flat')

xyzNED = 1 \times 3

10^3 \times -4.5572 -7.1244 -2.8580
```

Input Arguments

lla — Geodetic coordinates

three-element row vector | *n*-by-3 matrix

Geodetic coordinates, specified as a three-element row vector or an *n*-by-3 matrix. *n* is the number of points to transform. Specify each point in the form [lat lon alt]. lat and lon specify the latitude and longitude respectively in degrees. alt specifies the altitude in meters.

Data Types: double

11a0 — Origin of local NED system in geodetic coordinates

three-element row vector | n-by-3 matrix

Origin of the local NED system with the geodetic coordinates, specified as a three-element row vector or an n-by-3 matrix. n is the number of origin points. Specify each point in the form [lat0 lon0 alt0]. lat0 and lon0 specify the latitude and longitude respectively in degrees. alt0 specifies the altitude in meters.

Data Types: double

method — Transformation method

'flat'|'ellipsoid'

Transformation method, specified as 'flat' or 'ellipsoid'. This argument specifies whether the function assumes the planet is flat or ellipsoidal.

The flat Earth transformation method has these limitations:

- Assumes that the flight path and bank angle are zero.
- Assumes that the flat Earth *z*-axis is normal to the Earth at only the initial geodetic latitude and longitude. This method has higher accuracy over small distances from the initial geodetic latitude and longitude, and closer to the equator. The method calculates a longitude with higher accuracy when the variation in latitude is smaller.
- Latitude values of +90 and -90 may return unexpected values because of singularity at the poles.

Data Types: char | string

Output Arguments

xyzNED — Local NED Cartesian coordinates

three-element row vector | n-by-3 matrix

Local NED Cartesian coordinates, returned as a three-element row vector or an n-by-3 matrix. n is the number of transformed points. Each point is in the form [xNorth yEast zDown]. xNorth, yEast, and zDown are the respective x-, y-, and z-coordinates, in meters, of the point in the local NED system.

Data Types: double

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

Functions

enu2lla | lla2enu | ned2lla

Introduced in R2021a

lookangles

Satellite look angles from receiver and satellite positions

Syntax

```
[az,el,vis] = lookangles(recPos,satPos)
[az,el,vis] = lookangles(recPos,satPos,maskAngle)
```

Description

[az,el,vis] = lookangles(recPos,satPos) returns the look angles and visibilities of satellite positions for a given receiver position. The azimuth az and elevation el are the look angles in degrees in the Earth-centered Earth-fixed (ECEF) coordinate system. The visibility of the satellites vis is a logical array that the function calculates using the default receiver mask angle of 10 degrees.

[az,el,vis] = lookangles(recPos,satPos,maskAngle) returns the look angles and visibilities of satellites with a specified mask angle maskAngle in degrees.

Examples

Get Satellite Look Angles for Receiver Position

Use the lookangles function to get the azimuth and elevation angles of satellites for given satellite and receiver positions. Specify a mask angle of 5 degrees. Get the satellite positions using the gnssconstellation function.

Specify a receiver position in geodetic coordinates (latitude, longitude, altitude).

```
recPos = [42 -71 50];
```

Get the satellite positions for the current time.

```
t = datetime('now');
gpsSatPos = gnssconstellation(t);
```

Specify a mask angle of 5 degrees.

```
maskAngle = 5;
```

Get the azimuth and elevation look angles for the satellite positions. The vis output indicates which satellites are visible. Get the total using nnz.

```
[az,el,vis] = lookangles(recPos,gpsSatPos,maskAngle);
fprintf('%d satellites visible at %s.\n',nnz(vis),t);
9 satellites visible at 25-Feb-2021 12:29:41.
```

Input Arguments

recPos — Receiver position

three-element vector of the form [lat lon alt]

Receiver position in geodetic coordinates, specified as a three-element vector of the form [latitude longitude altitude]

Data Types: single | double

satPos — Satellite positions

N-by-3 matrix of scalars

Satellite positions in the Earth-centered Earth-fixed (ECEF) coordinate system in meters, specified as an *N*-by-3 matrix of scalars. *N* is the number of satellites in the constellation.

Data Types: single | double

maskAngle — Elevation mask angle

positive scalar

Elevation mask angle of the receiver, specified as a positive scalar in degrees.

Data Types: single | double

Output Arguments

az — Azimuth angles for visible satellite positions

n-element vector of angles

Azimuth angles for visible satellite positions, returned as an n-element vector of angles. n is the number of visible satellite positions in the plot. Azimuth angles are measured in degrees, clockwise-positive from the north direction looking down.

Example: [25 45 182 356]

Data Types: double

el — Elevation angles for visible satellite positions

n-element vector of angles

Elevation angles for visible satellite positions, returned as an n-element vector of angles. n is the number of visible satellite positions in the plot. Elevation angles are measured from the horizon line with 90 degrees being directly up.

Example: [45 90 27 74]

Data Types: double

vis — Satellite visibility

n-element logical array

Satellite visibility, returned as an n-element logical array. Each element indicates whether the satellite position given by az and el is visible.

Data Types: logical

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

Objects

gnssSensor|gpsSensor|imuSensor

Functions

gnssconstellation|pseudoranges|receiverposition|skyplot

Introduced in R2021a

ned2lla

Transform local north-east-down coordinates to geodetic coordinates

Syntax

```
lla = ned2lla(xyzNED,lla0,method)
```

Description

la = ned2lla(xyzNED, lla0, method) transforms the local north-east-down (NED) Cartesian coordinates xyzNED to geodetic coordinates lla. Specify the origin of the local NED system as the geodetic coordinates lla0.

Note

- The latitude and longitude values in the geodetic coordinate system use the World Geodetic System of 1984 (WGS84) standard.
- Specify altitude as height in meters above the WGS84 reference ellipsoid.

Examples

Transform NED Coordinates to Geodetic Coordinates

Specify the geodetic coordinates of the local origin in Zermatt, Switzerland.

```
lla0 = [46.017 7.750 1673]; % [lat0 lon0 alt0]
```

Specify the NED coordinates of a point of interest, in meters. In this case, the point of interest is the Matterhorn.

```
xyzNED = [-4556.3 -7134.8 -2852.4]; % [xNorth yEast zDown]
```

Transform the local NED coordinates to geodetic coordinates using flat earth approximation.

```
lla = ned2lla(xyzNED,lla0,'flat')

lla = 1 \times 3
10^3 \times

0.0460 0.0077 4.5254
```

Input Arguments

xyzNED — Local NED Cartesian coordinates

three-element row vector | *n*-by-3 matrix

Local NED Cartesian coordinates, specified as a three-element row vector or an n-by-3 matrix. n is the number of points to transform. Specify each point in the form [xNorth yEast zDown]. xNorth, yEast, and zDown are the respective x-, y-, and z-coordinates, in meters, of the point in the local NED system.

Data Types: double

11a0 — Origin of local NED system in geodetic coordinates

three-element row vector | *n*-by-3 matrix

Origin of the local NED system with the geodetic coordinates, specified as a three-element row vector or an n-by-3 matrix. n is the number of origin points. Specify each point in the form [lat0 lon0 alt0]. lat0 and lon0 specify the latitude and longitude respectively in degrees. alt0 specifies the altitude in meters.

Data Types: double

method — Transformation method

'flat'|'ellipsoid'

Transformation method, specified as 'flat' or 'ellipsoid'. This argument specifies whether the function assumes the planet is flat or ellipsoidal.

The flat Earth transformation method has these limitations:

- Assumes that the flight path and bank angle are zero.
- Assumes that the flat Earth *z*-axis is normal to the Earth at only the initial geodetic latitude and longitude. This method has higher accuracy over small distances from the initial geodetic latitude and longitude, and closer to the equator. The method calculates a longitude with higher accuracy when the variation in latitude is smaller.
- Latitude values of +90 and -90 may return unexpected values because of singularity at the poles.

Data Types: char | string

Output Arguments

lla — Geodetic coordinates

three-element row vector | *n*-by-3 matrix

Geodetic coordinates, returned as a three-element row vector or an n-by-3 matrix. n is the number of transformed points. Each point is in the form [$lat\ lon\ alt$]. $lat\ and\ lon\ specify$ the latitude and longitude, respectively, in degrees. $alt\ specifies$ the altitude in meters.

Data Types: double

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

Functions

enu2lla | lla2enu | lla2ned

Introduced in R2021a

copy

Create copy of path object

Syntax

path2 = copy(path1)

Description

path2 = copy(path1) creates a copy of the path object, path2, from the path object, path1.

Input Arguments

path1 - path object

navPath object

Path object, specified as a navPath object.

Data Types: object

Output Arguments

path2 — path object

navPath object

Path object, returned as a navPath object.

Data Types: object

See Also

navPath

Introduced in R2019b

magcal

Magnetometer calibration coefficients

Syntax

```
[A,b,expmfs] = magcal(D)
[A,b,expmfs] = magcal(D,fitkind)
```

Description

[A,b,expmfs] = magcal(D) returns the coefficients needed to correct uncalibrated magnetometer data D.

To produce the calibrated magnetometer data C, use equation C = (D-b)*A. The calibrated data C lies on a sphere of radius expmfs.

[A,b,expmfs] = magcal(D,fitkind) constrains the matrix A to be the type specified by fitkind. Use this syntax when only the soft- or hard-iron effect needs to be corrected.

Examples

Correct Data Lying on Ellipsoid

Generate uncalibrated magnetometer data lying on an ellipsoid.

```
c = [-50; 20; 100]; % ellipsoid center
r = [30; 20; 50]; % semiaxis radii

[x,y,z] = ellipsoid(c(1),c(2),c(3),r(1),r(2),r(3),20);
D = [x(:),y(:),z(:)];
```

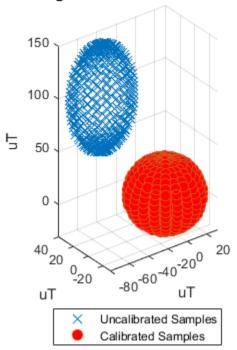
Correct the magnetometer data so that it lies on a sphere. The option for the calibration is set by default to 'auto'.

```
[A,b,expmfs] = magcal(D); % calibration coefficients
expmfs % Dipaly expected magnetic field strength in uT
expmfs = 31.0723
C = (D-b)*A; % calibrated data
```

Visualize the uncalibrated and calibrated magnetometer data.

```
ylabel('uT')
zlabel('uT')
legend('Uncalibrated Samples', 'Calibrated Samples', 'Location', 'southoutside')
title("Uncalibrated vs Calibrated" + newline + "Magnetometer Measurements")
hold off
```

Uncalibrated vs Calibrated Magnetometer Measurements



Input Arguments

D — Raw magnetometer data

N-by-3 matrix (default)

Input matrix of raw magnetometer data, specified as a N-by-3 matrix. Each column of the matrix corresponds to the magnetometer measurements in the first, second and third axes, respectively. Each row of the matrix corresponds to a single three-axis measurement.

Data Types: single | double

fitkind — Matrix output type

'auto' (default) | 'eye' | 'diag' | 'sym'

Matrix type for output A. The matrix type of A can be constrained to:

- 'eye' identity matrix
- 'diag' diagonal

- 'sym' symmetric
- 'auto' whichever of the previous options gives the best fit

Output Arguments

A — Correction matrix for soft-iron effect

3-by-3 matrix

Correction matrix for the soft-iron effect, returned as a 3-by-3 matrix.

b — Correction vector for hard-iron effect

3-by-1 vector

Correction vector for the hard-iron effect, returned as a 3-by-1 array.

expmfs — Expected magnetic field strength

scalar

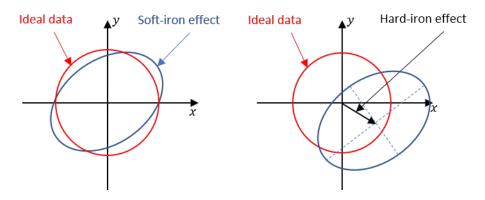
Expected magnetic filed strength, returned as a scalar.

More About

Soft- and Hard-Iron Effects

Because a magnetometer usually rotates through a full range of 3-D rotation, the ideal measurements from a magnetometer should form a perfect sphere centered at the origin if the magnetic field is unperturbed. However, due to distorting magnetic fields from the sensor circuit board and the surrounding environment, the spherical magnetic measurements can be perturbed. In general, two effects exist.

- 1 The soft-iron effect is described as the distortion of the ellipsoid from a sphere and the tilt of the ellipsoid, as shown in the left figure. This effect is caused by disturbances that influence the magnetic field but may not generate their own magnetic field. For example, metals such as nickel and iron can cause this kind of distortion.
- 2 The hard-iron effect is described as the offset of the ellipsoid center from the origin. This effect is produced by materials that exhibit a constant, additive field to the earth's magnetic field. This constant additive offset is in addition to the soft-iron effect as shown in the figure on the right.



The underlying algorithm in magcal determines the best-fit ellipsoid to the raw sensor readings and attempts to "invert" the ellipsoid to produce a sphere. The goal is to generate a correction matrix A to

account for the soft-iron effect and a vector b to account for the hard-iron effect. The three output options, 'eye', 'diag' and 'sym' correspond to three parameter-solving algorithms, and the 'auto' option chooses among these three options to give the best fit.

References

[1] Ozyagcilar, T. "Calibrating an eCompass in the Presence of Hard and Soft-iron Interference." *Freescale Semiconductor Ltd.* 1992, pp. 1-17.

See Also

Classes

magparams

Objects

imuSensor

Introduced in R2019a

mapClutter

Generate map with randomly scattered obstacles

Syntax

```
map = mapClutter
map = mapClutter(numObst)
map = mapClutter(numObst, shapes)
map = mapClutter(____, Name, Value)
```

Description

map = mapClutter generates a 2-D occupancy map as a binaryOccupancyMap object map, with a width and height of 50 meters and a resolution of 5 cells per meter. The map contains 20 randomly distributed obstacles of types Box and Circle. Generated obstacles have random sizes.

map = mapClutter(numObst) generates a 2-D occupancy map, of the default size and resolution,
with a specified number of randomly distributed obstacles, numObst, of default shapes.

map = mapClutter(numObst, shapes) generates a 2-D occupancy map, of the default size and resolution, with a specified number of obstacles, numObst, of specified shapes, shapes.

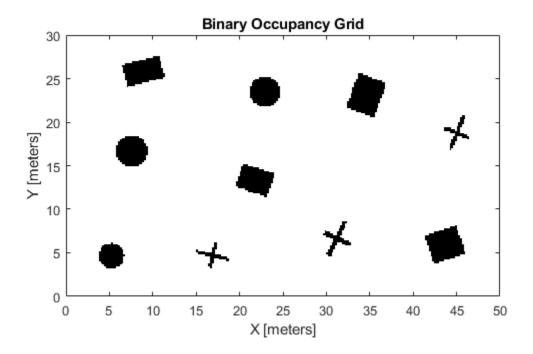
map = mapClutter(____, Name, Value) specifies options using one or more name-value pair arguments in addition to any combination of input arguments from previous syntaxes. For example, 'MapSize',[50 30] generates a randomly distributed obstacle map with a width of 50 meters and height of 30 meters.

Examples

Generate Randomly Distributed Obstacle Map

Generate a 2-D occupancy map with ten randomly scattered obstacles of types Box, Circle, and Plus. Specify the size of the map as 50 meters wide and 30 meters high with a resolution of 5 cells per meters.

```
map = mapClutter(10,{'Box','Plus','Circle'},'MapSize',[50 30],'MapResolution',5);
Visualize the generated obstacle map.
show(map)
```



Input Arguments

numObst — Number of obstacles

20 (default) | positive integer

Number of obstacles, specified as a positive integer.

Data Types: single | double

shapes — Obstacle shapes

{ 'Box', 'Circle'} (default) | string scalar | vector of strings | cell array of character vectors

Obstacle shapes, specified as a string scalar, vector of strings, or cell array of character vectors. The only valid shapes are Box, Circle, and Plus.

When you specify a string scalar, the function generates a map with obstacles of only the specified shape.

Example: "Box"

When you specify a vector of strings or a cell array of character vectors, the function generates a map with obstacles of each specified shape.

```
Example: ["Box","Plus"]
Example: {'Box','Plus','Circle'}
```

Data Types: cell | string

Name-Value Pair Arguments

Specify optional comma-separated pairs of Name, Value arguments. Name is the argument name and Value is the corresponding value. Name must appear inside quotes. You can specify several name and value pair arguments in any order as Name1, Value1, . . . , NameN, ValueN.

Example: 'MapSize', [50 40] generates a randomly distributed obstacle map with a width of 50 meters and height of 40 meters.

MapSize — Width and height of generated map

[50 50] (default) | two-element vector of positive real finite numbers

Width and height of the generated map, specified as the comma-separated pair consisting of 'MapSize' and a two-element vector of positive real finite numbers of the form [Width, Height]. Specify both values in meters.

Example: 'MapSize',[50 30]
Data Types: single | double

MapResolution — Resolution of generated map

5 (default) | positive real scalar

Resolution of the generated map, specified as the comma-separated pair consisting of 'MapResolution' and a positive real scalar in cells per meter.

Example: 'MapResolution',10
Data Types: single | double

Output Arguments

map — Map with randomly scattered obstacles

binaryOccupancyMap object

A map with randomly scattered obstacles, returned as a binaryOccupancyMap object.

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

binaryOccupancyMap | mapMaze | validatorOccupancyMap

Introduced in R2020b

mapMaze

Generate random 2-D maze map

Syntax

```
map = mapMaze
map = mapMaze(passageWidth)
map = mapMaze(passageWidth, wallThickness)
map = mapMaze(____, Name, Value)
```

Description

map = mapMaze generates a random 2-D maze map, map, as a binaryOccupancyMap object with a width and height of 50 meters and a resolution of 5 cells per meter. The maze map contains straight passages, turns, and T-junctions with a passage width of 4 grid cells and wall thickness of 1 grid cell.

map = mapMaze(passageWidth) generates a binaryOccupancyMap of a maze of the default size and resolution with a specified passage width, passageWidth, in number of grid cells.

map = mapMaze(passageWidth,wallThickness) specifies a wall thickness, wallThickness, in number of grid cells.

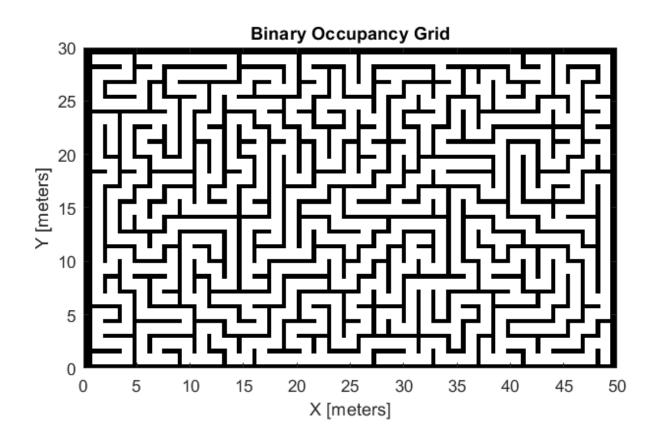
map = mapMaze(____, Name, Value) specifies options using one or more name-value pair
arguments in addition to any combination of input arguments from previous syntaxes. For example,
'MapSize',[50 30] generates a random maze map with a width of 50 meters and height of 30
meters.

Examples

Generate Random Maze Map

Generate a random 2-D maze map with a passage width of 5 grid cells and wall thickness of 2 grid cells. Specify the size of the map as 50 meters wide and 30 meters high with a resolution of 5 cells per meter.

```
map = mapMaze(5,2,'MapSize',[50 30],'MapResolution',5);
Visualize the generated obstacle map.
show(map)
```



Input Arguments

passageWidth — Width of maze passage

4 (default) | positive integer

Width of maze passage, specified as a positive integer in number of grid cells.

Data Types: single | double

wallThickness — Thickness of maze wall

1 (default) | positive integer

Thickness of maze wall, specified as a positive integer in number of grid cells.

Data Types: single | double

Name-Value Pair Arguments

Specify optional comma-separated pairs of Name, Value arguments. Name is the argument name and Value is the corresponding value. Name must appear inside quotes. You can specify several name and value pair arguments in any order as Name1, Value1, . . . , NameN, ValueN.

Example: 'MapSize', [50 40] generates a randomly distributed obstacle map with a width of 50 meters and height of 40 meters.

MapSize — Width and height of generated map

[50 50] (default) | two-element vector of positive real finite numbers

Width and height of the generated map, specified as the comma-separated pair consisting of 'MapSize' and a two-element vector of positive real finite numbers of the form [Width Height]. Specify both values in meters.

Example: 'MapSize',[50 30]
Data Types: single | double

MapResolution — Resolution of generated map

5 (default) | positive real scalar

Resolution of the generated map, specified as the comma-separated pair consisting of 'MapResolution' and a positive real scalar in cells per meter.

Example: 'MapResolution',10
Data Types: single | double

Output Arguments

map — Random maze map

binaryOccupancyMap object

Random maze map, returned as a binaryOccupancyMap object.

See Also

binaryOccupancyMap | mapClutter | validatorOccupancyMap

Introduced in R2021a

matchScans

Estimate pose between two laser scans

Syntax

```
pose = matchScans(currScan,refScan)
pose = matchScans(currRanges,currAngles,refRanges,refAngles)
[pose,stats] = matchScans(____, Name, Value)
```

Description

pose = matchScans(currScan, refScan) finds the relative pose between a reference
lidarScan and a current lidarScan object using the normal distributions transform (NDT).

pose = matchScans(currRanges,currAngles,refRanges,refAngles) finds the relative pose
between two laser scans specified as ranges and angles.

```
[pose, stats] = matchScans(____) returns additional statistics about the scan match result using the previous input arguments.
```

[___] = matchScans(___ , Name, Value) specifies additional options specified by one or more Name, Value pair arguments.

Examples

Match Lidar Scans

Create a reference lidar scan using lidarScan. Specify ranges and angles as vectors.

```
refRanges = 5*ones(1,300);
refAngles = linspace(-pi/2,pi/2,300);
refScan = lidarScan(refRanges,refAngles);
```

Using the transformScan (Robotics System Toolbox) function, generate a second lidar scan at an x, y offset of (0.5,0.2).

```
currScan = transformScan(refScan,[0.5 0.2 0]);
```

Match the reference scan and the second scan to estimate the pose difference between them.

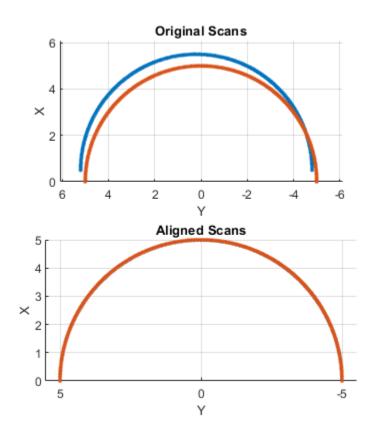
```
pose = matchScans(currScan, refScan);
```

Use the transformScan function to align the scans by transforming the second scan into the frame of the first scan using the relative pose difference. Plot both the original scans and the aligned scans.

```
currScan2 = transformScan(currScan,pose);
subplot(2,1,1);
hold on
```

```
plot(currScan)
plot(refScan)
title('Original Scans')
hold off

subplot(2,1,2);
hold on
plot(currScan2)
plot(refScan)
title('Aligned Scans')
xlim([0 5])
hold off
```



Match Laser Scans

This example uses the 'fminunc' solver algorithm to perform scan matching. This solver algorithm requires an Optimization Toolbox $^{\text{\tiny TM}}$ license.

Specify a reference laser scan as ranges and angles.

```
refRanges = 5*ones(1,300);
refAngles = linspace(-pi/2,pi/2,300);
```

Using the transformScan (Robotics System Toolbox) function, generate a second laser scan at an x, y offset of (0.5,0.2).

```
[currRanges,currAngles] = transformScan(refRanges,refAngles,[0.5 0.2 0]);
```

Match the reference scan and the second scan to estimate the pose difference between them.

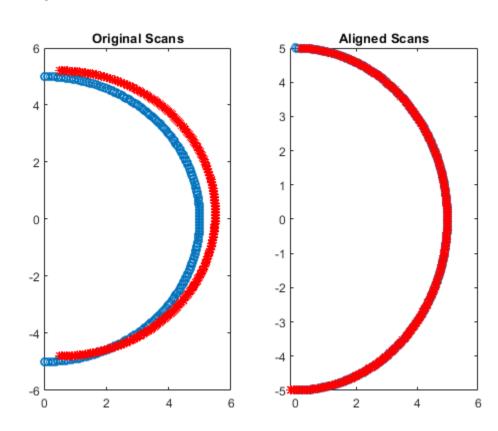
```
pose = matchScans(currRanges,currAngles,refRanges,refAngles,'SolverAlgorithm','fminunc');
```

Improve the estimate by giving an initial pose estimate.

Use the transformScan function to align the scans by transforming the second scan into the frame of the first scan using the relative pose difference. Plot both the original scans and the aligned scans.

[currRanges2,currAngles2] = transformScan(currRanges,currAngles,pose);

```
[x1, y1] = pol2cart(refAngles, refRanges);
[x2, y2] = pol2cart(currAngles, currRanges);
[x3, y3] = pol2cart(currAngles2, currRanges2);
subplot(1,2,1)
plot(x1,y1,'o',x2,y2,'*r')
title('Original Scans')
subplot(1,2,2)
plot(x1,y1,'o',x3,y3,'*r')
title('Aligned Scans')
```



Input Arguments

currScan — Current lidar scan readings

lidarScan object

Current lidar scan readings, specified as a lidarScan object.

Your lidar scan can contain Inf and NaN values, but the algorithm ignores them.

refScan — Reference lidar scan readings

lidarScan object

Reference lidar scan readings, specified as a lidarScan object.

Your lidar scan can contain Inf and NaN values, but the algorithm ignores them.

currRanges — Current laser scan ranges

vector in meters

Current laser scan ranges, specified as a vector. Ranges are given as distances to objects measured from the laser sensor.

Your laser scan ranges can contain Inf and NaN values, but the algorithm ignores them.

currAngles — Current laser scan angles

vector in radians

Current laser scan angles, specified as a vector in radians. Angles are given as the orientations of the corresponding range measurements.

refRanges — Reference laser scan ranges

vector in meters

Reference laser scan ranges, specified as a vector in meters. Ranges are given as distances to objects measured from the laser sensor.

Your laser scan ranges can contain Inf and NaN values, but the algorithm ignores them.

refAngles — Reference laser scan angles

vector in radians

Reference laser scan angles, specified as a vector in radians. Angles are given as the orientations of the corresponding range measurements.

Name-Value Pair Arguments

Specify optional comma-separated pairs of Name, Value arguments. Name is the argument name and Value is the corresponding value. Name must appear inside quotes. You can specify several name and value pair arguments in any order as Name1, Value1, . . . , NameN, ValueN.

Example: "InitialPose",[1 1 pi/2]

SolverAlgorithm — Optimization algorithm

"trust-region" (default) | "fminunc"

Optimization algorithm, specified as either "trust-region" or "fminunc". Using "fminunc" requires an Optimization Toolbox $^{\text{\tiny TM}}$ license.

InitialPose — Initial guess of current pose

[0 0 0] (default) | [x y theta]

Initial guess of the current pose relative to the reference laser scan, specified as the commaseparated pair consisting of "InitialPose" and an [x y theta] vector. [x y] is the translation in meters and theta is the rotation in radians.

CellSize — Length of cell side

1 (default) | numeric scalar

Length of a cell side in meters, specified as the comma-separated pair consisting of "CellSize" and a numeric scalar. matchScans uses the cell size to discretize the space for the NDT algorithm.

Tuning the cell size is important for proper use of the NDT algorithm. The optimal cell size depends on the input scans and the environment of your robot. Larger cell sizes can lead to less accurate matching with poorly sampled areas. Smaller cell sizes require more memory and less variation between subsequent scans. Sensor noise influences the algorithm with smaller cell sizes as well. Choosing a proper cell size depends on the scale of your environment and the input data.

MaxIterations — Maximum number of iterations

400 (default) | scalar integer

Maximum number of iterations, specified as the comma-separated pair consisting of "MaxIterations" and a scalar integer. A larger number of iterations results in more accurate pose estimates, but at the expense of longer execution time.

ScoreTolerance — Lower bounds on the change in NDT score

1e-6 (default) | numeric scalar

Lower bound on the change in NDT score, specified as the comma-separated pair consisting of "ScoreTolerance" and a numeric scalar. The NDT score is stored in the Score field of the output stats structure. Between iterations, if the score changes by less than this tolerance, the algorithm converges to a solution. A smaller tolerance results in more accurate pose estimates, but requires a longer execution time.

Output Arguments

pose — Pose of current scan

[x y theta]

Pose of current scan relative to the reference scan, returned as [x y theta], where [x y] is the translation in meters and theta is the rotation in radians.

stats — Scan matching statistics

structure

Scan matching statistics, returned as a structure with the following fields:

Score — Numeric scalar representing the NDT score while performing scan matching. This score
is an estimate of the likelihood that the transformed current scan matches the reference scan.
Score is always nonnegative. Larger scores indicate a better match.

• Hessian — 3-by-3 matrix representing the Hessian of the NDT cost function at the given pose solution. The Hessian is used as an indicator of the uncertainty associated with the pose estimate.

References

- [1] Biber, P., and W. Strasser. "The Normal Distributions Transform: A New Approach to Laser Scan Matching." *Intelligent Robots and Systems Proceedings*. 2003.
- [2] Magnusson, Martin. "The Three-Dimensional Normal-Distributions Transform -- an Efficient Representation for Registration, Surface Analysis, and Loop Detection." PhD Dissertation. Örebro University, School of Science and Technology, 2009.

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

Code generation is supported for the default SolverAlgorithm, "trust-region". You cannot use the "fminunc" algorithm in code generation.

See Also

Functions

lidarScan|matchScansGrid|matchScansLine|transformScan

Classes

monteCarloLocalization | occupancyMap

Topics

"Estimate Robot Pose with Scan Matching"

Introduced in R2019b

matchScansGrid

Estimate pose between two lidar scans using grid-based search

Syntax

```
pose = matchScansGrid(currScan, refScan)
[pose, stats] = matchScansGrid(____, Name, Value)
```

Description

pose = matchScansGrid(currScan, refScan) finds the relative pose between a reference lidarScan and a current lidarScan object using a grid-based search. matchScansGrid converts lidar scan pairs into probabilistic grids and finds the pose between the two scans by correlating their grids. The function uses a branch-and-bound strategy to speed up computation over large discretized search windows.

```
[pose,stats] = matchScansGrid(____) returns additional statistics about the scan match
result using the previous input arguments.

[___] = matchScansGrid(____, Name, Value) specifies options using one or more Name, Value
pair arguments. For example, 'InitialPose', [1 1 pi/2] specifies an initial pose estimate for
scan matching.
```

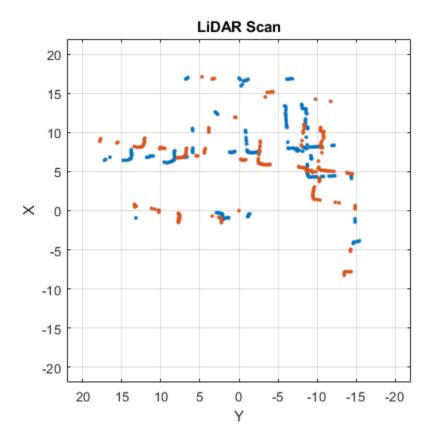
Examples

Match Scans Using Grid-Based Search

Perform scan matching using a grid-based search to estimate the pose between two laser scans. Generate a probabilistic grid from the scans and estimate the pose difference from those grids.

Load the laser scan data. These two scans are from an actual lidar sensor with changes in the robot pose and are stored as lidarScan objects.

```
load laserScans.mat scan scan2
plot(scan)
hold on
plot(scan2)
hold off
```



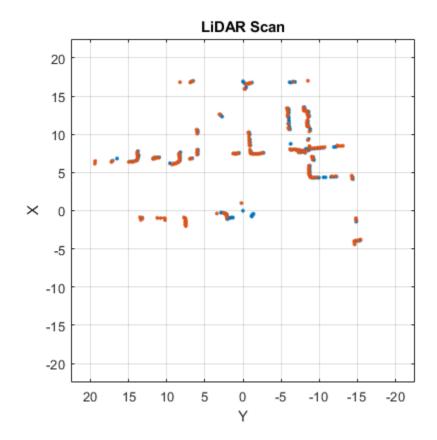
Use matchScansGrid to estimate the pose between the two scans.

```
relPose = matchScansGrid(scan2,scan);
```

Using the estimated pose, transform the current scan back to the reference scan. The scans overlap closely when you plot them together.

```
scan2Tformed = transformScan(scan2,relPose);
```

```
plot(scan)
hold on
plot(scan2Tformed)
hold off
```



Input Arguments

currScan — Current lidar scan readings

lidarScan object

Current lidar scan readings, specified as a lidarScan object.

Your lidar scan can contain Inf and NaN values, but the algorithm ignores them.

refScan — Reference lidar scan readings

lidarScan object

Reference lidar scan readings, specified as a lidarScan object.

Your lidar scan can contain Inf and NaN values, but the algorithm ignores them.

Name-Value Pair Arguments

Specify optional comma-separated pairs of Name, Value arguments. Name is the argument name and Value is the corresponding value. Name must appear inside quotes. You can specify several name and value pair arguments in any order as Name1, Value1, . . . , NameN, ValueN.

Example: 'InitialPose',[1 1 pi/2]

InitialPose — Initial guess of current pose

[0 0 0] (default) | [x y theta]

Initial guess of the current pose relative to the reference laser scan, specified as the commaseparated pair consisting of 'InitialPose' and an [x y theta] vector. [x y] is the translation in meters and theta is the rotation in radians.

Resolution — Grid cells per meter

20 (default) | positive integer

Grid cells per meter, specified as the comma-separated pair consisting of 'Resolution' and a positive integer. The accuracy of the scan matching result is accurate up to the grid cell size.

MaxRange — Maximum range of lidar sensor

8 (default) | positive scalar

Maximum range of lidar sensor, specified as the comma-separated pair consisting of 'MaxRange' and a positive scalar.

TranslationSearchRange — Search range for translation

[4 4] (default) | [x y] vector

Search range for translation, specified as the comma-separated pair consisting of 'TranslationSearchRange' and an $[x \ y]$ vector. These values define the search window in meters around the initial translation estimate given in InitialPose. If the InitialPose is given as $[x0 \ y0]$, then the search window coordinates are $[x0-x \ x0+x]$ and $[y0-y \ y0+y]$. This parameter is used only when InitialPose is specified.

RotationSearchRange — Search range for rotation

pi/4 (default) | positive scalar

Search range for rotation, specified as the comma-separated pair consisting of 'RotationSearchRange' and a positive scalar. This value defines the search window in radians around the initial rotation estimate given in InitialPose. If the InitialPose rotation is given as th0, then the search window is [th0-a th0+a], where a is the rotation search range. This parameter is used only when InitialPose is specified.

Output Arguments

pose — Pose of current scan

[x y theta] vector

Pose of current scan relative to the reference scan, returned as an $[x \ y \ theta]$ vector, where $[x \ y]$ is the translation in meters and theta is the rotation in radians.

stats — Scan matching statistics

structure

Scan matching statistics, returned as a structure with the following field:

- Score Numeric scalar representing the score while performing scan matching. This score is an
 estimate of the likelihood that the transformed current scan matches the reference scan. Score is
 always nonnegative. Larger scores indicate a better match, but values vary depending on the lidar
 data used.
- Covariance Estimated covariance representing the confidence of the computed relative pose, returned as a 3-by-3 matrix.

References

[1] Hess, Wolfgang, Damon Kohler, Holger Rapp, and Daniel Andor. "Real-Time Loop Closure in 2D LIDAR SLAM." 2016 IEEE International Conference on Robotics and Automation (ICRA). 2016.

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

Functions

lidarScan | matchScans | matchScansLine | transformScan

Classes

lidarSLAM

Topics

"Implement Simultaneous Localization And Mapping (SLAM) with Lidar Scans"

"Implement Online Simultaneous Localization And Mapping (SLAM) with Lidar Scans"

Introduced in R2019b

matchScansLine

Estimate pose between two laser scans using line features

Syntax

```
relpose = matchScansLine(currScan, refScan, initialRelPose)
[relpose, stats] = matchScansLine(____)
[relpose, stats, debugInfo] = matchScansLine(____)
[___] = matchScansLine(____, Name, Value)
```

Description

relpose = matchScansLine(currScan, refScan, initialRelPose) estimates the relative pose between two scans based on matched line features identified in each scan. Specify an initial guess on the relative pose, initialRelPose.

[relpose, stats] = matchScansLine(____) returns additional information about the covariance
and exit condition in stats as a structure using the previous inputs.

[relpose, stats, debugInfo] = matchScansLine(____) returns additional debugging info,
debugInfo, from the line-based scan matching result.

[___] = matchScansLine(___, Name, Value) specifies options using one or more Name, Value pair arguments.

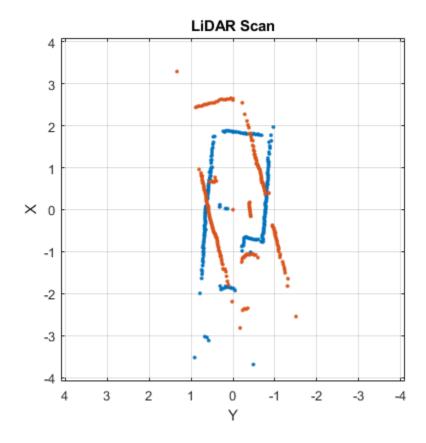
Examples

Estimate Pose of Scans with Line Features

This example shows how to use the matchScansLine function to estimate the relative pose between lidar scans given an initial estimate. The identified line features are visualized to show how the scanmatching algorithm associates features between scans.

Load a pair of lidar scans. The .mat file also contains an initial guess of the relative pose difference, initGuess, which could be based on odometry or other sensor data.

```
load tb3_scanPair.mat
plot(s1)
hold on
plot(s2)
hold off
```



Set parameters for line feature extraction and association. The noise of the lidar data determines the smoothness threshold, which defines when a line break occurs for a specific line feature. Increase this value for more noisy lidar data. The compatibility scale determines when features are considered matches. Increase this value for looser restrictions on line feature parameters.

```
smoothnessThresh = 0.2;
compatibilityScale = 0.002;
```

Call matchScansLine with the given initial guess and other parameters specified as name-value pairs. The function calculates line features for each scan, attempts to match them, and uses an overall estimate to get the difference in pose.

After matching the scans, the debugInfo output gives you information about the detected line feature parameters, [rho alpha], and the hypothesis of which features match between scans.

debugInfo.MatchHypothesis states that the first, second, and sixth line feature in s1 match the fifth, second, and fourth features in s2.

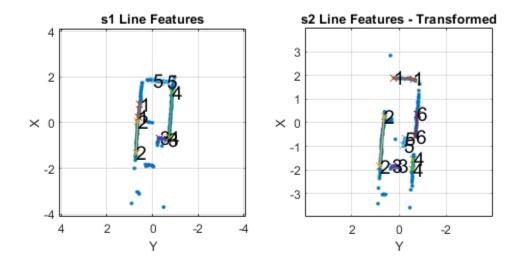
debugInfo.MatchHypothesis

```
ans = 1 \times 6

5 2 0 0 0 4
```

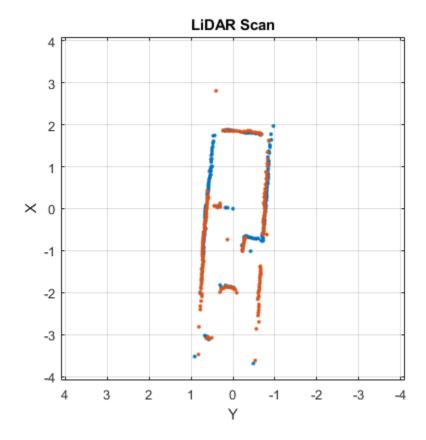
The provided helper function plots these two scans and the features extracted with labels. s2 is transformed to be in the same frame based on the initial guess for relative pose.

exampleHelperShowLineFeaturesInScan(s1, s2, debugInfo, initGuess);



Use the estimated relative pose from matchScansLine to transform s2. Then, plot both scans to show that the relative pose difference is accurate and the scans overlay to show the same environment.

```
s2t = transformScan(s2,relPose);
clf
plot(s1)
hold on
plot(s2t)
hold off
```



Input Arguments

currScan — Current lidar scan readings

lidarScan object

Current lidar scan readings, specified as a lidarScanobject.

Your lidar scan can contain Inf and NaN values, but the algorithm ignores them.

refScan — Reference lidar scan readings

lidarScan object

Reference lidar scan readings, specified as a lidarScan object.

Your lidar scan can contain Inf and NaN values, but the algorithm ignores them.

initialRelPose — Initial guess of relative pose

[x y theta]

Initial guess of the current pose relative to the reference laser scan frame, specified an $[x \ y]$ theta] vector. $[x \ y]$ is the translation in meters and theta is the rotation in radians.

Name-Value Pair Arguments

Specify optional comma-separated pairs of Name, Value arguments. Name is the argument name and Value is the corresponding value. Name must appear inside quotes. You can specify several name and value pair arguments in any order as Name1, Value1, . . . , NameN, ValueN.

Example: "LineMergeThreshold", [0.10 0.2]

SmoothnessThreshold — Threshold to detect line break points in scan

0.1 (default) | scalar

Threshold to detect line break points in scan, specified as a scalar. Smoothness is defined by calling diff(diff(scanData)) and assumes equally spaced scan angles. Scan points corresponding to smoothness values higher than this threshold are considered break points. For lidar scan data with a higher noise level, increase this threshold.

MinPointsPerLine — Minimum number of scan points in each line feature

10 (default) | positive integer greater than 3

Minimum number of scan points in each line feature, specified as a positive integer greater than 3.

A line feature cannot be identified from a set of scan points if the number of points in that set is below this threshold. When the lidar scan data is noisy, setting this property too small may result in low-quality line features being identified and skew the matching result. On the other hand, some key line features may be missed if this number is set too large.

LineMergeThreshold — Threshold on line parameters to merge line features

[0.05 0.1] (default) | two-element vector [rho alpha]

Threshold on line parameters to merge line features, specified as a two-element vector [rho alpha]. A line is defined by two parameters:

- rho Distance from the origin to the line along a vector perpendicular to the line, specified in meters.
- alpha -- Angle between the x-axis and the rho vector, specified in radians.

If the difference between these parameters for two line features is below the given threshold, the line features are merged.

MinCornerPromenance — Lower bound on prominence value to detect a corner

0.05 (default) | positive scalar

Lower bound on prominence value to detect a corner, specified as a positive scalar.

Prominence measures how much a local extrema stands out in the lidar data. Only values higher than this lower bound are considered a corner. Corners help identify line features, but are not part of the feature itself. For noisy lidar scan data, increase this lower bound.

CompatibilityScale — Scale used to adjust the compatibility thresholds for feature association

0.0005 (default) | positive scalar

Scale used to adjust the compatibility thresholds for feature association, specified as a positive scalar. A lower scale means tighter compatibility threshold for associating features. If no features are found

in lidar data with obvious line features, increase this value. For invalid feature matches, reduce this value.

Output Arguments

relpose — Pose of current scan

[x y theta]

Pose of current scan relative to the reference scan, returned as [x y theta], where [x y] is the translation in meters and theta is the rotation in radians.

stats — Scan matching information

structure

Scan matching information, returned as a structure with the following fields:

- Covariance -- 3-by-3 matrix representing the covariance of the relative pose estimation. The matScansLine function does not provide covariance between the (x,y) and the theta components of the relative pose. Therefore, the matrix follows the pattern: [Cxx, Cxy 0; Cyx Cyy 0; 0 0 Ctheta].
- ExitFlag -- Scalar value indicating the exit condition of the solver:
 - 0 -- No error.
 - 1 Insufficient number of line features (< 2) are found in one or both of the scans. Consider using different scans with more line features.
 - 2 -- Insufficient number of line feature matches are identified. This may indicate the initialRelPose is invalid or scans are too far apart.

debugInfo — Debugging information for line-based scan matching result

structure

Debugging information for line-based scan matching result, returned as a structure with the following fields:

- ReferenceFeatures -- Line features extracted from the reference scan as an n-by-2 matrix. Each line feature is represented as [rho alpha] for the parametric equation, $rho = x \cdot \cos(alpha) + y \cdot \sin(alpha)$.
- ReferenceScanMask Mask indicating which points in the reference scan are used for each line feature as an *n*-by-*p* matrix. Each row corresponds to a row in ReferenceFeatures and contains zeros and ones for each point in refScan.
- CurrentFeatures -- Line features extracted from the current scan as an n-by-2 matrix. Each line feature is represented as [rho alpha] for the parametric equation, $rho = x \cdot \cos(alpha) + y \cdot \sin(alpha)$.
- CurrentScanMask Mask indicating which points in the current scan are used for each line feature as an *n*-by-*p* matrix. Each row corresponds to a row in ReferenceFeatures and contains zeros and ones for each point in refScan.
- MatchHypothesis Best line feature matching hypothesis as an n element vector, where n is the number of line features in CurrentFeatures. Each element represents the corresponding feature in ReferenceFeatures and gives the index of the matched feature in ReferenceFeatures is an index match the

• MatchValue -- Scalar value indicating a score for each MatchHypothesis. A lower value is considered a better match. If two elements of MatchHypothesis have the same index, the feature with a lower score is used.

References

- [1] Neira, J., and J.d. Tardos. "Data Association in Stochastic Mapping Using the Joint Compatibility Test." *IEEE Transactions on Robotics and Automation* 17, no. 6 (2001): 890–97. https://doi.org/10.1109/70.976019.
- [2] Shen, Xiaotong, Emilio Frazzoli, Daniela Rus, and Marcelo H. Ang. "Fast Joint Compatibility Branch and Bound for Feature Cloud Matching." 2016 IEEE/RSJ International Conference on Intelligent Robots and Systems (IROS), 2016. https://doi.org/10.1109/iros.2016.7759281.

See Also

lidarSLAM | matchScans | matchScansGrid

Topics

"Estimate Robot Pose with Scan Matching"

"Implement Simultaneous Localization And Mapping (SLAM) with Lidar Scans"

Introduced in R2020a

optimizePoseGraph

Optimize nodes in pose graph

Syntax

```
updatedGraph = optimizePoseGraph(poseGraph)
updatedGraph = optimizePoseGraph(poseGraph,solver)
[updatedGraph,solutionInfo] = optimizePoseGraph(____)
[___] = optimizePoseGraph(____,Name,Value)
```

Description

updatedGraph = optimizePoseGraph(poseGraph) adjusts the poses based on their edge constraints defined in the specified graph to improve the overall graph. You optimize either a 2-D or 3-D pose graph. The returned pose graph has the same topology with updated nodes.

This pose graph optimization assumes all edge constraints and loop closures are valid. To consider trimming edges based on bad loop closures, see the trimLoopClosures function.

updatedGraph = optimizePoseGraph(poseGraph, solver) specifies the solver type for optimizing the pose graph.

```
[updatedGraph, solutionInfo] = optimizePoseGraph( \underline{ \  \  } ) \ returns \ additional \ statistics \ about the optimization process in solutionInfo using any of the previous syntaxes.
```

[____] = optimizePoseGraph(____, Name, Value) specifies additional options using one or more Name, Value pairs. For example, 'MaxIterations', 1000 increases the maximum number of iterations to 1000.

Examples

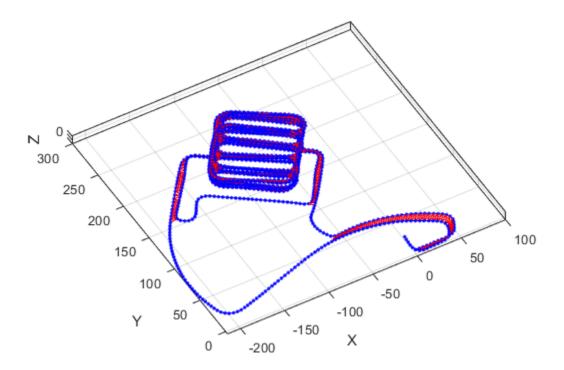
Optimize a 3-D Pose Graph

Optimize a pose graph based on the nodes and edge constraints. The pose graph used in this example is taken from the MIT Dataset and was generated using information extracted from a parking garage.

Load the pose graph from the MIT dataset. Inspect the poseGraph3D object to view the number of nodes and loop closures.

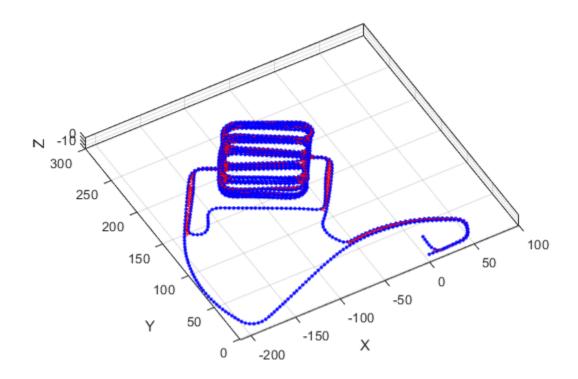
Plot the pose graph with IDs off. Red lines indicate loop closures identified in the dataset.

```
title('Original Pose Graph')
show(pg,'IDs','off');
view(-30,45)
```



Optimize the pose graph. Nodes are adjusted based on the edge constraints and loop closures. Plot the optimized pose graph to see the adjustment of the nodes with loop closures.

```
updatedPG = optimizePoseGraph(pg);
figure
title('Updated Pose Graph')
show(updatedPG,'IDs','off');
view(-30,45)
```



Input Arguments

poseGraph — 2-D or 3-D pose graph

poseGraph object | poseGraph3D object | digraph object

2-D or 3-D pose graph, specified as a poseGraph, poseGraph3D, digraph object.

To use the digraph object, generate the pose graph using createPoseGraph from an imageviewset or pcviewset object. You must have Computer Vision Toolbox™ and the solver must be set to "builtin-trust-region". The 'LoopClosuresToIgnore' and 'FirstNodePose' name-value pairs are ignored if specified.

The edges of digraph object are described by affine3d or rigid3d objects.

solver — Pose graph solver

"builtin-trust-region" (default) | "g2o-levenberg-marquardt"

Pose graph solver, specified as either "builtin-trust-region" or "g2o-levenberg-marquardt". To tune either solver, use the name-value pair arguments for that solver.

Name-Value Pair Arguments

Specify optional comma-separated pairs of Name, Value arguments. Name is the argument name and Value is the corresponding value. Name must appear inside quotes. You can specify several name and value pair arguments in any order as Name1, Value1, . . . , NameN, ValueN.

Example: 'MaxTime', 300

Note Depending on the solver input, the function supports different name-value pairs.

If the solver input is set to "builtin-trust-region":

MaxTime — **Maximum** time allowed

500 (default) | positive numeric scalar

Maximum time allowed, specified as the comma-separated pair consisting of 'MaxTime' and a positive numeric scalar in seconds. The optimizer exits after it exceeds this time.

GradientTolerance — Lower bound on norm of gradient

0.5e-8 (default) | scalar

Lower bound on the norm of the gradient, specified as the comma-separated pair consisting of 'GradientTolerance' and a scalar. The norm of the gradient is calculated based on the cost function of the optimization. If the norm falls below this value, the optimizer exits.

FunctionTolerance — Lower bound on change in cost function

1e-8 (default) | scalar

Lower bound on the change in the cost function, specified as the comma-separated pair consisting of 'FunctionTolerance' and a scalar. If the cost function change falls below this value between optimization steps, the optimizer exits.

StepTolerance — Lower bound on step size

1e-12 (default) | scalar

Lower bound on the step size, specified as the comma-separated pair consisting of 'StepTolerance' and a scalar. If the norm of the optimization step falls below this value, the optimizer exits.

InitialTrustRegionRadius — Initial trust region radius

100 (default) | scalar

Initial trust region radius, specified as a scalar.

VerboseOutput — Display intermediate iteration information

'off' (default) | 'on'

Display intermediate iteration information on the MATLAB command line, specified as the commaseparated pair consisting of 'VerboseOutput' and either 'off' or 'on'.

LoopClosuresToIgnore — IDs of loop closure edges in pose graph

vector

IDs of loop closure edges in poseGraph, specified as the comma-separated pair consisting of 'LoopClosuresToIgnore' and a vector. To get edge IDs from the pose graph, use findEdgeID.

FirstNodePose — Pose of first node

[0 0 0] or [0 0 0 1 0 0 0] (default) | [x y theta] | [x y z qw qx qy qz]

Pose of the first node in poseGraph, specified as the comma-separated pair consisting of 'FirstNodePose' and a pose vector.

For poseGraph (2-D), the pose is an [x y theta] vector, which defines the relative xy-position and orientation angle, theta.

For poseGraph3D, the pose is an $[x \ y \ z \ qw \ qx \ qy \ qz]$ vector, which defines the relative xyz-position and quaternion orientation, $[qw \ qx \ qy \ qz]$.

Note Many other sources for 3-D pose graphs, including .g2o formats, specify the quaternion orientation in a different order, for example, [qx qy qz qw]. Check the source of your pose graph data before adding nodes to your poseGraph3D object.

If the solver input is set to "g2o-levenberg-marquardt":

MaxIterations — Maximum number of iterations

300 (default) | positive integer

Maximum number of iterations, specified as the comma-separated pair consisting of 'MaxIterations' and a positive integer. The optimizer exits after it exceeds this number of iterations.

MaxTime — Maximum time allowed

500 (default) | positive numeric scalar

Maximum time allowed, specified as the comma-separated pair consisting of 'MaxTime' and a positive numeric scalar in seconds. The optimizer exits after it exceeds this time.

FunctionTolerance — Lower bound on change in cost function

1e-8 (default) | scalar

Lower bound on the change in the cost function, specified as the comma-separated pair consisting of 'FunctionTolerance' and a scalar. If the cost function change falls below this value between optimization steps, the optimizer exits.

VerboseOutput — **Display intermediate iteration information**

```
'off' (default) | 'on'
```

Display intermediate iteration information on the MATLAB command line, specified as the commaseparated pair consisting of 'VerboseOutput' and either 'off' or 'on'.

LoopClosuresToIgnore — IDs of loop closure edges in pose graph

vector

IDs of loop closure edges in poseGraph, specified as the comma-separated pair consisting of 'LoopClosuresToIgnore' and a vector. To get edge IDs from the pose graph, use findEdgeID.

FirstNodePose — Pose of first node

```
[0 0 0] or [0 0 0 1 0 0 0] (default) | [x y theta] | [x y z qw qx qy qz]
```

Pose of the first node in poseGraph, specified as the comma-separated pair consisting of 'FirstNodePose' and a pose vector.

For poseGraph (2-D), the pose is an [x y theta] vector, which defines the relative xy-position and orientation angle, theta.

For poseGraph3D, the pose is an [x y z qw qx qy qz] vector, which defines the relative xyz-position and quaternion orientation, [qw qx qy qz].

Note Many other sources for 3-D pose graphs, including .g2o formats, specify the quaternion orientation in a different order, for example, [qx qy qz qw]. Check the source of your pose graph data before adding nodes to your poseGraph3D object.

Output Arguments

updatedGraph — Optimized 2-D or 3-D pose graph

poseGraph object | poseGraph3D object

Optimized 2-D or 3-D pose graph, returned as a poseGraph or poseGraph3D object.

solutionInfo — Statistics of optimization process

structure

Statistics of optimization process, returned as a structure with these fields:

- Iterations Number of iterations used in optimization.
- ResidualError Value of cost function when optimizer exits.
- Exit Flag Exit condition for optimizer:
 - 1 Local minimum found.
 - 2 Maximum number of iterations reached. See MaxIterations name-value pair argument.
 - 3 Algorithm timed out during operation.
 - 4 Minimum step size. The step size is below the StepTolerance name-value pair argument.
 - 5 The change in error is below the minimum.
 - 8 Trust region radius is below the minimum set in InitialTrustRegionRadius.

References

- [1] Grisetti, G., R. Kummerle, C. Stachniss, and W. Burgard. "A Tutorial on Graph-Based SLAM." *IEEE Intelligent Transportation Systems Magazine*. Vol. 2, No. 4, 2010, pp. 31-43. doi:10.1109/mits.2010.939925.
- [2] Carlone, Luca, Roberto Tron, Kostas Daniilidis, and Frank Dellaert. "Initialization Techniques for 3D SLAM: a Survey on Rotation Estimation and its Use in Pose Graph Optimization." 2015 IEEE International Conference on Robotics and Automation (ICRA). 2015, pp. 4597–4604.

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

• Use this syntax when constructing poseGraph or poseGraph3D objects for code generation:

poseGraph = poseGraph('MaxNumEdges', maxEdges, 'MaxNumNodes', maxNodes) specifies
an upper bound on the number of edges and nodes allowed in the pose graph when generating
code. This limit is only required when generating code.

• The "g2o-levenberg-marquardt" solver input argument is not supported for code generation.

See Also

Functions

addRelativePose | edgeConstraints | edgeNodePairs | findEdgeID | nodeEstimates |
removeEdges | trimLoopClosures

Objects

lidarSLAM | poseGraph | poseGraph3D

Topics

- "Implement Simultaneous Localization And Mapping (SLAM) with Lidar Scans"
- "Implement Online Simultaneous Localization And Mapping (SLAM) with Lidar Scans"

Introduced in R2019b

plotTransforms

Plot 3-D transforms from translations and rotations

Syntax

```
ax = plotTransforms(translations, rotations)
ax = plotTransforms(translations, rotations, Name, Value)
```

Description

ax = plotTransforms(translations, rotations) draws transform frames in a 3-D figure window using the specified translations and rotations. The z-axis always points upward.

ax = plotTransforms(translations, rotations, Name, Value) specifies additional options using name-value pair arguments. Specify multiple name-value pairs to set multiple options.

Input Arguments

translations — xyz-positions

```
[x y z] vector | matrix of [x y z] vectors
```

xyz-positions specified as a vector or matrix of [x y z] vectors. Each row represents a new frame to plot with a corresponding orientation in rotations.

```
Example: [1 1 1; 2 2 2]
```

rotations — Rotations of xyz-positions

```
quaternion array | matrix of [w x y z] quaternion vectors
```

Rotations of xyz-positions specified as a array or n-by-4 matrix of [w x y z] quaternion vectors. Each element of the array or each row of the matrix represents the rotation of the xyz-positions specified in translations.

```
Example: [1 1 1 0; 1 3 5 0]
```

Name-Value Pair Arguments

Specify optional comma-separated pairs of Name, Value arguments. Name is the argument name and Value is the corresponding value. Name must appear inside quotes. You can specify several name and value pair arguments in any order as Name1, Value1, . . . , NameN, ValueN.

```
Example: 'FrameSize'.5
```

FrameSize — Size of frames and attached meshes

positive numeric scalar

Size of frame and attached meshes, specified as positive numeric scalar.

InertialZDirection — Direction of positive z-axis of inertial frame

```
"up" (default) | "down"
```

Direction of the positive *z*-axis of inertial frame, specified as either "up" or "down". In the plot, the positive *z*-axis always points up.

MeshFilePath — File path of mesh file attached to frames

character vector | string scalar

File path of mesh file attached to frames, specified as either a character vector or string scalar. The mesh is attached to each plotted frame at the specified position and orientation. Provided .stl are

- "fixedwing.stl"
- "multirotor.stl"
- "groundvehicle.stl"

Example: 'fixedwing.stl'

MeshColor — Color of attached mesh

"red" (default) | RGB triplet | string scalar

Color of attached mesh, specified as an RGB triple or string scalar.

Example: [0 0 1] or "green"

Parent — Axes used to plot transforms

Axes object | UIAxes object

Axes used to plot the pose graph, specified as the comma-separated pair consisting of 'Parent' and either an Axes or UIAxes object. See axes or uiaxes.

Output Arguments

ax — Axes used to plot transforms

Axes object | UIAxes object

Axes used to plot the pose graph, specified as the comma-separated pair consisting of 'Parent' and either an Axes or UIAxesobject. See axes or uiaxes.

See Also

eul2quat | hom2cart | quaternion | rotm2quat | tform2quat

Introduced in R2018b

poseGraphSolverOptions

Solver options for pose graph optimization

Syntax

```
solverOptions = poseGraphSolverOptions(solverType)
```

Description

solverOptions = poseGraphSolverOptions(solverType) returns the set of solver options
with default values for the specified pose graph solver type.

Examples

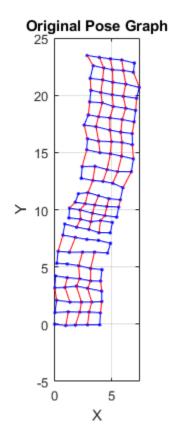
Optimize and Trim Loop Closures For 2-D Pose Graphs

Optimize a pose graph based on the nodes and edge constraints. Trim loop closed based on their edge residual errors.

Load the data set that contains a 2-D pose graph. Inspect the poseGraph object to view the number of nodes and loop closures.

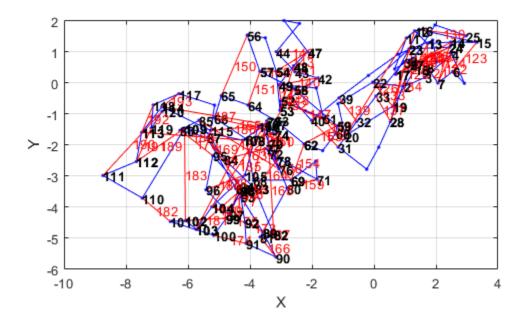
Plot the pose graph with IDs off. Red lines indicate loop closures identified in the dataset. The poses in the graph should follow a grid pattern, but show evidence of drift over time.

```
show(pg,'IDs','off');
title('Original Pose Graph')
```



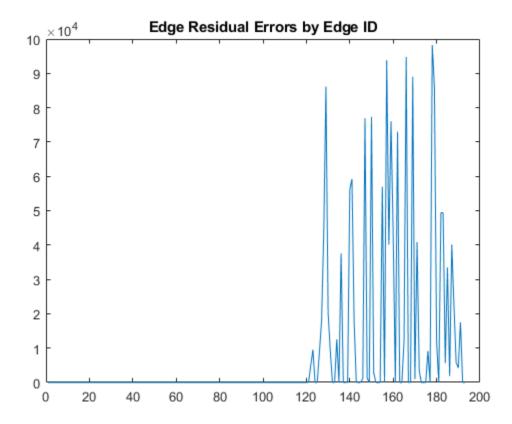
Optimize the pose grap using the optimizePoseGraph function. By default, this function uses the "builtin-trust-region" solver. Because the pose graph contains some bad loop closures, the resulting pose graph is actual not desirable.

```
pgOptim = optimizePoseGraph(pg);
figure;
show(pgOptim);
```



Look at the edge residual errors for the original pose graph. Large outlier error values at the end indicate bad loop closures.

```
resErrorVec = edgeResidualErrors(pg);
plot(resErrorVec);
title('Edge Residual Errors by Edge ID')
```



Certain loop closures should be trimmed from the pose graph based on their residual error. Use the trimLoopClosures function to trim therse bad loop closures. Set the maximum and truncation threshold for the trimmer parameters. This threshold is set based on the measurement accuracy and should be tuned for your system.

```
trimParams.MaxIterations = 100;
trimParams.TruncationThreshold = 25;
solverOptions = poseGraphSolverOptions;
```

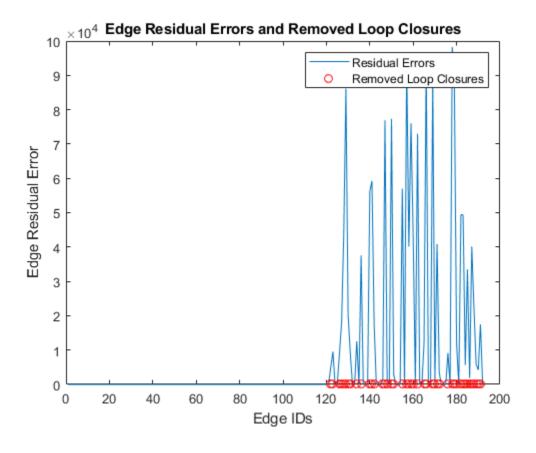
Use the trimLoopClosures function with the trimmer parameters and solver options.

```
[pgNew, trimInfo, debugInfo] = trimLoopClosures(pg,trimParams,solverOptions);
```

From the trimInfo output, plot the loop closures removed from the optimized pose graph. By plotting with the residual errors plot before, you can see the large error loop closures were removed.

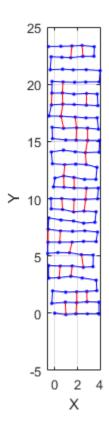
removedLCs = trimInfo.LoopClosuresToRemove;

```
hold on
plot(removedLCs,zeros(length(removedLCs)),'or')
title('Edge Residual Errors and Removed Loop Closures')
legend('Residual Errors', 'Removed Loop Closures')
xlabel('Edge IDs')
ylabel('Edge Residual Error')
hold off
```



Show the new pose graph with the bad loop closures trimmed.

show(pgNew,"IDs","off");



Input Arguments

solverType — Pose graph solver type

```
'builtin-trust-region' (default)|'g2o-levenberg-marquardt'
```

Pose graph sovler type, specified as 'builtin-trust-region' or 'g2o-levenberg-marquardt'.

The function generates a set of solver options with default values for the specified pose graph solver type:

```
pgSolverTrustRegion = poseGraphSolverOptions('builtin-trust-region')
pgSolverTrustRegion =
TrustRegion (builtin-trust-region-dogleg) options:
               MaxIterations: 300
                     MaxTime: 10
           FunctionTolerance: 1.0000e-08
           GradientTolerance: 5.0000e-09
               StepTolerance: 1.0000e-12
    InitialTrustRegionRadius: 100
               VerboseOutput: 'off'
pgSolverG2o = poseGraphSolverOptions('g2o-levenberg-marquardt')
```

FunctionTolerance: 1.0000e-09
 VerboseOutput: 'off'

Data Types: char | string

Output Arguments

solverOptions — Pose graph solver options

poseGraphSolverOptions parameters

Pose graph solver options, specified as a set of parameters generated by calling the poseGraphSolverOptions function. The function generates a set of solver options with default values for the specified pose graph solver type.

If the solverType input is set to "builtin-trust-region":

	Default	Description		
MaxIterations	300	Maximum number of iterations, specified as a positive integer. The optimizer exits after it exceeds this number of iterations.		
MaxTime	500	Maximum time allowed, specified as a positive numeric scalar in seconds. The optimizer exits after it exceeds this time.		
FunctionTolerance	1e-8	Lower bound on the change in the cost function, specified as a scalar. If the cost function change falls below this value between optimization steps, the optimizer exits.		
GradientTolerance	0.5e-8	Lower bound on the norm of the gradient, specified as a scalar. The norm of the gradient is calculated based on the cost function of the optimization. If the norm falls below this value, the optimizer exits.		
StepTolerance	1e-12	Lower bound on the step size, specified as a scalar. If the norm of the optimization step falls below this value, the optimizer exits.		
InitialTrustRegionRadius	100	Initial trust region radius, specified as a scalar.		
VerboseOutput	'off' or 'on'	Display intermediate iteration information on the MATLAB command line.		

If the solver input is set to "g2o-levenberg-marquardt":

	Default	Description		
MaxIterations	300	Maximum number of iterations, specified as a positive integer. The optimizer exits after it exceeds this number of iterations.		
MaxTime	500	Maximum time allowed, specified as a positive numeric scalar in seconds. The optimizer exits after it exceeds this time.		
FunctionTolerance	1e-8	Lower bound on the change in the cost function, specified as a scalar. If the cost function change falls below this value between optimization steps, the optimizer exits.		
VerboseOutput	'off' or 'on'	Display intermediate iteration information on the MATLAB command line.		

See Also

Functions

 $edge Constraints \mid edge Residual Errors \mid edge Residual Errors \mid edges \mid remove Edges \mid trimLoop Closures \\$

Objects

lidarSLAM | poseGraph | poseGraph3D

Introduced in R2020b

pseudoranges

Pseudoranges between GNSS receiver and satellites

Syntax

```
p = pseudoranges(recPos,satPos)
[p, pdot] = pseudoranges(____,recVel, satVel)
[p, pdot] = pseudoranges(____Name,Value)
```

Description

p = pseudoranges (recPos, satPos) returns the pseudoranges between the receiver at position recPos and the satellites at positions satPos.

```
[p, pdot] = pseudoranges(___, recVel, satVel) returns the pseudorange rates pdot between the receiver and satellites. Use this syntax with the input arguments in the previous syntax.
```

[p, pdot] = pseudoranges(___Name,Value) specifies the measurement noise for the ranges
and range rates using name-value arguments. For example, [p pdot] =
pseudoranges(__,'RangeAccuracy',2) sets the measurement noise in pseudoranges, specified
as a scalar standard deviation in meters.

Examples

Get Satellite Pseudoranges for Receiver Position and Velocity

Use the pseudoranges function to get the pseudorange and pseudorange rate for given satellite and receiver positions and velocities. Get the satellte positions and velocities using the gnssconstellation function.

Specify a receiver position in geodetic coordinates (latitude, longitude, altitude) and receiver velocity in the local navigation frame.

```
recPos = [42 -71 50];
recVel = [1 2 3];

Get the satellite positions for the current time.

t = datetime('now');
[gpsSatPos,gpsSatVel] = gnssconstellation(t);

Get the the pseudoranges and pseudorange rates between the receiver and satellites.
[p,pdot] = pseudoranges(recPos,gpsSatPos,recVel,gpsSatVel);
```

Input Arguments

```
recPos — Receiver position
three-element vector of the form [lat lon alt]
```

Receiver position in geodetic coordinates, specified as a three-element vector of the form [latitude longitude altitude]

Data Types: single | double

satPos — Satellite positions

N-by-3 matrix of scalars

Satellite positions in the Earth-centered Earth-fixed (ECEF) coordinate system in meters, specified as an *N*-by-3 matrix of scalars. *N* is the number of satellites in the constellation.

Data Types: single | double

recVel — Receiver velocity

three-element vector of the form [vx vy vz]

Receiver velocity in the local navigation frame using north-east-down (NED) coordinates, specified as a three-element vector of the form [vx vy vz].

Data Types: single | double

satVel — Satellite velocities

N-by-3 matrix of scalars

Satellite velocities in the Earth-centered Earth-fixed (ECEF) coordinate system in meters per second, specified as an N-by-3 matrix of scalars. N is the number of satellites in the constellation.

Data Types: single | double

Name-Value Pair Arguments

Specify optional comma-separated pairs of Name, Value arguments. Name is the argument name and Value is the corresponding value. Name must appear inside quotes. You can specify several name and value pair arguments in any order as Name1, Value1, . . . , NameN, ValueN.

Example: 'RangeAccuracy', '0.5' sets the measurement noise of the pseudoranges to 0.5 meters.

RangeAccuracy — Measurement noise in pseudoranges

1 (default) | scalar

Measurement noise in pseudoranges, specified as a scalar standard deviation in meters.

Data Types: single | double

RangeRateAccuracy — Measurement noise in pseudorange rates

0.02 (default) | scalar

Measurement noise in pseudorange rates, specified as a scalar standard deviation in meters per second.

Data Types: single | double

Output Arguments

p — Pseudoranges between satellites and receiver

n-element vector

Pseudoranges between the satellites and receiver, returned as an *n*-element vector in meters.

Data Types: single | double

pdot — Pseudorange rates between satellites and receiver

zeros(n,1) (default) | *n*-element vector

Pseudorange rates between the satellites and receiver, returned as an *n*-element vector in meters per second. If you do not provide velocity inputs, this output is zero.

Data Types: single | double

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

Objects

gnssSensor|gpsSensor|imuSensor

Functions

gnssconstellation|lookangles|receiverposition|skyplot

Introduced in R2021a

quat2axang

Convert quaternion to axis-angle rotation

Syntax

```
axang = quat2axang(quat)
```

Description

axang = quat2axang(quat) converts a quaternion, quat, to the equivalent axis-angle rotation, axang.

Examples

Convert Quaternion to Axis-Angle Rotation

Input Arguments

quat — Unit quaternion

n-by-4 matrix | n-element vector of quaternion objects

Unit quaternion, specified as an n-by-4 matrix or n-element vector of quaternion objects containing n quaternions. If the input is a matrix, each row is a quaternion vector of the form $q = [w \times y \ z]$, with w as the scalar number.

```
Example: [0.7071 0.7071 0 0]
```

Output Arguments

axang — Rotation given in axis-angle form

```
n-by-4 matrix
```

Rotation given in axis-angle form, returned as an n-by-4 matrix of n axis-angle rotations. The first three elements of every row specify the rotation axis, and the last element defines the rotation angle (in radians).

```
Example: [1 0 0 pi/2]
```

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder $^{\text{\tiny TM}}$.

See Also

axang2quat|quaternion

Introduced in R2015a

quat2eul

Convert quaternion to Euler angles

Syntax

```
eul = quat2eul(quat)
eul = quat2eul(quat,sequence)
```

Description

eul = quat2eul(quat) converts a quaternion rotation, quat, to the corresponding Euler angles, eul. The default order for Euler angle rotations is "ZYX".

eul = quat2eul(quat, sequence) converts a quaternion into Euler angles. The Euler angles are specified in the axis rotation sequence, sequence. The default order for Euler angle rotations is "ZYX".

Examples

Convert Quaternion to Euler Angles

```
quat = [0.7071 \ 0.7071 \ 0 \ 0]; eulZYX = quat2eul(quat) eulZYX = 1 \times 3 0 \ 0 \ 1.5708
```

Convert Quaternion to Euler Angles Using ZYZ Axis Order

Input Arguments

quat — Unit quaternion

n-by-4 matrix | n-element vector of quaternion objects

Unit quaternion, specified as an n-by-4 matrix or n-element vector of quaternion objects containing n quaternions. If the input is a matrix, each row is a quaternion vector of the form $q = [w \ x \ y \ z]$, with w as the scalar number.

Example: [0.7071 0.7071 0 0]

sequence — Axis rotation sequence

"ZYX" (default) | "ZYZ" | "XYZ"

Axis rotation sequence for the Euler angles, specified as one of these string scalars:

- "ZYX" (default) The order of rotation angles is *z*-axis, *y*-axis, *x*-axis.
- "ZYZ" The order of rotation angles is *z*-axis, *y*-axis, *z*-axis.
- "XYZ" The order of rotation angles is *x*-axis, *y*-axis, *z*-axis.

Data Types: string | char

Output Arguments

eul — Euler rotation angles

n-by-3 matrix

Euler rotation angles in radians, returned as an *n*-by-3 array of Euler rotation angles. Each row represents one Euler angle set.

Example: [0 0 1.5708]

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

eul2quat | quaternion

Introduced in R2015a

quat2rotm

Convert quaternion to rotation matrix

Syntax

```
rotm = quat2rotm(quat)
```

Description

rotm = quat2rotm(quat) converts a quaternion quat to an orthonormal rotation matrix, rotm.
When using the rotation matrix, premultiply it with the coordinates to be rotated (as opposed to
postmultiplying).

Examples

Convert Quaternion to Rotation Matrix

Input Arguments

quat — Unit quaternion

n-by-4 matrix | n-element vector of quaternion objects

Unit quaternion, specified as an n-by-4 matrix or n-element vector of objects containing n quaternions. If the input is a matrix, each row is a quaternion vector of the form $q = [w \ x \ y \ z]$, with w as the scalar number.

```
Example: [0.7071 0.7071 0 0]
```

Output Arguments

rotm — Rotation matrix

```
3-by-3-by-n matrix
```

Rotation matrix, returned as a 3-by-3-by-n matrix containing n rotation matrices. Each rotation matrix has a size of 3-by-3 and is orthonormal. When using the rotation matrix, premultiply it with the coordinates to be rotated (as opposed to postmultiplying).

```
Example: [0 0 1; 0 1 0; -1 0 0]
```

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder $^{\text{\tiny TM}}$.

See Also

quaternion|rotm2quat

Introduced in R2015a

quat2tform

Convert quaternion to homogeneous transformation

Syntax

```
tform = quat2tform(quat)
```

Description

tform = quat2tform(quat) converts a quaternion, quat, to a homogeneous transformation matrix, tform. When using the transformation matrix, premultiply it with the coordinates to be transformed (as opposed to postmultiplying).

Examples

Convert Quaternion to Homogeneous Transformation

Input Arguments

quat — Unit quaternion

n-by-4 matrix | n-element vector of quaternion objects

Unit quaternion, specified as an n-by-4 matrix or n-element vector of quaternion objects containing n quaternions. If the input is a matrix, each row is a quaternion vector of the form $q = [w \times y \ z]$, with w as the scalar number.

```
Example: [0.7071 0.7071 0 0]
```

Output Arguments

${\bf tform-Homogeneous\ transformation}$

```
4-by-4-by-n matrix
```

Homogeneous transformation matrix, returned as a 4-by-4-by-n matrix of n homogeneous transformations. When using the rotation matrix, premultiply it with the coordinates to be rotated (as opposed to postmultiplying).

```
Example: [0 0 1 0; 0 1 0 0; -1 0 0 0; 0 0 0 1]
```

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder $^{\text{\tiny TM}}$.

See Also

quaternion|tform2quat

Introduced in R2015a

read

Read data from GPS receiver

Syntax

```
[tt,overrun] = read(gps0bj)
[lla,groundSpeed,course, dops,gpsReceiverTime,timestamp, overrun] = read(gps0bj)
```

Description

[tt,overrun] = read(gps0bj) returns the GPS readings in timetable format. This is a non blocking read which returns N datapoints in timetable format where N is specified by SamplesPerRead and timetable is specified using OutputFormat property of gpsdev object.

[lla,groundSpeed,course, dops,gpsReceiverTime,timestamp, overrun] = read(gpsObj) returns matrices of measurements from the GPS. This is a non blocking read which returns N data points in matrix format where N is specified by SamplesPerRead and matrix is specified using OutputFormat property of the gpsdev object.

Examples

Read Data from GPS as a timetable

Create GPS object with properties available.

```
g = gpsdev('COM4','OutputFormat','timetable','SamplesPerRead',2)
Read samples of GPS.
[tt,overruns] = read(g)
```

tt =

2×5 timetable

Time		LLA		GroundSpeed	Course	DO	
31-Jan-2020 11:32:49.459 31-Jan-2020 11:32:50.416	12.944 12.944	77.692 77.692	806.8	0.0463 0.12861	258.87 262.7	1.31	0

```
overrun =
```

Display the time at which GPS data is read, in duration format.

```
g.TimeFormat = "duration";
[tt,overruns] = read(g)
```

```
tt =
 2×5 timetable
```

Time	LLA			GroundSpeed	Course	DOPs		
9.4257 sec	12.944	77.692	808.4	0.030867	4.93	1.51	0.78	1.29
10.404 sec	12.944	77.692	808.4	0.051444	41.26	1.1	0.76	0.79

overrun =

0

Read Data from GPS as a Matrix

Create GPS object with properties available.

```
g = gpsdev('COM4', "OutputFormat", "matrix", 'SamplesPerRead',2);
```

Read samples of GPS data.

[lla,speed,course,dops,gpsReceiverTime,timestamp,overruns] = read(g)

```
lla =
  12.9437
            77.6916 807.4000
  12.9437
          77.6916 807.4000
speed =
   0.0154
   0.0463
course =
 346.0100
 270.2100
dops =
   1.2400
           0.9200 0.8300
   1.7700
             0.9900 1.4700
gpsReceiverTime =
 2×1 datetime array
  31-Jan-2020 06:07:01.000
  31-Jan-2020 06:07:02.000
```

timestamp =

```
2×1 datetime array
31-Jan-2020 11:37:01.734
31-Jan-2020 11:37:02.436

overruns =
0
```

Input Arguments

gps0bj — GPS object

gpsdev object

The GPS object with the default or specified properties.

Output Arguments

tt — Data read as timetable

Data read from the GPS receiver when the output format is set to timetable. The timetable returned has the following fields:

- LLA (Latitude, Longitude, Altitude)
- Ground Speed
- Course over ground
- Dilution of Precisions(DOPs), VDOP, HDOP, PDOP,
- GPS Receiver Time
- Time System time when the data is read, in datetime or duration format

Data Types: timetable

lla — Position in LLA coordinate system

N-by-3

Position of the GPS receiver in the geodetic latitude, longitude, and altitude (LLA), returned as a real finite N-by-3 array. Latitude and longitude are in degrees with North and East being positive. Altitude is in meters.

Data Types: double

groundSpeed - Speed in m/s

N-by-1

Speed over ground, returned as a real finite N-by-1 column vector.

Data Types: double

course - Course over ground

N-by-1

Course over ground relative to true north, returned as a real finite N-by-1 column of values between 0 and 2pi radians.

Data Types: double

dops — Dilution of precisions

N-by-3

Dilution of precisions, returned as a real finite N-by-3 array. The order of the output is [PDOP, HDOP, VDOP].

Data Types: double

gpsReceiverTime — UTC time

N-by-1

UTC time returned by the GPS module.

Data Types: datetime

timestamp — Time at which GPS data is read

N-by-1

Time at which GPS data is read, returned as a real finite N-by-1 column vector. This is the system time. If the TimeFormat is datetime, the timestamp will be datetime. If the TimeFormat is a duration, the timestamp will be duration

- datetime Displays the date and time at which the data is read.
- duration Displays the time elapsed in seconds after the first call of the read function or the last execution of the release function.

Note If the SamplesPerRead is greater than 1, an extrapolation is done on the time value. Hence it might not be precise.

Data Types: datetime | duration

overrun - Overrun

The number of samples lost between consecutive calls to read. The overrun is zero when ReadMode is set to oldest.

Data Types: double

More About

read Output

The gpsdev object expects GPRMC, GPGGA, and GPGSA sentences as outputs from the GPS receiver to get the required values. The read function errors out if these sentences are not available.

The read function outputs NaN and NaT in the following situations:

• If the GPS module does not receive valid data because there is no satellite lock or when GPS does not give a particular value.

• If there is a checksum failure, corresponding data points will be NaN for numeric outputs (lla, speed, course, dops) and NaT for gpsRecieverTime. lla is taken from GPGGA sentence, speed,course, and gpsRecieverTime is taken GPRMC sentence and dops are taken from GPGSA sentence.

Because read function is non blocking, the following is expected:

• If no new data is available, the output of read is the previous data. For example, if the delay between subsequent reads is less than the UpdateRate of the GPS receiver.

Because GPS data is validated in the first read operation, it might take more time compared to the subsequent read operations.

See Also

Objects

Introduced in R2020b

readBinaryOccupancyGrid

Read binary occupancy grid

Syntax

```
map = readBinaryOccupancyGrid(msg)
map = readBinaryOccupancyGrid(msg,thresh)
map = readBinaryOccupancyGrid(msg,thresh,val)
```

Description

map = readBinaryOccupancyGrid(msg) returns a binaryOccupancyMap object by reading the data inside a ROS message, msg, which must be a 'nav_msgs/OccupancyGrid' message. All message data values greater than or equal to the occupancy threshold are set to occupied, 1, in the map. All other values, including unknown values (-1) are set to unoccupied, 0, in the map.

Note The msg input is an 'nav_msgs/OccupancyGrid' ROS message. For more info, see OccupancyGrid.

map = readBinaryOccupancyGrid(msg,thresh) specifies a threshold, thresh, for occupied values. All values greater than or equal to the threshold are set to occupied, 1. All other values are set to unoccupied, 0.

map = readBinaryOccupancyGrid(msg,thresh,val) specifies a value to set for unknown values (-1). By default, all unknown values are set to unoccupied, 0.

Input Arguments

msg — 'nav_msgs/OccupancyGrid' ROS message

OccupancyGrid object handle

'nav_msgs/OccupancyGrid' ROS message, specified as a OccupancyGrid object handle.

thresh — Threshold for occupied values

50 (default) | scalar

Threshold for occupied values, specified as a scalar. Any value greater than or equal to the threshold is set to occupied, 1. All other values are set to unoccupied, 0.

Data Types: double

val — Value to replace unknown values

0 (default) | 1

Value to replace unknown values, specified as either 0 or 1. Unknown message values (-1) are set to the given value.

Data Types: double | logical

Output Arguments

map — Binary occupancy grid

binaryOccupancyMap object handle

Binary occupancy grid, returned as a binaryOccupancyMap object handle. map is converted from a 'nav_msgs/OccupancyGrid' message on the ROS network. The object is a grid of binary values, where 1 indicates an occupied location and 0 indications an unoccupied location.

See Also

Objects

OccupancyGrid | binaryOccupancyMap | occupancyMap

Functions

readOccupancyGrid|writeBinaryOccupancyGrid|writeOccupancyGrid

Introduced in R2015a

readOccupancyGrid

Read occupancy grid message

Syntax

map = readOccupancyGrid(msg)

Description

map = readOccupancyGrid(msg) returns an occupancyMap object by reading the data inside a ROS message, msg, which must be a 'nav_msgs/OccupancyGrid' message. All message data values are converted to probabilities from 0 to 1. The unknown values (-1) in the message are set as 0.5 in the map.

Note The msg input is an 'nav_msgs/OccupancyGrid' ROS message. For more info, see OccupancyGrid.

Input Arguments

msg — 'nav msgs/OccupancyGrid' ROS message

OccupancyGrid object handle

'nav_msgs/OccupancyGrid' ROS message, specified as an OccupancyGrid ROS message object handle.

Output Arguments

map — Occupancy map

occupancyMap object handle

Occupancy map, returned as an occupancyMap object handle.

See Also

Functions

rosReadBinaryOccupancyGrid | rosReadOccupancyMap3D | rosWriteBinaryOccupancyGrid | rosWriteOccupancyGrid

Introduced in R2016b

readOccupancyMap3D

Read 3-D map from Octomap ROS message

Syntax

map = rosReadOccupancyMap3D(msg)

Description

map = rosReadOccupancyMap3D(msg) reads the data inside a ROS 'octomap_msgs/Octomap'
message to return an occupancyMap3D object. All message data values are converted to
probabilities from 0 to 1.

Input Arguments

msg — Octomap ROS message

structure

Octomap ROS message, specified as a structure of message type 'octomap_msgs/Octomap'. Get this message by subscribing to an 'octomap_msgs/Octomap' topic using rossubscriber on a live ROS network or by creating your own message using rosmessage.

Output Arguments

map — 3-D occupancy map

occupancyMap3D object handle

3-D occupancy map, returned as an occupancyMap3D object handle.

See Also

occupancyMap3D | rosmessage | rossubscriber

Introduced in R2021a

receiverposition

Estimate GNSS receiver position and velocity

Syntax

```
recPos = receiverposition(p,satPos)
[recPos,recVel] = receiverposition(____,pdot,satVel)
[recPos,recVel,hdop,vdop] = receiverposition(____)
```

Description

recPos = receiverposition(p,satPos) returns the receiver position estimated from the pseudoranges and satellite positions.

[recPos,recVel] = receiverposition(____,pdot,satVel) also returns the receiver velocity estimated from the pseudorange rates pdot and satellite velocities satVel.

[recPos,recVel,hdop,vdop] = receiverposition(____) also returns the horizontal dilation of precision hdop and vertical dilation of precision vdop associated with the position estimate.

Examples

Estimate Receiver Position from Pseudoranges and Satellite Positions

Use the receiverposition function to estimate a GNSS receiver position. Get the satellte positions and velocities using the gnssconstellation function. Generate pseudoranges from these positions using the pseudoranges function.

Specify a receiver position in geodetic coordinates (latitude, longitude, altitude) and a receiver velocity in the local navigation frame.

```
recPos = [42 -71 50];
recVel = [1 2 3];
```

Get the satellite positions for the current time.

```
t = datetime('now');
[gpsSatPos,gpsSatVel] = gnssconstellation(t);
```

Get the the pseudoranges and pseudorange rates between the GNSS receiver and the satellites.

```
[p,pdot] = pseudoranges(recPos,qpsSatPos,recVel,qpsSatVel);
```

Use the pseudoranges to estimate the receiver position and velocity. The values close to your original receiver position and velocity used to generate the satellite position and pseudoranges.

```
[lla,gnssVel] = receiverposition(p,gpsSatPos,pdot,gpsSatVel) 
 lla = 1 \times 3
```

```
42.0000 -71.0000 	 49.6568
gnssVel = 1 \times 3
1.0078 	 1.9987 	 3.0127
```

Input Arguments

p — Pseudoranges between satellites and receiver

n-element vector

Pseudoranges between the satellites and receiver, specified as an n-element vector in meters.

Data Types: single | double

satPos — Satellite positions

N-by-3 matrix of scalars

Satellite positions in the Earth-centered Earth-fixed (ECEF) coordinate system in meters, specified as an N-by-3 matrix of scalars. N is the number of satellites in the constellation.

Data Types: single | double

pdot — Pseudorange rates between satellites and receiver

n-element vector

Pseudorange rates between the satellites and receiver, specified as an *n*-element vector in meters per second.

Data Types: single | double

satVel — Velocity readings in local navigation coordinate system (m/s)

N-by-3 matrix of scalar

Velocity readings of the GNSS receiver in the local navigation coordinate system in meters per second, specified as an N-by-3 matrix of scalars. N is the number of satellites in the constellation.

Data Types: single | double

Output Arguments

recPos — Receiver position

three-element vector of the form [lat lon alt]

Receiver position in geodetic coordinates, returned as a three-element vector of the form [latitude longitude altitude]

Data Types: single | double

recVel — Receiver velocity

three-element vector of the form [vx vy vz]

Receiver velocity in the local navigation frame using north-east-down (NED) coordinates, returned as a three-element vector of the form $[vx\ vy\ vz]$.

Data Types: single | double

hdop — Horizontal dilation of precision

scalar

Horizontal dilation of precision, returned as a scalar.

Data Types: double

vdop — Vertical dilation of precision

scalar

Vertical dilation of precision, returned as a scalar.

Data Types: double

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

Objects

gnssSensor|gpsSensor|imuSensor

Functions

gnssconstellation | lookangles | pseudoranges | skyplot

Introduced in R2021a

release

Release the GPS object

Syntax

release(gpsdev)

Description

release(gpsdev) release the system objects, allows configuration of non tunable properties, clear the buffers, and sets SamplesRead and SamplesAvailable as 0.

Input Arguments

gpsdev — GPS sensor object

The GPS sensor object with the default or specified properties.

See Also

Introduced in R2020b

removelnvalidData

Remove invalid range and angle data

Syntax

```
validScan = removeInvalidData(scan)
validScan = removeInvalidData(scan, Name, Value)
```

Description

validScan = removeInvalidData(scan)returns a new lidarScan object with all Inf and NaN
values from the input scan removed. The corresponding angle readings are also removed.

validScan = removeInvalidData(scan, Name, Value) provides additional options specified by
one or more Name, Value pairs.

Examples

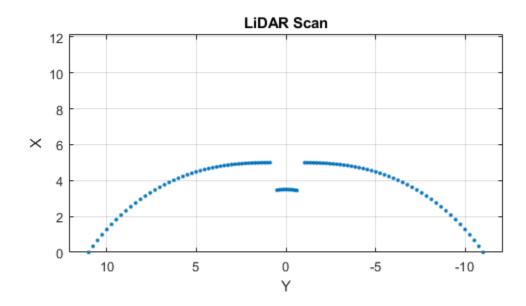
Plot Lidar Scan and Remove Invalid Points

Specify lidar data as vectors of ranges and angles. These values include readings outside of the sensors range.

```
x = linspace(-2,2);
ranges = abs((1.5).*x.^2 + 5);
ranges(45:55) = 3.5;
angles = linspace(-pi/2,pi/2,numel(ranges));
```

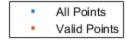
Create a lidar scan by specifying the ranges and angles. Plot all points of the lidar scan.

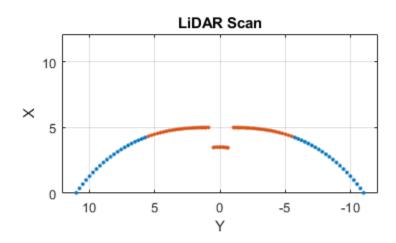
```
scan = lidarScan(ranges,angles);
plot(scan)
```



Remove invalid points based on a specified minimum and maximum range.

```
minRange = 0.1;
maxRange = 7;
scan2 = removeInvalidData(scan, 'RangeLimits', [minRange maxRange]);
hold on
plot(scan2)
legend('All Points', 'Valid Points')
```





Input Arguments

scan — Lidar scan readings

lidarScan object

Lidar scan readings, specified as a lidarScan object.

Name-Value Pair Arguments

Specify optional comma-separated pairs of Name, Value arguments. Name is the argument name and Value is the corresponding value. Name must appear inside quotes. You can specify several name and value pair arguments in any order as Name1, Value1, . . . , NameN, ValueN.

Example: ["RangeLimits",[0.05 2]

RangeLimits — Range reading limits

two-element vector

Range reading limits, specified as a two-element vector, [minRange maxRange], in meters. All range readings and corresponding angles outside these range limits are removed

Data Types: single | double

AngleLimits — Angle limits

two-element vector

Angle limits, specified as a two-element vector, [minAngle maxAngle] in radians. All angles and corresponding range readings outside these angle limits are removed.

Angles are measured counter-clockwise around the positivez-axis.

Data Types: single | double

Output Arguments

validScan — Lidar scan readings

lidarScan object

Lidar scan readings, specified as a lidarScan object. All invalid lidar scan readings are removed.

See Also

lidarScan | matchScans | transformScan

Introduced in R2019b

rotm2axang

Convert rotation matrix to axis-angle rotation

Syntax

```
axang = rotm2axang(rotm)
```

Description

axang = rotm2axang(rotm) converts a rotation given as an orthonormal rotation matrix, rotm, to
the corresponding axis-angle representation, axang. The input rotation matrix must be in the
premultiply form for rotations.

Examples

Convert Rotation Matrix to Axis-Angle Rotation

```
rotm = [1 0 0; 0 -1 0; 0 0 -1]; axang = rotm2axang(rotm) axang = 1 \times 4
1.0000 0 0 3.1416
```

Input Arguments

rotm — Rotation matrix

3-by-3-by-n matrix

Rotation matrix, specified as a 3-by-3-by-n matrix containing n rotation matrices. Each rotation matrix has a size of 3-by-3 and must be orthonormal. The input rotation matrix must be in the premultiply form for rotations.

Note Rotation matrices that are slightly non-orthonormal can give complex outputs. Consider validating your matrix before inputting to the function.

```
Example: [0 0 1; 0 1 0; -1 0 0]
```

Output Arguments

axang — Rotation given in axis-angle form

n-by-4 matrix

Rotation given in axis-angle form, returned as an n-by-4 matrix of n axis-angle rotations. The first three elements of every row specify the rotation axis, and the last element defines the rotation angle (in radians).

Example: [1 0 0 pi/2]

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder $^{\text{\tiny TM}}$.

See Also

axang2rotm

Introduced in R2015a

rotm2eul

Convert rotation matrix to Euler angles

Syntax

```
eul = rotm2eul(rotm)
eul = rotm2eul(rotm, sequence)
```

Description

eul = rotm2eul(rotm) converts a rotation matrix, rotm, to the corresponding Euler angles, eul. The input rotation matrix must be in the premultiply form for rotations. The default order for Euler angle rotations is "ZYX".

eul = rotm2eul(rotm, sequence) converts a rotation matrix to Euler angles. The Euler angles are specified in the axis rotation sequence, sequence. The default order for Euler angle rotations is "ZYX".

Examples

Convert Rotation Matrix to Euler Angles

```
rotm = [0 \ 0 \ 1; \ 0 \ 1 \ 0; \ -1 \ 0 \ 0];
eulZYX = rotm2eul(rotm)
eulZYX = 1 \times 3
           (-)
                 1.5708
                                    (-)
```

Convert Rotation Matrix to Euler Angles Using ZYZ Axis Order

```
rotm = [0 \ 0 \ 1; \ 0 \ -1 \ 0; \ -1 \ 0 \ 0];
eulZYZ = rotm2eul(rotm,'ZYZ')
eulZYZ = 1 \times 3
   -3.1416 -1.5708 -3.1416
```

Input Arguments

```
rotm — Rotation matrix
```

3-by-3-by-*n* matrix

Rotation matrix, specified as a 3-by-3-by-n matrix containing n rotation matrices. Each rotation matrix has a size of 3-by-3 and is orthonormal. The input rotation matrix must be in the premultiply form for rotations.

Note Rotation matrices that are slightly non-orthonormal can give complex outputs. Consider validating your matrix before inputting to the function.

Example: [0 0 1; 0 1 0; -1 0 0]

sequence — Axis rotation sequence

"ZYX" (default) | "ZYZ" | "XYZ"

Axis rotation sequence for the Euler angles, specified as one of these string scalars:

- "ZYX" (default) The order of rotation angles is *z*-axis, *y*-axis, *x*-axis.
- "ZYZ" The order of rotation angles is *z*-axis, *y*-axis, *z*-axis.
- "XYZ" The order of rotation angles is *x*-axis, *y*-axis, *z*-axis.

Data Types: string | char

Output Arguments

eul — Euler rotation angles

n-by-3 matrix

Euler rotation angles in radians, returned as an n-by-3 array of Euler rotation angles. Each row represents one Euler angle set.

Example: [0 0 1.5708]

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

eul2rotm

Introduced in R2015a

rotm2quat

Convert rotation matrix to quaternion

Syntax

```
quat = rotm2quat(rotm)
```

Description

quat = rotm2quat(rotm) converts a rotation matrix, rotm, to the corresponding unit quaternion
representation, quat. The input rotation matrix must be in the premultiply form for rotations.

Examples

Convert Rotation Matrix to Quaternion

```
rotm = [0 \ 0 \ 1; \ 0 \ 1 \ 0; \ -1 \ 0 \ 0];

quat = rotm2quat(rotm)

quat = 1 \times 4

0.7071 0 0.7071 0
```

Input Arguments

rotm — Rotation matrix

3-by-3-by-*n* matrix

Rotation matrix, specified as a 3-by-3-by-n matrix containing n rotation matrices. Each rotation matrix has a size of 3-by-3 and is orthonormal. The input rotation matrix must be in the premultiply form for rotations.

Note Rotation matrices that are slightly non-orthonormal can give complex outputs. Consider validating your matrix before inputting to the function.

```
Example: [0 0 1; 0 1 0; -1 0 0]
```

Output Arguments

quat — Unit quaternion

```
n-by-4 matrix
```

Unit quaternion, returned as an *n*-by-4 matrix containing *n* quaternions. Each quaternion, one per row, is of the form $q = [w \times y z]$, with w as the scalar number.

Example: [0.7071 0.7071 0 0]

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder $^{\text{\tiny TM}}$.

See Also

quat2rotm

Introduced in R2015a

rotm2tform

Convert rotation matrix to homogeneous transformation

Syntax

```
tform = rotm2tform(rotm)
```

Description

tform = rotm2tform(rotm) converts the rotation matrix, rotm, into a homogeneous transformation matrix, tform. The input rotation matrix must be in the premultiply form for rotations. When using the transformation matrix, premultiply it with the coordinates to be transformed (as opposed to postmultiplying).

Examples

Convert Rotation Matrix to Homogeneous Transformation

```
rotm = [1 0 0 ; 0 -1 0; 0 0 -1];

tform = rotm2tform(rotm)

tform = 4×4

1 0 0 0

0 -1 0 0

0 0 -1 0

0 0 1
```

Input Arguments

rotm — Rotation matrix

```
3-by-3-by-n matrix
```

Rotation matrix, specified as a 3-by-3-by-n matrix containing n rotation matrices. Each rotation matrix has a size of 3-by-3 and is orthonormal. The input rotation matrix must be in the premultiply form for rotations.

Note Rotation matrices that are slightly non-orthonormal can give complex outputs. Consider validating your matrix before inputting to the function.

```
Example: [0 0 1; 0 1 0; -1 0 0]
```

Output Arguments

tform — Homogeneous transformation

4-by-4-by-*n* matrix

Homogeneous transformation matrix, specified by a 4-by-4-by-n matrix of n homogeneous transformations. When using the rotation matrix, premultiply it with the coordinates to be rotated (as opposed to postmultiplying).

Example: [0 0 1 0; 0 1 0 0; -1 0 0 0; 0 0 0 1]

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

tform2rotm

Introduced in R2015a

show

Visualize path segment

Syntax

```
show(pathSeg)
show(pathSeg,Name,Value)
```

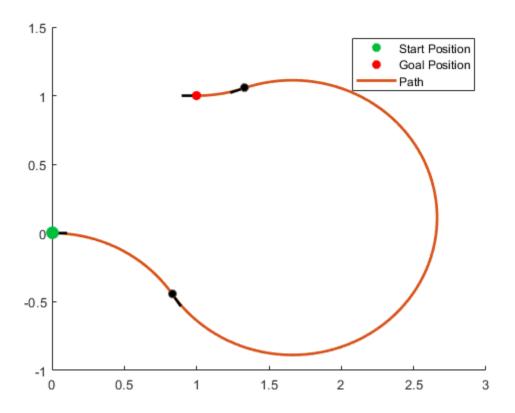
Description

show(pathSeg) plots the path segment with start and goal positions and their headings.
show(pathSeg,Name,Value) also specifies Name,Value pairs to control display settings.

Examples

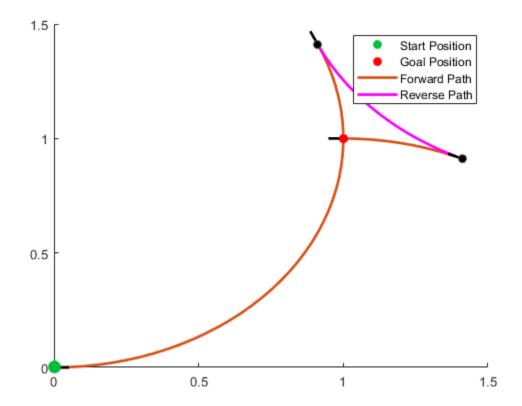
Connect Poses Using Dubins Connection Path

```
Create a dubinsConnection object.
dubConnObj = dubinsConnection;
Define start and goal poses as [x y theta] vectors.
startPose = [0 0 0];
goalPose = [1 1 pi];
Calculate a valid path segment to connect the poses.
[pathSegObj, pathCosts] = connect(dubConnObj,startPose,goalPose);
Show the generated path.
show(pathSegObj{1})
```



Modify Connection Types for Reeds-Shepp Path

```
Create a reedsSheppConnection object.
reedsConnObj = reedsSheppConnection;
Define start and goal poses as [x y theta] vectors.
startPose = [0 0 0];
goalPose = [1 1 pi];
Calculate a valid path segment to connect the poses.
[pathSegObj,pathCosts] = connect(reedsConnObj,startPose,goalPose);
Show the generated path. Notice the direction of the turns.
show(pathSegObj{1})
```



pathSegObj{1}.MotionTypes

```
ans = 1x5 cell
   {'L'} {'R'} {'L'}
                         {'N'} {'N'}
```

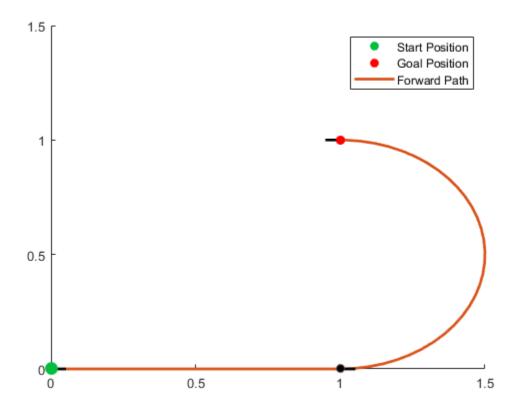
pathSegObj{1}.MotionDirections

```
ans = 1 \times 5
    1 -1 1 1
                        1
```

Disable this specific motion sequence in a new connection object. Reduce the MinTurningRadius if the robot is more maneuverable. Increase the reverse cost to reduce the likelihood of reverse directions being used. Connect the poses again to get a different path.

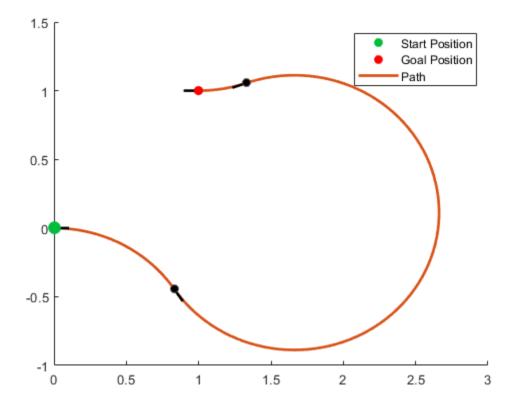
```
reedsConnObj = reedsSheppConnection('DisabledPathTypes',{'LpRnLp'});
reedsConnObj.MinTurningRadius = 0.5;
reedsConnObj.ReverseCost = 5;
[pathSegObj,pathCosts] = connect(reedsConnObj,startPose,goalPose);
pathSegObj{1}.MotionTypes
ans = 1x5 cell
   {'L'} {'S'} {'L'} {'N'} {'N'}
```

```
show(pathSeg0bj{1})
xlim([0 1.5])
ylim([0 1.5])
```



Interpolate Poses For Dubins Path

```
Create a dubinsConnection object.
dubConnObj = dubinsConnection;
Define start and goal poses as [x y theta] vectors.
startPose = [0 0 0];
goalPose = [1 1 pi];
Calculate a valid path segment to connect the poses.
[pathSegObj,pathCosts] = connect(dubConnObj,startPose,goalPose);
Show the generated path.
show(pathSegObj{1})
```

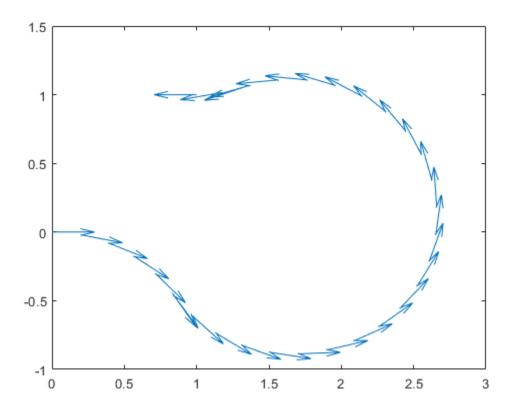


Interpolate poses along the path. Get a pose every 0.2 meters, including the transitions between turns.

```
length = pathSegObj{1}.Length;
poses = interpolate(pathSegObj{1},0:0.2:length)
poses = 32 \times 3
         0
                    0
                               0
    0.1987
             -0.0199
                         6.0832
    0.3894
             -0.0789
                         5.8832
    0.5646
             -0.1747
                         5.6832
    0.7174
             -0.3033
                         5.4832
    0.8309
             -0.4436
                         5.3024
    0.8418
             -0.4595
                         5.3216
    0.9718
             -0.6110
                         5.5216
    1.1293
             -0.7337
                         5.7216
    1.3081
             -0.8226
                         5.9216
```

Use the quiver function to plot these poses.

```
quiver(poses(:,1),poses(:,2),cos(poses(:,3)),sin(poses(:,3)),0.5)
```



Input Arguments

pathSeg — Path segment

dubinsPathSegment object | reedsSheppPathSegment object

Path segment, specified as a dubinsPathSegment or reedsSheppPathSegment object.

Name-Value Pair Arguments

Specify optional comma-separated pairs of Name, Value arguments. Name is the argument name and Value is the corresponding value. Name must appear inside quotes. You can specify several name and value pair arguments in any order as Name1, Value1, . . . , NameN, ValueN.

Example: 'Headings', { 'transitions' }

Parent — Axes to plot path onto

Axes handle

Axes to plot path onto, specified as an Axes handle.

Headings — **Heading angles to display**

cell array of character vector or string scalars

Heading angles to display, specified as a cell array of character vector or string scalars. Options are any combination of 'start', 'goal', and 'transitions'. To disable all heading displays, specify {''}.

Positions — Positions to display

'both' (default) | 'start' | 'goal' | 'none'

Positions to display, specified as 'both', 'start', 'goal', or 'none'. The start position is marked with green, and the goal position is marked with red.

HeadingLength — Length of heading

positive numeric scalar

Length of heading, specified as positive numeric scalar. By default the value is calculated according to the x- and y-axis limits of the plot.

Data Types: double

See Also

Functions

connect | interpolate

Objects

dubinsConnection | dubinsPathSegment | reedsSheppConnection |
reedsSheppPathSegment

Introduced in R2019b

skyplot

Plot satellite azimuth and elevation data

Syntax

```
skyplot(azdata,eldata)
skyplot(azdata,eldata,labeldata)
skyplot(status)
skyplot(____,Name,Value)

skyplot(parent,____)
h = skyplot(____)
```

Description

skyplot(azdata,eldata) creates a sky plot using the azimuth and elevation data specified as vectors in degrees. Azimuth angles are measured in degrees, clockwise-positive from the North direction. Elevation angles are measured from the horizon line with 90 degrees being directly up. For details about the sky plot figure elements, see "Main Sky Plot Elements" on page 1-173.

skyplot(azdata,eldata,labeldata) specifies data labels as a string array with elements corresponding to each data point in the azdata and eldata inputs.

skyplot(status) specifies the azimuth and elevation data in a structure with fields SatelliteAzimuth and SatelliteElevation.

skyplot(____, Name, Value) specifies options using one or more name-value arguments in addition to the input arguments in previous syntaxes. The name-value arguments are properties of the SkyPlotChart object. For a list of properties, see SkyPlotChart Properties.

skyplot(parent, ____) creates the sky plot in the figure, panel, or tab specified by parent.

h = skyplot(____) returns the sky plot as a SkyPlotChart object, h. Use h to modify the properties of the chart after creating it. For a list of properties, see SkyPlotChart Properties.

Examples

View Satellite Positions from GNSS Sensor

Create a GNSS sensor model as a gnssSensor System Object™.

```
gnss = gnssSensor;
```

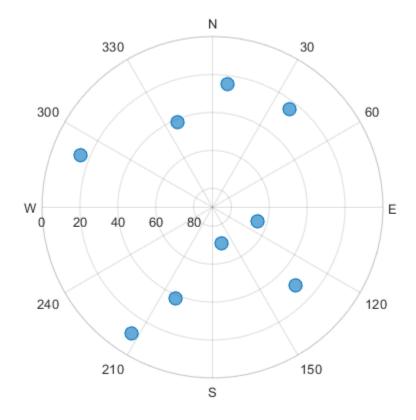
Specify the position and velocity of the sensor. Simulate the sensor readings and get status from visible satellites. Store the azimuth and elevation angles as vectors.

```
pos = [0 0 0];
vel = [0 0 0];
[~, ~, status] = gnss(pos, vel);
```

```
satAz = status.SatelliteAzimuth;
satEl = status.SatelliteElevation;
```

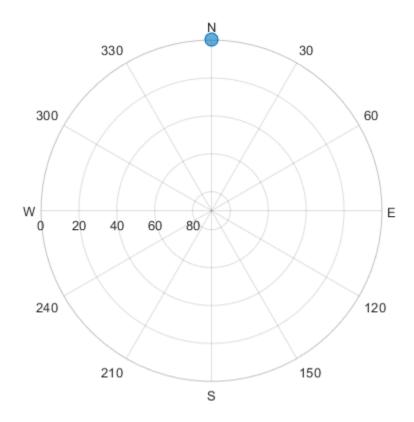
Plot the satellite postions.

skyplot(satAz,satEl)



Plot Series of Satellite Positions Over Time

Animate the trajectory of satellite positions over time from a GNSS sensor. Initialize the sky plot figure. Specify the relevant time-stepping information. skyplotHandle = skyplot(0,0);



```
numHours = 12;
dt = 100;
numSeconds = numHours * 60 * 60;
numSimSteps = numSeconds/dt;
```

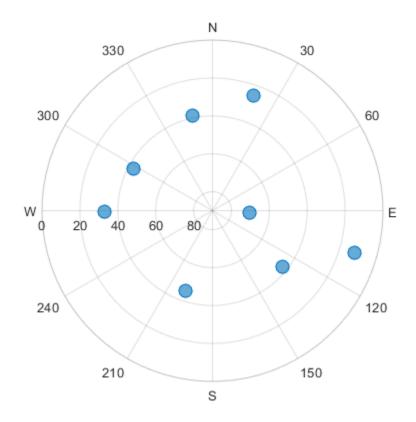
Create a GNSS sensor model as a gnssSensor System Object™.

```
gnss = gnssSensor('SampleRate', 1/dt);
```

Iterate through the time steps and do the following:

- Simulate the sensor readings. Specify the zero postion and velocity for the stationary sensor.
- Store the azimuth and elevation angles as vectors.
- Set the AzimuthData and ElevationData properties of the SkyPlotChart handle directly.

```
for i = 1:numSimSteps
   [~, ~, status] = gnss([0 0 0],[0 0 0]);
   satAz = status.SatelliteAzimuth;
   satEl = status.SatelliteElevation;
   set(skyplotHandle,'AzimuthData',satAz,'ElevationData',satEl);
   drawnow
end
```



View Satellite Positions For Different Groups

Load the azimuth and elevation data from a logfile generated by an Adafruit® GPS satellite sensor. The data provided in this example contains the azimuth and elevation of each satellite and the pseudorandom noise (PRN) codes. Store these values as vectors.

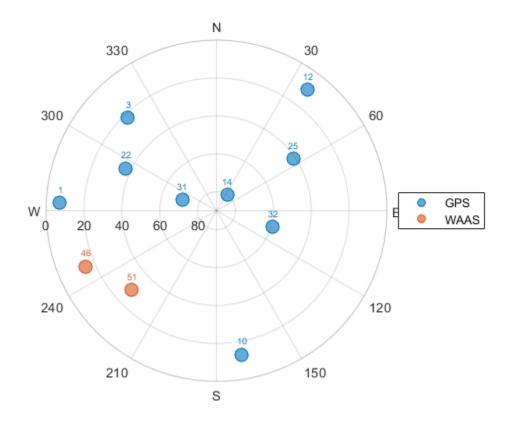
```
load('gpsHWInfo','hwInfo')
satAz = hwInfo.SatelliteAzimuths;
satEl = hwInfo.SatelliteElevations;
prn = hwInfo.SatellitePRNs;
```

Separate the satellites based on the PRN codes. To correlate each position with a group, create a categorical array. PRNs greater than 32 are part of the wide area augmentation system (WAAS).

```
isWAAS = (prn > 32);
constellationGroup = categorical(isWAAS,[false,true],{'GPS','WAAS'});
```

Visualize the satellites and specify the categorical groups in the GroupData name-value argument. Specify the PRN as the label for each point. Show the legend.

```
skyplot(satAz,satEl,prn,'GroupData',constellationGroup)
legend('GPS','WAAS')
```



Input Arguments

azdata — Azimuth angles for visible satellite positions

n-element vector of angles

Azimuth angles for visible satellite positions, specified as an n-element vector of angles. n is the number of visible satellite positions in the plot. Azimuth angles are measured in degrees, clockwise-positive from the North direction.

Example: [25 45 182 356]

Data Types: double

eldata — Elevation angles for visible satellite positions

n-element vector of angles

Elevation angles for visible satellite positions, specified as an n-element vector of angles. n is the number of visible satellite positions in the plot. Elevation angles are measured from the horizon line with 90 degrees being directly up.

Example: [45 90 27 74]

Data Types: double

labeldata — Labels for visible satellite positions

n-element string array

Labels for visible satellite positions, specified as an n-element string array. n is the number of visible satellite positions in the plot.

```
Example: ["G1" "G11" "G7" "G3"]
Data Types: string
```

status — Satellite status

structure array

Satellite status, specified as a structure array with fields SatelliteAzimuth and SatelliteElevation. Typically, this status structure comes from a gnssSensor object, which simulates satellite positions and velocities.

```
Example: gnss = gnssSensor; [\sim, \sim, status] = gnss(position, velocity)
Data Types: struct
```

parent — Parent container

Figure object | Panel object | Tab object | TiledChartLayout object | GridLayout object

Parent container, specified as a Figure, Panel, Tab, TiledChartLayout, or GridLayout object.

Output Arguments

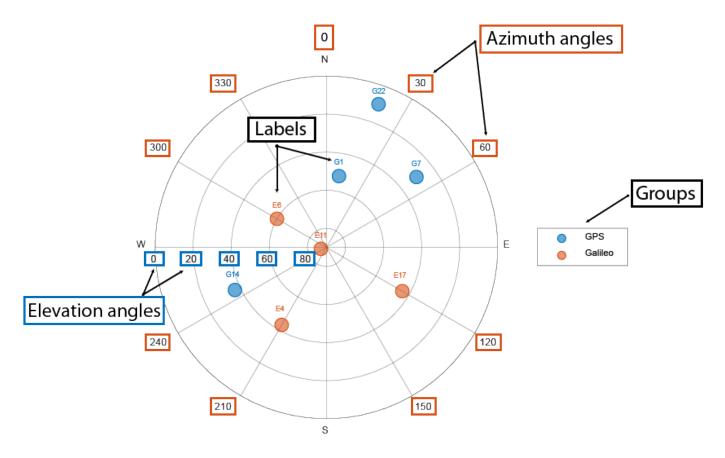
h — Sky plot chart

SkyplotChart object

Sky plot chart, returned as a SkyplotChart object, which is a standalone visualization on page 1-173. Use h to set properties on the sky plot chart. For more information, see SkyPlotChart Properties.

More About

Main Sky Plot Elements



The main elements of the figure are:

- Azimuth axes Specified by the azdata input argument, azimuth angle positions are measured clockwise-positive from the North direction.
- Elevation axes —Specified by the eldata input argument, elevation angle positions are measured from the horizon line with 90 degrees being directly up.
- Labels Specified by the labeldata input argument as a string array with an element for each point in the azdata and eldata vectors.
- Groups Specified by the GroupData property, a categorical array defines the group for each satellite position.

Standalone Visualization

A standalone visualization is a chart designed for a special purpose that works independently from other charts. Unlike other charts such as plot and surf, a standalone visualization has a preconfigured axes object built into it, and some customizations are not available. A standalone visualization also has these characteristics:

 It cannot be combined with other graphics elements, such as lines, patches, or surfaces. Thus, the hold command is not supported.

- The gca function can return the chart object as the current axes.
- You can pass the chart object to many MATLAB functions that accept an axes object as an input argument. For example, you can pass the chart object to the title function.

See Also

Functions

polarscatter

Properties

SkyPlotChart Properties

Objects

gnssSensor|nmeaParser

Introduced in R2021a

tform2axang

Convert homogeneous transformation to axis-angle rotation

Syntax

```
axang = tform2axang(tform)
```

Description

axang = tform2axang(tform) converts the rotational component of a homogeneous
transformation, tform, to an axis-angle rotation, axang. The translational components of tform are
ignored. The input homogeneous transformation must be in the premultiply form for transformations.

Examples

Convert Homogeneous Transformation to Axis-Angle Rotation

```
tform = [1 0 0 0; 0 0 -1 0; 0 1 0 0; 0 0 0 1]; axang = tform2axang(tform) axang = 1 \times 4
1.0000 0 0 1.5708
```

Input Arguments

tform — Homogeneous transformation

```
4-by-4-by-n matrix
```

Homogeneous transformation, specified by a 4-by-4-by-n matrix of n homogeneous transformations. The input homogeneous transformation must be in the premultiply form for transformations.

```
Example: [0 0 1 0; 0 1 0 0; -1 0 0 0; 0 0 0 1]
```

Output Arguments

axang — Rotation given in axis-angle form

```
n-by-4 matrix
```

Rotation given in axis-angle form, specified as an n-by-4 matrix of n axis-angle rotations. The first three elements of every row specify the rotation axes, and the last element defines the rotation angle (in radians).

```
Example: [1 0 0 pi/2]
```

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder $^{\text{\tiny TM}}$.

See Also

axang2tform

Introduced in R2015a

tform2eul

Extract Euler angles from homogeneous transformation

Syntax

```
eul = tform2eul(tform)
eul = tform2eul(tform, sequence)
```

Description

eul = tform2eul(tform) extracts the rotational component from a homogeneous transformation, tform, and returns it as Euler angles, eul. The translational components of tform are ignored. The input homogeneous transformation must be in the premultiply form for transformations. The default order for Euler angle rotations is "ZYX".

eul = tform2eul(tform, sequence) extracts the Euler angles, eul, from a homogeneous
transformation, tform, using the specified rotation sequence, sequence. The default order for Euler
angle rotations is "ZYX".

Examples

Extract Euler Angles from Homogeneous Transformation Matrix

```
tform = [1 0 0 0.5; 0 -1 0 5; 0 0 -1 -1.2; 0 0 0 1]; eulZYX = tform2eul(tform) eulZYX = 1 \times 3 0 0 3.1416
```

Extract Euler Angles from Homogeneous Transformation Matrix Using ZYZ Rotation

```
tform = [1 0 0 0.5; 0 -1 0 5; 0 0 -1 -1.2; 0 0 0 1];
eulZYZ = tform2eul(tform, 'ZYZ')
eulZYZ = 1 \times 3
0 -3.1416 3.1416
```

Input Arguments

tform — Homogeneous transformation

4-by-4-by-*n* matrix

Homogeneous transformation, specified by a 4-by-4-by-n matrix of n homogeneous transformations. The input homogeneous transformation must be in the premultiply form for transformations.

Example: [0 0 1 0; 0 1 0 0; -1 0 0 0; 0 0 0 1]

sequence — Axis rotation sequence

"ZYX" (default) | "ZYZ" | "XYZ"

Axis rotation sequence for the Euler angles, specified as one of these string scalars:

- "ZYX" (default) The order of rotation angles is *z*-axis, *y*-axis, *x*-axis.
- "ZYZ" The order of rotation angles is z-axis, y-axis, z-axis.
- "XYZ" The order of rotation angles is x-axis, y-axis, z-axis.

Data Types: string | char

Output Arguments

eul — Euler rotation angles

n-by-3 matrix

Euler rotation angles in radians, returned as an n-by-3 array of Euler rotation angles. Each row represents one Euler angle set.

Example: [0 0 1.5708]

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

eul2tform

Introduced in R2015a

tform2quat

Extract quaternion from homogeneous transformation

Syntax

```
quat = tform2quat(tform)
```

Description

quat = tform2quat(tform) extracts the rotational component from a homogeneous
transformation, tform, and returns it as a quaternion, quat. The translational components of tform
are ignored. The input homogeneous transformation must be in the premultiply form for
transformations.

Examples

Extract Quaternion from Homogeneous Transformation

```
tform = [1 0 0 0; 0 -1 0 0; 0 0 -1 0; 0 0 0 1]; 
quat = tform2quat(tform) 
quat = 1 \times 4
```

Input Arguments

tform — Homogeneous transformation

```
4-by-4-by-n matrix
```

Homogeneous transformation, specified by a 4-by-4-by-n matrix of n homogeneous transformations. The input homogeneous transformation must be in the premultiply form for transformations.

```
Example: [0 0 1 0; 0 1 0 0; -1 0 0 0; 0 0 0 1]
```

Output Arguments

quat — Unit quaternion

```
n-by-4 matrix
```

Unit quaternion, returned as an *n*-by-4 matrix containing *n* quaternions. Each quaternion, one per row, is of the form $q = [w \times v z]$, with *w* as the scalar number.

```
Example: [0.7071 0.7071 0 0]
```

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder $^{\text{\tiny TM}}$.

See Also

quat2tform

Introduced in R2015a

tform2rotm

Extract rotation matrix from homogeneous transformation

Syntax

```
rotm = tform2rotm(tform)
```

Description

rotm = tform2rotm(tform) extracts the rotational component from a homogeneous
transformation, tform, and returns it as an orthonormal rotation matrix, rotm. The translational
components of tform are ignored. The input homogeneous transformation must be in the premultiply form for transformations. When using the rotation matrix, premultiply it with the coordinates
to be rotated (as opposed to postmultiplying).

Examples

Convert Homogeneous Transformation to Rotation Matrix

Input Arguments

tform — Homogeneous transformation

4-by-4-by-*n* matrix

Homogeneous transformation matrix, specified by a 4-by-4-by-n matrix of n homogeneous transformations. The input homogeneous transformation must be in the pre-multiply form for transformations.

```
Example: [0 0 1 0; 0 1 0 0; -1 0 0 0; 0 0 0 1]
```

Output Arguments

rotm — Rotation matrix

3-by-3-by-n matrix

Rotation matrix, returned as a 3-by-3-by-n matrix containing n rotation matrices. Each rotation matrix has a size of 3-by-3 and is orthonormal. When using the rotation matrix, premultiply it with the coordinates to be rotated (as opposed to postmultiplying).

Example: [0 0 1; 0 1 0; -1 0 0]

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder $^{\text{\tiny TM}}$.

See Also

rotm2tform

Introduced in R2015a

tform2trvec

Extract translation vector from homogeneous transformation

Syntax

```
trvec = tform2trvec(tform)
```

Description

trvec = tform2trvec(tform) extracts the Cartesian representation of translation vector, trvec, from a homogeneous transformation, tform. The rotational components of tform are ignored. The input homogeneous transformation must be in the premultiply form for transformations.

Examples

Extract Translation Vector from Homogeneous Transformation

```
tform = [1 0 0 0.5; 0 -1 0 5; 0 0 -1 -1.2; 0 0 0 1];

trvec = tform2trvec(tform)

trvec = 1 \times 3

0.5000 5.0000 -1.2000
```

Input Arguments

tform — Homogeneous transformation

```
4-by-4-by-n matrix
```

Homogeneous transformation, specified by a 4-by-4-by-n matrix of n homogeneous transformations. The input homogeneous transformation must be in the premultiply form for transformations.

```
Example: [0 0 1 0; 0 1 0 0; -1 0 0 0; 0 0 0 1]
```

Output Arguments

trvec — Cartesian representation of a translation vector

n-by-3 matrix

Cartesian representation of a translation vector, returned as an n-by-3 matrix containing n translation vectors. Each vector is of the form $t = [x \ y \ z]$.

```
Example: [0.5 6 100]
```

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder $^{\text{\tiny TM}}$.

See Also

trvec2tform

Introduced in R2015a

transformMotion

Compute motion quantities between two relatively fixed frames

Syntax

[posS,ori	<pre>entS,velS,accS,angvelS] = transformMotion(posSFromP,orientSFromP)</pre>
posP)	
[] = -	transformMotion(posSFromP,orientSFromP,posP,orientP)
[] = -	transformMotion(posSFromP,orientSFromP,posP,orientP,velP)
[] = -	transformMotion(posSFromP,orientSFromP,posP,orientP,velP,accP)
$[\] = $	transformMotion(posSFromP,orientSFromP,posP,orientP,velP,accP,
angvelP)	

Description

[posS,orientS,velS,accS,angvelS] = transformMotion(posSFromP,orientSFromP, posP) computes motion quantities of the sensor frame relative to the navigation frame (posS, orientS, velS, accS, and angvelS) using the position of sensor frame relative to the platform frame, posSFromP, the orientation of the sensor frame relative to the platform frame, orientSFromP, and the position of the platform frame relative to the navigation frame, posP. Note that the position and orientation between the sensor frame and the platform frame are assumed to be fixed. Also, the unspecified quantities between the navigation frame and the platform frame (such as orientation, velocity, and acceleration) are assumed to be zero.

[] = transformMotion(posSfromP,orientSfromP,posP,orientP) additionally specific	ıes
the orientation of the platform frame relative to the navigation frame, orientP. The output	
arguments are the same as those of the previous syntax.	

[___] = transformMotion(posSFromP,orientSFromP,posP,orientP,velP) additionally specifies the velocity of the platform frame relative to the navigation frame, velP. The output arguments are the same as those of the previous syntax.

```
[ ____ ] = transformMotion(posSFromP,orientSFromP,posP,orientP,velP,accP) additionally specifies the acceleration of the platform frame relative to the navigation frame, accP. The output arguments are the same as those of the previous syntax.
```

[____] = transformMotion(posSFromP, orientSFromP, posP, orientP, velP, accP, angvelP) additionally specifies the angular velocity of the platform frame relative to the navigation frame, angvelP. The output arguments are the same as those of the previous syntax.

Examples

Transform State to Sensor Frame

Define the pose, velocity, and acceleration of the platform frame relative to the navigation frame.

```
posPlat = [20 -1 0];
orientPlat = quaternion(1, 0, 0, 0);
velPlat = [0 0 0];
```

 $accPlat = [0 \ 0 \ 0];$

```
angvelPlat = [0 \ 0 \ 1];
Define the position and orientation offset of IMU sensor frame relative to the platform frame.
posPlat2IMU = [1 2 3];
orientPlat2IMU = quaternion([45 0 0], 'eulerd', 'ZYX', 'frame');
Calculate the motion quantities of the sensor frame relative to the navigation frame and print the
results.
[posIMU, orientIMU, velIMU, accIMU, angvelIMU] ...
    = transformMotion(posPlat2IMU, orientPlat2IMU,
    posPlat, orientPlat, velPlat, accPlat, angvelPlat);
fprintf('IMU position is:\n');
IMU position is:
fprintf('%.2f %.2f %.2f\n', posIMU);
21.00 1.00 3.00
orientIMU
orientIMU = quaternion
     0.92388 + 0i +
                            0j + 0.38268k
velIMU
velIMU = 1×3
    - 2
          1
                  0
accPlat
accPlat = 1 \times 3
           0
                  0
```

Input Arguments

posSFromP — Position of sensor frame relative to platform frame

1-by-3 vector of real scalars

Position of the sensor frame relative to the platform frame, specified as a 1-by-3 vector of real scalars.

```
Example: [1 2 3]
```

orientSFromP — Orientation of sensor frame relative to platform frame

```
quaternion | 3-by-3 rotation matrix
```

Orientation of the sensor frame relative to the platform frame, specified as a quaternion or a 3-by-3 rotation matrix.

Example: quaternion(1,0,0,0)

posP — Position of platform frame relative to navigation frame

N-by-3 matrix of real scalars

Position of platform frame relative to navigation frame, specified as an N-by-3 matrix of real scalars. N is the number of position quantities.

Example: [1 2 3]

orientP — Orientation of platform frame relative to navigation frame

N-by-1 array of quaternion | 3-by-3-by-*N* array of scalars

Orientation of platform frame relative to navigation frame, specified as an N-by-1 array of quaternions, or a 3-by-3-by-N array of scalars. Each 3-by-3 matrix must be a rotation matrix. N is the number of orientation quantities.

Example: quaternion(1,0,0,0)

velP — Velocity of platform frame relative to navigation frame

N-by-3 matrix of real scalars

Velocity of platform frame relative to navigation frame, specified as an N-by-3 matrix of real scalars. N is the number of velocity quantities.

Example: [4 8 6]

accP — Acceleration of platform frame relative to navigation frame

N-by-3 matrix of real scalars

Acceleration of platform frame relative to navigation frame, specified as an N-by-3 matrix of real scalars. N is the number of acceleration quantities.

Example: [4 8 6]

angvelP — Angular velocity of platform frame relative to navigation frame

N-by-3 matrix of real scalars

Angular velocity of platform frame relative to navigation frame, specified as an N-by-3 matrix of real scalars. N is the number of angular velocity quantities.

Example: [4 2 3]

Output Arguments

posS — Position of sensor frame relative to navigation frame

N-by-3 matrix of real scalars

Position of sensor frame relative to navigation frame, returned as an N-by-3 matrix of real scalars. N is the number of position quantities specified by the posP input.

orientS — Orientation of sensor frame relative to navigation frame

N-by-1 array of quaternion | 3-by-3-by-*N* array of scalars

Orientation of sensor frame relative to navigation frame, returned as an N-by-1 array of quaternions, or a 3-by-3-by-N array of scalars. N is the number of orientation quantities specified by the orientP input. The returned orientation quantity type is same with the orientP input.

velS — Velocity of sensor frame relative to navigation frame

N-by-3 matrix of real scalars

Velocity of sensor frame relative to navigation frame, returned as an N-by-3 matrix of real scalars. N is the number of position quantities specified by the velP input.

accS — Acceleration of sensor frame relative to navigation frame

N-by-3 matrix of real scalars

Acceleration of sensor frame relative to navigation frame, returned as an N-by-3 matrix of real scalars. N is the number of position quantities specified by the accP input.

angvelS — Angular velocity of sensor frame relative to navigation frame

N-by-3 matrix of real scalars

Angular velocity of sensor frame relative to navigation frame, returned as an N-by-3 matrix of real scalars. N is the number of position quantities specified by the anguelP input.

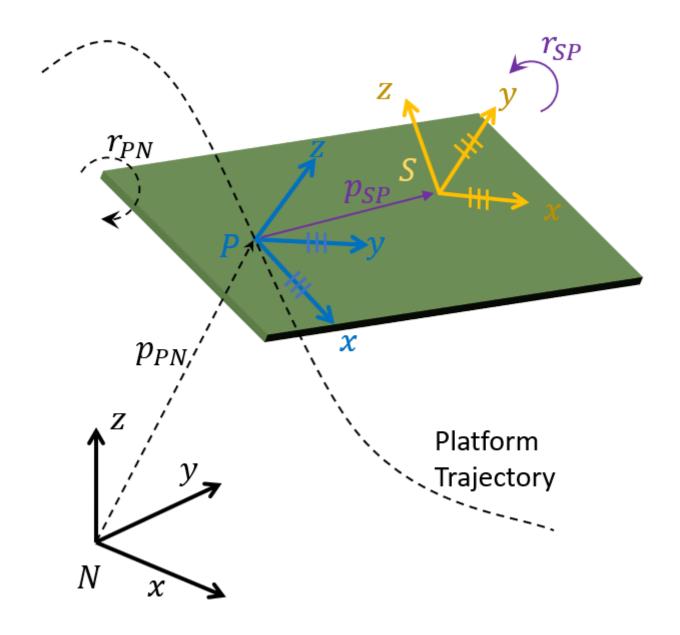
More About

Motion Quantities Used in transformMotion

The transformMotion function calculates the motion quantities of the sensor frame (S), which is fixed on a rigid platform, relative to the navigation frame (N) using the mounting information of the sensor on the platform and the motion information of the platform frame (P).

As shown in the figure, the position and orientation of the platform frame and the sensor frame are fixed on the platform. The position of the sensor frame relative to the platform frame is p_{SP} , and the orientation of the sensor frame relative to the platform frame is r_{SP} . Since the two frames are both fixed, p_{SP} and r_{SP} are constant.

To compute the motion quantities of the sensor frame relative to the navigation frame, the quantities describing the motion of the platform frame relative to the navigation frame are required. These quantities include: the platform position (p_{PN}) , orientation (r_{PN}) , velocity, acceleration, angular velocity, and angular acceleration relative to the navigation frame. You can specify these quantities through the function input arguments except the angular acceleration, which is always assumed to be zero in the function. The unspecified quantities are also assumed to be zero.



See Also quaternion | rotvec

Introduced in R2020a

transformScan

Transform laser scan based on relative pose

Syntax

```
transScan = transformScan(scan, relPose)
[transRanges, transAngles] = transformScan(ranges, angles, relPose)
```

Description

transScan = transformScan(scan, relPose) transforms the laser scan specified in scan by using the specified relative pose, relPose.

[transRanges, transAngles] = transformScan(ranges, angles, relPose) transforms the laser scan specified in ranges and angles by using the specified relative pose, relPose.

Examples

Transform Laser Scans

Create a lidarScan object. Specify the ranges and angles as vectors.

```
refRanges = 5*ones(1,300);
refAngles = linspace(-pi/2,pi/2,300);
refScan = lidarScan(refRanges,refAngles);

Translate the laser scan by an [x y] offset of (0.5,0.2).

transformedScan = transformScan(refScan,[0.5 0.2 0]);

Rotate the laser scan by 20 degrees.

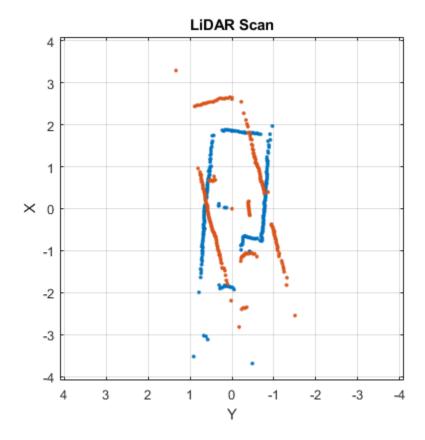
rotateScan = transformScan(refScan,[0,0,deg2rad(20)]);
```

Use Scan Matching to Transform Scans

Use the matchScans function to find the relative transformation between two lidar scans. Then, transform the second scan into the coordinate frame of the first scan.

Load a pair of lidar scans as a pair of lidarScan objects. They are two scans of the same scene with a change in relative pose.

```
load tb3_scanPair.mat
plot(s1)
hold on
plot(s2)
hold off
```



The relative pose is estimated from an odometry sensor and provided as a variable, initGuess, as [x y theta].

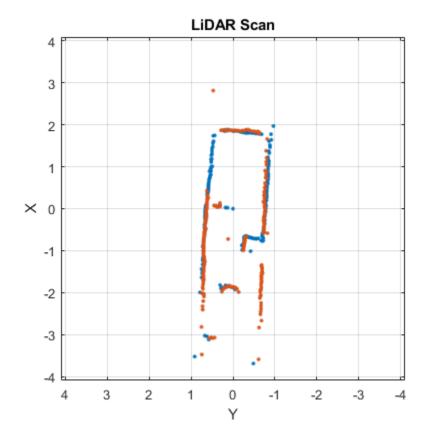
```
disp(initGuess)
  -0.7000   0.1500   -0.3254
```

Use scan matching to find the relative pose between the two laser scans and specify the initial guess for the pose.

```
pose = matchScans(s2,s1,"InitialPose",initGuess);
disp(pose)
    -0.7213     0.1160     -0.2854
```

Transform the second scan to the coordinate frame of the first scan. Plot the two scans to see that they now overlap.

```
s2Transformed = transformScan(s2,pose);
plot(s1)
hold on
plot(s2Transformed)
hold off
```



Input Arguments

scan — Lidar scan readings

lidarScan object

Lidar scan readings, specified as a lidarScan object.

ranges — Range values from scan data

vector

Range values from scan data, specified as a vector in meters. These range values are distances from a sensor at specified angles. The vector must be the same length as the corresponding angles vector.

angles — Angle values from scan data

vector

Angle values from scan data, specified as a vector in radians. These angle values are the specific angles of the specified ranges. The vector must be the same length as the corresponding ranges vector.

relPose — Relative pose of current scan

[x y theta]

Relative pose of current scan, specified as [x y theta], where [x y] is the translation in meters and theta is the rotation in radians.

Output Arguments

transScan — Transformed lidar scan readings

lidarScan object

Transformed lidar scan readings, specified as a lidarScan object.

transRanges — Range values of transformed scan

vector

Range values of transformed scan, returned as a vector in meters. These range values are distances from a sensor at specified transAngles. The vector is the same length as the corresponding transAngles vector.

transAngles — Angle values from scan data

vector

Angle values of transformed scan, returned as a vector in radians. These angle values are the specific angles of the specified transRanges. The vector is the same length as the corresponding ranges vector.

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

controllerVFH | matchScans | monteCarloLocalization | transformScan

Topics

"Estimate Robot Pose with Scan Matching"

Introduced in R2017a

trimLoopClosures

Optimize pose graph and remove bad loop closures

Syntax

poseGraphUpdated = trimLoopClosures(poseGraphObj,trimParams,solverOptions)
[poseGraphUpdated,trimInfo] = trimLoopClosures(poseGraphObj,trimParams,solverOptions)

Description

poseGraphUpdated = trimLoopClosures(poseGraphObj,trimParams,solverOptions)
optimizes the pose graph to best satisfy the edge constrains and removes any bad loop closure edges
based on the residual error parameters specified in trimParams. Create the solverOptions input
using the poseGraphSolverOptions function.

The function implements the graduated non-convexity (GNC) method with truncated least squares (TLS) robust cost in combination with the non-minimal pose graph solver [1] on page 1-200.

[poseGraphUpdated,trimInfo] = trimLoopClosures(poseGraphObj,trimParams, solverOptions) returns additional information related to the trimming process.

Examples

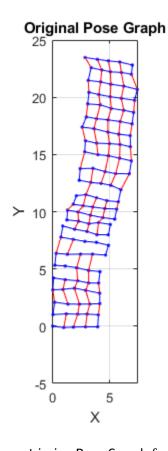
Optimize and Trim Loop Closures For 2-D Pose Graphs

Optimize a pose graph based on the nodes and edge constraints. Trim loop closed based on their edge residual errors.

Load the data set that contains a 2-D pose graph. Inspect the poseGraph object to view the number of nodes and loop closures.

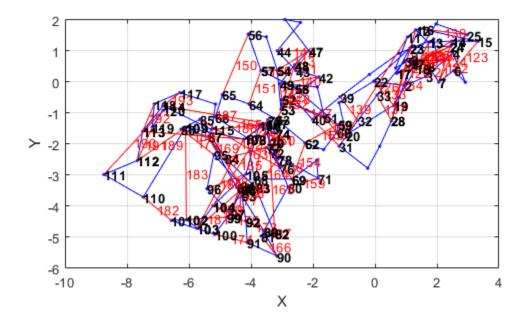
Plot the pose graph with IDs off. Red lines indicate loop closures identified in the dataset. The poses in the graph should follow a grid pattern, but show evidence of drift over time.

```
show(pg,'IDs','off');
title('Original Pose Graph')
```



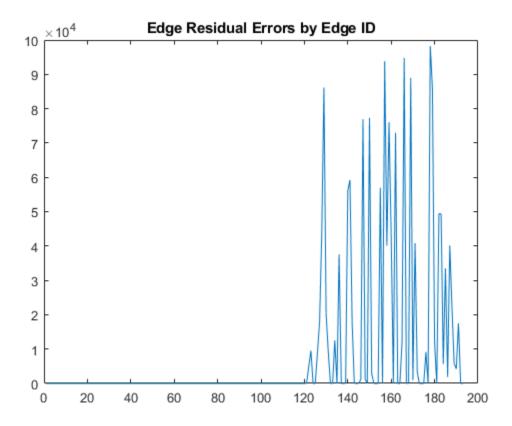
Optimize the pose grap using the optimizePoseGraph function. By default, this function uses the "builtin-trust-region" solver. Because the pose graph contains some bad loop closures, the resulting pose graph is actual not desirable.

```
pgOptim = optimizePoseGraph(pg);
figure;
show(pgOptim);
```



Look at the edge residual errors for the original pose graph. Large outlier error values at the end indicate bad loop closures.

```
resErrorVec = edgeResidualErrors(pg);
plot(resErrorVec);
title('Edge Residual Errors by Edge ID')
```



Certain loop closures should be trimmed from the pose graph based on their residual error. Use the trimLoopClosures function to trim therse bad loop closures. Set the maximum and truncation threshold for the trimmer parameters. This threshold is set based on the measurement accuracy and should be tuned for your system.

```
trimParams.MaxIterations = 100;
trimParams.TruncationThreshold = 25;
solverOptions = poseGraphSolverOptions;
```

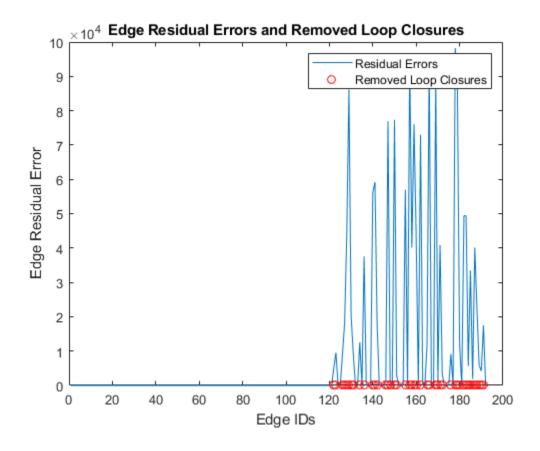
Use the trimLoopClosures function with the trimmer parameters and solver options.

```
[pgNew, trimInfo, debugInfo] = trimLoopClosures(pg,trimParams,solverOptions);
```

From the trimInfo output, plot the loop closures removed from the optimized pose graph. By plotting with the residual errors plot before, you can see the large error loop closures were removed.

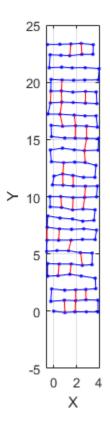
removedLCs = trimInfo.LoopClosuresToRemove;

```
hold on
plot(removedLCs,zeros(length(removedLCs)),'or')
title('Edge Residual Errors and Removed Loop Closures')
legend('Residual Errors', 'Removed Loop Closures')
xlabel('Edge IDs')
ylabel('Edge Residual Error')
hold off
```



Show the new pose graph with the bad loop closures trimmed.

show(pgNew,"IDs","off");



Input Arguments

poseGraphObj - Pose graph

poseGraph object | poseGraph3D object

Pose graph, specified as a poseGraph or poseGraph3D object.

trimParams — Residual error parameters for trimming structure

Residual error parameters for trimming loop closures, specified as a structure with fields:

- MaxIterations Maximum number of iterations allowed for loop closure trimming, specified as a positive integer. In one trimming iteration, the pose graph is optimized based on the solver options and any edges outside the TruncationThreshold are trimmed.
- TruncationThreshold Maximum allowed residual error for an edge. This value depends heavily on the pose graph you specify in poseGraphObj. To find a proper threshold based on all the errors, use the edgeResidualErrors function for the pose graph.

Example: struct('MaxIterations',10,'TruncationThreshold',20)

Data Types: struct

solverOptions — Pose graph solver options

poseGraphSolverOptions parameters

Pose graph solver options, specified as a set of parameters generated by calling the poseGraphSolverOptions function. The function generates a set of solver options with default values for the specified pose graph solver type:

```
pgSolverTrustRegion = poseGraphSolverOptions('builtin-trust-region')
pgSolverTrustRegion =
TrustRegion (builtin-trust-region-dogleg) options:
               MaxIterations: 300
                     MaxTime: 10
           FunctionTolerance: 1.0000e-08
           GradientTolerance: 5.0000e-09
               StepTolerance: 1.0000e-12
    InitialTrustRegionRadius: 100
               VerboseOutput: 'off'
pgSolverG2o = poseGraphSolverOptions('g2o-levenberg-marguardt')
pgSolverG2o =
G2oLevenbergMarguardt (g2o-levenberg-marguardt) options:
        MaxIterations: 300
             MaxTime: 10
    FunctionTolerance: 1.0000e-09
        VerboseOutput: 'off'
Modify the options to tune the solver parameters using dot notation.
pgSolverG2o.MaxIterations = 200;
```

Output Arguments

poseGraphUpdated — Pose graph with trimmed looped closures

poseGraph object | poseGraph3D object

Pose graph with trimmed looped closures, specified as a poseGraph or poseGraph3D object.

trimInfo — Information from trimming process

structure

Information from trimming process, returned as a structure with fields:

- LoopClosuresToRemove Loop closure edge IDs to remove from the input poseGraphObj. These loop closures are removed in the output poseGraphUpdated.
- Iterations Number of trimming iterations performed.

References

[1] Yang, Heng, et al. "Graduated Non-Convexity for Robust Spatial Perception: From Non-Minimal Solvers to Global Outlier Rejection." *IEEE Robotics and Automation Letters*, vol. 5, no. 2, Apr. 2020, pp. 1127–34. *DOI.org (Crossref)*, doi:10.1109/LRA.2020.2965893.

See Also

Functions

edgeConstraints|edgeResidualErrors|edges|poseGraphSolverOptions|removeEdges

Objects

lidarSLAM | poseGraph | poseGraph3D

Introduced in R2020b

trvec2tform

Convert translation vector to homogeneous transformation

Syntax

```
tform = trvec2tform(trvec)
```

Description

tform = trvec2tform(trvec) converts the Cartesian representation of a translation vector, trvec, to the corresponding homogeneous transformation, tform. When using the transformation matrix, premultiply it with the coordinates to be transformed (as opposed to postmultiplying).

Examples

Convert Translation Vector to Homogeneous Transformation

Input Arguments

trvec — Cartesian representation of a translation vector

n-by-3 matrix

Cartesian representation of a translation vector, specified as an n-by-3 matrix containing n translation vectors. Each vector is of the form $t = [x \ y \ z]$.

```
Example: [0.5 6 100]
```

Output Arguments

tform — Homogeneous transformation

```
4-by-4-by-n matrix
```

Homogeneous transformation matrix, returned as a 4-by-4-by-n matrix of n homogeneous transformations. When using the rotation matrix, premultiply it with the coordinates to be rotated (as opposed to postmultiplying).

```
Example: [0 0 1 0; 0 1 0 0; -1 0 0 0; 0 0 0 1]
```

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder $^{\text{\tiny TM}}$.

See Also

tform2trvec

Introduced in R2015a

tunernoise

Noise structure of fusion filter

Syntax

```
noiseStruct = tunernoise(filterName)
```

Description

noiseStruct = tunernoise(filterName) returns the measurement noise structure for the filter
with name specified by the filterName input.

Examples

Obtain Measurement Noise Structure of insfilterAsync

Obtain the measurement noise structure of the insfilterAsync object.

```
noiseStruct = tunernoise('insfilterAsync')
noiseStruct = struct with fields:
    AccelerometerNoise: 1
        GyroscopeNoise: 1
        MagnetometerNoise: 1
        GPSPositionNoise: 1
        GPSVelocityNoise: 1
```

Tune insfilterAsync to Optimize Pose Estimate

Load the recorded sensor data and ground truth data.

```
load('insfilterAsyncTuneData.mat');
```

Create timetables for the sensor data and the truth data.

```
sensorData = timetable(Accelerometer, Gyroscope, ...
    Magnetometer, GPSPosition, GPSVelocity, 'SampleRate', 100);
groundTruth = timetable(Orientation, Position, ...
    'SampleRate', 100);
```

Create an insfilterAsync filter object that has a few noise properties.

```
filter = insfilterAsync('State', initialState, ...
    'StateCovariance', initialStateCovariance, ...
    'AccelerometerBiasNoise', 1e-7, ...
    'GyroscopeBiasNoise', 1e-7, ...
    'MagnetometerBiasNoise', 1e-7, ...
    'GeomagneticVectorNoise', 1e-7);
```

Create a tuner configuration object for the filter. Set the maximum iterations to two. Also, set the tunable parameters as the unspecified properties.

Use the tuner noise function to obtain a set of initial sensor noises used in the filter.

```
measNoise = tunernoise('insfilterAsync')
measNoise = struct with fields:
    AccelerometerNoise: 1
        GyroscopeNoise: 1
        MagnetometerNoise: 1
        GPSPositionNoise: 1
        GPSVelocityNoise: 1
```

Tune the filter and obtain the tuned parameters.

tunedParams = tune(filter, measNoise, sensorData, groundTruth, config);

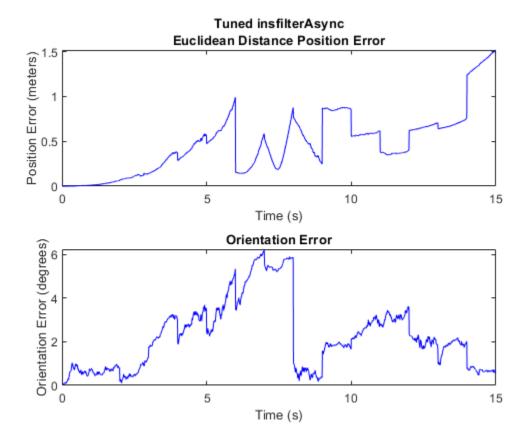
Iteration	Parameter	Metric
1	AccelerationNoise	2.1345
1	AccelerometerNoise	2.1264
1	AngularVelocityNoise	
1	GPSPositionNoise	1.9341
1	GPSVelocityNoise	1.8420
1	GyroscopeNoise	1.7589
1	MagnetometerNoise	1.7362
1	PositionNoise	1.7362
1	QuaternionNoise	1.7218
1	VelocityNoise	1.7218
2	AccelerationNoise	1.7190
2	AccelerometerNoise	1.7170
2	AngularVelocityNoise	1.6045
2	GPSPositionNoise	1.5948
2	GPSVelocityNoise	1.5323
2	GyroscopeNoise	1.4803
2	MagnetometerNoise	1.4703
2	PositionNoise	1.4703
2	QuaternionNoise	1.4632
2	VelocityNoise	1.4632
3	AccelerationNoise	1.4596
3	AccelerometerNoise	1.4548
3	AngularVelocityNoise	
3	GPSPositionNoise	1.3810
3	GPSVelocityNoise	1.3322
1 2 2 2 2 2 2 2 2 2 2 2 3 3 3 3 3 3 3	GyroscopeNoise	1.2998
3	MagnetometerNoise	1.2976
3	PositionNoise	1.2976

```
1.2943
             OuaternionNoise
3
             VelocityNoise
                                       1.2943
4
             AccelerationNoise
                                       1.2906
                                       1.2836
4
             AccelerometerNoise
4
             AngularVelocityNoise
                                       1.2491
4
             GPSPositionNoise
                                       1.2258
4
             GPSVelocityNoise
                                       1.1880
4
             GyroscopeNoise
                                       1.1701
4
             MagnetometerNoise
                                       1.1698
4
             PositionNoise
                                       1.1698
4
             QuaternionNoise
                                       1.1688
4
             VelocityNoise
                                       1.1688
5
             AccelerationNoise
                                       1.1650
5
                                       1.1569
             AccelerometerNoise
5
             AngularVelocityNoise
                                       1.1454
5
                                       1.1100
             GPSPositionNoise
5
                                       1.0778
             GPSVelocityNoise
5
             GyroscopeNoise
                                       1.0709
5
             MagnetometerNoise
                                       1.0675
5
                                       1.0675
             PositionNoise
5
             QuaternionNoise
                                       1.0669
5
                                       1.0669
             VelocityNoise
6
             AccelerationNoise
                                       1.0634
6
             AccelerometerNoise
                                       1.0549
                                       1.0549
6
             AngularVelocityNoise
6
             GPSPositionNoise
                                       1.0180
                                       0.9866
6
             GPSVelocityNoise
6
                                       0.9810
             GyroscopeNoise
6
             MagnetometerNoise
                                       0.9775
6
             PositionNoise
                                       0.9775
6
             QuaternionNoise
                                       0.9768
                                       0.9768
6
             VelocityNoise
7
             AccelerationNoise
                                       0.9735
7
             AccelerometerNoise
                                       0.9652
7
             AngularVelocityNoise
                                       0.9652
7
                                       0.9283
             GPSPositionNoise
7
                                       0.8997
             GPSVelocityNoise
7
             GyroscopeNoise
                                       0.8947
7
             MagnetometerNoise
                                       0.8920
7
             PositionNoise
                                       0.8920
7
             QuaternionNoise
                                       0.8912
7
             VelocityNoise
                                       0.8912
8
             AccelerationNoise
                                       0.8885
8
             AccelerometerNoise
                                       0.8811
8
             AngularVelocityNoise
                                       0.8807
8
             GPSPositionNoise
                                       0.8479
                                       0.8238
8
             GPSVelocityNoise
8
                                       0.8165
             GyroscopeNoise
8
             MagnetometerNoise
                                       0.8165
8
             PositionNoise
                                       0.8165
8
             QuaternionNoise
                                       0.8159
             VelocityNoise
                                       0.8159
```

Fuse the sensor data using the tuned filter.

```
dt = seconds(diff(groundTruth.Time));
N = size(sensorData,1);
qEst = quaternion.zeros(N,1);
```

```
posEst = zeros(N,3);
% Iterate the filter for prediction and correction using sensor data.
for ii=1:N
    if ii ~= 1
        predict(filter, dt(ii-1));
   end
    if all(~isnan(Accelerometer(ii,:)))
        fuseaccel(filter,Accelerometer(ii,:), ...
            tunedParams.AccelerometerNoise);
    end
    if all(~isnan(Gyroscope(ii,:)))
        fusegyro(filter, Gyroscope(ii,:), ...
            tunedParams.GyroscopeNoise);
    end
    if all(~isnan(Magnetometer(ii,1)))
        fusemag(filter, Magnetometer(ii,:), ...
            tunedParams.MagnetometerNoise);
    end
    if all(~isnan(GPSPosition(ii,1)))
        fuseqps(filter, GPSPosition(ii,:), ...
            tunedParams.GPSPositionNoise, GPSVelocity(ii,:), ...
            tunedParams.GPSVelocityNoise);
    [posEst(ii,:), qEst(ii,:)] = pose(filter);
end
Compute the RMS errors.
orientationError = rad2deg(dist(qEst, Orientation));
rmsorientationError = sqrt(mean(orientationError.^2))
rmsorientationError = 2.7801
positionError = sqrt(sum((posEst - Position).^2, 2));
rmspositionError = sqrt(mean( positionError.^2))
rmspositionError = 0.5966
Visualize the results.
figure();
t = (0:N-1)./ groundTruth.Properties.SampleRate;
subplot(2,1,1)
plot(t, positionError, 'b');
title("Tuned insfilterAsync" + newline + "Euclidean Distance Position Error")
xlabel('Time (s)');
ylabel('Position Error (meters)')
subplot(2,1,2)
plot(t, orientationError, 'b');
title("Orientation Error")
xlabel('Time (s)');
ylabel('Orientation Error (degrees)');
```



Input Arguments

filterName — Name of fusion filter

'insfilterAsync'|'ahrs10filter'|'insfilterMARG'|'insfilterNonholonomic'|
'insfitlerErrorState'

Name of fusion filter, specified as specified as one of these:

- 'ahrs10filter'
- 'insfilterAsync'
- 'insfilterMARG'
- 'insfitlerErrorState'
- 'insfilterNonholonomic'

.

Output Arguments

noiseStruct — Structure of measurement noise

structure

Structure of measurement noise, returned as a structure. For the insfilterAsync object, the structure contains these fields.

Field	Description	Default
AccelerometerNoise	Variance of accelerometer noise, specified as a scalar in $(m^2/s)^2$	1
GyroscopeNoise	Variance of gyroscope noise, specified as a scalar in (rad/s) ²	1
MagnetometerNoise	Variance of magnetometer noise, specified as a scalar in $(\mu T)^2$.	1
GPSPositionNoise	Variance of GPS position noise, specified as a scalar in m ²	1
GPSVelocityNoise	Standard deviation of GPS velocity noise, specified as a scalar in (m/s) ²	1

To use this structure with the tune function, change the values of the noise to proper values as initial guesses for tuning the noise.

See Also

Introduced in R2020b

tunerPlotPose

Plot filter pose estimates during tuning

Syntax

```
stopTuning = tunerPlotPose(params, tunerValues)
```

Description

stopTuning = tunerPlotPose(params, tunerValues) plots the current pose estimate,
consisting of orientation (and possibly position, depending on the filter), and the ground truth values.
params contains the best estimates of the filter parameters during the current tuning iteration.
tunerValues contains information on the tuner configuration, sensor data, and ground truth data.
Use this function as the value for the OutputFcn property of the tunerconfig object to plot the
tuning results during iterations.

Examples

Visualize Tuning Results Using tunerPlotPose

Create a tunerconfiguration object. Set the tunerPlotPose function as the output function of the object.

```
tc = tunerconfig('imufilter','OutputFcn',@tunerPlotPose)
tc =
    tunerconfig with properties:
        Filter: "imufilter"
    TunableParameters: [1x5 string]
        StepForward: 1.1000
        StepBackward: 0.5000
        MaxIterations: 20
        ObjectiveLimit: 0.1000
FunctionTolerance: 0
        Display: iter
        Cost: RMS
        OutputFcn: @tunerPlotPose
```

Load prerecorded sensor data.

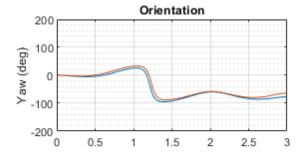
```
ld = load('imufilterTuneData.mat');
```

Tune an imufilter object using the sensor data. The truth data and the estimates are shown in a figure.

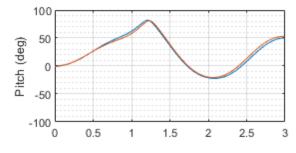
tune(imufilter,ld.sensorData,ld.groundTruth,tc)

Iteration	Parameter	Metric

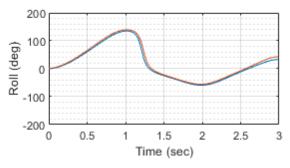
1	AccelerometerNoise	0.1149
1	GyroscopeNoise	0.1146
1	GyroscopeDriftNoise	0.1146
1	LinearAccelerationNoise	0.1122
1	LinearAccelerationDecayFactor	0.1103
2	AccelerometerNoise	0.1102
2	GyroscopeNoise	0.1098
2	GyroscopeDriftNoise	0.1098
2	LinearAccelerationNoise	0.1070
2	LinearAccelerationDecayFactor	0.1053
3	AccelerometerNoise	0.1053
3	GyroscopeNoise	0.1048
3	GyroscopeDriftNoise	0.1048
3	LinearAccelerationNoise	0.1016
3	LinearAccelerationDecayFactor	0.1002
4	AccelerometerNoise	0.1001
4	GyroscopeNoise	0.0996



Iteration: 4 RMS Orientation Error (deg): 5.7042







Input Arguments

params — Estimates of filter parameters

structure

Estimates of filter parameters during the current iteration of the tuning process, specified as a structure. The structure contains one field for every public property of the filter and additional fields for any required measurement noise. The exact field names vary depending on the filter being tuned.

tunerValues — Tuner values

structure

Tuner values, specified as a structure. The structure has these fields:

Field Name	Description
Iteration	Iteration count of the tuner, specified as a positive integer
SensorData	Sensor data input to the tune function
GroundTruth	Ground truth input to the tune function
Configuration	tunerconfig object used for tuning
Cost	Tuning cost at the end of the current iteration

Output Arguments

stopTuning — Stop tuning process

false

Stop the tuning process, returned as false. As a result, using the tunerPlotPose function as the output function of a tunerconfig object never terminates the tuning process of a fusion filter.

See Also

ahrs10filter|ahrsfilter|imufilter|insfilterAsync|insfilterErrorState|
insfilterMARG|insfilterNonholonomic|tunerconfig|tunernoise

Introduced in R2021a

writeBinaryOccupancyGrid

Write values from grid to ROS message

Syntax

writeBinaryOccupancyGrid(msg,map)

Description

writeBinaryOccupancyGrid(msg,map) writes occupancy values and other information to the ROS message, msg, from the binary occupancy grid, map.

Input Arguments

map — Binary occupancy grid

binaryOccupancyMap object handle

Binary occupancy grid, specified as a binaryOccupancyMap object handle. map is converted to a 'nav_msgs/OccupancyGrid' message on the ROS network. map is an object with a grid of binary values, where 1 indicates an occupied location and 0 indications an unoccupied location.

msg — 'nav_msgs/OccupancyGrid' ROS message

OccupancyGrid object handle

'nav_msgs/OccupancyGrid' ROS message, specified as a OccupancyGrid object handle.

See Also

Functions

rosReadBinaryOccupancyGrid | rosReadOccupancyGrid | rosReadOccupancyMap3D |
rosWriteOccupancyGrid

writeBytes

Write raw commands to the GPS receiver

Syntax

writeBytes(gps0bj,dataArray)

Description

writeBytes(gps0bj,dataArray) writes raw data specified by dataArray to configure the GPS module.

Input Arguments

gps0bj — GPS object

gpsdev object

The GPS object with the default or specified properties.

dataArray — Raw data

array

Raw data to write to the GPS module to configure the module, specified as an array.

Data Types: uint8

See Also

Objects

Introduced in R2020b

writeOccupancyGrid

Write values from grid to ROS message

Syntax

writeOccupancyGrid(msg,map)

Description

writeOccupancyGrid(msg,map) writes occupancy values and other information to the ROS message, msg, from the occupancy grid, map.

Input Arguments

msg — 'nav_msgs/OccupancyGrid' ROS message

OccupancyGrid object handle

'nav_msgs/OccupancyGrid' ROS message, specified as an OccupancyGrid ROS message object handle.

map — Occupancy map

occupancyMap object handle

Occupancy map, specified as an occupancyMap object handle.

See Also

Functions

rosReadBinaryOccupancyGrid | rosReadOccupancyGrid | rosReadOccupancyMap3D |
rosWriteOccupancyGrid

Introduced in R2016b

Classes

accelparams

Accelerometer sensor parameters

Description

The accelparams class creates an accelerometer sensor parameters object. You can use this object to model an accelerometer when simulating an IMU with imuSensor.

Creation

Syntax

```
params = accelparams
params = accelparams(Name, Value)
```

Description

params = accelparams returns an ideal accelerometer sensor parameters object with default values.

params = accelparams(Name, Value) configures an accelerometer sensor parameters object properties using one or more Name-Value pair arguments. Name is a property name and Value is the corresponding value. Name must appear inside single quotes (''). You can specify several name-value pair arguments in any order as (Name1, Value1, ..., NameN, ValueN). Any unspecified properties take default values.

Properties

MeasurementRange — Maximum sensor reading (m/s²)

inf (default) | real positive scalar

Maximum sensor reading in m/s^2 , specified as a real positive scalar.

Data Types: single | double

Resolution — Resolution of sensor measurements $((m/s^2)/LSB)$

0 (default) | real nonnegative scalar

Resolution of sensor measurements in (m/s²)/LSB, specified as a real nonnegative scalar.

Data Types: single | double

ConstantBias — Constant sensor offset bias (m/s²)

```
[0 0 0] (default) | real scalar | real 3-element row vector
```

Constant sensor offset bias in m/s^2 , specified as a real scalar or 3-element row vector. Any scalar input is converted into a real 3-element row vector where each element has the input scalar value.

Data Types: single | double

AxesMisalignment — Sensor axes skew (%)

[0 0 0] (default) | real scalar in the range [0,100] | real 3-element row vector in the range [0,100]

Sensor axes skew in %, specified as a real scalar or 3-element row vector with values ranging from 0 to 100. Any scalar input is converted into a real 3-element row vector where each element has the input scalar value.

Data Types: single | double

NoiseDensity — Power spectral density of sensor noise $(m/s^2/\sqrt{Hz})$

[0 0 0] (default) | real scalar | real 3-element row vector

Power spectral density of sensor noise in $(m/s^2/\sqrt{Hz})$, specified as a real scalar or 3-element row vector. This property corresponds to the velocity random walk (VRW). Any scalar input is converted into a real 3-element row vector where each element has the input scalar value.

Data Types: single | double

BiasInstability — Instability of the bias offset (m/s²)

[0 0 0] (default) | real scalar | real 3-element row vector

Instability of the bias offset in m/s², specified as a real scalar or 3-element row vector. Any scalar input is converted into a real 3-element row vector where each element has the input scalar value.

Data Types: single | double

RandomWalk — Integrated white noise of sensor $((m/s^2)(\sqrt{Hz}))$

[0 0 0] (default) | real scalar | real 3-element row vector

Integrated white noise of sensor in $(m/s^2)(\sqrt{Hz})$, specified as a real scalar or 3-element row vector. Any scalar input is converted into a real 3-element row vector where each element has the input scalar value.

Data Types: single | double

TemperatureBias — Sensor bias from temperature ((m/s²)/°C)

[0 0 0] (default) | real scalar | real 3-element row vector

Sensor bias from temperature in (m/s^2) /°C, specified as a real scalar or 3-element row vector. Any scalar input is converted into a real 3-element row vector where each element has the input scalar value.

Data Types: single | double

TemperatureScaleFactor — Scale factor error from temperature (%/°C)

[0 0 0] (default) | real scalar in the range [0,100] | real 3-element row vector in the range [0,100]

Scale factor error from temperature in %C, specified as a real scalar or real 3-element row vector with values ranging from 0 to 100. Any scalar input is converted into a real 3-element row vector where each element has the input scalar value.

Data Types: single | double

Examples

Generate Accelerometer Data from Stationary Inputs

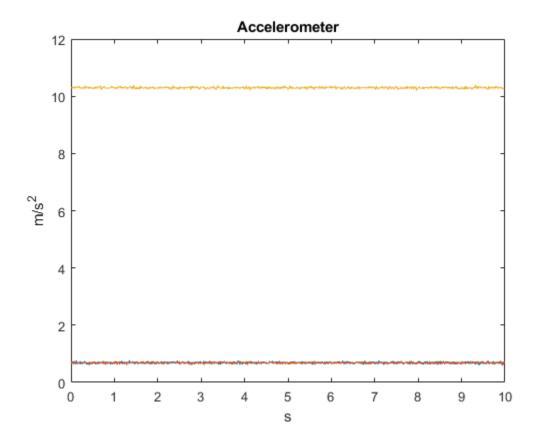
Generate accelerometer data for an imuSensor object from stationary inputs.

Generate an accelerometer parameter object with a maximum sensor reading of 19.6 m/s² and a resolution of 0.598 (mm/s²)/LSB. The constant offset bias is 0.49 m/s². The sensor has a power spectral density of 3920 (μ m/s²)/ \sqrt{Hz} . The bias from temperature is 0.294 (m/s²)/ 0 C. The scale factor error from temperature is 0.02%/ 0 C. The sensor axes are skewed by 2%.

```
params = accelparams('MeasurementRange', 19.6, 'Resolution', 0.598e-3, 'ConstantBias', 0.49, 'NoiseDen
```

Use a sample rate of 100 Hz spaced out over 1000 samples. Create the imuSensor object using the accelerometer parameter object.

```
Fs = 100;
numSamples = 1000;
t = 0:1/Fs:(numSamples-1)/Fs;
imu = imuSensor('SampleRate', Fs, 'Accelerometer', params);
Generate accelerometer data from the imuSensor object.
orient = quaternion.ones(numSamples, 1);
acc = zeros(numSamples, 3);
angvel = zeros(numSamples, 3);
accelData = imu(acc, angvel, orient);
Plot the resultant accelerometer data.
plot(t, accelData)
title('Accelerometer')
xlabel('s')
ylabel('m/s^2')
```



Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder $^{\text{\tiny TM}}$.

See Also

gyroparams|imuSensor|magparams

Introduced in R2018b

ahrs10filter

Height and orientation from MARG and altimeter readings

Description

The ahrs10filter object fuses MARG and altimeter sensor data to estimate device height and orientation. MARG (magnetic, angular rate, gravity) data is typically derived from magnetometer, gyroscope, and accelerometer sensors. The filter uses an 18-element state vector to track the orientation quaternion, vertical velocity, vertical position, MARG sensor biases, and geomagnetic vector. The ahrs10filter object uses an extended Kalman filter to estimate these quantities.

Creation

Syntax

```
FUSE = ahrs10filter
FUSE = ahrs10filter('ReferenceFrame',RF)
FUSE = ahrs10filter(____,Name,Value)
```

Description

FUSE = ahrs10filter returns an extended Kalman filter object, FUSE, for sensor fusion of MARG and altimeter readings to estimate device height and orientation.

FUSE = ahrs10filter('ReferenceFrame', RF) returns an extended Kalman filter object that estimates device height and orientation relative to the reference frame RF. Specify RF as 'NED' (North-East-Down) or 'ENU' (East-North-Up). The default value is 'NED'.

FUSE = ahrs10filter(____, Name, Value) sets each property Name to the specified Value. Unspecified properties have default values.

Properties

IMUSampleRate — Sample rate of the IMU (Hz)

100 (default) | positive scalar

Sample rate of the IMU in Hz, specified as a positive scalar.

Data Types: single | double

GyroscopeNoise — Multiplicative process noise variance from gyroscope ((rad/s)²)

```
[1e-9,1e-9] (default) | scalar | three-element row vector
```

Multiplicative process noise variance from the gyroscope in $(rad/s)^2$, specified as positive real finite numbers.

```
Data Types: single | double
```

AccelerometerNoise — Multiplicative process noise variance from accelerometer $((m/s^2)^2)$

[1e-4,1e-4,1e-4] (default) | scalar | three-element row vector

Multiplicative process noise variance from the accelerometer in $(m/s^2)^2$, specified as positive real finite numbers.

Data Types: single | double

GyroscopeBiasNoise — Multiplicative process noise variance from gyroscope bias ((rad/ s^2)²)

[1e-10, 1e-10, 1e-10] (default) | scalar | three-element row vector

Multiplicative process noise variance from the gyroscope bias in $(rad/s^2)^2$, specified as positive real finite numbers.

Data Types: single | double

AccelerometerBiasNoise — Multiplicative process noise variance from accelerometer bias $((m/s^2)^2)$

[1e-4,1e-4,1e-4] (default) | scalar | three-element row vector

Multiplicative process noise variance from the accelerometer bias in $(m/s^2)^2$, specified as positive real finite numbers.

Data Types: single | double

Geomagnetic Vector Noise — Additive process noise for geomagnetic vector (μT^2)

[1e-6, 1e-6, 1e-6] (default) | scalar | three-element row vector

Additive process noise for geomagnetic vector in μT^2 , specified as positive real finite numbers.

Data Types: single | double

MagnetometerBiasNoise — Additive process noise for magnetometer bias (μT^2)

[0.1,0.1,0.1] (default) | scalar | three-element row vector

Additive process noise for magnetometer bias in μT^2 , specified as positive real finite numbers.

Data Types: single | double

State — State vector of extended Kalman filter

18-element column vector

State vector of the extended Kalman filter. The state values represent:

State	Units	Index
Orientation (quaternion parts)	N/A	1:4
Altitude (NED or ENU)	m	5
Vertical Velocity (NED or ENU)	m/s	6
Delta Angle Bias (XYZ)	rad/s	7:9
Delta Velocity Bias (XYZ)	m/s	10:12
Geomagnetic Field Vector (NED or ENU)	μТ	13:15
Magnetometer Bias (XYZ)	μΤ	16:18

The default initial state corresponds to an object at rest located at $[0\ 0\ 0]$ in geodetic LLA coordinates.

Data Types: single | double

StateCovariance — State error covariance for extended Kalman filter

```
eye(18)*1e-6 (default) | 18-by-18 matrix
```

State error covariance for the Kalman filter, specified as an 18-by-18-element matrix of real numbers.

Data Types: single | double

Object Functions

predict Update states using accelerometer and gyroscope data for ahrs10filter

fusemag Correct states using magnetometer data for ahrs10filter fusealtimeter Correct states using altimeter data for ahrs10filter

correct Correct states using direct state measurements for ahrs10filter

residual Residuals and residual covariances from direct state measurements for

ahrs10filter

residualmag Residuals and residual covariance from magnetometer measurements for

ahrs10filter

residualaltimeter Residuals and residual covariance from altimeter measurements for ahrs10filter

pose Current orientation and position estimate for ahrs10filter

reset Reset internal states for ahrs10filter

stateinfo Display state vector information for ahrs10filter

tune Tune ahrs10filter parameters to reduce estimation error

copy Create copy of ahrs10filter

Examples

Estimate Pose of UAV

Load logged sensor data, ground truth pose, and initial state and initial state covariance. Calculate the number of IMU samples per altimeter sample and the number of IMU samples per magnetometer sample.

```
load('fuse10exampledata.mat', ...
    'imuFs','accelData','gyroData', ...
    'magnetometerFs','magData', ...
    'altimeterFs','altData', ...
    'expectedHeight','expectedOrient', ...
    'initstate','initcov');

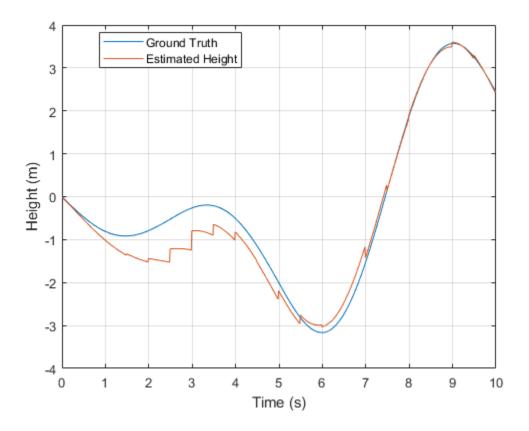
imuSamplesPerAlt = fix(imuFs/altimeterFs);
imuSamplesPerMag = fix(imuFs/magnetometerFs);
```

Create an AHRS filter that fuses MARG and altimeter readings to estimate height and orientation. Set the sampling rate and measurement noises of the sensors. The values were determined from datasheets and experimentation.

```
Ralt = 0.24;
Rmag = 0.9;
Preallocate variables to log height and orientation.
numIMUSamples = size(accelData,1);
estHeight = zeros(numIMUSamples,1);
estOrient = zeros(numIMUSamples,1,'quaternion');
Fuse accelerometer, gyroscope, magnetometer and altimeter data. The outer loop predicts the filter
forward at the fastest sample rate (the IMU sample rate).
for ii = 1:numIMUSamples
    % Use predict to estimate the filter state based on the accelometer and
    % gyroscope data.
    predict(filt,accelData(ii,:),gyroData(ii,:));
    % Magnetometer data is collected at a lower rate than IMU data. Fuse
    % magnetometer data at the lower rate.
    if ~mod(ii,imuSamplesPerMag)
        fusemag(filt,magData(ii,:),Rmag);
    end
    % Altimeter data is collected at a lower rate than IMU data. Fuse
    % altimeter data at the lower rate.
    if ~mod(ii, imuSamplesPerAlt)
        fusealtimeter(filt,altData(ii),Ralt);
    end
    % Log the current height and orientation estimate.
    [estHeight(ii),estOrient(ii)] = pose(filt);
end
Calculate the RMS errors between the known true height and orientation and the output from the
AHRS filter.
pErr = expectedHeight - estHeight;
qErr = rad2deg(dist(expected0rient,est0rient));
pRMS = sqrt(mean(pErr.^2));
qRMS = sqrt(mean(qErr.^2));
fprintf('Altitude RMS Error\n');
Altitude RMS Error
fprintf('\t%.2f (meters)\n\n',pRMS);
    0.38 (meters)
Visualize the true and estimated height over time.
t = (0:(numIMUSamples-1))/imuFs;
plot(t,expectedHeight);hold on
plot(t,estHeight);hold off
legend('Ground Truth', 'Estimated Height', 'location', 'best')
```

ylabel('Height (m)')

```
xlabel('Time (s)')
grid on
```



Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

ahrsfilter|insfilter

correct

Correct states using direct state measurements for ahrs10filter

Syntax

correct(FUSE,idx,measurement,measurementCovariance)

Description

correct(FUSE,idx,measurement,measurementCovariance) corrects the state and state estimation error covariance based on the measurement and measurement covariance. The measurement maps directly to the state specified by the indices idx.

Input Arguments

FUSE — ahrs10filter object

object

Object of ahrs10filter.

idx — State vector index of measurement to correct

N-element vector of increasing integers in the range [1,18]

State vector index of measurement to correct, specified as an N-element vector of increasing integers in the range [1,18].

The state values represent:

State	Units	Index
Orientation (quaternion parts)	N/A	1:4
Altitude (NED)	m	5
Vertical Velocity (NED)	m/s	6
Delta Angle Bias (XYZ)	rad/s	7:9
Delta Velocity Bias (XYZ)	m/s	10:12
Geomagnetic Field Vector (NED)) μΤ	13:15
Magnetometer Bias (XYZ)	μΤ	16:18

Data Types: single | double

measurement — Direct measurement of state

N-element vector

Direct measurement of state, specified as a N-element vector. N is the number of elements of the index argument, idx.

Data Types: single | double

measurementCovariance — Covariance of measurement

scalar | *N*-element vector | *N*-by-*N* matrix

Covariance of measurement, specified as a scalar, N-element vector, or N-by-N matrix. N is the number of elements of the index argument, idx.

Data Types: single | double

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

ahrs10filter|insfilter

copy

Create copy of ahrs10filter

Syntax

newFilter = copy(filter)

Description

newFilter = copy(filter) returns a copy of the ahrs10filter, filter, with the exactly same
property values.

Input Arguments

filter — Filter to be copied

ahrs10filter

Filter to be copied, specified as an ahrs10filter object.

Output Arguments

newFilter — New copied filter

ahrs10filter

New copied filter, returned as an ahrs10filter object.

See Also

ahrs10filter

Introduced in R2020b

fusealtimeter

Correct states using altimeter data for ahrs10filter

Syntax

[res,resCov] = fusealtimeter(FUSE,altimeterReadings, altimeterReadingsCovariance)

Description

[res,resCov] = fusealtimeter(FUSE,altimeterReadings,
altimeterReadingsCovariance) fuses altimeter data to correct the state estimate.

Input Arguments

FUSE — ahrs10filter object

object

Object of ahrs10filter.

altimeterReadings — Altimeter readings (m)

real scalar

Altimeter readings in meters, specified as a real scalar.

Data Types: single | double

altimeterReadingsCovariance — Altimeter readings error covariance (m²)

real scalar

Altimeter readings error covariance in m², specified as a real scalar.

Data Types: single | double

Output Arguments

res — Measurement residual

scalar

Measurement residual, returned as a scalar in meters.

resCov — Residual covariance

nonnegative scalar

Residual covariance, returned as a nonnegative scalar in m^2 .

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

ahrs10filter|insfilter

fusemag

Correct states using magnetometer data for ahrs10filter

Syntax

[res,resCov] = fusemag(FUSE,magReadings,magReadingsCovariance)

Description

[res,resCov] = fusemag(FUSE,magReadings,magReadingsCovariance) fuses
magnetometer data to correct the state estimate.

Input Arguments

FUSE — ahrs10filter object

object

Object of ahrs10filter.

magReadings — Magnetometer readings (μT)

3-element row vector

Magnetometer readings in μT , specified as a 3-element row vector of finite real numbers.

Data Types: single | double

magReadingsCovariance — Magnetometer readings error covariance (μT^2)

scalar | 3-element row vector | 3-by-3 matrix

Magnetometer readings error covariance in μT^2 , specified as a scalar, 3-element row vector, or 3-by-3 matrix.

Data Types: single | double

res — Residual

1-by-3 vector of real values

Residual, returned as a 1-by-3 vector of real values in μT .

Data Types: single | double

resCov — Residual covariance

3-by-3 matrix of real values

Residual covariance, returned a 3-by-3 matrix of real values in $(\mu T)^2$.

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

ahrs10filter|insfilter

pose

Current orientation and position estimate for ahrs10filter

Syntax

```
[position, orientation, velocity] = pose(FUSE)
[position, orientation, velocity] = pose(FUSE, format)
```

Description

[position, orientation, velocity] = pose(FUSE) returns the current estimate of the pose.

[position, orientation, velocity] = pose(FUSE, format) returns the current estimate of the pose with orientation in the specified orientation format.

Input Arguments

FUSE — ahrs10filter object

object

Object of ahrs10filter.

format — Output orientation format

```
'quaternion' (default) | 'rotmat'
```

Output orientation format, specified as either 'quaternion' for a quaternion or 'rotmat' for a rotation matrix.

Data Types: char | string

Output Arguments

position — Vertical position estimate in the local NED coordinate system (m)

scalar

Vertical position estimate in the local NED coordinate system in meters, returned as a scalar.

Data Types: single | double

orientation — Orientation estimate in the local NED coordinate system

quaternion (default) | 3-by-3 rotation matrix

Orientation estimate in the local NED coordinate system, returned as a scalar quaternion or 3-by-3 rotation matrix. The quaternion or rotation matrix represents a frame rotation from the local NED reference frame to the body reference frame.

Data Types: single | double | quaternion

velocity — Vertical velocity estimate in the local NED coordinate system (m/s)

scalar

Vertical velocity estimate in the local NED coordinate system in m/s, returned as a scalar.

Data Types: single | double

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder $^{\text{\tiny TM}}$.

See Also

ahrs10filter|insfilter

predict

Update states using accelerometer and gyroscope data for ahrs10filter

Syntax

predict(FUSE,accelReadings,gyroReadings)

Description

predict(FUSE,accelReadings,gyroReadings) fuses accelerometer and gyroscope data to update the state estimate.

Input Arguments

FUSE — ahrs10Filter object

object

Object of ahrs10filter.

accelReadings — Accelerometer readings in the sensor body coordinate system (m/s 2) N-bv-3 matrix

Accelerometer readings in local sensor body coordinate system in m/s^2 , specified as an N-by-3 matrix. N is the number of samples, and the three columns of accelReadings represent the $[x \ y \ z]$ measurements. Accelerometer readings are assumed to correspond to the sample rate specified by the IMUSampleRate property.

Data Types: single | double

gyroReadings — Gyroscope readings in the sensor body coordinate system (rad/s) N-by-3 matrix

Gyroscope readings in the sensor body coordinate system in rad/s, specified as an N-by-3 matrix. N is the number of samples, and the three columns of <code>gyroReadings</code> represent the $[x\ y\ z]$ measurements. Gyroscope readings are assumed to correspond to the sample rate specified by the <code>IMUSampleRate</code> property.

Data Types: single | double

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

ahrs10filter|insfilter

reset

Reset internal states for ahrs10filter

Syntax

reset(FUSE)

Description

reset (FUSE) resets the State, StateCovariance, and internal integrators to their default values.

Input Arguments

FUSE — ahrs10filter object

object

Object of ahrs10filter.

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

ahrs10filter|insfilter

residual

Residuals and residual covariances from direct state measurements for ahrs10filter

Syntax

[res, resCov] = residual(FUSE,idx,measurement,measurementCovariance)

Description

[res, resCov] = residual(FUSE,idx,measurement,measurementCovariance) computes the residual, res, and the residual covariance, resCov, based on the direct state measurement and measurement covariance. The measurement maps directly to the states specified by indices, idx.

Input Arguments

FUSE — ahrs10filter

ahrs10filter | object

ahrs10filter, specified as an object.

idx — State vector index of measurement to correct

N-element vector of increasing integers in the range [1,18]

State vector index of measurement to correct, specified as an N-element vector of increasing integers in the range [1,18].

The state values represent:

State	Units	Index
Orientation (quaternion parts)	N/A	1:4
Altitude (NED)	m	5
Vertical Velocity (NED)	m/s	6
Delta Angle Bias (XYZ)	rad/s	7:9
Delta Velocity Bias (XYZ)	m/s	10:12
Geomagnetic Field Vector (NED)	μΤ	13:15
Magnetometer Bias (XYZ)	μΤ	16:18

measurement — Direct measurement of state

N-element vector

Direct measurement of state, specified as a N-element vector. N is the number of elements of the index argument, idx.

measurementCovariance — Covariance of measurement

N-by-*N* matrix

Covariance of measurement, specified as an N-by-N matrix. N is the number of elements of the index argument, idx.

Output Arguments

res — Measurement residual

1-by-*N* vector of real values

Measurement residual, returned as a 1-by-N vector of real values.

resCov — Residual covariance

N-by-N matrix of real values

Residual covariance, returned as a *N*-by-*N* matrix of real values.

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

ahrs10filter

Introduced in R2020a

residualaltimeter

Residuals and residual covariance from altimeter measurements for ahrs10filter

Syntax

[res,resCov] = residualaltimeter(FUSE,altimeterReadings, altimeterReadingsCovariance)

Description

[res,resCov] = residualaltimeter(FUSE,altimeterReadings,
altimeterReadingsCovariance) computes the residual, res, and the innovation covariance,
resCov, based on the magnetometer readings and the corresponding covariance.

Input Arguments

FUSE — ahrs10filter

ahrs10filter | object

ahrs10filter, specified as an object.

altimeterReadings — Altimeter readings (m)

real scalar

Altimeter readings in meters, specified as a real scalar.

Data Types: single | double

altimeterReadingsCovariance — Altimeter readings error covariance (m²)

real scalar

Altimeter readings error covariance in m², specified as a real scalar.

Data Types: single | double

Output Arguments

res - Measurement residual

scalar

Measurement residual, returned as a scalar in meters.

resCov — Residual covariance

nonnegative scalar

Residual covariance, returned as a nonnegative scalar in m^2 .

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder $^{\text{\tiny TM}}$.

See Also

ahrs10filter|insfilter

Introduced in R2020a

residualmag

Residuals and residual covariance from magnetometer measurements for ahrs10filter

Syntax

[res,resCov] = residualmag(FUSE,magReadings,magReadingsCovariance)

Description

[res,resCov] = residualmag(FUSE,magReadings,magReadingsCovariance) computes the
residual, residual, and the residual covariance, resCov, based on the magnetometer readings and
the corresponding covariance.

Input Arguments

FUSE — ahrs10filter

ahrs10filter | object

ahrs10filter, specified as an object.

magReadings — Magnetometer readings (μT)

3-element row vector

Magnetometer readings in μT, specified as a 3-element row vector of finite real numbers.

Data Types: single | double

magReadingsCovariance — Magnetometer readings error covariance (μ T²)

scalar | 3-element row vector | 3-by-3 matrix

Magnetometer readings error covariance in μT^2 , specified as a scalar, 3-element row vector, or 3-by-3 matrix.

Data Types: single | double

Output Arguments

res - Residual

1-by-3 vector of real values

Residual, returned as a 1-by-3 vector of real values in μ T.

Data Types: single | double

resCov — Residual covariance

3-by-3 matrix of real values

Residual covariance, returned a 3-by-3 matrix of real values in $(\mu T)^2$.

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder $^{\text{\tiny TM}}$.

See Also

ahrs10filter

Introduced in R2020a

stateinfo

Display state vector information for ahrs10filter

Syntax

```
stateinfo(FUSE)
info = stateinfo(FUSE)
```

Description

stateinfo(FUSE) displays the meaning of each index of the State property and the associated units.

info = stateinfo(FUSE) returns a structure with fields containing descriptions of the elements of
the state vector of the filter, FUSE.

Examples

State information of ahrs10filter

Create an ahrs10filter object.

```
filter = ahrs10filter;
```

Display the state information of the created filter.

stateinfo(filter)

States	Units	Index
Orientation (quaternion parts)		1:4
Altitude (NAV)	m	5
Vertical Velocity (NAV)	m/s	6
Delta Angle Bias (XYZ)	rad	7:9
Delta Velocity Bias (XYZ)	m/s	10:12
Geomagnetic Field Vector (NAV)	μΤ	13:15
Magnetometer Bias (XYZ)	μΤ	16:18

Output the state information of the filter as a structure.

info = stateinfo(filter)

Input Arguments

FUSE — ahrs10filter object

object

Object of ahrs10filter.

Output Arguments

info — State information

structure

State information, returned as a structure with fields containing descriptions of the elements of the state vector of the filter. The values of each field are the corresponding indices of the state vector.

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

ahrs10filter|insfilter

tune

Tune ahrs10filter parameters to reduce estimation error

Syntax

Description

tunedMeasureNoise = tune(filter,measureNoise,sensorData,groundTruth) adjusts the properties of the ahrs10filter filter object, filter, and measurement noises to reduce the root-mean-squared (RMS) state estimation error between the fused sensor data and the ground truth. The function also returns the tuned measurement noise, tunedMeasureNoise. The function uses the property values in the filter and the measurement noise provided in the measureNoise structure as the initial estimate for the optimization algorithm.

tunedMeasureNoise = tune(____, config) specifies the tuning configuration based on a tunerconfig object, config.

Examples

Tune ahrs10filter to Optimize Pose Estimate

Load the recorded sensor data and ground truth data.

```
load('ahrs10filterTuneData.mat');
Create tables for the sensor data and the truth data.
sensorData = table(Accelerometer, Gyroscope,...
    Magnetometer, Altimeter);
groundTruth = table(Orientation, Altitude);
Create an ahrs10filter filter object.
filter = ahrs10filter('State', initialState, ...
    'StateCovariance', initialStateCovariance);
```

Create a tuner configuration object for the filter. Set the maximum iterations to ten and set the objective limit to 0.001.

Use the tuner noise function to obtain a set of initial sensor noises used in the filter.

```
measNoise = tunernoise('ahrs10filter')
measNoise = struct with fields:
    MagnetometerNoise: 1
```

AltimeterNoise: 1

Tune the filter and obtain the tuned parameters.

tunedNoise = tune(filter, measNoise, sensorData, ... groundTruth, cfg);

Iteration	Parameter	Metric
1	AccelerometerNoise	0.0526
1	GyroscopeNoise	0.0526
1	MagnetometerNoise	0.0523
1	AltimeterNoise	0.0515
1	AccelerometerBiasNoise	0.0510
1	GyroscopeBiasNoise	0.0510
1	GeomagneticVectorNoise	0.0510
1	MagnetometerBiasNoise	0.0508
2	AccelerometerNoise	0.0508
2		0.0508
2	GyroscopeNoise	0.0504
2	MagnetometerNoise	
	AltimeterNoise	0.0494
2	AccelerometerBiasNoise	0.0490
2	GyroscopeBiasNoise	0.0490
2	GeomagneticVectorNoise	0.0490
2	MagnetometerBiasNoise	0.0487
3	AccelerometerNoise	0.0487
3	GyroscopeNoise	0.0487
3	MagnetometerNoise	0.0482
3	AltimeterNoise	0.0472
3	AccelerometerBiasNoise	0.0467
3	GyroscopeBiasNoise	0.0467
2 2 3 3 3 3 3 3 3 3	GeomagneticVectorNoise	0.0467
	MagnetometerBiasNoise	0.0463
4	AccelerometerNoise	0.0463
4	GyroscopeNoise	0.0463
4	MagnetometerNoise	0.0456
4	AltimeterNoise	0.0446
4	AccelerometerBiasNoise	0.0442
4	GyroscopeBiasNoise	0.0442
4	GeomagneticVectorNoise	0.0442
4	MagnetometerBiasNoise	0.0437
5	AccelerometerNoise	0.0437
5	GyroscopeNoise	0.0437
5 5 5 5	MagnetometerNoise	0.0428
5	AltimeterNoise	0.0417
5	AccelerometerBiasNoise	0.0413
5	GyroscopeBiasNoise	0.0413
5	GeomagneticVectorNoise	0.0413
5	MagnetometerBiasNoise	0.0408
6	AccelerometerNoise	0.0408
6	GyroscopeNoise	0.0408
6	MagnetometerNoise	0.0397
6	AltimeterNoise	0.0385
6	AccelerometerBiasNoise	0.0381
6	GyroscopeBiasNoise	0.0381
6	GeomagneticVectorNoise	0.0381
6	MagnetometerBiasNoise	0.0375

```
AccelerometerNoise
                                       0.0375
7
             GyroscopeNoise
                                       0.0375
7
             MagnetometerNoise
                                       0.0363
7
             AltimeterNoise
                                       0.0351
7
             AccelerometerBiasNoise
                                       0.0347
7
             GyroscopeBiasNoise
                                       0.0347
7
             GeomagneticVectorNoise
                                       0.0347
7
             MagnetometerBiasNoise
                                       0.0342
8
             AccelerometerNoise
                                       0.0342
8
             GvroscopeNoise
                                       0.0342
8
             MagnetometerNoise
                                       0.0331
8
             AltimeterNoise
                                       0.0319
8
             AccelerometerBiasNoise
                                       0.0316
8
                                       0.0316
             GyroscopeBiasNoise
8
             GeomagneticVectorNoise
                                       0.0316
8
                                       0.0313
             MagnetometerBiasNoise
9
                                       0.0313
             AccelerometerNoise
9
             GyroscopeNoise
                                       0.0313
9
             MagnetometerNoise
                                       0.0313
9
             AltimeterNoise
                                       0.0301
9
             AccelerometerBiasNoise
                                       0.0298
9
                                       0.0298
             GyroscopeBiasNoise
9
             GeomagneticVectorNoise
                                       0.0298
9
                                       0.0296
             MagnetometerBiasNoise
10
                                       0.0296
             AccelerometerNoise
             GyroscopeNoise
10
                                       0.0296
10
                                       0.0296
             MagnetometerNoise
10
                                       0.0285
             AltimeterNoise
10
             AccelerometerBiasNoise
                                       0.0283
10
             GyroscopeBiasNoise
                                       0.0283
10
             GeomagneticVectorNoise
                                       0.0283
10
             MagnetometerBiasNoise
                                       0.0282
```

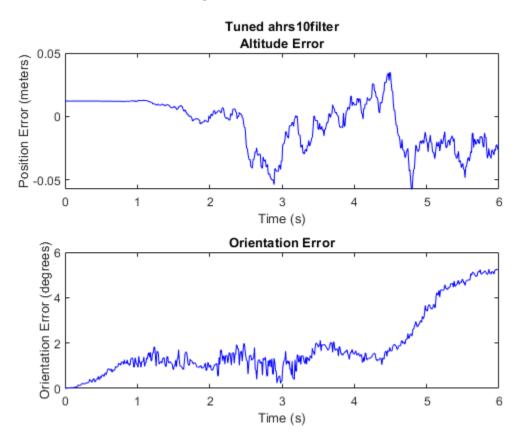
Fuse the sensor data using the tuned filter.

```
N = size(sensorData,1);
qEstTuned = quaternion.zeros(N,1);
altEstTuned = zeros(N,1);
for ii=1:N
    predict(filter,Accelerometer(ii,:),Gyroscope(ii,:));
    if all(~isnan(Magnetometer(ii,1)))
        fusemag(filter, Magnetometer(ii,:),tunedNoise.MagnetometerNoise);
    end
    if ~isnan(Altimeter(ii))
        fusealtimeter(filter, Altimeter(ii),tunedNoise.AltimeterNoise);
    [altEstTuned(ii), qEstTuned(ii)] = pose(filter);
end
Compute the RMS errors.
orientationErrorTuned = rad2deg(dist(qEstTuned, Orientation));
rmsOrientationErrorTuned = sqrt(mean(orientationErrorTuned.^2))
rmsOrientationErrorTuned = 2.2899
positionErrorTuned = altEstTuned - Altitude;
rmsPositionErrorTuned = sqrt(mean( positionErrorTuned.^2))
```

rmsPositionErrorTuned = 0.0199

Visualize the results.

```
figure;
t = (0:N-1)./ filter.IMUSampleRate;
subplot(2,1,1)
plot(t, positionErrorTuned, 'b');
title("Tuned ahrs10filter" + newline + ...
    "Altitude Error")
xlabel('Time (s)');
ylabel('Position Error (meters)')
subplot(2,1,2)
plot(t, orientationErrorTuned, 'b');
title("Orientation Error")
xlabel('Time (s)');
ylabel('Orientation Error (degrees)');
```



Input Arguments

filter — Filter object

ahrs10filter object

Filter object, specified as an ahrs10filter object.

measureNoise — Measurement noise

structure

Measurement noise, specified as a structure. The function uses the measurement noise input as the initial guess for tuning the measurement noise. The structure must contain these fields:

Field name	Description
MagnetometerNoise	Variance of magnetometer noise, specified as a scalar in $(\mu T)^2$
	Variance of altimeter noise, specified as a scalar in \mathbf{m}^2

sensorData — Sensor data

table

Sensor data, specified as a table. In each row, the sensor data is specified as:

- Accelerometer Accelerometer data, specified as a 1-by-3 vector of scalars in m²/s.
- Gyroscope—Gyroscope data, specified as a 1-by-3 vector of scalars in rad/s.
- Magnetometer Magnetometer data, specified as a 1-by-3 vector of scalars in μT.
- Altimeter Altimeter data, specified as a scalar in meters.

If the magnetometer does not produce measurements, specify the corresponding entry as NaN. If you set the Cost property of the tuner configuration input, config, to Custom, then you can use other data types for the sensorData input based on your choice.

groundTruth — Ground truth data

table

Ground truth data, specified as a table. In each row, the table can optionally contain any of these variables:

- Orientation Orientation from the navigation frame to the body frame, specified as a quaternion or a 3-by-3 rotation matrix.
- Altitude Altitude, specified as a scalar in meters.
- VertialVelocity Velocity in the vertical direction, specified as a scalar in m/s.
- DeltaAngleBias Delta angle bias, specified as a 1-by-3 vector of scalars in radians.
- DeltaVelocityBias Delta velocity bias, specified as a 1-by-3 vector of scalars in m/s.
- GeomagneticFieldVector Geomagnetic field vector in navigation frame, specified as a 1-by-3 vector of scalars.
- MagnetometerBias Magnetometer bias in body frame, specified as a 1-by-3 vector of scalars in μT .

The function processes each row of the sensorData and groundTruth tables sequentially to calculate the state estimate and RMS error from the ground truth. State variables not present in groundTruth input are ignored for the comparison. The sensorData and the groundTruth tables must have the same number of rows.

If you set the Cost property of the tuner configuration input, config, to Custom, then you can use other data types for the groundTruth input based on your choice.

config — Tuner configuration

tunerconfig object

Tuner configuration, specified as a tunerconfig object.

Output Arguments

tunedMeasureNoise — Tuned measurement noise

structure

Tuned measurement noise, returned as a structure. The structure contains these fields.

Field name	Description
	Variance of magnetometer noise, specified as a scalar in $(\mu T)^2$
	Variance of altimeter noise, specified as a scalar in \mathbf{m}^2

References

[1] Abbeel, P., Coates, A., Montemerlo, M., Ng, A.Y. and Thrun, S. Discriminative Training of Kalman Filters. In *Robotics: Science and systems*, Vol. 2, pp. 1, 2005.

See Also

tunerconfig|tunernoise

Introduced in R2021a

ahrsfilter

Orientation from accelerometer, gyroscope, and magnetometer readings

Description

The ahrsfilter System object $^{\text{\tiny TM}}$ fuses accelerometer, magnetometer, and gyroscope sensor data to estimate device orientation.

To estimate device orientation:

- 1 Create the ahrsfilter object and set its properties.
- **2** Call the object with arguments, as if it were a function.

To learn more about how System objects work, see What Are System Objects?.

Creation

Syntax

```
FUSE = ahrsfilter
FUSE = ahrsfilter('ReferenceFrame',RF)
FUSE = ahrsfilter(____,Name,Value)
```

Description

FUSE = ahrsfilter returns an indirect Kalman filter System object, FUSE, for sensor fusion of accelerometer, gyroscope, and magnetometer data to estimate device orientation and angular velocity. The filter uses a 12-element state vector to track the estimation error for the orientation, the gyroscope bias, the linear acceleration, and the magnetic disturbance.

FUSE = ahrsfilter('ReferenceFrame', RF) returns an ahrsfilter System object that fuses accelerometer, gyroscope, and magnetometer data to estimate device orientation relative to the reference frame RF. Specify RF as 'NED' (North-East-Down) or 'ENU' (East-North-Up). The default value is 'NED'.

FUSE = ahrsfilter(____, Name, Value) sets each property Name to the specified Value. Unspecified properties have default values.

Properties

Unless otherwise indicated, properties are *nontunable*, which means you cannot change their values after calling the object. Objects lock when you call them, and the release function unlocks them.

If a property is tunable, you can change its value at any time.

For more information on changing property values, see System Design in MATLAB Using System Objects.

SampleRate — Input sample rate of sensor data (Hz)

100 (default) | positive scalar

Input sample rate of the sensor data in Hz, specified as a positive scalar.

Tunable: No

Data Types: single | double

DecimationFactor — Decimation factor

1 (default) | positive integer

Decimation factor by which to reduce the input sensor data rate as part of the fusion algorithm, specified as a positive integer.

The number of rows of the inputs -- accelReadings, gyroReadings, and magReadings -- must be a multiple of the decimation factor.

Data Types: single | double

AccelerometerNoise — Variance of accelerometer signal noise $((m/s^2)^2)$

0.00019247 (default) | positive real scalar

Variance of accelerometer signal noise in $(m/s^2)^2$, specified as a positive real scalar.

Tunable: Yes

Data Types: single | double

MagnetometerNoise — Variance of magnetometer signal noise (μT^2)

0.1 (default) | positive real scalar

Variance of magnetometer signal noise in μT^2 , specified as a positive real scalar.

Tunable: Yes

Data Types: single | double

GyroscopeNoise — Variance of gyroscope signal noise ((rad/s)²)

9.1385e-5 (default) | positive real scalar

Variance of gyroscope signal noise in (rad/s)², specified as a positive real scalar.

Tunable: Yes

Data Types: single | double

GyroscopeDriftNoise — Variance of gyroscope offset drift ((rad/s)²)

3.0462e-13 (default) | positive real scalar

Variance of gyroscope offset drift in (rad/s)², specified as a positive real scalar.

Tunable: Yes

Data Types: single | double

LinearAccelerationNoise — Variance of linear acceleration noise (m/s²)²

0.0096236 (default) | positive real scalar

Variance of linear acceleration noise in $(m/s^2)^2$, specified as a positive real scalar. Linear acceleration is modeled as a lowpass-filtered white noise process.

Tunable: Yes

Data Types: single | double

LinearAccelerationDecayFactor — Decay factor for linear acceleration drift

0.5 (default) | scalar in the range [0,1)

Decay factor for linear acceleration drift, specified as a scalar in the range [0,1). If linear acceleration is changing quickly, set LinearAcclerationDecayFactor to a lower value. If linear acceleration changes slowly, set LinearAcclerationDecayFactor to a higher value. Linear acceleration drift is modeled as a lowpass-filtered white noise process.

Tunable: Yes

Data Types: single | double

MagneticDisturbanceNoise — Variance of magnetic disturbance noise (μT^2)

0.5 (default) | real finite positive scalar

Variance of magnetic disturbance noise in μT^2 , specified as a real finite positive scalar.

Tunable: Yes

Data Types: single | double

${\tt Magnetic Disturbance Decay Factor-Decay factor for magnetic disturbance}$

0.5 (default) | positive scalar in the range [0,1]

Decay factor for magnetic disturbance, specified as a positive scalar in the range [0,1]. Magnetic disturbance is modeled as a first order Markov process.

Tunable: Yes

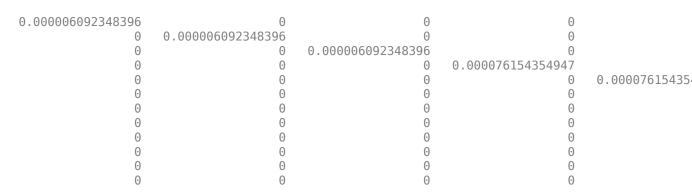
Data Types: single | double

InitialProcessNoise — Covariance matrix for process noise

12-by-12 matrix

Covariance matrix for process noise, specified as a 12-by-12 matrix. The default is:

Co	lumns	1	th	roug	h 6



Columns 7 through 12	2			
0	0	0	0	
0	0	0	0	
0	0	0	0	
0	0	0	0	
0	0	0	0	
0	0	0	0	
0.009623610000000	0	0	0	
0	0.009623610000000	0	0	
0	0	0.009623610000000	0	
0	0	0	0.600000000000000	
0	0	0	0	0.6000000000000
0	0	0	Θ	

The initial process covariance matrix accounts for the error in the process model.

Data Types: single | double

ExpectedMagneticFieldStrength — Expected estimate of magnetic field strength (μT) 50 (default) | real positive scalar

Expected estimate of magnetic field strength in μ T, specified as a real positive scalar. The expected magnetic field strength is an estimate of the magnetic field strength of the Earth at the current location.

Tunable: Yes

Data Types: single | double

OrientationFormat — **Output orientation format**

'quaternion' (default) | 'Rotation matrix'

Output orientation format, specified as 'quaternion' or 'Rotation matrix'. The size of the output depends on the input size, N, and the output orientation format:

- 'quaternion' -- Output is an N-by-1 quaternion.
- 'Rotation matrix' -- Output is a 3-by-3-by-*N* rotation matrix.

Data Types: char | string

Usage

Syntax

[orientation,angularVelocity] = FUSE(accelReadings,gyroReadings,magReadings)

Description

[orientation, angular Velocity] = FUSE (accelReadings, gyroReadings, magReadings) fuses accelerometer, gyroscope, and magnetometer data to compute orientation and angular velocity measurements. The algorithm assumes that the device is stationary before the first call.

Input Arguments

accelReadings — Accelerometer readings in sensor body coordinate system (m/s²)

N-by-3 matrix

Accelerometer readings in the sensor body coordinate system in m/s^2 , specified as an N-by-3 matrix. N is the number of samples, and the three columns of accelReadings represent the $[x\ y\ z]$ measurements. Accelerometer readings are assumed to correspond to the sample rate specified by the SampleRate property.

Data Types: single | double

gyroReadings — Gyroscope readings in sensor body coordinate system (rad/s)

N-by-3 matrix

Gyroscope readings in the sensor body coordinate system in rad/s, specified as an N-by-3 matrix. N is the number of samples, and the three columns of <code>gyroReadings</code> represent the [x y z] measurements. Gyroscope readings are assumed to correspond to the sample rate specified by the SampleRate property.

Data Types: single | double

magReadings — Magnetometer readings in sensor body coordinate system (μT)

N-by-3 matrix

Magnetometer readings in the sensor body coordinate system in μT , specified as an N-by-3 matrix. N is the number of samples, and the three columns of magReadings represent the $[x\ y\ z]$ measurements. Magnetometer readings are assumed to correspond to the sample rate specified by the SampleRate property.

Data Types: single | double

Output Arguments

orientation — Orientation that rotates quantities from local navigation coordinate system to sensor body coordinate system

M-by-1 array of quaternions (default) | 3-by-3-by-*M* array

Orientation that can rotate quantities from the local navigation coordinate system to a body coordinate system, returned as quaternions or an array. The size and type of orientation depends on whether the OrienationFormat property is set to 'quaternion' or 'Rotation matrix':

- 'quaternion' -- the output is an *M*-by-1 vector of quaternions, with the same underlying data type as the inputs
- 'Rotation matrix' -- the output is a 3-by-3-by-M array of rotation matrices the same data type as the inputs

The number of input samples, N, and the DecimationFactor property determine M.

You can use orientation in a rotateframe function to rotate quantities from a local navigation system to a sensor body coordinate system.

Data Types: quaternion | single | double

angularVelocity — Angular velocity in sensor body coordinate system (rad/s)

M-by-3 array (default)

Angular velocity with gyroscope bias removed in the sensor body coordinate system in rad/s, returned as an M-by-3 array. The number of input samples, N, and the DecimationFactor property determine M.

Data Types: single | double

Object Functions

To use an object function, specify the System object as the first input argument. For example, to release system resources of a System object named obj, use this syntax:

release(obj)

Specific to ahrsfilter

tune Tune ahrsfilter parameters to reduce estimation error

Common to All System Objects

step Run System object algorithm

release Release resources and allow changes to System object property values and input

characteristics

reset Reset internal states of System object

Examples

Estimate Orientation Using ahrsfilter

Load the rpy_9axis file, which contains recorded accelerometer, gyroscope, and magnetometer sensor data from a device oscillating in pitch (around y-axis), then yaw (around z-axis), and then roll (around x-axis). The file also contains the sample rate of the recording.

```
load 'rpy_9axis' sensorData Fs
accelerometerReadings = sensorData.Acceleration;
gyroscopeReadings = sensorData.AngularVelocity;
magnetometerReadings = sensorData.MagneticField;
```

Create an ahrsfilter System object™ with SampleRate set to the sample rate of the sensor data. Specify a decimation factor of two to reduce the computational cost of the algorithm.

```
decim = 2;
fuse = ahrsfilter('SampleRate',Fs,'DecimationFactor',decim);
```

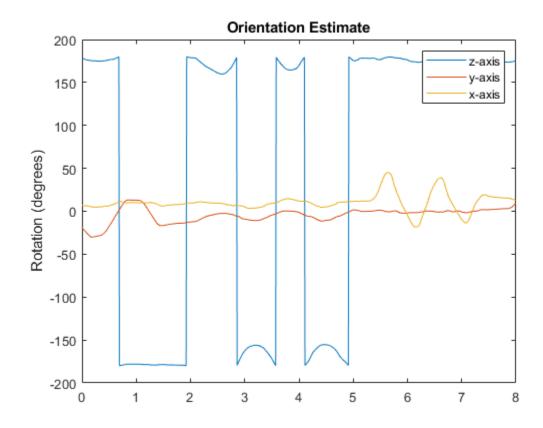
Pass the accelerometer readings, gyroscope readings, and magnetometer readings to the ahrsfilter object, fuse, to output an estimate of the sensor body orientation over time. By default, the orientation is output as a vector of quaternions.

```
q = fuse(accelerometerReadings,gyroscopeReadings,magnetometerReadings);
```

Orientation is defined by angular displacement required to rotate a parent coordinate system to a child coordinate system. Plot the orientation in Euler angles in degrees over time.

ahrsfilter correctly estimates the change in orientation over time, including the south-facing initial orientation.

```
time = (0:decim:size(accelerometerReadings,1)-1)/Fs;
plot(time,eulerd(q,'ZYX','frame'))
title('Orientation Estimate')
legend('z-axis', 'y-axis', 'x-axis')
ylabel('Rotation (degrees)')
```



Simulate Magnetic Jamming on ahrsFilter

This example shows how performance of the ahrsfilter System object $^{\text{\tiny TM}}$ is affected by magnetic jamming.

Load StationaryIMUReadings, which contains accelerometer, magnetometer, and gyroscope readings from a stationary IMU.

```
load 'StationaryIMUReadings.mat' accelReadings magReadings gyroReadings SampleRate
numSamples = size(accelReadings,1);
```

The ahrsfilter uses magnetic field strength to stabilize its orientation against the assumed constant magnetic field of the Earth. However, there are many natural and man-made objects which output magnetic fields and can confuse the algorithm. To account for the presence of transient magnetic fields, you can set the MagneticDisturbanceNoise property on the ahrsfilter object.

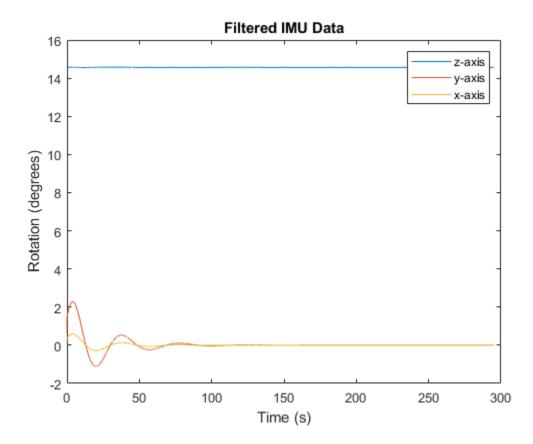
Create an ahrsfilter object with the decimation factor set to 2 and note the default expected magnetic field strength.

```
decim = 2;
FUSE = ahrsfilter('SampleRate', SampleRate, 'DecimationFactor', decim);
```

Fuse the IMU readings using the attitude and heading reference system (AHRS) filter, and then visualize the orientation of the sensor body over time. The orientation fluctuates at the beginning and stabilizes after approximately 60 seconds.

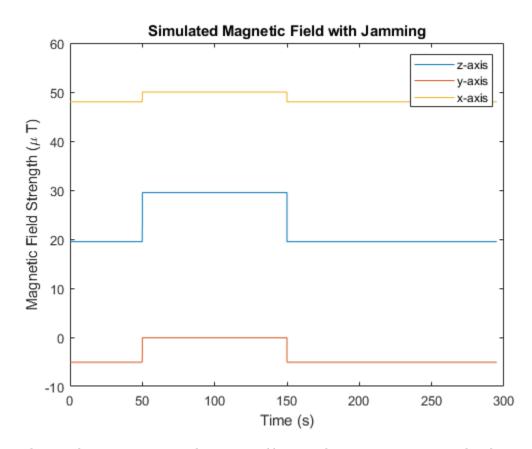
```
orientation = FUSE(accelReadings,gyroReadings,magReadings);
orientationEulerAngles = eulerd(orientation,'ZYX','frame');
time = (0:decim:(numSamples-1))'/SampleRate;

figure(1)
plot(time,orientationEulerAngles(:,1), ...
    time,orientationEulerAngles(:,2), ...
    time,orientationEulerAngles(:,3))
xlabel('Time (s)')
ylabel('Rotation (degrees)')
legend('z-axis','y-axis','x-axis')
title('Filtered IMU Data')
```



Mimic magnetic jamming by adding a transient, strong magnetic field to the magnetic field recorded in the magReadings. Visualize the magnetic field jamming.

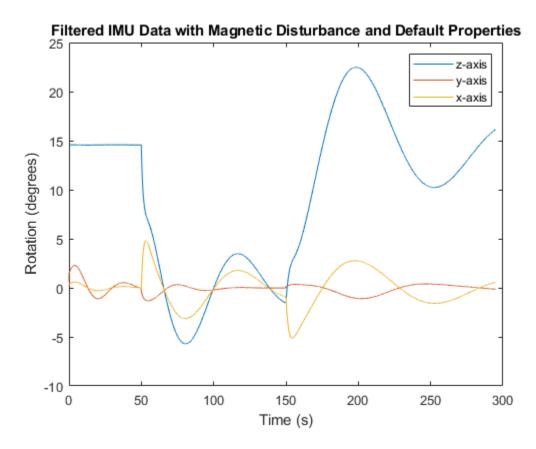
```
jamStrength = [10,5,2];
startStop = (50*SampleRate):(150*SampleRate);
jam = zeros(size(magReadings));
jam(startStop,:) = jamStrength.*ones(numel(startStop),3);
magReadings = magReadings + jam;
figure(2)
plot(time,magReadings(1:decim:end,:))
xlabel('Time (s)')
ylabel('Magnetic Field Strength (\mu T)')
title('Simulated Magnetic Field with Jamming')
legend('z-axis','y-axis','x-axis')
```



Run the simulation again using the magReadings with magnetic jamming. Plot the results and note the decreased performance in orientation estimation.

```
reset(FUSE)
orientation = FUSE(accelReadings,gyroReadings,magReadings);
orientationEulerAngles = eulerd(orientation,'ZYX','frame');
figure(3)
plot(time,orientationEulerAngles(:,1), ...
        time,orientationEulerAngles(:,2), ...
        time,orientationEulerAngles(:,2), ...
        time,orientationEulerAngles(:,3))
xlabel('Time (s)')
ylabel('Rotation (degrees)')
```

```
legend('z-axis','y-axis','x-axis')
title('Filtered IMU Data with Magnetic Disturbance and Default Properties')
```



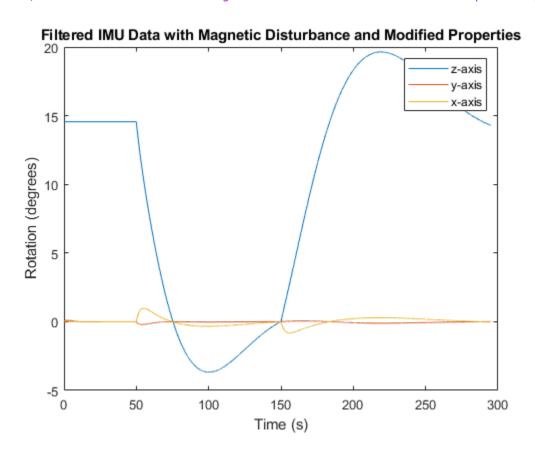
The magnetic jamming was misinterpreted by the AHRS filter, and the sensor body orientation was incorrectly estimated. You can compensate for jamming by increasing the MagneticDisturbanceNoise property. Increasing the MagneticDisturbanceNoise property increases the assumed noise range for magnetic disturbance, and the entire magnetometer signal is weighted less in the underlying fusion algorithm of ahrsfilter.

Set the MagneticDisturbanceNoise to 200 and run the simulation again.

The orientation estimation output from ahrsfilter is more accurate and less affected by the magnetic transient. However, because the magnetometer signal is weighted less in the underlying fusion algorithm, the algorithm may take more time to restabilize.

```
reset(FUSE)
FUSE.MagneticDisturbanceNoise = 20;
orientation = FUSE(accelReadings,gyroReadings,magReadings);
orientationEulerAngles = eulerd(orientation,'ZYX','frame');
figure(4)
plot(time,orientationEulerAngles(:,1), ...
    time,orientationEulerAngles(:,2), ...
    time,orientationEulerAngles(:,3))
xlabel('Time (s)')
```

```
ylabel('Rotation (degrees)')
legend('z-axis','y-axis','x-axis')
title('Filtered IMU Data with Magnetic Disturbance and Modified Properties')
```



Track Shaking 9-Axis IMU

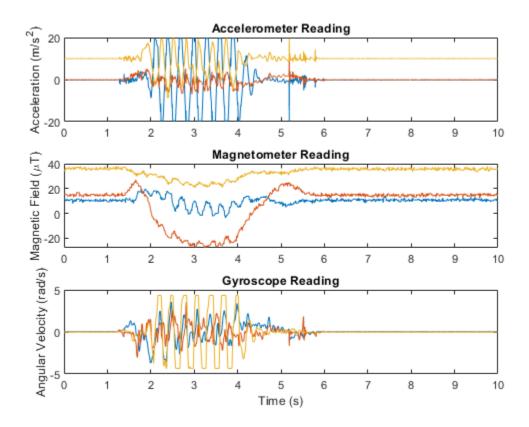
This example uses the ahrsfilter System object $^{\text{\tiny IM}}$ to fuse 9-axis IMU data from a sensor body that is shaken. Plot the quaternion distance between the object and its final resting position to visualize performance and how quickly the filter converges to the correct resting position. Then tune parameters of the ahrsfilter so that the filter converges more quickly to the ground-truth resting position.

Load IMUReadingsShaken into your current workspace. This data was recorded from an IMU that was shaken then laid in a resting position. Visualize the acceleration, magnetic field, and angular velocity as recorded by the sensors.

```
load 'IMUReadingsShaken' accelReadings gyroReadings magReadings SampleRate
numSamples = size(accelReadings,1);
time = (0:(numSamples-1))'/SampleRate;

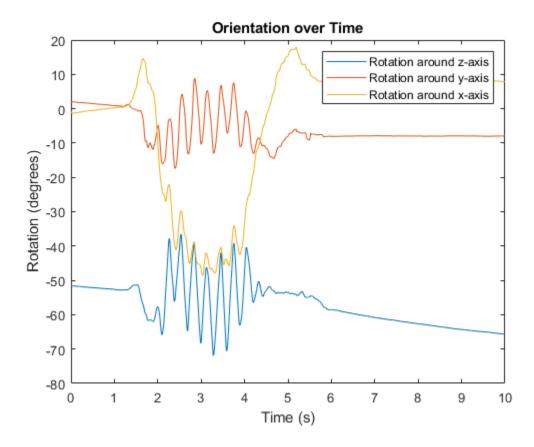
figure(1)
subplot(3,1,1)
plot(time,accelReadings)
title('Accelerometer Reading')
ylabel('Acceleration (m/s^2)')
```

```
subplot(3,1,2)
plot(time,magReadings)
title('Magnetometer Reading')
ylabel('Magnetic Field (\muT)')
subplot(3,1,3)
plot(time,gyroReadings)
title('Gyroscope Reading')
ylabel('Angular Velocity (rad/s)')
xlabel('Time (s)')
```



Create an ahrsfilter and then fuse the IMU data to determine orientation. The orientation is returned as a vector of quaternions; convert the quaternions to Euler angles in degrees. Visualize the orientation of the sensor body over time by plotting the Euler angles required, at each time step, to rotate the global coordinate system to the sensor body coordinate system.

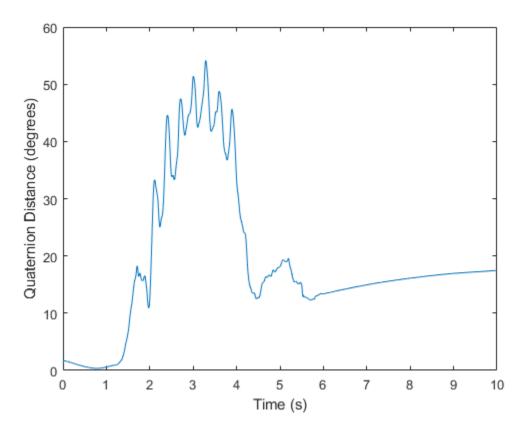
```
fuse = ahrsfilter('SampleRate', SampleRate);
orientation = fuse(accelReadings, gyroReadings, magReadings);
orientationEulerAngles = eulerd(orientation, 'ZYX', 'frame');
figure(2)
plot(time, orientationEulerAngles(:,1), ...
    time, orientationEulerAngles(:,2), ...
    time, orientationEulerAngles(:,3))
xlabel('Time (s)')
```



In the IMU recording, the shaking stops after approximately six seconds. Determine the resting orientation so that you can characterize how fast the ahrsfilter converges.

To determine the resting orientation, calculate the averages of the magnetic field and acceleration for the final four seconds and then use the ecompass function to fuse the data.

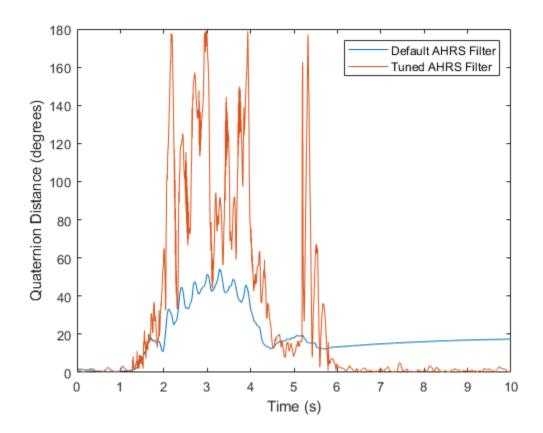
Visualize the quaternion distance from the resting position over time.



Modify the default ahrsfilter properties so that the filter converges to gravity more quickly. Increase the GyroscopeDriftNoise to 1e-2 and decrease the LinearAccelerationNoise to 1e-4. This instructs the ahrsfilter algorithm to weigh gyroscope data less and accelerometer data more. Because the accelerometer data provides the stabilizing and consistent gravity vector, the resulting orientation converges more quickly.

Reset the filter, fuse the data, and plot the results.

```
fuse.LinearAccelerationNoise = 1e-4;
fuse.GyroscopeDriftNoise = 1e-2;
reset(fuse)
orientation = fuse(accelReadings,gyroReadings,magReadings);
figure(3)
plot(time,rad2deg(dist(restingOrientation,orientation)))
legend('Default AHRS Filter','Tuned AHRS Filter')
```



Algorithms

Note: The following algorithm only applies to an NED reference frame.

The ahrsfilter uses the nine-axis Kalman filter structure described in [1]. The algorithm attempts to track the errors in orientation, gyroscope offset, linear acceleration, and magnetic disturbance to output the final orientation and angular velocity. Instead of tracking the orientation directly, the indirect Kalman filter models the error process, x, with a recursive update:

$$x_k = \begin{bmatrix} \theta_k \\ b_k \\ a_k \\ d_k \end{bmatrix} = F_k \begin{bmatrix} \theta_{k-1} \\ b_{k-1} \\ a_{k-1} \\ d_{k-1} \end{bmatrix} + w_k$$

where x_k is a 12-by-1 vector consisting of:

- θ_k -- 3-by-1 orientation error vector, in degrees, at time k
- b_k -- 3-by-1 gyroscope zero angular rate bias vector, in deg/s, at time k
- a_k -- 3-by-1 acceleration error vector measured in the sensor frame, in g, at time k
- d_k -- 3-by-1 magnetic disturbance error vector measured in the sensor frame, in μT , at time k

and where w_k is a 12-by-1 additive noise vector, and F_k is the state transition model.

Because x_k is defined as the error process, the *a priori* estimate is always zero, and therefore the state transition model, F_k , is zero. This insight results in the following reduction of the standard Kalman equations:

Standard Kalman equations:

$$x_{k}^{-} = F_{k}x_{k-1}^{+}$$

$$P_{k}^{-} = F_{k}P_{k-1}^{+}F_{k}^{T} + Q_{k}$$

$$y_{k} = z_{k} - H_{k}x_{k}^{-}$$

$$S_{k} = R_{k} + H_{k}P_{k}^{-}H_{k}^{T}$$

$$K_{k} = P_{k}^{-}H_{k}^{T}(S_{k})^{-1}$$

$$x_{k}^{+} = x_{k}^{-} + K_{k}y_{k}$$

$$P_{k}^{+} = P_{k} - K_{k}H_{k}P_{k}^{-}$$

Kalman equations used in this algorithm:

$$x_k^- = 0$$

$$P_k^- = Q_k$$

$$y_k = z_k$$

$$S_k = R_k + H_k P_k^- H_k^T$$

$$K_k = P_k^- H_k^T (S_k)^{-1}$$

$$x_k^+ = K_k y_k$$

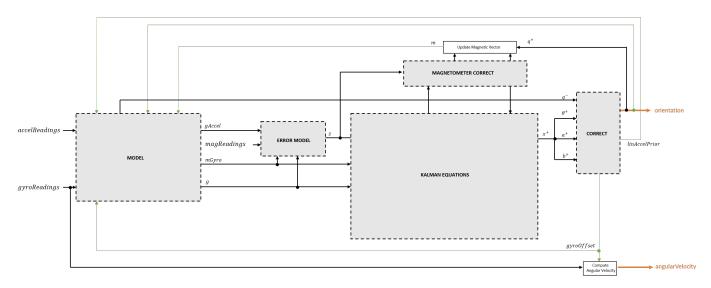
$$P_k^+ = P_k - K_k H_k P_k^-$$

where:

- x_k^- -- predicted (*a priori*) state estimate; the error process
- P_k^- -- predicted (a priori) estimate covariance
- y_k -- innovation
- S_k -- innovation covariance
- K_k -- Kalman gain
- x_k^+ -- updated (a posteriori) state estimate
- P_k^+ -- updated (a posteriori) estimate covariance

k represents the iteration, the superscript $^+$ represents an a posteriori estimate, and the superscript $^-$ represents an a priori estimate.

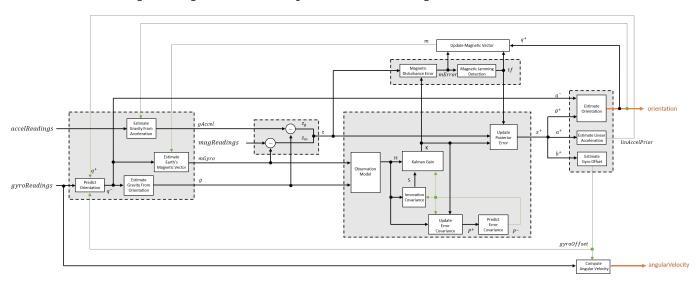
The graphic and following steps describe a single frame-based iteration through the algorithm.



Before the first iteration, the accelReadings, gyroReadings, and magReadings inputs are chunked into DecimationFactor-by-3 frames. For each chunk, the algorithm uses the most current accelerometer and magnetometer readings corresponding to the chunk of gyroscope readings.

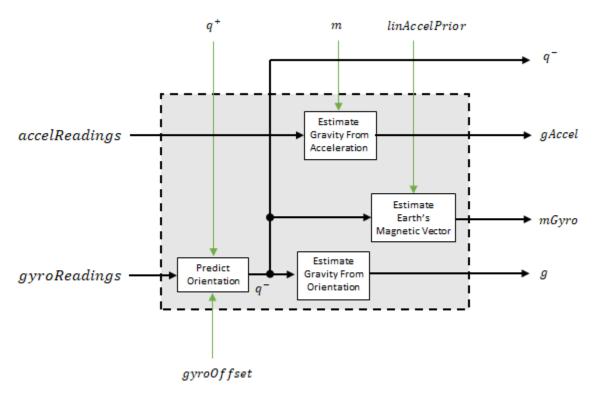
Detailed Overview

Walk through the algorithm for an explanation of each stage of the detailed overview.



Model

The algorithm models acceleration and angular change as linear processes.



Predict Orientation

The orientation for the current frame is predicted by first estimating the angular change from the previous frame:

$$\Delta \varphi_{N \times 3} = \frac{(gyroReadings_{N \times 3} - gyroOffset_{1 \times 3})}{fs}$$

where N is the decimation factor specified by the DecimationFactor property and fs is the sample rate specified by the SampleRate property.

The angular change is converted into quaternions using the rotvec quaternion construction syntax:

$$\Delta Q_{N \times 1} = \text{quaternion}(\Delta \varphi_{N \times 3}, 'rotvec')$$

The previous orientation estimate is updated by rotating it by ΔQ :

$$q_{1\times 1}^- = (q_{1\times 1}^+) \left(\prod_{n=1}^N \Delta Q_n\right)$$

During the first iteration, the orientation estimate, q^- , is initialized by **ecompass**.

Estimate Gravity from Orientation

The gravity vector is interpreted as the third column of the quaternion, q^- , in rotation matrix form:

$$g_{1\times 3}=(rPrior(:,3))^T$$

See [1] for an explanation of why the third column of *rPrior* can be interpreted as the gravity vector.

Estimate Gravity from Acceleration

A second gravity vector estimation is made by subtracting the decayed linear acceleration estimate of the previous iteration from the accelerometer readings:

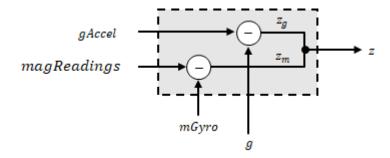
$$gAccel_{1 \times 3} = accelReadings_{1 \times 3} - linAccelprior_{1 \times 3}$$

Estimate Earth's Magnetic Vector

Earth's magnetic vector is estimated by rotating the magnetic vector estimate from the previous iteration by the *a priori* orientation estimate, in rotation matrix form:

$$mGyro_{1 \times 3} = ((rPrior)(m^T))^T$$

Error Model

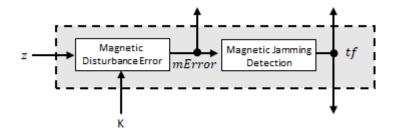


The error model combines two differences:

- The difference between the gravity estimate from the accelerometer readings and the gravity estimate from the gyroscope readings: $z_q = g gAccel$
- The difference between the magnetic vector estimate from the gyroscope readings and the magnetic vector estimate from the magnetometer: $z_m = mGyro magReadings$

Magnetometer Correct

The magnetometer correct estimates the error in the magnetic vector estimate and detects magnetic jamming.



Magnetometer Disturbance Error

The magnetic disturbance error is calculated by matrix multiplication of the Kalman gain associated with the magnetic vector with the error signal:

$$mError_{3 \times 1} = ((K(10:12,:)_{3 \times 6})(z_{1 \times 6})^T)^T$$

The Kalman gain, K, is the Kalman gain calculated in the current iteration.

Magnetic Jamming Detection

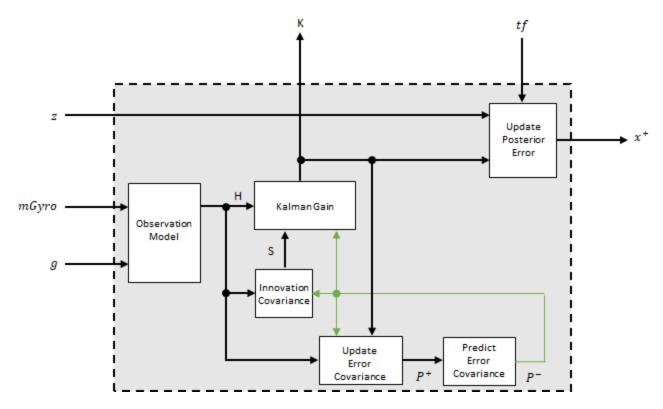
Magnetic jamming is determined by verifying that the power of the detected magnetic disturbance is less than or equal to four times the power of the expected magnetic field strength:

$$tf = \begin{cases} \text{true if } \sum |mError|^2 > (4)(\text{ExpectedMagneticFieldStrength})^2 \end{cases}$$

ExpectedMagneticFieldStrength is a property of ahrsfilter.

Kalman Equations

The Kalman equations use the gravity estimate derived from the gyroscope readings, g, the magnetic vector estimate derived from the gyroscope readings, mGyro, and the observation of the error process, z, to update the Kalman gain and intermediary covariance matrices. The Kalman gain is applied to the error signal, z, to output an a posteriori error estimate, x^+ .



Observation Model

The observation model maps the 1-by-3 observed states, g and mGyro, into the 6-by-12 true state, H.

The observation model is constructed as:

$$H_{3 \times 9} = \begin{bmatrix} 0 & g_z & -g_y & 0 & -\kappa g_z & \kappa g_y & 1 & 0 & 0 & 0 & 0 \\ -g_z & 0 & g_x & \kappa g_z & 0 & -\kappa g_x & 0 & 1 & 0 & 0 & 0 & 0 \\ g_y & -g_x & 0 & -\kappa g_y & \kappa g_x & 0 & 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & m_z & -m_y & 0 & -\kappa m_z & -\kappa m_y & 0 & 0 & -1 & 0 & 0 \\ -m_z & 0 & m_x & \kappa m_z & 0 & -\kappa m_x & 0 & 0 & 0 & 0 & -1 & 0 \\ m_y & -m_x & 0 & -\kappa m_y & \kappa m_x & 0 & 0 & 0 & 0 & 0 & -1 \end{bmatrix}$$

where g_x , g_y , and g_z are the x-, y-, and z-elements of the gravity vector estimated from the a priori orientation, respectively. m_x , m_y , and m_z are the x-, y-, and z-elements of the magnetic vector estimated from the a priori orientation, respectively. κ is a constant determined by the SampleRate and DecimationFactor properties: $\kappa = \text{DecimationFactor/SampleRate}$.

See sections 7.3 and 7.4 of [1] for a derivation of the observation model.

Innovation Covariance

The innovation covariance is a 6-by-6 matrix used to track the variability in the measurements. The innovation covariance matrix is calculated as:

$$S_{6x6} = R_{6x6} + (H_{6x12})(P_{12x12}^{-})(H_{6x12})^{T}$$

where

- *H* is the observation model matrix
- *P*⁻ is the predicted (*a priori*) estimate of the covariance of the observation model calculated in the previous iteration
- *R* is the covariance of the observation model noise, calculated as:

$$R_{6 \times 6} = \begin{bmatrix} accel_{\text{noise}} & 0 & 0 & 0 & 0 & 0 \\ 0 & accel_{\text{noise}} & 0 & 0 & 0 & 0 \\ 0 & 0 & accel_{\text{noise}} & 0 & 0 & 0 \\ 0 & 0 & 0 & mag_{\text{noise}} & 0 & 0 \\ 0 & 0 & 0 & 0 & mag_{\text{noise}} & 0 \\ 0 & 0 & 0 & 0 & 0 & mag_{\text{noise}} \end{bmatrix}$$

where

 $accel_{noise}$ = Accelerometer Noise + Linear Acceleration Noise + κ^2 (Gyroscope Drift Noise + Gyroscope Noise)

and

 $mag_{\text{noise}} = \text{MagnetometerNoise} + \text{MagneticDisturbanceNoise} + \kappa^2$ (GyroscopeDriftNoise + GyroscopeNoise)

The following properties define the observation model noise variance:

κ -- DecimationFactor/SampleRate

- AccelerometerNoise
- LinearAccelerationNoise
- GyroscopeDriftNoise
- GyroscopeNoise
- MagneticDisturbanceNoise
- MagnetometerNoise

Update Error Estimate Covariance

The error estimate covariance is a 12-by-12 matrix used to track the variability in the state.

The error estimate covariance matrix is updated as:

$$P_{12 \times 12}^+ = P_{12 \times 12}^- - (K_{12 \times 6})(H_{6 \times 12})(P_{12 \times 12}^-)$$

where K is the Kalman gain, H is the measurement matrix, and P^- is the error estimate covariance calculated during the previous iteration.

Predict Error Estimate Covariance

The error estimate covariance is a 12-by-12 matrix used to track the variability in the state. The *a priori* error estimate covariance, P^- , is set to the process noise covariance, Q, determined during the previous iteration. Q is calculated as a function of the *a posteriori* error estimate covariance, P^+ . When calculating Q, it is assumed that the cross-correlation terms are negligible compared to the autocorrelation terms, and are set to zero:

Q =

$P^+(1) + \kappa^2 P^+(40) + \beta + \eta$	0	0	$-\kappa (P^+(40) + \beta)$	0
0	$P^+(14) + \kappa^2 P^+(53) + \beta + \eta$	0	0	$-\kappa (P^+(53) +$
0	0	$P^{+}(27) + \kappa^{2}P^{+}(66) + \beta + \eta$	0	0
$-\kappa \big(P^+(40)+\beta\big)$	0	0	$P^+(40) + \beta$	0
0	$-\kappa \left(P^+(53) + \beta\right)$	0	0	$P^+(53) + \beta$
0	0	$-\kappa \left(P^+(66) + \beta\right)$	0	0
0	0	0	0	0
0	0	0	0	0
0	0	0	0	0
0	0	0	0	0
0	0	0	0	0
0	0	0	0	0

where

- P⁺ -- is the updated (a posteriori) error estimate covariance
- *K* -- DecimationFactor/SampleRate
- β -- GyroscopeDriftNoise
- η -- GyroscopeNoise
- ν -- LinearAcclerationDecayFactor
- ξ -- LinearAccelerationNoise
- σ -- Magnetic Disturbance Decay Factor
- γ -- MagneticDisturbanceNoise

See section 10.1 of [1] for a derivation of the terms of the process error matrix.

Kalman Gain

The Kalman gain matrix is a 12-by-6 matrix used to weight the innovation. In this algorithm, the innovation is interpreted as the error process, z.

The Kalman gain matrix is constructed as:

$$K_{12 \times 6} = (P_{12 \times 12}^{-})(H_{6 \times 12})^{T}((S_{6 \times 6})^{T})^{-1}$$

where

- *P*⁻ -- predicted error covariance
- *H* -- observation model
- S -- innovation covariance

Update a Posteriori Error

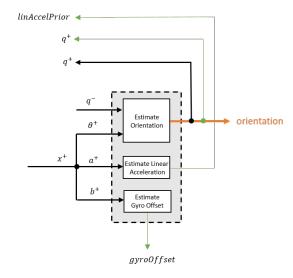
The *a posterior* error estimate is determined by combining the Kalman gain matrix with the error in the gravity vector and magnetic vector estimations:

$$x_{12 \times 1} = (K_{12 \times 6})(z_{1 \times 6})^T$$

If magnetic jamming is detected in the current iteration, the magnetic vector error signal is ignored, and the *a posterior* error estimate is calculated as:

$$x_{9 \times 1} = (K(1:9, 1:3)(z_a)^T$$

Correct



Estimate Orientation

The orientation estimate is updated by multiplying the previous estimation by the error:

$$q^+ = (q^-)(\theta^+)$$

Estimate Linear Acceleration

The linear acceleration estimation is updated by decaying the linear acceleration estimation from the previous iteration and subtracting the error:

$$linAccelPrior = (linAccelPrior_{k-1})\nu - b^+$$

where

• ν -- LinearAcclerationDecayFactor

Estimate Gyroscope Offset

The gyroscope offset estimation is updated by subtracting the gyroscope offset error from the gyroscope offset from the previous iteration:

$$gyroOffset = gyroOffset_{k-1} - a^+$$

Compute Angular Velocity

To estimate angular velocity, the frame of <code>gyroReadings</code> are averaged and the gyroscope offset computed in the previous iteration is subtracted:

$$angular Velocity_{1\times 3} = \frac{\sum gyroReadings_{N\times 3}}{N} - gyroOffset_{1\times 3}$$

where N is the decimation factor specified by the **DecimationFactor** property.

The gyroscope offset estimation is initialized to zeros for the first iteration.

Update Magnetic Vector

If magnetic jamming was not detected in the current iteration, the magnetic vector estimate, m, is updated using the a posteriori magnetic disturbance error and the a posteriori orientation.

The magnetic disturbance error is converted to the navigation frame:

$$mErrorNED_{1 \times 3} = ((rPost_{3 \times 3})^T (mError_{1 \times 3})^T)^T$$

The magnetic disturbance error in the navigation frame is subtracted from the previous magnetic vector estimate and then interpreted as inclination:

```
M = m - mErrorNED

inclination = atan2(M(3), M(1))
```

The inclination is converted to a constrained magnetic vector estimate for the next iteration:

- m(1) = (ExpectedMagneticFieldStrength)(cos(inclination))
- m(2) = 0
- m(3) = (ExpectedMagneticFieldStrength)(sin(inclination))

ExpectedMagneticFieldStrength is a property of ahrsfilter.

References

- [1] Open Source Sensor Fusion. https://github.com/memsindustrygroup/Open-Source-Sensor-Fusion/tree/master/docs
- [2] Roetenberg, D., H.J. Luinge, C.T.M. Baten, and P.H. Veltink. "Compensation of Magnetic Disturbances Improves Inertial and Magnetic Sensing of Human Body Segment Orientation." *IEEE Transactions on Neural Systems and Rehabilitation Engineering*. Vol. 13. Issue 3, 2005, pp. 395-405.

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

Usage notes and limitations:

See "System Objects in MATLAB Code Generation" (MATLAB Coder).

See Also

ecompass | gpsSensor | imuSensor | imufilter

Introduced in R2018b

tune

Tune ahrsfilter parameters to reduce estimation error

Syntax

```
tune(filter,sensorData,groundTruth)
tune(____,config)
```

Description

tune(filter, sensorData, groundTruth) adjusts the properties of the ahrsfilter filter object, filter, to reduce the root-mean-squared (RMS) quaternion distance error between the fused sensor data and the ground truth. The function uses the property values in the filter as the initial estimate for the optimization algorithm.

tune(,config) specifies the tuning configuration based on a tunerconfig object, config.

Examples

Tune ahrsfilter to Improve Orientation Estimate

Load recorded sensor data and ground truth data.

```
ld = load('ahrsfilterTuneData.mat');
qTrue = ld.groundTruth.Orientation; % true orientation
```

Create an arhsfitler object.

```
fuse = ahrsfilter;
```

Fuse the sensor data using the default, untuned filter.

```
qEstUntuned = fuse(ld.sensorData.Accelerometer, ...
ld.sensorData.Gyroscope, ld.sensorData.Magnetometer);
```

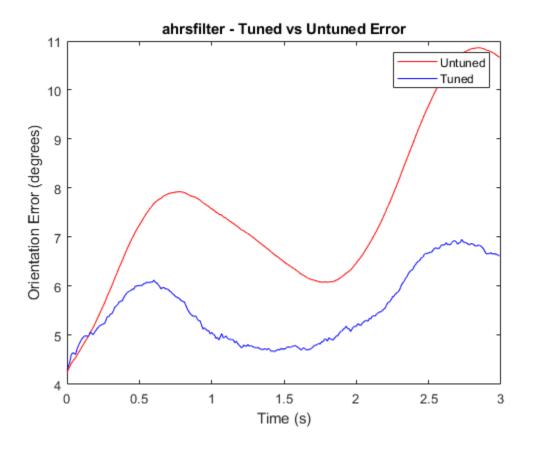
Create a tunerconfig object. Tune the ahrsfilter object to improve the orientation estimation based on the configuration.

```
config = tunerconfig('ahrsfilter');
tune(fuse,ld.sensorData,ld.groundTruth,config);
```

Iteration	Parameter	Metric
1	AccelerometerNoise	0.1345
1	GyroscopeNoise	0.1342
1	MagnetometerNoise	0.1341
1	GyroscopeDriftNoise	0.1341
1	LinearAccelerationNoise	0.1332
1	MagneticDisturbanceNoise	0.1324
1	LinearAccelerationDecayFactor	0.1317
1	MagneticDisturbanceDecayFactor	0.1316

_		
2	AccelerometerNoise	0.1316
2	GyroscopeNoise	0.1312
	, ,	
2	MagnetometerNoise	0.1311
2	GyroscopeDriftNoise	0.1311
2	LinearAccelerationNoise	0.1300
2	MagneticDisturbanceNoise	0.1292
2	-	0.1285
	LinearAccelerationDecayFactor	
2	MagneticDisturbanceDecayFactor	0.1285
3	AccelerometerNoise	0.1285
2		
3	GyroscopeNoise	0.1280
3 3 3	MagnetometerNoise	0.1279
2	GyroscopeDriftNoise	0.1279
2	· ·	
3	LinearAccelerationNoise	0.1267
3	MagneticDisturbanceNoise	0.1258
2		
3	LinearAccelerationDecayFactor	0.1253
3	MagneticDisturbanceDecayFactor	0.1253
4	AccelerometerNoise	0.1252
4	GyroscopeNoise	0.1247
4	MagnetometerNoise	0.1246
-		
4	GyroscopeDriftNoise	0.1246
4	LinearAccelerationNoise	0.1233
4	MagneticDisturbanceNoise	0.1224
-		
4	LinearAccelerationDecayFactor	0.1220
4	MagneticDisturbanceDecayFactor	0.1220
5	AccelerometerNoise	0.1220
5	GyroscopeNoise	0.1213
5	MagnetometerNoise	0.1212
5		
5	GyroscopeDriftNoise	0.1212
5	LinearAccelerationNoise	0.1200
_		
5 5	MagneticDisturbanceNoise	0.1190
5	LinearAccelerationDecayFactor	0.1187
5	MagneticDisturbanceDecayFactor	0.1187
6	AccelerometerNoise	0.1187
6	GyroscopeNoise	0.1180
6	MagnetometerNoise	0.1178
6	GyroscopeDriftNoise	0.1178
6	LinearAccelerationNoise	0.1167
6		
	MagneticDisturbanceNoise	0.1156
6	LinearAccelerationDecayFactor	0.1155
6	MagneticDisturbanceDecayFactor	0.1155
7	AccelerometerNoise	0.1155
7	GyroscopeNoise	0.1147
7	MagnetometerNoise	0.1145
7	GyroscopeDriftNoise	0.1145
7	LinearAccelerationNoise	0.1137
7		
	MagneticDisturbanceNoise	0.1126
7	LinearAccelerationDecayFactor	0.1125
7	MagneticDisturbanceDecayFactor	0.1125
8	AccelerometerNoise	0.1125
8	GyroscopeNoise	0.1117
8	MagnetometerNoise	0.1116
8	GyroscopeDriftNoise	0.1116
8	LinearAccelerationNoise	0.1112
8		
	MagneticDisturbanceNoise	0.1100
8	LinearAccelerationDecayFactor	0.1099
8	MagneticDisturbanceDecayFactor	0.1099
9	AccelerometerNoise	0.1099
9	GyroscopeNoise	0.1091

```
0.1090
                  MagnetometerNoise
                  GyroscopeDriftNoise
                                                      0.1090
    9
                  LinearAccelerationNoise
                                                      0.1090
    9
                  MagneticDisturbanceNoise
                                                      0.1076
    9
                  LinearAccelerationDecayFactor
                                                      0.1075
    9
                  MagneticDisturbanceDecayFactor
                                                      0.1075
    10
                  AccelerometerNoise
                                                      0.1075
    10
                  GyroscopeNoise
                                                      0.1066
    10
                  MagnetometerNoise
                                                      0.1064
    10
                  GvroscopeDriftNoise
                                                      0.1064
    10
                  LinearAccelerationNoise
                                                      0.1064
    10
                  MagneticDisturbanceNoise
                                                      0.1049
    10
                  LinearAccelerationDecayFactor
                                                      0.1047
    10
                  MagneticDisturbanceDecayFactor
                                                      0.1047
    11
                                                      0.1047
                  AccelerometerNoise
    11
                  GyroscopeNoise
                                                      0.1038
    11
                  MagnetometerNoise
                                                      0.1036
    11
                  GyroscopeDriftNoise
                                                      0.1036
    11
                  LinearAccelerationNoise
                                                      0.1036
    11
                  MagneticDisturbanceNoise
                                                      0.1016
    11
                  LinearAccelerationDecayFactor
                                                      0.1014
    11
                                                      0.1014
                  MagneticDisturbanceDecayFactor
    12
                  AccelerometerNoise
                                                      0.1014
    12
                  GyroscopeNoise
                                                      0.1005
    12
                                                      0.1002
                  MagnetometerNoise
    12
                                                      0.1002
                  GyroscopeDriftNoise
    12
                                                      0.1002
                  LinearAccelerationNoise
    12
                  MagneticDisturbanceNoise
                                                      0.0978
Fuse the sensor data using the tuned filter.
qEstTuned = fuse(ld.sensorData.Accelerometer, ...
    ld.sensorData.Gyroscope, ld.sensorData.Magnetometer);
Compare the tuned and untuned RMS error performances.
dUntuned = rad2deg(dist(qEstUntuned, qTrue));
dTuned = rad2deg(dist(qEstTuned, qTrue));
rmsUntuned = sqrt(mean(dUntuned.^2))
rmsUntuned = 7.7088
rmsTuned = sqrt(mean(dTuned.^2))
rmsTuned = 5.6033
Visualize the errors with respect to time.
N = numel(dUntuned);
t = (0:N-1)./ fuse.SampleRate;
plot(t, dUntuned, 'r', t, dTuned, 'b');
legend('Untuned', 'Tuned');
title('ahrsfilter - Tuned vs Untuned Error')
xlabel('Time (s)');
ylabel('Orientation Error (degrees)');
```



Input Arguments

filter — Filter object

ahrsfilter object

Filter object, specified as an ahrsfilter object.

sensorData — Sensor data

table

Sensor data, specified as a table. In each row, the sensor data is specified as:

- Accelerometer Accelerometer data, specified as a 1-by-3 vector of scalars in m²/s.
- Gyroscope Gyroscope data, specified as a 1-by-3 vector of scalars in rad/s.
- Magnetometer Magnetometer data, specified as a 1-by-3 vector of scalars in μT.

If you set the Cost property of the tuner configuration input, config, to Custom, then you can use other data types for the sensorData input based on your choice.

groundTruth — Ground truth data

timetable

Ground truth data, specified as a table. The table has only one column of Orientation data. In each row, the orientation is specified as a quaternion object or a 3-by-3 rotation matrix.

The function processes each row of the sensorData and groundTruth tables sequentially to calculate the state estimate and RMS error from the ground truth. Each row of the sensorData and the groundTruth tables must correspond to each other.

If you set the Cost property of the tuner configuration input, config, to Custom, then you can use other data types for the groundTruth input based on your choice.

config — Tuner configuration

tunerconfig object

Tuner configuration, specified as a tunerconfig object.

References

[1] Abbeel, P., Coates, A., Montemerlo, M., Ng, A.Y. and Thrun, S. Discriminative Training of Kalman Filters. In *Robotics: Science and systems*, Vol. 2, pp. 1, 2005.

See Also

Introduced in R2020b

altimeterSensor

Altimeter simulation model

Description

The altimeterSensor System object models receiving data from an altimeter sensor.

To model an altimeter:

- 1 Create the altimeterSensor object and set its properties.
- **2** Call the object with arguments, as if it were a function.

To learn more about how System objects work, see What Are System Objects?.

Creation

Syntax

```
altimeter = altimeterSensor
altimeter = altimeterSensor('ReferenceFrame',RF)
altimeter = altimeterSensor(____,Name,Value)
```

Description

altimeter = altimeterSensor returns an altimeterSensor System object that simulates altimeter readings.

altimeter = altimeterSensor('ReferenceFrame', RF) returns an altimeterSensor System object that simulates altimeter readings relative to the reference frame RF. Specify RF as 'NED' (North-East-Down) or 'ENU' (East-North-Up). The default value is 'NED'.

altimeter = altimeterSensor(____, Name, Value) sets each property Name to the specified Value. Unspecified properties have default values.

Properties

Unless otherwise indicated, properties are *nontunable*, which means you cannot change their values after calling the object. Objects lock when you call them, and the release function unlocks them.

If a property is tunable, you can change its value at any time.

For more information on changing property values, see System Design in MATLAB Using System Objects.

SampleRate — Update rate of sensor (Hz)

1 (default) | positive scalar

Update rate of sensor in Hz, specified as a positive scalar.

Data Types: single | double

ConstantBias — Constant offset bias (m)

0 (default) | scalar

Constant offset bias in meters, specified as a scalar.

Tunable: Yes

Data Types: single | double

NoiseDensity — Power spectral density of sensor noise (m/\sqrt{Hz})

0 (default) | nonnegative scalar

Power spectral density of sensor noise in m/VHz, specified as a nonnegative scalar.

Tunable: Yes

Data Types: single | double

BiasInstability — Instability of bias offset (m)

0 (default) | nonnegative scalar

Instability of the bias offset in meters, specified as a nonnegative scalar.

Tunable: Yes

Data Types: single | double

DecayFactor — Bias instability noise decay factor

0 (default) | scalar in the range [0,1]

Bias instability noise decay factor, specified as a scalar in the range [0,1]. A decay factor of 0 models the bias instability noise as a white noise process. A decay factor of 1 models the bias instability noise as a random walk process.

Tunable: Yes

Data Types: single | double

RandomStream — Random number source

'Global stream' (default) | 'mt19937ar with seed'

Random number source, specified as a character vector or string:

- 'Global stream' -- Random numbers are generated using the current global random number stream.
- 'mt19937ar with seed' -- Random numbers are generated using the mt19937ar algorithm with the seed specified by the Seed property.

Data Types: char | string

Seed — Initial seed

67 (default) | nonnegative integer scalar

Initial seed of an mt19937ar random number generator algorithm, specified as a nonnegative integer scalar.

Dependencies

To enable this property, set RandomStream to 'mt19937ar with seed'.

Data Types: single | double

Usage

Syntax

altimeterReadings = altimeter(position)

Description

altimeterReadings = altimeter(position) generates an altimeter sensor altitude reading
from the position input.

Input Arguments

position — Position of sensor in local navigation coordinate system (m)

N-by-3 matrix

Position of sensor in the local navigation coordinate system, specified as an *N*-by-3 matrix with elements measured in meters. *N* is the number of samples in the current frame.

Data Types: single | double

Output Arguments

altimeterReadings — Altitude of sensor relative to local navigation coordinate system (m)

N-element column vector

Altitude of sensor relative to the local navigation coordinate system in meters, returned as an N-element column vector. N is the number of samples in the current frame.

Data Types: single | double

Object Functions

To use an object function, specify the System object as the first input argument. For example, to release system resources of a System object named obj, use this syntax:

release(obj)

Common to All System Objects

step Run System object algorithm

release Release resources and allow changes to System object property values and input

characteristics

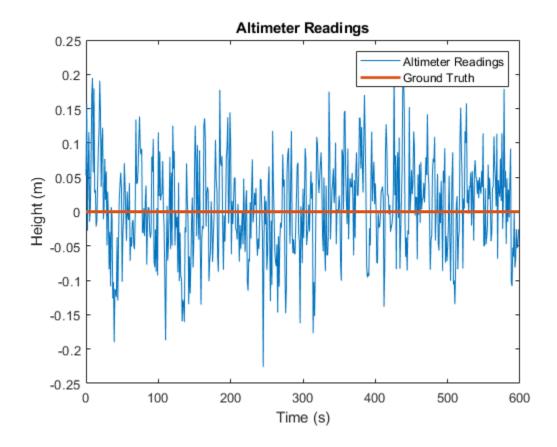
reset Reset internal states of System object

Examples

Generate Noisy Altimeter Readings from Stationary Input

Create an altimeterSensor System object[™] to model receiving altimeter sensor data. Assume a typical one Hz sample rate and a 10 minute simulation time. Set ConstantBias to 0.01, NoiseDensity to 0.05, BiasInstability to 0.05, and DecayFactor to 0.5.

```
Fs = 1;
duration = 60*10;
numSamples = duration*Fs;
altimeter = altimeterSensor('SampleRate',Fs, ...
                              'ConstantBias',0.01, ...
                              'NoiseDensity',0.05, ...
                              'BiasInstability',0.05, ...
                              'DecayFactor',0.5);
truePosition = zeros(numSamples,3);
Call altimeter with the specified truePosition to model noisy altimeter readings from a
stationary platform.
altimeterReadings = altimeter(truePosition);
Plot the true position and the altimeter sensor readings for height.
t = (0:(numSamples-1))/Fs;
plot(t,altimeterReadings)
hold on
plot(t,truePosition(:,3),'LineWidth',2)
hold off
title('Altimeter Readings')
xlabel('Time (s)')
ylabel('Height (m)')
legend('Altimeter Readings','Ground Truth')
```



Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

Usage notes and limitations:

See "System Objects in MATLAB Code Generation" (MATLAB Coder).

See Also

gpsSensor|imuSensor

complementaryFilter

Orientation estimation from a complementary filter

Description

The complementaryFilter System object fuses accelerometer, gyroscope, and magnetometer sensor data to estimate device orientation and angular velocity.

To estimate orientation using this object:

- 1 Create the complementaryFilter object and set its properties.
- **2** Call the object with arguments, as if it were a function.

To learn more about how System objects work, see What Are System Objects?.

Creation

Syntax

```
FUSE = complementaryFilter
FUSE = complementaryFilter('ReferenceFrame',RF)
FUSE = complementaryFilter(____,Name,Value)
```

Description

FUSE = complementaryFilter returns a complementaryFilter System object, FUSE, for sensor fusion of accelerometer, gyroscope, and magnetometer data to estimate device orientation and angular velocity.

FUSE = complementaryFilter('ReferenceFrame', RF) returns a complementaryFilter System object that fuses accelerometer, gyroscope, and magnetometer data to estimate device orientation relative to the reference frame RF. Specify RF as 'NED' (North-East-Down) or 'ENU' (East-North-Up). The default value is 'NED'.

FUSE = complementaryFilter(____, Name, Value) sets each property Name to the specified Value. Unspecified properties have default values.

Properties

Unless otherwise indicated, properties are *nontunable*, which means you cannot change their values after calling the object. Objects lock when you call them, and the release function unlocks them.

If a property is *tunable*, you can change its value at any time.

For more information on changing property values, see System Design in MATLAB Using System Objects.

SampleRate — Input sample rate of sensor data (Hz)

100 (default) | positive scalar

Input sample rate of the sensor data in Hz, specified as a positive scalar.

Tunable: No

Data Types: single | double

AccelerometerGain — Accelerometer gain

0.01 (default) | real scar in [0, 1]

Accelerometer gain, specified as a real scalar in the range of [0, 1]. The gain determines how much the accelerometer measurement is trusted over the gyroscope measurement for orientation estimation. This property is tunable.

Data Types: single | double

MagnetometerGain — Magnetometer gain

0.01 (default) | real scar in [0, 1]

Magnetometer gain, specified as a real scalar in the range of [0, 1]. The gain determines how much the magnetometer measurement is trusted over the gyroscope measurement for orientation estimation. This property is tunable.

Data Types: single | double

HasMagnetometer — Enable magnetometer input

true (default) | false

Enable magnetometer input, specified as true or false.

Data Types: logical

OrientationFormat — Output orientation format

```
'quaternion' (default) | 'Rotation matrix'
```

Output orientation format, specified as 'quaternion' or 'Rotation matrix'. The size of the output depends on the output orientation format:

- 'quaternion' -- Output is an *N*-by-1 quaternion.
- 'Rotation matrix' -- Output is a 3-by-3-by-*N* rotation matrix.

N is the number of samples.

Data Types: char | string

Usage

Syntax

```
[orientation,angularVelocity] = FUSE(accelReadings,gyroReadings,magReadings)
[orientation,angularVelocity] = FUSE(accelReadings,gyroReadings)
```

Description

[orientation, angular Velocity] = FUSE(accelReadings, gyroReadings, magReadings) fuses accelerometer, gyroscope, and magnetometer data to compute orientation and angular velocity. To use this syntax, set the HasMagnetometer property as true.

[orientation, angular Velocity] = FUSE (accelReadings, gyroReadings) fuses accelerometer and gyroscope data to compute orientation and angular velocity. To use this syntax, set the HasMagnetometer property as false.

Input Arguments

accelReadings — Accelerometer readings in sensor body coordinate system (m/s²)

N-bv-3 matrix

Accelerometer readings in the sensor body coordinate system in m/s^2 , specified as an N-by-3 matrix. N is the number of samples, and the three columns of accelReadings represent the $[x\ y\ z]$ measurements. Accelerometer readings are assumed to correspond to the sample rate specified by the SampleRate property. In the filter, the gravity constant g is assumed to be 9.81 m/s².

Data Types: single | double

gyroReadings — Gyroscope readings in sensor body coordinate system (rad/s)

N-by-3 matrix

Gyroscope readings in the sensor body coordinate system in rad/s, specified as an N-by-3 matrix. N is the number of samples, and the three columns of <code>gyroReadings</code> represent the $[x\ y\ z]$ measurements. Gyroscope readings are assumed to correspond to the sample rate specified by the <code>SampleRate</code> property.

Data Types: single | double

magReadings — Magnetometer readings in sensor body coordinate system (μT)

N-by-3 matrix

Magnetometer readings in the sensor body coordinate system in μT , specified as an N-by-3 matrix. N is the number of samples, and the three columns of magReadings represent the $[x\ y\ z]$ measurements. Magnetometer readings are assumed to correspond to the sample rate specified by the SampleRate property.

Data Types: single | double

Output Arguments

orientation — Orientation that rotates quantities from local navigation coordinate system to sensor body coordinate system

N-by-1 array of quaternions (default) | 3-by-3-by-N array

Orientation that rotates quantities from the local navigation coordinate system to the body coordinate system, returned as quaternions or an array. The size and type of orientation depends on whether the OrienationFormat property is set to 'quaternion' or 'Rotation matrix':

- 'quaternion' -- the output is an *N*-by-1 vector of quaternions, where *N* is the number of samples.
- 'Rotation matrix' the output is a 3-by-3-by-N array of rotation matrices, where N is the number of samples.

Data Types: quaternion | single | double

angularVelocity — Angular velocity in sensor body coordinate system (rad/s) N-by-3 array (default)

Angular velocity expressed in the sensor body coordinate system in rad/s, returned as an N-by-3 array, where N is the number of samples.

```
Data Types: single | double
```

Object Functions

To use an object function, specify the System object as the first input argument. For example, to release system resources of a System object named obj, use this syntax:

```
release(obj)
```

Common to All System Objects

step Run System object algorithm

release Release resources and allow changes to System object property values and input

characteristics

reset Reset internal states of System object

clone Create duplicate System object isLocked Determine if System object is in use

Examples

Estimate Orientation from Recorded IMU Data

Load the rpy_9axis file, which contains recorded accelerometer, gyroscope, and magnetometer sensor data from a device oscillating in pitch (around *y*-axis), then yaw (around *z*-axis), and then roll (around *x*-axis). The file also contains the sample rate of the recording.

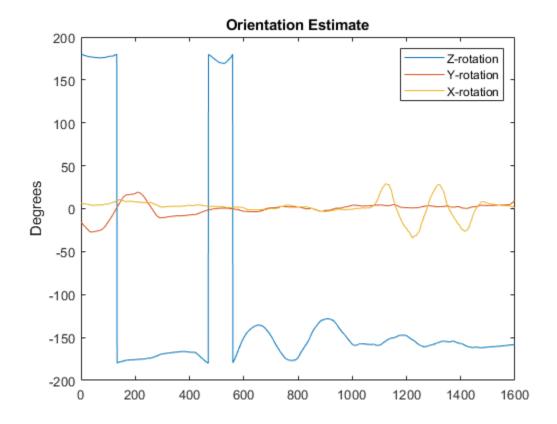
```
ld = load('rpy_9axis.mat');
accel = ld.sensorData.Acceleration;
gyro = ld.sensorData.AngularVelocity;
mag = ld.sensorData.MagneticField;
```

Create a complementary filter object with sample rate equal to the frequency of the data.

```
Fs = ld.Fs; % Hz
fuse = complementaryFilter('SampleRate', Fs);
```

Fuse accelerometer, gyroscope, and magnetometer data using the filter.

```
q = fuse(accel, gyro, mag);
Visualize the results.
plot(eulerd( q, 'ZYX', 'frame'));
title('Orientation Estimate');
legend('Z-rotation', 'Y-rotation', 'X-rotation');
ylabel('Degrees');
```



References

[1] Valenti, R., I. Dryanovski, and J. Xiao. "Keeping a good attitude: A quaternion-based orientation filter for IMUs and MARGs." *Sensors.* Vol. 15, Number 8, 2015, pp. 19302-19330.

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder $^{\text{\tiny TM}}$.

See Also

ahrsfilter|imufilter

insfilterAsync

Estimate pose from asynchronous MARG and GPS data

Description

The insfilterAsync object implements sensor fusion of MARG and GPS data to estimate pose in the NED (or ENU) reference frame. MARG (magnetic, angular rate, gravity) data is typically derived from magnetometer, gyroscope, and accelerometer data, respectively. The filter uses a 28-element state vector to track the orientation quaternion, velocity, position, MARG sensor biases, and geomagnetic vector. The insfilterAsync object uses a continuous-discrete extended Kalman filter to estimate these quantities.

Creation

Syntax

```
filter = insfilterAsync
filter = insfilterAsync('ReferenceFrame',RF)
filter = insfilterAsync(____,Name,Value)
```

Description

filter = insfilterAsync creates an insfilterAsync object to fuse asynchronous MARG and GPS data with default property values.

filter = insfilterAsync('ReferenceFrame', RF) allows you to specify the reference frame, RF, of the filter. Specify RF as 'NED' (North-East-Down) or 'ENU' (East-North-Up). The default value is 'NED'.

filter = insfilterAsync(____, Name, Value) also allows you set properties of the created filter using one or more name-value pairs. Enclose each property name in single quotes.

Properties

ReferenceLocation — Reference location (deg, deg, meters)

[0 0 0] (default) | three-element positive row vector

Reference location, specified as a three-element row vector in geodetic coordinates (latitude, longitude, and altitude). Altitude is the height above the reference ellipsoid model, WGS84. The reference location units are [degrees degrees meters].

Data Types: single | double

QuaternionNoise — Additive quaternion process noise variance

[1e-6 1e-6 1e-6] (default) | scalar | four-element row vector

Additive quaternion process noise variance, specified as a scalar or four-element vector of quaternion parts.

Data Types: single | double

Angular Velocity Noise — Additive angular velocity process noise in local navigation coordinate system $((rad/s)^2)$

[0.005 0.005 0.005] (default) | scalar | three-element row vector

Additive angular velocity process noise in the local navigation coordinate system in (rad/s)², specified as a scalar or three-element row vector of positive real finite numbers.

- If AngularVelocityNoise is a row vector, the elements correspond to the noise in the *x*, *y*, and *z* axes of the local navigation coordinate system, respectively.
- If Angular Velocity Noise is a scalar, the single element is applied to each axis.

Data Types: single | double

PositionNoise — Additive position process noise variance in local navigation coordinate system (m^2)

[1e-6 1e-6] (default) | scalar | three-element row vector

Additive position process noise in the local navigation coordinate system in m^2 , specified as a scalar or three-element row vector of positive real finite numbers.

- If PositionNoise is a row vector, the elements correspond to the noise in the *x*, *y*, and *z* axes of the local navigation coordinate system, respectively.
- If PositionNoise is a scalar, the single element is applied to each axis.

Data Types: single | double

VelocityNoise — Additive velocity process noise variance in local navigation coordinate system $((m/s)^2)$

[1e-6 1e-6] (default) | scalar | three-element row vector

Additive velocity process noise in the local navigation coordinate system in $(m/s)^2$, specified as a scalar or three-element row vector of positive real finite numbers.

- If VelocityNoise is a row vector, the elements correspond to the noise in the x, y, and z axes of the local navigation coordinate system, respectively.
- If VelocityNoise is a scalar, the single element is applied to each axis.

Data Types: single | double

AccelerationNoise — Additive acceleration process noise variance in local navigation coordinate system $((m/s^2)^2)$

[50 50 50] (default) | scalar | three-element row vector

Additive acceleration process noise in $(m/s^2)^2$, specified as a scalar or three-element row vector of positive real finite numbers.

- If AccelerationNoise is a row vector, the elements correspond to the noise in the x, y, and z axes of the local navigation coordinate system, respectively.
- If AccelerationNoise is a scalar, the single element is applied to each axis.

Data Types: single | double

GyroscopeBiasNoise — Additive process noise variance from gyroscope bias ((rad/s)²)

[1e-10 1e-10 1e-10] (default) | scalar | three-element row vector

Additive process noise variance from the gyroscope bias in $(rad/s)^2$, specified as a scalar or three-element row vector of positive real finite numbers.

- If GyroscopeBiasNoise is a row vector, the elements correspond to the noise in the x, y, and z axes of the gyroscope, respectively.
- If GyroscopeBiasNoise is a scalar, the single element is applied to each axis.

Data Types: single | double

AccelerometerBiasNoise — Additive process noise variance from accelerometer bias $((m/s^2)^2)$

[1e-4 1e-4] (default) | positive scalar | three-element row vector

Additive process noise variance from accelerometer bias in $(m/s^2)^2$, specified as a scalar or three-element row vector of positive real numbers.

- If AccelerometerBiasNoise is a row vector, the elements correspond to the noise in the x, y, and z axes of the accelerometer, respectively.
- If AccelerometerBiasNoise is a scalar, the single element is applied to each axis.

GeomagneticVectorNoise — Additive process noise variance of geomagnetic vector in local navigation coordinate system (μT^2)

[1e-6 1e-6] (default) | positive scalar | three-element row vector

Additive process noise variance of geomagnetic vector in μT^2 , specified as a scalar or three-element row vector of positive real numbers.

- If GeomagneticVectorNoise is a row vector, the elements correspond to the noise in the x, y, and z axes of the local navigation coordinate system, respectively.
- If GeomagneticVectorNoise is a scalar, the single element is applied to each axis.

MagnetometerBiasNoise — Additive process noise variance from magnetometer bias (μT^2) [0.1 0.1] (default) | positive scalar | three-element row vector

Additive process noise variance from magnetometer bias in μT^2 , specified as a scalar or three-element row vector of positive real numbers.

- If MagnetometerBiasNoise is a row vector, the elements correspond to the noise in the x, y, and z axes of the magnetometer, respectively.
- If MagnetometerBiasNoise is a scalar, the single element is applied to each axis.

State — State vector of extended Kalman filter

28-element column vector

State vector of the extended Kalman filter. The state values represent:

State	Units	Index
Orientation (quaternion parts)	N/A	1:4
Angular Velocity (XYZ)	rad/s	5:7

State	Units	Index
Position (NED or ENU)	m	8:10
Velocity (NED or ENU)	m/s	11:13
Acceleration (NED or ENU)	m/s ²	14:16
Accelerometer Bias (XYZ)	m/s ²	17:19
Gyroscope Bias (XYZ)	rad/s	20:22
Geomagnetic Field Vector (NED or ENU)	μТ	23:25
Magnetometer Bias (XYZ)	μΤ	26:28

The default initial state corresponds to an object at rest located at $[0\ 0\ 0]$ in geodetic LLA coordinates.

Data Types: single | double

StateCovariance — State error covariance for extended Kalman filter

eye(28) (default) | 28-by-28 matrix

State error covariance for the extended Kalman filter, specified as a 28-by-28-element matrix of real numbers.

Data Types: single | double

Object Functions

predict	Update states based on motion model for insfilterAsync
fuseaccel	Correct states using accelerometer data for insfilterAsync
fusegyro	Correct states using gyroscope data for insfilterAsync
fusemag	Correct states using magnetometer data for insfilterAsync
fusegps	Correct states using GPS data for insfilterAsync
correct	Correct states using direct state measurements for insfilterAsync
residual	Residuals and residual covariances from direct state measurements for insfilterAsync
residualaccel	Residuals and residual covariance from accelerometer measurements for
	insfilterAsync
residualgps	Residuals and residual covariance from GPS measurements for insfilterAsync
residualmag	Residuals and residual covariance from magnetometer measurements for
	insfilterAsync
residualgyro	Residuals and residual covariance from gyroscope measurements for insfilterAsync
pose	Current position, orientation, and velocity estimate for insfilterAsync
reset	Reset internal states for insfilterAsync
stateinfo	Display state vector information for insfilterAsync
copy	Create copy of insfilterAsync
tune	Tune insfilterAsync parameters to reduce estimation error
tunernoise	Noise structure of fusion filter

Examples

Estimate Pose of UAV

Load logged sensor data and ground truth pose.

```
load('uavshort.mat','refloc','initstate','imuFs', ...
  'accel','gyro','mag','lla','gpsvel', ...
  'trueOrient','truePos')
```

Create an INS filter to fuse asynchronous MARG and GPS data to estimate pose.

```
filt = insfilterAsync;
filt.ReferenceLocation = refloc;
filt.State = [initstate(1:4);0;0;0;initstate(5:10);0;0;0;initstate(11:end)];
```

Define sensor measurement noises. The noises were determined from datasheets and experimentation.

```
Rmag = 80;
Rvel = 0.0464;
Racc = 800;
Rgyro = 1e-4;
Rpos = 34;
```

Preallocate variables for position and orientation. Allocate a variable for indexing into the GPS data.

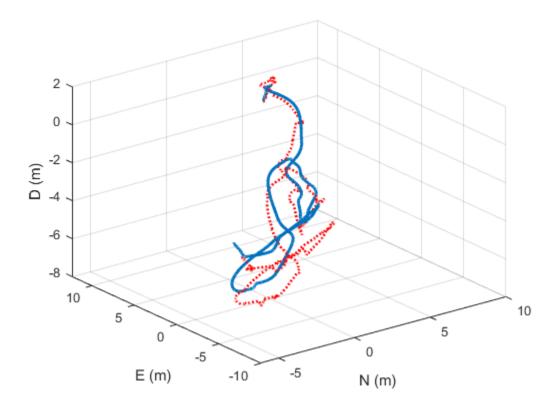
```
N = size(accel,1);
p = zeros(N,3);
q = zeros(N,1,'quaternion');
gpsIdx = 1;
```

Fuse accelerometer, gyroscope, magnetometer, and GPS data. The outer loop predicts the filter forward one time step and fuses accelerometer and gyroscope data at the IMU sample rate.

```
for ii = 1:N
    % Predict the filter forward one time step
    predict(filt,1./imuFs);
    % Fuse accelerometer and gyroscope readings
    fuseaccel(filt,accel(ii,:),Racc);
    fusegyro(filt,gyro(ii,:),Rgyro);
    % Fuse magnetometer at 1/2 the IMU rate
    if ~mod(ii, fix(imuFs/2))
        fusemag(filt,mag(ii,:),Rmag);
   % Fuse GPS once per second
    if ~mod(ii,imuFs)
        fusegps(filt,lla(gpsIdx,:),Rpos,gpsvel(gpsIdx,:),Rvel);
        gpsIdx = gpsIdx + 1;
    end
   % Log the current pose estimate
    [p(ii,:),q(ii)] = pose(filt);
end
```

Calculate the RMS errors between the known true position and orientation and the output from the asynchronous IMU filter.

```
posErr = truePos - p;
qErr = rad2deg(dist(true0rient,q));
pRMS = sqrt(mean(posErr.^2));
qRMS = sqrt(mean(qErr.^2));
fprintf('Position RMS Error\n');
Position RMS Error
fprintf('\tX: %.2f, Y: %.2f, Z: %.2f (meters)\n\n',pRMS(1),pRMS(2),pRMS(3));
   X: 0.55, Y: 0.71, Z: 0.74 (meters)
fprintf('Quaternion Distance RMS Error\n');
Ouaternion Distance RMS Error
fprintf('\t%.2f (degrees)\n\n', qRMS);
    4.72 (degrees)
Visualize the true position and the estimated position.
plot3(truePos(:,1),truePos(:,2),truePos(:,3),'LineWidth',2)
hold on
plot3(p(:,1),p(:,2),p(:,3),'r:','LineWidth',2)
grid on
xlabel('N (m)')
ylabel('E (m)')
zlabel('D (m)')
```



Algorithms

Dynamic Model Used in insfilterAsync

Note: The following algorithm only applies to an NED reference frame.

insfilterAsync implements a 28-axis continuous-discrete extended Kalman filter using sequential fusion. The filter relies on the assumption that individual sensor measurements are uncorrelated. The filter uses an omnidirectional motion model and assumes constant angular velocity and constant acceleration. The state is defined as:

```
q_0
                           q_1
                           q_2
                           q_3
                      angVel_X
                      angVel_{Y}
                      angVel<sub>7</sub>
                     position<sub>N</sub>
                     position<sub>E</sub>
                     position<sub>D</sub>
                          \nu_{
m N}
                          \nu_{
m E}
                          \nu_{
m D}
                       accel_N
\chi =
                       accel_{\rm F}
                       accel<sub>D</sub>
                    accelbias<sub>X</sub>
                    accelbias<sub>Y</sub>
                    accelbias<sub>7</sub>
                    gyrobias_X
                    gyrobias_{Y}
                    gyrobias_Z
       geomagneticFieldVector_N
       geomagneticFieldVector_{E}
       geomagneticFieldVector<sub>D</sub>
                     magbias_X
                     magbias<sub>Y</sub>
                     magbias<sub>7</sub>
```

where

- q_0 , q_1 , q_2 , q_3 Parts of orientation quaternion. The orientation quaternion represents a frame rotation from the platform's current orientation to the local NED coordinate system.
- angVel_x, angVel_y, angVel_z -- Angular velocity relative to the platform's body frame.
- $position_N$, $position_E$, $position_D$ -- Position of the platform in the local NED coordinate system.
- $\nu_{\rm N}, \nu_{\rm E}, \nu_{\rm D}$ -- Velocity of the platform in the local NED coordinate system.
- *accel*_N, *accel*_E, *accel*_D -- Acceleration of the platform in the local NED coordinate system.
- accelbias_x, accelbias_y, accelbias_z -- Bias in the accelerometer reading.
- *gyrobias*_X, *gyrobias*_Y, *gyrobias*_Z -- Bias in the gyroscope reading.

- $geomagneticFieldVector_N$, $geomagneticFieldVector_E$, $geomagneticFieldVector_D$ Estimate of the geomagnetic field vector at the reference location.
- $magbias_X$, $magbias_Y$, $magbias_Z$ Bias in the magnetometer readings.

Given the conventional formation of the process equation, $\dot{x} = f(x) + w$, w is the process noise, \dot{x} is the derivative of x, and:

	$\left[\frac{-(q_1)(angVel_X) - (q_2)(angVel_Y) - (q_3)(angVel_Z)}{2}\right]$
	Δ
	$\frac{(q_0)(angVel_X) - (q_3)(angVel_Y) + (q_1)(angVel_Z)}{2}$
	2
	$\frac{(q_3)(angVel_X) + (q_0)(angVel_Y) - (q_1)(angVel_Z)}{2}$
	$\frac{(q_1)(angVel_X) - (q_2)(angVel_Y) + (q_0)(angVel_Z)}{(q_1)(angVel_X) - (q_2)(angVel_Y)}$
	2
	0
	0
	0
	$ u_{ m N}$
	$ u_{ m E}$
	$ u_{ m D}$
	$\mathit{accel}_{\mathrm{N}}$
.	$\mathit{accel}_{\mathrm{E}}$
f(x) =	accel_{D}
	0
	0
	0
	0
	0
	0
	0
	0
	0
	0
	0
	0
	0
	0
	0

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder $^{\text{\tiny TM}}$.

See Also

insfilterErrorState|insfilterMARG|insfilterNonholonomic

correct

Correct states using direct state measurements for insfilterAsync

Syntax

correct(FUSE,idx,measurement,measurementCovariance)

Description

correct(FUSE,idx,measurement,measurementCovariance) corrects the state and state estimation error covariance based on the measurement and measurement covariance. The measurement maps directly to the state specified by the indices idx.

Input Arguments

FUSE — insfilterAsync object

object

insfilterAsync, specified as an object.

idx — State vector index of measurement to correct

N-element vector of increasing integers in the range [1, 28]

State vector index of measurement to correct, specified as an N-element vector of increasing integers in the range [1, 28].

The state values represent:

State	Units	Index
Orientation (quaternion parts)	N/A	1:4
Angular Velocity (XYZ)	rad/s	5:7
Position (NED)	m	8:10
Velocity (NED)	m/s	11:13
Acceleration (NED)	m/s ²	14:16
Accelerometer Bias (XYZ)	m/s ²	17:19
Gyroscope Bias (XYZ)	rad/s	20:22
Geomagnetic Field Vector (NED)	μТ	23:25
Magnetometer Bias (XYZ)	μΤ	26:28

Data Types: single | double

measurement — Direct measurement of state

N-element vector

Direct measurement of state, specified as an N-element vector. N is the number of elements of the index argument, idx.

Data Types: single | double

measurementCovariance — Covariance of measurement

scalar | *N*-element vector | *N*-by-*N* matrix

Covariance of measurement, specified as a scalar, N-element vector, or N-by-N matrix. N is the number of elements of the index argument, idx.

Data Types: single | double

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

insfilter|insfilterAsync

copy

Create copy of insfilterAsync

Syntax

newFilter = copy(filter)

Description

newFilter = copy(filter) returns a copy of the insfilterAsync, filter, that has exactly the same property values.

Input Arguments

filter — Filter to be copied

insfilterAsync

Filter to be copied, specified as an insfilterAsync object.

Output Arguments

newFilter — New copied filter

insfilterAsync

New copied filter, returned as an insfilterAsync object.

See Also

insfilterAsync

Introduced in R2020b

fuseaccel

Correct states using accelerometer data for insfilterAsync

Syntax

[res,resCov] = fuseaccel(FUSE,acceleration,accelerationCovariance)

Description

[res,resCov] = fuseaccel(FUSE,acceleration,accelerationCovariance) fuses
accelerometer data to correct the state estimate.

Input Arguments

FUSE — insfilterAsync object

object

insfilterAsync, specified as an object.

acceleration — Accelerometer readings in local sensor body coordinate system (m/s²)

3-element row vector

Accelerometer readings in local sensor body coordinate system in m/s², specified as a 3-element row vector

Data Types: single | double

accelerationCovariance — Acceleration error covariance of accelerometer measurement $((m/s^2)^2)$

scalar | 3-element row vector | 3-by-3 matrix

Acceleration error covariance of the accelerometer measurement in $(m/s^2)^2$, specified as a scalar, 3-element row vector, or 3-by-3 matrix.

Data Types: single | double

Output Arguments

res - Residual

1-by-3 vector of real values

Residual, returned a 1-by-3 vector of real values in m/s².

resCov — Residual covariance

3-by-3 matrix of real values

Residual covariance, returned as a 3-by-3 matrix of real values in $(m/s^2)^2$.

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder $^{\text{\tiny TM}}$.

See Also

insfilter|insfilterAsync

fusegps

Correct states using GPS data for insfilterAsync

Syntax

```
[res,resCov] = fusegps(FUSE,position,positionCovariance)
[res,resCov] = fusegps(FUSE,position,positionCovariance,velocity,
velocityCovariance)
```

Description

[res,resCov] = fusegps(FUSE,position,positionCovariance) fuses GPS position data to correct the state estimate.

[res,resCov] = fusegps(FUSE,position,positionCovariance,velocity,
velocityCovariance) fuses GPS position and velocity data to correct the state estimate.

Input Arguments

FUSE — insfilterAsync object

object

insfilterAsync, specified as an object.

position — Position of GPS receiver (LLA)

3-element row vector

Position of GPS receiver in geodetic latitude, longitude, and altitude (LLA) specified as a real finite 3-element row vector. Latitude and longitude are in degrees with north and east being positive. Altitude is in meters.

Data Types: single | double

positionCovariance — Position measurement covariance of GPS receiver (m²)

3-by-3 matrix

Position measurement covariance of GPS receiver in m², specified as a 3-by-3 matrix.

Data Types: single | double

velocity — Velocity of GPS receiver in local NED coordinate system (m/s)

3-element row vector

Velocity of the GPS receiver in the local NED coordinate system in m/s, specified as a 3-element row vector.

Data Types: single | double

velocityCovariance — Velocity measurement covariance of GPS receiver (m/s²)

3-by-3 matrix

Velocity measurement covariance of the GPS receiver in the local NED coordinate system in m/s², specified as a 3-by-3 matrix.

Data Types: single | double

Output Arguments

res — Position and velocity residual

1-by-6 vector of real values

Position and velocity residual, returned as a 1-by-6 vector of real values in m and m/s, respectively.

resCov — Residual covariance

6-by-6 matrix of real values

Residual covariance, returned as a 6-by-6 matrix of real values.

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

insfilter|insfilterAsync|insfilterMARG

fusegyro

Correct states using gyroscope data for insfilterAsync

Syntax

[res,resCov] = fusegyro(FUSE,gyroReadings,gyroCovariance)

Description

[res,resCov] = fusegyro(FUSE,gyroReadings,gyroCovariance) fuses gyroscope data to correct the state estimate.

Input Arguments

FUSE — insfilterAsync object

object

insfilterAsync, specified as an object.

gyroReadings — Gyroscope readings in local sensor body coordinate system (rad/s)

3-element row vector

Gyroscope readings in local sensor body coordinate system in rad/s, specified as a 3-element row vector.

Data Types: single | double

gyroCovariance — Covariance of gyroscope measurement error ((rad/s)²)

scalar | 3-element row vector | 3-by-3 matrix

Covariance of gyroscope measurement error in $(rad/s)^2$, specified as a scalar, 3-element row vector, or 3-by-3 matrix.

Data Types: single | double

Output Arguments

res — Residual

1-by-3 vector of real values

Residual, returned as a 1-by-3 vector of real values in rad/s.

resCov — Residual covariance

3-by-3 matrix of real values

Residual covariance, returned as a 3-by-3 matrix of real values in (rad/s)².

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder $^{\text{\tiny TM}}$.

See Also

insfilter|insfilterAsync

fusemag

Correct states using magnetometer data for insfilterAsync

Syntax

[res,resCov] = fusemag(FUSE,magReadings,magReadingsCovariance)

Description

[res,resCov] = fusemag(FUSE,magReadings,magReadingsCovariance) fuses
magnetometer data to correct the state estimate.

Input Arguments

FUSE — insfilterAsync object

object

insfilterAsync, specified as an object.

magReadings — Magnetometer readings (μT)

3-element row vector

Magnetometer readings in μT , specified as a 3-element row vector of finite real numbers.

Data Types: single | double

magReadingsCovariance — Magnetometer readings error covariance (μT²)

scalar | 3-element row vector | 3-by-3 matrix

Magnetometer readings error covariance in μT^2 , specified as a scalar, 3-element row vector, or 3-by-3 matrix.

Data Types: single | double

Output Arguments

res - Residual

1-by-3 vector of real values

Residual, returned a 1-by-3 vector of real values in µT.

Data Types: single | double

resCov — Residual covariance

3-by-3 matrix of real values

Residual covariance, returned a 3-by-3 matrix of real values in $(\mu T)^2$.

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder $^{\text{\tiny TM}}$.

See Also

insfilter|insfilterAsync

pose

Current position, orientation, and velocity estimate for insfilterAsync

Syntax

```
[position,orientation,velocity] = pose(FUSE)
[position,orientation,velocity] = pose(FUSE,format)
```

Description

[position, orientation, velocity] = pose(FUSE) returns the current estimate of the pose.

[position, orientation, velocity] = pose(FUSE, format) returns the current estimate of the pose with orientation in the specified orientation format.

Input Arguments

FUSE — insfilterAsync object

object

insfilterAsync, specified as an object.

format — Output orientation format

```
'quaternion' (default) | 'rotmat'
```

Output orientation format, specified as either 'quaternion' for a quaternion or 'rotmat' for a rotation matrix.

Data Types: char | string

Output Arguments

position — Position estimate in the local NED coordinate system (m)

3-element row vector

Position estimate in the local NED coordinate system in meters, returned as a 3-element row vector.

Data Types: single | double

orientation — Orientation estimate in the local NED coordinate system

quaternion (default) | 3-by-3 rotation matrix

Orientation estimate in the local NED coordinate system, returned as a scalar quaternion or 3-by-3 rotation matrix, depending on the specified orientation format. The quaternion or rotation matrix represents a frame rotation from the local NED reference frame to the body reference frame.

Data Types: single | double | quaternion

velocity — Velocity estimate in the local NED coordinate system (m/s)

3-element row vector

Velocity estimate in the local NED coordinate system in m/s, returned as a 3-element row vector.

Data Types: single | double

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder $^{\text{\tiny TM}}$.

See Also

insfilter|insfilterAsync

predict

Update states based on motion model for insfilterAsync

Syntax

predict(FUSE,dt)

Description

predict(FUSE,dt) updates states based on the motion model.

Input Arguments

FUSE — insfilterAsync object

object

insfilterAsync, specified as an object.

dt — Delta time to propagate forward (s)

scalar

Delta time to propagate forward in seconds, specified as a positive scalar.

Data Types: single | double

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

insfilter|insfilterAsync

reset

Reset internal states for insfilterAsync

Syntax

reset(FUSE)

Description

reset(FUSE) resets the State and StateCovariance properties of the insfilterAsync object to their default values.

Input Arguments

FUSE — insfilterAsync object

object

insfilterAsync, specified as an object.

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

insfilter|insfilterAsync

residual

Residuals and residual covariances from direct state measurements for insfilterAsync

Syntax

[res, resCov] = residual(FUSE,idx,measurement,measurementCovariance)

Description

[res, resCov] = residual(FUSE,idx,measurement,measurementCovariance) computes the residual, res, and the residual covariance, resCov, based on the direct state measurement and measurement covariance. The measurement maps directly to the states specified by indices, idx.

Input Arguments

FUSE — insfilterAsync

ahrs10filter | object

insfilterAsync, specified as an object.

idx — State vector index of measurement to correct

N-element vector of increasing integers in the range [1, 28]

State vector index of measurement to correct, specified as an N-element vector of increasing integers in the range [1, 28].

The state values represent:

State	Units	Index
Orientation (quaternion parts)	N/A	1:4
Angular Velocity (XYZ)	rad/s	5:7
Position (NED)	m	8:10
Velocity (NED)	m/s	11:13
Acceleration (NED)	m/s ²	14:16
Accelerometer Bias (XYZ)	m/s ²	17:19
Gyroscope Bias (XYZ)	rad/s	20:22
Geomagnetic Field Vector (NED)	μТ	23:25
Magnetometer Bias (XYZ)	μΤ	26:28

Data Types: single | double

measurement — Direct measurement of state

N-element vector

Direct measurement of state, specified as a N-element vector. N is the number of elements of the index argument, idx.

measurementCovariance — Covariance of measurement

N-by-*N* matrix

Covariance of measurement, specified as an N-by-N matrix. N is the number of elements of the index argument, idx.

Output Arguments

res — Measurement residual

1-by-*N* vector of real values

Measurement residual, returned as a 1-by-N vector of real values.

resCov — Residual covariance

N-by-N matrix of real values

Residual covariance, returned as a *N*-by-*N* matrix of real values.

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

insfilterAsync

Introduced in R2020a

residualaccel

Residuals and residual covariance from accelerometer measurements for insfilterAsync

Syntax

[res,resCov] = residualaccel(FUSE,acceleration,accelerationCovariance)

Description

[res,resCov] = residualaccel(FUSE,acceleration,accelerationCovariance)
computes the residual, res, and the residual covariance, resCov, based on the acceleration readings
and the corresponding covariance.

Input Arguments

FUSE — insfilterAsync

ahrs10filter | object

insfilterAsync, specified as an object.

acceleration — Accelerometer readings in local sensor body coordinate system (m/s²)

3-element row vector

Accelerometer readings in local sensor body coordinate system in m/s², specified as a 3-element row vector

Data Types: single | double

accelerationCovariance — Acceleration error covariance of accelerometer measurement $((m/s^2)^2)$

scalar | 3-element row vector | 3-by-3 matrix

Acceleration error covariance of the accelerometer measurement in $(m/s^2)^2$, specified as a scalar, 3-element row vector, or 3-by-3 matrix.

Data Types: single | double

Output Arguments

res - Residual

1-by-3 vector of real values

Residual, returned a 1-by-3 vector of real values in m/s².

resCov — Residual covariance

3-by-3 matrix of real values

Residual covariance, returned a 3-by-3 matrix of real values in $(m/s^2)^2$.

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder $^{\text{\tiny TM}}$.

See Also

insfilter|insfilterAsync

Introduced in R2020a

residualgps

Residuals and residual covariance from GPS measurements for insfilterAsync

Syntax

```
[res,resCov] = residualgps(FUSE,position,positionCovariance)
[res,resCov] = residualgps(FUSE,position,positionCovariance,velocity,velocityCovariance)
```

Description

[res,resCov] = residualgps(FUSE,position,positionCovariance) computes the
residual, res, and the residual covariance, resCov, based on the GPS position measurement and
covariance.

[res,resCov] = residualgps(FUSE,position,positionCovariance,velocity,
velocityCovariance) computes the residual, res, and the residual covariance, resCov, based on
the GPS position measurement and covariance.

Input Arguments

FUSE — insfilterAsync

ahrs10filter | object

insfilterAsync, specified as an object.

position — Position of GPS receiver (LLA)

3-element row vector

Position of GPS receiver in geodetic latitude, longitude, and altitude (LLA) specified as a real finite 3element row vector. Latitude and longitude are in degrees with north and east being positive. Altitude is in meters.

Data Types: single | double

positionCovariance — Position measurement covariance of GPS receiver (m²)

3-by-3 matrix

Position measurement covariance of GPS receiver in m², specified as a 3-by-3 matrix.

Data Types: single | double

velocity — Velocity of GPS receiver in local NED coordinate system (m/s)

3-element row vector

Velocity of the GPS receiver in the local NED coordinate system in m/s, specified as a 3-element row vector.

Data Types: single | double

velocityCovariance — Velocity measurement covariance of GPS receiver (m/s²)

3-by-3 matrix

Velocity measurement covariance of the GPS receiver in the local NED coordinate system in m/s², specified as a 3-by-3 matrix.

Data Types: single | double

Output Arguments

res - Position and velocity residual

1-by-3 vector of real values | 1-by-6 vector of real values

Position and velocity residual, returned as a 1-by-3 vector of real values if the inputs only contain position information, and returned as 1-by-6 vector of real values if the inputs also contain velocity information.

resCov — Residual covariance

3-by-3 matrix of real values | 6-by-6 matrix of real values

Residual covariance, returned as a 3-by-3 matrix of real values if the inputs only contain position information, and a 6-by-6 matrix of real values if the inputs also contain velocity information.

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

insfilterAsync

Introduced in R2020a

residualgyro

Residuals and residual covariance from gyroscope measurements for insfilterAsync

Syntax

[res,resCov] = residualgyro(FUSE,gyroReadings,gyroCovariance)

Description

[res,resCov] = residualgyro(FUSE,gyroReadings,gyroCovariance) computes the residual, res, and the innovation covariance, resCov, based on the gyroscope readings and the corresponding covariance.

Input Arguments

FUSE — insfilterAsync

ahrs10filter | object

insfilterAsync, specified as an object.

gyroReadings — Gyroscope readings in local sensor body coordinate system (rad/s)

3-element row vector

Gyroscope readings in local sensor body coordinate system in rad/s, specified as a 3-element row vector.

Data Types: single | double

gyroCovariance — Covariance of gyroscope measurement error ((rad/s)²)

scalar | 3-element row vector | 3-by-3 matrix

Covariance of gyroscope measurement error in $(rad/s)^2$, specified as a scalar, 3-element row vector, or 3-by-3 matrix.

Data Types: single | double

Output Arguments

res - Residual

1-by-3 vector of real values

Residual, returned as a 1-by-3 vector of real values in rad/s.

resCov — Residual covariance

3-by-3 matrix of real values

Residual covariance, returned as a 3-by-3 matrix of real values in (rad/s)².

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder $^{\text{\tiny TM}}$.

See Also

insfilter|insfilterAsync

Introduced in R2020a

residualmag

Residuals and residual covariance from magnetometer measurements for insfilterAsync

Syntax

[res,resCov] = residualmag(FUSE,magReadings,magReadingsCovariance)

Description

[res,resCov] = residualmag(FUSE,magReadings,magReadingsCovariance) computes the
residual, residual, and the residual covariance, resCov, based on the magnetometer readings and
the corresponding covariance.

Input Arguments

FUSE — insfilterAsync

ahrs10filter | object

insfilterAsync, specified as an object.

magReadings — Magnetometer readings (μT)

3-element row vector

Magnetometer readings in μT, specified as a 3-element row vector of finite real numbers.

Data Types: single | double

magReadingsCovariance — Magnetometer readings error covariance (μ T²)

scalar | 3-element row vector | 3-by-3 matrix

Magnetometer readings error covariance in μT^2 , specified as a scalar, 3-element row vector, or 3-by-3 matrix.

Data Types: single | double

Output Arguments

res - Residual

1-by-3 vector of real values

Residual, returned as a 1-by-3 vector of real values in μ T.

Data Types: single | double

resCov — Residual covariance

3-by-3 matrix of real values

Residual covariance, returned a 3-by-3 matrix of real values in $(\mu T)^2$.

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder $^{\text{\tiny TM}}$.

See Also

insfilterAsync

Introduced in R2020a

stateinfo

Display state vector information for insfilterAsync

Syntax

```
stateinfo(FUSE)
info = stateinfo(FUSE)
```

Description

stateinfo(FUSE) displays the description of each index of the State property of the insfilterAsync object and the associated units.

info = stateinfo(FUSE) returns a structure with fields containing descriptions of the elements of
the state vector of the filter, FUSE.

Examples

State Information of insfilterAsync

Create an insfilterAsync object.

```
filter = insfilterAsync;
```

Display the state information of the created filter.

stateinfo(filter)

States	Units	Index
Orientation (quaternion parts)		1:4
Angular Velocity (XYZ)	rad/s	5:7
Position (NAV)	m	8:10
Velocity (NAV)	m/s	11:13
Acceleration (NAV)	m/s^2	14:16
Accelerometer Bias (XYZ)	m/s^2	17:19
Gyroscope Bias (XYZ)	rad/s	20:22
Geomagnetic Field Vector (NAV)	μΤ	23:25
Magnetometer Bias (XYZ)	μΤ	26:28

Output the state information of the filter as a structure.

info = stateinfo(filter)

```
info = struct with fields:
    Orientation: [1 2 3 4]
    AngularVelocity: [5 6 7]
        Position: [8 9 10]
        Velocity: [11 12 13]
        Acceleration: [14 15 16]
        AccelerometerBias: [17 18 19]
        GyroscopeBias: [20 21 22]
```

GeomagneticFieldVector: [23 24 25] MagnetometerBias: [26 27 28]

Input Arguments

FUSE — insfilterAsync object

object

insfilterAsync, specified as an object.

Output Arguments

info — State information

structure

State information, returned as a structure with fields containing descriptions of the elements of the state vector of the filter. The values of each field are the corresponding indices of the state vector.

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

insfilter|insfilterAsync

Introduced in R2019a

tune

Tune insfilterAsync parameters to reduce estimation error

Syntax

```
tunedMeasureNoise = tune(filter,measureNoise,sensorData,groundTruth)
tunedMeasureNoise = tune(___,config)
```

Description

tunedMeasureNoise = tune(filter, measureNoise, sensorData, groundTruth) adjusts the properties of the insfilterAsync filter object, filter, and measurement noises to reduce the root-mean-squared (RMS) state estimation error between the fused sensor data and the ground truth. The function also returns the tuned measurement noise, tunedMeasureNoise. The function uses the property values in the filter and the measurement noise provided in the measureNoise structure as the initial estimate for the optimization algorithm.

tunedMeasureNoise = tune(____, config) specifies the tuning configuration based on a tunerconfig object, config.

Examples

Tune insfilterAsync to Optimize Pose Estimate

Load the recorded sensor data and ground truth data.

```
load('insfilterAsyncTuneData.mat');
```

Create timetables for the sensor data and the truth data.

```
sensorData = timetable(Accelerometer, Gyroscope, ...
   Magnetometer, GPSPosition, GPSVelocity, 'SampleRate', 100);
groundTruth = timetable(Orientation, Position, ...
   'SampleRate', 100);
```

Create an insfilterAsync filter object that has a few noise properties.

```
filter = insfilterAsync('State', initialState, ...
    'StateCovariance', initialStateCovariance, ...
    'AccelerometerBiasNoise', 1e-7, ...
    'GyroscopeBiasNoise', 1e-7, ...
    'MagnetometerBiasNoise', 1e-7, ...
    'GeomagneticVectorNoise', 1e-7);
```

Create a tuner configuration object for the filter. Set the maximum iterations to two. Also, set the tunable parameters as the unspecified properties.

```
'GyroscopeBiasNoise', 'MagnetometerBiasNoise'});
config.TunableParameters

ans = 1×10 string
    "AccelerationNoise" "AccelerometerNoise" "AngularVelocityNoise" "GPSPositionNoise"
```

Use the tuner noise function to obtain a set of initial sensor noises used in the filter.

```
measNoise = tunernoise('insfilterAsync')
measNoise = struct with fields:
    AccelerometerNoise: 1
        GyroscopeNoise: 1
        MagnetometerNoise: 1
        GPSPositionNoise: 1
        GPSVelocityNoise: 1
```

Tune the filter and obtain the tuned parameters.

tunedParams = tune(filter,measNoise,sensorData,groundTruth,config);

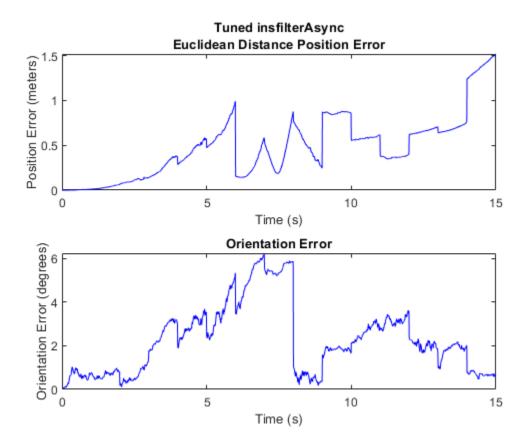
Iteration	Parameter	Metric
1	AccelerationNoise	2.1345
1	AccelerometerNoise	2.1264
1	AngularVelocityNoise	1.9659
1	GPSPositionNoise	1.9341
1	GPSVelocityNoise	1.8420
1	GyroscopeNoise	1.7589
1	MagnetometerNoise	1.7362
1	PositionNoise	1.7362
1	QuaternionNoise	1.7218
1	VelocityNoise	1.7218
2	AccelerationNoise	1.7190
2	AccelerometerNoise	1.7170
2	AngularVelocityNoise	1.6045
2	GPSPositionNoise	1.5948
1 2 2 2 2 2 2 2 2 2 2 2 3 3 3 3 3 3 3 3	GPSVelocityNoise	1.5323
2	GyroscopeNoise	1.4803
2	MagnetometerNoise	1.4703
2	PositionNoise	1.4703
2	QuaternionNoise	1.4632
2	VelocityNoise	1.4632
3	AccelerationNoise	1.4596
3	AccelerometerNoise	1.4548
3	AngularVelocityNoise	1.3923
3	GPSPositionNoise	1.3810
3	GPSVelocityNoise	1.3322
3	GyroscopeNoise	1.2998
3	MagnetometerNoise	1.2976
3	PositionNoise	1.2976
3	QuaternionNoise	1.2943
	VelocityNoise	1.2943
4	AccelerationNoise	1.2906
4	AccelerometerNoise	1.2836
4	AngularVelocityNoise	1.2491
4	GPSPositionNoise	1.2258

```
GPSVelocityNoise
                                      1.1880
4
             GyroscopeNoise
                                      1.1701
4
             MagnetometerNoise
                                      1.1698
4
             PositionNoise
                                      1.1698
4
             QuaternionNoise
                                      1.1688
4
             VelocityNoise
                                      1.1688
5
             AccelerationNoise
                                      1.1650
5
             AccelerometerNoise
                                      1.1569
5
             AngularVelocityNoise
                                      1.1454
5
             GPSPositionNoise
                                      1.1100
5
                                      1.0778
             GPSVelocityNoise
5
             GyroscopeNoise
                                      1.0709
5
             MagnetometerNoise
                                      1.0675
5
                                      1.0675
             PositionNoise
5
                                      1.0669
             QuaternionNoise
5
                                      1.0669
             VelocityNoise
6
             AccelerationNoise
                                      1.0634
6
             AccelerometerNoise
                                      1.0549
6
             AngularVelocityNoise
                                      1.0549
6
             GPSPositionNoise
                                      1.0180
6
             GPSVelocityNoise
                                      0.9866
6
                                      0.9810
             GyroscopeNoise
6
             MagnetometerNoise
                                      0.9775
6
                                      0.9775
             PositionNoise
                                      0.9768
6
             QuaternionNoise
6
             VelocityNoise
                                      0.9768
7
                                      0.9735
             AccelerationNoise
7
                                      0.9652
             AccelerometerNoise
7
             AngularVelocityNoise
                                      0.9652
7
             GPSPositionNoise
                                      0.9283
7
             GPSVelocityNoise
                                      0.8997
7
             GyroscopeNoise
                                      0.8947
7
             MagnetometerNoise
                                      0.8920
7
             PositionNoise
                                      0.8920
7
             QuaternionNoise
                                      0.8912
7
                                      0.8912
             VelocityNoise
8
             AccelerationNoise
                                      0.8885
8
             AccelerometerNoise
                                      0.8811
8
             AngularVelocityNoise
                                      0.8807
8
             GPSPositionNoise
                                      0.8479
8
             GPSVelocityNoise
                                      0.8238
8
             GyroscopeNoise
                                      0.8165
8
                                      0.8165
             MagnetometerNoise
8
             PositionNoise
                                      0.8165
8
             QuaternionNoise
                                      0.8159
             VelocityNoise
                                      0.8159
```

Fuse the sensor data using the tuned filter.

```
dt = seconds(diff(groundTruth.Time));
N = size(sensorData,1);
qEst = quaternion.zeros(N,1);
posEst = zeros(N,3);
% Iterate the filter for prediction and correction using sensor data.
for ii=1:N
    if ii ~= 1
        predict(filter, dt(ii-1));
    end
```

```
if all(~isnan(Accelerometer(ii,:)))
        fuseaccel(filter,Accelerometer(ii,:), ...
            tunedParams.AccelerometerNoise);
    end
    if all(~isnan(Gyroscope(ii,:)))
        fusegyro(filter, Gyroscope(ii,:), ...
            tunedParams.GyroscopeNoise);
    end
    if all(~isnan(Magnetometer(ii,1)))
        fusemag(filter, Magnetometer(ii,:), ...
            tunedParams.MagnetometerNoise);
    end
    if all(~isnan(GPSPosition(ii,1)))
        fusegps(filter, GPSPosition(ii,:), ...
            tunedParams.GPSPositionNoise, GPSVelocity(ii,:), ...
            tunedParams.GPSVelocityNoise);
    end
    [posEst(ii,:), qEst(ii,:)] = pose(filter);
end
Compute the RMS errors.
orientationError = rad2deg(dist(qEst, Orientation));
rmsorientationError = sqrt(mean(orientationError.^2))
rmsorientationError = 2.7801
positionError = sqrt(sum((posEst - Position).^2, 2));
rmspositionError = sqrt(mean( positionError.^2))
rmspositionError = 0.5966
Visualize the results.
figure();
t = (0:N-1)./ groundTruth.Properties.SampleRate;
subplot(2,1,1)
plot(t, positionError, 'b');
title("Tuned insfilterAsync" + newline + "Euclidean Distance Position Error")
xlabel('Time (s)');
ylabel('Position Error (meters)')
subplot(2,1,2)
plot(t, orientationError, 'b');
title("Orientation Error")
xlabel('Time (s)');
ylabel('Orientation Error (degrees)');
```



Input Arguments

filter — Filter object

infilterAsync object

Filter object, specified as an insfilterAsync object.

measureNoise — Measurement noise

structure

Measurement noise, specified as a structure. The function uses the measurement noise input as the initial guess for tuning the measurement noise. The structure must contain these fields:

Field name	Description
AccelerometerNoise	Variance of accelerometer noise, specified as a scalar in (m^2/s)
GyroscopeNoise	Variance of gyroscope noise, specified as a scalar in $(rad/s)^2$
MagnetometerNoise	Variance of magnetometer noise, specified as a scalar in $(\mu T)^2$
GPSPositionNoise	Variance of GPS position noise, specified as a scalar in m ²

Field name	Description
	Variance of GPS velocity noise, specified as a scalar in $(m/s)^2$

sensorData — Sensor data

duration

Sensor data, specified as a timetable. In each row, the time and sensor data is specified as:

- Time Time at which the data is obtained, specified as a scalar in seconds.
- Accelerometer Accelerometer data, specified as a 1-by-3 vector of scalars in m²/s.
- Gyroscope Gyroscope data, specified as a 1-by-3 vector of scalars in rad/s.
- Magnetometer Magnetometer data, specified as a 1-by-3 vector of scalars in μT.
- GPSPosition GPS position data, specified as a 1-by-3 vector of scalars in meters.
- GPSVelocity GPS velocity data, specified as a 1-by-3 vector of scalars in m/s.

If a sensor does not produce measurements, specify the corresponding entry as NaN. If you set the Cost property of the tuner configuration input, config, to Custom, then you can use other data types for the sensorData input based on your choice.

groundTruth — Ground truth data

duration

Ground truth data, specified as a timetable. In each row, the table can optionally contain any of these variables:

- Orientation Orientation from the navigation frame to the body frame, specified as a quaternion or a 3-by-3 rotation matrix.
- AngularVelocity Angular velocity in body frame, specified as a 1-by-3 vector of scalars in rad/s.
- Position Position in navigation frame, specified as a 1-by-3 vector of scalars in meters.
- Velocity Velocity in navigation frame, specified as a 1-by-3 vector of scalars in m/s.
- Acceleration Acceleration in navigation frame, specified as a 1-by-3 vector of scalars in m²/s.
- AccelerometerBias Accelerometer delta angle bias in body frame, specified as a 1-by-3 vector of scalars in m²/s.
- GyroscopeBias Gyroscope delta angle bias in body frame, specified as a 1-by-3 vector of scalars in rad/s.
- GeomagneticFieldVector Geomagnetic field vector in navigation frame, specified as a 1-by-3 vector of scalars.
- MagnetometerBias Magnetometer bias in body frame, specified as a 1-by-3 vector of scalars in μT .

The function processes each row of the sensorData and groundTruth tables sequentially to calculate the state estimate and RMS error from the ground truth. State variables not present in groundTruth input are ignored for the comparison. The sensorData and the groundTruth tables must have the same time steps.

If you set the Cost property of the tuner configuration input, config, to Custom, then you can use other data types for the groundTruth input based on your choice.

config — Tuner configuration

tunerconfig object

Tuner configuration, specified as a tunerconfig object.

Output Arguments

tunedMeasureNoise — Tuned measurement noise

structure

Tuned measurement noise, returned as a structure. The structure contains these fields.

Field name	Description
AccelerometerNoise	Variance of accelerometer noise, specified as a scalar in $(m^2/s)^2$
GyroscopeNoise	Variance of gyroscope noise, specified as a scalar in $(rad/s)^2$
MagnetometerNoise	Variance of magnetometer noise, specified as a scalar in $(\mu T)^2$
GPSPositionNoise	Variance of GPS position noise, specified as a scalar in m ²
GPSVelocityNoise	Variance of GPS velocity noise, specified as a scalar in (m/s) ²

References

[1] Abbeel, P., Coates, A., Montemerlo, M., Ng, A.Y. and Thrun, S. Discriminative Training of Kalman Filters. In *Robotics: Science and systems*, Vol. 2, pp. 1, 2005.

See Also

tunerconfig|tunernoise

Introduced in R2020b

binaryOccupancyMap

Create occupancy grid with binary values

Description

The binaryOccupancyMap creates a 2-D occupancy map object, which you can use to represent and visualize a robot workspace, including obstacles. The integration of sensor data and position estimates create a spatial representation of the approximate locations of the obstacles.

Occupancy grids are used in robotics algorithms such as path planning. They are also used in mapping applications, such as for finding collision-free paths, performing collision avoidance, and calculating localization. You can modify your occupancy grid to fit your specific application.

Each cell in the occupancy grid has a value representing the occupancy status of that cell. An occupied location is represented as true (1) and a free location is represented as false (0).

The object keeps track of three reference frames: world, local, and, grid. The world frame origin is defined by GridLocationInWorld, which defines the bottom-left corner of the map relative to the world frame. The LocalOriginInWorld property specifies the location of the origin of the local frame relative to the world frame. The first grid location with index (1,1) begins in the top-left corner of the grid.

Note This object was previously named robotics.BinaryOccupancyGrid.

Creation

Syntax

```
map = binaryOccupancyMap
map = binaryOccupancyMap(width,height)
map = binaryOccupancyMap(width,height,resolution)

map = binaryOccupancyMap(rows,cols,resolution,"grid")

map = binaryOccupancyMap(p)
map = binaryOccupancyMap(p,resolution)
map = binaryOccupancyMap(p,resolution)

map = binaryOccupancyMap(sourcemap)
map = binaryOccupancyMap(sourcemap,resolution)
```

Description

map = binaryOccupancyMap creates a 2-D binary occupancy grid with a width and height of 10m. The default grid resolution is one cell per meter.

map = binaryOccupancyMap(width, height) creates a 2-D binary occupancy grid representing a
work space of width and height in meters. The default grid resolution is one cell per meter.

map = binaryOccupancyMap(width,height,resolution) creates a grid with the Resolution
property specified in cells per meter. The map is in world coordinates by default.

map = binaryOccupancyMap(rows,cols,resolution,"grid") creates a 2-D binary occupancy
grid of size (rows,cols).

map = binaryOccupancyMap(p) creates a grid from the values in matrix p. The size of the grid matches the size of the matrix, with each cell value interpreted from its location in the matrix. p contains any numeric or logical type with zeros (0) and ones (1).

map = binaryOccupancyMap(p,resolution) creates a map from a matrix with the Resolution
property specified in cells per meter.

map = binaryOccupancyMap(p,resolution) creates an object with the Resolution property
specified in cells per meter.

map = binaryOccupancyMap(sourcemap) creates an object using values from another binaryOccupancyMap object.

map = binaryOccupancyMap(sourcemap, resolution) creates an object using values from another binaryOccupancyMap object, but resamples the matrix to have the specified resolution.

Input Arguments

width - Map width

positive scalar

Map width, specified as a positive scalar in meters.

height — Map height

positive scalar

Map height, specified as a positive scalar in meters.

p — Map grid values

matrix

Map grid values, specified as a matrix.

sourcemap — Occupancy map object

binaryOccupancyMap object

Occupancy map object, specified as a binaryOccupancyMap object.

Properties

GridSize — Number of rows and columns in grid

two-element horizontal vector

This property is read-only.

Number of rows and columns in grid, stored as a two-element horizontal vector of the form [rows cols].

Resolution — Grid resolution

1 (default) | scalar in cells per meter

This property is read-only.

Grid resolution, stored as a scalar in cells per meter.

${\tt XLocalLimits-Minimum\ and\ maximum\ values\ of\ \it x-coordinates\ in\ local\ frame}$

two-element vector

This property is read-only.

Minimum and maximum values of x-coordinates in local frame, stored as a two-element horizontal vector of the form [min max]. Local frame is defined by LocalOriginInWorld property.

YLocalLimits — Minimum and maximum values of y-coordinates in local frame

two-element vector

This property is read-only.

Minimum and maximum values of y-coordinates in local frame, stored as a two-element horizontal vector of the form [min max]. Local frame is defined by LocalOriginInWorld property.

XWorldLimits — Minimum and maximum values of x-coordinates in world frame

two-element vector

This property is read-only.

Minimum and maximum values of x-coordinates in world frame, stored as a two-element horizontal vector of the form [min max]. These values indicate the world range of the x-coordinates in the grid.

YWorldLimits — Minimum and maximum values of y-coordinates

two-element vector

This property is read-only.

Minimum and maximum values of *y*-coordinates, stored as a two-element vector of the form [min max]. These values indicate the world range of the *y*-coordinates in the grid.

GridLocationInWorld — **Location of the grid in world coordinates**

[0 0] (default) | two-element vector | [xGrid yGrid]

Location of the bottom-left corner of the grid in world coordinates, specified as a two-element vector, [xGrid yGrid].

LocalOriginInWorld — Location of the local frame in world coordinates

[0 0] (default) | two-element vector | [xWorld yWorld]

Location of the origin of the local frame in world coordinates, specified as a two-element vector, [xLocal yLocal]. Use the move function to shift the local frame as your vehicle moves.

GridOriginInLocal — **Location of the grid in local coordinates**

[0 0] (default) | two-element vector | [xLocal yLocal]

Location of the bottom-left corner of the grid in local coordinates, specified as a two-element vector, [xLocal yLocal].

DefaultValue — Default value for unspecified map locations

0 (default) | 1

Default value for unspecified map locations including areas outside the map, specified as 0 or 1.

Object Functions

checkOccupancy Check occupancy values for locations getOccupancy Get occupancy value of locations

grid2local Convert grid indices to local coordinates grid2world Convert grid indices to world coordinates inflate Inflate each occupied grid location

inflate inflate each occupied grid location insertRay Insert ray from laser scan observation local2grid Convert local coordinates to grid indices

local2world Convert local coordinates to world coordinates

move Move map in world frame

occupancyMatrix Convert occupancy grid to matrix raycast Compute cell indices along a ray

rayIntersection Find intersection points of rays and occupied map cells

setOccupancy Set occupancy value of locations show Show occupancy grid values syncWith Sync map with overlapping map

world2grid Convert world coordinates to grid indices world2local Convert world coordinates to local coordinates

Examples

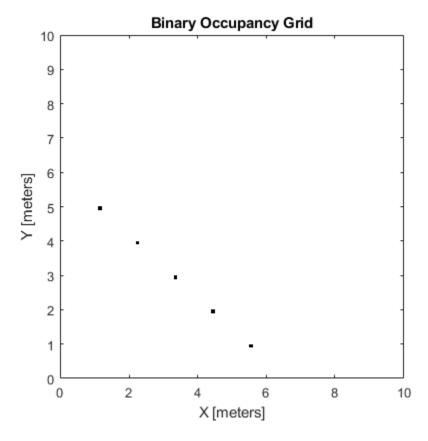
Create and Modify Binary Occupancy Grid

```
Create a 10m x 10m empty map.
```

```
map = binaryOccupancyMap(10,10,10);
```

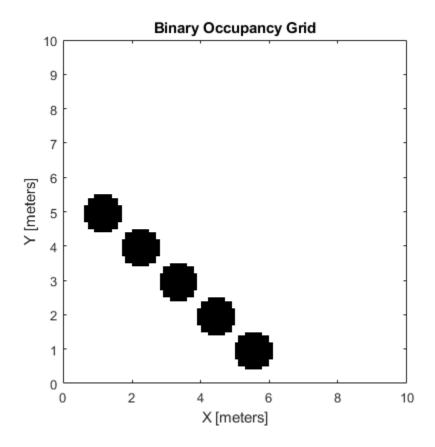
Set occupancy of world locations and show map.

```
x = [1.2; 2.3; 3.4; 4.5; 5.6];
y = [5.0; 4.0; 3.0; 2.0; 1.0];
setOccupancy(map, [x y], ones(5,1))
figure
show(map)
```



Inflate occupied locations by a given radius.

inflate(map, 0.5)
figure
show(map)



Get grid locations from world locations.

```
ij = world2grid(map, [x y]);
Set grid locations to free locations.
setOccupancy(map, ij, zeros(5,1), 'grid')
figure
show(map)
```

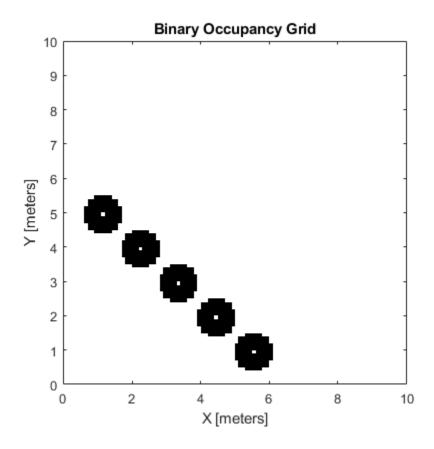


Image to Binary Occupancy Grid Example

This example shows how to convert an image to a binary occupancy grid for using with mapping and path planning.

```
Import image.
```

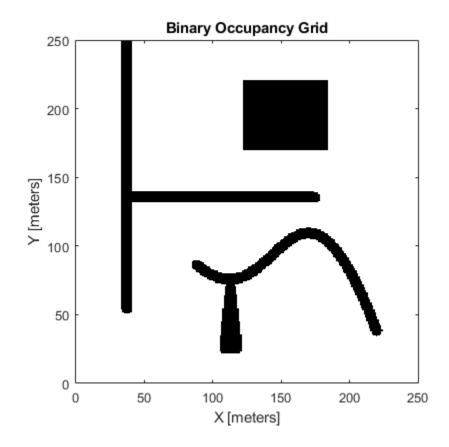
```
image = imread('imageMap.png');
```

Convert to grayscale and then black and white image based on given threshold value.

```
grayimage = rgb2gray(image);
bwimage = grayimage < 0.5;</pre>
```

Use black and white image as matrix input for binary occupancy grid.

```
grid = binaryOccupancyMap(bwimage);
show(grid)
```

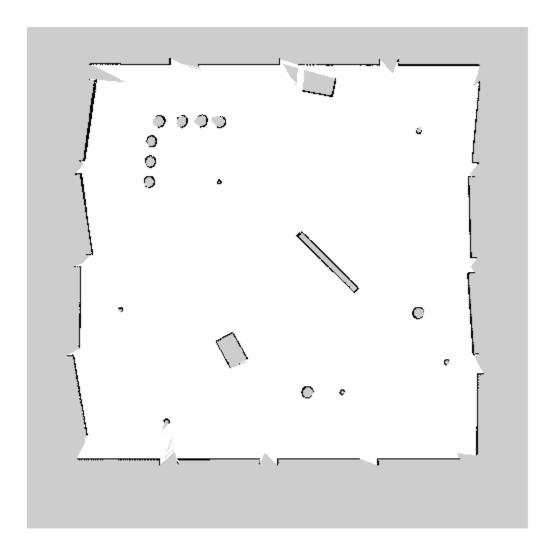


Convert PGM Image to Map

This example shows how to convert a .pgm file into a binaryOccupancyMap object for use in MATLAB.

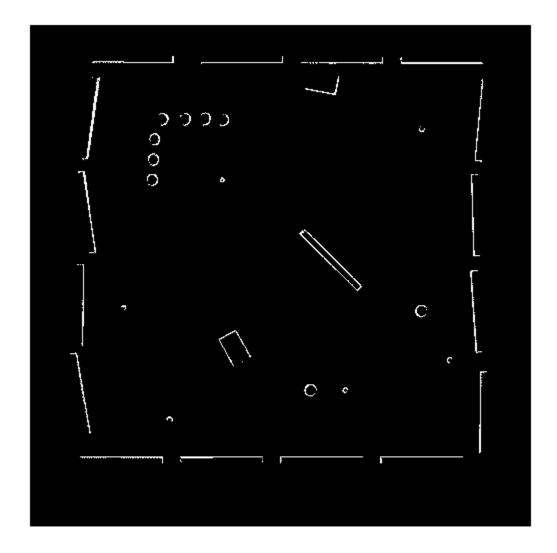
Import image using imread. The image is quite large and should be cropped to the relevant area.

```
image = imread('playpen_map.pgm');
imageCropped = image(750:1250,750:1250);
imshow(imageCropped)
```



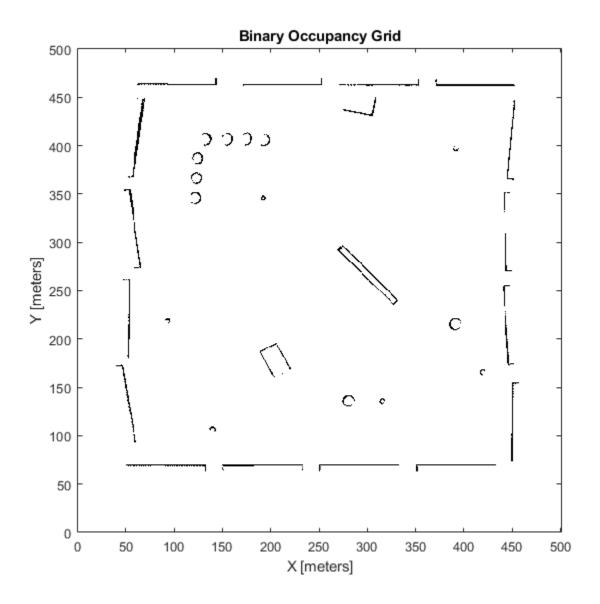
Unknown areas (gray) should be removed and treated as free space. Create a logical matrix based on a threshold. Depending on your image, this value could be different. Occupied space should be set as 1 (white in image).

imageBW = imageCropped < 100; imshow(imageBW)



Create binaryOccupancyMap object using adjusted map image.

```
map = binaryOccupancyMap(imageBW);
show(map)
```



Compatibility Considerations

binaryOccupancyMap was renamed

Behavior change in future release

The binaryOccupancyMap object was renamed from robotics.BinaryOccupancyGrid. Use binaryOccupancyMap for all object creation.

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

controllerPurePursuit

Topics

"Occupancy Grids"

Introduced in R2015a

checkOccupancy

Check occupancy values for locations

Syntax

```
occVal = checkOccupancy(map,xy)
occVal = checkOccupancy(map,xy,"local")
occVal = checkOccupancy(map,ij,"grid")
[occVal,validPts] = checkOccupancy(____)

occMatrix = checkOccupancy(map)
occMatrix = checkOccupancy(map,bottomLeft,matSize)
occMatrix = checkOccupancy(map,bottomLeft,matSize,"local")
occMatrix = checkOccupancy(map,topLeft,matSize,"grid")
```

Description

occVal = checkOccupancy(map,xy) returns an array of occupancy values at the xy locations in the world frame. Obstacle-free cells return 0, occupied cells return 1. Unknown locations, including outside the map, return -1.

occVal = checkOccupancy(map,xy,"local") returns an array of occupancy values at the xy locations in the local frame. The local frame is based on the LocalOriginInWorld property of the map.

occVal = checkOccupancy(map,ij,"grid") specifies ij grid cell indices instead of xy locations. Grid indices start at (1,1) from the top left corner.

[occVal, validPts] = checkOccupancy(____) also outputs an n-element vector of logical values indicating whether input coordinates are within the map limits.

occMatrix = checkOccupancy(map) returns a matrix that contains the occupancy status of each location. Obstacle-free cells return 0, occupied cells return 1. Unknown locations, including outside the map, return -1.

occMatrix = checkOccupancy(map,bottomLeft,matSize) returns a matrix of occupancy values by specifying the bottom-left corner location in world coordinates and the matrix size in meters.

occMatrix = checkOccupancy(map,bottomLeft,matSize,"local") returns a matrix of occupancy values by specifying the bottom-left corner location in local coordinates and the matrix size in meters.

occMatrix = checkOccupancy(map,topLeft,matSize,"grid") returns a matrix of occupancy values by specifying the top-left cell index in grid coordinates and the matrix size.

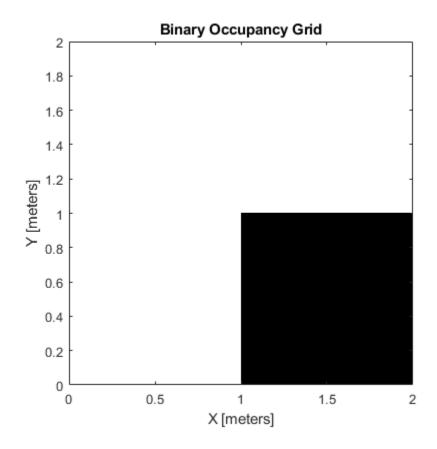
Examples

Get Occupancy Values and Check Occupancy Status

Access occupancy values and check their occupancy status based on the occupied and free thresholds of the occupancyMap object.

Create a matrix and populate it with values. Use this matrix to create an occupancy map.

```
p = zeros(20,20);
p(11:20,11:20) = ones(10,10);
map = binaryOccupancyMap(p,10);
show(map)
```



Get the occupancy of different locations and check their occupancy statuses. The occupancy status returns 0 for free space and 1 for occupied space. Unknown values return -1.

```
pocc = getOccupancy(map,[1.5 1]);
occupied = checkOccupancy(map,[1.5 1]);
pocc2 = getOccupancy(map,[5 5],'grid');
```

Input Arguments

map — Map representation

binaryOccupancyMap object

Map representation, specified as a binaryOccupancyMap object.

xy — Coordinates in the map

n-by-2 matrix

Coordinates in the map, specified as an n-by-2 matrix of $[x \ y]$ pairs, where n is the number of coordinates. Coordinates can be world or local coordinates depending on the syntax.

Data Types: double

ij — Grid locations in the map

n-by-2 matrix

Grid locations in the map, specified as an n-by-2 matrix of $[i \ j]$ pairs, where n is the number of locations. Grid locations are given as $[row\ col]$.

Data Types: double

bottomLeft — Location of output matrix in world or local

two-element vector | [xCoord vCoord]

Location of bottom left corner of output matrix in world or local coordinates, specified as a twoelement vector, [xCoord yCoord]. Location is in world or local coordinates based on syntax.

Data Types: double

matSize — Output matrix size

two-element vector | [xLength yLength] | [gridRow gridCol]

Output matrix size, specified as a two-element vector, [xLength yLength], or [gridRow gridCol]. Size is in world, local, or grid coordinates based on syntax.

Data Types: double

topLeft — Location of grid

two-element vector | [iCoord jCoord]

Location of top left corner of grid, specified as a two-element vector, [iCoord jCoord].

Data Types: double

Output Arguments

occVal — Occupancy values

n-by-1 column vector

Occupancy values, returned as an n-by-1 column vector equal in length to xy or ij input. Occupancy values can be obstacle free (0), occupied (1), or unknown (-1).

validPts — Valid map locations

n-by-1 column vector

Valid map locations, returned as an n-by-1 column vector equal in length to xy or ij. Locations inside the map return a value of 1. Locations outside the map limits return a value of 0.

occMatrix — Matrix of occupancy values

matrix

Matrix of occupancy values, returned as matrix with size equal to matSize or the size of your map. Occupancy values can be obstacle free (0), occupied (1), or unknown (-1).

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

binaryOccupancyMap | getOccupancy | occupancyMap

Introduced in R2019b

getOccupancy

Get occupancy value of locations

Syntax

```
occVal = getOccupancy(map,xy)
occVal = getOccupancy(map,xy,"local")
occVal = getOccupancy(map,ij,"grid")
[occVal,validPts] = getOccupancy(____)

occMatrix = getOccupancy(map)
occMatrix = getOccupancy(map,bottomLeft,matSize)
occMatrix = getOccupancy(map,bottomLeft,matSize,"local")
occMatrix = getOccupancy(map,topLeft,matSize,"grid")
```

Description

occVal = getOccupancy(map,xy) returns an array of occupancy values at the xy locations in the world frame. Unknown locations, including outside the map, return map.DefaultValue.

occVal = getOccupancy(map,xy,"local") returns an array of occupancy values at the xy
locations in the local frame.

occVal = getOccupancy(map,ij,"grid") specifies ij grid cell indices instead of xy locations.

[occVal,validPts] = getOccupancy(____) additionally outputs an n-element vector of logical values indicating whether input coordinates are within the map limits.

occMatrix = getOccupancy(map) returns all occupancy values in the map as a matrix.

occMatrix = getOccupancy(map,bottomLeft,matSize) returns a matrix of occupancy values by specifying the bottom-left corner location in world coordinates and the matrix size in meters.

occMatrix = getOccupancy(map,bottomLeft,matSize,"local") returns a matrix of occupancy values by specifying the bottom-left corner location in local coordinates and the matrix size in meters.

occMatrix = getOccupancy(map,topLeft,matSize,"grid") returns a matrix of occupancy
values by specifying the top-left cell index in grid indices and the matrix size.

Examples

Insert Laser Scans into Binary Occupancy Map

Create an empty binary occupancy grid map.

```
map = binaryOccupancyMap(10,10,20);
```

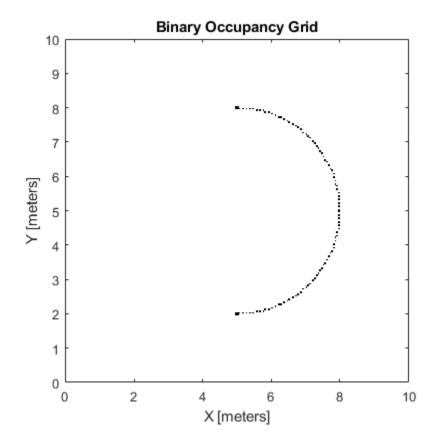
Input pose of the vehicle, ranges, angles, and the maximum range of the laser scan.

```
pose = [5,5,0];
ranges = 3*ones(100,1);
angles = linspace(-pi/2,pi/2,100);
maxrange = 20;

Create a lidarScan object with the specified ranges and angles.
scan = lidarScan(ranges,angles);

Insert the laser scan data into the occupancy map.
insertRay(map,pose,scan,maxrange);

Show the map to see the results of inserting the laser scan.
show(map)
```



Check the occupancy of the spot directly in front of the vehicle.

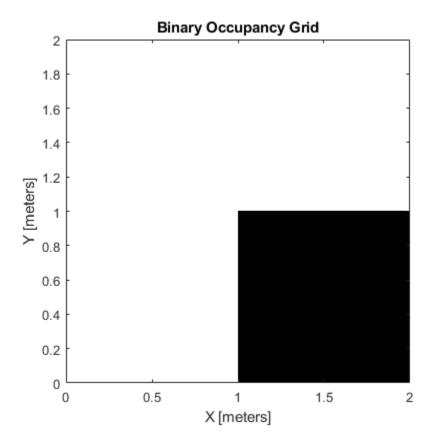
```
getOccupancy(map,[8 5])
ans = logical
1
```

Get Occupancy Values and Check Occupancy Status

Access occupancy values and check their occupancy status based on the occupied and free thresholds of the occupancyMap object.

Create a matrix and populate it with values. Use this matrix to create an occupancy map.

```
p = zeros(20,20);
p(11:20,11:20) = ones(10,10);
map = binaryOccupancyMap(p,10);
show(map)
```



Get the occupancy of different locations and check their occupancy statuses. The occupancy status returns 0 for free space and 1 for occupied space. Unknown values return -1.

```
pocc = getOccupancy(map,[1.5 1]);
occupied = checkOccupancy(map,[1.5 1]);
pocc2 = getOccupancy(map,[5 5],'grid');
```

Input Arguments

map — Map representation

binaryOccupancyMap object

Map representation, specified as a binaryOccupancyMap object. This object represents the environment of the vehicle.

xy — Coordinates in the map

n-by-2 matrix

Coordinates in the map, specified as an n-by-2 matrix of $[x \ y]$ pairs, where n is the number of coordinates. Coordinates can be world or local coordinates depending on the syntax.

Data Types: double

ij — Grid locations in the map

n-by-2 matrix

Grid locations in the map, specified as an n-by-2 matrix of $[i \ j]$ pairs, where n is the number of locations. Grid locations are given as $[row\ col]$.

Data Types: double

bottomLeft — Location of output matrix in world or local

two-element vector | [xCoord yCoord]

Location of bottom left corner of output matrix in world or local coordinates, specified as a twoelement vector, [xCoord yCoord]. Location is in world or local coordinates based on syntax.

Data Types: double

matSize — Output matrix size

two-element vector | [xLength yLength] | [gridRow gridCol]

Output matrix size, specified as a two-element vector, [xLength yLength] or [gridRow gridCol]. The size is in world coordinates, local coordinates, or grid indices based on syntax.

Data Types: double

topLeft — Location of grid

two-element vector | [iCoord jCoord]

Location of top left corner of grid, specified as a two-element vector, [iCoord jCoord].

Data Types: double

Output Arguments

occVal — Occupancy values

n-by-1 column vector

Occupancy values, returned as an n-by-1 column vector equal in length to xy or ij. Occupancy values can be obstacle free (0) or occupied (1).

validPts — Valid map locations

n-by-1 column vector

Valid map locations, returned as an n-by-1 column vector equal in length to xy or ij. Locations inside the map return a value of 1. Locations outside the map limits return a value of 0.

occMatrix — Matrix of occupancy values

matrix

Matrix of occupancy values, returned as matrix with size equal to matSize or the size of map.

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

binaryOccupancyMap|setOccupancy

Topics

"Occupancy Grids"

Introduced in R2015a

grid2local

Convert grid indices to local coordinates

Syntax

```
xy = grid2local(map,ij)
```

Description

xy = grid2local(map,ij) converts a [row col] array of grid indices, ij, to an array of local
coordinates, xy.

Input Arguments

map — Map representation

binaryOccupancyMap object

Map representation, specified as a binaryOccupancyMap object. This object represents the environment of the robot. The object contains a matrix grid with binary values indicating obstacles as true (1) and free locations as false (0).

ij - Grid positions

n-by-2 vertical array

Grid positions, specified as an n-by-2 vertical array of $[i \ j]$ pairs in $[rows \ cols]$ format, where n is the number of grid positions.

Output Arguments

xy — Local coordinates

n-by-2 vertical array

Local coordinates, specified as an n-by-2 vertical array of $[x \ y]$ pairs, where n is the number of local coordinates.

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

binaryOccupancyMap | world2grid

Introduced in R2019b

grid2world

Convert grid indices to world coordinates

Syntax

xy = grid2world(map,ij)

Description

xy = grid2world(map,ij) converts a [row col] array of grid indices, ij, to an array of world
coordinates, xy.

Input Arguments

map — Map representation

binaryOccupancyMap object

Map representation, specified as a binaryOccupancyMap object. This object represents the environment of the robot. The object contains a matrix grid with binary values indicating obstacles as true (1) and free locations as false (0).

ij - Grid positions

n-by-2 vertical array

Grid positions, specified as an n-by-2 vertical array of $[i \ j]$ pairs in $[rows \ cols]$ format, where n is the number of grid positions.

Output Arguments

xy — World coordinates

n-by-2 vertical array

World coordinates, specified as an n-by-2 vertical array of $[x \ y]$ pairs, where n is the number of world coordinates.

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

binaryOccupancyMap | grid2local | world2grid

Introduced in R2015a

inflate

Inflate each occupied grid location

Syntax

```
inflate(map, radius)
inflate(map, gridradius, 'grid')
```

Description

inflate(map, radius) inflates each occupied position of the map by the radius given in meters.
radius is rounded up to the nearest cell equivalent based on the resolution of the map. Every cell
within the radius is set to true (1).

inflate(map,gridradius,'grid') inflates each occupied position by the radius given in number
of cells.

Examples

Create and Modify Binary Occupancy Grid

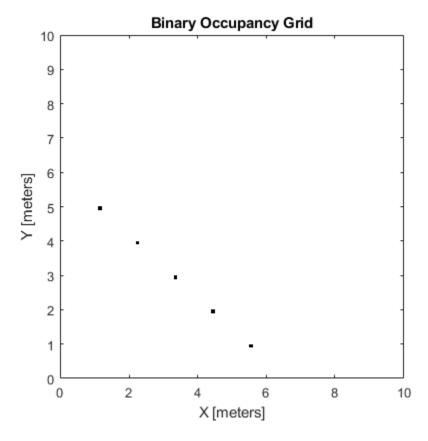
```
Create a 10m x 10m empty map.

map = binaryOccupancyMap(10,10,10);

Set occupancy of world locations and show map.

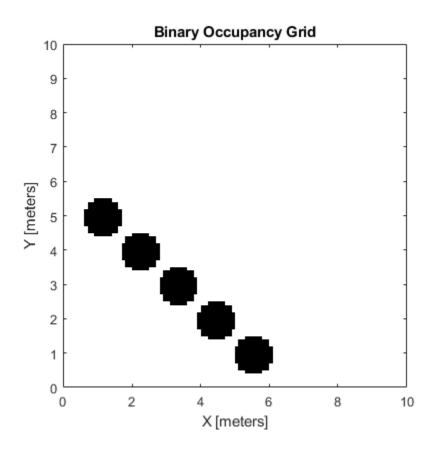
x = [1.2; 2.3; 3.4; 4.5; 5.6];
y = [5.0; 4.0; 3.0; 2.0; 1.0];

setOccupancy(map, [x y], ones(5,1))
figure show(map)
```



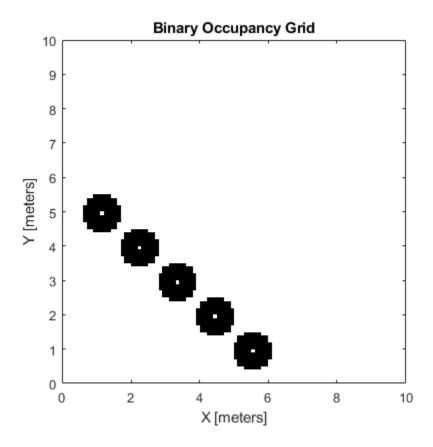
Inflate occupied locations by a given radius.

inflate(map, 0.5)
figure
show(map)



Get grid locations from world locations.

```
ij = world2grid(map, [x y]);
Set grid locations to free locations.
setOccupancy(map, ij, zeros(5,1), 'grid')
figure
show(map)
```



Input Arguments

map — Map representation

binaryOccupancyMap object

Map representation, specified as a binaryOccupancyMap object. This object represents the environment of the robot. The object contains a matrix grid with binary values indicating obstacles as true (1) and free locations as false (0).

radius — Dimension the defines how much to inflate occupied locations scalar

Dimension that defines how much to inflate occupied locations, specified as a scalar. radius is rounded up to the nearest cell value.

Data Types: double

gridradius — Dimension the defines how much to inflate occupied locations positive scalar

Dimension that defines how much to inflate occupied locations, specified as a positive scalar. gridradius is the number of cells to inflate the occupied locations.

Data Types: double

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder $^{\text{\tiny TM}}$.

See Also

binaryOccupancyMap|setOccupancy

Topics

"Occupancy Grids"

Introduced in R2015a

insertRay

Insert ray from laser scan observation

Syntax

```
insertRay(map,pose,scan,maxrange)
insertRay(map,pose,ranges,angles,maxrange)
insertRay(map,startpt,endpoints)
```

Description

insertRay(map,pose,scan,maxrange) inserts one or more lidar scan sensor observations in the occupancy grid, map, using the input lidarScan object, scan, to get ray endpoints. End point locations are updated with an occupied value. If the ranges are above maxrange, the ray endpoints are considered free space. All other points along the ray are treated as obstacle-free.

insertRay(map,pose,ranges,angles,maxrange) specifies the range readings as vectors
defined by the input ranges and angles.

insertRay(map, startpt, endpoints) inserts observations between the line segments from the start point to the end points. The endpoints are updated are occupied space and other points along the line segments are updated as free space.

Examples

show(map)

Insert Laser Scans into Binary Occupancy Map

```
Create an empty binary occupancy grid map.

map = binaryOccupancyMap(10,10,20);

Input pose of the vehicle, ranges, angles, and the maximum range of the laser scan.

pose = [5,5,0];
ranges = 3*ones(100,1);
angles = linspace(-pi/2,pi/2,100);
maxrange = 20;

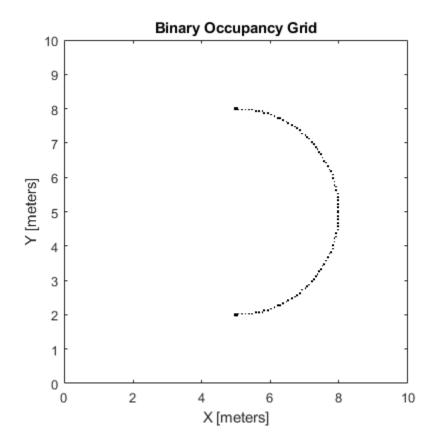
Create a lidarScan object with the specified ranges and angles.

scan = lidarScan(ranges,angles);

Insert the laser scan data into the occupancy map.

insertRay(map,pose,scan,maxrange);

Show the map to see the results of inserting the laser scan.
```



Check the occupancy of the spot directly in front of the vehicle.

getOccupancy(map,[8 5])

ans = logical

Input Arguments

map — Map representation

binaryOccupancyMap object

Map representation, specified as a binaryOccupancyMap object. This object represents the environment of the robot. The object contains a matrix grid with binary values indicating obstacles as true (1) and free locations as false (0).

pose — Position and orientation of vehicle

three-element vector

Position and orientation of vehicle, specified as an $[x \ y \ theta]$ vector. The vehicle pose is an x and y position with angular orientation theta (in radians) measured from the x-axis.

scan — Lidar scan readings

lidarScan object

Lidar scan readings, specified as a lidarScan object.

ranges — Range values from scan data

vector

Range values from scan data, specified as a vector of elements measured in meters. These range values are distances from a sensor at given angles. The vector must be the same length as the corresponding angles vector.

angles - Angle values from scan data

vector

Angle values from scan data, specified as a vector of elements measured in radians. These angle values correspond to the given ranges. The vector must be the same length as the corresponding ranges vector.

maxrange — Maximum range of sensor

scalar

Maximum range of laser range sensor, specified as a scalar in meters. Range values greater than or equal to maxrange are considered free along the whole length of the ray, up to maxrange.

startpt — Start point for rays

two-element vector

Start point for rays, specified as a two-element vector, $[x \ y]$, in the world coordinate frame. All rays are line segments that originate at this point.

endpoints — Endpoints for rays

n-by-2 matrix

Endpoints for rays, specified as an n-by-2 matrix of $[x \ y]$ pairs in the world coordinate frame, where n is the length of ranges or angles. All rays are line segments that originate at startpt.

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

binaryOccupancyMap | lidarScan | lidarScan | occupancyMap

Topics

"Occupancy Grids" (Robotics System Toolbox)

Introduced in R2019b

local2grid

Convert local coordinates to grid indices

Syntax

ij = local2grid(map,xy)

Description

ij = local2grid(map,xy) converts an array of local coordinates, xy, to an array of grid indices,
ij in [row col] format.

Input Arguments

map — Map representation

binaryOccupancyMap object

Map representation, specified as a binaryOccupancyMap object. This object represents the environment of the vehicle.

xy — Local coordinates

n-by-2 matrix

Local coordinates, specified as an n-by-2 matrix of $[x \ y]$ pairs, where n is the number of local coordinates.

Data Types: double

Output Arguments

ij — Grid positions

n-by-2 matrix

Grid positions, returned as an n-by-2 matrix of $[i \ j]$ pairs in $[row \ col]$ format, where n is the number of grid positions. The grid cell locations are counted from the top left corner of the grid.

Data Types: double

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

binaryOccupancyMap | grid2world | grid2world | occupancyMap

Topics

"Occupancy Grids"

Introduced in R2019b

local2world

Convert local coordinates to world coordinates

Syntax

xyWorld = local2world(map,xy)

Description

xyWorld = local2world(map,xy) converts an array of local coordinates to world coordinates.

Input Arguments

map — Map representation

binaryOccupancyMap object

Map representation, specified as a binaryOccupancyMap object. This object represents the environment of the vehicle.

xy — Local coordinates

n-by-2 matrix

Local coordinates, specified as an n-by-2 matrix of $[x \ y]$ pairs, where n is the number of local coordinates.

Data Types: double

Output Arguments

xyWorld — World coordinates

n-by-2 matrix

World coordinates, specified as an n-by-2 matrix of $[x \ y]$ pairs, where n is the number of world coordinates.

Data Types: double

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

Topics

"Occupancy Grids"

Introduced in R2019b

move

Move map in world frame

Syntax

```
move(map, moveValue)
move(map, moveValue, Name, Value)
```

Description

move(map, moveValue) moves the local origin of the map to an absolute location, moveValue, in the world frame, and updates the map limits. Move values are truncated based on the resolution of the map. By default, newly revealed regions are set to map. DefaultValue.

move(map, moveValue, Name, Value) specifies additional options specified by one or more name-value pair arguments.

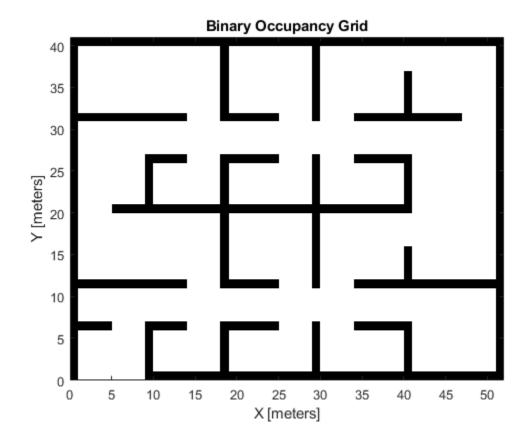
Examples

Move Local Map and Sync with World Map

This example shows how to move a local egocentric map and sync it with a larger world map. This process emulates a vehicle driving in an environment and getting updates on obstacles in the new areas.

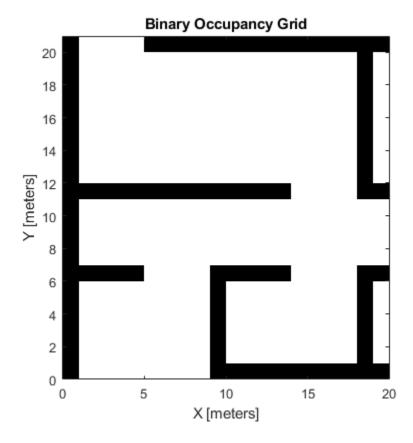
Load example maps. Create a binary occupancy map from the complexMap.

```
load exampleMaps.mat
map = binaryOccupancyMap(complexMap);
show(map)
```



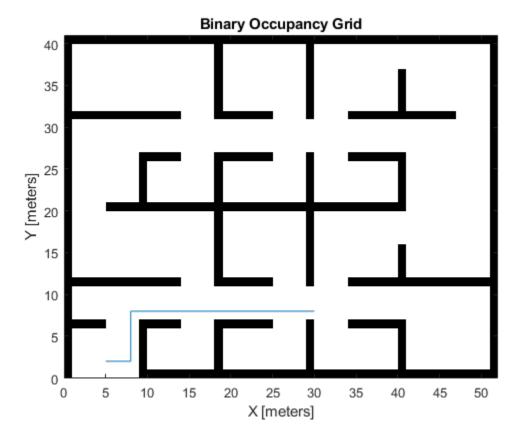
Create a smaller local map.

mapLocal = binaryOccupancyMap(complexMap(end-20:end,1:20));
show(mapLocal)

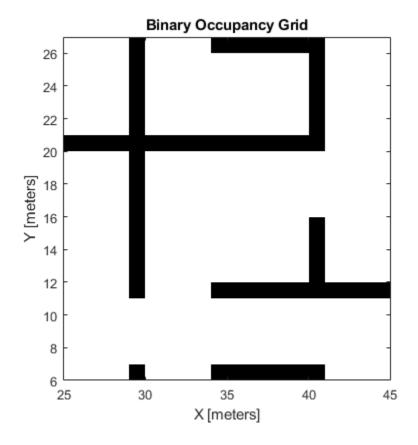


Follow a path planned in the world map and update the local map as you move your local frame.

Specify path locations and plot on the map.



Create a loop for moving between points by the map resolution. Divide the difference between points by the map resolution to see how many incremental moves you can make.



Input Arguments

map — Map representation

binaryOccupancyMap object

Map representation, specified as a binaryOccupancyMap object. This object represents the environment of the vehicle.

moveValue — Local map origin move value

[x y] vector

Local map origin move value, specified as an $[x \ y]$ vector. By default, the value is an absolute location to move the local origin to in the world frame. Use the MoveType name-value pair to specify a relative move.

Name-Value Pair Arguments

Specify optional comma-separated pairs of Name, Value arguments. Name is the argument name and Value is the corresponding value. Name must appear inside quotes. You can specify several name and value pair arguments in any order as Name1, Value1, . . . , NameN, ValueN.

Example: 'MoveType', 'relative'

MoveType — Type of move

'absolute' (default) | 'relative'

Type of move, specified as 'absolute' or 'relative'. For relative moves, specify a relative [x y] vector for moveValue based on your current local frame.

FillValue — Fill value for revealed locations

0 (default) | 1

Fill value for revealed locations because of the shifted map limits, specified as 0 or 1.

SyncWith — Secondary map to sync with

binaryOccupancyMap object

Secondary map to sync with, specified as a binaryOccupancyMap object. Any revealed locations based on the move are updated with values in this map using the world coordinates.

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

binaryOccupancyMap | occupancyMap | occupancyMatrix

Introduced in R2019b

occupancyMatrix

Convert occupancy grid to matrix

Syntax

mat = occupancyMatrix(map)

Description

mat = occupancyMatrix(map) returns occupancy values stored in the occupancy grid object as a
matrix.

Input Arguments

map — Map representation

binaryOccupancyMap object

Map representation, specified as a binaryOccupancyMap object. This object represents the environment of the robot. The object contains a matrix grid with binary values indicating obstacles as true (1) and free locations as false (0).

Output Arguments

mat — Occupancy values

matrix

Occupancy values, returned as an h-by-w matrix, where h and w are defined by the two elements of the GridSize property of the occupancy grid object.

Data Types: double

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

binaryOccupancyMap | occupancyMap

Topics

"Occupancy Grids"

Introduced in R2016b

raycast

Compute cell indices along a ray

Syntax

```
[endpoints,midpoints] = raycast(map,pose,range,angle)
[endpoints,midpoints] = raycast(map,p1,p2)
```

Description

[endpoints, midpoints] = raycast(map, pose, range, angle) returns cell indices of the specified map for all cells traversed by a ray originating from the specified pose at the specified angle and range values. endpoints contains all indices touched by the end of the ray, with all other points included in midpoints.

[endpoints, midpoints] = raycast(map,p1,p2) returns the cell indices of the line segment between the two specified points.

Input Arguments

map — Map representation

binaryOccupancyMap object

Map representation, specified as a binaryOccupancyMap object. This object represents the environment of the robot. The object contains a matrix grid with binary values indicating obstacles as true (1) and free locations as false (0).

pose — Position and orientation of sensor

three-element vector

Position and orientation of sensor, specified as an $[x \ y \ theta]$ vector. The sensor pose is an x and y position with angular orientation theta (in radians) measured from the x-axis.

range — Range of ray

scalar

Range of ray, specified as a scalar in meters.

angle — Angle of ray

scalar

Angle of ray, specified as a scalar in radians. The angle value is for the corresponding range.

p1 — Starting point of ray

two-element vector

Starting point of ray, specified as an $[x \ y]$ two-element vector. Points are defined with respect to the world-frame.

p2 — Endpoint of ray

two-element vector

Endpoint of ray, specified as an $[x \ y]$ two-element vector. Points are defined with respect to the world-frame.

Output Arguments

endpoints — Endpoint grid indices

n-by-2 matrix

Endpoint indices, returned as an n-by-2 matrix of $[i \ j]$ pairs, where n is the number of grid indices. The endpoints are where the range value hits at the specified angle. Multiple indices are returned when the endpoint lies on the boundary of multiple cells.

midpoints — Midpoint grid indices

n-by-2 matrix

Midpoint indices, returned as an n-by-2 matrix of $[i \ j]$ pairs, where n is the number of grid indices. This argument includes all grid indices the ray intersects, excluding the endpoint.

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

binaryOccupancyMap | insertRay | occupancyMap

Topics

"Occupancy Grids" (Robotics System Toolbox)

Introduced in R2019b

[&]quot;Occupancy Grids"

rayIntersection

Find intersection points of rays and occupied map cells

Syntax

intersectionPts = rayIntersection(map,pose,angles,maxrange)

Description

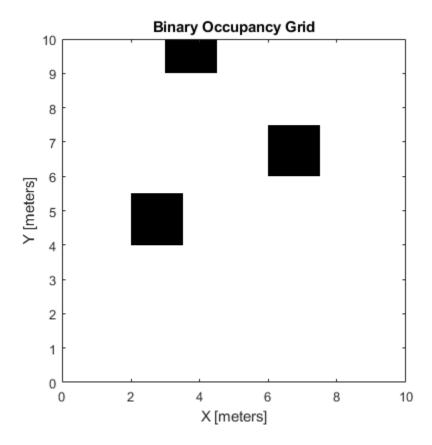
intersectionPts = rayIntersection(map,pose,angles,maxrange) returns intersection points of rays and occupied cells in the specified map. Rays emanate from the specified pose and angles. Intersection points are returned in the world coordinate frame. If there is no intersection up to the specified maxrange, [NaN NaN] is returned.

Examples

Get Ray Intersection Points on Occupancy Map

Create a binary occupancy grid map. Add obstacles and inflate them. A lower resolution map is used to illustrate the importance of the size of your grid cells. Show the map.

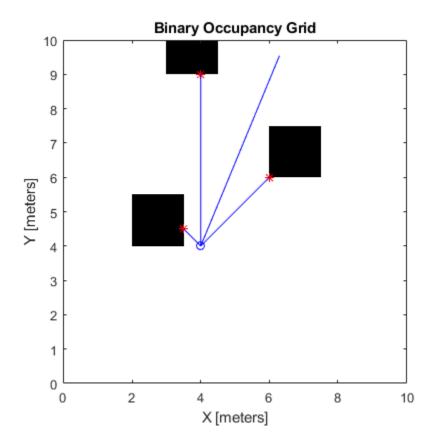
```
map = binaryOccupancyMap(10,10,2);
obstacles = [4 10; 3 5; 7 7];
setOccupancy(map,obstacles,ones(length(obstacles),1))
inflate(map,0.25)
show(map)
```



Find the intersection points of occupied cells and rays that emit from the given vehicle pose. Specify the max range and angles for these rays. The last ray does not intersect with an obstacle within the max range, so it has no collision point.

Plot the intersection points and rays from the pose.

```
hold on
plot(intsectionPts(:,1),intsectionPts(:,2),'*r') % Intersection points
plot(vehiclePose(1),vehiclePose(2),'ob') % Vehicle pose
for i = 1:3
    plot([vehiclePose(1),intsectionPts(i,1)],...
        [vehiclePose(2),intsectionPts(i,2)],'-b') % Plot intersecting rays
end
plot([vehiclePose(1),vehiclePose(1)-6*sin(angles(4))],...
    [vehiclePose(2),vehiclePose(2)+6*cos(angles(4))],'-b') % No intersection ray
```



Input Arguments

map — Map representation

binaryOccupancyMap object

Map representation, specified as a binaryOccupancyMap object. This object represents the environment of the robot. The object contains a matrix grid with binary values indicating obstacles as true (1) and free locations as false (0).

pose — Position and orientation of sensor

three-element vector

Position and orientation of the sensor, specified as an $[x \ y \ theta]$ vector. The sensor pose is an x and y position with angular orientation theta (in radians) measured from the x-axis.

${\bf angles-Ray\ angles\ emanating\ from\ sensor}$

vector

Ray angles emanating from the sensor, specified as a vector with elements in radians. These angles are relative to the specified sensor pose.

maxrange — Maximum range of sensor

scalar

Maximum range of laser range sensor, specified as a scalar in meters. Range values greater than or equal to maxrange are considered free along the whole length of the ray, up to maxrange.

Output Arguments

intersectionPts — Intersection points

n-by-2 matrix

Intersection points, returned as n-by-2 matrix of $[x \ y]$ pairs in the world coordinate frame, where n is the length of angles.

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

binaryOccupancyMap | occupancyMap

Topics

"Occupancy Grids" (Robotics System Toolbox)

"Occupancy Grids" (Robotics System Toolbox)

Introduced in R2019b

setOccupancy

Set occupancy value of locations

Syntax

```
setOccupancy(map,xy,occval)
setOccupancy(map,xy,occval,"local")
setOccupancy(map,ij,occval,"grid")
validPts = setOccupancy(____)
setOccupancy(map,bottomLeft,inputMatrix)
setOccupancy(map,bottomLeft,inputMatrix,"local")
setOccupancy(map,topLeft,inputMatrix,"grid")
```

Description

setOccupancy (map, xy, occval) assigns occupancy values, occval, to the input array of world coordinates, xy in the occupancy grid, map. Each row of the array, xy, is a point in the world and is represented as an $[x \ y]$ coordinate pair. occval is either a scalar or a single column array of the same length as xy. An occupied location is represented as true (1), and a free location is represented as false (0).

setOccupancy(map,xy,occval,"local") assigns occupancy values, occval, to the input array of local coordinates, xy, as local coordinates.

setOccupancy(map,ij,occval,"grid") assigns occupancy values, occval, to the input array of
grid indices, ij, as [rows cols].

 $validPts = setOccupancy(___)$ outputs an n-element vector of logical values indicating whether input coordinates are within the map limits.

setOccupancy(map,bottomLeft,inputMatrix) assigns a matrix of occupancy values by specifying the bottom-left corner location in world coordinates.

setOccupancy(map,bottomLeft,inputMatrix,"local") assigns a matrix of occupancy values by specifying the bottom-left corner location in local coordinates.

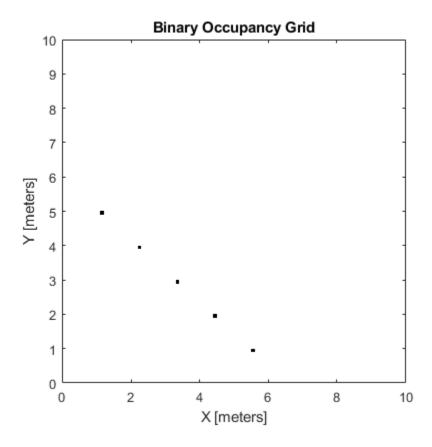
setOccupancy(map,topLeft,inputMatrix,"grid") assigns a matrix of occupancy values by specifying the top-left cell index in grid indices and the matrix size.

Examples

Create and Modify Binary Occupancy Grid

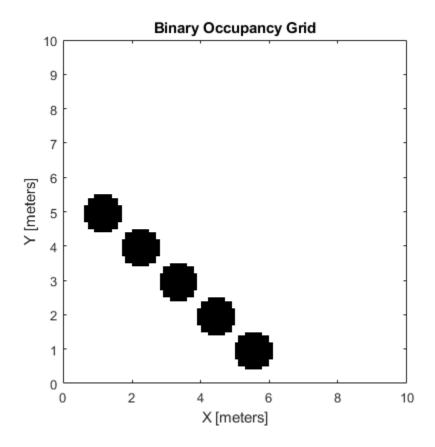
```
Create a 10m x 10m empty map.
map = binaryOccupancyMap(10,10,10);
Set occupancy of world locations and show map.
```

```
x = [1.2; 2.3; 3.4; 4.5; 5.6];
y = [5.0; 4.0; 3.0; 2.0; 1.0];
setOccupancy(map, [x y], ones(5,1))
figure
show(map)
```



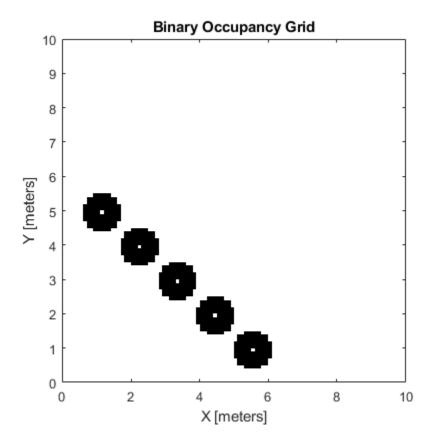
Inflate occupied locations by a given radius.

```
inflate(map, 0.5)
figure
show(map)
```



Get grid locations from world locations.

```
ij = world2grid(map, [x y]);
Set grid locations to free locations.
setOccupancy(map, ij, zeros(5,1), 'grid')
figure
show(map)
```



Input Arguments

map — Map representation

binaryOccupancyMap object

Map representation, specified as a binaryOccupancyMap object. This object represents the environment of the robot. The object contains a matrix grid with binary values indicating obstacles as true (1) and free locations as false (0).

xy — World coordinates

n-by-2 vertical array

World coordinates, specified as an n-by-2 vertical array of $[x \ y]$ pairs, where n is the number of world coordinates.

Data Types: double

ij - Grid positions

n-by-2 vertical array

Grid positions, specified as an n-by-2 vertical array of [i j] pairs in [rows cols] format, where n is the number of grid positions.

Data Types: double

occval — Occupancy values

n-by-1 vertical array

Occupancy values of the same length as either xy or ij, returned as an n-by-1 vertical array, where n is the same n in either xy or ij. Values are given between 0 and 1 inclusively.

inputMatrix — Occupancy values

matrix

Occupancy values, specified as a matrix. Values are given between 0 and 1 inclusively.

bottomLeft — Location of output matrix in world or local

two-element vector | [xCoord yCoord]

Location of bottom left corner of output matrix in world or local coordinates, specified as a twoelement vector, [xCoord yCoord]. Location is in world or local coordinates based on syntax.

Data Types: double

topLeft — Location of grid

two-element vector | [iCoord jCoord]

Location of top left corner of grid, specified as a two-element vector, [iCoord jCoord].

Data Types: double

Output Arguments

validPts — Valid map locations

n-by-1 column vector

Valid map locations, returned as an n-by-1 column vector equal in length to xy or ij. Locations inside the map return a value of 1. Locations outside the map limits return a value of 0.

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

binaryOccupancyMap | getOccupancy | occupancyMap

Introduced in R2015a

show

Show occupancy grid values

Syntax

```
show(map)
show(map, "local")
show(map, "grid")
show(____, Name, Value)
mapImage = show(____)
```

Description

show(map) displays the binary occupancy grid map in the current axes, with the axes labels representing the world coordinates.

show(map, "local") displays the binary occupancy grid map in the current axes, with the axes
labels representing the local coordinates instead of world coordinates.

show(map, "grid") displays the binary occupancy grid map in the current axes, with the axes
labels representing the grid coordinates.

 $\verb|show(___ , Name , Value)| | specifies additional options specified by one or more name-value pair arguments.$

mapImage = show(____) returns the handle to the image object created by show.

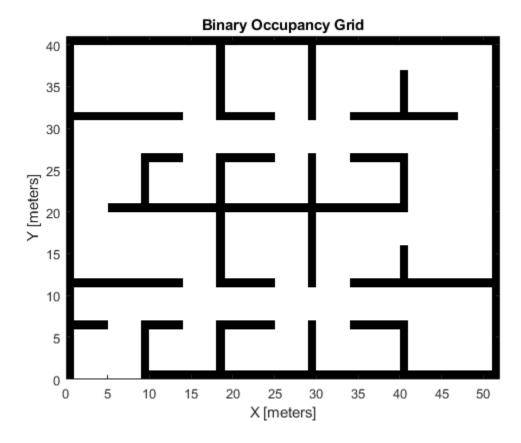
Examples

Move Local Map and Sync with World Map

This example shows how to move a local egocentric map and sync it with a larger world map. This process emulates a vehicle driving in an environment and getting updates on obstacles in the new areas.

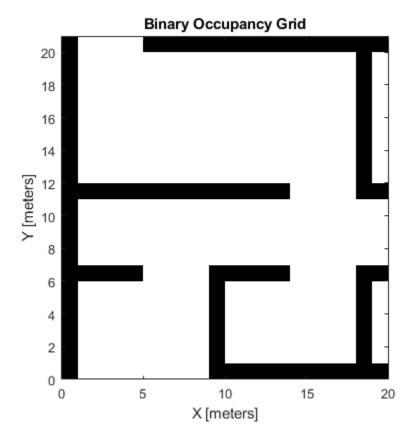
Load example maps. Create a binary occupancy map from the complexMap.

```
load exampleMaps.mat
map = binaryOccupancyMap(complexMap);
show(map)
```



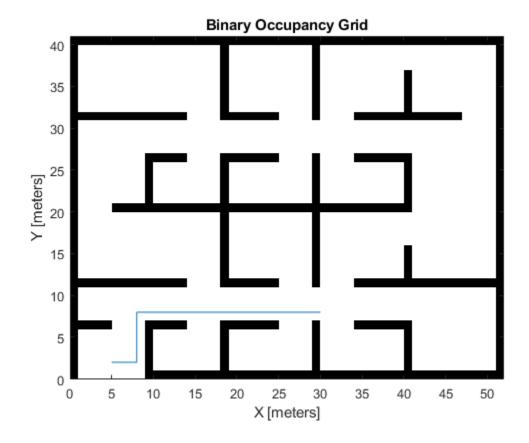
Create a smaller local map.

mapLocal = binaryOccupancyMap(complexMap(end-20:end,1:20));
show(mapLocal)

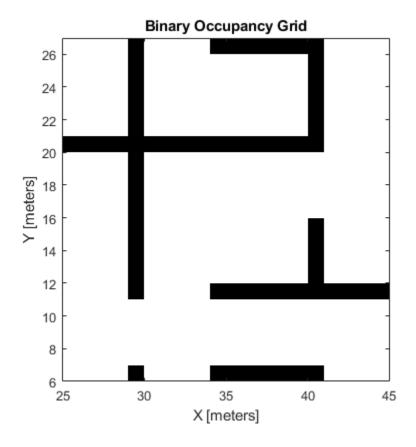


Follow a path planned in the world map and update the local map as you move your local frame.

Specify path locations and plot on the map.



Create a loop for moving between points by the map resolution. Divide the difference between points by the map resolution to see how many incremental moves you can make.



Input Arguments

map — Map representation

binaryOccupancyMap object

Map representation, specified as a binaryOccupancyMap object. This object represents the environment of the vehicle.

Name-Value Pair Arguments

Specify optional comma-separated pairs of Name, Value arguments. Name is the argument name and Value is the corresponding value. Name must appear inside quotes. You can specify several name and value pair arguments in any order as Name1, Value1, . . . , NameN, ValueN.

Example: 'Parent', axHandle

Parent — Axes to plot the map

Axes object | UIAxes object

Axes to plot the map specified as either an Axes or UIAxesobject. See axes or uiaxes.

FastUpdate — Update existing map plot

0 (default) | 1

Update existing map plot, specified as 0 or 1. If you previously plotted your map on your figure, set to 1 for a faster update to the figure. This is useful for updating the figure in a loop for fast animations.

See Also

occupancyMap|binaryOccupancyMap

Introduced in R2015a

syncWith

Sync map with overlapping map

Syntax

```
mat = syncWith(map,sourcemap)
```

Description

mat = syncWith(map, sourcemap) updates map with data from another binaryOccupancyMap object, sourcemap. Locations in map that are also found in sourcemap are updated. All other cells in map are set to map.DefaultValue.

Examples

Sync Map With an Overlapping Map

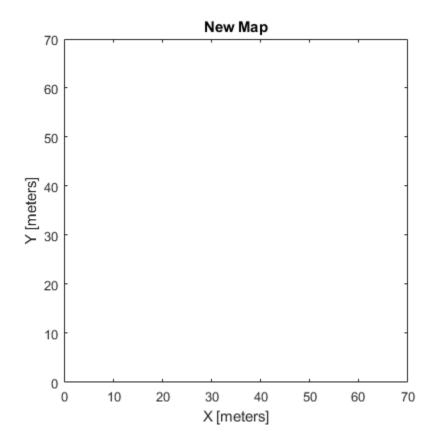
This example shows how to sync two overlapping maps using the syncWith function.

2-D occupancy maps are used to represent and visualize robot workspaces. In this example 2-D occupancy maps are created using existing map grid values stored inside exampleMaps.mat.

```
load('exampleMaps.mat');
```

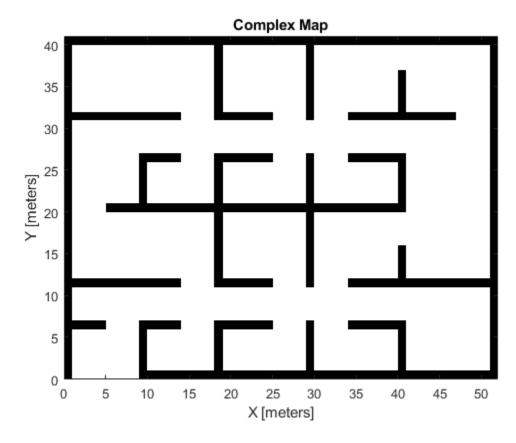
Create and display a new empty 2-D occupancy map object using binaryOccupancyMap function.

```
map1 = binaryOccupancyMap(70,70);
show(map1)
title('New Map')
```



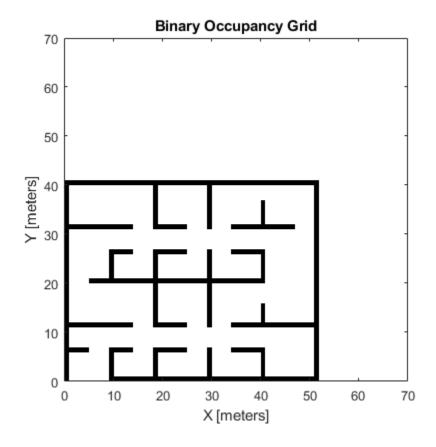
Create and display 2-D occupancy map using the map grid values stored in complexMap.

```
map2 = binaryOccupancyMap(complexMap);
show(map2)
title('Complex Map')
```



Now update map1 with map2 using the syncWith function.

syncWith(map1,map2);
show(map1)



Input Arguments

map — Map representation

binaryOccupancyMap object

Map representation, specified as a binaryOccupancyMap object.

sourcemap — Map representation

binaryOccupancyMap object

Map representation, specified as a binaryOccupancyMap object.

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

binaryOccupancyMap | occupancyMap

Topics

"Occupancy Grids"

world2grid

Convert world coordinates to grid indices

Syntax

ij = world2grid(map,xy)

Description

ij = world2grid(map,xy) converts an array of world coordinates, xy, to a [rows cols] array of
grid indices, ij.

Input Arguments

map — Map representation

binaryOccupancyMap object

Map representation, specified as a binaryOccupancyMap object.

xy — World coordinates

n-by-2 vertical array

World coordinates, specified as an n-by-2 vertical array of $[x \ y]$ pairs, where n is the number of world coordinates.

Output Arguments

ij - Grid indices

n-by-2 vertical array

Grid indices, specified as an n-by-2 vertical array of [i j] pairs in [rows cols] format, where n is the number of grid positions.

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

binaryOccupancyMap|grid2world

Introduced in R2015a

world2local

Convert world coordinates to local coordinates

Syntax

xyLocal = world2local(map,xy)

Description

xyLocal = world2local(map,xy) converts an array of world coordinates to local coordinates.

Input Arguments

map — Map representation

binaryOccupancyMap object

Map representation, specified as a binaryOccupancyMap object.

xy — World coordinates

n-by-2 vertical array

World coordinates, specified as an n-by-2 vertical array of $[x \ y]$ pairs, where n is the number of world coordinates.

Output Arguments

xyLocal — Local coordinates

n-by-2 vertical array

Local coordinates, specified as an n-by-2 vertical array of $[x \ y]$ pairs, where n is the number of local coordinates.

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

binaryOccupancyMap | grid2world | local2world

controllerVFH

Avoid obstacles using vector field histogram

Description

The controllerVFH System object enables your vehicle to avoid obstacles based on range sensor data using vector field histograms (VFH). Given laser scan readings and a target direction to drive toward, the object computes an obstacle-free steering direction.

controllerVFH specifically uses the VFH+ algorithm to compute an obstacle-free direction. First, the algorithm takes the ranges and angles from laser scan data and builds a polar histogram for obstacle locations. Then, the input histogram thresholds are used to calculate a binary histogram that indicates occupied and free directions. Finally, the algorithm computes a masked histogram, which is computed from the binary histogram based on the minimum turning radius of the vehicle.

The algorithm selects multiple steering directions based on the open space and possible driving directions. A cost function, with weights corresponding to the previous, current, and target directions, calculates the cost of different possible directions. The object then returns an obstacle-free direction with minimal cost. Using the obstacle-free direction, you can input commands to move your vehicle in that direction.

To use this object for your own application and environment, you must tune the properties of the algorithm. Property values depend on the type of vehicle, the range sensor, and the hardware you use.

To find an obstacle-free steering direction:

- 1 Create the controllerVFH object and set its properties.
- **2** Call the object with arguments, as if it were a function.

To learn more about how System objects work, see What Are System Objects?.

Creation

Syntax

VFH = controllerVFH

VFH = controllerVFH(Name, Value)

Description

VFH = controllerVFH returns a vector field histogram object that computes the obstacle-free steering direction using the VFH+ algorithm.

VFH = controllerVFH(Name, Value) returns a vector field histogram object with additional options specified by one or more Name, Value pairs. Name is the property name and Value is the corresponding value. Name must appear inside single quotes (' '). You can specify several name-

value pair arguments in any order as Name1, Value1, ..., NameN, ValueN. Properties not specified retain their default values.

Properties

NumAngularSectors — Number of angular sectors in histogram

180 (default) | positive integer

Number of angular sectors in the vector field histogram, specified as a scalar. This property defines the number of bins used to create the histograms. This property is non-tunable. You can only set this when the object is initialized.

DistanceLimits — Limits for range readings

[0.05 2] (default) | 2-element vector

Limits for range readings, specified as a 2-element vector with elements measured in meters. The range readings specified when calling the object are considered only if they fall within the distance limits. Use the lower distance limit to ignore false positives from poor sensor performance at lower ranges. Use the upper limit to ignore obstacles that are too far from the vehicle.

RobotRadius — Radius of vehicle

0.1 (default) | scalar

Radius of the vehicle in meters, specified as a scalar. This dimension defines the smallest circle that can circumscribe your vehicle. The vehicle radius is used to account for vehicle size when computing the obstacle-free direction.

SafetyDistance — Safety distance around vehicle

0.1 (default) | scalar

Safety distance around the vehicle, specified as a scalar in meters. This is a safety distance to leave around the vehicle position in addition to the value of the RobotRadius parameter. The sum of the vehicle radius and the safety distance is used to compute the obstacle-free direction.

MinTurningRadius — Minimum turning radius at current speed

0.1 (default) | scalar

Minimum turning radius in meters for the vehicle moving at its current speed, specified as a scalar.

${\bf TargetDirectionWeight-Cost\ function\ weight\ for\ target\ direction}$

5 (default) | scalar

Cost function weight for moving toward the target direction, specified as a scalar. To follow a target direction, set this weight to be higher than the sum of the CurrentDirectionWeight and PreviousDirectionWeight properties. To ignore the target direction cost, set this weight to zero.

CurrentDirectionWeight — Cost function weight for current direction

2 (default) | scalar

Cost function weight for moving the robot in the current heading direction, specified as a scalar. Higher values of this weight produce efficient paths. To ignore the current direction cost, set this weight to zero.

PreviousDirectionWeight — Cost function weight for previous direction

2 (default) | scalar

Cost function weight for moving in the previously selected steering direction, specified as a scalar. Higher values of this weight produces smoother paths. To ignore the previous direction cost, set this weight to zero.

HistogramThresholds — Thresholds for binary histogram computation

```
[3 10] (default) | 2-element vector
```

Thresholds for binary histogram computation, specified as a 2-element vector. The algorithm uses these thresholds to compute the binary histogram from the polar obstacle density. Polar obstacle density values higher than the upper threshold are represented as occupied space (1) in the binary histogram. Values smaller than the lower threshold are represented as free space (0). Values that fall between the limits are set to the values in the previous binary histogram, with the default being free space (0).

UseLidarScan — Use lidarScan object as scan input

```
false (default) | true
```

Use lidarScan object as scan input, specified as either true or false.

Usage

Syntax

```
steeringDir = vfh(scan,targetDir)
steeringDir = vfh(ranges,angles,targetDir)
```

Description

steeringDir = vfh(scan,targetDir) finds an obstacle-free steering direction using the VFH+
algorithm for the input lidarScan object, scan. A target direction is given based on the target
location.

To enable this syntax, you must set the UseLidarScan property to true. For example:

```
mcl = monteCarloLocalization('UseLidarScan', true);
...
[isUpdated, pose, covariance] = mcl(odomPose, scan);
```

steeringDir = vfh(ranges, angles, targetDir) defines the lidar scan with two vectors: ranges and angles.

Input Arguments

scan — Lidar scan readings

lidarScan object

Lidar scan readings, specified as a lidarScan object.

Dependencies

To use this argument, you must set the UseLidarScan property to true.

```
mcl.UseLidarScan = true;
```

ranges — Range values from scan data

vector

Range values from scan data, specified as a vector in meters. These range values are distances from a sensor at given angles. The vector must be the same length as the corresponding angles vector.

angles — Angle values from scan data

vector

Angle values from scan data, specified as a vector in radians. These angle values are the specific angles of the given ranges. The vector must be the same length as the corresponding ranges vector.

targetDir — Target direction for vehicle

scalar

Target direction for the vehicle, specified as a scalar in radians. The forward direction of the vehicle is considered zero radians, with positive angles measured counterclockwise.

Output Arguments

steeringDir — Steering direction for vehicle

scalar

Steering direction for the vehicle, specified as a scalar in radians. This obstacle-free direction is calculated based on the VFH+ algorithm. The forward direction of the vehicle is considered zero radians, with positive angles measured counterclockwise.

Object Functions

To use an object function, specify the System object as the first input argument. For example, to release system resources of a System object named obj, use this syntax:

release(obj)

Specific to controllerVFH

show Display VectorFieldHistogram information in figure window

Common to All System Objects

step Run System object algorithm

release Release resources and allow changes to System object property values and input

characteristics

reset Reset internal states of System object

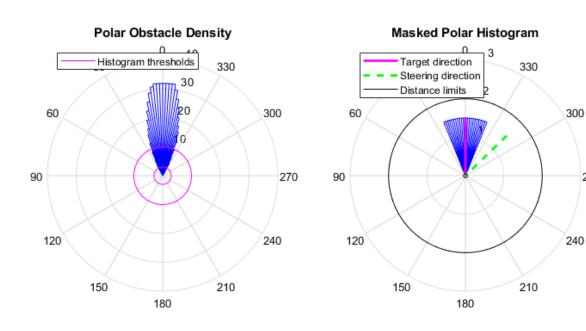
Examples

Create a Vector Field Histogram Object and Visualize Data

This example shows how to calculate a steering direction based on input laser scan data.

Create a controllerVFH object. Set the UseLidarScan property to true.

```
vfh = controllerVFH;
vfh.UseLidarScan = true;
Input laser scan data and target direction.
ranges = 10*ones(1,500);
ranges(1,225:275) = 1.0;
angles = linspace(-pi,pi,500);
targetDir = 0;
Create a lidarScan object by specifying the ranges and angles.
scan = lidarScan(ranges,angles);
Compute an obstacle-free steering direction.
steeringDir = vfh(scan,targetDir);
Visualize the VectorFieldHistogram computation.
h = figure;
set(h,'Position',[50 50 800 400])
show(vfh)
```



270

References

- [1] Borenstein, J., and Y. Koren. "The Vector Field Histogram Fast Obstacle Avoidance for Mobile Robots." IEEE Journal of Robotics and Automation. Vol. 7, Number 3, 1991, pp.278-88.
- [2] Ulrich, I., and J. Borenstein. "VFH: Reliable Obstacle Avoidance for Fast Mobile Robots."

 Proceedings. 1998 IEEE International Conference on Robotics and Automation. (1998): 1572–1577.

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

Usage notes and limitations:

Use in a MATLAB Function block is not supported.

Lidar scans require a limited size in code generation. The lidar scans, scan, are limited to 4000 points (range and angles) as a maximum.

For additional information about code generation for System objects, see "System Objects in MATLAB Code Generation" (MATLAB Coder)

See Also

lidarScan|show

Topics

"Obstacle Avoidance with TurtleBot and VFH"

"Vector Field Histogram"

show

Display VectorFieldHistogram information in figure window

Syntax

```
show(vfh)
show(vfh, 'Parent', parent)
h = show( )
```

Description

show(vfh) shows histograms calculated by the VFH+ algorithm in a figure window. The figure also includes the parameters of the controllerVFH object and range values from the last object call.

```
show(vfh, 'Parent', parent) sets the specified axes handle, parent, to the axes.
```

h = show(____) returns the figure object handle created by show using any of the arguments from the previous syntaxes.

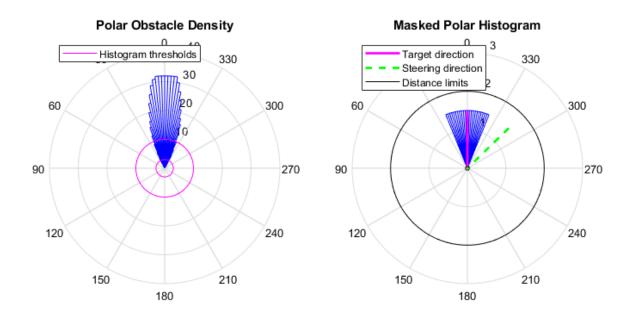
Examples

Create a Vector Field Histogram Object and Visualize Data

This example shows how to calculate a steering direction based on input laser scan data.

Create a controllerVFH object. Set the UseLidarScan property to true.

```
vfh = controllerVFH;
vfh.UseLidarScan = true;
Input laser scan data and target direction.
ranges = 10*ones(1,500);
ranges(1,225:275) = 1.0;
angles = linspace(-pi,pi,500);
targetDir = 0;
Create a lidarScan object by specifying the ranges and angles.
scan = lidarScan(ranges,angles);
Compute an obstacle-free steering direction.
steeringDir = vfh(scan,targetDir);
Visualize the VectorFieldHistogram computation.
h = figure;
set(h,'Position',[50 50 800 400])
show(vfh)
```



Input Arguments

vfh — Vector field histogram algorithm

controllerVFH object

Vector field histogram algorithm, specified as a controllerVFH object. This object contains all the parameters for tuning the VFH+ algorithm.

parent — Axes properties

handle

Axes properties, specified as a handle.

Output Arguments

h — Axes handles for VFH algorithm display

Axes array

Axes handles for VFH algorithm display, specified as an Axes array. The VFH histogram and HistogramThresholds are shown in the first axes. The binary histogram, range sensor readings, target direction, and steering directions are shown in the second axes.

See Also

controllerVFH

controllerPurePursuit

Create controller to follow set of waypoints

Description

The controllerPurePursuit System object creates a controller object used to make a differential-drive vehicle follow a set of waypoints. The object computes the linear and angular velocities for the vehicle given the current pose. Successive calls to the object with updated poses provide updated velocity commands for the vehicle. Use the MaxAngularVelocity and DesiredLinearVelocity properties to update the velocities based on the vehicle's performance.

The LookaheadDistance property computes a look-ahead point on the path, which is a local goal for the vehicle. The angular velocity command is computed based on this point. Changing LookaheadDistance has a significant impact on the performance of the algorithm. A higher lookahead distance results in a smoother trajectory for the vehicle, but can cause the vehicle to cut corners along the path. A low look-ahead distance can result in oscillations in tracking the path, causing unstable behavior. For more information on the pure pursuit algorithm, see "Pure Pursuit Controller".

Note Starting in R2016b, instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, y = step(obj,x) and y = obj(x) perform equivalent operations.

To compute linear and angular velocity control commands:

- 1 Create the controllerPurePursuit object and set its properties.
- **2** Call the object with arguments, as if it were a function.

To learn more about how System objects work, see What Are System Objects?.

Creation

Syntax

```
controller = controllerPurePursuit
controller = controllerPurePursuit(Name, Value)
```

Description

controller = controllerPurePursuit creates a pure pursuit object that uses the pure pursuit
algorithm to compute the linear and angular velocity inputs for a differential drive vehicle.

controller = controllerPurePursuit(Name, Value) creates a pure pursuit object with
additional options specified by one or more Name, Value pairs. Name is the property name and Value
is the corresponding value. Name must appear inside single quotes (' '). You can specify several

name-value pair arguments in any order as Name1, Value1, ..., NameN, ValueN. Properties not specified retain their default values.

Example: controller = controllerPurePursuit('DesiredLinearVelocity', 0.5)

Properties

DesiredLinearVelocity — Desired constant linear velocity

0.1 (default) | scalar in meters per second

Desired constant linear velocity, specified as a scalar in meters per second. The controller assumes that the vehicle drives at a constant linear velocity and that the computed angular velocity is independent of the linear velocity.

Data Types: double

LookaheadDistance — Look-ahead distance

1.0 (default) | scalar in meters

Look-ahead distance, specified as a scalar in meters. The look-ahead distance changes the response of the controller. A vehicle with a higher look-ahead distance produces smooth paths but takes larger turns at corners. A vehicle with a smaller look-ahead distance follows the path closely and takes sharp turns, but potentially creating oscillations in the path.

Data Types: double

MaxAngularVelocity — Maximum angular velocity

1.0 (default) | scalar in radians per second

Maximum angular velocity, specified a scalar in radians per second. The controller saturates the absolute angular velocity output at the given value.

Data Types: double

Waypoints — Waypoints

[] (default) | n-by-2 array

Waypoints, specified as an n-by-2 array of [x y] pairs, where n is the number of waypoints. You can generate the waypoints from the mobileRobotPRM class or from another source.

Data Types: double

Usage

Syntax

```
[vel,angvel] = controller(pose)
[vel,angvel,lookaheadpoint] = controller(pose)
```

Description

[vel,angvel] = controller(pose) processes the vehicle's position and orientation, pose, and outputs the linear velocity, vel, and angular velocity, angvel.

[vel,angvel,lookaheadpoint] = controller(pose) returns the look-ahead point, which is a location on the path used to compute the velocity commands. This location on the path is computed using the LookaheadDistance property on the controller object.

Input Arguments

pose — Position and orientation of vehicle

3-by-1 vector in the form [x y theta]

Position and orientation of vehicle, specified as a 3-by-1 vector in the form [x y theta]. The vehicle pose is an x and y position with angular orientation θ (in radians) measured from the x-axis.

Output Arguments

vel — Linear velocity

scalar in meters per second

Linear velocity, specified as a scalar in meters per second.

Data Types: double

angvel — Angular velocity

scalar in radians per second

Angular velocity, specified as a scalar in radians per second.

Data Types: double

lookaheadpoint — Look-ahead point on path

[x y] vector

Look-ahead point on the path, returned as an $[x \ y]$ vector. This value is calculated based on the LookaheadDistance property.

Object Functions

To use an object function, specify the System object as the first input argument. For example, to release system resources of a System object named obj, use this syntax:

release(obj)

Specific to controllerPurePursuit

info Characteristic information about controllerPurePursuit object

Common to All System Objects

step Run System object algorithm

release Release resources and allow changes to System object property values and input

characteristics

reset Reset internal states of System object

Examples

Get Additional Pure Pursuit Object Information

Use the info method to get more information about a controllerPurePursuit object. The info function returns two fields, RobotPose and LookaheadPoint, which correspond to the current position and orientation of the robot and the point on the path used to compute outputs from the last call of the object.

Create a controllerPurePursuit object.

```
pp = controllerPurePursuit;
Assign waypoints.
pp.Waypoints = [0 0;1 1];
```

Compute control commands using the pp object with the initial pose [x y theta] given as the input.

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

Usage notes and limitations:

Use in a MATLAB Function block is not supported.

For additional information about code generation for System objects, see "System Objects in MATLAB Code Generation" (MATLAB Coder)

See Also

binaryOccupancyMap | binaryOccupancyMap | controllerVFH | occupancyMap |
occupancyMap

Topics

"Pure Pursuit Controller"

info

Characteristic information about controllerPurePursuit object

Syntax

```
controllerInfo = info(controller)
```

Description

controllerInfo = info(controller) returns a structure, controllerInfo, with additional
information about the status of the controllerPurePursuit object, controller. The structure
contains the fields, RobotPose and LookaheadPoint.

Examples

Get Additional Pure Pursuit Object Information

Use the info method to get more information about a controllerPurePursuit object. The info function returns two fields, RobotPose and LookaheadPoint, which correspond to the current position and orientation of the robot and the point on the path used to compute outputs from the last call of the object.

Create a controllerPurePursuit object.

```
pp = controllerPurePursuit;
Assign waypoints.
pp.Waypoints = [0 0;1 1];
```

Compute control commands using the pp object with the initial pose [x y theta] given as the input.

Input Arguments

controller — Pure pursuit controller

```
controllerPurePursuit object
```

Pure pursuit controller, specified as a controllerPurePursuit object.

Output Arguments

controllerInfo — Information on the controllerPurePursuit object

structure

Information on the controllerPurePursuit object, returned as a structure. The structure contains two fields:

- RobotPose A three-element vector in the form [x y theta] that corresponds to the x-y position and orientation of the vehicle. The angle, theta, is measured in radians with positive angles measured counterclockwise from the x-axis.
- LookaheadPoint- A two-element vector in the form $[x \ y]$. The location is a point on the path that was used to compute outputs of the last call to the object.

See Also

controllerPurePursuit

Topics

"Pure Pursuit Controller"

dubinsConnection

Dubins path connection type

Description

The dubinsConnection object holds information for computing a dubinsPathSegment path segment to connect between poses. A Dubins path segment connects two poses as a sequence of three motions. The motion options are:

- Straight
- Left turn at maximum steer
- · Right turn at maximum steer

A Dubins path segment only allows motion in the forward direction.

Use this connection object to define parameters for a robot motion model, including the minimum turning radius and options for path types. To generate a path segment between poses using this connection type, call the connect function.

Creation

Syntax

```
dubConnObj = dubinsConnection
dubConnObj = dubinsConnection(Name, Value)
```

Description

dubConnObj = dubinsConnection creates an object using default property values.

dubConnObj = dubinsConnection(Name, Value) specifies property values using name-value
pairs. To set multiple properties, specify multiple name-value pairs.

Properties

MinTurningRadius — Minimum turning radius of the vehicle

1 (default) | positive scalar in meters

Minimum turning radius of the vehicle, specified as a positive scalar in meters. The minimum turning radius is for the smallest circle the vehicle can make with maximum steer in a single direction.

Data Types: double

DisabledPathTypes — Path types to disable

{} (default) | cell array of three-element character vectors | vector of three-element string scalars

Dubins path types to disable, specified as a cell array of three-element character vectors or vector of string scalars. The cell array defines three sequences of motions that are prohibited by the vehicle motion model.

Motion Type	Description
"S"	Straight
	Left turn at the maximum steering angle of the vehicle
	Right turn at the maximum steering angle of the vehicle

To see all available path types, see the AllPathTypes property.

```
For Dubins connections, the available path types are: {"LSL"} {"RSR"} {"RSR"} {"RSR"}
```

```
Example: ["LSL", "LSR"]
Data Types: string | cell
```

AllPathTypes — All possible path types

cell array of character vectors

This property is read-only.

All possible path types, returned as a cell array of character vectors. This property lists all types. To disable certain types, specify types from this list in DisabledPathTypes.

```
For Dubins connections, the available path types are: {'LSL'} {'RSR'} {'RSR'} {'RLR'} {'LRL'}.
```

Data Types: cell

Object Functions

connect Connect poses for given connection type

Examples

Connect Poses Using Dubins Connection Path

```
Create a dubinsConnection object.

dubConnObj = dubinsConnection;

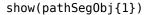
Define start and goal poses as [x y theta] vectors.

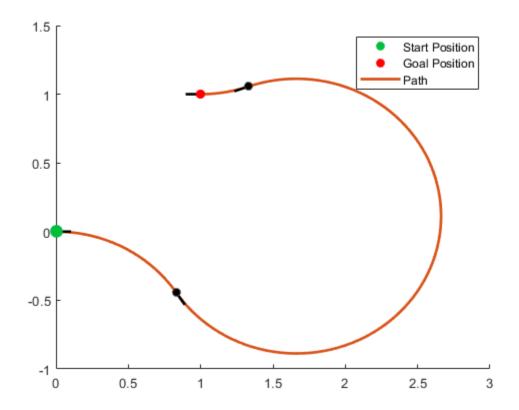
startPose = [0 0 0];
goalPose = [1 1 pi];

Calculate a valid path segment to connect the poses.

[pathSegObj, pathCosts] = connect(dubConnObj, startPose, goalPose);
```

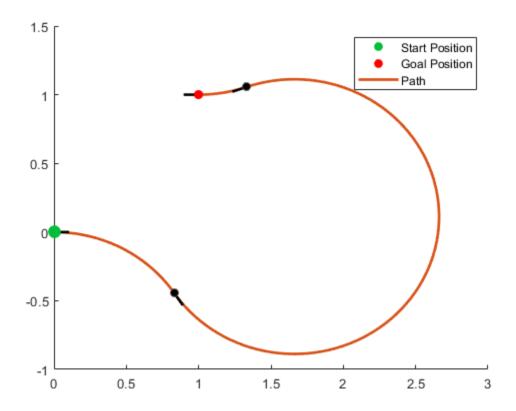
Show the generated path.





Modify Connection Types for Dubins Path

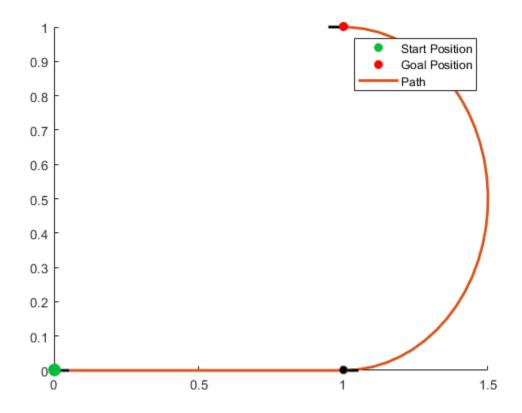
```
Create a dubinsConnection object.
dubConnObj = dubinsConnection;
Define start and goal poses as [x y theta] vectors.
startPose = [0 0 0];
goalPose = [1 1 pi];
Calculate a valid path segment to connect the poses.
pathSegObj = connect(dubConnObj,startPose,goalPose);
Show the generated path. Notice the direction of the turns.
show(pathSegObj{1})
```



pathSegObj{1}.MotionTypes

```
ans = 1x3 cell {'R'} {'L'} {'R'}
```

Disable this specific motion sequence in a new connection object. Reduce the MinTurningRadius if the robot is more maneuverable. Connect the poses again to get a different path.



References

[1] Shkel, Andrei M., and Vladimir Lumelsky. "Classification of the Dubins set." *Robotics and Autonomous Systems*. Vol. 34, No. 4, 2001, pp. 179–202.

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

Objects

dubinsPathSegment | reedsSheppConnection | reedsSheppPathSegment

Functions

connect | interpolate | show

dubinsPathSegment

Dubins path segment connecting two poses

Description

The dubinsPathSegment object holds information for a Dubins path segment that connects two poses as a sequence of three motions. The motion options are:

- Straight
- Left turn at maximum steer
- · Right turn at maximum steer

Creation

To generate a dubinsPathSegment object, use the connect function with a dubinsConnection object:

dubPathSeg = connect(connectionObj,start,goal) connects the start and goal pose using
the specified connection type object.

To specifically define a path segment:

dubPathSeg = dubinsPathSegment(connectionObj,start,goal,motionLengths,
motionTypes) specifies the Dubins connection type, the start and goal poses, and the corresponding
motion lengths and types. These values are set to the corresponding properties in the object.

Properties

MinTurningRadius — Minimum turning radius of vehicle

positive scalar

This property is read-only.

Minimum turning radius of the vehicle, specified as a positive scalar in meters. This value corresponds to the radius of the turning circle at the maximum steering angle of the vehicle.

Data Types: double

StartPose — Initial pose of the vehicle

 $[x, y, \Theta]$ vector

This property is read-only.

Initial pose of the vehicle at the start of the path segment, specified as an $[x, y, \Theta]$ vector. x and y are in meters. Θ is in radians.

Data Types: double

GoalPose — **Goal pose of the vehicle**

[x, y, Θ] vector

This property is read-only.

Goal pose of the vehicle at the end of the path segment, specified as an $[x, y, \Theta]$ vector. x and y are in meters. Θ is in radians.

Data Types: double

MotionLengths — Length of each motion

three-element numeric vector

This property is read-only.

Length of each motion in the path segment, in world units, specified as a three-element numeric vector. Each motion length corresponds to a motion type specified in MotionTypes.

Data Types: double

MotionTypes — Type of each motion

three-element string cell array

This property is read-only.

Type of each motion in the path segment, specified as a three-element string cell array.

Motion Type	Description
"S"	Straight
	Left turn at the maximum steering angle of the vehicle
"R"	Right turn at the maximum steering angle of the vehicle

Each motion type corresponds to a motion length specified in MotionLengths.

For Dubins connections, the available path types are: ${"LSL"} {"RSR"} {"RSR"} {"RLR"}.$

Example: {"R" "S" "R"}

Data Types: cell

Length — Length of path segment

positive scalar

This property is read-only.

Length of the path segment, specified as a positive scalar in meters. This length is just a sum of the elements in MotionLengths.

Data Types: double

Object Functions

show Visualize path segment

Examples

Connect Poses Using Dubins Connection Path

```
Create a dubinsConnection object.
```

```
dubConnObj = dubinsConnection;
```

Define start and goal poses as $[x \ y \ theta]$ vectors.

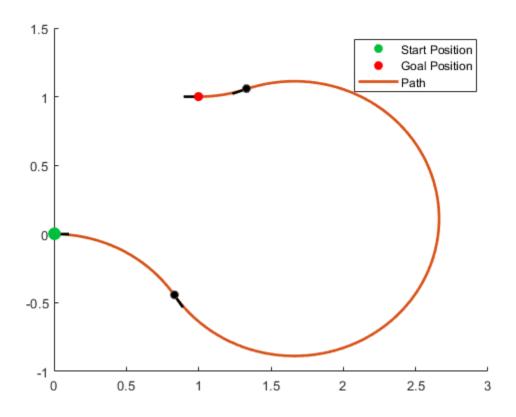
```
startPose = [0 0 0];
goalPose = [1 1 pi];
```

Calculate a valid path segment to connect the poses.

```
[pathSegObj, pathCosts] = connect(dubConnObj,startPose,goalPose);
```

Show the generated path.

show(pathSegObj{1})



Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

Objects

dubinsConnection | reedsSheppConnection | reedsSheppPathSegment

Functions

connect|interpolate|show

dynamicCapsuleList

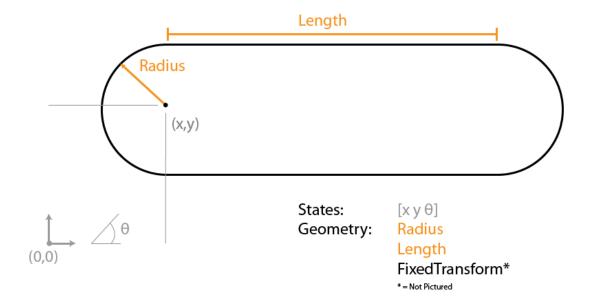
Dynamic capsule-based obstacle list

Description

The dynamicCapsuleList object manages two lists of capsule-based collision objects in 2-D space. Collision objects are separated into two lists, ego bodies and obstacles. For ego bodies and obstacles in 3-D, see the dynamicCapsuleList3D object.

Each collision object in the two lists has three key elements:

- **ID** -- Integer that identifies each object, stored in the **EgoIDs** property for ego bodies and the **ObstacleIDs** property for obstacles.
- **States** Location and orientation of the object as an *M*-by-3 matrix, where each row is of form [x y theta] and *M* is the number of states along the path of the object in the world frame. The list of states assumes each state is separated by a fixed time interval. *xy*-positions are in meters, and theta is in radians. The default local origin is located at the center of the left semicircle of the capsule.
- **Geometry** Size of the capsule-based object based on a specified length and radius. The radius applies to the semicircle end caps, and the length applies to the central rectangle length. To shift the capsule geometry and local origin relative to the default origin point, specify a fixed transform relative to the local frame of the capsule.



Use the object functions to dynamically add, remove, and update the geometries and states of the various objects in your environment. To add an ego body, see the addEgo object function. To add an obstacle, see the addObstacle object function.

After specifying all of the object states, validate the ego-body paths and check for collisions with obstacles at every step using the checkCollision object function. The function only checks if an ego body collides with an obstacle, ignoring collisions between only obstacles or only ego bodies.

Creation

Syntax

obstacleList = dynamicCapsuleList

Description

obstacleList = dynamicCapsuleList creates a dynamic capsule-based obstacle list with no ego
bodies or obstacles. To begin building an obstacle list, use the addEgo or addObstacle object
functions.

Properties

MaxNumSteps — Maximum number of time steps in obstacle list

31 (default) | positive integer

Maximum number of time steps in the obstacle list, specified as a positive integer. The number of steps determines to the maximum length of the States field for a specific ego body or obstacle.

Data Types: double

EgoIDs — List of IDs for ego bodies

vector of positive integers

This property is read-only.

List of identifiers for ego bodies, returned as a vector of positive integers.

Data Types: double

ObstacleIDs — **IDs** for obstacles

vector of positive integers

This property is read-only.

List of identifiers for obstacles, returned as a vector of positive integers.

Data Types: double

NumObstacles — Number of obstacles in list

integer

This property is read-only.

Number of obstacles in list, returned as an integer.

Data Types: double

NumEgos — Number of ego bodies in list

integer

This property is read-only.

Number of ego bodies in list, returned as an integer.

Data Types: double

Object Functions

addEgo Add ego bodies to capsule list addObstacle Add obstacles to 2-D capsule list

checkCollision Check for collisions between ego bodies and obstacles

egoGeometry Geometric properties of ego bodies

egoPose Poses of ego bodies

obstacleGeometry Geometric properties of obstacles

obstaclePose Poses of obstacles

removeEgo Remove ego bodies from capsule list removeObstacle Remove obstacles from capsule list

show Display ego bodies and obstacles in environment updateEgoGeometry Update geometric properties of ego bodies

updateEgoPose Update states of ego bodies

updateObstacleGeometry Update geometric properties of obstacles

updateObstaclePose Update states of obstacles

Examples

Build Ego Body Paths and Check for Collisions with Obstacles

Build an ego body path and maintain obstacle states using the dynamicCapsuleList object. Visualize the states of all objects in the environment at different timestamps. Validate the path of the ego body by checking for collisions with obstacles in the environment.

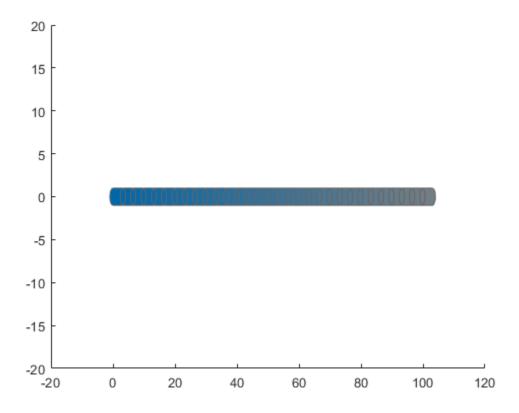
Create the dynamicCapsuleList object. Extract the maximum number of steps to use as the number of time stamps for your object paths.

```
obsList = dynamicCapsuleList;
numSteps = obsList.MaxNumSteps;
```

Add Ego Body

Define an ego body by specifying the ID, geometry, and state together in a structure. The capsule geometry has a length of 3 m and radius of 1 m. Specify the state as a linear path from x = 0m to x = 100m.

```
egoID1 = 1;
geom = struct("Length",3,"Radius",1,"FixedTransform",eye(3));
states = linspace(0,1,obsList.MaxNumSteps)'.*[100 0 0];
egoCapsule1 = struct('ID',egoID1,'States',states,'Geometry',geom);
addEgo(obsList,egoCapsule1);
show(obsList,"TimeStep",[1:numSteps]);
ylim([-20 20])
```

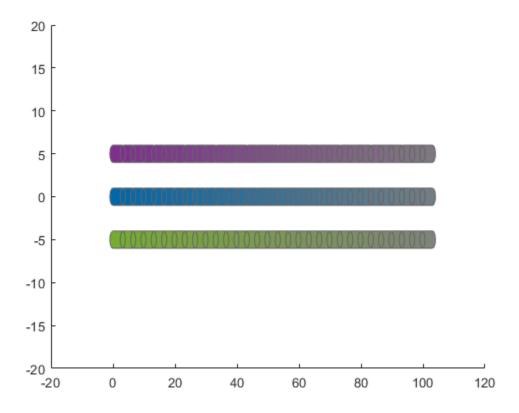


Add Obstacles

Specify states for two obstacles that are separated from the ego body by 5 m in opposite directions on the y-axis.. Assume the obstacles have the same geometry geom as the ego body.

```
obsState1 = states + [0 5 0];
obsState2 = states + [0 -5 0];

obsCapsule1 = struct('ID',1,'States',obsState1,'Geometry',geom);
obsCapsule2 = struct('ID',2,'States',obsState2,'Geometry',geom);
addObstacle(obsList,obsCapsule1);
addObstacle(obsList,obsCapsule2);
show(obsList,"TimeStep",[1:numSteps]);
ylim([-20 20])
```



Update Obstacles

Alter your obstacle locations and geometry dimensions over time. Use the previously generated structure, modify the fields, and update the obstacles using the updateObstacleGeometry and updateObstaclePose object functions. Reduces the radius of the first obstacle to 0.5 m, and change the path to move it towards the ego body.

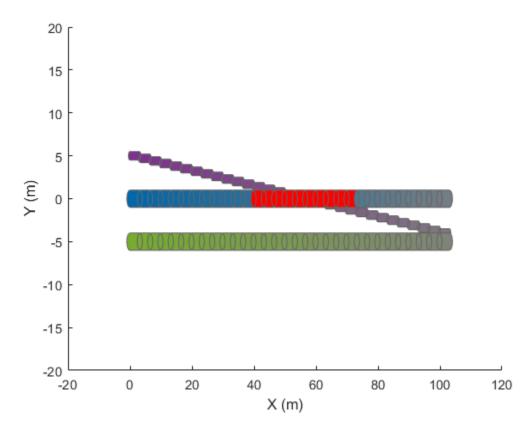
```
obsCapsule1.Geometry.Radius = 0.5;
obsCapsule1.States = ...
   [linspace(0,100,numSteps)' ... % x
        linspace(5,-4,numSteps)' ... % y
        zeros(numSteps,1)]; % theta

updateObstacleGeometry(obsList,1,obsCapsule1);
updateObstaclePose(obsList,1,obsCapsule1);
```

Check for Collisions

Visualize the new paths. Show where collisions between the ego body and an obstacle, which the display highlights in red. Notice that collisions between the obstacles are not checked.

```
show(obsList,"TimeStep",[1:numSteps],"ShowCollisions",1);
ylim([-20 20])
xlabel("X (m)")
ylabel("Y (m)")
```



Programmatically check for collisions by using the checkCollision object function. The function returns a vector of logical values that indicates the status of each time step. The vector is transposed for display purposes.

```
collisions = checkCollision(obsList)'
collisions = 1x31 logical array
   0
       0
           0
                                0
                        0
                            0
                                     0
                                         0
                                             0
                                                 0
                                                      1
                                                              1
                                                                  1
                                                                       1
                                                                           1
                                                                               1
                                                                                    1
                                                                                        1
                                                                                            1
                                                          1
```

To validate paths with a large number of steps, use the any function on the vector of collision values.

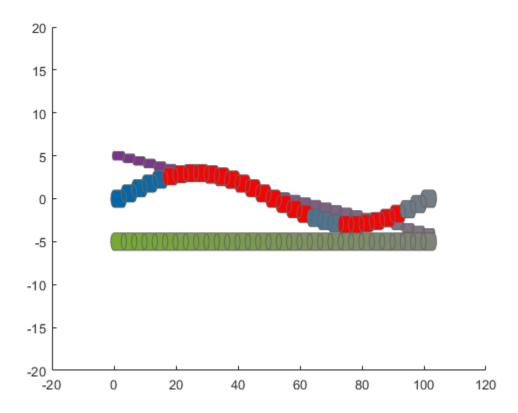
```
if any(collisions)
    disp("Collision detected.")
end
Collision detected.
```

Update Ego Path

Specify a new path for the ego body. Visualize the paths again, displaying collisions.

```
egoCapsule1.States = ...
[linspace(0,100,numSteps)' ... % x
    3*sin(linspace(0,2*pi,numSteps))' ... % y
    zeros(numSteps,1)]; % theta
```

```
updateEgoPose(obsList,1,egoCapsule1);
show(obsList,"TimeStep",[1:numSteps],"ShowCollisions",1);
ylim([-20 20])
```



Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

Objects

dynamicCapsuleList3D

Functions

addEgo | addObstacle | checkCollision | egoGeometry | egoPose | obstacleGeometry |
obstaclePose | removeEgo | removeObstacle | show | updateEgoGeometry | updateEgoPose |
updateObstacleGeometry | updateObstaclePose

Topics

"Highway Trajectory Planning Using Frenet Reference Path"

addEgo

Add ego bodies to capsule list

Syntax

```
addEgo(capsuleListObj,egoStruct)
status = addEgo(capsuleListObj,egoStruct)
```

Description

addEgo(capsuleListObj,egoStruct) adds one or more ego bodies to the 2-D dynamic capsule list with the specified ID, state, and geometry values given in egoStruct.

status = addEgo(capsuleListObj,egoStruct) additionally returns an indicator of whether
each specified ego body was added, updated, or a duplicate.

Examples

Build Ego Body Paths and Check for Collisions with Obstacles

Build an ego body path and maintain obstacle states using the dynamicCapsuleList object. Visualize the states of all objects in the environment at different timestamps. Validate the path of the ego body by checking for collisions with obstacles in the environment.

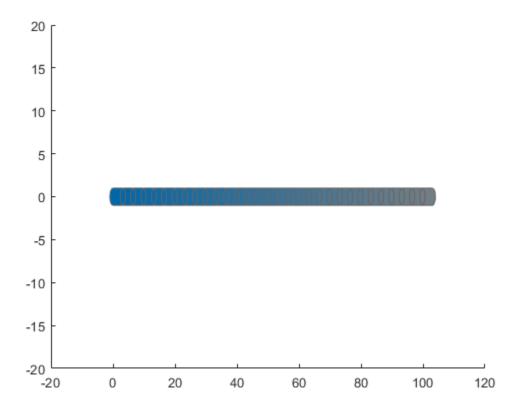
Create the dynamicCapsuleList object. Extract the maximum number of steps to use as the number of time stamps for your object paths.

```
obsList = dynamicCapsuleList;
numSteps = obsList.MaxNumSteps;
```

Add Ego Body

Define an ego body by specifying the ID, geometry, and state together in a structure. The capsule geometry has a length of 3 m and radius of 1 m. Specify the state as a linear path from x = 0m to x = 100m.

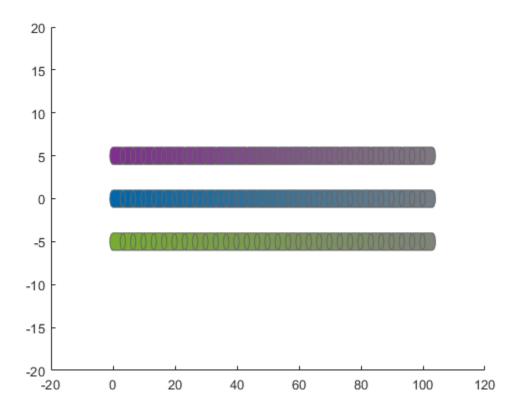
```
egoID1 = 1;
geom = struct("Length",3,"Radius",1,"FixedTransform",eye(3));
states = linspace(0,1,obsList.MaxNumSteps)'.*[100 0 0];
egoCapsule1 = struct('ID',egoID1,'States',states,'Geometry',geom);
addEgo(obsList,egoCapsule1);
show(obsList,"TimeStep",[1:numSteps]);
ylim([-20 20])
```



Add Obstacles

Specify states for two obstacles that are separated from the ego body by 5 m in opposite directions on the y-axis.. Assume the obstacles have the same geometry geom as the ego body.

```
obsState1 = states + [0 5 0];
obsState2 = states + [0 -5 0];
obsCapsule1 = struct('ID',1,'States',obsState1,'Geometry',geom);
obsCapsule2 = struct('ID',2,'States',obsState2,'Geometry',geom);
addObstacle(obsList,obsCapsule1);
addObstacle(obsList,obsCapsule2);
show(obsList,"TimeStep",[1:numSteps]);
ylim([-20 20])
```



Update Obstacles

Alter your obstacle locations and geometry dimensions over time. Use the previously generated structure, modify the fields, and update the obstacles using the updateObstacleGeometry and updateObstaclePose object functions. Reduces the radius of the first obstacle to 0.5 m, and change the path to move it towards the ego body.

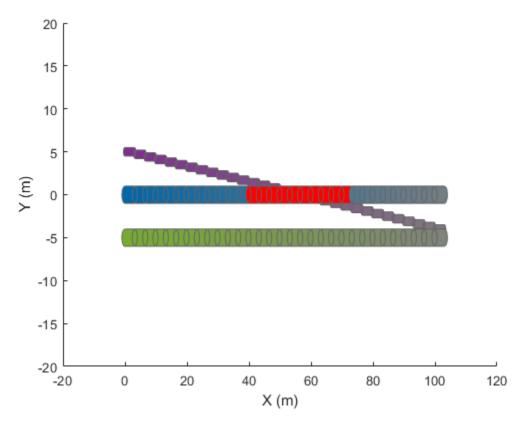
```
obsCapsule1.Geometry.Radius = 0.5;
obsCapsule1.States = ...
   [linspace(0,100,numSteps)' ... % x
        linspace(5,-4,numSteps)' ... % y
        zeros(numSteps,1)]; % theta

updateObstacleGeometry(obsList,1,obsCapsule1);
updateObstaclePose(obsList,1,obsCapsule1);
```

Check for Collisions

Visualize the new paths. Show where collisions between the ego body and an obstacle, which the display highlights in red. Notice that collisions between the obstacles are not checked.

```
show(obsList,"TimeStep",[1:numSteps],"ShowCollisions",1);
ylim([-20 20])
xlabel("X (m)")
ylabel("Y (m)")
```



Programmatically check for collisions by using the checkCollision object function. The function returns a vector of logical values that indicates the status of each time step. The vector is transposed for display purposes.

```
collisions = checkCollision(obsList)'
collisions = 1x31 logical array
   0
       0
           0
                                 0
                        0
                             0
                                     0
                                         0
                                              0
                                                  0
                                                      1
                                                          1
                                                               1
                                                                   1
                                                                       1
                                                                            1
                                                                                    1
                                                                                        1
                                                                                             1
                                                                                1
```

To validate paths with a large number of steps, use the any function on the vector of collision values.

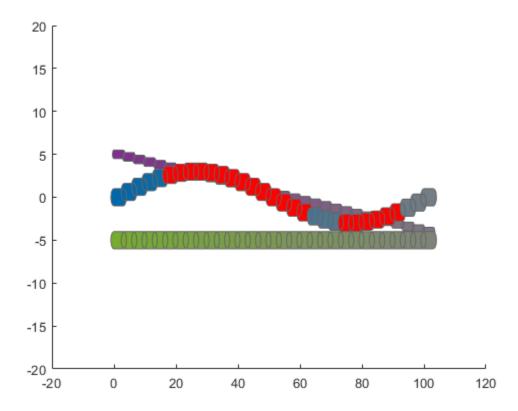
```
if any(collisions)
    disp("Collision detected.")
end
Collision detected.
```

Update Ego Path

Specify a new path for the ego body. Visualize the paths again, displaying collisions.

```
egoCapsule1.States = ...
[linspace(0,100,numSteps)' ... % x
    3*sin(linspace(0,2*pi,numSteps))' ... % y
    zeros(numSteps,1)]; % theta
```

```
updateEgoPose(obsList,1,egoCapsule1);
show(obsList,"TimeStep",[1:numSteps],"ShowCollisions",1);
ylim([-20 20])
```



Input Arguments

capsuleList0bj — Dynamic capsule list

dynamicCapsuleList object

Dynamic capsule list, specified as a dynamicCapsuleList object.

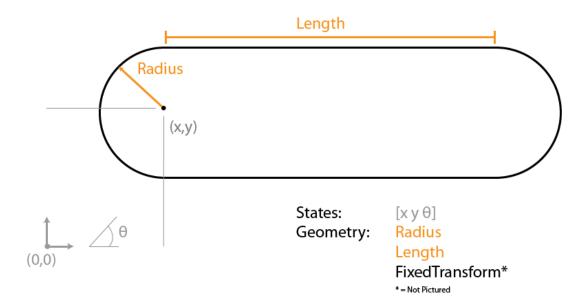
egoStruct — Ego body parameters

structure | *N*-element structure array

Ego body parameters, specified as an N-element structure or a structure array, where N is the number of added ego bodies. The fields of each structure define the ID, geometry, and states of an ego body:

- ID -- Integer that identifies each object. Stored in the EgoIDs property of the dynamicCapsuleList object specified by the capsuleListObj argument.
- States -- Location and orientation of the object as an *M*-by-3 matrix, where each row is of form [x y theta], and *M* is the number of states for the specified ego body in the world frame. The list of states assumes each state is separated by a fixed time interval. xy-positions are in meters and theta is in radians.

• Geometry — Structure with fields Length, Radius, and FixedTransform. These fields define the size of the capsule-based object using the specified length for the cylinder and semicircle radius for the end caps. To shift the capsule geometry from the default origin, specify the FixedTransform field as a fixed transform relative to the local frame of the capsule. To keep the default capsule origin, specify the transform as eye(3).



Output Arguments

status — Result of adding ego bodies

N-element column vector

Result of adding ego bodies, returned as a N-element column vector of ones, zeros, and negative ones. N is the number of ego bodies specified in the egoStruct argument. Each value indicates whether the associated body is added (1), updated (0), or a duplicate (-1). While adding ego bodies, if multiple structures with the same body ID are found in the structure array egoStruct, then the function marks the previous entry as duplicate and ignores it.

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

Objects

dynamicCapsuleList|dynamicCapsuleList3D

Functions

addObstacle | checkCollision | egoGeometry | egoPose | obstacleGeometry |
obstaclePose | removeEgo | removeObstacle | show | updateEgoGeometry | updateEgoPose |
updateObstacleGeometry | updateObstaclePose

Topics

"Highway Trajectory Planning Using Frenet Reference Path"

addObstacle

Add obstacles to 2-D capsule list

Syntax

```
addObstacle(capsuleListObj,obstacleStruct)
status = addObstacle(capsuleListObj,obstacleStruct)
```

Description

addObstacle(capsuleListObj,obstacleStruct) adds one or more obstacles to the 2-D dynamic capsule list with the specified ID, state, and geometry values given in obstacleStruct.

status = addObstacle(capsuleListObj,obstacleStruct) additionally returns an indicator
of whether each specified obstacle was added, updated, or a duplicate.

Examples

Build Ego Body Paths and Check for Collisions with Obstacles

Build an ego body path and maintain obstacle states using the dynamicCapsuleList object. Visualize the states of all objects in the environment at different timestamps. Validate the path of the ego body by checking for collisions with obstacles in the environment.

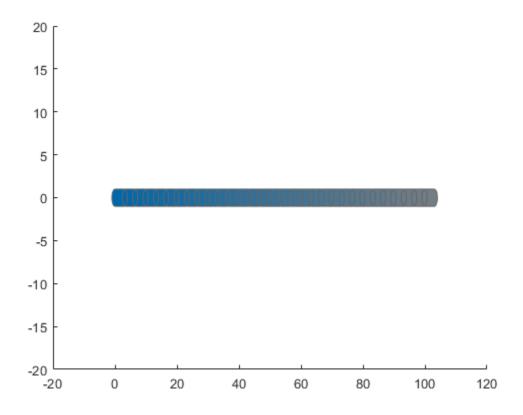
Create the dynamicCapsuleList object. Extract the maximum number of steps to use as the number of time stamps for your object paths.

```
obsList = dynamicCapsuleList;
numSteps = obsList.MaxNumSteps;
```

Add Ego Body

Define an ego body by specifying the ID, geometry, and state together in a structure. The capsule geometry has a length of 3 m and radius of 1 m. Specify the state as a linear path from x = 0m to x = 100m.

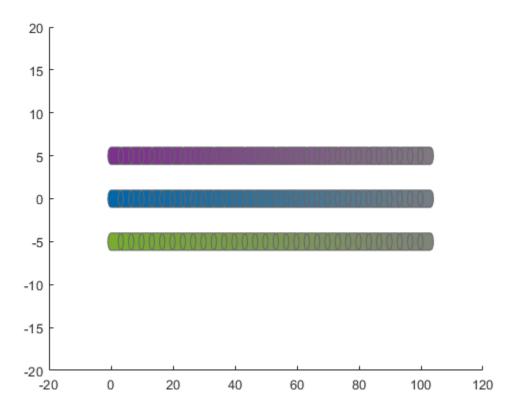
```
egoID1 = 1;
geom = struct("Length",3,"Radius",1,"FixedTransform",eye(3));
states = linspace(0,1,obsList.MaxNumSteps)'.*[100 0 0];
egoCapsule1 = struct('ID',egoID1,'States',states,'Geometry',geom);
addEgo(obsList,egoCapsule1);
show(obsList,"TimeStep",[1:numSteps]);
ylim([-20 20])
```



Add Obstacles

Specify states for two obstacles that are separated from the ego body by 5 m in opposite directions on the *y*-axis.. Assume the obstacles have the same geometry **geom** as the ego body.

```
obsState1 = states + [0 5 0];
obsState2 = states + [0 -5 0];
obsCapsule1 = struct('ID',1,'States',obsState1,'Geometry',geom);
obsCapsule2 = struct('ID',2,'States',obsState2,'Geometry',geom);
addObstacle(obsList,obsCapsule1);
addObstacle(obsList,obsCapsule2);
show(obsList,"TimeStep",[1:numSteps]);
ylim([-20 20])
```



Update Obstacles

Alter your obstacle locations and geometry dimensions over time. Use the previously generated structure, modify the fields, and update the obstacles using the updateObstacleGeometry and updateObstaclePose object functions. Reduces the radius of the first obstacle to 0.5 m, and change the path to move it towards the ego body.

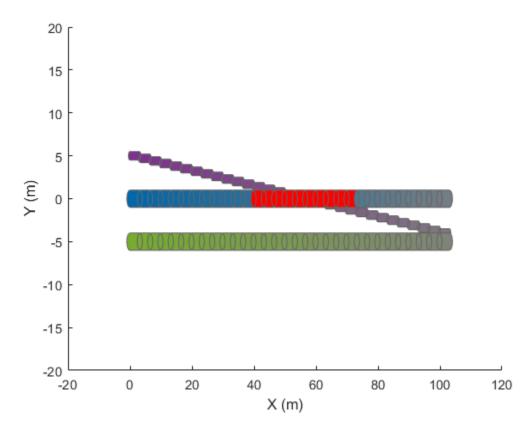
```
obsCapsule1.Geometry.Radius = 0.5;
obsCapsule1.States = ...
   [linspace(0,100,numSteps)' ... % x
        linspace(5,-4,numSteps)' ... % y
        zeros(numSteps,1)]; % theta

updateObstacleGeometry(obsList,1,obsCapsule1);
updateObstaclePose(obsList,1,obsCapsule1);
```

Check for Collisions

Visualize the new paths. Show where collisions between the ego body and an obstacle, which the display highlights in red. Notice that collisions between the obstacles are not checked.

```
show(obsList,"TimeStep",[1:numSteps],"ShowCollisions",1);
ylim([-20 20])
xlabel("X (m)")
ylabel("Y (m)")
```



Programmatically check for collisions by using the checkCollision object function. The function returns a vector of logical values that indicates the status of each time step. The vector is transposed for display purposes.

```
collisions = checkCollision(obsList)'
collisions = 1x31 logical array
   0
       0
           0
                                 0
                        0
                             0
                                     0
                                         0
                                             0
                                                  0
                                                      1
                                                          1
                                                              1
                                                                  1
                                                                       1
                                                                           1
                                                                               1
                                                                                    1
                                                                                        1
                                                                                            1
```

To validate paths with a large number of steps, use the any function on the vector of collision values.

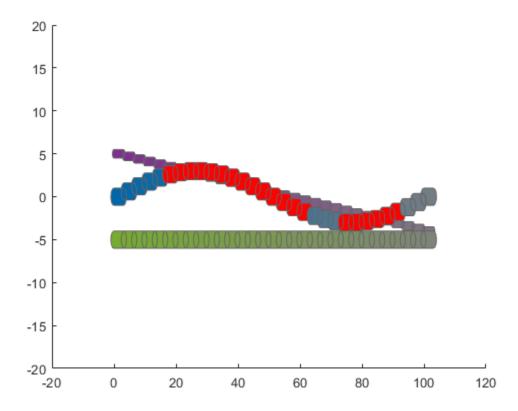
```
if any(collisions)
    disp("Collision detected.")
end
Collision detected.
```

Update Ego Path

Specify a new path for the ego body. Visualize the paths again, displaying collisions.

```
egoCapsule1.States = ...
[linspace(0,100,numSteps)' ... % x
    3*sin(linspace(0,2*pi,numSteps))' ... % y
    zeros(numSteps,1)]; % theta
```

```
updateEgoPose(obsList,1,egoCapsule1);
show(obsList,"TimeStep",[1:numSteps],"ShowCollisions",1);
ylim([-20 20])
```



Input Arguments

capsuleListObj — Dynamic capsule list

dynamicCapsuleList object

Dynamic capsule list, specified as a dynamicCapsuleList object.

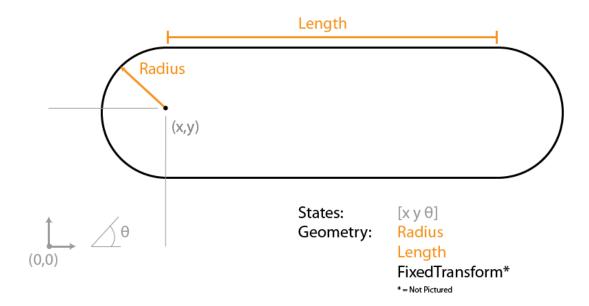
obstacleStruct — **Obstacle parameters**

structure | N-element structure array

Obstacle parameters, specified as an N-element structure or a structure array, where N is the number of added obstacles. The fields of each structure define the ID, geometry, and states of an obstacle:

- ID -- Integer that identifies each object. Stored in the ObstacleIDs property of the dynamicCapsuleList object specified by the capsuleListObj argument.
- States -- Location and orientation of the object as an *M*-by-3 matrix, where each row is of form [x y theta], and *M* is the number of states for the specified obstacle in the world frame. The list of states assumes each state is separated by a fixed time interval. xy-positions are in meters and theta is in radians.

• Geometry — Structure with fields Length, Radius, and FixedTransform. These fields define the size of the capsule-based object using the specified length for the cylinder and semicircle radius for the end caps. To shift the capsule geometry from the default origin, specify the FixedTransform field as a fixed transform relative to the local frame of the capsule. To keep the default capsule origin, specify the transform as eye(3).



Output Arguments

status — Result of adding obstacles

N-element column vector

Result of adding obstacles, returned as a N-element column vector of ones, zeros, and negative ones. N is the number of obstacles specified in the obstacleStruct argument. Each value indicates whether the associated body is added (1), updated (0), or a duplicate (-1). While adding obstacles, if multiple structures with the same body ID are found in the structure array obstaclesStruct, then the function marks the previous entry as duplicate and ignores it.

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

Objects

dynamicCapsuleList|dynamicCapsuleList3D

Functions

addEgo | checkCollision | egoGeometry | egoPose | obstacleGeometry | obstaclePose |
removeEgo | removeObstacle | show | updateEgoGeometry | updateEgoPose |
updateObstacleGeometry | updateObstaclePose

Topics

"Highway Trajectory Planning Using Frenet Reference Path"

checkCollision

Check for collisions between ego bodies and obstacles

Syntax

```
collisionFound = checkCollision(capsuleListObj)
[fullResults,distance] = checkCollision(capsuleListObj,options)
```

Description

collisionFound = checkCollision(capsuleListObj) checks each ego body for collisions with obstacles in the environment. The function indicates whether each ego body is in collision at each time step..

[fullResults,distance] = checkCollision(capsuleListObj,options) checks each ego body for collisions with obstacles in the environment, and returns the results using additional specified collision detection options options.

Examples

Build Ego Body Paths and Check for Collisions with Obstacles

Build an ego body path and maintain obstacle states using the dynamicCapsuleList object. Visualize the states of all objects in the environment at different timestamps. Validate the path of the ego body by checking for collisions with obstacles in the environment.

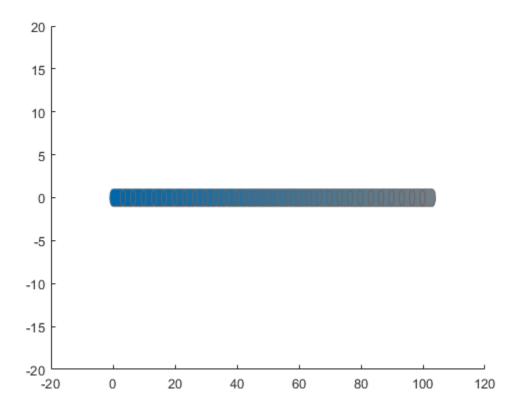
Create the dynamicCapsuleList object. Extract the maximum number of steps to use as the number of time stamps for your object paths.

```
obsList = dynamicCapsuleList;
numSteps = obsList.MaxNumSteps;
```

Add Ego Body

Define an ego body by specifying the ID, geometry, and state together in a structure. The capsule geometry has a length of 3 m and radius of 1 m. Specify the state as a linear path from x = 0m to x = 100m.

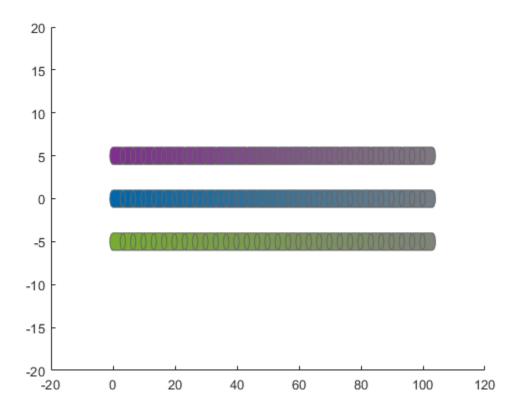
```
egoID1 = 1;
geom = struct("Length",3,"Radius",1,"FixedTransform",eye(3));
states = linspace(0,1,obsList.MaxNumSteps)'.*[100 0 0];
egoCapsule1 = struct('ID',egoID1,'States',states,'Geometry',geom);
addEgo(obsList,egoCapsule1);
show(obsList,"TimeStep",[1:numSteps]);
ylim([-20 20])
```



Add Obstacles

Specify states for two obstacles that are separated from the ego body by 5 m in opposite directions on the y-axis.. Assume the obstacles have the same geometry geom as the ego body.

```
obsState1 = states + [0 5 0];
obsState2 = states + [0 -5 0];
obsCapsule1 = struct('ID',1,'States',obsState1,'Geometry',geom);
obsCapsule2 = struct('ID',2,'States',obsState2,'Geometry',geom);
addObstacle(obsList,obsCapsule1);
addObstacle(obsList,obsCapsule2);
show(obsList,"TimeStep",[1:numSteps]);
ylim([-20 20])
```



Update Obstacles

Alter your obstacle locations and geometry dimensions over time. Use the previously generated structure, modify the fields, and update the obstacles using the updateObstacleGeometry and updateObstaclePose object functions. Reduces the radius of the first obstacle to 0.5 m, and change the path to move it towards the ego body.

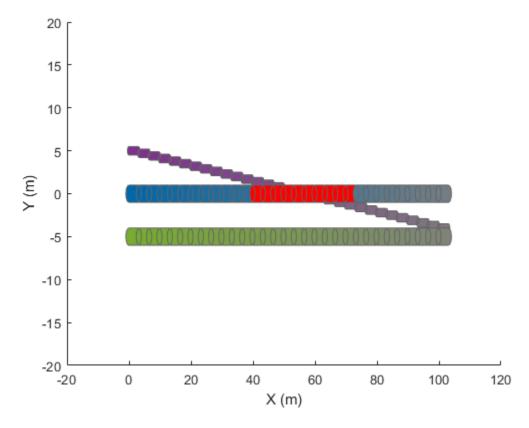
```
obsCapsule1.Geometry.Radius = 0.5;
obsCapsule1.States = ...
   [linspace(0,100,numSteps)' ... % x
        linspace(5,-4,numSteps)' ... % y
        zeros(numSteps,1)]; % theta

updateObstacleGeometry(obsList,1,obsCapsule1);
updateObstaclePose(obsList,1,obsCapsule1);
```

Check for Collisions

Visualize the new paths. Show where collisions between the ego body and an obstacle, which the display highlights in red. Notice that collisions between the obstacles are not checked.

```
show(obsList,"TimeStep",[1:numSteps],"ShowCollisions",1);
ylim([-20 20])
xlabel("X (m)")
ylabel("Y (m)")
```



Programmatically check for collisions by using the checkCollision object function. The function returns a vector of logical values that indicates the status of each time step. The vector is transposed for display purposes.

```
collisions = checkCollision(obsList)'
collisions = 1x31 logical array
   0
       0
           0
                                 0
                        0
                            0
                                     0
                                         0
                                             0
                                                  0
                                                      1
                                                          1
                                                              1
                                                                  1
                                                                       1
                                                                           1
                                                                               1
                                                                                    1
                                                                                        1
                                                                                            1
```

To validate paths with a large number of steps, use the any function on the vector of collision values.

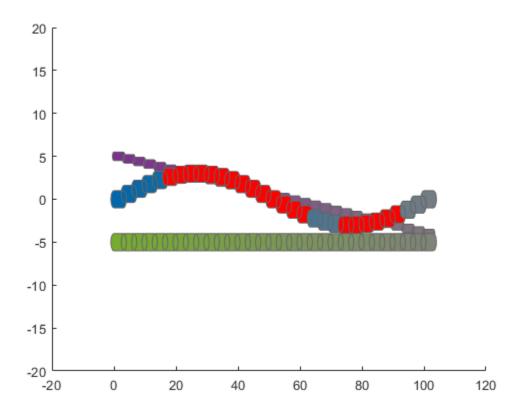
```
if any(collisions)
    disp("Collision detected.")
end
Collision detected.
```

Update Ego Path

Specify a new path for the ego body. Visualize the paths again, displaying collisions.

```
egoCapsule1.States = ...
[linspace(0,100,numSteps)' ... % x
    3*sin(linspace(0,2*pi,numSteps))' ... % y
    zeros(numSteps,1)]; % theta
```

```
updateEgoPose(obsList,1,egoCapsule1);
show(obsList, "TimeStep", [1:numSteps], "ShowCollisions", 1);
ylim([-20 20])
```



Input Arguments

capsuleList0bj — Dynamic capsule list

dynamicCapsuleList object | dynamicCapsuleList3D object

Dynamic capsule list, specified as a dynamicCapsuleList or dynamicCapsuleList3D object.

options — Collision detection options structure

Collision detection options, specified as a structure with these fields:

- FullResults -- Return the collision results for each obstacle separately , specified as a logical 0 (false) or 1 (true). See the fullResults output argument.
- ReturnDistance -- Return the distance calculation from collision checking, specified as a logical 0 (false) or 1 (true). See the distance output argument.

Data Types: struct

Output Arguments

collisionFound — Collision checking results

n-by-*e* matrix of logical values

Collision checking results, returned as an n-by-e matrix of logical values. By default, the function checks for any collision between any object, which returns an n-by-e matrix, where n is the maximum number of states for ego bodies in the specified capsuleListobj object, and e is the number of ego bodies.

Data Types: logical

fullResults — Full collision checking results for each obstacle

n-by-*o*-by-*e* array of logical values

Full collision checking results for each obstacle, returned as an n-by-o-by-e array of logical values. n is the maximum number of states for ego bodies in the specified capsuleListobj argument, o is the number of obstacles, and e is the number of ego bodies.

Dependencies

To return the fullResults output argument, specify the options input argument with the FullResults field set to true.

Data Types: logical

distance — Distance from obstacles

n-by-*e* numeric matrix | *n*-by-oby-*e* numeric array

Distance from obstacles, returned as an *n*-by-*e* numeric matrix or *n*-by-*o*by-*e* numeric array. The dimensions and behavior of the distance argument depend on the value of the FullResults field of the options argument

distance Dimensions	FullResults Value	Behavior
n-by-e numeric matrix	false	Returns the distance between each ego body and the closest obstacle at each time step. n is the maximum number of states for ego bodies specified in the capsuleListObj argument, and e is the number of ego bodies.
n-by-oby-e numeric array	true	Returns the distance between each ego body and each obstacle at each time step. o is the number of obstacles.

Dependencies

To return the distance output argument, specify the options input argument with the ReturnDistance field set to true.

Data Types: single | double

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

Objects

dynamicCapsuleList|dynamicCapsuleList3D

Functions

addEgo | addObstacle | egoGeometry | egoPose | obstacleGeometry | obstaclePose |
removeEgo | removeObstacle | show | updateEgoGeometry | updateEgoPose |
updateObstacleGeometry | updateObstaclePose

Topics

"Highway Trajectory Planning Using Frenet Reference Path"

egoGeometry

Geometric properties of ego bodies

Syntax

```
[egoIDs,geomStruct] = egoGeometry(capsuleList0bj)
[egoIDs,geomStruct] = egoGeometry(capsuleList0bj,selectEgoIDs)
[egoIDs,geomStruct,status] = egoGeometry(capsuleList0bj,selectEgoIDs)
```

Description

[egoIDs,geomStruct] = egoGeometry(capsuleListObj) returns the ego ID and the geometry parameters for each ego body in the capsule list.

[egoIDs,geomStruct] = egoGeometry(capsuleListObj,selectEgoIDs) specifies which ego
bodies to return the ID and geometry parameters for.

[egoIDs,geomStruct,status] = egoGeometry(capsuleListObj,selectEgoIDs) returns an indicator of whether each ID in selectEgoIDs exists.

Input Arguments

capsuleList0bj — Dynamic capsule list

dynamicCapsuleList object | dynamicCapsuleList3D object

Dynamic capsule list, specified as a dynamicCapsuleList or dynamicCapsuleList3D object.

selectEgoIDs — Ego body IDs

vector of positive integers

Ego body IDs, specified as a vector of positive integers. The function returns the ego IDs and geometry parameters for only the ego bodies specified in this vector.

Output Arguments

egoIDs — IDs of ego bodies

vector of positive integers

IDs of ego bodies, returned as a vector of positive integers.

geomStruct — Geometry parameters for ego bodies

structure | structure array

Geometry parameters for ego bodies, returned as a structure or structure array where each structure contains the fields from the structure in the Geometry field of the associated ego body. The fields of this structure depend on whether you are using a dynamicCapsuleList or dynamicCapsuleList3D object.

status — Indication of ego body existence

N-element column vector

Indication of ego body existence, returned as a N-element column vector of ones, zeros, and negative ones. Each value indicates whether the associated body exists (1), updated (0), or a duplicate (-1). If you specify the same ego body ID more than once in the selectEgoIDs argument, then the function marks all instances of that ID after the first as duplicates and ignores them.

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder $^{\text{\tiny TM}}$.

See Also

Objects

dynamicCapsuleList|dynamicCapsuleList3D

Functions

addEgo | addObstacle | checkCollision | egoPose | obstacleGeometry | obstaclePose |
removeEgo | removeObstacle | show | updateEgoGeometry | updateEgoPose |
updateObstacleGeometry | updateObstaclePose

Topics

"Highway Trajectory Planning Using Frenet Reference Path"

egoPose

Poses of ego bodies

Syntax

```
[egoIDs,poseStruct] = egoPose(capsuleList0bj)
[egoIDs,poseStruct] = egoPose(capsuleList0bj,selectEgoIDs)
[egoIDs,poseStruct,status] = egoPose(capsuleList0bj,selectEgoIDs)
```

Description

[egoIDs,poseStruct] = egoPose(capsuleListObj) returns the ego ID and the states for each ego body in the specified capsule list.

[egoIDs,poseStruct] = egoPose(capsuleListObj,selectEgoIDs) specifies which ego
bodies to return the ID and states for.

[egoIDs,poseStruct,status] = egoPose(capsuleListObj,selectEgoIDs) returns an indicator of whether each ID in selectEgoIDs exists.

Input Arguments

capsuleListObj — Dynamic capsule list

dynamicCapsuleList object | dynamicCapsuleList3D object

Dynamic capsule list, specified as a dynamicCapsuleList or dynamicCapsuleList3D object.

selectEgoIDs — Ego body IDs

vector of positive integers

Ego body IDs, specified as a vector of positive integers. The function returns the ego IDs and states for only the ego bodies specified in this vector.

Output Arguments

egoIDs — IDs of ego bodies

vector of positive integers

IDs of ego bodies, returned as a vector of positive integers.

poseStruct — States for ego bodies

structure | structure array

States for ego bodies, returned as a structure or structure array. Each structure contains a matrix of states for each ego body. The state matrix size depends on whether you are using a dynamicCapsuleList or dynamicCapsuleList3D object.

Data Types: struct

status — Indication of ego body existence

N-element column vector

Indication of ego body existence, returned as a N-element column vector of ones, zeros, and negative ones. Each value indicates whether the associated body exists (1), updated (0), or a duplicate (-1). If you specify the same ego body ID more than once in the selectEgoIDs argument, then the function marks all instances of that ID after the first as duplicates and ignores them.

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

Objects

dynamicCapsuleList|dynamicCapsuleList3D

Functions

addEgo | addObstacle | checkCollision | egoGeometry | obstaclePose | removeEgo |
removeObstacle | show | updateEgoGeometry | updateEgoPose | updateObstacleGeometry |
updateObstaclePose

Topics

"Highway Trajectory Planning Using Frenet Reference Path"

obstacleGeometry

Geometric properties of obstacles

Syntax

```
[obstacleIDs,geomStruct] = obstacleGeometry(capsuleList0bj)
[obstacleIDs,geomStruct] = obstacleGeometry(capsuleList0bj,select0bstacleIDs)
[obstacleIDs,geomStruct,status] = obstacleGeometry(capsuleList0bj,select0bstacleIDs)
```

Description

[obstacleIDs,geomStruct] = obstacleGeometry(capsuleListObj) returns the obstacle ID and the geometry parameters for each obstacle in the capsule list.

[obstacleIDs,geomStruct] = obstacleGeometry(capsuleListObj,selectObstacleIDs) specifies which obstacle to return the ID and geometry parameters for.

[obstacleIDs,geomStruct,status] = obstacleGeometry(capsuleListObj,
selectObstacleIDs) returns an indicator of whether each ID in selectobstacleIDs exists.

Input Arguments

capsuleListObj — Dynamic capsule list

dynamicCapsuleList object | dynamicCapsuleList3D object

Dynamic capsule list, specified as a dynamicCapsuleList or dynamicCapsuleList3D object.

selectObstacleIDs — Obstacle IDs

vector of positive integers

Obstacle IDs, specified as a vector of positive integers. The function returns the obstacle IDs and geometry parameters for only the obstacles specified in this vector.

Output Arguments

obstacleIDs — IDs of obstacles

vector of positive integers

IDs of obstacles, returned as a vector of positive integers.

geomStruct — Geometry parameters for obstacles

structure | structure array

Geometry parameters for obstacles, returned as a structure or structure array where each structure contains the fields from the structure in the Geometry field of the associated obstacle. The fields of this structure depend on whether you are using a dynamicCapsuleList or dynamicCapsuleList3D object.

status — Indication of obstacle existence

vector of ones, zeros, and negative ones

Indication of obstacle existence, returned as a N-element column vector of ones, zeros, and negative ones. Each value indicates whether the associated obstacle exists (1), updated (0), or a duplicate (-1). If you specify the same ego body ID more than once in the selectObstacleIDs argument, then the function marks all instances of that ID after the first as duplicates and ignores them.

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

Objects

dynamicCapsuleList|dynamicCapsuleList3D

Functions

addEgo | addObstacle | checkCollision | egoGeometry | egoPose | obstaclePose |
removeEgo | removeObstacle | show | updateEgoGeometry | updateEgoPose |
updateObstacleGeometry | updateObstaclePose

Topics

"Highway Trajectory Planning Using Frenet Reference Path"

obstaclePose

Poses of obstacles

Syntax

```
[obstacleIDs,poseStruct] = obstaclePose(capsuleListObj)
[obstacleIDs,poseStruct] = obstaclePose(capsuleListObj,selectObstacleIDs)
[obstacleIDs,poseStruct,status] = obstaclePose(capsuleListObj,selectObstacleIDs)
```

Description

[obstacleIDs,poseStruct] = obstaclePose(capsuleListObj) returns the obstacle ID and states for each obstacle in the specified capsule list.

[obstacleIDs,poseStruct] = obstaclePose(capsuleListObj,selectObstacleIDs) specifies which obstacles to return the ID and states for.

[obstacleIDs,poseStruct,status] = obstaclePose(capsuleListObj, selectObstacleIDs) returns an indicator of whether each ID in selectObstacleIDs exists.

Input Arguments

capsuleListObj — Dynamic capsule list

dynamicCapsuleList object | dynamicCapsuleList3D object

Dynamic capsule list, specified as a dynamicCapsuleList or dynamicCapsuleList3D object.

selectObstacleIDs — Obstacle IDs

vector of positive integers

Obstacle IDs, specified as a vector of positive integers. The function returns the obstacle IDs and states for only the obstacles specified in this vector.

Output Arguments

obstacleIDs — IDs of obstacles

vector of positive integers

IDs of obstacles, specified as a vector of positive integers.

poseStruct — States for ego bodies

structure | structure array

States for obstacles, returned as a structure or structure array. Each structure contains a matrix of states for each obstacle. The state matrix size depends on whether you are using a dynamicCapsuleList or dynamicCapsuleList3D object.

Data Types: struct

status — Indication of obstacle existence

N-element column vector

Indication of obstacle existence, returned as a *N*-element column vector of ones, zeros, and negative ones. Each value indicates whether the associated obstacle exists (1), updated (0), or a duplicate (-1). If you specify the same obstacle ID more than once in the selectObstacleIDs argument, then the function marks all instances of that ID after the first as duplicates and ignores them.

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

Objects

dynamicCapsuleList|dynamicCapsuleList3D

Functions

addEgo | addObstacle | checkCollision | egoGeometry | egoPose | obstacleGeometry |
removeEgo | removeObstacle | show | updateEgoGeometry | updateEgoPose |
updateObstacleGeometry | updateObstaclePose

Topics

"Highway Trajectory Planning Using Frenet Reference Path"

removeEgo

Remove ego bodies from capsule list

Syntax

removeEgo(capsuleListObj,egoIDs)
status = removeEgo(capsuleListObj,egoIDs)

Description

removeEgo(capsuleListObj,egoIDs) removes ego bodies with the specified IDs from the dynamic capsule list.

status = removeEgo(capsuleListObj,egoIDs) additionally returns an indicator of whether an
ego body is removed, not found, or a duplicate.

Input Arguments

capsuleListObj — Dynamic capsule list

dynamicCapsuleList object | dynamicCapsuleList3D object

Dynamic capsule list, specified as a dynamicCapsuleList or dynamicCapsuleList3D object.

egoIDs — IDs of ego bodies

vector of positive integers

IDs of ego bodies to remove, specified as a vector of positive integers.

Output Arguments

status — Result of removing ego bodies

N-element column vector

Result of removing ego bodies, specified as N-element column vector of ones, zeros, and negative ones. N is the number of ego bodies specified in the egoIDs argument. Each value indicates whether the body is removed (1), not found (0), or a duplicate (-1). If you specify the same ego ID multiple times in the egoIDs input argument, then all entries besides the last are marked as a duplicate.

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

Objects

dynamicCapsuleList|dynamicCapsuleList3D

Functions

addEgo | addObstacle | checkCollision | egoGeometry | egoPose | obstacleGeometry |
obstaclePose | removeObstacle | show | updateEgoGeometry | updateEgoPose |
updateObstacleGeometry | updateObstaclePose

Topics

"Highway Trajectory Planning Using Frenet Reference Path"

removeObstacle

Remove obstacles from capsule list

Syntax

removeObstacle(capsuleListObj,obstacleIDs)
status = removeObstacle(capsuleListObj,obstacleIDs)

Description

removeObstacle(capsuleListObj,obstacleIDs) removes obstacles with the specified IDs from the dynamic capsule list.

status = removeObstacle(capsuleListObj,obstacleIDs) additionally returns an indicator
of whether an obstacles is removed, not found, or a duplicate.

Input Arguments

capsuleListObj — Dynamic capsule list

dynamicCapsuleList object | dynamicCapsuleList3D object

Dynamic capsule list, specified as a dynamicCapsuleList or dynamicCapsuleList3D object.

obstacleIDs — IDs of obstacles

vector of positive integers

IDs of obstacles to remove, specified as a vector of positive integers.

Output Arguments

status — Result of removing obstacles

N-element column vector

Result of removing obstacles, specified as N-element column vector of ones, zeros, and negative ones. N is the number of obstacles specified in the obstacleIDs argument. Each value indicates whether the obstacle is removed (1), not found (0), or a duplicate (-1). If you specify the same obstacle ID multiple times in the obstacleIDs input argument, then all entries besides the last are marked as a duplicate.

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

Objects

dynamicCapsuleList|dynamicCapsuleList3D

Functions

addEgo | addObstacle | checkCollision | egoGeometry | egoPose | obstacleGeometry |
obstaclePose | removeEgo | show | updateEgoGeometry | updateEgoPose |
updateObstacleGeometry | updateObstaclePose

Topics

"Highway Trajectory Planning Using Frenet Reference Path"

show

Display ego bodies and obstacles in environment

Syntax

```
ax = show(capsuleList0bj)
ax = show(capsuleList0bj, Name, Value)
```

Description

ax = show(capsuleListObj) displays the initial state of all ego bodies and obstacles in the specified capsule list, and returns the axes handle of the plot.

ax = show(capsuleListObj, Name, Value) specifies options using name-value pair arguments on page 2-253. For example, 'FastUpdate', true enables fast updates to an existing plot.

Examples

Build Ego Body Paths and Check for Collisions with Obstacles

Build an ego body path and maintain obstacle states using the dynamicCapsuleList object. Visualize the states of all objects in the environment at different timestamps. Validate the path of the ego body by checking for collisions with obstacles in the environment.

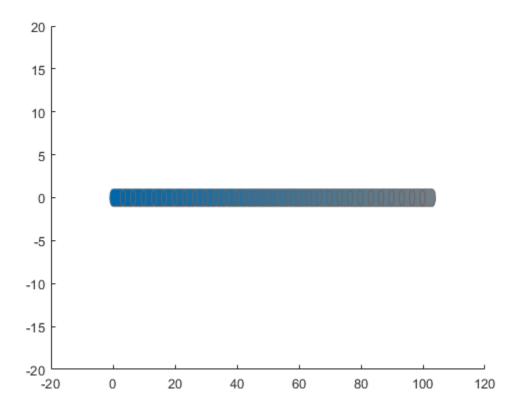
Create the dynamicCapsuleList object. Extract the maximum number of steps to use as the number of time stamps for your object paths.

```
obsList = dynamicCapsuleList;
numSteps = obsList.MaxNumSteps;
```

Add Ego Body

Define an ego body by specifying the ID, geometry, and state together in a structure. The capsule geometry has a length of 3 m and radius of 1 m. Specify the state as a linear path from x = 0m to x = 100m.

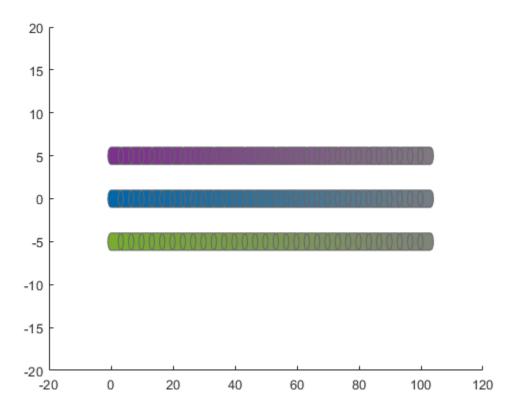
```
egoID1 = 1;
geom = struct("Length",3,"Radius",1,"FixedTransform",eye(3));
states = linspace(0,1,obsList.MaxNumSteps)'.*[100 0 0];
egoCapsule1 = struct('ID',egoID1,'States',states,'Geometry',geom);
addEgo(obsList,egoCapsule1);
show(obsList,"TimeStep",[1:numSteps]);
ylim([-20 20])
```



Add Obstacles

Specify states for two obstacles that are separated from the ego body by 5 m in opposite directions on the *y*-axis.. Assume the obstacles have the same geometry **geom** as the ego body.

```
obsState1 = states + [0 5 0];
obsState2 = states + [0 -5 0];
obsCapsule1 = struct('ID',1,'States',obsState1,'Geometry',geom);
obsCapsule2 = struct('ID',2,'States',obsState2,'Geometry',geom);
addObstacle(obsList,obsCapsule1);
addObstacle(obsList,obsCapsule2);
show(obsList,"TimeStep",[1:numSteps]);
ylim([-20 20])
```



Update Obstacles

Alter your obstacle locations and geometry dimensions over time. Use the previously generated structure, modify the fields, and update the obstacles using the updateObstacleGeometry and updateObstaclePose object functions. Reduces the radius of the first obstacle to 0.5 m, and change the path to move it towards the ego body.

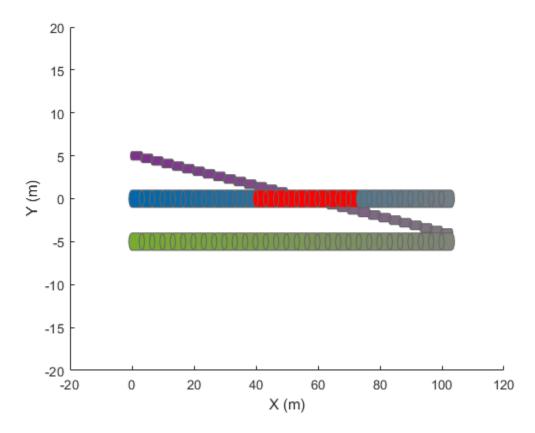
```
obsCapsule1.Geometry.Radius = 0.5;
obsCapsule1.States = ...
   [linspace(0,100,numSteps)' ... % x
        linspace(5,-4,numSteps)' ... % y
        zeros(numSteps,1)]; % theta

updateObstacleGeometry(obsList,1,obsCapsule1);
updateObstaclePose(obsList,1,obsCapsule1);
```

Check for Collisions

Visualize the new paths. Show where collisions between the ego body and an obstacle, which the display highlights in red. Notice that collisions between the obstacles are not checked.

```
show(obsList,"TimeStep",[1:numSteps],"ShowCollisions",1);
ylim([-20 20])
xlabel("X (m)")
ylabel("Y (m)")
```



Programmatically check for collisions by using the checkCollision object function. The function returns a vector of logical values that indicates the status of each time step. The vector is transposed for display purposes.

```
collisions = checkCollision(obsList)'
collisions = 1x31 logical array
   0
       0
           0
                                 0
                        0
                             0
                                     0
                                         0
                                             0
                                                  0
                                                      1
                                                              1
                                                                  1
                                                                       1
                                                                           1
                                                                                1
                                                                                    1
                                                                                        1
                                                                                            1
                                                          1
```

To validate paths with a large number of steps, use the any function on the vector of collision values.

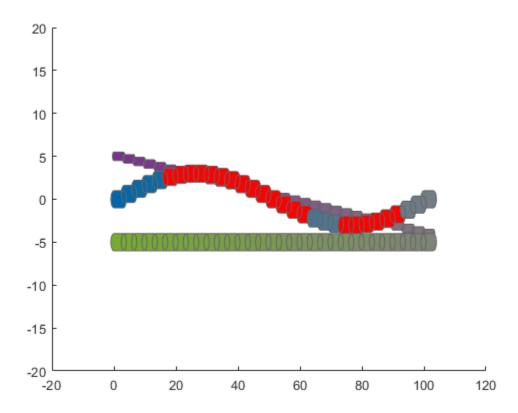
```
if any(collisions)
    disp("Collision detected.")
end
Collision detected.
```

Update Ego Path

Specify a new path for the ego body. Visualize the paths again, displaying collisions.

```
egoCapsule1.States = ...
[linspace(0,100,numSteps)' ... % x
    3*sin(linspace(0,2*pi,numSteps))' ... % y
    zeros(numSteps,1)]; % theta
```

```
updateEgoPose(obsList,1,egoCapsule1);
show(obsList,"TimeStep",[1:numSteps],"ShowCollisions",1);
ylim([-20 20])
```



Input Arguments

capsuleListObj — Dynamic capsule list

dynamicCapsuleList object | dynamicCapsuleList3D object

Dynamic capsule list, specified as a dynamicCapsuleList or dynamicCapsuleList3D object.

Name-Value Pair Arguments

Specify optional comma-separated pairs of Name, Value arguments. Name is the argument name and Value is the corresponding value. Name must appear inside quotes. You can specify several name and value pair arguments in any order as Name1, Value1, . . . , NameN, ValueN.

Example: 'FastUpdate', true enables the option for fast updates in an existing plot.

Parent — Parent axes to plot on

gca (default) | Axes handle

Parent axes to plot on, specified as the comma-separated pair consisting of 'Parent' and an Axes handle.

FastUpdate — Perform fast update to existing plot

false or 0 (default) | true or 1

Perform a fast update to an existing plot, specified as the comma-separated pair consisting of 'FastUpdate' and a logical 0 (false) or 1 (true). You must use the show object function to initially display your capsule list before you can specify it with this argument.

Data Types: logical

TimeStep — Time steps to display

1 (default) | numeric vector

Time steps to display, specified as the comma-separated pair consisting of 'TimeStep' and numeric vector of values in the range [1, N], where N is the value of the MaxNumSteps property of the object specified in the capsuleListObj argument. Each time step corresponds to a row of the state matrix for each ego body and obstacle.

ShowCollisions — Check for and highlight collisions in display

false or 0 (default) | true or 1

Check for and highlight collisions in the display, specified as the comma-separated pair consisting of 'ShowCollisions' and a logical 0 (false) or 1 (true).

Data Types: logical

EgoIDs — Ego IDs to display

vector of positive integers

Ego IDs to display, specified as the comma-separated pair consisting of 'EgoIDs' and a vector of positive integers. By default, the object function displays all ego bodies.

ObstacleIDs — Obstacle IDs to display

vector of positive integers

Obstacle IDs to display, specified as the comma-separated pair consisting of 'ObstacleIDs' and a vector of positive integers. By default, the function displays all obstacles.

Output Arguments

ax — Parent axes of dynamic capsule list plot

Axes handle

Parent axes of the dynamic capsule list plot, returned as anAxes handle.

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

Objects

dynamicCapsuleList|dynamicCapsuleList3D

Functions

addEgo | addObstacle | checkCollision | egoGeometry | egoPose | obstacleGeometry |
obstaclePose | removeEgo | removeObstacle | updateEgoGeometry | updateEgoPose |
updateObstacleGeometry | updateObstaclePose

Topics

"Highway Trajectory Planning Using Frenet Reference Path"

Introduced in R2020b

updateEgoGeometry

Update geometric properties of ego bodies

Syntax

updateEgoGeometry(capsuleListObj,egoIDs,geomStruct)
status = updateEgoGeometry(capsuleListObj,egoIDs,geomStruct)

Description

updateEgoGeometry(capsuleListObj,egoIDs,geomStruct) updates geometry parameters for the specified ego bodies in the capsule list. If a specified ego ID does not already exist, the function adds a new ego body with that ID to the list.

status = updateEgoGeometry(capsuleListObj,egoIDs,geomStruct) additionally returns
an indicator of whether an ego body is added, updated, or a duplicate.

Input Arguments

capsuleListObj — Dynamic capsule list

dynamicCapsuleList object | dynamicCapsuleList3D object

Dynamic capsule list, specified as a dynamicCapsuleList or dynamicCapsuleList3D object.

egoIDs — IDs of ego bodies to update

vector of positive integers

IDs of ego bodies to update, specified as a vector of positive integers.

geomStruct — Geometry parameters for ego bodies

structure | structure array

Geometry parameters for ego bodies, specified as a structure or structure array, where each structure contains the fields of the structure in the Geometry field of the ego body to be updated. The fields of this structure depend on whether you are using a dynamicCapsuleList or dynamicCapsuleList3D object.

Data Types: struct

Output Arguments

status — Result of updating ego bodies

N-element column vector

Result of updating ego bodies, specified as N-element column vector of ones, zeros, and negative ones. N is the number of ego bodies specified in the egoIDs argument. Each value indicates whether the body is removed (1), not found (0), or a duplicate (-1). If you specify the same ego ID multiple times in the egoIDs input argument, then all entries besides the last are marked as a duplicate.

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

Objects

dynamicCapsuleList|dynamicCapsuleList3D

Functions

addEgo | addObstacle | checkCollision | egoGeometry | egoPose | obstacleGeometry |
obstaclePose | removeEgo | removeObstacle | show | updateEgoPose |
updateObstacleGeometry | updateObstaclePose

Topics

"Highway Trajectory Planning Using Frenet Reference Path"

Introduced in R2020b

updateEgoPose

Update states of ego bodies

Syntax

```
updateEgoPose(capsuleListObj,egoIDs,poseStruct)
status = updateEgoPose(capsuleListObj,egoIDs,poseStruct)
```

Description

updateEgoPose(capsuleListObj,egoIDs,poseStruct) updates the states of the specified ego
bodies in the capsule list. If a specified ego ID does not already exist, the function adds a new ego
body with that ID to the list.

status = updateEgoPose(capsuleListObj,egoIDs,poseStruct) returns an indicator of
whether an ego body is added, updated, or a duplicate.

Examples

Build Ego Body Paths and Check for Collisions with Obstacles

Build an ego body path and maintain obstacle states using the dynamicCapsuleList object. Visualize the states of all objects in the environment at different timestamps. Validate the path of the ego body by checking for collisions with obstacles in the environment.

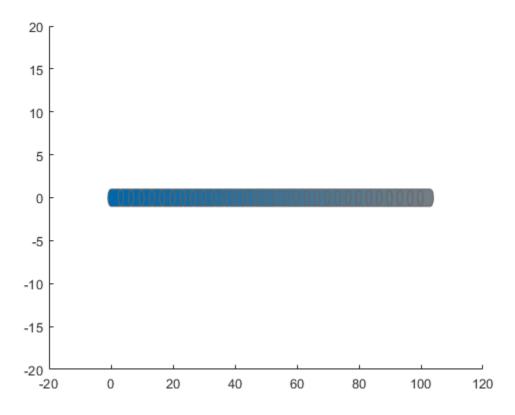
Create the dynamicCapsuleList object. Extract the maximum number of steps to use as the number of time stamps for your object paths.

```
obsList = dynamicCapsuleList;
numSteps = obsList.MaxNumSteps;
```

Add Ego Body

Define an ego body by specifying the ID, geometry, and state together in a structure. The capsule geometry has a length of 3 m and radius of 1 m. Specify the state as a linear path from x = 0m to x = 100m.

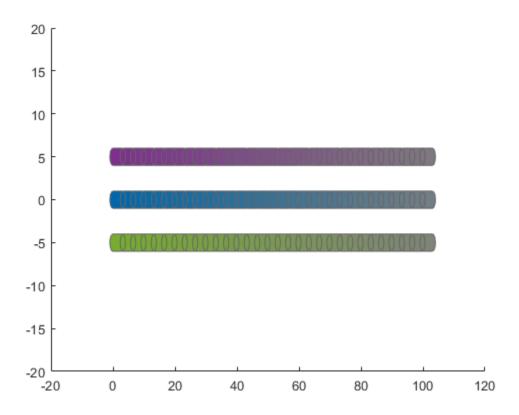
```
egoID1 = 1;
geom = struct("Length",3,"Radius",1,"FixedTransform",eye(3));
states = linspace(0,1,obsList.MaxNumSteps)'.*[100 0 0];
egoCapsule1 = struct('ID',egoID1,'States',states,'Geometry',geom);
addEgo(obsList,egoCapsule1);
show(obsList,"TimeStep",[1:numSteps]);
ylim([-20 20])
```



Add Obstacles

Specify states for two obstacles that are separated from the ego body by 5 m in opposite directions on the y-axis.. Assume the obstacles have the same geometry geom as the ego body.

```
obsState1 = states + [0 5 0];
obsState2 = states + [0 -5 0];
obsCapsule1 = struct('ID',1,'States',obsState1,'Geometry',geom);
obsCapsule2 = struct('ID',2,'States',obsState2,'Geometry',geom);
addObstacle(obsList,obsCapsule1);
addObstacle(obsList,obsCapsule2);
show(obsList,"TimeStep",[1:numSteps]);
ylim([-20 20])
```



Update Obstacles

Alter your obstacle locations and geometry dimensions over time. Use the previously generated structure, modify the fields, and update the obstacles using the updateObstacleGeometry and updateObstaclePose object functions. Reduces the radius of the first obstacle to 0.5 m, and change the path to move it towards the ego body.

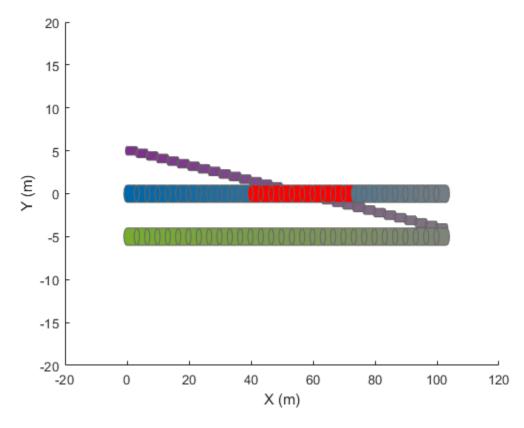
```
obsCapsule1.Geometry.Radius = 0.5;
obsCapsule1.States = ...
   [linspace(0,100,numSteps)' ... % x
        linspace(5,-4,numSteps)' ... % y
        zeros(numSteps,1)]; % theta

updateObstacleGeometry(obsList,1,obsCapsule1);
updateObstaclePose(obsList,1,obsCapsule1);
```

Check for Collisions

Visualize the new paths. Show where collisions between the ego body and an obstacle, which the display highlights in red. Notice that collisions between the obstacles are not checked.

```
show(obsList,"TimeStep",[1:numSteps],"ShowCollisions",1);
ylim([-20 20])
xlabel("X (m)")
ylabel("Y (m)")
```



Programmatically check for collisions by using the checkCollision object function. The function returns a vector of logical values that indicates the status of each time step. The vector is transposed for display purposes.

```
collisions = checkCollision(obsList)'
collisions = 1x31 logical array
   0
       0
           0
                                 0
                        0
                             0
                                     0
                                         0
                                              0
                                                  0
                                                      1
                                                          1
                                                               1
                                                                   1
                                                                       1
                                                                            1
                                                                                    1
                                                                                         1
                                                                                             1
                                                                                1
```

To validate paths with a large number of steps, use the any function on the vector of collision values.

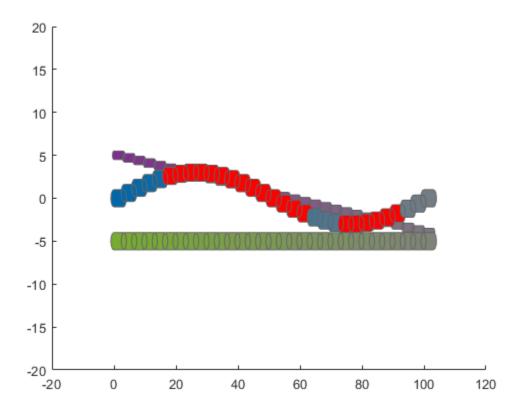
```
if any(collisions)
    disp("Collision detected.")
end
Collision detected.
```

Update Ego Path

Specify a new path for the ego body. Visualize the paths again, displaying collisions.

```
egoCapsule1.States = ...
[linspace(0,100,numSteps)' ... % x
    3*sin(linspace(0,2*pi,numSteps))' ... % y
    zeros(numSteps,1)]; % theta
```

```
updateEgoPose(obsList,1,egoCapsule1);
show(obsList,"TimeStep",[1:numSteps],"ShowCollisions",1);
ylim([-20 20])
```



Input Arguments

capsuleListObj — Dynamic capsule list

dynamicCapsuleList object | dynamicCapsuleList3D object

Dynamic capsule list, specified as a dynamicCapsuleList or dynamicCapsuleList3D object.

egoIDs — IDs of ego bodies to update

vector of positive integers

IDs of ego bodies to update, specified as a vector of positive integers.

poseStruct — States for ego bodies

structure | structure array

States for ego bodies, specified as a structure array or structure array, where each structure contains the fields of the structure in the Geometry field of the ego body to be updated. Each element of the structure array contains a matrix of states for each ego body. The state matrix size depends on whether you are using a dynamicCapsuleList or dynamicCapsuleList3D object.

Data Types: struct

Output Arguments

status — Result of updating ego bodies

N-element column vector

Result of updating ego bodies, specified as N-element column vector of ones, zeros, and negative ones. N is the number of ego bodies specified in the egoIDs argument. Each value indicates whether the body is updated (1), not found (0), or a duplicate (-1). If you specify the same ego ID multiple times in the egoIDs input argument, then all entries besides the last are marked as a duplicate.

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

Objects

dynamicCapsuleList|dynamicCapsuleList3D

Functions

addEgo | addObstacle | checkCollision | egoGeometry | egoPose | obstacleGeometry |
obstaclePose | removeEgo | removeObstacle | show | updateEgoGeometry |
updateObstacleGeometry | updateObstaclePose

Topics

"Highway Trajectory Planning Using Frenet Reference Path"

Introduced in R2020b

updateObstacleGeometry

Update geometric properties of obstacles

Syntax

```
updateObstacleGeometry(capsuleListObj,obstacleIDs,geomStruct)
status = updateObstacleGeometry(capsuleListObj,obstacleIDs,geomStruct)
```

Description

updateObstacleGeometry(capsuleListObj,obstacleIDs,geomStruct) updates geometry parameters for the specified obstacles in the capsule list. If a specified obstacle ID does not already exist, the function adds a new obstacle with that ID to the list.

status = updateObstacleGeometry(capsuleListObj,obstacleIDs,geomStruct) returns
an indicator of whether an obstacle is added, updated, or a duplicate.

Examples

Build Ego Body Paths and Check for Collisions with Obstacles

Build an ego body path and maintain obstacle states using the dynamicCapsuleList object. Visualize the states of all objects in the environment at different timestamps. Validate the path of the ego body by checking for collisions with obstacles in the environment.

Create the dynamicCapsuleList object. Extract the maximum number of steps to use as the number of time stamps for your object paths.

```
obsList = dynamicCapsuleList;
numSteps = obsList.MaxNumSteps;
```

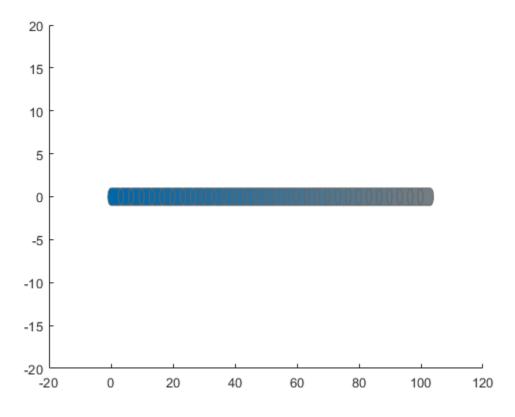
Add Ego Body

Define an ego body by specifying the ID, geometry, and state together in a structure. The capsule geometry has a length of 3 m and radius of 1 m. Specify the state as a linear path from x = 0m to x = 100m.

```
egoID1 = 1;
geom = struct("Length",3,"Radius",1,"FixedTransform",eye(3));
states = linspace(0,1,obsList.MaxNumSteps)'.*[100 0 0];

egoCapsule1 = struct('ID',egoID1,'States',states,'Geometry',geom);
addEgo(obsList,egoCapsule1);

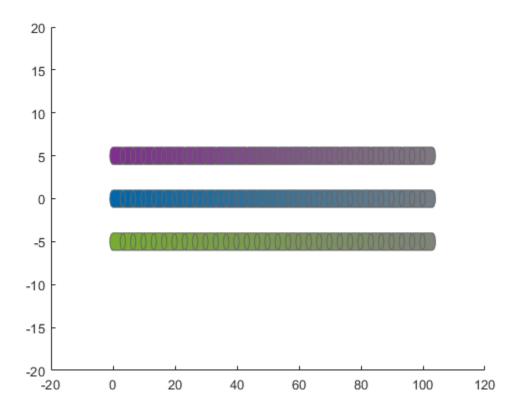
show(obsList,"TimeStep",[1:numSteps]);
ylim([-20 20])
```



Add Obstacles

Specify states for two obstacles that are separated from the ego body by 5 m in opposite directions on the y-axis.. Assume the obstacles have the same geometry geom as the ego body.

```
obsState1 = states + [0 5 0];
obsState2 = states + [0 -5 0];
obsCapsule1 = struct('ID',1,'States',obsState1,'Geometry',geom);
obsCapsule2 = struct('ID',2,'States',obsState2,'Geometry',geom);
addObstacle(obsList,obsCapsule1);
addObstacle(obsList,obsCapsule2);
show(obsList,"TimeStep",[1:numSteps]);
ylim([-20 20])
```



Update Obstacles

Alter your obstacle locations and geometry dimensions over time. Use the previously generated structure, modify the fields, and update the obstacles using the updateObstacleGeometry and updateObstaclePose object functions. Reduces the radius of the first obstacle to 0.5 m, and change the path to move it towards the ego body.

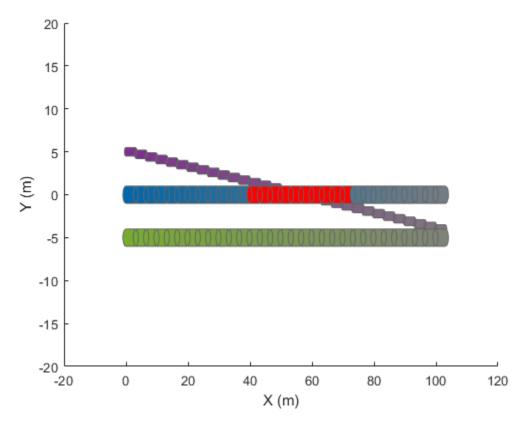
```
obsCapsule1.Geometry.Radius = 0.5;
obsCapsule1.States = ...
   [linspace(0,100,numSteps)' ... % x
        linspace(5,-4,numSteps)' ... % y
        zeros(numSteps,1)]; % theta

updateObstacleGeometry(obsList,1,obsCapsule1);
updateObstaclePose(obsList,1,obsCapsule1);
```

Check for Collisions

Visualize the new paths. Show where collisions between the ego body and an obstacle, which the display highlights in red. Notice that collisions between the obstacles are not checked.

```
show(obsList,"TimeStep",[1:numSteps],"ShowCollisions",1);
ylim([-20 20])
xlabel("X (m)")
ylabel("Y (m)")
```



Programmatically check for collisions by using the checkCollision object function. The function returns a vector of logical values that indicates the status of each time step. The vector is transposed for display purposes.

```
collisions = checkCollision(obsList)'
collisions = 1x31 logical array
   0
       0
           0
                                 0
                        0
                             0
                                     0
                                         0
                                              0
                                                  0
                                                      1
                                                           1
                                                               1
                                                                   1
                                                                       1
                                                                            1
                                                                                    1
                                                                                         1
                                                                                             1
                                                                                1
```

To validate paths with a large number of steps, use the any function on the vector of collision values.

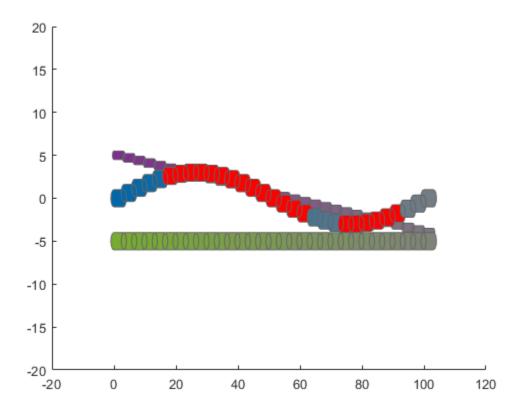
```
if any(collisions)
    disp("Collision detected.")
end
Collision detected.
```

Update Ego Path

Specify a new path for the ego body. Visualize the paths again, displaying collisions.

```
egoCapsule1.States = ...
[linspace(0,100,numSteps)' ... % x
    3*sin(linspace(0,2*pi,numSteps))' ... % y
    zeros(numSteps,1)]; % theta
```

```
updateEgoPose(obsList,1,egoCapsule1);
show(obsList,"TimeStep",[1:numSteps],"ShowCollisions",1);
ylim([-20 20])
```



Input Arguments

capsuleListObj — Dynamic capsule list

dynamicCapsuleList object | dynamicCapsuleList3D object

Dynamic capsule list, specified as a dynamicCapsuleList or dynamicCapsuleList3D object.

obstacleIDs — IDs of obstacles to update

vector of positive integers

IDs of obstacles to update, specified as a vector of positive integers.

geomStruct — Geometry parameters for ego bodies

structure | structure array

Geometry parameters for ego bodies, specified as a structure or structure array, where each structure contains the fields of the structure in the Geometry field of the obstacle to be updated.. The fields of this structure depend on whether you are using a dynamicCapsuleList or dynamicCapsuleList3D object.

Data Types: struct

Output Arguments

status — Result of updating obstacles

N-element column vector

Result of updating obstacles, specified as N-element column vector of ones, zeros, and negative ones. N is the number of obstacles specified in the obstacleIDs argument. Each value indicates whether the obstacle is removed (1), not found (0), or a duplicate (-1). If you specify the same obstacle ID multiple times in the obstacleIDs input argument, then all entries besides the last are marked as a duplicate.

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

Objects

dynamicCapsuleList|dynamicCapsuleList3D

Functions

addEgo | addObstacle | checkCollision | egoGeometry | egoPose | obstacleGeometry |
obstaclePose | removeEgo | removeObstacle | show | updateEgoGeometry | updateEgoPose |
updateObstaclePose

Topics

"Highway Trajectory Planning Using Frenet Reference Path"

Introduced in R2020b

updateObstaclePose

Update states of obstacles

Syntax

```
updateObstaclePose(capsuleListObj,obstacleIDs,poseStruct)
status = updateObstaclePose(capsuleListObj,obstacleIDs,poseStruct)
```

Description

updateObstaclePose(capsuleListObj,obstacleIDs,poseStruct) updates the states of the specified obstacles in the capsule list. If a specified obstacle ID does not already exist, the function adds a new ego body with that ID to the list.

status = updateObstaclePose(capsuleListObj,obstacleIDs,poseStruct) returns an indicator of whether an obstacle is added, updated, or a duplicate.

Examples

Build Ego Body Paths and Check for Collisions with Obstacles

Build an ego body path and maintain obstacle states using the dynamicCapsuleList object. Visualize the states of all objects in the environment at different timestamps. Validate the path of the ego body by checking for collisions with obstacles in the environment.

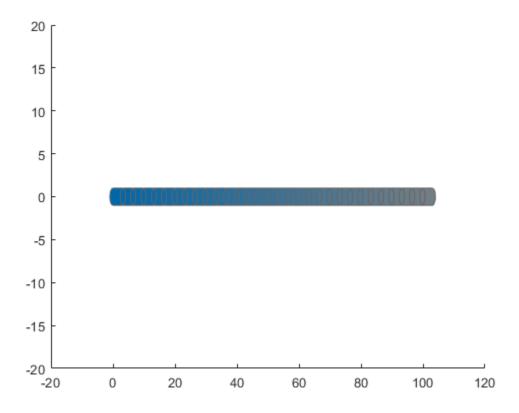
Create the dynamicCapsuleList object. Extract the maximum number of steps to use as the number of time stamps for your object paths.

```
obsList = dynamicCapsuleList;
numSteps = obsList.MaxNumSteps;
```

Add Ego Body

Define an ego body by specifying the ID, geometry, and state together in a structure. The capsule geometry has a length of 3 m and radius of 1 m. Specify the state as a linear path from x = 0m to x = 100m.

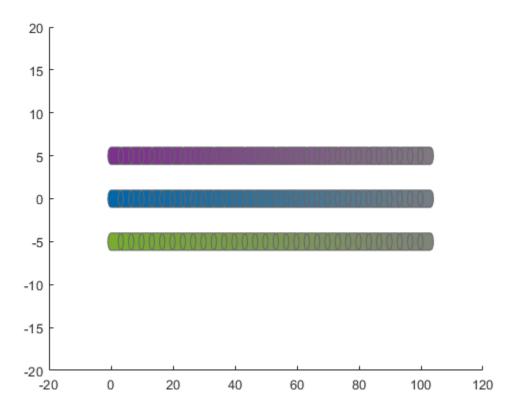
```
egoID1 = 1;
geom = struct("Length",3,"Radius",1,"FixedTransform",eye(3));
states = linspace(0,1,obsList.MaxNumSteps)'.*[100 0 0];
egoCapsule1 = struct('ID',egoID1,'States',states,'Geometry',geom);
addEgo(obsList,egoCapsule1);
show(obsList,"TimeStep",[1:numSteps]);
ylim([-20 20])
```



Add Obstacles

Specify states for two obstacles that are separated from the ego body by 5 m in opposite directions on the y-axis.. Assume the obstacles have the same geometry geom as the ego body.

```
obsState1 = states + [0 5 0];
obsState2 = states + [0 -5 0];
obsCapsule1 = struct('ID',1,'States',obsState1,'Geometry',geom);
obsCapsule2 = struct('ID',2,'States',obsState2,'Geometry',geom);
addObstacle(obsList,obsCapsule1);
addObstacle(obsList,obsCapsule2);
show(obsList,"TimeStep",[1:numSteps]);
ylim([-20 20])
```



Update Obstacles

Alter your obstacle locations and geometry dimensions over time. Use the previously generated structure, modify the fields, and update the obstacles using the updateObstacleGeometry and updateObstaclePose object functions. Reduces the radius of the first obstacle to 0.5 m, and change the path to move it towards the ego body.

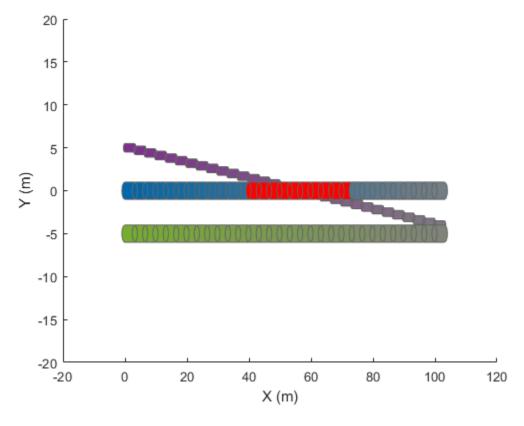
```
obsCapsule1.Geometry.Radius = 0.5;
obsCapsule1.States = ...
   [linspace(0,100,numSteps)' ... % x
        linspace(5,-4,numSteps)' ... % y
        zeros(numSteps,1)]; % theta

updateObstacleGeometry(obsList,1,obsCapsule1);
updateObstaclePose(obsList,1,obsCapsule1);
```

Check for Collisions

Visualize the new paths. Show where collisions between the ego body and an obstacle, which the display highlights in red. Notice that collisions between the obstacles are not checked.

```
show(obsList,"TimeStep",[1:numSteps],"ShowCollisions",1);
ylim([-20 20])
xlabel("X (m)")
ylabel("Y (m)")
```



Programmatically check for collisions by using the checkCollision object function. The function returns a vector of logical values that indicates the status of each time step. The vector is transposed for display purposes.

```
collisions = checkCollision(obsList)'
collisions = 1x31 logical array
   0
       0
           0
                                 0
                        0
                             0
                                     0
                                         0
                                              0
                                                  0
                                                      1
                                                           1
                                                               1
                                                                   1
                                                                        1
                                                                            1
                                                                                1
                                                                                     1
                                                                                         1
                                                                                             1
```

To validate paths with a large number of steps, use the any function on the vector of collision values.

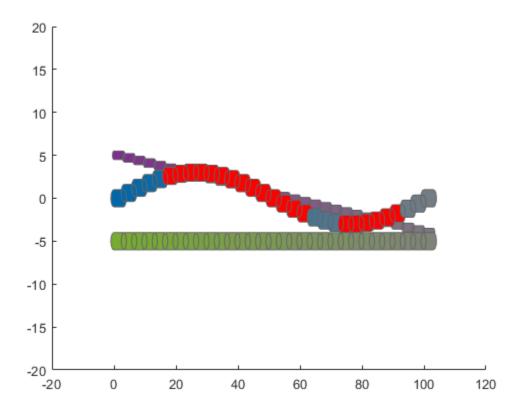
```
if any(collisions)
    disp("Collision detected.")
end
Collision detected.
```

Update Ego Path

Specify a new path for the ego body. Visualize the paths again, displaying collisions.

```
egoCapsule1.States = ...
[linspace(0,100,numSteps)' ... % x
    3*sin(linspace(0,2*pi,numSteps))' ... % y
    zeros(numSteps,1)]; % theta
```

```
updateEgoPose(obsList,1,egoCapsule1);
show(obsList,"TimeStep",[1:numSteps],"ShowCollisions",1);
ylim([-20 20])
```



Input Arguments

capsuleListObj — Dynamic capsule list

dynamicCapsuleList object | dynamicCapsuleList3D object

Dynamic capsule list, specified as a dynamicCapsuleList or dynamicCapsuleList3D object.

obstacleIDs — IDs of obstacles to update

vector of positive integers

IDs of obstacles to update, specified as a vector of positive integers.

poseStruct — States for obstacles

structure | structure array

States for ego bodies, specified as a structure or structure array, where each structure contains the fields of the structure in the Geometry field of the obstacle to be updated. Each element of the structure array contains a matrix of states for each ego body. The state matrix size depends on whether you are using a dynamicCapsuleList or dynamicCapsuleList3D object.

Data Types: struct

Output Arguments

status — Result of updating obstacles

N-element column vector

Result of updating obstacles, specified as N-element column vector of ones, zeros, and negative ones. N is the number of obstacles specified in the obstacleIDs argument. Each value indicates whether the obstacle is removed (1), not found (0), or a duplicate (-1). If you specify the same obstacle ID multiple times in the obstacleIDs input argument, then all entries besides the last are marked as a duplicate.

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

Objects

dynamicCapsuleList|dynamicCapsuleList3D

Functions

addEgo | addObstacle | checkCollision | egoGeometry | egoPose | obstacleGeometry |
obstaclePose | removeEgo | removeObstacle | show | updateEgoGeometry | updateEgoPose |
updateObstacleGeometry

Topics

"Highway Trajectory Planning Using Frenet Reference Path"

Introduced in R2020b

dynamicCapsuleList3D

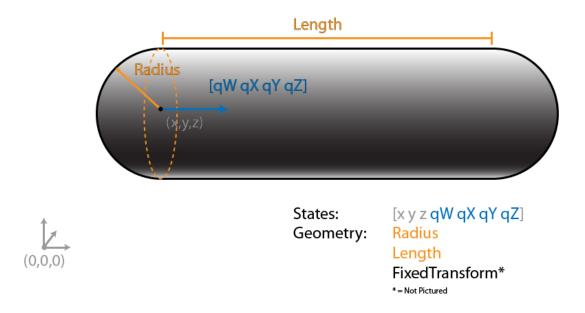
Dynamic capsule-based obstacle list

Description

The dynamicCapsuleList3D object manages two lists of capsule-based collision objects in 3-D space. Collision objects are separated into two lists, ego bodies and obstacles. For ego bodies and obstacles in 2-D, see the dynamicCapsuleList object.

Each collision object in the two lists has three key elements:

- **ID** Integer that identifies each object, stored in the **EgoIDs** property for ego bodies and the **ObstacleIDs** property for obstacles.
- **States** Location and orientation of the object as an *M*-by-6 matrix, where each row is of form [x y z qW qX qY qZ], and *M* is the number of states along the path of the object in the world frame. The list of states assumes each state is separated by a fixed time interval. *xyz*-positions are in meters, and the orientation is a four-element quaternion vector. The default local origin is located at the center of the left hemisphere of the capsule.
- **Geometry** Size of the capsule-based object based on the specified length and radius. The radius applies to the spherical ends, and the length applies to the cylinder length. TTo shift the capsule geometry and local origin relative to the default origin point, specify a 4-by-4 transform relative to the local frame of the capsule. To keep the default transform, specify eye(4).



Use the object functions to dynamically add, remove, and update the geometries and states of the various objects in your environment. To add an ego body, see the addEgo object function. To add an obstacle, see the addObstacle object function.

After specifying all the object paths, validate the ego-body paths and check for collisions with obstacles at every step using the checkCollision object function. The function only checks if an ego body collides with an obstacle, ignoring collisions between only obstacles or only ego bodies.

Creation

Syntax

obstacleList = dynamicCapsuleList3D

Description

obstacleList = dynamicCapsuleList3D creates a dynamic capsule-based obstacle list with no
ego bodies or obstacles. To begin building an obstacle list, use the addEgo or addObstacle object
functions.

Properties

MaxNumSteps — Maximum number of time steps in obstacle list

31 (default) | positive integer

Maximum number of time steps in the obstacle list, specified as a positive integer. The number of steps determines to the maximum length of the States field for a specific ego body or obstacle.

Data Types: double

EgoIDs — List of IDs for ego bodies

vector of positive integers

This property is read-only.

List of identifiers for ego bodies, returned as a vector of positive integers.

Data Types: double

ObstacleIDs — **IDs** for obstacles

vector of positive integers

This property is read-only.

List of identifiers for obstacles, returned as a vector of positive integers.

Data Types: double

NumObstacles — Number of obstacles in list

integer

This property is read-only.

Number of obstacles in list, returned as an integer.

Data Types: double

NumEgos — Number of ego bodies in list

integer

This property is read-only.

Number of ego bodies in list, returned as an integer.

Data Types: double

Object Functions

addEgo Add ego bodies to 3D capsule list addObstacle Add obstacles to 3-D capsule list

checkCollision Check for collisions between ego bodies and obstacles

egoGeometry Geometric properties of ego bodies

egoPose Poses of ego bodies

obstacleGeometry Geometric properties of obstacles

obstaclePose Poses of obstacles

removeEgo Remove ego bodies from capsule list removeObstacle Remove obstacles from capsule list

show Display ego bodies and obstacles in environment updateEgoGeometry Update geometric properties of ego bodies

updateEgoPose Update states of ego bodies

updateObstacleGeometry Update geometric properties of obstacles

updateObstaclePose Update states of obstacles

Examples

Build 3-D Ego Body Paths and Check for Collisions with 3-D Obstacles

Build an ego body path and maintain obstacle states using the dynamicCapsuleList3D object. Visualize the states of all objects in the environment at different timestamps. Validate the path of the ego body by checking for collisions with obstacles in the environment.

Create the dynamicCapsuleList3D object. Extract the maximum number of steps to use as the number of time stamps for your object paths.

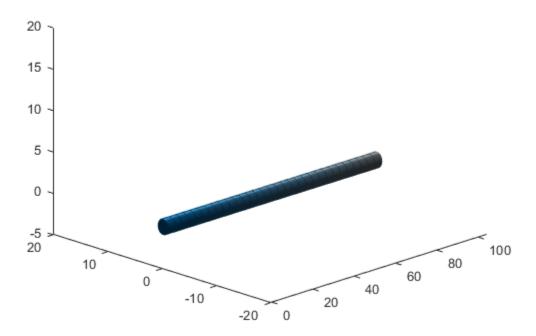
```
obsList = dynamicCapsuleList3D;
numSteps = obsList.MaxNumSteps;
```

Add Ego Body

Define an ego body by specifying the ID, geometry, and state together in a structure. The capsule geometry has a length of 3 m and radius of 1 m. Specify the state as a linear path from x = 0 m to x = 100 m.

```
egoID1 = 1;
geom = struct("Length",3,"Radius",1,"FixedTransform",eye(4));
states = linspace(0,1,obsList.MaxNumSteps)'.*[100 0 0];
states = [states ones(numSteps,2) zeros(numSteps,2)];
egoCapsule1 = struct('ID',egoID1,'States',states,'Geometry',geom);
addEgo(obsList,egoCapsule1);
show(obsList,"TimeStep",1:numSteps);
ylim([-20 20])
zlim([-5 20])
```

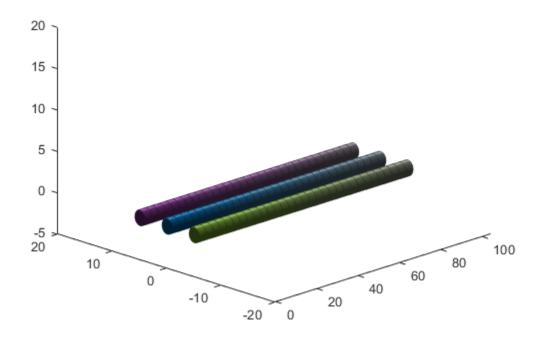
view(-45,25)
hold on



Add Obstacles

Specify states for two obstacles that are separated from the ego body by 5 m in opposite directions on the y-axis. Assume the obstacles have the same geometry geom as the ego body.

```
obsState1 = states + [0 5 0 0 0 0 0];
obsState2 = states + [0 -5 0 0 0 0 0];
obsCapsule1 = struct('ID',1,'States',obsState1,'Geometry',geom);
obsCapsule2 = struct('ID',2,'States',obsState2,'Geometry',geom);
addObstacle(obsList,obsCapsule1);
addObstacle(obsList,obsCapsule2);
cla
show(obsList,"TimeStep",1:numSteps);
```



Update Obstacles

Alter your obstacle locations and geometry dimensions over time. Use the previously generated structure, modify the fields, and update the obstacles using the updateObstacleGeometry and updateObstaclePose object functions. Reduce the radius of the first obstacle to 0.5 m, and change the path to move it towards the ego body.

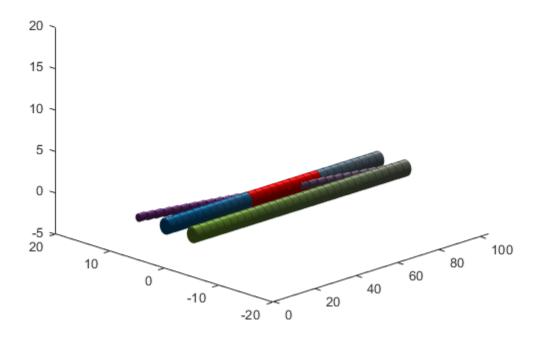
% quaternio

```
obsCapsule1.Geometry.Radius = 0.5;
obsCapsule1.States = ...
   [linspace(0,100,numSteps)' ... % x
    linspace(5,-4,numSteps)' ... % y
    zeros(numSteps,1) ... % z
    ones(numSteps,2) zeros(numSteps,2)]; % quaternion
updateObstacleGeometry(obsList,1,obsCapsule1);
updateObstaclePose(obsList,1,obsCapsule1);
```

Check for Collisions

Visualize the new paths. Show where collisions between the ego body and an obstacle occur, which the display highlights in red. Notice that collisions between the obstacles are not checked.

```
cla
show(obsList, "TimeStep", 1:numSteps, "ShowCollisions", 1);
```



Programmatically check for collisions bu using the checkCollision object function. The function returns a vector of logical values that indicates the collision status at each time step. The vector is transposed for display purposes.

```
collisions = checkCollision(obsList)'
collisions = 1x31 logical array
      0
          0
                       0
                           0
                               0
                                   0
                                       0
                                           0
                                               0
                                                   1
                                                           1
                                                              1
                                                                  1
                                                                       1
                                                                           1
                                                                               1
                                                                                   1
                                                                                       1
                                                       1
```

To validate paths with a large number of steps, use the any function on the vector of collision values.

```
if any(collisions)
    disp("Collision detected.")
end
Collision detected.
```

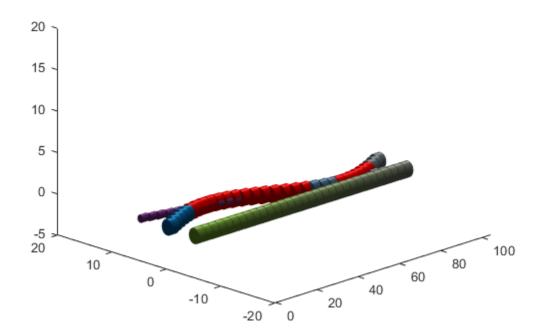
Update Ego Path

Specify a new path for the ego body. Visualize the paths again, displaying collisions.

```
egoCapsule1.States = ...
  [linspace(0,100,numSteps)' ... % x
  3*sin(linspace(0,2*pi,numSteps))' ... % y
  zeros(numSteps,1)... % z
  ones(numSteps,2) zeros(numSteps,2)]; %quaternion
```

% quaterni

```
updateEgoPose(obsList,1,egoCapsule1);
cla
show(obsList,"TimeStep",1:numSteps,"ShowCollisions",1);
```



Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder $^{\text{\tiny TM}}$.

See Also

Objects

dynamicCapsuleList

Functions

addEgo | addObstacle | checkCollision | egoGeometry | egoPose | obstacleGeometry |
obstaclePose | removeEgo | removeObstacle | show | updateEgoGeometry | updateEgoPose |
updateObstacleGeometry | updateObstaclePose

Topics

"Highway Trajectory Planning Using Frenet Reference Path"

Introduced in R2020b

addEgo

Add ego bodies to 3D capsule list

Syntax

```
addEgo(capsuleListObj,egoStruct)
status = addEgo(capsuleListObj,egoStruct)
```

Description

addEgo(capsuleListObj,egoStruct) adds one or more ego bodies to the 3-D dynamic capsule list with the specified ID, state, and geometry values given in egoStruct.

status = addEgo(capsuleListObj,egoStruct) additionally returns an indicator of whether
each specified ego body was added, updated, or a duplicate.

Examples

Build 3-D Ego Body Paths and Check for Collisions with 3-D Obstacles

Build an ego body path and maintain obstacle states using the dynamicCapsuleList3D object. Visualize the states of all objects in the environment at different timestamps. Validate the path of the ego body by checking for collisions with obstacles in the environment.

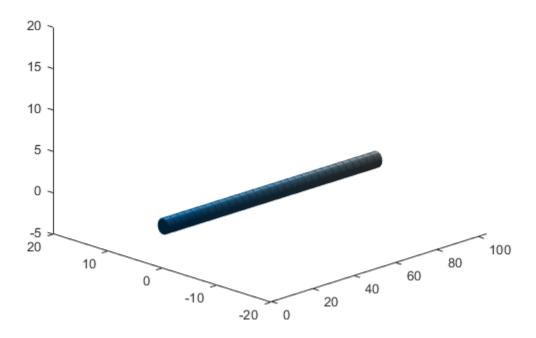
Create the dynamicCapsuleList3D object. Extract the maximum number of steps to use as the number of time stamps for your object paths.

```
obsList = dynamicCapsuleList3D;
numSteps = obsList.MaxNumSteps;
```

Add Ego Body

Define an ego body by specifying the ID, geometry, and state together in a structure. The capsule geometry has a length of 3 m and radius of 1 m. Specify the state as a linear path from x = 0 m to x = 100 m.

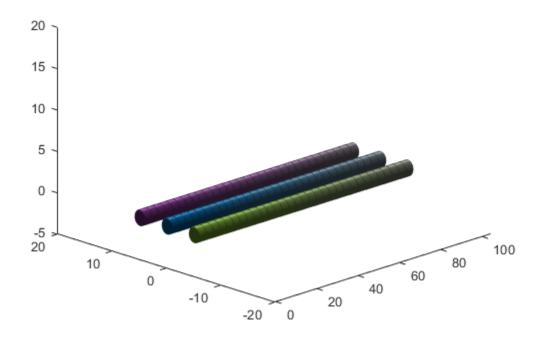
```
egoID1 = 1;
geom = struct("Length",3,"Radius",1,"FixedTransform",eye(4));
states = linspace(0,1,obsList.MaxNumSteps)'.*[100 0 0];
states = [states ones(numSteps,2) zeros(numSteps,2)];
egoCapsule1 = struct('ID',egoID1,'States',states,'Geometry',geom);
addEgo(obsList,egoCapsule1);
show(obsList,"TimeStep",1:numSteps);
ylim([-20 20])
zlim([-5 20])
view(-45,25)
hold on
```



Add Obstacles

Specify states for two obstacles that are separated from the ego body by 5 m in opposite directions on the y-axis. Assume the obstacles have the same geometry geom as the ego body.

```
obsState1 = states + [0 5 0 0 0 0 0];
obsState2 = states + [0 -5 0 0 0 0 0];
obsCapsule1 = struct('ID',1,'States',obsState1,'Geometry',geom);
obsCapsule2 = struct('ID',2,'States',obsState2,'Geometry',geom);
addObstacle(obsList,obsCapsule1);
addObstacle(obsList,obsCapsule2);
cla
show(obsList,"TimeStep",1:numSteps);
```



Update Obstacles

Alter your obstacle locations and geometry dimensions over time. Use the previously generated structure, modify the fields, and update the obstacles using the updateObstacleGeometry and updateObstaclePose object functions. Reduce the radius of the first obstacle to 0.5 m, and change the path to move it towards the ego body.

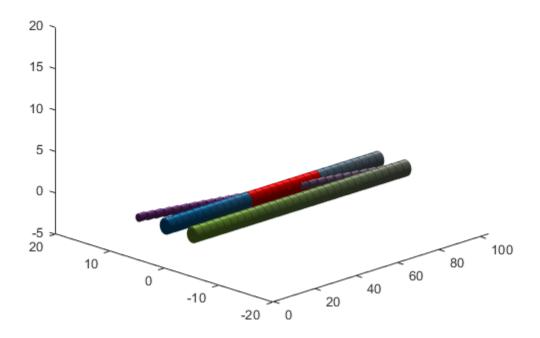
% quaternio

```
obsCapsule1.Geometry.Radius = 0.5;
obsCapsule1.States = ...
   [linspace(0,100,numSteps)' ... % x
    linspace(5,-4,numSteps)' ... % y
    zeros(numSteps,1) ... % z
    ones(numSteps,2) zeros(numSteps,2)]; % quaternion
updateObstacleGeometry(obsList,1,obsCapsule1);
updateObstaclePose(obsList,1,obsCapsule1);
```

Check for Collisions

Visualize the new paths. Show where collisions between the ego body and an obstacle occur, which the display highlights in red. Notice that collisions between the obstacles are not checked.

```
cla
show(obsList,"TimeStep",1:numSteps,"ShowCollisions",1);
```



Programmatically check for collisions bu using the checkCollision object function. The function returns a vector of logical values that indicates the collision status at each time step. The vector is transposed for display purposes.

```
collisions = checkCollision(obsList)'
collisions = 1x31 logical array
       0
           0
                       0
                           0
                               0
                                    0
                                        0
                                            0
                                                0
                                                    1
                                                            1
                                                                1
                                                                    1
                                                                         1
                                                                            1
                                                                                 1
                                                                                     1
                                                                                         1
                                                        1
```

To validate paths with a large number of steps, use the any function on the vector of collision values.

```
if any(collisions)
    disp("Collision detected.")
end
Collision detected.
```

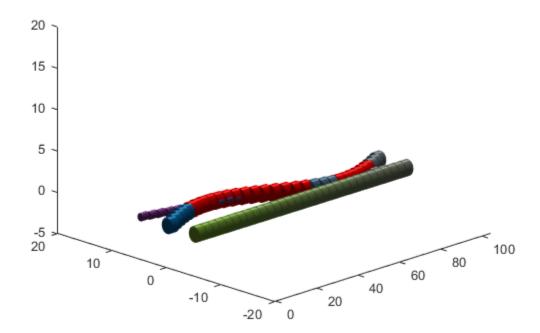
Update Ego Path

Specify a new path for the ego body. Visualize the paths again, displaying collisions.

```
egoCapsule1.States = ...
  [linspace(0,100,numSteps)' ... % x
  3*sin(linspace(0,2*pi,numSteps))' ... % y
  zeros(numSteps,1)... % z
  ones(numSteps,2) zeros(numSteps,2)]; %quaternion
```

% quaterni

```
updateEgoPose(obsList,1,egoCapsule1);
cla
show(obsList,"TimeStep",1:numSteps,"ShowCollisions",1);
```



Input Arguments

capsuleList0bj — Dynamic capsule list

dvnamicCapsuleList3D object

Dynamic capsule list, specified as a dynamicCapsuleList3D object.

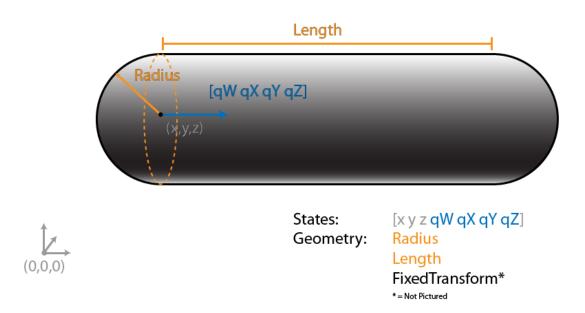
egoStruct — Ego body parameters

structure | structure array

Ego body parameters, specified as an N-element structure or a structure array, where N is the number of added ego bodies. The fields of each structure define the ID, geometry, and states of an ego body:

- ID -- Integer that identifies each object. Stored in the EgoIDs property of the dynamicCapsuleList3D object specified by the capsuleList0bj argument.
- States -- Location and orientation of the object as an M-by-6 matrix, where each row is of form [x y z qW qX qY qZ], and M is the number of states along the path of the object in the world frame. The list of states assumes each state is separated by a fixed time interval. xyz-positions are

- in meters, and the orientation is a four-element quaternion vector. The default local origin is located at the center of the left hemisphere of the capsule.
- Geometry Structure with fields Length, Radius, and FixedTransform. These fields define the size of the capsule-based object using the specified length for the cylinder and hemisphere radius for the end caps. To shift the capsule geometry from the default origin, specify the FixedTransform field as a fixed transform relative to the local frame of the capsule. To keep the default capsule origin, specify the transform as eye(4).



Output Arguments

status — Result of adding ego bodies

N-element column vector

Result of adding ego bodies, returned as a N-element column vector of ones, zeros, and negative ones. N is the number of ego bodies specified in the egoStruct argument. Each value indicates whether the associated body is added (1), updated (0), or a duplicate (-1). While adding ego bodies, if multiple structures with the same body ID are found in the structure array egoStruct, then the function marks the previous entry as duplicate and ignores it.

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

Objects

dynamicCapsuleList|dynamicCapsuleList3D

Functions

addObstacle | checkCollision | egoGeometry | egoPose | obstacleGeometry |
obstaclePose | removeEgo | removeObstacle | show | updateEgoGeometry | updateEgoPose |
updateObstacleGeometry | updateObstaclePose

Topics

"Highway Trajectory Planning Using Frenet Reference Path"

Introduced in R2020b

addObstacle

Add obstacles to 3-D capsule list

Syntax

```
addObstacle(capsuleListObj,obstacleStruct)
status = addObstacle(capsuleListObj,obstacleStruct)
```

Description

addObstacle(capsuleListObj,obstacleStruct) adds one or more obstacles to the 3-D dynamic capsule list with the specified ID, state, and geometry values given in obstacleStruct.

status = addObstacle(capsuleListObj,obstacleStruct) additionally returns an indicator
of whether each specified obstacle was added, updated, or a duplicate.

Examples

Build 3-D Ego Body Paths and Check for Collisions with 3-D Obstacles

Build an ego body path and maintain obstacle states using the dynamicCapsuleList3D object. Visualize the states of all objects in the environment at different timestamps. Validate the path of the ego body by checking for collisions with obstacles in the environment.

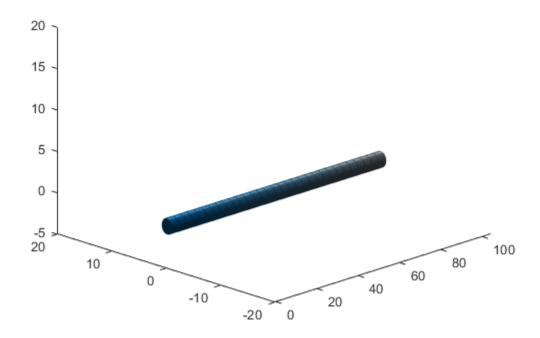
Create the dynamicCapsuleList3D object. Extract the maximum number of steps to use as the number of time stamps for your object paths.

```
obsList = dynamicCapsuleList3D;
numSteps = obsList.MaxNumSteps;
```

Add Ego Body

Define an ego body by specifying the ID, geometry, and state together in a structure. The capsule geometry has a length of 3 m and radius of 1 m. Specify the state as a linear path from x = 0 m to x = 100 m.

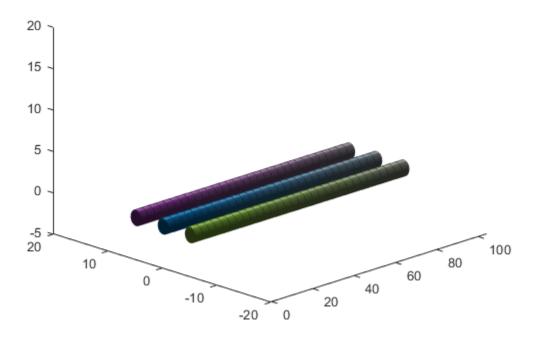
```
egoID1 = 1;
geom = struct("Length",3,"Radius",1,"FixedTransform",eye(4));
states = linspace(0,1,obsList.MaxNumSteps)'.*[100 0 0];
states = [states ones(numSteps,2) zeros(numSteps,2)];
egoCapsule1 = struct('ID',egoID1,'States',states,'Geometry',geom);
addEgo(obsList,egoCapsule1);
show(obsList,"TimeStep",1:numSteps);
ylim([-20 20])
zlim([-5 20])
view(-45,25)
hold on
```



Add Obstacles

Specify states for two obstacles that are separated from the ego body by 5 m in opposite directions on the y-axis. Assume the obstacles have the same geometry geom as the ego body.

```
obsState1 = states + [0 5 0 0 0 0 0];
obsState2 = states + [0 -5 0 0 0 0 0];
obsCapsule1 = struct('ID',1,'States',obsState1,'Geometry',geom);
obsCapsule2 = struct('ID',2,'States',obsState2,'Geometry',geom);
addObstacle(obsList,obsCapsule1);
addObstacle(obsList,obsCapsule2);
cla
show(obsList,"TimeStep",1:numSteps);
```



Update Obstacles

Alter your obstacle locations and geometry dimensions over time. Use the previously generated structure, modify the fields, and update the obstacles using the updateObstacleGeometry and updateObstaclePose object functions. Reduce the radius of the first obstacle to 0.5 m, and change the path to move it towards the ego body.

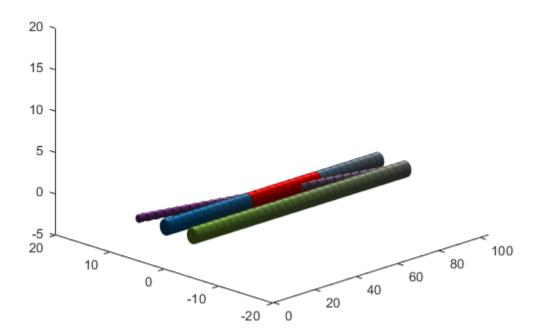
```
obsCapsule1.Geometry.Radius = 0.5;
obsCapsule1.States = ...
   [linspace(0,100,numSteps)' ... % x
    linspace(5,-4,numSteps)' ... % y
   zeros(numSteps,1) ... % z
   ones(numSteps,2) zeros(numSteps,2)]; % quaternion
updateObstacleGeometry(obsList,1,obsCapsule1);
updateObstaclePose(obsList,1,obsCapsule1);
```

Check for Collisions

Visualize the new paths. Show where collisions between the ego body and an obstacle occur, which the display highlights in red. Notice that collisions between the obstacles are not checked.

```
cla
show(obsList,"TimeStep",1:numSteps,"ShowCollisions",1);
```

% quaternio



Programmatically check for collisions bu using the checkCollision object function. The function returns a vector of logical values that indicates the collision status at each time step. The vector is transposed for display purposes.

```
collisions = checkCollision(obsList)'
collisions = 1x31 logical array
   0
      0
           0
                                0
                                                                                      1
                       0
                           0
                                    0
                                        0
                                            0
                                                0
                                                    1
                                                        1
                                                            1
                                                                1
                                                                     1
                                                                         1
                                                                             1
                                                                                 1
                                                                                         1
```

To validate paths with a large number of steps, use the any function on the vector of collision values.

```
if any(collisions)
    disp("Collision detected.")
end
Collision detected.
```

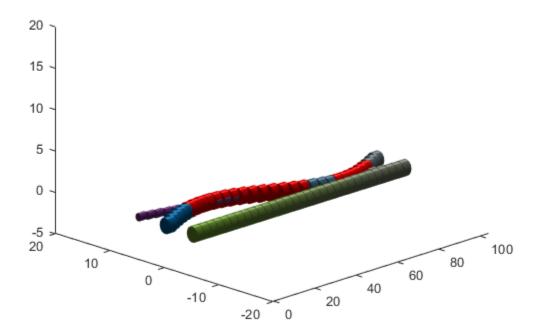
Update Ego Path

Specify a new path for the ego body. Visualize the paths again, displaying collisions.

```
egoCapsule1.States = ...
  [linspace(0,100,numSteps)' ... % x
  3*sin(linspace(0,2*pi,numSteps))' ... % y
  zeros(numSteps,1)... % z
  ones(numSteps,2) zeros(numSteps,2)]; %quaternion
```

% quaterni

```
updateEgoPose(obsList,1,egoCapsule1);
cla
show(obsList,"TimeStep",1:numSteps,"ShowCollisions",1);
```



Input Arguments

capsuleListObj — Dynamic capsule-list

dynamicCapsuleList3D object

Dynamic capsule-list, specified as a dynamicCapsuleList3D object.

Output Arguments

obstacleStruct — Obstacle parameters

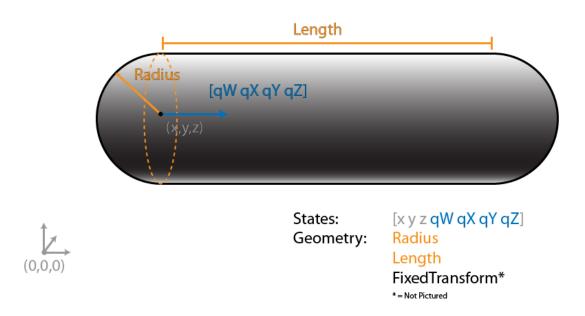
structure | structure array

Obstacle parameters, specified as an N-element structure or a structure array, where N is the number of added ego bodies. The fields of each structure define the ID, geometry, and states of an obstacle:

- ID Integer that identifies each object. Stored in the ObstacleIDs property of the dynamicCapsuleList3D object specified by the capsuleList0bj argument.
- States -- Location and orientation of the object as an M-by-6 matrix, where each row is of form
 [x y z qW qX qY qZ], and M is the number of states along the path of the object in the world

frame. The list of states assumes each state is separated by a fixed time interval. xyz-positions are in meters, and the orientation is a four-element quaternion vector. The default local origin is located at the center of the left hemisphere of the capsule.

• Geometry — Structure with fields Length, Radius, and FixedTransform. These fields define the size of the capsule-based object using the specified length for the cylinder and hemisphere radius for the end caps. To shift the capsule geometry from the default origin, specify the FixedTransform field as a fixed transform relative to the local frame of the capsule. To keep the default capsule origin, specify the transform as eye(4).



status — Result of adding obstacles

N-element column vector

Result of adding obstacles, returned as a N-element column vector of ones, zeros, and negative ones. N is the number of obstacles specified in the obstacleStruct argument. Each value indicates whether the associated body is added (1), updated (0), or a duplicate (-1). While adding obstacles, if multiple structures with the same body ID are found in the structure array obstaclesStruct, then the function marks the previous entry as duplicate and ignores it.

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

Objects

dynamicCapsuleList|dynamicCapsuleList3D

Functions

addEgo | checkCollision | egoGeometry | egoPose | obstacleGeometry | obstaclePose |
removeEgo | removeObstacle | show | updateEgoGeometry | updateEgoPose |
updateObstacleGeometry | updateObstaclePose

Topics

"Highway Trajectory Planning Using Frenet Reference Path"

Introduced in R2020b

insfilterErrorState

Estimate pose from IMU, GPS, and monocular visual odometry (MVO) data

Description

The insfilterErrorState object implements sensor fusion of IMU, GPS, and monocular visual odometry (MVO) data to estimate pose in the NED (or ENU) reference frame. The filter uses a 17-element state vector to track the orientation quaternion, velocity, position, IMU sensor biases, and the MVO scaling factor. The insfilterErrorState object uses an error-state Kalman filter to estimate these quantities.

Creation

Syntax

```
filter = insfilterErrorState
filter = insfilterErrorState('ReferenceFrame', RF)
filter = insfilterErrorState(____, Name, Value)
```

Description

filter = insfilterErrorState creates an insfilterErrorState object with default property values.

filter = insfilterErrorState('ReferenceFrame', RF) allows you to specify the reference frame, RF, of the filter. Specify RF as 'NED' (North-East-Down) or 'ENU' (East-North-Up). The default value is 'NED'.

filter = insfilterErrorState(____, Name, Value) also allows you set properties of the created filter using one or more name-value pairs. Enclose each property name in single quotes.

Properties

IMUSampleRate — Sample rate of IMU (Hz)

100 (default) | positive scalar

Sample rate of the inertial measurement unit (IMU) in Hz, specified as a positive scalar.

Data Types: single | double

ReferenceLocation — Reference location (deg, deg, meters)

```
[0 0 0] (default) | 3-element positive row vector
```

Reference location, specified as a 3-element row vector in geodetic coordinates (latitude, longitude, and altitude). Altitude is the height above the reference ellipsoid model, WGS84. The reference location units are [degrees degrees meters].

```
Data Types: single | double
```

GyroscopeNoise — Multiplicative process noise variance from gyroscope ((rad/s)²)

[1e-6 1e-6] (default) | scalar | 3-element row vector

Multiplicative process noise variance from the gyroscope in (rad/s)², specified as a scalar or 3-element row vector of positive real finite numbers.

- If GyroscopeNoise is specified as a row vector, the elements correspond to the noise in the *x*, *y*, and *z* axes of the gyroscope, respectively.
- If GyroscopeNoise is specified as a scalar, the single element is applied to each axis.

Data Types: single | double

GyroscopeBiasNoise — Additive process noise variance from gyroscope bias ((rad/s)²)

[1e-9 1e-9] (default) | scalar | 3-element row vector

Additive process noise variance from the gyroscope bias in $(rad/s)^2$, specified as a scalar or 3-element row vector of positive real finite numbers.

- If GyroscopeBiasNoise is specified as a row vector, the elements correspond to the noise in the *x*, *y*, and *z* axes of the gyroscope, respectively.
- If GyroscopeBiasNoise is specified as a scalar, the single element is applied to each axis

Data Types: single | double

AccelerometerNoise — Multiplicative process noise variance from accelerometer $((m/s^2)^2)$

[1e-4 1e-4 1e-4] (default) | scalar | 3-element row vector

Multiplicative process noise variance from the accelerometer in $(m/s^2)^2$, specified as a scalar or 3-element row vector of positive real finite numbers.

- If AccelerometerNoise is specified as a row vector, the elements correspond to the noise in the x, y, and z axes of the accelerometer, respectively.
- If AccelerometerNoise is specified as a scalar, the single element is applied to each axis.

Data Types: single | double

AccelerometerBiasNoise — Additive process noise variance from accelerometer bias $((m/s^2)^2)$

[1e-4 1e-4] (default) | scalar | 3-element row vector

Additive process noise variance from accelerometer bias in $(m/s^2)^2$, specified as a scalar or 3-element row vector of positive real numbers.

- If AccelerometerBiasNoise is specified as a row vector, the elements correspond to the noise in the *x*, *y*, and *z* axes of the accelerometer, respectively.
- If AccelerometerBiasNoise is specified as a scalar, the single element is applied to each axis.

State — State vector of Kalman filter

[1; zeros(15,1);1] (default) | 17-element column vector

State vector of the extended Kalman filter, specified as a 17-element column vector. The state values represent:

State	Units	Index
Orientation (quaternion parts)	N/A	1:4
Position (NED or ENU)	m	5:7
Velocity (NED or ENU)	m/s	8:10
Gyroscope Bias (XYZ)	rad/s	11:13
Accelerometer Bias (XYZ)	m/s ²	14:16
Visual Odometry Scale (XYZ)	N/A	17

The default initial state corresponds to an object at rest located at $[0\ 0\ 0]$ in geodetic LLA coordinates.

Data Types: single | double

StateCovariance — State error covariance for Kalman filter

ones (16) (default) | 16-by-16 matrix

State error covariance for the Kalman filter, specified as a 16-by-16-element matrix of real numbers. The state error covariance values represent:

State Covariance	Row/Column Index
δ Rotation Vector (XYZ)	1:3
δ Position (NED or ENU)	4:6
δ Velocity (NED or ENU)	7:9
δ Gyroscope Bias (XYZ)	10:12
δ Accelerometer Bias (XYZ)	13:15
δ Visual Odometry Scale (XYZ)	16

Note that because this is an error-state Kalman filter, it tracks the errors in the states. δ represents the error in the corresponding state.

Data Types: single | double

Object Functions

predict correct residual	Update states using accelerometer and gyroscope data for insfilterErrorState Correct states using direct state measurements for insfilterErrorState Residuals and residual covariances from direct state measurements for
	insfilterErrorState
fusegps	Correct states using GPS data for insfilterErrorState
residualgps	Residuals and residual covariance from GPS measurements for insfilterErrorState
fusemvo	Correct states using monocular visual odometry for insfilterErrorState
residualmvo	Residuals and residual covariance from monocular visual odometry measurements for insfilterErrorState
pose	Current orientation and position estimate for insfilterErrorState
reset	Reset internal states for insfilterErrorState
stateinfo	Display state vector information for insfilterErrorState
tune	Tune insfilterErrorState parameters to reduce estimation error
copy	Create copy of insfilterErrorState

Examples

Estimate Pose of Ground Vehicle

Load logged data of a ground vehicle following a circular trajectory. The .mat file contains IMU and GPS sensor measurements and ground truth orientation and position.

```
load('loggedGroundVehicleCircle.mat', ...
   'imuFs','localOrigin', ...
   'initialStateCovariance', ...
   'accelData','gyroData', ...
   'gpsFs','gpsLLA','Rpos','gpsVel','Rvel', ...
   'trueOrient','truePos');
```

Create an INS filter to fuse IMU and GPS data using an error-state Kalman filter.

```
initialState = [compact(trueOrient(1)),truePos(1,:),-6.8e-3,2.5002,0,zeros(1,6),1].';
filt = insfilterErrorState;
filt.IMUSampleRate = imuFs;
filt.ReferenceLocation = localOrigin;
filt.State = initialState;
filt.StateCovariance = initialStateCovariance;
```

Preallocate variables for position and orientation. Allocate a variable for indexing into the GPS data.

```
numIMUSamples = size(accelData,1);
estOrient = ones(numIMUSamples,1,'quaternion');
estPos = zeros(numIMUSamples,3);

gpsIdx = 1;
```

Fuse accelerometer, gyroscope, and GPS data. The outer loop predicts the filter forward at the fastest sample rate (the IMU sample rate).

```
for idx = 1:numIMUSamples

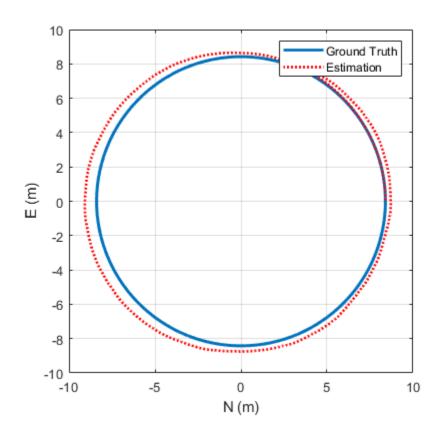
% Use predict to estimate the filter state based on the accelData and
% gyroData arrays.
predict(filt,accelData(idx,:),gyroData(idx,:));

% GPS data is collected at a lower sample rate than IMU data. Fuse GPS
% data at the lower rate.
if mod(idx, imuFs / gpsFs) == 0
% Correct the filter states based on the GPS data.
fusegps(filt,gpsLLA(gpsIdx,:),Rpos,gpsVel(gpsIdx,:),Rvel);
gpsIdx = gpsIdx + 1;
end
% Log the current pose estimate
[estPos(idx,:), estOrient(idx,:)] = pose(filt);
end
```

Calculate the RMS errors between the known true position and orientation and the output from the error-state filter.

```
pErr = truePos - estPos;
qErr = rad2deg(dist(estOrient,trueOrient));
```

```
pRMS = sqrt(mean(pErr.^2));
qRMS = sqrt(mean(qErr.^2));
fprintf('Position RMS Error\n');
Position RMS Error
fprintf('\tX: %.2f, Y: %.2f, Z: %.2f (meters)\n\n',pRMS(1),pRMS(2),pRMS(3));
    X: 0.40, Y: 0.24, Z: 0.05 (meters)
fprintf('Quaternion Distance RMS Error\n');
Quaternion Distance RMS Error
fprintf('\t%.2f (degrees)\n\n',qRMS);
    0.30 (degrees)
Visualize the true position and the estimated position.
plot(truePos(:,1),truePos(:,2),estPos(:,1),estPos(:,2),'r:','LineWidth',2)
grid on
axis square
xlabel('N (m)')
ylabel('E (m)')
legend('Ground Truth', 'Estimation')
```



Algorithms

Note: The following algorithm only applies to an NED reference frame.

insfilterErrorState uses a 17-axis error state Kalman filter structure to estimate pose in the NED reference frame. The state is defined as:

where

- q_0 , q_1 , q_2 , q_3 Parts of orientation quaternion. The orientation quaternion represents a frame rotation from the platform's current orientation to the local NED coordinate system.
- position_N, position_E, position_D -- Position of the platform in the local NED coordinate system.
- *gyrobias*_X, *gyrobias*_Y, *gyrobias*_Z -- Bias in the gyroscope reading.
- accelbias_x, accelbias_y, accelbias_z -- Bias in the accelerometer reading.
- *scaleFactor* -- Scale factor of the pose estimate.

Given the conventional formulation of the state transition function,

$$x_{k|k-1} = f(\widehat{x}_{k-1|k-1})$$

the predicted state estimate is:

$$x_{k|k-1} =$$

```
q_0 + \Delta t * q_1(gyrobias_X/2 - gyro_X/2) + \Delta t * q_2 * (gyrobias_Y/2 - gyro_Y/2) + \Delta t * q_3 * (gyrobias_Z/2 - gyro_Z/2)
q_1 - \Delta t * q_0(gyrobias_X/2 - gyro_X/2) + \Delta t * q_3 * (gyrobias_Y/2 - gyro_Y/2) - \Delta t * q_2 * (gyrobias_Z/2 - gyro_Z/2)
q_2 - \Delta t * q_3(gyrobias_X/2 - gyro_X/2) - \Delta t * q_0 * (gyrobias_Y/2 - gyro_Y/2) + \Delta t * q_1 * (gyrobias_Z/2 - gyro_Z/2)
q_3 + \Delta t * q_2(gyrobias_X/2 - gyro_X/2) - \Delta t * q_1 * (gyrobias_Y/2 - gyro_Y/2) - \Delta t * q_0 * (gyrobias_Z/2 - gyro_Z/2)
                                                                                                            position_N + \Delta t * v_N
                                                                                                            position_E + \Delta t * v_E
                                                                                                            position_D + \Delta t * v_D
                          q_0 * (q_0 * (accelbias_X - accel_X) - q_3 * (accelbias_Y - accel_Y) + q_2 * (accelbias_Z - accel_Z)) + q_N + q_
                           | q_2*(q_1*(accelbias_Y - accel_Y) - q_2*(accelbias_X - accel_X) + q_0*(accelbias_Z - accel_Z)) + \\ 
                           q_1*(q_1*(accelbias_X - accel_X) + q_2*(accelbias_Y - accel_Y) + q_3*(accelbias_Z - accel_Z)) - \\
                          q_3 * (q_3 * (accelbias_X - accel_X) + q_0 * (accelbias_Y - accel_Y) - q_1 * (accelbias_Z - accel_Z))
                          q_1*(q_1*(accelbias_Y-accel_Y)-q_2*(accelbias_X-accel_X)+q_0*(accelbias_Z-accel_Z))+\\
                           q_2*(q_1*(accelbias_X-accel_X)+q_2*(accelbias_Y-accel_Y)+q_3*(accelbias_Z-accel_Z))+\\
                            q_3 * (q_0 * (accelbias_X - accel_X) - q_3 * (accelbias_Y - accel_Y) + q_2 * (accelbias_Z - accel_Z))
                            q_0*(q_1*(accelbias_Y-accel_Y)-q_2*(accelbias_X-accel_X)+q_0*(accelbias_Z-accel_Z))+g_D+c
                                  +(a + (accolhies - accol ) + a + (accolhies - accol )
```

where

- Δt -- IMU sample time.
- + $g_{\rm N}$, $g_{\rm E}$, $g_{\rm D}$ -- Constant gravity vector in the NED frame.

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

insfilterAsync|insfilterMARG|insfilterNonholonomic

correct

Correct states using direct state measurements for insfilterErrorState

Syntax

correct(FUSE,idx,measurement,measurementCovariance)

Description

correct(FUSE,idx,measurement,measurementCovariance) corrects the state and state estimation error covariance of FUSE, an insfilterErrorState object, based on the measurement and measurement covariance. The measurement maps directly to the state specified by the indices idx.

Input Arguments

FUSE — INS filter object

insfilterErrorState

insfilterErrorState, specified as an object.

idx — State vector index of measurements to correct

N-element vector of increasing integers in the range [1, 17]

State vector index of measurements to correct, specified as an N-element vector of increasing integers in the range [1, 17].

The state values represent:

State	Units	Index
Orientation (quaternion parts)	N/A	1:4
Position (NED)	m	5:7
Velocity (NED)	m/s	8:10
Gyroscope Bias (XYZ)	rad/s	11:13
Accelerometer Bias (XYZ)	m/s ²	14:16
Visual Odometry Scale (XYZ)	N/A	17

Data Types: single | double

measurement — Direct measurement of state

N-element vector

Direct measurement of state, specified as a N-element vector. N is the number of elements of the index argument, idx.

Data Types: single | double

measurementCovariance — Covariance of measurement

scalar | *M*-element vector | *M*-by-*M* matrix

Covariance of measurement, specified as a scalar, M-element vector, or M-by-M matrix. If you correct orientation (state indices 1-4), then M = numel(idx)-1. If you do not correct orientation, then M = numel(idx).

Data Types: single | double

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

insfilter|insfilterErrorState

copy

Create copy of insfilterErrorState

Syntax

newFilter = copy(filter)

Description

newFilter = copy(filter) returns a copy of the insfilterErrorState, filter, with the
exactly same property values.

Input Arguments

filter — Filter to be copied

insfilterErrorState

Filter to be copied, specified as an insfilterErrorState object.

Output Arguments

newFilter — New copied filter

insfilterErrorState

New copied filter, returned as an insfilterErrorState object.

See Also

insfilterErrorState

Introduced in R2020b

fusegps

Correct states using GPS data for insfilterErrorState

Syntax

```
[res,resCov] = fusegps(FUSE,position,positionCovariance)
[res,resCov] = fusegps(FUSE,position,positionCovariance,velocity,velocityCovariance)
```

Description

[res,resCov] = fusegps(FUSE,position,positionCovariance) fuses GPS position data to correct the state estimate.

[res,resCov] = fusegps(FUSE,position,positionCovariance,velocity,
velocityCovariance) fuses GPS position and velocity data to correct the state estimate.

Input Arguments

FUSE — INS filter object

insfilterErrorState

insfilterErrorState, specified as an object.

position — Position of GPS receiver (LLA)

3-element row vector

Position of GPS receiver in geodetic latitude, longitude, and altitude (LLA) specified as a real finite 3element row vector. Latitude and longitude are in degrees with north and east being positive. Altitude is in meters.

Data Types: single | double

positionCovariance — Position measurement covariance of GPS receiver (m²)

scalar | 3-element row vector | 3-by-3 matrix

Position measurement covariance of GPS receiver in m², specified as a 3-by-3 matrix.

Data Types: single | double

velocity — Velocity of GPS receiver in local NED coordinate system (m/s)

3-element row vector

Velocity of the GPS receiver in the local NED coordinate system in m/s, specified as a 3-element row vector.

Data Types: single | double

velocityCovariance — Velocity measurement covariance of GPS receiver (m/s)²

scalar | 3-element row vector | 3-by-3 matrix

Velocity measurement covariance of the GPS receiver in the local NED coordinate system in $(m/s)^2$, specified as a 3-by-3 matrix.

Data Types: single | double

Output Arguments

res - Position and velocity residual

1-by-6 vector of real values

Position and velocity residual, returned as a 1-by-6 vector of real values in m and m/s, respectively.

resCov — Innovation residual

6-by-6 matrix of real values

Innovation residual, returned as a 6-by-6 matrix of real values.

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

insfilter|insfilterErrorState

fusemvo

Correct states using monocular visual odometry for insfilterErrorState

Syntax

[pResidual,oResidual,resCov] = fusemvo(FUSE,position,positionCovariance,ornt, orntCovariance)

Description

[pResidual,oResidual,resCov] = fusemvo(FUSE,position,positionCovariance,ornt,orntCovariance) fuses position and orientation data from monocular visual odometry (MVO) measurements to correct the state and state estimation error covariance.

Input Arguments

FUSE — **INS** filter object

insfilterErrorState

insfilterErrorState, specified as an object.

position — Position of camera in local NED coordinate system (m)

3-element row vector

Position of camera in the local NED coordinate system in meters, specified as a real finite 3-element row vector.

Data Types: single | double

positionCovariance — Position measurement covariance of MVO (m²)

scalar | 3-element vector | 3-by-3 matrix

Position measurement covariance of MVO in m², specified as a scalar, 3-element vector, or 3-by-3 matrix.

Data Types: single | double

ornt — Orientation of camera with respect to local NED coordinate system

scalar quaternion | rotation matrix

Orientation of the camera with respect to the local NED coordinate system, specified as a scalar quaternion or 3-by-3 rotation matrix. The quaternion or rotation matrix is a frame rotation from the NED coordinate system to the current camera coordinate system.

Data Types: quaternion | single | double

orntCovariance — Orientation measurement covariance of monocular visual odometry (rad²)

scalar | 3-element vector | 3-by-3 matrix

Orientation measurement covariance of monocular visual odometry in rad², specified as a scalar, 3-element vector, or 3-by-3 matrix.

Data Types: single | double

Output Arguments

pResidual — Position residual

1-by-3 vector of real values

Position residual, returned as a 1-by-3 vector of real values in m.

oResidual — Rotation vector residual

1-by-3 vector of real values

Rotation vector residual, returned as a 1-by-3 vector of real values in radians.

resCov — Residual covariance

6-by-6 matrix of real values

Residual covariance, returned as a 6-by-6 matrix of real values.

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

insfilter|insfilterErrorState

predict

Update states using accelerometer and gyroscope data for insfilterErrorState

Syntax

predict(FUSE,accelReadings,gyroReadings)

Description

predict(FUSE,accelReadings,gyroReadings) fuses accelerometer and gyroscope data to update the state estimate.

Input Arguments

FUSE — INS filter object

insfilterErrorState

insfilterErrorState, specified as an object.

accelReadings — Accelerometer readings in local sensor body coordinate system (m/s²)

3-element row vector

Accelerometer readings in m/s², specified as a 3-element row vector.

Data Types: single | double

gyroReadings — Gyroscope readings in local sensor body coordinate system (rad/s)

3-element row vector

Gyroscope readings in rad/s, specified as a 3-element row vector.

Data Types: single | double

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

insfilter | insfilterErrorState

reset

Reset internal states for insfilterErrorState

Syntax

reset(FUSE)

Description

reset(FUSE) resets the State, StateCovariance, and internal integrators of FUSE, an insfilterErrorState object, to their default values.

Input Arguments

FUSE — **INS** filter object

insfilterErrorState

insfilterErrorState, specified as an object.

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

insfilter|insfilterErrorState

residual

Residuals and residual covariances from direct state measurements for insfilterErrorState

Syntax

[res, resCov] = residual(FUSE,idx,measurement,measurementCovariance)

Description

[res, resCov] = residual(FUSE,idx,measurement,measurementCovariance) computes the residual, res, and the residual covariance, resCov, based on the direct state measurement and measurement covariance. The measurement maps directly to the states specified by indices, idx.

Input Arguments

FUSE — INS filter object

insfilterErrorState

insfilterErrorState, specified as an object.

idx — State vector index of measurements to correct

N-element vector of increasing integers in the range [1, 17]

State vector index of measurements to correct, specified as an N-element vector of increasing integers in the range [1, 17].

The state values represent:

State	Units	Index
Orientation (quaternion parts)	N/A	1:4
Position (NED)	m	5:7
Velocity (NED)	m/s	8:10
Gyroscope Bias (XYZ)	rad/s	11:13
Accelerometer Bias (XYZ)	m/s ²	14:16
Visual Odometry Scale (XYZ)	N/A	17

Data Types: single | double

measurement — Direct measurement of state

N-element vector

Direct measurement of state, specified as a N-element vector. N is the number of elements of the index argument, idx.

measurementCovariance — Covariance of measurement

N-by-*N* matrix

Covariance of measurement, specified as an N-by-N matrix. N is the number of elements of the index argument, idx.

Output Arguments

res — Measurement residual

1-by-*N* vector of real values

Measurement residual, returned as a 1-by-N vector of real values.

resCov — Residual covariance

N-by-*N* matrix of real values

Residual covariance, returned as a *N*-by-*N* matrix of real values.

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder $^{\text{\tiny TM}}$.

See Also

insfilterErrorState

Introduced in R2020a

residualgps

Residuals and residual covariance from GPS measurements for insfilterErrorState

Syntax

```
[res,resCov] = residualgps(FUSE,position,positionCovariance)
[res,resCov] = residualgps(FUSE,position,positionCovariance,velocity,
velocityCovariance)
```

Description

[res,resCov] = residualgps(FUSE,position,positionCovariance) computes the
residual, res, and the residual covariance, resCov, based on the GPS position measurement and
covariance.

[res,resCov] = residualgps(FUSE,position,positionCovariance,velocity,
velocityCovariance) computes the residual, res, and the residual covariance, resCov, based on
the GPS position measurement and covariance.

Input Arguments

FUSE — **INS** filter object

insfilterErrorState

insfilterErrorState, specified as an object.

position — Position of GPS receiver (LLA)

3-element row vector

Position of GPS receiver in geodetic latitude, longitude, and altitude (LLA) specified as a real finite 3element row vector. Latitude and longitude are in degrees with north and east being positive. Altitude is in meters.

Data Types: single | double

positionCovariance — Position measurement covariance of GPS receiver (m²)

3-by-3 matrix

Position measurement covariance of GPS receiver in m², specified as a 3-by-3 matrix.

Data Types: single | double

velocity — Velocity of GPS receiver in local NED coordinate system (m/s)

3-element row vector

Velocity of the GPS receiver in the local NED coordinate system in m/s, specified as a 3-element row vector.

Data Types: single | double

velocityCovariance — Velocity measurement covariance of GPS receiver (m/s²)

3-by-3 matrix

Velocity measurement covariance of the GPS receiver in the local NED coordinate system in m/s², specified as a 3-by-3 matrix.

Data Types: single | double

Output Arguments

res — Position and velocity residual

1-by-3 vector of real values | 1-by-6 vector of real values

Position and velocity residual, returned as a 1-by-3 vector of real values if the inputs only contain position information, and returned as 1-by-6 vector of real values if the inputs also contain velocity information.

resCov — Residual covariance

3-by-3 matrix of real values | 6-by-6 matrix of real values

Residual covariance, returned as a 3-by-3 matrix of real values if the inputs only contain position information, and a 6-by-6 matrix of real values if the inputs also contain velocity information.

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

insfilterErrorState

Introduced in R2020a

residualmyo

Residuals and residual covariance from monocular visual odometry measurements for insfilterErrorState

Syntax

[pResidual,oResidual,resCov] = residualmvo(FUSE,position,positionCovariance, ornt.orntCovariance)

Description

[pResidual, oResidual, resCov] = residualmvo(FUSE, position, positionCovariance, ornt, orntCovariance) computes the residual information based on the monocular visual odometry measurements and covariance.

Input Arguments

FUSE — INS filter object

insfilterErrorState

insfilterErrorState, specified as an object.

position — Position of camera in local NED coordinate system (m)

3-element row vector

Position of camera in the local NED coordinate system in meters, specified as a real finite 3-element row vector.

Data Types: single | double

positionCovariance — Position measurement covariance of MVO (m²)

scalar | 3-element vector | 3-by-3 matrix

Position measurement covariance of MVO in m², specified as a scalar, 3-element vector, or 3-by-3 matrix.

Data Types: single | double

ornt — Orientation of camera with respect to local NED coordinate system

scalar quaternion | rotation matrix

Orientation of the camera with respect to the local NED coordinate system, specified as a scalar quaternion or 3-by-3 rotation matrix. The quaternion or rotation matrix is a frame rotation from the NED coordinate system to the current camera coordinate system.

Data Types: quaternion | single | double

$\label{eq:covariance} \textbf{orntCovariance} \ \textbf{-} \ \textbf{Orientation} \ \textbf{measurement} \ \textbf{covariance} \ \textbf{of} \ \textbf{monocular} \ \textbf{visual} \ \textbf{odometry} \ (\textbf{rad}^2)$

scalar | 3-element vector | 3-by-3 matrix

Orientation measurement covariance of monocular visual odometry in rad², specified as a scalar, 3-element vector, or 3-by-3 matrix.

Data Types: single | double

Output Arguments

pResidual — Position residual

1-by-3 vector of real values

Position residual, returned as a 1-by-3 vector of real values in meters.

oResidual — Rotation vector residual

1-by-3 vector of real values

Rotation vector residual, returned a 1-by-3 vector of real values in radians.

resCov — Residual covariance

6-by-6 matrix of real values

Residual covariance, returned as a 6-by-6 matrix of real values.

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

insfilter|insfilterErrorState

Introduced in R2020a

stateinfo

Display state vector information for insfilterErrorState

Syntax

```
stateinfo(FUSE)
info = stateinfo(FUSE)
```

Description

stateinfo(FUSE) displays the meaning of each index of the State property of FUSE, an insfilterErrorState object, and the associated units.

info = stateinfo(FUSE) returns a structure with fields containing descriptions of the elements of
the state vector of the filter, FUSE.

Examples

State Information of insfilterErrorState

Create an insfilterErrorState object.

```
filter = insfilterErrorState;
```

Display the state information of the created filter.

stateinfo(filter)

States	Units	Index
Orientation (quaternion parts)		1:4
Position (NAV)	m	5:7
Velocity (NAV)	m/s	8:10
Gyroscope Bias (XYZ)	rad/s	11:13
Accelerometer Bias (XYZ)	m/s^2	14:16
Visual Odometry Scale		17

Output the state information of the filter as a structure.

info = stateinfo(filter)

Input Arguments

FUSE — **INS** filter object

insfilterErrorState

insfilterErrorState, specified as an object.

Output Arguments

info — State information

structure

State information, returned as a structure with fields containing descriptions of the elements of the state vector of the filter. The values of each field are the corresponding indices of the state vector.

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

insfilter|insfilterErrorState

Introduced in R2019a

pose

Current orientation and position estimate for insfilterErrorState

Syntax

```
[position,orientation,velocity] = pose(FUSE)
[position,orientation,velocity] = pose(FUSE,format)
```

Description

[position, orientation, velocity] = pose(FUSE) returns the current estimate of the pose of the object tracked by FUSE, an insfilterErrorState object.

[position, orientation, velocity] = pose(FUSE, format) returns the current estimate of the pose with orientation in the specified orientation format.

Input Arguments

FUSE — INS filter object

insfilterErrorState

insfilterErrorState, specified as an object.

format — Output orientation format

```
'quaternion' (default) | 'rotmat'
```

Output orientation format, specified as either 'quaternion' for a quaternion or 'rotmat' for a rotation matrix.

Data Types: char | string

Output Arguments

position — Position estimate in local NED coordinate system (m)

3-element row vector

Position estimate in the local NED coordinate system in meters, returned as a 3-element row vector.

Data Types: single | double

orientation — Orientation estimate in local NED coordinate system

quaternion (default) | 3-by-3 rotation matrix

Orientation estimate in the local NED coordinate system, returned as a scalar quaternion or 3-by-3 rotation matrix, depending on the specified orientation format. The quaternion or rotation matrix represents a frame rotation from the local NED reference frame to the body reference frame.

Data Types: single | double | quaternion

velocity — Velocity estimate in local NED coordinate system (m/s)

3-element row vector

Velocity estimate in the local NED coordinate system in m/s, returned as a 3-element row vector.

Data Types: single | double

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder $^{\text{\tiny TM}}$.

See Also

insfilter|insfilterErrorState

Introduced in R2019a

tune

Tune insfilterErrorState parameters to reduce estimation error

Syntax

```
tunedMeasureNoise = tune(filter,measureNoise,sensorData,groundTruth)
tunedMeasureNoise = tune(____,config)
```

Description

tunedMeasureNoise = tune(filter, measureNoise, sensorData, groundTruth) adjusts the properties of the insfilterErrorState filter object, filter, and measurement noises to reduce the root-mean-squared (RMS) state estimation error between the fused sensor data and the ground truth. The function also returns the tuned measurement noise, tunedMeasureNoise. The function uses the property values in the filter and the measurement noise provided in the measureNoise structure as the initial estimate for the optimization algorithm.

tunedMeasureNoise = tune(____, config) specifies the tuning configuration based on a tunerconfig object, config.

Examples

Tune insfilterErrorState to Optimize Pose Estimate

Load the recorded sensor data and ground truth data.

```
load('insfilterErrorStateTuneData.mat');
Create tables for the sensor data and the truth data.
sensorData = table(Accelerometer,Gyroscope, ...
    GPSPosition,GPSVelocity,MV00rientation, ...
    MV0Position);
groundTruth = table(Orientation,Position);
Create an insfilterErrorState filter object.
filter = insfilterErrorState('State',initialState, ...
    'StateCovariance',initialStateCovariance);
```

Create a tuner configuration object for the filter. Use the tuner noise function to obtain a set of initial sensor noises used in the filter.

```
cfg = tunerconfig('insfilterErrorState','MaxIterations',40);
measNoise = tunernoise('insfilterErrorState')

measNoise = struct with fields:
    MV00rientationNoise: 1
    MV0PositionNoise: 1
    GPSPositionNoise: 1
```

GPSVelocityNoise: 1

Tune the filter and obtain the tuned parameters.

tunedmn = tune(filter,measNoise,sensorData, ...
groundTruth,cfg);

Iteration	Parameter	Metric
1	AccelerometerNoise	4.1291
1	GyroscopeNoise	4.1291
1	AccelerometerBiasNoise	4.1290
1	GyroscopeBiasNoise	4.1290
1	GPSPositionNoise	4.0213
1	GPSVelocityNoise	4.0051
1	MV0PositionNoise	3.9949
1	MV00rientationNoise	3.9886
2	AccelerometerNoise	3.9886
2 2	GyroscopeNoise	3.9886
2	AccelerometerBiasNoise	3.9886
2	GyroscopeBiasNoise	3.9886
2	GPSPositionNoise	3.8381
2	GPSVelocityNoise	3.8268
2	MVOPositionNoise	3.8219
2	MV00rientationNoise	3.8035
3	AccelerometerNoise	3.8035
3	GyroscopeNoise	3.8035
3	AccelerometerBiasNoise	3.8035
2 2 3 3 3 3 3 3 3 3	GyroscopeBiasNoise	3.8035
3	GPSPositionNoise	3.6299
3	GPSVelocityNoise	3.6276
3	MVOPositionNoise	3.6241
	MV00rientationNoise	3.5911
4	AccelerometerNoise	3.5911
4	GyroscopeNoise	3.5911
4	AccelerometerBiasNoise	
4	GyroscopeBiasNoise	3.5911
4	GPSPositionNoise	3.1728
4	GPSVelocityNoise	3.1401
4	MVOPositionNoise	2.7686
4	MV00rientationNoise	2.6632
5	AccelerometerNoise	2.6632 2.6632
5	GyroscopeNoise	2.6632
5	AccelerometerBiasNoise	2.6632
5	GyroscopeBiasNoise GPSPositionNoise	2.3242
5 5 5 5 5	GPSVelocityNoise	2.3242
5	MV0PositionNoise	2.2291
5	MV00rientationNoise	2.2291
6	AccelerometerNoise	2.0904
6	GyroscopeNoise	2.0903
6	AccelerometerBiasNoise	2.0903
6	GyroscopeBiasNoise	2.0903
6	GPSPositionNoise	2.0903
6	GPSVelocityNoise	2.0141
6	MVOPositionNoise	1.9952
6	MV00rientationNoise	1.8497

7	AccoloromotorNojco	1 0407
7	AccelerometerNoise	1.8497
7	GyroscopeNoise	1.8496
7	AccelerometerBiasNoise	1.8496
7	GyroscopeBiasNoise	1.8496
7	GPSPositionNoise	1.8398
7	GPSVelocityNoise	1.7528
7	MVOPositionNoise	1.7362
7	MV00rientationNoise	1.5762
8	AccelerometerNoise	1.5762
		1.5762
8	GyroscopeNoise	
8	AccelerometerBiasNoise	1.5762
8	GyroscopeBiasNoise	1.5762
8	GPSPositionNoise	1.5762
8	GPSVelocityNoise	1.5107
		1.4786
8	MVOPositionNoise	
8	MV00rientationNoise	1.3308
9	AccelerometerNoise	1.3308
9	GyroscopeNoise	1.3308
9	AccelerometerBiasNoise	1.3308
		1.3308
9	GyroscopeBiasNoise	
9	GPSPositionNoise	1.3308
9	GPSVelocityNoise	1.2934
9	MVOPositionNoise	1.2525
9	MV00rientationNoise	1.1462
10	AccelerometerNoise	1.1462
10	GyroscopeNoise	1.1462
10	AccelerometerBiasNoise	1.1462
10	GyroscopeBiasNoise	1.1462
10	GPSPositionNoise	1.1443
10	GPSVelocityNoise	1.1332
10	MVOPositionNoise	1.0964
10	MV00rientationNoise	1.0382
11	AccelerometerNoise	1.0382
11	GyroscopeNoise	1.0382
11	AccelerometerBiasNoise	1.0382
11	GyroscopeBiasNoise	1.0382
11		
	GPSPositionNoise	1.0348
11	GPSVelocityNoise	1.0348
11	MVOPositionNoise	1.0081
11	MV00rientationNoise	0.9734
12	AccelerometerNoise	0.9734
		0.9734
12	GyroscopeNoise	
12	AccelerometerBiasNoise	0.9734
12	GyroscopeBiasNoise	0.9734
12	GPSPositionNoise	0.9693
12	GPSVelocityNoise	0.9682
12	MVOPositionNoise	0.9488
12	MV00rientationNoise	
		0.9244
13	AccelerometerNoise	0.9244
13	GyroscopeNoise	0.9244
13	AccelerometerBiasNoise	0.9244
13	GyroscopeBiasNoise	0.9244
13	GPSPositionNoise	0.9203
13	GPSVelocityNoise	0.9199
13	MVOPositionNoise	0.9045
13	MV00rientationNoise	0.8846
14	AccelerometerNoise	0.8846
14	GyroscopeNoise	0.8846
	•	

14	AccelerometerBiasNoise	0.8845
14	GyroscopeBiasNoise	0.8845
14	GPSPositionNoise	0.8807
14	GPSVelocityNoise	0.8807
14	MVOPositionNoise	0.8659
14	MV00rientationNoise	0.8501
15	AccelerometerNoise	0.8501
15	GyroscopeNoise	0.8501
15		0.8500
	AccelerometerBiasNoise	
15	GyroscopeBiasNoise	0.8500
15	GPSPositionNoise	0.8457
15	GPSVelocityNoise	0.8453
15	MVOPositionNoise	0.8299
15	MV00rientationNoise	0.8173
16	AccelerometerNoise	0.8173
16	GyroscopeNoise	0.8173
16	AccelerometerBiasNoise	0.8172
16	GyroscopeBiasNoise	0.8172
16	GPSPositionNoise	0.8122
16	GPSVelocityNoise	0.8116
16	MVOPositionNoise	0.7961
16	MV00rientationNoise	0.7858
17	AccelerometerNoise	0.7858
17		0.7858
	GyroscopeNoise	
17	AccelerometerBiasNoise	0.7857
17	GyroscopeBiasNoise	0.7857
17	GPSPositionNoise	0.7807
17	GPSVelocityNoise	0.7800
17	MVOPositionNoise	0.7655
17	MV00rientationNoise	0.7572
18		0.7572
	AccelerometerNoise	
18	GyroscopeNoise	0.7572
18	AccelerometerBiasNoise	0.7570
18	GyroscopeBiasNoise	0.7570
18	GPSPositionNoise	0.7525
18	GPSVelocityNoise	0.7520
18	MVOPositionNoise	0.7401
18	MV00rientationNoise	0.7338
19	AccelerometerNoise	0.7337
19	GyroscopeNoise	0.7337
19	AccelerometerBiasNoise	0.7335
19		0.7335
	GyroscopeBiasNoise	
19	GPSPositionNoise	0.7293
19	GPSVelocityNoise	0.7290
19	MV0PositionNoise	0.7185
19	MV00rientationNoise	0.7140
20	AccelerometerNoise	0.7138
20	GyroscopeNoise	0.7138
20	AccelerometerBiasNoise	0.7134
20	GyroscopeBiasNoise	0.7134
20	GPSPositionNoise	0.7086
20	GPSVelocityNoise	0.7068
20	MVOPositionNoise	0.6956
20	MV00rientationNoise	0.6926
21	AccelerometerNoise	0.6922
21		
	GyroscopeNoise	0.6922
21	AccelerometerBiasNoise	0.6916
21	GyroscopeBiasNoise	0.6916
	0,103copcb1d3N013c	0.0010

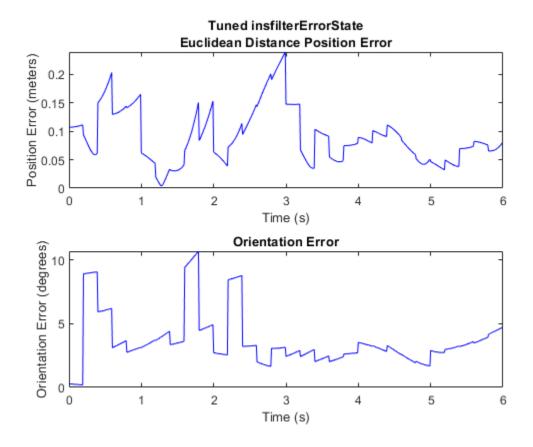
21	GPSPositionNoise	0.6862
21	GPSVelocityNoise	0.6822
21	MVOPositionNoise	0.6682
21	MV00rientationNoise	0.6667
22		
	AccelerometerNoise	0.6660
22	GyroscopeNoise	0.6660
22	AccelerometerBiasNoise	0.6650
22	GyroscopeBiasNoise	0.6650
22	GPSPositionNoise	0.6605
22	GPSVelocityNoise	0.6541
22	MVOPositionNoise	0.6372
22		
	MV00rientationNoise	0.6368
23	AccelerometerNoise	0.6356
23	GyroscopeNoise	0.6356
23	AccelerometerBiasNoise	0.6344
23	GyroscopeBiasNoise	0.6344
23	GPSPositionNoise	0.6324
23	GPSVelocityNoise	0.6252
23	MVOPositionNoise	0.6087
23	MV00rientationNoise	0.6087
24	AccelerometerNoise	0.6075
24	GyroscopeNoise	0.6075
24	AccelerometerBiasNoise	0.6068
24	GyroscopeBiasNoise	0.6068
24	GPSPositionNoise	0.6061
24	GPSVelocityNoise	0.6032
24	MVOPositionNoise	0.6032
24	MV00rientationNoise	0.6032
25	AccelerometerNoise	0.6017
25	GyroscopeNoise	0.6017
25	AccelerometerBiasNoise	0.6012
25	GyroscopeBiasNoise	0.6012
25	GPSPositionNoise	0.6010
25	GPSVelocityNoise	0.6005
25	MVOPositionNoise	0.6005
25	MV00rientationNoise	0.6005
26	AccelerometerNoise	0.5992
26	GyroscopeNoise	0.5992
26	AccelerometerBiasNoise	0.5987
26	GyroscopeBiasNoise	0.5987
26	GPSPositionNoise	0.5983
20		0.5965
26	GPSVelocityNoise	0.5983
26	MVOPositionNoise	0.5983
26	MV00rientationNoise	0.5980
27	AccelerometerNoise	0.5973
27	GyroscopeNoise	0.5973
27	AccelerometerBiasNoise	0.5972
27	GyroscopeBiasNoise	0.5972
27	GPSPositionNoise	0.5970
27	GPSVelocityNoise	0.5970
27	MVOPositionNoise	0.5970
27	MV00rientationNoise	0.5970
28	AccelerometerNoise	0.5970
28		
	GyroscopeNoise	0.5970
28	AccelerometerBiasNoise	0.5970
28		0.5970
	GyroscopeBiasNoise	
28	GPSPositionNoise	0.5970
		0.5970
28	GPSVelocityNoise	0.39/0

28	MVOPositionNoise	0.5969
28	MV00rientationNoise	0.5966
29	AccelerometerNoise	0.5966
29	GyroscopeNoise	0.5966
29	AccelerometerBiasNoise	0.5966
29	GyroscopeBiasNoise	0.5966
29	GPSPositionNoise	0.5966
29	GPSVelocityNoise	0.5966
29	MVOPositionNoise	0.5965
29	MV00rientationNoise	0.5965
30	AccelerometerNoise	0.5965
30	GyroscopeNoise	0.5965
	-	
30	AccelerometerBiasNoise	0.5965
30	GyroscopeBiasNoise	0.5965
30	GPSPositionNoise	0.5964
30	GPSVelocityNoise	0.5964
30	MVOPositionNoise	0.5964
30	MV00rientationNoise	0.5961
31	AccelerometerNoise	0.5961
31	GyroscopeNoise	0.5961
31	AccelerometerBiasNoise	0.5960
31	GyroscopeBiasNoise	0.5960
31	GPSPositionNoise	0.5960
31	GPSVelocityNoise	0.5960
31	MVOPositionNoise	0.5960
31	MV00rientationNoise	0.5958
32	AccelerometerNoise	0.5956
32	GyroscopeNoise	0.5956
32	AccelerometerBiasNoise	0.5956
32	GyroscopeBiasNoise	0.5956
32	GPSPositionNoise	0.5955
32	GPSVelocityNoise	0.5955
32	MVOPositionNoise	0.5954
32	MV00rientationNoise	0.5954
33	AccelerometerNoise	0.5954
33	GyroscopeNoise	0.5954
33	AccelerometerBiasNoise	0.5953
33	GyroscopeBiasNoise	0.5953
33	GPSPositionNoise	0.5953
33	GPSVelocityNoise	0.5953
33	MVOPositionNoise	0.5952
33	MV00rientationNoise	0.5950
34	AccelerometerNoise	0.5949
34	GyroscopeNoise	0.5949
34	AccelerometerBiasNoise	0.5949
34	GyroscopeBiasNoise	0.5949
34	GPSPositionNoise	0.5948
34	GPSVelocityNoise	0.5947
34	MVOPositionNoise	0.5946
34	MV00rientationNoise	0.5946
35	AccelerometerNoise	0.5946
35	GyroscopeNoise	0.5946
	-	
35	AccelerometerBiasNoise	0.5946
35	GyroscopeBiasNoise	0.5946
35	GPSPositionNoise	0.5946
35	GPSVelocityNoise	0.5945
35	MVOPositionNoise	0.5944
35	MV00rientationNoise	0.5943

```
36
             AccelerometerNoise
                                        0.5942
36
             GyroscopeNoise
                                        0.5942
36
             AccelerometerBiasNoise
                                        0.5942
36
             GyroscopeBiasNoise
                                        0.5942
36
             GPSPositionNoise
                                        0.5941
36
             GPSVelocityNoise
                                        0.5941
36
             MVOPositionNoise
                                        0.5939
36
             MV00rientationNoise
                                        0.5939
37
             AccelerometerNoise
                                        0.5939
37
             GvroscopeNoise
                                        0.5939
37
             AccelerometerBiasNoise
                                        0.5939
37
             GyroscopeBiasNoise
                                        0.5939
37
             GPSPositionNoise
                                        0.5939
37
             GPSVelocityNoise
                                        0.5939
37
             MV0PositionNoise
                                        0.5937
37
             MV00rientationNoise
                                        0.5937
38
             AccelerometerNoise
                                        0.5937
38
             GyroscopeNoise
                                        0.5937
38
             AccelerometerBiasNoise
                                        0.5937
38
             GyroscopeBiasNoise
                                        0.5937
38
             GPSPositionNoise
                                        0.5936
             GPSVelocityNoise
38
                                        0.5935
38
             MVOPositionNoise
                                        0.5935
38
             MV00rientationNoise
                                        0.5935
39
                                        0.5935
             AccelerometerNoise
39
                                        0.5935
             GyroscopeNoise
39
             AccelerometerBiasNoise
                                        0.5935
39
             GyroscopeBiasNoise
                                        0.5935
39
             GPSPositionNoise
                                        0.5934
39
             GPSVelocityNoise
                                        0.5934
39
             MV0PositionNoise
                                        0.5934
39
             MV00rientationNoise
                                        0.5934
40
             AccelerometerNoise
                                        0.5934
40
             GyroscopeNoise
                                        0.5934
40
             AccelerometerBiasNoise
                                        0.5934
40
             GyroscopeBiasNoise
                                        0.5934
40
             GPSPositionNoise
                                        0.5933
40
             GPSVelocityNoise
                                        0.5933
40
             MVOPositionNoise
                                        0.5933
40
             MV00rientationNoise
                                        0.5933
```

Fuse the sensor data using the tuned filter.

```
[posEstTuned(ii,:),qEstTuned(ii,:)] = pose(filter);
end
Compute the RMS errors.
orientationErrorTuned = rad2deg(dist(qEstTuned,Orientation));
rmsOrientationErrorTuned = sqrt(mean(orientationErrorTuned.^2))
rmsOrientationErrorTuned = 4.2335
positionErrorTuned = sqrt(sum((posEstTuned - Position).^2,2));
rmsPositionErrorTuned = sqrt(mean( positionErrorTuned.^2))
rmsPositionErrorTuned = 0.1024
Visualize the results.
figure;
t = (0:N-1)./filter.IMUSampleRate;
subplot(2,1,1)
plot(t, positionErrorTuned, 'b');
title("Tuned insfilterErrorState" + newline + ...
    "Euclidean Distance Position Error")
xlabel('Time (s)');
ylabel('Position Error (meters)')
subplot(2,1,2)
plot(t, orientationErrorTuned, 'b');
title("Orientation Error")
xlabel('Time (s)');
ylabel('Orientation Error (degrees)');
```



Input Arguments

filter — Filter object

insfilterErrorState object

Filter object, specified as an insfilterErrorState object.

measureNoise — Measurement noise

structure

Measurement noise, specified as a structure. The function uses the measurement noise input as the initial guess for tuning the measurement noise. The structure must contain these fields:

Field name	Description
MV00rientationNoise	Orientation measurement covariance of monocular visual odometry, specified as a scalar, 3-element vector, or 3-by-3 matrix in rad ²
MVOPositionNoise	Position measurement covariance of MVO, specified as a scalar, 3-element vector, or 3-by-3 matrix in m ²
GPSPositionNoise	Variance of GPS position noise, specified as a scalar in m ²

Field name	Description
	Variance of GPS velocity noise, specified as a scalar in $(m/s)^2$

sensorData — Sensor data

table

Sensor data, specified as a table. In each row, the sensor data is specified as:

- Accelerometer Accelerometer data, specified as a 1-by-3 vector of scalars in m²/s.
- Gyroscope—Gyroscope data, specified as a 1-by-3 vector of scalars in rad/s.
- MV00rienation Orientation of the camera with respect to the local navigation frame, specified as a scalar quaternion or 3-by-3 rotation matrix. The quaternion or rotation matrix is a frame rotation from the local navigation frame to the current camera coordinate system.
- MVOPosition Position of camera in the local navigation frame, specified as a real 3-element row vector in meters.
- GPSPosition GPS position data, specified as a 1-by-3 vector of scalars in meters.
- GPSVelocity GPS velocity data, specified as a 1-by-3 vector of scalars in m/s.

If the GPS sensor does not produce complete measurements, specify the corresponding entry for GPSPosition and/or GPSVelocity as NaN. If you set the Cost property of the tuner configuration input, config, to Custom, then you can use other data types for the sensorData input based on your choice.

groundTruth — Ground truth data

table

Ground truth data, specified as a table. In each row, the table can optionally contain any of these variables:

- Orientation Orientation from the navigation frame to the body frame, specified as a quaternion or a 3-by-3 rotation matrix.
- Position Position in navigation frame, specified as a 1-by-3 vector of scalars in meters.
- Velocity Velocity in navigation frame, specified as a 1-by-3 vector of scalars in m/s.
- AccelerometerBias Accelerometer delta angle bias in body frame, specified as a 1-by-3 vector of scalars in m²/s.
- VisualOdometryScale Visual odometry scale factor, specified as a scalar.

The function processes each row of the sensorData and groundTruth tables sequentially to calculate the state estimate and RMS error from the ground truth. State variables not present in groundTruth input are ignored for the comparison. The sensorData and the groundTruth tables must have the same number of rows.

If you set the Cost property of the tuner configuration input, config, to Custom, then you can use other data types for the groundTruth input based on your choice.

config — Tuner configuration

tunerconfig object

Tuner configuration, specified as a tunerconfig object.

Output Arguments

tunedMeasureNoise — Tuned measurement noise

structure

Tuned measurement noise, returned as a structure. The structure contains these fields.

Field name	Description
MV00rientationNoise	Orientation measurement covariance of monocular visual odometry, specified as a scalar, 3-element vector, or 3-by-3 matrix in rad ²
MVOPositionNoise	Position measurement covariance of MVO, specified as a scalar, 3-element vector, or 3-by-3 matrix in m ²
GPSPositionNoise	Variance of GPS position noise, specified as a scalar in m ²
GPSVelocityNoise	Variance of GPS velocity noise, specified as a scalar in $(m/s)^2$

References

[1] Abbeel, P., Coates, A., Montemerlo, M., Ng, A.Y. and Thrun, S. Discriminative Training of Kalman Filters. In *Robotics: Science and systems*, Vol. 2, pp. 1, 2005.

See Also

tunerconfig|tunernoise

Introduced in R2021a

gpsSensor

GPS receiver simulation model

Description

The gpsSensor System object models data output from a Global Positioning System (GPS) receiver.

To model a GPS receiver:

- **1** Create the **gpsSensor** object and set its properties.
- **2** Call the object with arguments, as if it were a function.

To learn more about how System objects work, see What Are System Objects?.

Creation

Syntax

```
GPS = gpsSensor
GPS = gpsSensor('ReferenceFrame',RF)
GPS = gpsSensor(____,Name,Value)
```

Description

GPS = gpsSensor returns a gpsSensor System object that computes a Global Positioning System receiver reading based on a local position and velocity input signal. The default reference position in geodetic coordinates is

latitude: 0° N
longitude: 0° E
altitude: 0 m

GPS = gpsSensor('ReferenceFrame', RF) returns a gpsSensor System object that computes a global positioning system receiver reading relative to the reference frame RF. Specify RF as 'NED' (North-East-Down) or 'ENU'(East-North-Up). The default value is 'NED'.

GPS = gpsSensor(____, Name, Value) sets each property Name to the specified Value. Unspecified properties have default values.

Properties

Unless otherwise indicated, properties are *nontunable*, which means you cannot change their values after calling the object. Objects lock when you call them, and the release function unlocks them.

If a property is *tunable*, you can change its value at any time.

For more information on changing property values, see System Design in MATLAB Using System Objects.

SampleRate — Update rate of receiver (Hz)

1 (default) | positive real scalar

Update rate of the receiver in Hz, specified as a positive real scalar.

Data Types: single | double

ReferenceLocation — Origin of local navigation reference frame

[0 0 0] (default) | [degrees degrees meters]

Reference location, specified as a 3-element row vector in geodetic coordinates (latitude, longitude, and altitude). Altitude is the height above the reference ellipsoid model, WGS84. The reference location is in [degrees degrees meters]. The degree format is decimal degrees (DD).

Data Types: single | double

PositionInputFormat — Position coordinate input format

'Local' (default) | 'Geodetic'

Position coordinate input format, specified as 'Local' or 'Geodetic'.

- If you set the property as 'Local', then you need to specify the truePosition input as Cartesian coordinates with respect to the local navigation frame whose origin is fixed and defined by the ReferenceLcation property. Additionally, when you specify the trueVelocity input, you need to specify it with respect to this local navigation frame.
- If you set the property as 'Geodetic', then you need to specify the truePosition input as geodetic coordinates in latitude, longitude, and altitude. Additionally, when you specify the trueVelocity input, you need to specify it with respect to the navigation frame (NED or ENU) whose origin corresponds to the truePosition input. When setting the property as 'Geodetic', the gpsSensor object neglects the ReferenceLocation property.

Data Types: character vector

Horizontal Position Accuracy — Horizontal position accuracy (m)

1.6 (default) | nonnegative real scalar

Horizontal position accuracy in meters, specified as a nonnegative real scalar. The horizontal position accuracy specifies the standard deviation of the noise in the horizontal position measurement.

Tunable: Yes

Data Types: single | double

VerticalPositionAccuracy — Vertical position accuracy (m)

3 (default) | nonnegative real scalar

Vertical position accuracy in meters, specified as a nonnegative real scalar. The vertical position accuracy specifies the standard deviation of the noise in the vertical position measurement.

Tunable: Yes

Data Types: single | double

VelocityAccuracy — Velocity accuracy (m/s)

0.1 (default) | nonnegative real scalar

Velocity accuracy in meters per second, specified as a nonnegative real scalar. The velocity accuracy specifies the standard deviation of the noise in the velocity measurement.

Tunable: Yes

Data Types: single | double

DecayFactor — Global position noise decay factor

0.999 (default) | scalar in the range [0,1]

Global position noise decay factor, specified as a scalar in the range [0,1].

A decay factor of 0 models the global position noise as a white noise process. A decay factor of 1 models the global position noise as a random walk process.

Tunable: Yes

Data Types: single | double

RandomStream — Random number source

'Global stream' (default) | 'mt19937ar with seed'

Random number source, specified as a character vector or string:

- 'Global stream' -- Random numbers are generated using the current global random number stream.
- 'mt19937ar with seed' -- Random numbers are generated using the mt19937ar algorithm with the seed specified by the Seed property.

Data Types: char | string

Seed — Initial seed

67 (default) | nonnegative integer scalar

Initial seed of an mt19937ar random number generator algorithm, specified as a nonnegative integer scalar.

Dependencies

To enable this property, set RandomStream to 'mt19937ar with seed'.

Data Types: single | double | int8 | int16 | int32 | int64 | uint8 | uint16 | uint32 | uint64

Usage

Syntax

[position, velocity, groundspeed, course] = GPS(truePosition, trueVelocity)

Description

[position, velocity, groundspeed, course] = GPS(truePosition, trueVelocity) computes global navigation satellite system receiver readings from the position and velocity inputs.

Input Arguments

truePosition — Position of GPS receiver in navigation coordinate system

N-by-3 matrix

Position of the GPS receiver in the navigation coordinate system, specified as a real finite N-by-3 matrix. N is the number of samples in the current frame.

- When the PositionInputFormat property is specified as 'Local', specify turePosition as Cartesian coordinates with respect to the local navigation frame whose origin is fixed at ReferenceLocation.
- When the PositionInputFormat property is specified as 'Geodetic', specify turePosition as geodetic coordinates in [latitude,longitude,altitude]. Latitude and longitude are in meters. altitude is the height above the WGS84 ellipsoid model in meters.

Data Types: single | double

trueVelocity — Velocity of GPS receiver in navigation coordinate system (m/s)

N-by-3 matrix

Velocity of GPS receiver in the navigation coordinate system in meters per second, specified as a real finite *N*-by-3 matrix. *N* is the number of samples in the current frame.

- When the PositionInputFormat property is specified as 'Local', specify trueVelocity with respect to the local navigation frame (NED or ENU) whose origin is fixed at ReferenceLocation.
- When the PositionInputFormat property is specified as 'Geodetic', specify trueVelocity with respect to the navigation frame (NED or ENU) whose origin corresponds to the truePosition input.

Data Types: single | double

Output Arguments

position — Position in LLA coordinate system

N-by-3 matrix

Position of the GPS receiver in the geodetic latitude, longitude, and altitude (LLA) coordinate system, returned as a real finite *N*-by-3 array. Latitude and longitude are in degrees with North and East being positive. Altitude is in meters.

N is the number of samples in the current frame.

Data Types: single | double

velocity — Velocity in local navigation coordinate system (m/s)

N-by-3 matrix

Velocity of the GPS receiver in the local navigation coordinate system in meters per second, returned as a real finite N-by-3 array. N is the number of samples in the current frame.

• When the PositionInputFormat property is specified as 'Local', the returned velocity is with respect to the local navigation frame whose origin is fixed at ReferenceLocation.

 When the PositionInputFormat property is specified as 'Geodetic', the returned velocity is with respect to the navigation frame (NED or ENU) whose origin corresponds to the position output.

Data Types: single | double

groundspeed — Magnitude of horizontal velocity in local navigation coordinate system (m/s)

N-by-1 column vector

Magnitude of the horizontal velocity of the GPS receiver in the local navigation coordinate system in meters per second, returned as a real finite *N*-by-1 column vector.

N is the number of samples in the current frame.

Data Types: single | double

course — Direction of horizontal velocity in local navigation coordinate system (°)

N-by-1 column vector

Direction of the horizontal velocity of the GPS receiver in the local navigation coordinate system in degrees, returned as a real finite N-by-1 column of values between 0 and 360. North corresponds to 360 degrees and East corresponds to 90 degrees.

N is the number of samples in the current frame.

Data Types: single | double

Object Functions

To use an object function, specify the System object as the first input argument. For example, to release system resources of a System object named obj, use this syntax:

release(obj)

Common to All System Objects

step Run System object algorithm

release Release resources and allow changes to System object property values and input

characteristics

reset Reset internal states of System object

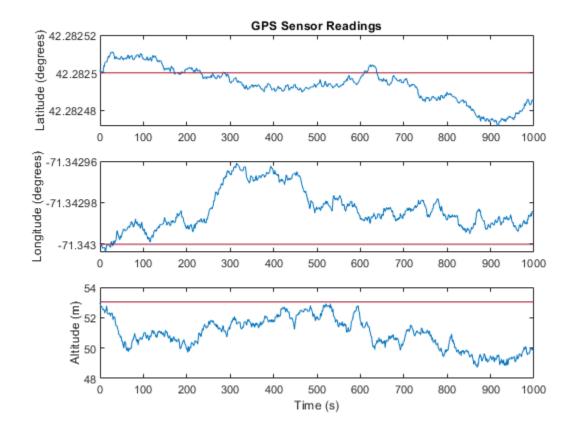
Examples

Generate GPS Position Measurements From Stationary Input

Create a gpsSensor System object[™] to model GPS receiver data. Assume a typical one Hz sample rate and a 1000-second simulation time. Define the reference location in terms of latitude, longitude, and altitude (LLA) of Natick, MA (USA). Define the sensor as stationary by specifying the true position and velocity with zeros.

```
fs = 1;
duration = 1000;
numSamples = duration*fs;
```

```
refLoc = [42.2825 -71.343 53.0352];
truePosition = zeros(numSamples,3);
trueVelocity = zeros(numSamples,3);
gps = gpsSensor('SampleRate',fs,'ReferenceLocation',refLoc);
Call gps with the specified truePosition and trueVelocity to simulate receiving GPS data for a
stationary platform.
position = gps(truePosition,trueVelocity);
Plot the true position and the GPS sensor readings for position.
t = (0:(numSamples-1))/fs;
subplot(3, 1, 1)
plot(t, position(:,1), ...
     t, ones(numSamples)*refLoc(1))
title('GPS Sensor Readings')
ylabel('Latitude (degrees)')
subplot(3, 1, 2)
plot(t, position(:,2), ...
     t, ones(numSamples)*refLoc(2))
ylabel('Longitude (degrees)')
subplot(3, 1, 3)
plot(t, position(:,3), ...
     t, ones(numSamples)*refLoc(3))
ylabel('Altitude (m)')
xlabel('Time (s)')
```

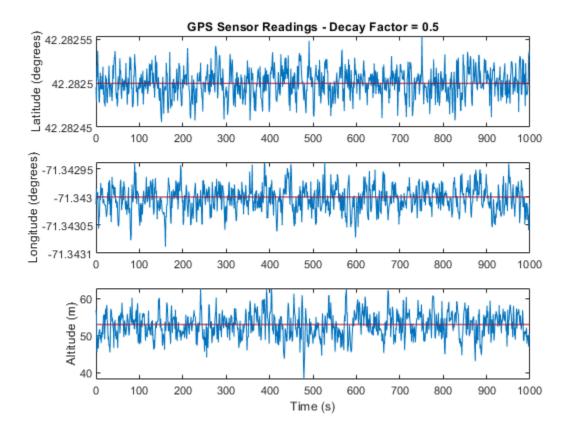


The position readings have noise controlled by HorizontalPositionAccuracy, VerticalPositionAccuracy, VelocityAccuracy, and DecayFactor. The DecayFactor property controls the drift in the noise model. By default, DecayFactor is set to 0.999, which approaches a random walk process. To observe the effect of the DecayFactor property:

- 1 Reset the gps object.
- 2 Set DecayFactor to 0.5.
- **3** Call **gps** with variables specifying a stationary position.
- 4 Plot the results.

The GPS position readings now oscillate around the true position.

```
subplot(3, 1, 3)
plot(t, position(:,3), ...
    t, ones(numSamples)*refLoc(3))
ylabel('Altitude (m)')
xlabel('Time (s)')
```



Relationship Between Groundspeed and Course Accuracy

GPS receivers achieve greater course accuracy as groundspeed increases. In this example, you create a GPS receiver simulation object and simulate the data received from a platform that is accelerating from a stationary position.

Create a default gpsSensor System object™ to model data returned by a GPS receiver.

Create matrices to describe the position and velocity of a platform in the NED coordinate system. The platform begins from a stationary position and accelerates to 60 m/s North-East over 60 seconds, then has a vertical acceleration to 2 m/s over 2 seconds, followed by a 2 m/s rate of climb for another 8 seconds. Assume a constant velocity, such that the velocity is the simple derivative of the position.

```
duration = 70:
numSamples = duration*GPS.SampleRate;
course = 45*ones(duration,1);
groundspeed = [(1:60)';60*ones(10,1)];
Nvelocity
            = groundspeed.*sind(course);
            = groundspeed.*cosd(course);
Evelocity
           = [zeros(60,1);-1;-2*ones(9,1)];
Dvelocity
NEDvelocity = [Nvelocity, Evelocity, Dvelocity];
Ndistance
           = cumsum(Nvelocity);
Edistance
           = cumsum(Evelocity):
Ddistance = cumsum(Dvelocity);
NEDposition = [Ndistance,Edistance,Ddistance];
```

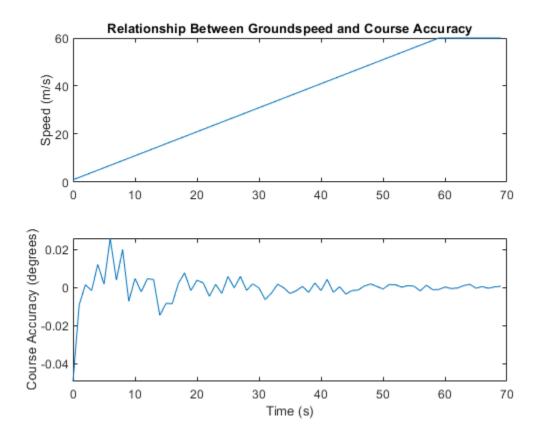
Model GPS measurement data by calling the GPS object with your velocity and position matrices.

```
[\sim,\sim, groundspeedMeasurement, courseMeasurement] = GPS(NEDposition, NEDvelocity);
```

Plot the groundspeed and the difference between the true course and the course returned by the GPS simulator.

As groundspeed increases, the accuracy of the course increases. Note that the velocity increase during the last ten seconds has no effect, because the additional velocity is not in the ground plane.

```
t = (0:numSamples-1)/GPS.SampleRate;
subplot(2,1,1)
plot(t,groundspeed);
ylabel('Speed (m/s)')
title('Relationship Between Groundspeed and Course Accuracy')
subplot(2,1,2)
courseAccuracy = courseMeasurement - course;
plot(t,courseAccuracy)
xlabel('Time (s)');
ylabel('Course Accuracy (degrees)')
```



Model GPS Receiver Data

Simulate GPS data received during a trajectory from the city of Natick, MA, to Boston, MA.

Define the decimal degree latitude and longitude for the city of Natick, MA USA, and Boston, MA USA. For simplicity, set the altitude for both locations to zero.

```
NatickLLA = [42.27752809999999, -71.34680909999997, 0];
BostonLLA = [42.3600825, -71.05888010000001, 0];
```

Define a motion that can take a platform from Natick to Boston in 20 minutes. Set the origin of the local NED coordinate system as Natick. Create a waypointTrajectory object to output the trajectory 10 samples at a time.

```
fs = 1;
duration = 60*20;
bearing = 68; % degrees
distance = 25.39e3; % meters
distanceEast = distance*sind(bearing);
distanceNorth = distance*cosd(bearing);
NatickNED = [0,0,0];
BostonNED = [distanceNorth,distanceEast,0];
```

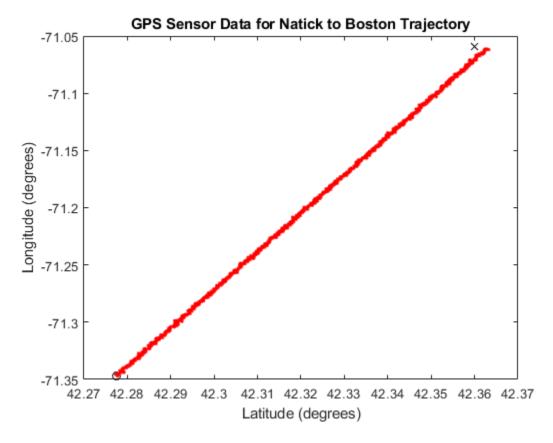
```
trajectory = waypointTrajectory( ...
   'Waypoints', [NatickNED;BostonNED], ...
   'TimeOfArrival',[0;duration], ...
   'SamplesPerFrame',10, ...
   'SampleRate',fs);
```

Create a gpsSensor object to model receiving GPS data for the platform. Set the HorizontalPositionalAccuracy to 25 and the DecayFactor to 0.25 to emphasize the noise. Set the ReferenceLocation to the Natick coordinates in LLA.

```
GPS = gpsSensor( ...
    'HorizontalPositionAccuracy',25, ...
    'DecayFactor',0.25, ...
    'SampleRate',fs, ...
    'ReferenceLocation',NatickLLA);
```

Open a figure and plot the position of Natick and Boston in LLA. Ignore altitude for simplicity.

In a loop, call the <code>gpsSensor</code> object with the ground-truth trajectory to simulate the received GPS data. Plot the ground-truth trajectory and the model of received GPS data.



As a best practice, release System objects when complete.

release(GPS)
release(trajectory)

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

Usage notes and limitations:

See "System Objects in MATLAB Code Generation" (MATLAB Coder).

See Also

Objects

imuSensor|insSensor

Introduced in R2019b

gyroparams

Gyroscope sensor parameters

Description

The gyroparams class creates a gyroscope sensor parameters object. You can use this object to model a gyroscope when simulating an IMU with imuSensor.

Creation

Syntax

```
params = gyroparams
params = gyroparams(Name, Value)
```

Description

params = gyroparams returns an ideal gyroscope sensor parameters object with default values.

params = gyroparams(Name, Value) configures gyroparams object properties using one or more Name, Value pair arguments. Name is a property name and Value is the corresponding value. Name must appear inside single quotes (''). You can specify several name-value pair arguments in any order as Name1, Value1,..., NameN, ValueN. Any unspecified properties take default values.

Properties

MeasurementRange — Maximum sensor reading (rad/s)

Inf (default) | real positive scalar

Maximum sensor reading in rad/s, specified as a real positive scalar.

Data Types: single | double

Resolution — Resolution of sensor measurements ((rad/s)/LSB)

0 (default) | real nonnegative scalar

Resolution of sensor measurements in (rad/s)/LSB, specified as a real nonnegative scalar

Data Types: single | double

ConstantBias — Constant sensor offset bias (rad/s)

```
[0 0 0] (default) | real scalar | real 3-element row vector
```

Constant sensor offset bias in rad/s, specified as a real scalar or 3-element row vector. Any scalar input is converted into a real 3-element row vector where each element has the input scalar value.

Data Types: single | double

AxesMisalignment — Sensor axes skew (%)

[0 0 0] (default) | real scalar in the range [0,100] | real 3-element row vector in the range [0,100]

Sensor axes skew in %, specified as a real scalar or 3-element row vector with values ranging from 0 to 100. Any scalar input is converted into a real 3-element row vector where each element has the input scalar value.

Data Types: single | double

NoiseDensity — Power spectral density of sensor noise ((rad/s)/√Hz)

[0 0 0] (default) | real scalar | real 3-element row vector

Power spectral density of sensor noise in (rad/s)/√Hz, specified as a real scalar or 3-element row vector. This property corresponds to the angle random walk (ARW). Any scalar input is converted into a real 3-element row vector where each element has the input scalar value.

Data Types: single | double

BiasInstability — Instability of the bias offset (rad/s)

[0 0 0] (default) | real scalar | real 3-element row vector

Instability of the bias offset in rad/s, specified as a real scalar or 3-element row vector. Any scalar input is converted into a real 3-element row vector where each element has the input scalar value.

Data Types: single | double

RandomWalk — Integrated white noise of sensor $((rad/s)(\sqrt{Hz}))$

[0 0 0] (default) | real scalar | real 3-element row vector

Integrated white noise of sensor in $(rad/s)(\sqrt{Hz})$, specified as a real scalar or 3-element row vector. Any scalar input is converted into a real 3-element row vector where each element has the input scalar value.

Data Types: single | double

TemperatureBias — Sensor bias from temperature ((rad/s)/°C)

[0 0 0] (default) | real scalar | real 3-element row vector

Sensor bias from temperature in ((rad/s)/°C), specified as a real scalar or 3-element row vector. Any scalar input is converted into a real 3-element row vector where each element has the input scalar value.

Data Types: single | double

TemperatureScaleFactor — Scale factor error from temperature (%/°C)

[0 0 0] (default) | real scalar in the range [0,100] | real 3-element row vector in the range [0,100]

Scale factor error from temperature in (%/°C), specified as a real scalar or 3-element row vector with values ranging from 0 to 100. Any scalar input is converted into a real 3-element row vector where each element has the input scalar value.

Data Types: single | double

AccelerationBias — Sensor bias from linear acceleration (rad/s)/(m/s²)

[0 0 0] (default) | real scalar | real 3-element row vector

Sensor bias from linear acceleration in $(rad/s)/(m/s^2)$, specified as a real scalar or 3-element row vector. Any scalar input is converted into a real 3-element row vector where each element has the input scalar value.

Data Types: single | double

Examples

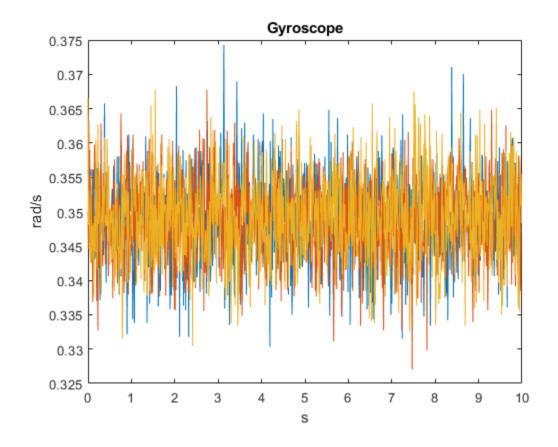
Generate Gyroscope Data from Stationary Inputs

Generate gyroscope data for an imuSensor object from stationary inputs.

```
Generate a gyroscope parameter object with a maximum sensor reading of 4.363 rad/s and a resolution of 1.332e-4 (rad/s)/LSB. The constant offset bias is 0.349 rad/s. The sensor has a power spectral density of 8.727e-4 \frac{\text{rad/s}}{\text{Hz}}. The bias from temperature is 0.349 \frac{\text{rad/s}}{\text{c}}. The bias from temperature is 0.349 \frac{\text{rad/s}}{\text{c}}. The sensor axes are skewed by 2%. The sensor bias from linear acceleration is 0.178e-3 (rad/s)/(m/s²) params = gyroparams('MeasurementRange', 4.363, 'Resolution', 1.332e-04, 'ConstantBias', 0.349, 'NoiseDelta's approach size of 100 Hz speed out even 1000 samples. Create the impresence object using the
```

Use a sample rate of 100 Hz spaced out over 1000 samples. Create the imuSensor object using the gyroscope parameter object.

```
Fs = 100;
numSamples = 1000;
t = 0:1/Fs:(numSamples-1)/Fs;
imu = imuSensor('accel-gyro','SampleRate', Fs, 'Gyroscope', params);
Generate gyroscope data from the imuSensor object.
orient = quaternion.ones(numSamples, 1);
acc = zeros(numSamples, 3);
angvel = zeros(numSamples, 3);
[~, gyroData] = imu(acc, angvel, orient);
Plot the resultant gyroscope data.
plot(t, gyroData)
title('Gyroscope')
xlabel('s')
ylabel('rad/s')
```



Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder $^{\text{\tiny TM}}$.

See Also

accelparams | imuSensor | magparams

Introduced in R2018b

imufilter

Orientation from accelerometer and gyroscope readings

Description

The imufilter System object fuses accelerometer and gyroscope sensor data to estimate device orientation.

To estimate device orientation:

- 1 Create the imufilter object and set its properties.
- **2** Call the object with arguments, as if it were a function.

To learn more about how System objects work, see What Are System Objects?.

Creation

Syntax

```
FUSE = imufilter
FUSE = imufilter('ReferenceFrame',RF)
FUSE = imufilter(____,Name,Value)
```

Description

FUSE = imufilter returns an indirect Kalman filter System object, FUSE, for fusion of accelerometer and gyroscope data to estimate device orientation. The filter uses a nine-element state vector to track error in the orientation estimate, the gyroscope bias estimate, and the linear acceleration estimate.

FUSE = imufilter('ReferenceFrame', RF) returns an imufilter filter System object that fuses accelerometer and gyroscope data to estimate device orientation relative to the reference frame RF. Specify RF as 'NED' (North-East-Down) or 'ENU' (East-North-Up). The default value is 'NED'.

FUSE = imufilter(____, Name, Value) sets each property Name to the specified Value. Unspecified properties have default values.

Example: FUSE = imufilter('SampleRate', 200, 'GyroscopeNoise', 1e-6) creates a System object, FUSE, with a 200 Hz sample rate and gyroscope noise set to 1e-6 radians per second squared.

Properties

Unless otherwise indicated, properties are *nontunable*, which means you cannot change their values after calling the object. Objects lock when you call them, and the release function unlocks them.

If a property is *tunable*, you can change its value at any time.

For more information on changing property values, see System Design in MATLAB Using System Objects.

SampleRate — Sample rate of input sensor data (Hz)

100 (default) | positive finite scalar

Sample rate of the input sensor data in Hz, specified as a positive finite scalar.

Tunable: No

Data Types: single | double | uint8 | uint16 | uint32 | uint64 | int8 | int16 | int32 | int64

DecimationFactor — **Decimation factor**

1 (default) | positive integer scalar

Decimation factor by which to reduce the sample rate of the input sensor data, specified as a positive integer scalar.

The number of rows of the inputs, accelReadings and gyroReadings, must be a multiple of the decimation factor.

Tunable: No.

Data Types: single | double | uint8 | uint16 | uint32 | uint64 | int8 | int16 | int32 | int64

AccelerometerNoise — Variance of accelerometer signal noise $((m/s^2)^2)$

0.00019247 (default) | positive real scalar

Variance of accelerometer signal noise in $(m/s^2)^2$, specified as a positive real scalar.

Tunable: Yes

Data Types: single | double | uint8 | uint16 | uint32 | uint64 | int8 | int16 | int32 | int64

GyroscopeNoise — Variance of gyroscope signal noise ((rad/s)²)

9.1385e-5 (default) | positive real scalar

Variance of gyroscope signal noise in (rad/s)², specified as a positive real scalar.

Tunable: Yes

Data Types: single | double | uint8 | uint16 | uint32 | uint64 | int8 | int16 | int32 | int64

GyroscopeDriftNoise — Variance of gyroscope offset drift ((rad/s)²)

3.0462e-13 (default) | positive real scalar

Variance of gyroscope offset drift in (rad/s)², specified as a positive real scalar.

Tunable: Yes

Data Types: single | double | uint8 | uint16 | uint32 | uint64 | int8 | int16 | int32 | int64

LinearAccelerationNoise — Variance of linear acceleration noise ((m/s²)²)

0.0096236 (default) | positive real scalar

Variance of linear acceleration noise in $(m/s^2)^2$, specified as a positive real scalar. Linear acceleration is modeled as a lowpass filtered white noise process.

Tunable: Yes

Data Types: single | double | uint8 | uint16 | uint32 | uint64 | int8 | int16 | int32 | int64

LinearAcclerationDecayFactor — Decay factor for linear acceleration drift

0.5 (default) | scalar in the range [0,1]

Decay factor for linear acceleration drift, specified as a scalar in the range [0,1]. If linear acceleration is changing quickly, set LinearAccelerationDecayFactor to a lower value. If linear acceleration changes slowly, set LinearAccelerationDecayFactor to a higher value. Linear acceleration drift is modeled as a lowpass-filtered white noise process.

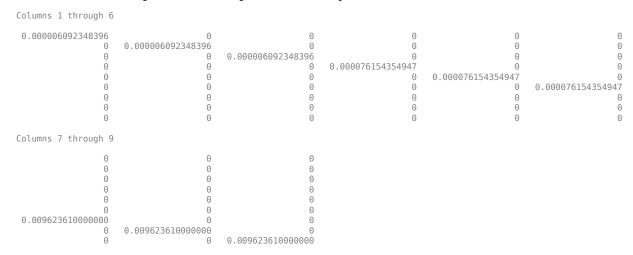
Tunable: Yes

Data Types: single | double | uint8 | uint16 | uint32 | uint64 | int8 | int16 | int32 | int64

InitialProcessNoise — Covariance matrix for process noise

9-by-9 matrix

Covariance matrix for process noise, specified as a 9-by-9 matrix. The default is:



The initial process covariance matrix accounts for the error in the process model.

Data Types: single | double | uint8 | uint16 | uint32 | uint64 | int8 | int16 | int32 | int64

OrientationFormat — Output orientation format

'quaternion' (default) | 'Rotation matrix'

Output orientation format, specified as 'quaternion' or 'Rotation matrix'. The size of the output depends on the input size, N, and the output orientation format:

- 'quaternion' -- Output is an N-by-1 quaternion.
- 'Rotation matrix' -- Output is a 3-by-3-by-N rotation matrix.

Data Types: char | string

Usage

Syntax

[orientation,angularVelocity] = FUSE(accelReadings,gyroReadings)

Description

[orientation, angular Velocity] = FUSE(accelReadings, gyroReadings) fuses accelerometer and gyroscope readings to compute orientation and angular velocity measurements. The algorithm assumes that the device is stationary before the first call.

Input Arguments

accelReadings - Accelerometer readings in sensor body coordinate system (m/s²)

N-by-3 matrix

Accelerometer readings in the sensor body coordinate system in m/s^2 , specified as an N-by-3 matrix. N is the number of samples, and the three columns of accelReadings represent the $[x\ y\ z]$ measurements. Accelerometer readings are assumed to correspond to the sample rate specified by the SampleRate property.

Data Types: single | double

gyroReadings — Gyroscope readings in sensor body coordinate system (rad/s)

N-by-3 matrix

Gyroscope readings in the sensor body coordinate system in rad/s, specified as an N-by-3 matrix. N is the number of samples, and the three columns of <code>gyroReadings</code> represent the $[x\ y\ z]$ measurements. Gyroscope readings are assumed to correspond to the sample rate specified by the SampleRate property.

Data Types: single | double

Output Arguments

orientation — Orientation that rotates quantities from global coordinate system to sensor body coordinate system

M-by-1 vector of guaternions (default) | 3-by-3-by-*M* array

Orientation that can rotate quantities from a global coordinate system to a body coordinate system, returned as quaternions or an array. The size and type of orientation depends on whether the OrienationFormat property is set to 'quaternion' or 'Rotation matrix':

- 'quaternion' -- The output is an *M*-by-1 vector of quaternions, with the same underlying data type as the inputs.
- 'Rotation matrix' -- The output is a 3-by-3-by-M array of rotation matrices the same data type as the inputs.

The number of input samples, N, and the DecimationFactor property determine M.

You can use orientation in a rotateframe function to rotate quantities from a global coordinate system to a sensor body coordinate system.

Data Types: quaternion | single | double

angular Velocity — Angular velocity in sensor body coordinate system (rad/s)

M-by-3 array (default)

Angular velocity with gyroscope bias removed in the sensor body coordinate system in rad/s, returned as an M-by-3 array. The number of input samples, N, and the DecimationFactor property determine M.

Data Types: single | double

Object Functions

To use an object function, specify the System object as the first input argument. For example, to release system resources of a System object named obj, use this syntax:

release(obi)

Specific to imufilter

tune Tune imufilter parameters to reduce estimation error

Common to All System Objects

step Run System object algorithm

release Release resources and allow changes to System object property values and input

characteristics

reset Reset internal states of System object

Examples

Estimate Orientation from IMU data

Load the rpy_9axis file, which contains recorded accelerometer, gyroscope, and magnetometer sensor data from a device oscillating in pitch (around y-axis), then yaw (around z-axis), and then roll (around x-axis). The file also contains the sample rate of the recording.

```
load 'rpy_9axis.mat' sensorData Fs
accelerometerReadings = sensorData.Acceleration;
gyroscopeReadings = sensorData.AngularVelocity;
```

Create an imufilter System object[™] with sample rate set to the sample rate of the sensor data. Specify a decimation factor of two to reduce the computational cost of the algorithm.

```
decim = 2;
fuse = imufilter('SampleRate',Fs,'DecimationFactor',decim);
```

Pass the accelerometer readings and gyroscope readings to the imufilter object, fuse, to output an estimate of the sensor body orientation over time. By default, the orientation is output as a vector of quaternions.

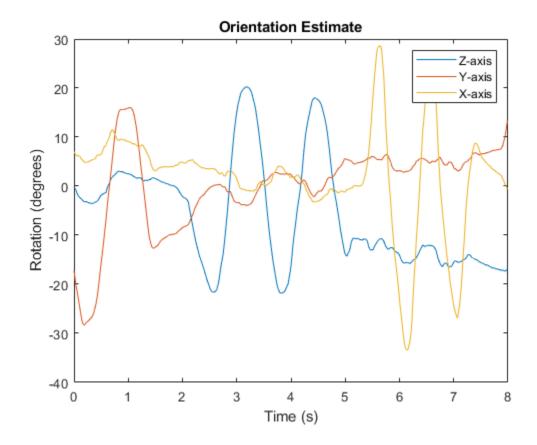
```
q = fuse(accelerometerReadings,gyroscopeReadings);
```

Orientation is defined by the angular displacement required to rotate a parent coordinate system to a child coordinate system. Plot the orientation in Euler angles in degrees over time.

imufilter fusion correctly estimates the change in orientation from an assumed north-facing initial orientation. However, the device's x-axis was pointing southward when recorded. To correctly estimate the orientation relative to the true initial orientation or relative to NED, use ahrsfilter.

time = (0:decim:size(accelerometerReadings,1)-1)/Fs;

```
plot(time,eulerd(q,'ZYX','frame'))
title('Orientation Estimate')
legend('Z-axis', 'Y-axis', 'X-axis')
xlabel('Time (s)')
ylabel('Rotation (degrees)')
```



Model Tilt Using Gyroscope and Accelerometer Readings

Model a tilting IMU that contains an accelerometer and gyroscope using the imuSensor System object. Use ideal and realistic models to compare the results of orientation tracking using the imufilter System object.

Load a struct describing ground-truth motion and a sample rate. The motion struct describes sequential rotations:

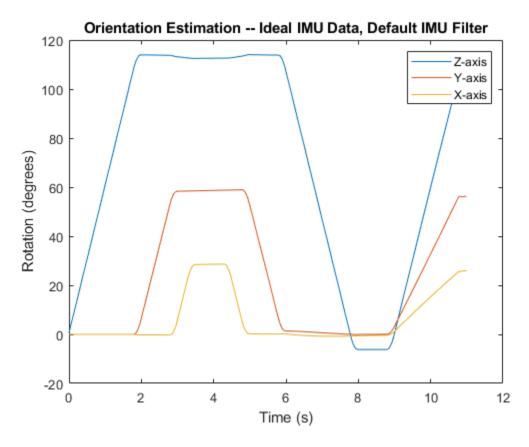
- 1 yaw: 120 degrees over two seconds
- 2 pitch: 60 degrees over one second

- **3** roll: 30 degrees over one-half second
- 4 roll: -30 degrees over one-half second
- 5 pitch: -60 degrees over one second
- 6 yaw: -120 degrees over two seconds

load y120p60r30.mat motion fs

In the last stage, the motion struct combines the 1st, 2nd, and 3rd rotations into a single-axis rotation. The acceleration, angular velocity, and orientation are defined in the local NED coordinate system.

```
accNED = motion.Acceleration;
angVelNED = motion.AngularVelocity;
orientationNED = motion.Orientation;
numSamples = size(motion.Orientation,1);
t = (0:(numSamples-1)).'/fs;
Create an ideal IMU sensor object and a default IMU filter object.
IMU = imuSensor('accel-gyro', 'SampleRate', fs);
aFilter = imufilter('SampleRate',fs);
In a loop:
   Simulate IMU output by feeding the ground-truth motion to the IMU sensor object.
   Filter the IMU output using the default IMU filter object.
orientation = zeros(numSamples,1,'quaternion');
for i = 1:numSamples
    [accelBody,gyroBody] = IMU(accNED(i,:),angVelNED(i,:),orientationNED(i,:));
    orientation(i) = aFilter(accelBody,gyroBody);
end
release(aFilter)
Plot the orientation over time.
figure(1)
plot(t,eulerd(orientation,'ZYX','frame'))
xlabel('Time (s)')
vlabel('Rotation (degrees)')
title('Orientation Estimation -- Ideal IMU Data, Default IMU Filter')
legend('Z-axis','Y-axis','X-axis')
```

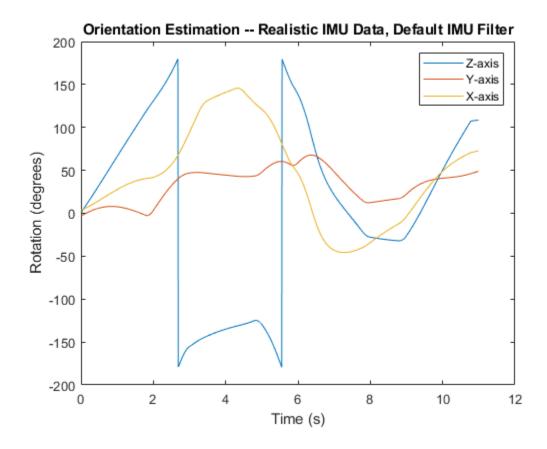


Modify properties of your imuSensor to model real-world sensors. Run the loop again and plot the orientation estimate over time.

```
IMU.Accelerometer = accelparams( ...
    'MeasurementRange',19.62, ...
    'Resolution',0.00059875, ...
    'ConstantBias',0.4905, ...
    'AxesMisalignment',2, ...
    'NoiseDensity',0.003924, ...
    'BiasInstability',0, ...
    'TemperatureBias', [0.34335 0.34335 0.5886], ...
    'TemperatureScaleFactor', 0.02);
IMU.Gyroscope = gyroparams( ...
    'MeasurementRange',4.3633, ...
    'Resolution',0.00013323, ...
    'AxesMisalignment',2, ...
    'NoiseDensity',8.7266e-05, ...
    'TemperatureBias',0.34907, ...
    'TemperatureScaleFactor', 0.02, ...
    'AccelerationBias',0.00017809, ...
    'ConstantBias',[0.3491,0.5,0]);
orientationDefault = zeros(numSamples,1,'quaternion');
for i = 1:numSamples
    [accelBody,gyroBody] = IMU(accNED(i,:),angVelNED(i,:),orientationNED(i,:));
```

```
orientationDefault(i) = aFilter(accelBody,gyroBody);
end
release(aFilter)

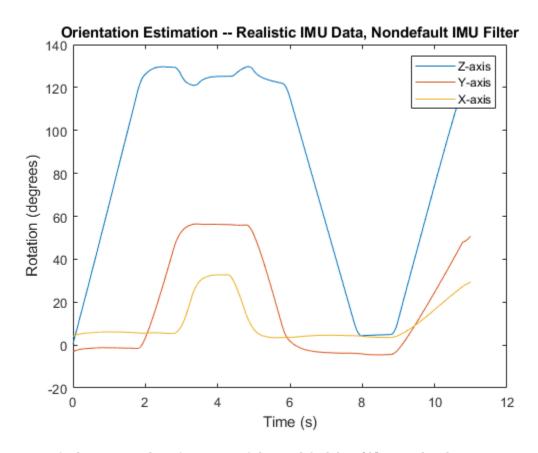
figure(2)
plot(t,eulerd(orientationDefault,'ZYX','frame'))
xlabel('Time (s)')
ylabel('Rotation (degrees)')
title('Orientation Estimation -- Realistic IMU Data, Default IMU Filter')
legend('Z-axis','Y-axis','X-axis')
```



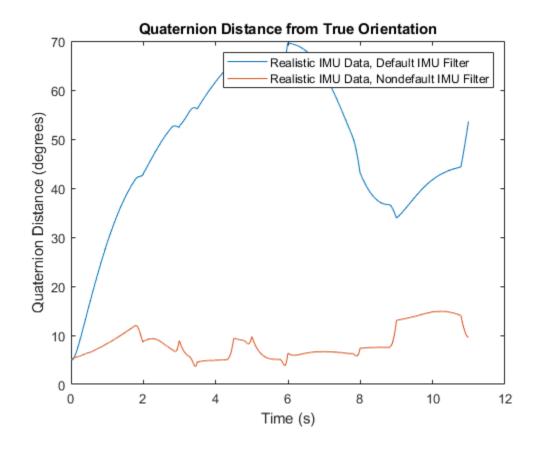
The ability of the imufilter to track the ground-truth data is significantly reduced when modeling a realistic IMU. To improve performance, modify properties of your imufilter object. These values were determined empirically. Run the loop again and plot the orientation estimate over time.

```
end
release(aFilter)

figure(3)
plot(t,eulerd(orientationNondefault,'ZYX','frame'))
xlabel('Time (s)')
ylabel('Rotation (degrees)')
title('Orientation Estimation -- Realistic IMU Data, Nondefault IMU Filter')
legend('Z-axis','Y-axis','X-axis')
```



To quantify the improved performance of the modified imufilter, plot the quaternion distance between the ground-truth motion and the orientation as returned by the imufilter with default and nondefault properties.



Remove Bias from Angular Velocity Measurement

This example shows how to remove gyroscope bias from an IMU using imufilter.

Use kinematicTrajectory to create a trajectory with two parts. The first part has a constant angular velocity about the y- and z-axes. The second part has a varying angular velocity in all three axes.

```
duration = 60*8;
fs = 20;
numSamples = duration * fs;
rng('default') % Seed the RNG to reproduce noisy sensor measurements.

initialAngVel = [0,0.5,0.25];
finalAngVel = [-0.2,0.6,0.5];
constantAngVel = repmat(initialAngVel,floor(numSamples/2),1);
varyingAngVel = [linspace(initialAngVel(1), finalAngVel(1), ceil(numSamples/2)).', ...
    linspace(initialAngVel(2), finalAngVel(2), ceil(numSamples/2)).', ...
    linspace(initialAngVel(3), finalAngVel(3), ceil(numSamples/2)).'];

angVelBody = [constantAngVel; varyingAngVel];
accBody = zeros(numSamples,3);

traj = kinematicTrajectory('SampleRate',fs);
[~,qNED,~,accNED,angVelNED] = traj(accBody,angVelBody);
```

Create an imuSensor System objectTM, IMU, with a nonideal gyroscope. Call IMU with the ground-truth acceleration, angular velocity, and orientation.

```
IMU = imuSensor('accel-gyro', ...
    'Gyroscope',gyroparams('RandomWalk',0.003,'ConstantBias',0.3), ...
    'SampleRate',fs);
```

[accelReadings, gyroReadingsBody] = IMU(accNED,angVelNED,gNED);

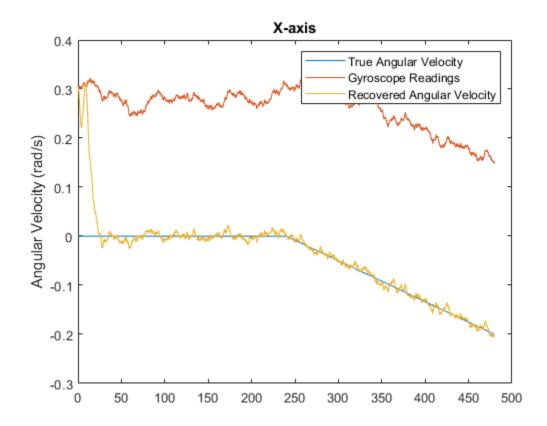
Create an imufilter System object, fuse. Call fuse with the modeled accelerometer readings and gyroscope readings.

```
fuse = imufilter('SampleRate',fs, 'GyroscopeDriftNoise', 1e-6);
[~,angVelBodyRecovered] = fuse(accelReadings,gyroReadingsBody);
```

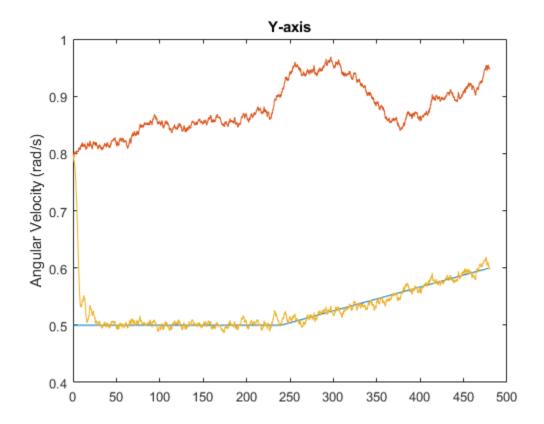
Plot the ground-truth angular velocity, the gyroscope readings, and the recovered angular velocity for each axis.

The angular velocity returned from the imufilter compensates for the effect of the gyroscope bias over time and converges to the true angular velocity.

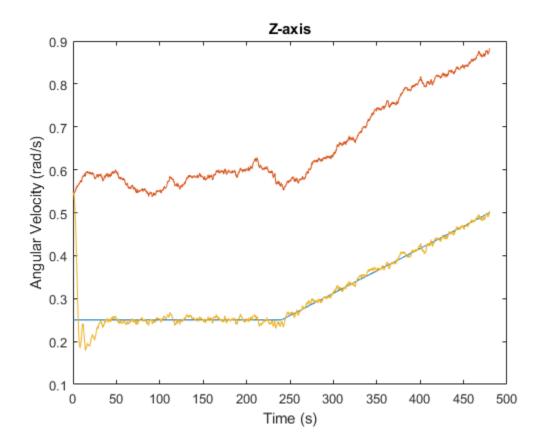
```
time = (0:numSamples-1)'/fs;
figure(1)
plot(time,angVelBody(:,1), ...
    time,gyroReadingsBody(:,1), ...
    time,angVelBodyRecovered(:,1))
title('X-axis')
legend('True Angular Velocity', ...
    'Gyroscope Readings', ...
    'Recovered Angular Velocity')
ylabel('Angular Velocity (rad/s)')
```



```
figure(2)
plot(time,angVelBody(:,2), ...
    time,gyroReadingsBody(:,2), ...
    time,angVelBodyRecovered(:,2))
title('Y-axis')
ylabel('Angular Velocity (rad/s)')
```



```
figure(3)
plot(time,angVelBody(:,3), ...
    time,gyroReadingsBody(:,3), ...
    time,angVelBodyRecovered(:,3))
title('Z-axis')
ylabel('Angular Velocity (rad/s)')
xlabel('Time (s)')
```



Algorithms

Note: The following algorithm only applies to an NED reference frame.

The imufilter uses the six-axis Kalman filter structure described in [1]. The algorithm attempts to track the errors in orientation, gyroscope offset, and linear acceleration to output the final orientation and angular velocity. Instead of tracking the orientation directly, the indirect Kalman filter models the error process, x, with a recursive update:

$$x_k = \begin{bmatrix} \theta_k \\ b_k \\ a_k \end{bmatrix} = F_k \begin{bmatrix} \theta_{k-1} \\ b_{k-1} \\ a_{k-1} \end{bmatrix} + w_k$$

where x_k is a 9-by-1 vector consisting of:

- θ_k -- 3-by-1 orientation error vector, in degrees, at time k
- b_k -- 3-by-1 gyroscope zero angular rate bias vector, in deg/s, at time k
- a_k -- 3-by-1 acceleration error vector measured in the sensor frame, in g, at time k
- w_k -- 9-by-1 additive noise vector
- F_k -- state transition model

Because x_k is defined as the error process, the *a priori* estimate is always zero, and therefore the state transition model, F_k , is zero. This insight results in the following reduction of the standard Kalman equations:

Standard Kalman equations:

$$x_{k}^{-} = F_{k}x_{k-1}^{+}$$

$$P_{k}^{-} = F_{k}P_{k-1}^{+}F_{k}^{T} + Q_{k}$$

$$y_{k} = z_{k} - H_{k}x_{k}^{-}$$

$$S_{k} = R_{k} + H_{k}P_{k}^{-}H_{k}^{T}$$

$$K_{k} = P_{k}^{-}H_{k}^{T}(S_{k})^{-1}$$

$$x_{k}^{+} = x_{k}^{-} + K_{k}y_{k}$$

$$P_{k}^{+} = P_{k}^{-} - K_{k}H_{k}P_{k}^{-}$$

Kalman equations used in this algorithm:

$$x_{k}^{-} = 0$$

$$P_{k}^{-} = Q_{k}$$

$$y_{k} = z_{k}$$

$$S_{k} = R_{k} + H_{k}P_{k}^{-}H_{k}^{T}$$

$$K_{k} = P_{k}^{-}H_{k}^{T}(S_{k})^{-1}$$

$$x_{k}^{+} = K_{k}y_{k}$$

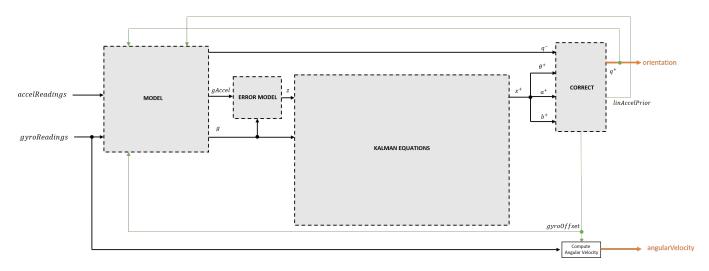
$$P_{k}^{+} = P_{k}^{-} - K_{k}H_{k}P_{k}^{-}$$

where

- x_k^- -- predicted (a priori) state estimate; the error process
- P_k^- --- predicted (a priori) estimate covariance
- y_k -- innovation
- S_k -- innovation covariance
- K_k -- Kalman gain
- x_k^+ -- updated (a posteriori) state estimate
- P_k^+ -- updated (a posteriori) estimate covariance

k represents the iteration, the superscript $^+$ represents an a posteriori estimate, and the superscript $^-$ represents an a priori estimate.

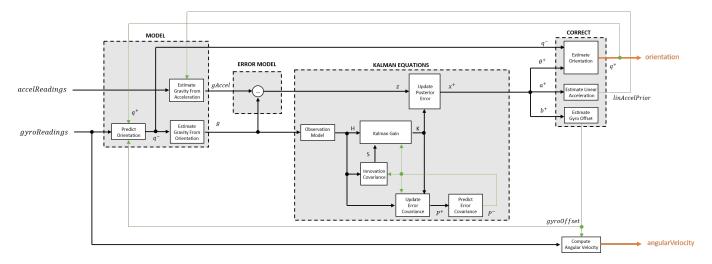
The graphic and following steps describe a single frame-based iteration through the algorithm.



Before the first iteration, the accelReadings and gyroReadings inputs are chunked into 1-by-3 frames and DecimationFactor-by-3 frames, respectively. The algorithm uses the most current accelerometer readings corresponding to the chunk of gyroscope readings.

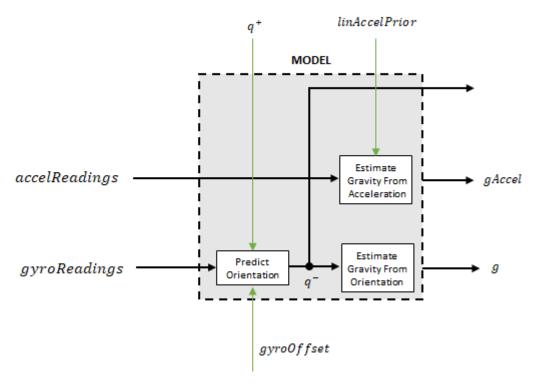
Detailed Overview

Step through the algorithm for an explanation of each stage of the detailed overview.



Model

The algorithm models acceleration and angular change as linear processes.



Predict Orientation

The orientation for the current frame is predicted by first estimating the angular change from the previous frame:

$$\Delta \varphi_{N \times 3} = \frac{(gyroReadings_{N \times 3} - gyroOffset_{1 \times 3})}{fs}$$

where N is the decimation factor specified by the <code>DecimationFactor</code> property, and fs is the sample rate specified by the <code>SampleRate</code> property.

The angular change is converted into quaternions using the rotvec quaternion construction syntax:

$$\Delta Q_{N \times 1} = \text{quaternion}(\Delta \varphi_{N \times 3}, 'rotvec')$$

The previous orientation estimate is updated by rotating it by ΔQ :

$$q_{1\times 1}^{-} = \left(q_{1\times 1}^{+}\right) \left(\prod_{n=1}^{N} \Delta Q_{n}\right)$$

During the first iteration, the orientation estimate, q^- , is initialized by ecompass with an assumption that the x-axis points north.

Estimate Gravity from Orientation

The gravity vector is interpreted as the third column of the quaternion, q^- , in rotation matrix form:

$$g_{1\times 3} = (rPrior(:,3))^T$$

See ecompass for an explanation of why the third column of rPrior can be interpreted as the gravity vector.

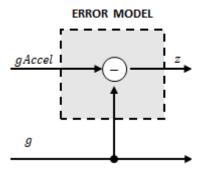
Estimate Gravity from Acceleration

A second gravity vector estimation is made by subtracting the decayed linear acceleration estimate of the previous iteration from the accelerometer readings:

$$gAccel_{1 \times 3} = accelReadings_{1 \times 3} - linAccelprior_{1 \times 3}$$

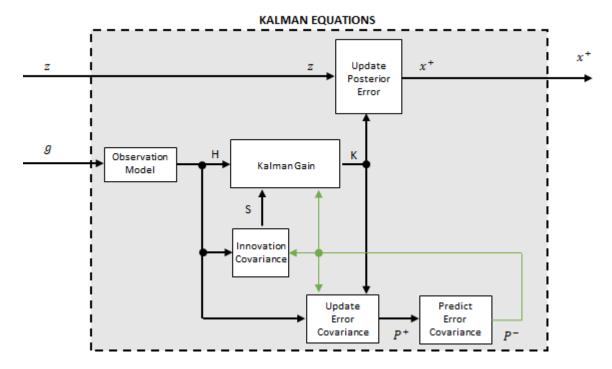
Error Model

The error model is the difference between the gravity estimate from the accelerometer readings and the gravity estimate from the gyroscope readings: z = g - gAccel.



Kalman Equations

The Kalman equations use the gravity estimate derived from the gyroscope readings, g, and the observation of the error process, z, to update the Kalman gain and intermediary covariance matrices. The Kalman gain is applied to the error signal, z, to output an a posteriori error estimate, x^+ .



Observation Model

The observation model maps the 1-by-3 observed state, q, into the 3-by-9 true state, H.

The observation model is constructed as:

$$H_{3 \times 9} = \begin{bmatrix} 0 & g_z & -g_y & 0 & -\kappa g_z & \kappa g_y & 1 & 0 & 0 \\ -g_z & 0 & g_x & \kappa g_z & 0 & -\kappa g_x & 0 & 1 & 0 \\ g_y & -g_x & 0 & -\kappa g_y & \kappa g_x & 0 & 0 & 0 & 1 \end{bmatrix}$$

where g_x , g_y , and g_z are the x-, y-, and z-elements of the gravity vector estimated from the orientation, respectively. κ is a constant determined by the SampleRate and DecimationFactor properties: $\kappa = \text{DecimationFactor/SampleRate}$.

See sections 7.3 and 7.4 of [1] for a derivation of the observation model.

Innovation Covariance

The innovation covariance is a 3-by-3 matrix used to track the variability in the measurements. The innovation covariance matrix is calculated as:

$$S_{3x3} = R_{3x3} + (H_{3x9})(P_{9x9}^{-})(H_{3x9})^{T}$$

where

- H is the observation model matrix
- P^- is the predicted (a priori) estimate of the covariance of the observation model calculated in the previous iteration

• *R* is the covariance of the observation model noise, calculated as:

$$R_{3\times 3} = (\lambda + \xi + \kappa(\beta + \eta)) \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}.$$

The following properties define the observation model noise variance:

- κ -- (DecimationFactor/SampleRate)²
- *β* -- GyroscopeDriftNoise
- η -- GyroscopeNoise
- λ -- AccelerometerNoise
- ξ -- LinearAccelerationNoise

Update Error Estimate Covariance

The error estimate covariance is a 9-by-9 matrix used to track the variability in the state.

The error estimate covariance matrix is updated as:

$$P_{q \times q}^+ = P_{q \times q}^- - (K_{9 \times 3})(H_{3 \times 9})(P_{q \times q}^-)$$

where K is the Kalman gain, H is the measurement matrix, and P^- is the error estimate covariance calculated during the previous iteration.

Predict Error Estimate Covariance

The error estimate covariance is a 9-by-9 matrix used to track the variability in the state. The *a priori* error estimate covariance, P^- , is set to the process noise covariance, Q, determined during the previous iteration. Q is calculated as a function of the *a posteriori* error estimate covariance, P^+ . When calculating Q, the cross-correlation terms are assumed to be negligible compared to the autocorrelation terms, and are set to zero:

$$Q =$$

$P^+(1) + \kappa^2 P^+(31) + \mu$	$3 + \eta$ 0	0	$-\kappa \left(P^+(31) + \beta\right)$	0
0	$P^{+}(11) + \kappa^{2}P^{+}(41) + \beta + \eta$	0	0	$-\kappa(P^{+}(41) +$
0	0	$P^{+}(21) + \kappa^{2}P^{+}(51) + \beta + \eta$	0	0
$-\kappa (P^+(31) + \beta)$	0	0	$P^+(31) + \beta$	0
0	$-\kappa(P^+(41)+\beta)$	0	0	$P^+(41) + \beta$
0	0	$-\kappa(P^+(51)+\beta)$	0	0
0	0	0	0	0
0	0	0	0	0
0	0	0	0	0

where

- P^+ -- is the updated (a posteriori) error estimate covariance
- κ --- DecimationFactor/SampleRate
- β -- GyroscopeDriftNoise
- η -- GyroscopeNoise
- ν -- LinearAcclerationDecayFactor
- ξ -- LinearAccelerationNoise

See section 10.1 of [1] for a derivation of the terms of the process error matrix.

Kalman Gain

The Kalman gain matrix is a 9-by-3 matrix used to weight the innovation. In this algorithm, the innovation is interpreted as the error process, z.

The Kalman gain matrix is constructed as:

$$K_{9 \times 3} = (P_{9 \times 9}^{-})(H_{3 \times 9})^{T}((S_{3 \times 3})^{T})^{-1}$$

where

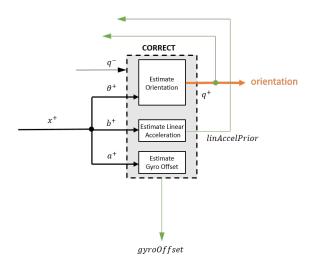
- *P* -- predicted error covariance
- *H* -- observation model
- *S* -- innovation covariance

Update a Posteriori Error

The *a posterior* error estimate is determined by combining the Kalman gain matrix with the error in the gravity vector estimations:

$$x_{9 \times 1} = (K_{9 \times 3})(z_{1 \times 3})^T$$

Correct



Estimate Orientation

The orientation estimate is updated by multiplying the previous estimation by the error:

$$q^+ = (q^-) (\theta^+)$$

Estimate Linear Acceleration

The linear acceleration estimation is updated by decaying the linear acceleration estimation from the previous iteration and subtracting the error:

$$linAccelPrior = (linAccelPrior_{k-1})\nu - b^+$$

where

• ν -- LinearAcclerationDecayFactor

Estimate Gyroscope Offset

The gyroscope offset estimation is updated by subtracting the gyroscope offset error from the gyroscope offset from the previous iteration:

$$gyroOffset = gyroOffset_{k-1} - a^+$$

Compute Angular Velocity

To estimate angular velocity, the frame of gyroReadings are averaged and the gyroscope offset computed in the previous iteration is subtracted:

$$angular Velocity_{1\times 3} = \frac{\sum gyroReadings_{N\times 3}}{N} - gyroOffset_{1\times 3}$$

where N is the decimation factor specified by the **DecimationFactor** property.

The gyroscope offset estimation is initialized to zeros for the first iteration.

References

- [1] Open Source Sensor Fusion. https://github.com/memsindustrygroup/Open-Source-Sensor-Fusion/tree/master/docs
- [2] Roetenberg, D., H.J. Luinge, C.T.M. Baten, and P.H. Veltink. "Compensation of Magnetic Disturbances Improves Inertial and Magnetic Sensing of Human Body Segment Orientation." *IEEE Transactions on Neural Systems and Rehabilitation Engineering*. Vol. 13. Issue 3, 2005, pp. 395-405.

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

Usage notes and limitations:

See "System Objects in MATLAB Code Generation" (MATLAB Coder).

See Also

ahrsfilter | ecompass | gpsSensor | imuSensor

Introduced in R2018b

tune

Tune imufilter parameters to reduce estimation error

Syntax

```
tune(filter,sensorData,groundTruth)
tune(____,config)
```

Description

tune(filter, sensorData, groundTruth) adjusts the properties of the imufilter filter object, filter, to reduce the root-mean-squared (RMS) quaternion distance error between the fused sensor data and the ground truth. The function fuses the sensor data to estimate the orientation, which is compared to the orientation in the ground truth. The function uses the property values in the filter as the initial estimate for the optimization algorithm.

tune(____, config) specifies the tuning configuration based on a tunerconfig object, config.

Examples

Tune imufilter to Optimize Orientation Estimate

Load recorded sensor data and ground truth data.

```
ld = load('imufilterTuneData.mat');
qTrue = ld.groundTruth.Orientation; % true orientation
```

Create an imufilter object and fuse the filter with the sensor data.

```
fuse = imufilter;
qEstUntuned = fuse(ld.sensorData.Accelerometer, ...
ld.sensorData.Gyroscope);
```

Create a tunerconfig object and tune the imufilter to improve the orientation estimate.

```
cfg = tunerconfig('imufilter');
tune(fuse, ld.sensorData, ld.groundTruth, cfg);
```

Iteration	Parameter	Metric
1	AccelerometerNoise	0.1149
1		
1	GyroscopeNoise	0.1146
1	GyroscopeDriftNoise	0.1146
1	LinearAccelerationNoise	0.1122
1	LinearAccelerationDecayFactor	0.1103
2	AccelerometerNoise	0.1102
2	GyroscopeNoise	0.1098
2	GyroscopeDriftNoise	0.1098
2	LinearAccelerationNoise	0.1070
2	LinearAccelerationDecayFactor	0.1053
3	AccelerometerNoise	0.1053

		0 1010
3	GyroscopeNoise	0.1048
3	GyroscopeDriftNoise	0.1048
3	LinearAccelerationNoise	0.1016
3		
	LinearAccelerationDecayFactor	0.1002
4	AccelerometerNoise	0.1001
4	GyroscopeNoise	0.0996
4	GyroscopeDriftNoise	0.0996
4	LinearAccelerationNoise	0.0962
4		0.0950
	LinearAccelerationDecayFactor	
5	AccelerometerNoise	0.0950
5	GyroscopeNoise	0.0943
5 5 5	GyroscopeDriftNoise	0.0943
5	LinearAccelerationNoise	0.0910
5	LinearAccelerationDecayFactor	0.0901
6		
	AccelerometerNoise	0.0900
6	GyroscopeNoise	0.0893
6	GyroscopeDriftNoise	0.0893
6	LinearAccelerationNoise	0.0862
6	LinearAccelerationDecayFactor	0.0855
7	AccelerometerNoise	0.0855
7	GyroscopeNoise	0.0848
7	GyroscopeDriftNoise	0.0848
7	LinearAccelerationNoise	0.0822
7	LinearAccelerationDecayFactor	0.0818
8	AccelerometerNoise	0.0817
8	GyroscopeNoise	0.0811
8	GyroscopeDriftNoise	0.0811
8	LinearAccelerationNoise	0.0791
8	LinearAccelerationDecayFactor	0.0789
9	AccelerometerNoise	0.0788
9	GyroscopeNoise	0.0782
9	GyroscopeDriftNoise	0.0782
9	LinearAccelerationNoise	0.0769
9	LinearAccelerationDecayFactor	0.0768
10	AccelerometerNoise	0.0768
10	GyroscopeNoise	0.0762
10	GyroscopeDriftNoise	0.0762
10	LinearAccelerationNoise	0.0754
10	LinearAccelerationDecayFactor	0.0753
11	AccelerometerNoise	0.0753
11	GyroscopeNoise	0.0747
11	GyroscopeDriftNoise	0.0747
11	LinearAccelerationNoise	0.0741
11		0.0741
	LinearAccelerationDecayFactor	
12	AccelerometerNoise	0.0740
12	GyroscopeNoise	0.0734
12	GyroscopeDriftNoise	0.0734
12	LinearAccelerationNoise	0.0728
12	LinearAccelerationDecayFactor	0.0728
13	AccelerometerNoise	0.0728
13	GyroscopeNoise	0.0721
13	GyroscopeDriftNoise	0.0721
13	LinearAccelerationNoise	0.0715
13	LinearAccelerationDecayFactor	0.0715
14	AccelerometerNoise	0.0715
14	GyroscopeNoise	0.0706
14	GyroscopeDriftNoise	0.0706
14	LinearAccelerationNoise	0.0700
		3.0,00

```
14
             LinearAccelerationDecayFactor
                                                0.0700
15
             AccelerometerNoise
                                                0.0700
15
             GyroscopeNoise
                                                0.0690
15
             GyroscopeDriftNoise
                                                0.0690
15
             LinearAccelerationNoise
                                                0.0684
15
                                                0.0684
             LinearAccelerationDecayFactor
16
             AccelerometerNoise
                                                0.0684
16
             GyroscopeNoise
                                                0.0672
16
             GyroscopeDriftNoise
                                                0.0672
16
             LinearAccelerationNoise
                                                0.0668
             LinearAccelerationDecayFactor
                                                0.0667
16
17
             AccelerometerNoise
                                                0.0667
17
             GyroscopeNoise
                                                0.0655
17
                                                0.0655
             GyroscopeDriftNoise
17
             LinearAccelerationNoise
                                                0.0654
17
             LinearAccelerationDecayFactor
                                                0.0654
18
                                                0.0654
             AccelerometerNoise
18
             GyroscopeNoise
                                                0.0641
18
             GyroscopeDriftNoise
                                                0.0641
18
             LinearAccelerationNoise
                                                0.0640
18
             LinearAccelerationDecayFactor
                                                0.0639
19
             AccelerometerNoise
                                                0.0639
19
             GyroscopeNoise
                                                0.0627
19
             GyroscopeDriftNoise
                                                0.0627
19
             LinearAccelerationNoise
                                                0.0627
19
             LinearAccelerationDecayFactor
                                                0.0624
20
                                                0.0624
             AccelerometerNoise
20
                                                0.0614
             GyroscopeNoise
20
             GyroscopeDriftNoise
                                                0.0614
20
             LinearAccelerationNoise
                                                0.0613
20
             LinearAccelerationDecayFactor
                                                0.0613
```

Fuse the sensor data again using the tuned filter.

```
qEstTuned = fuse(ld.sensorData.Accelerometer, ...
ld.sensorData.Gyroscope);
```

Compare the tuned and untuned filter RMS error performances.

```
dUntuned = rad2deg(dist(qEstUntuned, qTrue));
dTuned = rad2deg(dist(qEstTuned, qTrue));
rmsUntuned = sqrt(mean(dUntuned.^2))

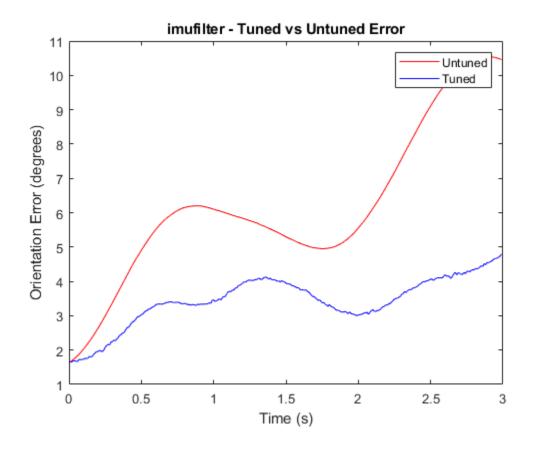
rmsUntuned = 6.5864

rmsTuned = sqrt(mean(dTuned.^2))

rmsTuned = 3.5098

Visualize the results.

N = numel(dUntuned);
t = (0:N-1)./ fuse.SampleRate;
plot(t, dUntuned, 'r', t, dTuned, 'b');
legend('Untuned', 'Tuned');
title('imufilter - Tuned vs Untuned Error')
xlabel('Time (s)');
ylabel('Orientation Error (degrees)');
```



Input Arguments

filter — Filter object

imufilter object

Filter object, specified as an imufilter object.

sensorData — Sensor data

table

Sensor data, specified as a table. In each row, the sensor data is specified as:

- Accelerometer Accelerometer data, specified as a 1-by-3 vector of scalars in m²/s.
- Gyroscope Gyroscope data, specified as a 1-by-3 vector of scalars in rad/s.

If you set the Cost property of the tuner configuration input, config, to Custom, then you can use other data types for the sensorData input based on your choice.

groundTruth — Ground truth data

timetable

Ground truth data, specified as a table. The table has only one column of Orientation data. In each row, the orientation is specified as a quaternion object or a 3-by-3 rotation matrix.

The function processes each row of the sensorData and groundTruth tables sequentially to calculate the state estimate and RMS error from the ground truth. Each row of the sensorData and the groundTruth tables must correspond to each other.

If you set the Cost property of the tuner configuration input, config, to Custom, then you can use other data types for the groundTruth input based on your choice.

config — Tuner configuration

tunerconfig object

Tuner configuration, specified as a tunerconfig object.

References

[1] Abbeel, P., Coates, A., Montemerlo, M., Ng, A.Y. and Thrun, S. Discriminative Training of Kalman Filters. In *Robotics: Science and systems*, Vol. 2, pp. 1, 2005.

See Also

Introduced in R2020b

imuSensor

IMU simulation model

Description

The imuSensor System object models receiving data from an inertial measurement unit (IMU).

To model an IMU:

- **1** Create the imuSensor object and set its properties.
- **2** Call the object with arguments, as if it were a function.

To learn more about how System objects work, see What Are System Objects?.

Creation

Syntax

```
IMU = imuSensor
IMU = imuSensor('accel-gyro')
IMU = imuSensor('accel-mag')
IMU = imuSensor('accel-gyro-mag')
IMU = imuSensor(____, 'ReferenceFrame', RF)
IMU = imuSensor(____, Name, Value)
```

Description

IMU = imuSensor returns a System object, IMU, that computes an inertial measurement unit reading based on an inertial input signal. IMU has an ideal accelerometer and gyroscope.

IMU = imuSensor('accel-gyro') returns an imuSensor System object with an ideal
accelerometer and gyroscope. imuSensor and imuSensor('accel-gyro') are equivalent creation
syntaxes.

 $\label{eq:imuSensor} IMU = imuSensor('accel-mag') \ returns an \ imuSensor \ System \ object \ with \ an \ ideal \ accelerometer \ and \ magnetometer.$

 ${\tt IMU = imuSensor('accel-gyro-mag') \ returns \ an \ imuSensor \ System \ object \ with \ an \ ideal \ accelerometer, \ gyroscope, \ and \ magnetometer.}$

 $\label{eq:musensor} IMU = imuSensor(\underline{\hspace{1cm}} , 'ReferenceFrame', RF) \ returns \ an \ imuSensor \ System \ object \ that \ computes \ an \ inertial \ measurement \ unit \ reading \ relative \ to \ the \ reference \ frame \ RF. \ Specify \ RF \ as 'NED' \ (North-East-Down) \ or 'ENU' \ (East-North-Up). \ The \ default \ value \ is 'NED'.$

IMU = imuSensor(____, Name, Value) sets each property Name to the specified Value.
Unspecified properties have default values. This syntax can be used in combination with any of the previous input arguments.

Properties

Unless otherwise indicated, properties are *nontunable*, which means you cannot change their values after calling the object. Objects lock when you call them, and the release function unlocks them.

If a property is *tunable*, you can change its value at any time.

For more information on changing property values, see System Design in MATLAB Using System Objects.

IMUType — Type of inertial measurement unit

```
'accel-gyro' (default) | 'accel-mag' | 'accel-gyro-mag'
```

Type of inertial measurement unit, specified as a 'accel-gyro', 'accel-mag', or 'accel-gyro-mag'.

The type of inertial measurement unit specifies which sensor readings to model:

- 'accel-gyro' -- Accelerometer and gyroscope
- 'accel-mag' -- Accelerometer and magnetometer
- 'accel-gyro-mag' -- Accelerometer, gyroscope, and magnetometer

You can specify IMUType as a value-only argument during creation or as a Name, Value pair.

Data Types: char | string

SampleRate — Sample rate of sensor (Hz)

100 (default) | positive scalar

Sample rate of the sensor model in Hz, specified as a positive scalar.

Data Types: single | double

Temperature — Temperature of IMU (°C)

25 (default) | real scalar

Operating temperature of the IMU in degrees Celsius, specified as a real scalar.

When the object calculates temperature scale factors and environmental drift noises, $25~^{\circ}\text{C}$ is used as the nominal temperature.

Tunable: Yes

Data Types: single | double

$\label{eq:magneticField} \textbf{Magnetic field vector in local navigation coordinate system (μT)}$

```
[27.5550 -2.4169 -16.0849] (default) | real scalar
```

Magnetic field vector in microtesla, specified as a three-element row vector in the local navigation coordinate system.

The default magnetic field corresponds to the magnetic field at latitude zero, longitude zero, and altitude zero.

Tunable: Yes

Data Types: single | double

Accelerometer — Accelerometer sensor parameters

accelparams object (default)

Accelerometer sensor parameters, specified by an accelparams object.

Tunable: Yes

Gyroscope — **Gyroscope** sensor parameters

gyroparams object (default)

Gyroscope sensor parameters, specified by a gyroparams object.

Tunable: Yes

Magnetometer — Magnetometer sensor parameters

magparams object (default)

Magnetometer sensor parameters, specified by a magparams object.

Tunable: Yes

RandomStream — Random number source

```
'Global stream' (default) | 'mt19937ar with seed'
```

Random number source, specified as a character vector or string:

- 'Global stream' -- Random numbers are generated using the current global random number stream.
- 'mt19937ar with seed' -- Random numbers are generated using the mt19937ar algorithm with the seed specified by the Seed property.

Data Types: char | string

Seed — Initial seed

67 (default) | nonnegative integer scalar

Initial seed of an mt19937ar random number generator algorithm, specified as a real, nonnegative integer scalar.

Dependencies

To enable this property, set RandomStream to 'mt19937ar with seed'.

Data Types: single | double | int8 | int16 | int32 | int64 | uint8 | uint16 | uint32 | uint64

Usage

Syntax

```
[accelReadings,gyroReadings] = IMU(acc,angVel)
[accelReadings,gyroReadings] = IMU(acc,angVel,orientation)

[accelReadings,magReadings] = IMU(acc,angVel)
[accelReadings,magReadings] = IMU(acc,angVel,orientation)
```

```
[accelReadings,gyroReadings,magReadings] = IMU(acc,angVel)
[accelReadings,gyroReadings,magReadings] = IMU(acc,angVel,orientation)
```

Description

[accelReadings,gyroReadings] = IMU(acc,angVel) generates accelerometer and gyroscope readings from the acceleration and angular velocity inputs.

This syntax is only valid if IMUType is set to 'accel-gyro' or 'accel-gyro-mag'.

[accelReadings,gyroReadings] = IMU(acc,angVel,orientation) generates accelerometer and gyroscope readings from the acceleration, angular velocity, and orientation inputs.

This syntax is only valid if IMUType is set to 'accel-gyro' or 'accel-gyro-mag'.

[accelReadings,magReadings] = IMU(acc,angVel) generates accelerometer and magnetometer readings from the acceleration and angular velocity inputs.

This syntax is only valid if IMUType is set to 'accel-mag'.

[accelReadings,magReadings] = IMU(acc,angVel,orientation) generates accelerometer and magnetometer readings from the acceleration, angular velocity, and orientation inputs.

This syntax is only valid if IMUType is set to 'accel-mag'.

[accelReadings,gyroReadings,magReadings] = IMU(acc,angVel) generates accelerometer, gyroscope, and magnetometer readings from the acceleration and angular velocity inputs.

This syntax is only valid if IMUType is set to 'accel-gyro-mag'.

[accelReadings,gyroReadings,magReadings] = IMU(acc,angVel,orientation) generates accelerometer, gyroscope, and magnetometer readings from the acceleration, angular velocity, and orientation inputs.

This syntax is only valid if IMUType is set to 'accel-gyro-mag'.

Input Arguments

acc — Acceleration of IMU in local navigation coordinate system (m/s2)

N-by-3 matrix

Acceleration of the IMU in the local navigation coordinate system, specified as a real, finite N-by-3 array in meters per second squared. N is the number of samples in the current frame.

Data Types: single | double

angVel — Angular velocity of IMU in local navigation coordinate system (rad/s)

N-by-3 matrix

Angular velocity of the IMU in the local navigation coordinate system, specified as a real, finite N-by-3 array in radians per second. N is the number of samples in the current frame.

Data Types: single | double

orientation — Orientation of IMU in local navigation coordinate system

N-element quaternion column vector | 3-by-3-by-*N*-element rotation matrix

Orientation of the IMU with respect to the local navigation coordinate system, specified as a quaternion N-element column vector or a 3-by-3-by-N rotation matrix. Each quaternion or rotation matrix represents a frame rotation from the local navigation coordinate system to the current IMU sensor body coordinate system. N is the number of samples in the current frame.

Data Types: single | double | quaternion

Output Arguments

accelReadings — Accelerometer measurement of IMU in sensor body coordinate system (m/s^2)

N-by-3 matrix

Accelerometer measurement of the IMU in the sensor body coordinate system, specified as a real, finite *N*-by-3 array in meters per second squared. *N* is the number of samples in the current frame.

Data Types: single | double

gyroReadings — Gyroscope measurement of IMU in sensor body coordinate system (rad/s) N-by-3 matrix

Gyroscope measurement of the IMU in the sensor body coordinate system, specified as a real, finite N-by-3 array in radians per second. N is the number of samples in the current frame.

Data Types: single | double

magReadings — Magnetometer measurement of IMU in sensor body coordinate system (μ T) N-by-3 matrix (default)

Magnetometer measurement of the IMU in the sensor body coordinate system, specified as a real, finite N-by-3 array in microtelsa. N is the number of samples in the current frame.

Data Types: single | double

Object Functions

To use an object function, specify the System object as the first input argument. For example, to release system resources of a System object named obj, use this syntax:

release(obj)

Specific to imuSensor

loadparams Load sensor parameters from JSON file

Common to All System Objects

step Run System object algorithm

release Release resources and allow changes to System object property values and input

characteristics

reset Reset internal states of System object

Examples

Create Default imuSensor System object

The imuSensor System object[™] enables you to model the data received from an inertial measurement unit consisting of a combination of gyroscope, accelerometer, and magnetometer.

Create a default imuSensor object.

The imuSensor object, IMU, contains an idealized gyroscope and accelerometer. Use dot notation to view properties of the gyroscope.

IMU.Gyroscope

```
ans =
 gyroparams with properties:
   MeasurementRange: Inf
                                 rad/s
         Resolution: 0
                                 (rad/s)/LSB
        ConstantBias: [0 0 0]
                                 rad/s
   AxesMisalignment: [0 0 0]
      NoiseDensity: [0 0 0]
                                (rad/s)/√Hz
   BiasInstability: [0 0 0]
                                rad/s
         RandomWalk: [0 0 0]
                                (rad/s)*√Hz
           TemperatureBias: [0 0 0]
                                       (rad/s)/°C
   TemperatureScaleFactor: [0 0 0]
                                       %/°C
         AccelerationBias: [0 0 0]
                                       (rad/s)/(m/s^2)
```

Sensor properties are defined by corresponding parameter objects. For example, the gyroscope model used by the imuSensor is defined by an instance of the gyroparams class. You can modify properties of the gyroscope model using dot notation. Set the gyroscope measurement range to 4.3 rad/s.

```
IMU.Gyroscope.MeasurementRange = 4.3;
```

You can also set sensor properties to preset parameter objects. Create an accelparams object to mimic specific hardware, and then set the IMU Accelerometer property to the accelparams object. Display the Accelerometer property to verify the properties are correctly set.

```
SpecSheet1 = accelparams( ...
    'MeasurementRange',19.62, ...
    'Resolution',0.00059875, ...
    'ConstantBias',0.4905, ...
    'AxesMisalignment',2, ...
```

```
'NoiseDensity', 0.003924, ...
    'BiasInstability',0, ...
    'TemperatureBias', [0.34335 0.34335 0.5886], ...
    'TemperatureScaleFactor', 0.02);
IMU.Accelerometer = SpecSheet1;
IMU.Accelerometer
 accelparams with properties:
    MeasurementRange: 19.62
                                                   m/s^2
          Resolution: 0.00059875
                                                   (m/s^2)/LSB
        ConstantBias: [0.4905 0.4905 0.4905]
                                                   \rm m/s^2
    AxesMisalignment: [2 2 2]
       NoiseDensity: [0.003924 0.003924 0.003924]
                                                         (m/s^2)/\sqrt{Hz}
    BiasInstability: [0 0 0]
                                                        m/s^2
         RandomWalk: [0 0 0]
                                                         (m/s^2)*\sqrt{Hz}
           TemperatureBias: [0.34335 0.34335 0.5886]
                                                           (m/s^2)/^{\circ}C
    TemperatureScaleFactor: [0.02 0.02 0.02]
                                                            %/°C
```

Generate Ideal IMU Data from Stationary Input

Use the imuSensor System object[™] to model receiving data from a stationary ideal IMU containing an accelerometer, gyroscope, and magnetometer.

Create an ideal IMU sensor model that contains an accelerometer, gyroscope, and magnetometer.

Define the ground-truth, underlying motion of the IMU you are modeling. The acceleration and angular velocity are defined relative to the local NED coordinate system.

```
numSamples = 1000;
acceleration = zeros(numSamples,3);
angularVelocity = zeros(numSamples,3);
```

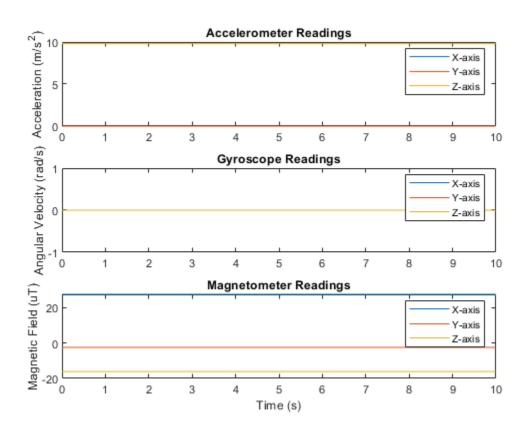
Call IMU with the ground-truth acceleration and angular velocity. The object outputs accelerometer readings, gyroscope readings, and magnetometer readings, as modeled by the properties of the

imuSensor System object. The accelerometer readings, gyroscope readings, and magnetometer readings are relative to the IMU sensor body coordinate system.

[accelReading,gyroReading,magReading] = IMU(acceleration,angularVelocity);

Plot the accelerometer readings, gyroscope readings, and magnetometer readings.

```
t = (0:(numSamples-1))/IMU.SampleRate;
subplot(3,1,1)
plot(t,accelReading)
legend('X-axis','Y-axis','Z-axis')
title('Accelerometer Readings')
ylabel('Acceleration (m/s^2)')
subplot(3,1,2)
plot(t,gyroReading)
legend('X-axis','Y-axis','Z-axis')
title('Gyroscope Readings')
ylabel('Angular Velocity (rad/s)')
subplot(3,1,3)
plot(t,magReading)
legend('X-axis','Y-axis','Z-axis')
title('Magnetometer Readings')
xlabel('Time (s)')
ylabel('Magnetic Field (uT)')
```



Orientation is not specified and the ground-truth motion is stationary, so the IMU sensor body coordinate system and the local NED coordinate system overlap for the entire simulation.

- Accelerometer readings: The *z*-axis of the sensor body corresponds to the Down-axis. The 9.8 m/s² acceleration along the *z*-axis is due to gravity.
- Gyroscope readings: The gyroscope readings are zero along each axis, as expected.
- Magnetometer readings: Because the sensor body coordinate system is aligned with the local NED coordinate system, the magnetometer readings correspond to the MagneticField property of imuSensor. The MagneticField property is defined in the local NED coordinate system.

Model Rotating Six-Axis IMU Data

Use imuSensor to model data obtained from a rotating IMU containing an ideal accelerometer and an ideal magnetometer. Use kinematicTrajectory to define the ground-truth motion. Fuse the imuSensor model output using the ecompass function to determine orientation over time.

Define the ground-truth motion for a platform that rotates 360 degrees in four seconds, and then another 360 degrees in two seconds. Use kinematicTrajectory to output the orientation, acceleration, and angular velocity in the NED coordinate system.

```
fs = 100;
firstLoopNumSamples = fs*4;
secondLoopNumSamples = fs*2;
totalNumSamples = firstLoopNumSamples + secondLoopNumSamples;

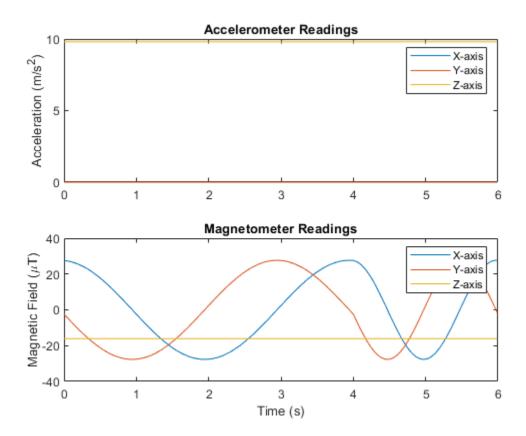
traj = kinematicTrajectory('SampleRate',fs);

accBody = zeros(totalNumSamples,3);
angVelBody = zeros(totalNumSamples,3);
angVelBody(1:firstLoopNumSamples,3) = (2*pi)/4;
angVelBody(firstLoopNumSamples+1:end,3) = (2*pi)/2;
[~,orientationNED,~,accNED,angVelNED] = traj(accBody,angVelBody);
```

Create an imuSensor object with an ideal accelerometer and an ideal magnetometer. Call IMU with the ground-truth acceleration, angular velocity, and orientation to output accelerometer readings and magnetometer readings. Plot the results.

```
IMU = imuSensor('accel-mag','SampleRate',fs);
[accelReadings,magReadings] = IMU(accNED,angVelNED,orientationNED);
figure(1)
t = (0:(totalNumSamples-1))/fs;
subplot(2,1,1)
plot(t,accelReadings)
legend('X-axis','Y-axis','Z-axis')
ylabel('Acceleration (m/s^2)')
title('Accelerometer Readings')
subplot(2,1,2)
plot(t,magReadings)
legend('X-axis','Y-axis','Z-axis')
```

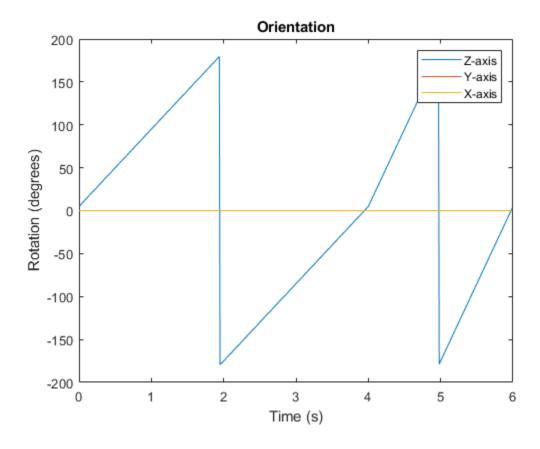
```
ylabel('Magnetic Field (\muT)')
xlabel('Time (s)')
title('Magnetometer Readings')
```



The accelerometer readings indicate that the platform has no translation. The magnetometer readings indicate that the platform is rotating around the z-axis.

Feed the accelerometer and magnetometer readings into the ecompass function to estimate the orientation over time. The ecompass function returns orientation in quaternion format. Convert orientation to Euler angles and plot the results. The orientation plot indicates that the platform rotates about the z-axis only.

```
orientation = ecompass(accelReadings,magReadings);
orientationEuler = eulerd(orientation,'ZYX','frame');
figure(2)
plot(t,orientationEuler)
legend('Z-axis','Y-axis','X-axis')
xlabel('Time (s)')
ylabel('Rotation (degrees)')
title('Orientation')
```



Model Rotating Six-Axis IMU Data with Noise

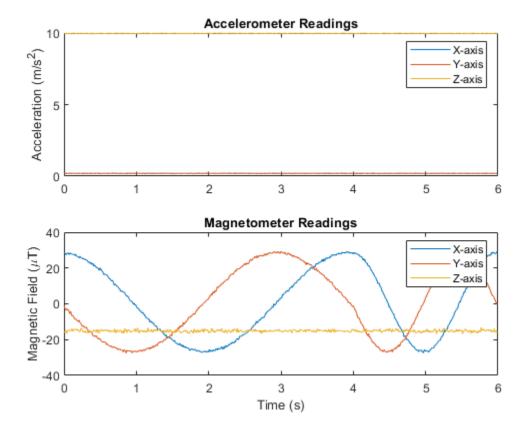
Use imuSensor to model data obtained from a rotating IMU containing a realistic accelerometer and a realistic magnetometer. Use kinematicTrajectory to define the ground-truth motion. Fuse the imuSensor model output using the ecompass function to determine orientation over time.

Define the ground-truth motion for a platform that rotates 360 degrees in four seconds, and then another 360 degrees in two seconds. Use kinematicTrajectory to output the orientation, acceleration, and angular velocity in the NED coordinate system.

```
fs = 100;
firstLoopNumSamples = fs*4;
secondLoopNumSamples = fs*2;
totalNumSamples = firstLoopNumSamples + secondLoopNumSamples;
traj = kinematicTrajectory('SampleRate',fs);
accBody = zeros(totalNumSamples,3);
angVelBody = zeros(totalNumSamples,3);
angVelBody(1:firstLoopNumSamples,3) = (2*pi)/4;
angVelBody(firstLoopNumSamples+1:end,3) = (2*pi)/2;
[~,orientationNED,~,accNED,angVelNED] = traj(accBody,angVelBody);
```

Create an imuSensor object with a realistic accelerometer and a realistic magnetometer. Call IMU with the ground-truth acceleration, angular velocity, and orientation to output accelerometer readings and magnetometer readings. Plot the results.

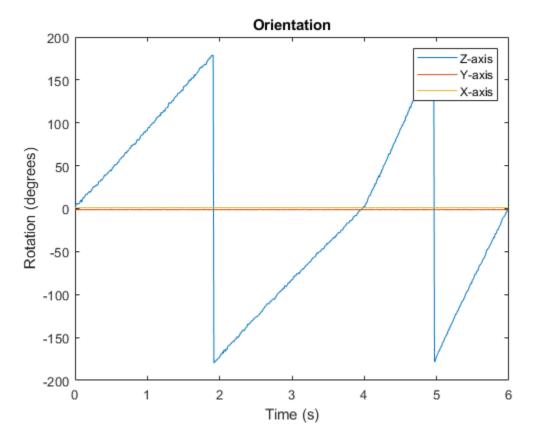
```
IMU = imuSensor('accel-mag', 'SampleRate', fs);
IMU.Accelerometer = accelparams( ...
    'MeasurementRange',19.62, ...
                                            % m/s^2
    'Resolution',0.0023936, ...
                                            % m/s^2 / LSB
    'TemperatureScaleFactor',0.008, ... % % / degree C
    'ConstantBias',0.1962, ...
                                           % m/s^2
                                        % m/s^2 / degree C
    'TemperatureBias',0.0014715, ...
    'NoiseDensity',0.0012361);
                                            % m/s^2 / Hz^(1/2)
IMU.Magnetometer = magparams( ...
    'MeasurementRange',1200, ...
                                            % uT
                                            % uT / LSB
    'Resolution',0.1, ...
    'TemperatureScaleFactor',0.1, ...
                                          % % / degree C
    'ConstantBias',1, ...
                                            % uT
    'TemperatureBias',[0.8 0.8 2.4], ... % uT / degree C
    'NoiseDensity',[0.6 0.6 0.9]/sqrt(100)); % uT / Hz^(1/2)
[accelReadings,magReadings] = IMU(accNED,angVelNED,orientationNED);
figure(1)
t = (0:(totalNumSamples-1))/fs;
subplot(2,1,1)
plot(t,accelReadings)
legend('X-axis','Y-axis','Z-axis')
ylabel('Acceleration (m/s^2)')
title('Accelerometer Readings')
subplot(2,1,2)
plot(t,magReadings)
legend('X-axis','Y-axis','Z-axis')
ylabel('Magnetic Field (\muT)')
xlabel('Time (s)')
title('Magnetometer Readings')
```



The accelerometer readings indicate that the platform has no translation. The magnetometer readings indicate that the platform is rotating around the z-axis.

Feed the accelerometer and magnetometer readings into the **ecompass** function to estimate the orientation over time. The **ecompass** function returns orientation in quaternion format. Convert orientation to Euler angles and plot the results. The orientation plot indicates that the platform rotates about the *z*-axis only.

```
orientation = ecompass(accelReadings,magReadings);
orientationEuler = eulerd(orientation,'ZYX','frame');
figure(2)
plot(t,orientationEuler)
legend('Z-axis','Y-axis','X-axis')
xlabel('Time (s)')
ylabel('Rotation (degrees)')
title('Orientation')
```



%

Model Tilt Using Gyroscope and Accelerometer Readings

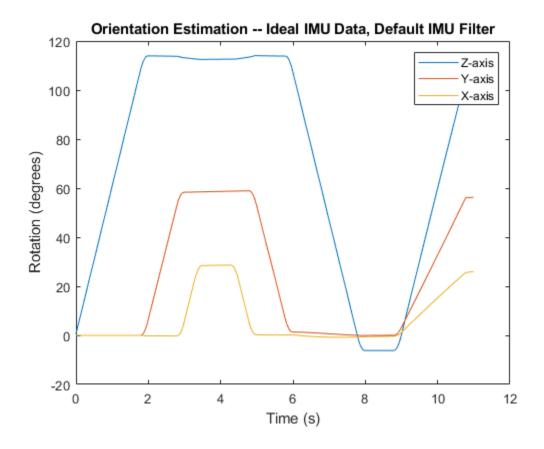
Model a tilting IMU that contains an accelerometer and gyroscope using the imuSensor System object. Use ideal and realistic models to compare the results of orientation tracking using the imufilter System object.

Load a struct describing ground-truth motion and a sample rate. The motion struct describes sequential rotations:

- **1** yaw: 120 degrees over two seconds
- 2 pitch: 60 degrees over one second
- **3** roll: 30 degrees over one-half second
- 4 roll: -30 degrees over one-half second
- 5 pitch: -60 degrees over one second
- **6** yaw: -120 degrees over two seconds

In the last stage, the motion struct combines the 1st, 2nd, and 3rd rotations into a single-axis rotation. The acceleration, angular velocity, and orientation are defined in the local NED coordinate system.

```
load y120p60r30.mat motion fs
accNED = motion.Acceleration;
angVelNED = motion.AngularVelocity;
orientationNED = motion.Orientation;
numSamples = size(motion.Orientation,1);
t = (0:(numSamples-1)).'/fs;
Create an ideal IMU sensor object and a default IMU filter object.
IMU = imuSensor('accel-gyro', 'SampleRate', fs);
aFilter = imufilter('SampleRate',fs);
In a loop:
1
   Simulate IMU output by feeding the ground-truth motion to the IMU sensor object.
2
   Filter the IMU output using the default IMU filter object.
orientation = zeros(numSamples,1,'quaternion');
for i = 1:numSamples
    [accelBody,gyroBody] = IMU(accNED(i,:),angVelNED(i,:),orientationNED(i,:));
    orientation(i) = aFilter(accelBody,gyroBody);
end
release(aFilter)
Plot the orientation over time.
figure(1)
plot(t,eulerd(orientation,'ZYX','frame'))
xlabel('Time (s)')
ylabel('Rotation (degrees)')
title('Orientation Estimation -- Ideal IMU Data, Default IMU Filter')
legend('Z-axis','Y-axis','X-axis')
```

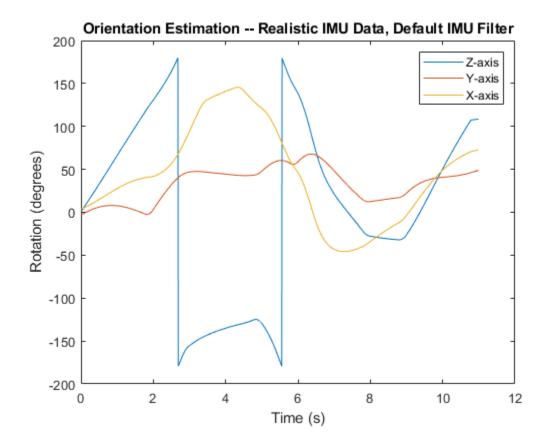


Modify properties of your imuSensor to model real-world sensors. Run the loop again and plot the orientation estimate over time.

```
IMU.Accelerometer = accelparams( ...
    'MeasurementRange',19.62, ...
    'Resolution',0.00059875, ...
    'ConstantBias',0.4905, ...
    'AxesMisalignment',2, ...
    'NoiseDensity',0.003924, ...
    'BiasInstability',0, ...
    'TemperatureBias', [0.34335 0.34335 0.5886], ...
    'TemperatureScaleFactor',0.02);
IMU.Gyroscope = gyroparams( ...
    'MeasurementRange',4.3633, ...
    'Resolution',0.00013323, ...
    'AxesMisalignment',2, ...
    'NoiseDensity',8.7266e-05, ...
    'TemperatureBias',0.34907, ...
    'TemperatureScaleFactor', 0.02, ...
    'AccelerationBias',0.00017809, ...
    'ConstantBias',[0.3491,0.5,0]);
orientationDefault = zeros(numSamples,1,'quaternion');
for i = 1:numSamples
    [accelBody,gyroBody] = IMU(accNED(i,:),angVelNED(i,:),orientationNED(i,:));
```

```
orientationDefault(i) = aFilter(accelBody,gyroBody);
end
release(aFilter)

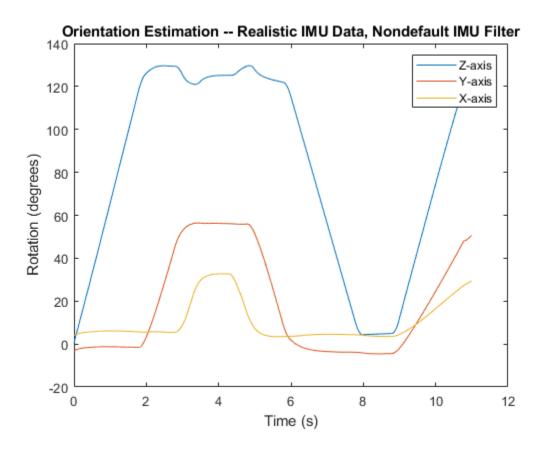
figure(2)
plot(t,eulerd(orientationDefault,'ZYX','frame'))
xlabel('Time (s)')
ylabel('Rotation (degrees)')
title('Orientation Estimation -- Realistic IMU Data, Default IMU Filter')
legend('Z-axis','Y-axis','X-axis')
```



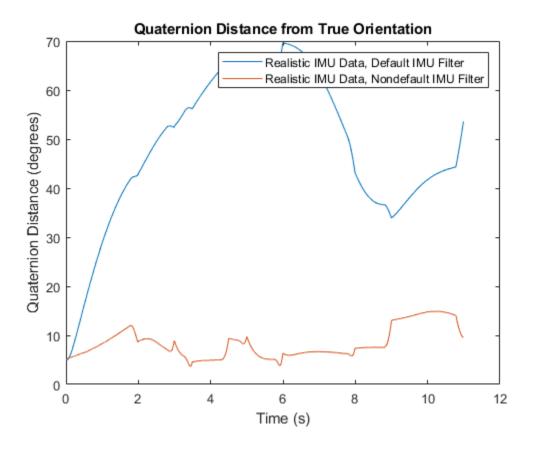
The ability of the imufilter to track the ground-truth data is significantly reduced when modeling a realistic IMU. To improve performance, modify properties of your imufilter object. These values were determined empirically. Run the loop again and plot the orientation estimate over time.

```
end
release(aFilter)

figure(3)
plot(t,eulerd(orientationNondefault,'ZYX','frame'))
xlabel('Time (s)')
ylabel('Rotation (degrees)')
title('Orientation Estimation -- Realistic IMU Data, Nondefault IMU Filter')
legend('Z-axis','Y-axis','X-axis')
```



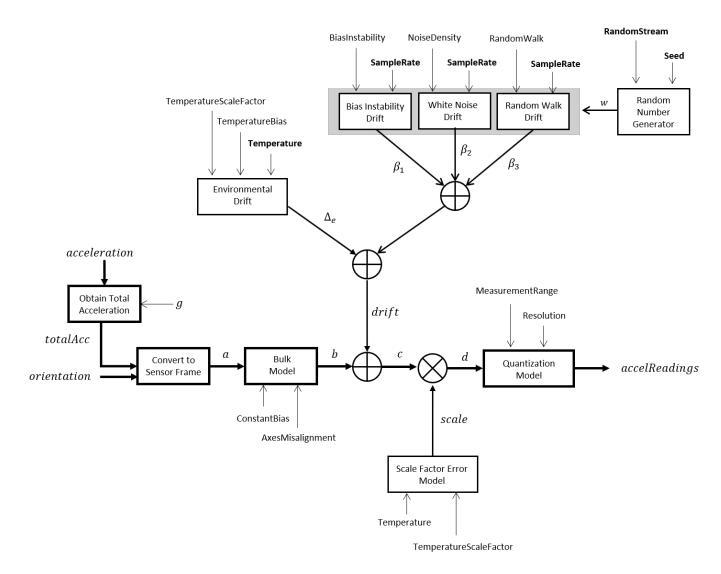
To quantify the improved performance of the modified imufilter, plot the quaternion distance between the ground-truth motion and the orientation as returned by the imufilter with default and nondefault properties.



Algorithms

Accelerometer

The accelerometer model uses the ground-truth orientation and acceleration inputs and the imuSensor and accelerams properties to model accelerometer readings.



Obtain Total Acceleration

To obtain the total acceleration (totalAcc), the acceleration is preprocessed by negating and adding the gravity constant vector ($g = [0; 0; 9.8] \text{ m/s}^2$) as:

$$totalAcc = -acceleration + g$$

Convert to Sensor Frame

Then the total acceleration is converted from the local navigation frame to the sensor frame using:

$$a = (orientation)(totalAcc)^T$$

If the orientation is input in quaternion form, it is converted to a rotation matrix before processing.

Bulk Model

The ground-truth acceleration in the sensor frame, a, passes through the bulk model, which adds axes misalignment and bias:

$$b = \begin{pmatrix} 1 & \frac{\alpha_2}{100} & \frac{\alpha_3}{100} \\ \frac{\alpha_1}{100} & 1 & \frac{\alpha_3}{100} \\ \frac{\alpha_1}{100} & \frac{\alpha_2}{100} & 1 \end{pmatrix} + \text{ConstantBias}$$

where ConstantBias is a property of accelparams, and α_1 , α_2 , and α_3 are given by the first, second, and third elements of the AxesMisalignment property of accelparams.

Bias Instability Drift

The bias instability drift is modeled as white noise biased and then filtered:

$$\beta_1 = h_1 * (w)$$
(BiasInstability)

where BiasInstability is a property of accelparams, and h_1 is a filter defined by the SampleRate property:

$$H_1(z) = \frac{1}{1 - \frac{1}{2}z^{-1}}$$

White Noise Drift

White noise drift is modeled by multiplying elements of the white noise random stream by the standard deviation:

$$\beta_2 = (w) \left(\sqrt{\frac{\text{SampleRate}}{2}} \right) (\text{NoiseDensity})$$

where SampleRate is an imuSensor property, and NoiseDensity is an accelparams property. Elements of w are random numbers given by settings of the imuSensor random stream.

Random Walk Drift

The random walk drift is modeled by biasing elements of the white noise random stream and then filtering:

$$\beta_3 = h_2 * (w) \left(\frac{\text{RandomWalk}}{\sqrt{\frac{\text{SampleRate}}{2}}} \right)$$

where RandomWalk is a property of accelparams, SampleRate is a property of imuSensor, and h_2 is a filter defined as:

$$H_2(z) = \frac{1}{1 - z^{-1}}$$

Environmental Drift Noise

The environmental drift noise is modeled by multiplying the temperature difference from a standard with the temperature bias:

$$\Delta_e$$
 = (Temperature – 25)(TemperatureBias)

where Temperature is a property of imuSensor, and TemperatureBias is a property of accelparams. The constant 25 corresponds to a standard temperature.

Scale Factor Error Model

The temperature scale factor error is modeled as:

$$scaleFactorError = 1 + \left(\frac{\text{Temperature} - 25}{100}\right) (\text{TemperatureScaleFactor})$$

where Temperature is a property of imuSensor, and TemperatureScaleFactor is a property of accelparams. The constant 25 corresponds to a standard temperature.

Quantization Model

The quantization is modeled by first saturating the continuous signal model:

$$e = \begin{cases} \text{MeasurementRange} & \text{if} & d > \text{MeasurementRange} \\ -\text{MeasurementRange} & \text{if} & -d > \text{MeasurementRange} \\ d & \text{else} \end{cases}$$

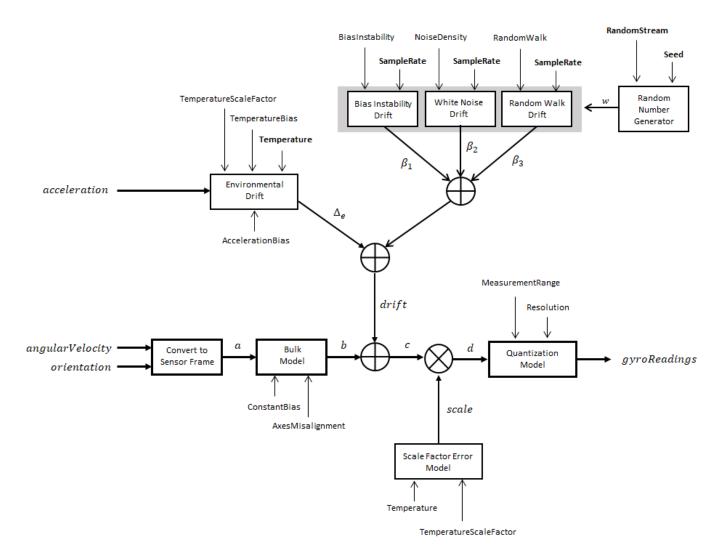
and then setting the resolution:

$$accelReadings = (\text{Resolution}) \Big(\text{round} \Big(\frac{e}{\text{Resolution}} \Big) \Big)$$

where MeasurementRange is a property of accelparams.

Gyroscope

The gyroscope model uses the ground-truth orientation, acceleration, and angular velocity inputs, and the imuSensor and gyroparams properties to model accelerometer readings.



Convert to Sensor Frame

The ground-truth angular velocity is converted from the local frame to the sensor frame using the ground-truth orientation:

 $a = (orientation)(angularVelocity)^T$

If the orientation is input in quaternion form, it is converted to a rotation matrix before processing.

Bulk Model

The ground-truth angular velocity in the sensor frame, a, passes through the bulk model, which adds axes misalignment and bias:

$$b = \begin{pmatrix} 1 & \frac{\alpha_2}{100} & \frac{\alpha_3}{100} \\ \frac{\alpha_1}{100} & 1 & \frac{\alpha_3}{100} \\ \frac{\alpha_1}{100} & \frac{\alpha_2}{100} & 1 \end{pmatrix} + \text{ConstantBias}$$

where ConstantBias is a property of gyroparams, and α_1 , α_2 , and α_3 are given by the first, second, and third elements of the AxesMisalignment property of gyroparams.

Bias Instability Drift

The bias instability drift is modeled as white noise biased and then filtered:

$$\beta_1 = h_1 * (w)$$
(BiasInstability)

where BiasInstability is a property of gyroparams and h_1 is a filter defined by the SampleRate property:

$$H_1(z) = \frac{1}{1 - \frac{1}{2}z^{-1}}$$

White Noise Drift

White noise drift is modeled by multiplying elements of the white noise random stream by the standard deviation:

$$\beta_2 = (w) \left(\sqrt{\frac{\text{SampleRate}}{2}} \right) (\text{NoiseDensity})$$

where SampleRate is an imuSensor property, and NoiseDensity is an gyroparams property. The elements of w are random numbers given by settings of the imuSensor random stream.

Random Walk Drift

The random walk drift is modeled by biasing elements of the white noise random stream and then filtering:

$$\beta_3 = h_2 * (w) \left(\frac{\text{RandomWalk}}{\sqrt{\frac{\text{SampleRate}}{2}}} \right)$$

where RandomWalk is a property of gyroparams, SampleRate is a property of imuSensor, and h_2 is a filter defined as:

$$H_2(z) = \frac{1}{1 - z^{-1}}$$

Environmental Drift Noise

The environmental drift noise is modeled by multiplying the temperature difference from a standard with the temperature bias:

$$\Delta_e$$
 = (Temperature – 25)(TemperatureBias)

where Temperature is a property of imuSensor, and TemperatureBias is a property of gyroparams. The constant 25 corresponds to a standard temperature.

Scale Factor Error Model

The temperature scale factor error is modeled as:

$$scaleFactorError = 1 + \left(\frac{\text{Temperature} - 25}{100}\right) (\text{TemperatureScaleFactor})$$

where Temperature is a property of imuSensor, and TemperatureScaleFactor is a property of gyroparams. The constant 25 corresponds to a standard temperature.

Quantization Model

The quantization is modeled by first saturating the continuous signal model:

$$e = \begin{cases} \text{MeasurementRange} & \text{if} & d > \text{MeasurementRange} \\ -\text{MeasurementRange} & \text{if} & -d > \text{MeasurementRange} \\ d & \text{else} \end{cases}$$

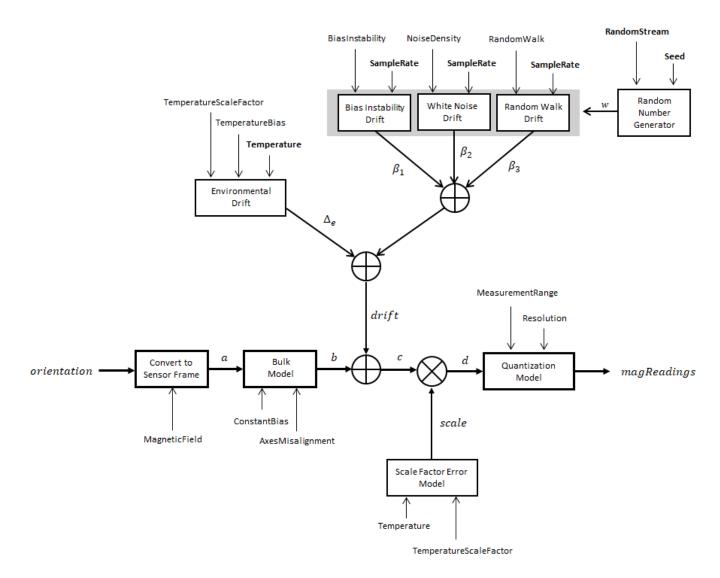
and then setting the resolution:

$$gyroReadings = (Resolution) \left(round \left(\frac{e}{Resolution} \right) \right)$$

where MeasurementRange is a property of gyroparams.

Magnetometer

The magnetometer model uses the ground-truth orientation and acceleration inputs, and the imuSensor and magparams properties to model magnetometer readings.



Convert to Sensor Frame

The ground-truth acceleration is converted from the local frame to the sensor frame using the ground-truth orientation:

$$a = (orientation)(totalAcc)^{T}$$

If the orientation is input in quaternion form, it is converted to a rotation matrix before processing.

Bulk Model

The ground-truth acceleration in the sensor frame, *a*, passes through the bulk model, which adds axes misalignment and bias:

$$b = \begin{pmatrix} 1 & \frac{\alpha_2}{100} & \frac{\alpha_3}{100} \\ \frac{\alpha_1}{100} & 1 & \frac{\alpha_3}{100} \\ \frac{\alpha_1}{100} & \frac{\alpha_2}{100} & 1 \end{pmatrix} + \text{ConstantBias}$$

where ConstantBias is a property of magparams, and α_1 , α_2 , and α_3 are given by the first, second, and third elements of the AxesMisalignment property of magparams.

Bias Instability Drift

The bias instability drift is modeled as white noise biased and then filtered:

$$\beta_1 = h_1 * (w)$$
(BiasInstability)

where BiasInstability is a property of magparams and h_1 is a filter defined by the SampleRate property:

$$H_1(z) = \frac{1}{1 - \frac{1}{2}z^{-1}}$$

White Noise Drift

White noise drift is modeled by multiplying elements of the white noise random stream by the standard deviation:

$$\beta_2 = (w) \left(\sqrt{\frac{\text{SampleRate}}{2}} \right) (\text{NoiseDensity})$$

where SampleRate is an imuSensor property, and NoiseDensity is an magparams property. The elements of w are random numbers given by settings of the imuSensor random stream.

Random Walk Drift

The random walk drift is modeled by biasing elements of the white noise random stream and then filtering:

$$\beta_3 = h_2 * (w) \left(\frac{\text{RandomWalk}}{\sqrt{\frac{\text{SampleRate}}{2}}} \right)$$

where RandomWalk is a property of magparams, SampleRate is a property of imuSensor, and h_2 is a filter defined as:

$$H_2(z) = \frac{1}{1 - z^{-1}}$$

Environmental Drift Noise

The environmental drift noise is modeled by multiplying the temperature difference from a standard with the temperature bias:

$$\Delta_e$$
 = (Temperature – 25)(TemperatureBias)

where Temperature is a property of imuSensor, and TemperatureBias is a property of magparams. The constant 25 corresponds to a standard temperature.

Scale Factor Error Model

The temperature scale factor error is modeled as:

$$scaleFactorError = 1 + \left(\frac{\text{Temperature} - 25}{100}\right) (\text{TemperatureScaleFactor})$$

where Temperature is a property of imuSensor, and TemperatureScaleFactor is a property of magparams. The constant 25 corresponds to a standard temperature.

Quantization Model

The quantization is modeled by first saturating the continuous signal model:

$$e = \begin{cases} \text{MeasurementRange} & \text{if} & d > \text{MeasurementRange} \\ -\text{MeasurementRange} & \text{if} & -d > \text{MeasurementRange} \\ d & \text{else} \end{cases}$$

and then setting the resolution:

$$magReadings = (Resolution) \left(round \left(\frac{e}{Resolution} \right) \right)$$

where MeasurementRange is a property of magparams.

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

Usage notes and limitations:

See "System Objects in MATLAB Code Generation" (MATLAB Coder).

See Also

Classes

accelparams | gyroparams | magparams

Objects

gpsSensor

Introduced in R2018b

insSensor

Inertial navigation system and GNSS/GPS simulation model

Description

The insSensor System object models a device that fuses measurements from an inertial navigation system (INS) and global navigation satellite system (GNSS) such as a GPS, and outputs the fused measurements.

To output fused INS and GNSS measurements:

- **1** Create the insSensor object and set its properties.
- **2** Call the object with arguments, as if it were a function.

To learn more about how System objects work, see What Are System Objects?.

Creation

Syntax

INS = insSensor

INS = insSensor(Name, Value)

Description

INS = insSensor returns a System object, INS, that models a device that outputs measurements from an INS and GNSS.

INS = insSensor(Name, Value) sets properties on page 2-409 using one or more name-value pairs. Unspecified properties have default values. Enclose each property name in quotes.

Properties

Unless otherwise indicated, properties are *nontunable*, which means you cannot change their values after calling the object. Objects lock when you call them, and the release function unlocks them.

If a property is tunable, you can change its value at any time.

For more information on changing property values, see System Design in MATLAB Using System Objects.

MountingLocation — Location of sensor on platform (m)

[0 0 0] (default) | three-element real-valued vector of form $[x \ y \ z]$

Location of the sensor on the platform, in meters, specified as a three-element real-valued vector of the form $[x \ y \ z]$. The vector defines the offset of the sensor origin from the origin of the platform.

Tunable: Yes

Data Types: single | double

RollAccuracy — Accuracy of roll measurement (deg)

0.2 (default) | nonnegative real scalar

Accuracy of the roll measurement of the sensor body, in degrees, specified as a nonnegative real scalar.

Roll is the rotation around the *x*-axis of the sensor body. Roll noise is modeled as a white noise process. RollAccuracy sets the standard deviation of the roll measurement noise.

Tunable: Yes

Data Types: single | double

PitchAccuracy — Accuracy of pitch measurement (deg)

0.2 (default) | nonnegative real scalar

Accuracy of the pitch measurement of the sensor body, in degrees, specified as a nonnegative real scalar.

Pitch is the rotation around the y-axis of the sensor body. Pitch noise is modeled as a white noise process. PitchAccuracy defines the standard deviation of the pitch measurement noise.

Tunable: Yes

Data Types: single | double

YawAccuracy — Accuracy of yaw measurement (deg)

1 (default) | nonnegative real scalar

Accuracy of the yaw measurement of the sensor body, in degrees, specified as a nonnegative real scalar.

Yaw is the rotation around the z-axis of the sensor body. Yaw noise is modeled as a white noise process. YawAccuracy defines the standard deviation of the yaw measurement noise.

Tunable: Yes

Data Types: single | double

PositionAccuracy — Accuracy of position measurement (m)

[1 1 1] (default) | nonnegative real scalar | three-element real-valued vector

Accuracy of the position measurement of the sensor body, in meters, specified as a nonnegative real scalar or a three-element real-valued vector. The elements of the vector set the accuracy of the x-, y-, and z-position measurements, respectively. If you specify PositionAccuracy as a scalar value, then the object sets the accuracy of all three positions to this value.

Position noise is modeled as a white noise process. PositionAccuracy defines the standard deviation of the position measurement noise.

Tunable: Yes

Data Types: single | double

VelocityAccuracy — Accuracy of velocity measurement (m/s)

0.05 (default) | nonnegative real scalar

Accuracy of the velocity measurement of the sensor body, in meters per second, specified as a nonnegative real scalar.

Velocity noise is modeled as a white noise process. VelocityAccuracy defines the standard deviation of the velocity measurement noise.

Tunable: Yes

Data Types: single | double

AccelerationAccuracy — Accuracy of acceleration measurement (m/s²)

0 (default) | nonnegative real scalar

Accuracy of the acceleration measurement of the sensor body, in meters per second, specified as a nonnegative real scalar.

Acceleration noise is modeled as a white noise process. AccelerationAccuracy defines the standard deviation of the acceleration measurement noise.

Tunable: Yes

Data Types: single | double

Angular Velocity Accuracy — Accuracy of angular velocity measurement (deg/s)

0 (default) | nonnegative real scalar

Accuracy of the angular velocity measurement of the sensor body, in meters per second, specified as a nonnegative real scalar.

Angular velocity is modeled as a white noise process. AngularVelocityAccuracy defines the standard deviation of the acceleration measurement noise.

Tunable: Yes

Data Types: single | double

TimeInput — Enable input of simulation time

false or 0 (default) | true or 1

Enable input of simulation time, specified as a logical 0 (false) or 1 (true). Set this property to true to input the simulation time by using the simTime argument.

Tunable: No

Data Types: logical

HasGNSSFix — **Enable GNSS** fix

true or 1 (default) | false or 0

Enable GNSS fix, specified as a logical 1 (true) or 0 (false). Set this property to false to simulate the loss of a GNSS receiver fix. When a GNSS receiver fix is lost, position measurements drift at a rate specified by the PositionErrorFactor property.

Tunable: Yes

Dependencies

To enable this property, set TimeInput to true.

Data Types: logical

PositionErrorFactor — Position error factor without GNSS fix

[0 0 0] (default) | nonnegative scalar | 1-by-3 vector of scalars

Position error factor without GNSS fix, specified as a scalar or a 1-by-3 vector of scalars.

When the HasGNSSFix property is set to false, the position error grows at a quadratic rate due to constant bias in the accelerometer. The position error for a position component E(t) can be expressed as $E(t) = 1/2\alpha t^2$, where α is the position error factor for the corresponding component and t is the time since the GNSS fix is lost. While running, the object computes t based on the simTime input. The computed E(t) values for the x, y, and z components are added to the corresponding position components of the gTruth input.

Tunable: Yes

Dependencies

To enable this property, set TimeInput to true and HasGNSSFix to false.

Data Types: single | double

RandomStream — Random number source

'Global stream' (default) | 'mt19937ar with seed'

Random number source, specified as one of these options:

- 'Global stream' -- Generate random numbers using the current global random number stream.
- 'mt19937ar with seed' -- Generate random numbers using the mt19937ar algorithm, with the seed specified by the Seed property.

Data Types: char | string

Seed — Initial seed

67 (default) | nonnegative integer

Initial seed of the mt19937ar random number generator algorithm, specified as a nonnegative integer.

Dependencies

To enable this property, set RandomStream to 'mt19937ar with seed'.

Data Types: single | double | int8 | int16 | int32 | int64 | uint8 | uint16 | uint32 | uint64

Usage

Syntax

```
measurement = INS(gTruth)
measurement = INS(gTruth, simTime)
```

Description

measurement = INS(gTruth) models the data received from an INS sensor reading and GNSS sensor reading. The output measurement is based on the inertial ground-truth state of the sensor body, gTruth.

measurement = INS(gTruth, simTime) additionally specifies the time of simulation, simTime. To
enable this syntax, set the TimeInput property to true.

Input Arguments

${\tt gTruth-Inertial\ ground-truth\ state\ of\ sensor\ body}$

structure

Inertial ground-truth state of sensor body, in local Cartesian coordinates, specified as a structure containing these fields:

Field	Description
'Position'	Position, in meters, specified as a real, finite N -by-3 matrix of $[x \ y \ z]$ vectors. N is the number of samples in the current frame.
'Velocity'	Velocity (ν), in meters per second, specified as a real, finite N -by-3 matrix of [$\nu_x \nu_y \nu_z$] vector. N is the number of samples in the current frame.
'Orientation'	Orientation with respect to the local Cartesian coordinate system, specified as one of these options:
	N-element column vector of quaternion objects
	3-by-3-by-N array of rotation matrices
	• N-by-3 matrix of $[x_{roll} y_{pitch} z_{yaw}]$ angles in degrees
	Each quaternion or rotation matrix is a frame rotation from the local Cartesian coordinate system to the current sensor body coordinate system. N is the number of samples in the current frame.
'Acceleration'	Acceleration (a), in meters per second squared, specified as a real, finite N -by-3 matrix of $[a_x \ a_y \ a_z]$ vectors. N is the number of samples in the current frame.
'AngularVelocity'	Angular velocity (ω), in meters per second squared, specified as a real, finite N -by-3 matrix of [$\omega_x \omega_y \omega_z$] vectors. N is the number of samples in the current frame.

The field values must be of type double or single.

The Position, Velocity, and Orientation fields are required. The other fields are optional.

Example: struct('Position',[0 0 0],'Velocity',[0 0 0],'Orientation',quaternion([1 0 0 0]))

simTime — Simulation time

nonnegative real scalar

Simulation time, in seconds, specified as a nonnegative real scalar.

Data Types: single | double

Output Arguments

measurement — Measurement of sensor body motion

structure

Measurement of the sensor body motion, in local Cartesian coordinates, returned as a structure containing these fields:

Field	Description
'Position'	Position, in meters, specified as a real, finite N -by-3 matrix of $[x \ y \ z]$ vectors. N is the number of samples in the current frame.
'Velocity'	Velocity (ν), in meters per second, specified as a real, finite N -by-3 matrix of [$\nu_x \ \nu_y \ \nu_z$] vector. N is the number of samples in the current frame.
'Orientation'	Orientation with respect to the local Cartesian coordinate system, specified as one of these options:
	N-element column vector of quaternion objects
	3-by-3-by-N array of rotation matrices
	• N-by-3 matrix of $[x_{\text{roll}} y_{\text{pitch}} z_{\text{yaw}}]$ angles in degrees
	Each quaternion or rotation matrix is a frame rotation from the local Cartesian coordinate system to the current sensor body coordinate system. N is the number of samples in the current frame.
'Acceleration'	Acceleration (a), in meters per second squared, specified as a real, finite N -by-3 matrix of $[a_x \ a_y \ a_z]$ vectors. N is the number of samples in the current frame.
'AngularVelocity'	Angular velocity (ω) , in meters per second squared, specified as a real, finite N -by-3 matrix of $[\omega_x \ \omega_y \ \omega_z]$ vectors. N is the number of samples in the current frame.

The returned field values are of type double or single and are of the same type as the corresponding field values in the gTruth input.

Object Functions

To use an object function, specify the System object as the first input argument. For example, to release system resources of a System object named obj, use this syntax:

```
release(obj)
```

Specific to insSensor

perturbations Perturbation defined on object Apply perturbations to object

Common to All System Objects

step Run System object algorithm
clone Create duplicate System object
isLocked Determine if System object is in use
reset Reset internal states of System object

release Release resources and allow changes to System object property values and input

characteristics

Examples

Generate INS Measurements from Stationary Input

Create a motion structure that defines a stationary position at the local north-east-down (NED) origin. Because the platform is stationary, you need to define only a single sample. Assume the ground-truth motion is sampled for 10 seconds with a 100 Hz sample rate. Create a default insSensor System object™. Preallocate variables to hold output from the insSensor object.

```
Fs = 100;
duration = 10;
numSamples = Fs*duration;

motion = struct( ...
    'Position',zeros(1,3), ...
    'Velocity',zeros(1,3), ...
    'Orientation',ones(1,1,'quaternion'));

INS = insSensor;

positionMeasurements = zeros(numSamples,3);
velocityMeasurements = zeros(numSamples,3);
orientationMeasurements = zeros(numSamples,1,'quaternion');
```

In a loop, call INS with the stationary motion structure to return the position, velocity, and orientation measurements in the local NED coordinate system. Log the position, velocity, and orientation measurements.

```
for i = 1:numSamples
   measurements = INS(motion);

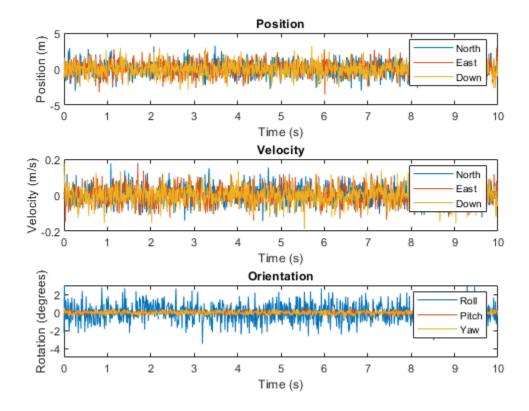
positionMeasurements(i,:) = measurements.Position;
velocityMeasurements(i,:) = measurements.Velocity;
```

```
orientationMeasurements(i) = measurements.Orientation;
```

end

Convert the orientation from quaternions to Euler angles for visualization purposes. Plot the position, velocity, and orientation measurements over time.

```
orientationMeasurements = eulerd(orientationMeasurements,'ZYX','frame');
t = (0:(numSamples-1))/Fs;
subplot(3,1,1)
plot(t,positionMeasurements)
title('Position')
xlabel('Time (s)')
ylabel('Position (m)')
legend('North','East','Down')
subplot(3,1,2)
plot(t,velocityMeasurements)
title('Velocity')
xlabel('Time (s)')
ylabel('Velocity (m/s)')
legend('North','East','Down')
subplot(3,1,3)
plot(t,orientationMeasurements)
title('Orientation')
xlabel('Time (s)')
ylabel('Rotation (degrees)')
legend('Roll', 'Pitch', 'Yaw')
```

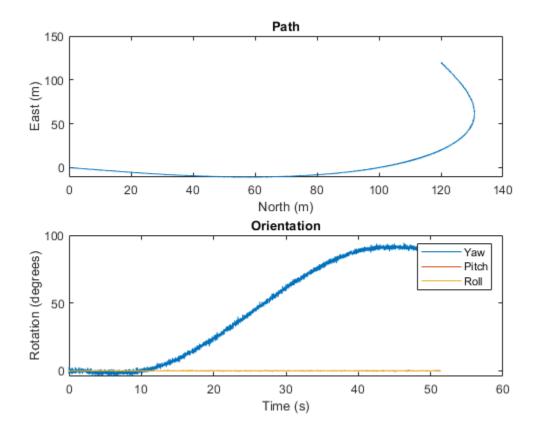


Generate INS Measurements for a Turning Platform

Generate INS measurements using the insSensor System object™. Use waypointTrajectory to generate the ground-truth path.

Specify a ground-truth orientation that begins with the sensor body x-axis aligned with North and ends with the sensor body x-axis aligned with East. Specify waypoints for an arc trajectory and a time-of-arrival vector for the corresponding waypoints. Use a 100 Hz sample rate. Create a waypointTrajectory System object with the waypoint constraints, and set SamplesPerFrame so that the entire trajectory is output with one call.

```
Fs = 100;
numSamples = floor(Fs*toa(end));
path = waypointTrajectory('Waypoints', waypoints, ...
    'TimeOfArrival',toa, ...
    'Orientation', orientation, ...
    'SampleRate', Fs, ...
    'SamplesPerFrame', numSamples);
Create an insSensor System object to model receiving INS data. Set the PositionAccuracy to
0.1.
ins = insSensor('PositionAccuracy', 0.1);
Call the waypoint trajectory object, path, to generate the ground-truth motion. Call the INS
simulator, ins, with the ground-truth motion to generate INS measurements.
[motion.Position,motion.Orientation,motion.Velocity] = path();
insMeas = ins(motion);
Convert the orientation returned by ins to Euler angles in degrees for visualization purposes. Plot
the full path and orientation over time.
orientationMeasurementEuler = eulerd(insMeas.Orientation,'ZYX','frame');
subplot(2,1,1)
plot(insMeas.Position(:,1),insMeas.Position(:,2));
title('Path')
xlabel('North (m)')
ylabel('East (m)')
subplot(2,1,2)
t = (0:(numSamples-1)).'/Fs;
plot(t,orientationMeasurementEuler(:,1), ...
     t,orientationMeasurementEuler(:,2), ...
     t,orientationMeasurementEuler(:,3));
title('Orientation')
legend('Yaw','Pitch','Roll')
xlabel('Time (s)')
ylabel('Rotation (degrees)')
```



Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

Usage notes and limitations:

See "System Objects in MATLAB Code Generation" (MATLAB Coder).

See Also

Objects

gpsSensor|imuSensor

Introduced in R2020b

loadparams

Load sensor parameters from JSON file

Syntax

loadparams(sensor,file,PN)

Description

loadparams (sensor, file, PN) configures the imuSensor object, sensor, to match the parameters in the PN part of a JSON file, File.

Examples

Load Pre-defined Parameters in imuSensor

Create an imuSensor system object.

```
s = imuSensor;
Load a JSON file.
fn = fullfile(matlabroot, 'toolbox', 'shared',...
    'positioning', 'positioningdata', 'generic.json');
```

Here is a screen shot of the JSON file with some parts collapsed.

```
"GenericLowCost9Axis":
{
    "Accelerometer":
    {
        "MeasurementRange": 19.6133,
        "Resolution": 0.0023928,
        "ConstantBias": [0.19,0.19,0.19],
        "AxesMisalignment": [0,0,0],
        "NoiseDensity": [0.0012356,0.0012356],
        "BiasInstability": [0,0,0],
        "RandomWalk": [0,0,0],
        "TemperatureBias": [0,0,0],
        "TemperatureScaleFactor": [0,0,0]
      },
      "Gyroscope":
      {
        }
        "Magnetometer":
      {
        }
    }
    "GenericLowCost6Axis":
{
      }
}
```

Configure the object as a 6-axis sensor.

loadparams(s,fn,'GenericLowCost6Axis')

```
s
  imuSensor with properties:
          IMUType: 'accel-gyro'
       SampleRate: 100
      Temperature: 25
    Accelerometer: [1x1 accelparams]
        Gyroscope: [1x1 gyroparams]
     RandomStream: 'Global stream'
Configure the object as a 9-axis sensor.
loadparams(s,fn,'GenericLowCost9Axis')
  imuSensor with properties:
          IMUType: 'accel-gyro-mag'
       SampleRate: 100
      Temperature: 25
    MagneticField: [27.5550 -2.4169 -16.0849]
    Accelerometer: [1x1 accelparams]
        Gyroscope: [1x1 gyroparams]
     Magnetometer: [1x1 magparams]
     RandomStream: 'Global stream'
```

Input Arguments

sensor — IMU sensor

imuSensor object

IMU sensor, specified as an imuSensor system object.

file - JSON file

```
.json file
```

JavaScript Object Notation (JSON) format file, specified as a .json file.

PN — Part name

string

Part name in a JSON file, specified as a string.

See Also

imuSensor

Introduced in R2020a

kinematicTrajectory

Rate-driven trajectory generator

Description

The kinematicTrajectory System object generates trajectories using specified acceleration and angular velocity.

To generate a trajectory from rates:

- 1 Create the kinematicTrajectory object and set its properties.
- **2** Call the object with arguments, as if it were a function.

To learn more about how System objects work, see What Are System Objects?.

Creation

Syntax

```
trajectory = kinematicTrajectory
trajectory = kinematicTrajectory(Name, Value)
```

Description

trajectory = kinematicTrajectory returns a System object, trajectory, that generates a
trajectory based on acceleration and angular velocity.

trajectory = kinematicTrajectory(Name, Value) sets each property Name to the specified Value. Unspecified properties have default values.

Example: trajectory = kinematicTrajectory('SampleRate',200,'Position',[0,1,10]) creates a kinematic trajectory System object, trajectory, with a sample rate of 200 Hz and the initial position set to [0,1,10].

Properties

If a property is *tunable*, you can change its value at any time.

SampleRate — Sample rate of trajectory (Hz)

100 (default) | positive scalar

Sample rate of trajectory in Hz, specified as a positive scalar.

Tunable: Yes

Data Types: single | double

Position — Position state in local navigation coordinate system (m)

[0 0 0] (default) | 3-element row vector

Position state in the local navigation coordinate system in meters, specified as a three-element row vector.

Tunable: Yes

Data Types: single | double

Velocity — Velocity state in local navigation coordinate system (m/s)

[0 0 0] (default) | 3-element row vector

Velocity state in the local navigation coordinate system in m/s, specified as a three-element row vector.

Tunable: Yes

Data Types: single | double

Orientation — Orientation state in local navigation coordinate system

quaternion (1,0,0,0) (default) | scalar quaternion | 3-by-3 real matrix

Orientation state in the local navigation coordinate system, specified as a scalar quaternion or 3-by-3 real matrix. The orientation is a frame rotation from the local navigation coordinate system to the current body frame.

Tunable: Yes

Data Types: quaternion | single | double

AccelerationSource — Source of acceleration state

'Input' (default) | 'Property'

Source of acceleration state, specified as 'Input' or 'Property'.

- 'Input' -- specify acceleration state as an input argument to the kinematic trajectory object
- 'Property' -- specify acceleration state by setting the Acceleration property

Tunable: No

Data Types: char | string

Acceleration — Acceleration state (m/s²)

[0 0 0] (default) | three-element row vector

Acceleration state in m/s^2 , specified as a three-element row vector.

Tunable: Yes

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Dependencies

To enable this property, set AccelerationSource to 'Property'.

Data Types: single | double

Angular Velocity Source — Source of angular velocity state

```
'Input' (default) | 'Property'
```

Source of angular velocity state, specified as 'Input' or 'Property'.

- 'Input' -- specify angular velocity state as an input argument to the kinematic trajectory object
- 'Property' -- specify angular velocity state by setting the AngularVelocity property

Tunable: No

Data Types: char | string

AngularVelocity — Angular velocity state (rad/s)

[0 0 0] (default) | three-element row vector

Angular velocity state in rad/s, specified as a three-element row vector.

Tunable: Yes

Dependencies

To enable this property, set AngularVelocitySource to 'Property'.

Data Types: single | double

SamplesPerFrame — Number of samples per output frame

1 (default) | positive integer

Number of samples per output frame, specified as a positive integer.

Tunable: No

Dependencies

To enable this property, set AngularVelocitySource to 'Property' and AccelerationSource to 'Property'.

Data Types: single | double

Usage

Syntax

```
[position,orientation,velocity,acceleration,angularVelocity] = trajectory(
bodyAcceleration,bodyAngularVelocity)
[position,orientation,velocity,acceleration,angularVelocity] = trajectory(
bodyAngularVelocity)
[position,orientation,velocity,acceleration,angularVelocity] = trajectory(
bodyAcceleration)
[position,orientation,velocity,acceleration,angularVelocity] = trajectory()
```

Description

[position, orientation, velocity, acceleration, angular Velocity] = trajectory(bodyAcceleration, bodyAngular Velocity) outputs the trajectory state and then updates the trajectory state based on bodyAcceleration and bodyAngular Velocity.

This syntax is only valid if AngularVelocitySource is set to 'Input' and AccelerationSource is set to 'Input'.

[position, orientation, velocity, acceleration, angular Velocity] = trajectory(bodyAngular Velocity) outputs the trajectory state and then updates the trajectory state based on bodyAngular Acceleration.

This syntax is only valid if AngularVelocitySource is set to 'Input' and AccelerationSource is set to 'Property'.

[position, orientation, velocity, acceleration, angular Velocity] = trajectory(bodyAcceleration) outputs the trajectory state and then updates the trajectory state based on bodyAcceleration.

This syntax is only valid if AngularVelocitySource is set to 'Property' and AccelerationSource is set to 'Input'.

[position, orientation, velocity, acceleration, angular Velocity] = trajectory() outputs the trajectory state and then updates the trajectory state.

This syntax is only valid if AngularVelocitySource is set to 'Property' and AccelerationSource is set to 'Property'.

Input Arguments

bodyAcceleration — Acceleration in body coordinate system (m/s²)

N-by-3 matrix

Acceleration in the body coordinate system in meters per second squared, specified as an N-by-3 matrix.

N is the number of samples in the current frame.

bodyAngularVelocity — Angular velocity in body coordinate system (rad/s)

N-by-3 matrix

Angular velocity in the body coordinate system in radians per second, specified as an *N*-by-3 matrix.

N is the number of samples in the current frame.

Output Arguments

position — Position in local navigation coordinate system (m)

N-by-3 matrix

Position in the local navigation coordinate system in meters, returned as an N-by-3 matrix.

N is the number of samples in the current frame.

Data Types: single | double

orientation — Orientation in local navigation coordinate system

N-element quaternion column vector | 3-by-3-by-N real array

Orientation in the local navigation coordinate system, returned as an *N*-by-1 quaternion column vector or a 3-by-3-by-*N* real array. Each quaternion or 3-by-3 rotation matrix is a frame rotation from the local navigation coordinate system to the current body coordinate system.

N is the number of samples in the current frame.

Data Types: single | double

velocity — Velocity in local navigation coordinate system (m/s)

N-by-3 matrix

Velocity in the local navigation coordinate system in meters per second, returned as an N-by-3 matrix.

N is the number of samples in the current frame.

Data Types: single | double

acceleration — Acceleration in local navigation coordinate system (m/s²)

N-by-3 matrix

Acceleration in the local navigation coordinate system in meters per second squared, returned as an N-by-3 matrix.

N is the number of samples in the current frame.

Data Types: single | double

angular Velocity — Angular velocity in local navigation coordinate system (rad/s)

N-by-3 matrix

Angular velocity in the local navigation coordinate system in radians per second, returned as an N-by-3 matrix.

N is the number of samples in the current frame.

Data Types: single | double

Object Functions

Specific to kinematicTrajectory

perturbations Perturbation defined on object Apply perturbations to object

Common to All System Objects

step Run System object algorithm

Examples

Create Default kinematicTrajectory

Create a default kinematicTrajectory System object $^{\text{m}}$ and explore the relationship between input, properties, and the generated trajectories.

```
trajectory = kinematicTrajectory
```

```
Position: [0 0 0]
Orientation: [1x1 quaternion]
Velocity: [0 0 0]
AccelerationSource: 'Input'
AngularVelocitySource: 'Input'
```

By default, the kinematicTrajectory object has an initial position of $[0\ 0\ 0]$ and an initial velocity of $[0\ 0\ 0]$. Orientation is described by a quaternion one $(1\ +\ 0\ i\ +\ 0\ j\ +\ 0\ k)$.

The kinematicTrajectory object maintains a visible and writable state in the properties Position, Velocity, and Orientation. When you call the object, the state is output and then updated.

For example, call the object by specifying an acceleration and angular velocity relative to the body coordinate system.

```
bodyAcceleration = [5,5,0];
bodyAngularVelocity = [0,0,1];
[position, orientation, velocity, acceleration, angular Velocity] = trajectory(bodyAcceleration, bodyA
position = 1 \times 3
      0
            0
                   0
orientation = quaternion
     1 + 0i + 0j + 0k
velocity = 1 \times 3
     (-)
            (-)
                   0
acceleration = 1 \times 3
            5
angular Velocity = 1 \times 3
            0
                   1
```

The position, orientation, and velocity output from the trajectory object correspond to the state reported by the properties before calling the object. The trajectory state is updated after being called and is observable from the properties:

trajectory

```
AngularVelocitySource: 'Input'
```

The acceleration and angularVelocity output from the trajectory object correspond to the bodyAcceleration and bodyAngularVelocity, except that they are returned in the navigation coordinate system. Use the orientation output to rotate acceleration and angularVelocity to the body coordinate system and verify they are approximately equivalent to bodyAcceleration and bodyAngularVelocity.

The kinematicTrajectory System object $^{\text{\tiny{M}}}$ enables you to modify the trajectory state through the properties. Set the position to [0,0,0] and then call the object with a specified acceleration and angular velocity in the body coordinate system. For illustrative purposes, clone the trajectory object before modifying the Position property. Call both objects and observe that the positions diverge.

Create Oscillating Trajectory

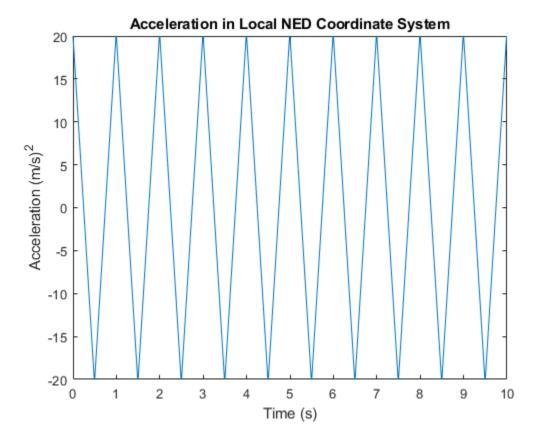
This example shows how to create a trajectory oscillating along the North axis of a local NED coordinate system using the kinematicTrajectory System object $^{\text{TM}}$.

Create a default kinematicTrajectory object. The default initial orientation is aligned with the local NED coordinate system.

```
traj = kinematicTrajectory
```

Define a trajectory for a duration of 10 seconds consisting of rotation around the East axis (pitch) and an oscillation along North axis of the local NED coordinate system. Use the default kinematicTrajectory sample rate.

```
fs = traj.SampleRate;
duration = 10;
numSamples = duration*fs;
cvclesPerSecond = 1;
samplesPerCycle = fs/cyclesPerSecond;
numCycles = ceil(numSamples/samplesPerCycle);
maxAccel = 20;
triangle = [linspace(maxAccel,1/fs-maxAccel,samplesPerCycle/2), ...
    linspace(-maxAccel, maxAccel-(1/fs), samplesPerCycle/2)]';
oscillation = repmat(triangle,numCycles,1);
oscillation = oscillation(1:numSamples);
accNED = [zeros(numSamples,2),oscillation];
angVelNED = zeros(numSamples,3);
angVelNED(:,2) = 2*pi;
Plot the acceleration control signal.
timeVector = 0:1/fs:(duration-1/fs);
figure(1)
plot(timeVector,oscillation)
xlabel('Time (s)')
ylabel('Acceleration (m/s)^2')
title('Acceleration in Local NED Coordinate System')
```



Generate the trajectory sample-by-sample in a loop. The kinematicTrajectory System object assumes the acceleration and angular velocity inputs are in the local sensor body coordinate system. Rotate the acceleration and angular velocity control signals from the NED coordinate system to the sensor body coordinate system using rotateframe and the Orientation state. Update a 3-D plot of the position at each time. Add pause to mimic real-time processing. Once the loop is complete, plot the position over time. Rotating the accNED and angVelNED control signals to the local body coordinate system assures the motion stays along the Down axis.

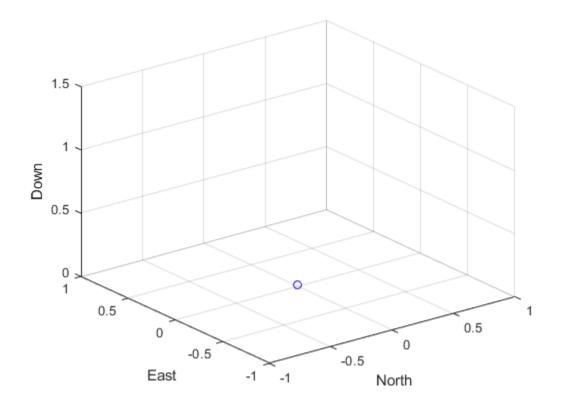
```
figure(2)
plotHandle = plot3(traj.Position(1),traj.Position(2),traj.Position(3),'bo');
grid on
xlabel('North')
ylabel('East')
zlabel('Down')
axis([-1 1 -1 1 0 1.5])
hold on

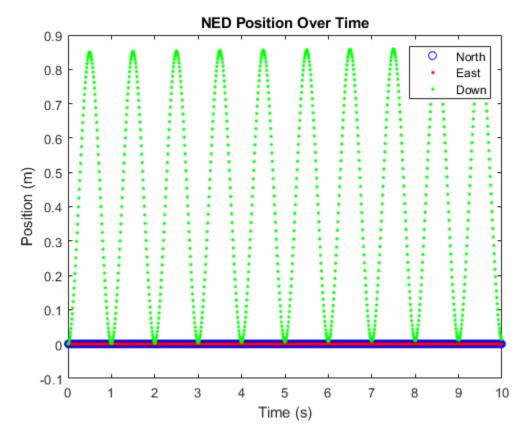
q = ones(numSamples,1,'quaternion');
for ii = 1:numSamples
    accBody = rotateframe(traj.Orientation,accNED(ii,:));
    angVelBody = rotateframe(traj.Orientation,angVelNED(ii,:));

[pos(ii,:),q(ii),vel,ac] = traj(accBody,angVelBody);
set(plotHandle,'XData',pos(ii,1),'YData',pos(ii,2),'ZData',pos(ii,3))
    pause(1/fs)
```

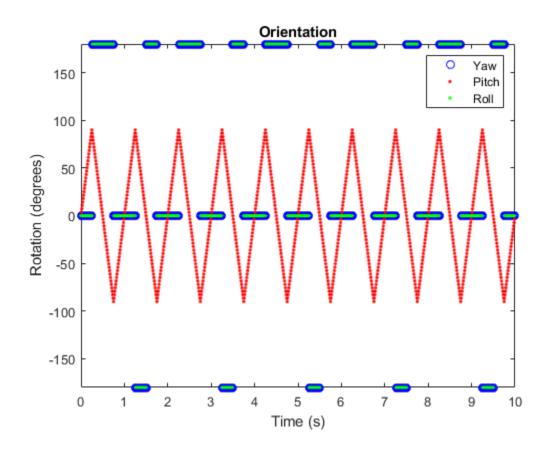
end

```
figure(3)
plot(timeVector,pos(:,1),'bo',...
    timeVector,pos(:,2),'r.',...
    timeVector,pos(:,3),'g.')
xlabel('Time (s)')
ylabel('Position (m)')
title('NED Position Over Time')
legend('North','East','Down')
```





Convert the recorded orientation to Euler angles and plot. Although the orientation of the platform changed over time, the acceleration always acted along the North axis.



Generate a Coil Trajectory

This example shows how to generate a coil trajectory using the kinematicTrajectory System objectTM.

Create a circular trajectory for a 1000 second duration and a sample rate of 10 Hz. Set the radius of the circle to 5000 meters and the speed to 80 meters per second. Set the climb rate to 100 meters per second and the pitch to 15 degrees. Specify the initial orientation as pointed in the direction of motion.

```
duration = 1000; % seconds
fs = 10;
                 % Hz
N = duration*fs; % number of samples
                 % meters
radius = 5000;
                 % meters per second
speed = 80;
climbRate = 50; % meters per second
initialYaw = 90; % degrees
pitch = 15;
                 % degrees
initPos = [radius, 0, 0];
initVel = [0, speed, climbRate];
initOrientation = quaternion([initialYaw,pitch,0],'eulerd','zyx','frame');
trajectory = kinematicTrajectory('SampleRate',fs, ...
```

```
'Velocity',initVel, ...
'Position',initPos, ...
'Orientation',initOrientation);
```

Specify a constant acceleration and angular velocity in the body coordinate system. Rotate the body frame to account for the pitch.

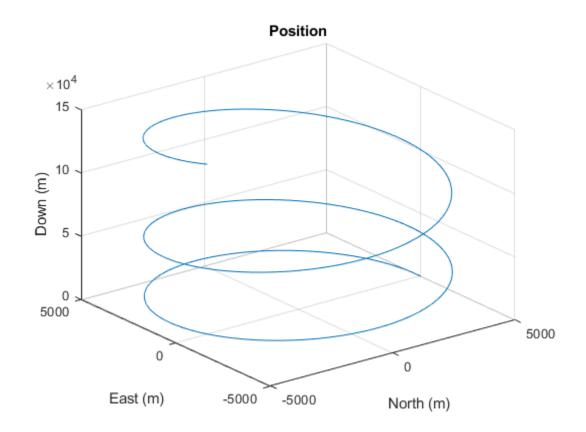
```
accBody = zeros(N,3);
accBody(:,2) = speed^2/radius;
accBody(:,3) = 0.2;
angVelBody = zeros(N,3);
angVelBody(:,3) = speed/radius;
pitchRotation = quaternion([0,pitch,0],'eulerd','zyx','frame');
angVelBody = rotateframe(pitchRotation,angVelBody);
accBody = rotateframe(pitchRotation,accBody);
```

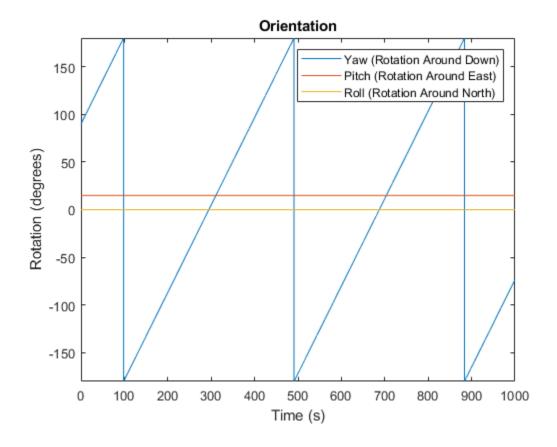
Call trajectory with the specified acceleration and angular velocity in the body coordinate system. Plot the position, orientation, and speed over time.

```
[position, orientation, velocity] = trajectory(accBody,angVelBody);
eulerAngles = eulerd(orientation,'ZYX','frame');
speed = sqrt(sum(velocity.^2,2));

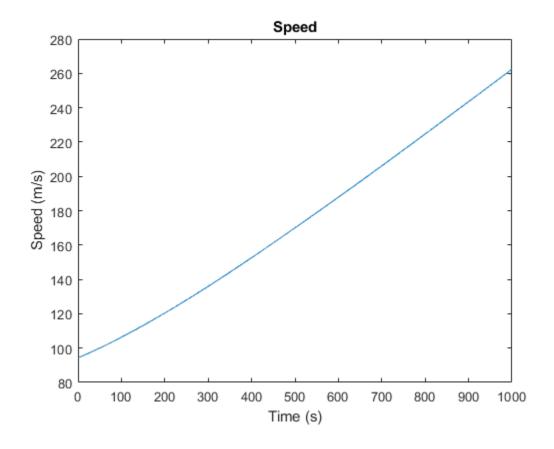
timeVector = (0:(N-1))/fs;

figure(1)
plot3(position(:,1),position(:,2),position(:,3))
xlabel('North (m)')
ylabel('East (m)')
zlabel('Down (m)')
title('Position')
grid on
```





figure(3)
plot(timeVector, speed)
xlabel('Time (s)')
ylabel('Speed (m/s)')
title('Speed')



Generate Spiraling Circular Trajectory with No Inputs

Define a constant angular velocity and constant acceleration that describe a spiraling circular trajectory.

```
Fs = 100;
r = 10;
speed = 2.5;
initialYaw = 90;
initPos = [r 0 0];
initVel = [0 speed 0];
initOrient = quaternion([initialYaw 0 0], 'eulerd', 'ZYX', 'frame');
accBody = [0 speed^2/r 0.01];
angVelBody = [0 \ 0 \ \text{speed/r}];
Create a kinematic trajectory object.
traj = kinematicTrajectory('SampleRate',Fs, ...
    'Position',initPos, ...
    'Velocity', initVel, ...
    'Orientation',initOrient, ...
    'AccelerationSource', 'Property', ...
    'Acceleration',accBody, ...
```

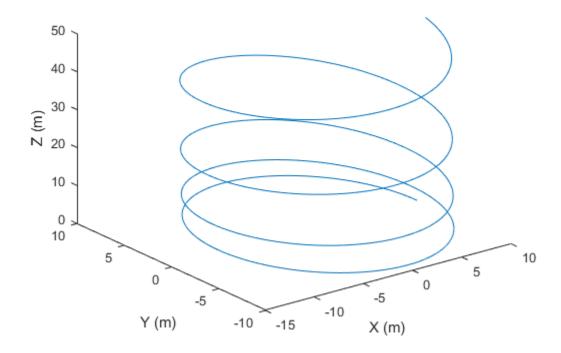
```
'AngularVelocitySource','Property', ...
'AngularVelocity',angVelBody);
```

Call the kinematic trajectory object in a loop and log the position output. Plot the position over time.

```
N = 10000;
pos = zeros(N, 3);
for i = 1:N
         pos(i,:) = traj();
end

plot3(pos(:,1), pos(:,2), pos(:,3))
title('Position')
xlabel('X (m)')
ylabel('Y (m)')
zlabel('Z (m)')
```

Position



Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder $^{\text{\tiny TM}}$.

Usage notes and limitations:

"System Objects in MATLAB Code Generation" (MATLAB Coder)

See Also

waypointTrajectory

Introduced in R2019b

lidarScan

Create object for storing 2-D lidar scan

Description

A lidarScan object contains data for a single 2-D lidar (light detection and ranging) scan. The lidar scan is a laser scan for a 2-D plane with distances (Ranges) measured from the sensor to obstacles in the environment at specific angles (Angles). Use this laser scan object as an input to other robotics algorithms such as matchScans, controllerVFH, or monteCarloLocalization.

Creation

Syntax

```
scan = lidarScan(ranges,angles)
scan = lidarScan(cart)
```

Description

scan = lidarScan(ranges, angles) creates a lidarScan object from the ranges and angles, that represent the data collected from a lidar sensor. The ranges and angles inputs are vectors of the same length and are set directly to the Ranges and Angles properties.

scan = lidarScan(cart) creates a lidarScan object using the input Cartesian coordinates as an n-by-2 matrix. The Cartesian property is set directly from this input.

scan = lidarScan(scanMsg) creates a lidarScan object from a LaserScan ROS message
object.

Properties

Ranges — Range readings from lidar

vector

Range readings from lidar, specified as a vector. This vector is the same length as Angles, and the vector elements are measured in meters.

```
Data Types: single | double
```

Angles — Angle of readings from lidar

vector

Angle of range readings from lidar, specified as a vector. This vector is the same length as Ranges, and the vector elements are measured in radians. Angles are measured counter-clockwise around the positive *z*-axis.

Data Types: single | double

Cartesian — Cartesian coordinates of lidar readings

[x y] matrix

Cartesian coordinates of lidar readings, returned as an $[x \ y]$ matrix. In the lidar coordinate frame, positive x is forward and positive y is to the left.

Data Types: single | double

Count — Number of lidar readings

scalar

Number of lidar readings, returned as a scalar. This scalar is also equal to the length of the Ranges and Angles vectors or the number of rows in Cartesian.

Data Types: double

Object Functions

plot Display laser or lidar scan readings removeInvalidData Remove invalid range and angle data transformScan Transform laser scan based on relative pose

Examples

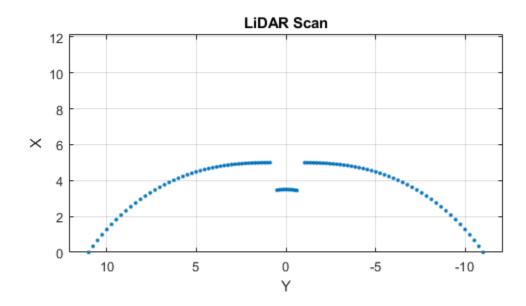
Plot Lidar Scan and Remove Invalid Points

Specify lidar data as vectors of ranges and angles. These values include readings outside of the sensors range.

```
x = linspace(-2,2);
ranges = abs((1.5).*x.^2 + 5);
ranges(45:55) = 3.5;
angles = linspace(-pi/2,pi/2,numel(ranges));
```

Create a lidar scan by specifying the ranges and angles. Plot all points of the lidar scan.

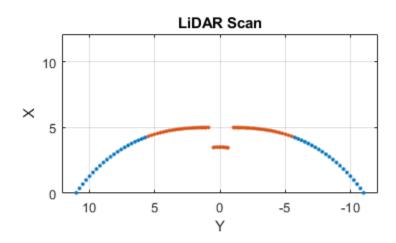
```
scan = lidarScan(ranges,angles);
plot(scan)
```



Remove invalid points based on a specified minimum and maximum range.

```
minRange = 0.1;
maxRange = 7;
scan2 = removeInvalidData(scan, 'RangeLimits', [minRange maxRange]);
hold on
plot(scan2)
legend('All Points', 'Valid Points')
```





Transform Laser Scans

Create a lidarScan object. Specify the ranges and angles as vectors.

```
refRanges = 5*ones(1,300);
refAngles = linspace(-pi/2,pi/2,300);
refScan = lidarScan(refRanges,refAngles);

Translate the laser scan by an [x y] offset of (0.5,0.2).

transformedScan = transformScan(refScan,[0.5 0.2 0]);

Rotate the laser scan by 20 degrees.

rotateScan = transformScan(refScan,[0,0,deg2rad(20)]);
```

Match Lidar Scans

Create a reference lidar scan using lidarScan (Robotics System Toolbox). Specify ranges and angles as vectors.

```
refRanges = 5*ones(1,300);
refAngles = linspace(-pi/2,pi/2,300);
refScan = lidarScan(refRanges,refAngles);
```

Using the transformScan (Robotics System Toolbox) function, generate a second lidar scan at an x, y offset of (0.5,0.2).

```
currScan = transformScan(refScan,[0.5 0.2 0]);
```

Match the reference scan and the second scan to estimate the pose difference between them.

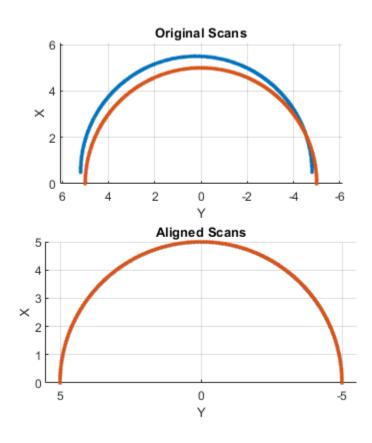
```
pose = matchScans(currScan, refScan);
```

Use the transformScan function to align the scans by transforming the second scan into the frame of the first scan using the relative pose difference. Plot both the original scans and the aligned scans.

```
currScan2 = transformScan(currScan,pose);
```

```
subplot(2,1,1);
hold on
plot(currScan)
plot(refScan)
title('Original Scans')
hold off

subplot(2,1,2);
hold on
plot(currScan2)
plot(refScan)
title('Aligned Scans')
xlim([0 5])
hold off
```



Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

Usage notes and limitations:

Lidar scans require a limited size in code generation. The lidar scans are limited to 4000 points (range and angles) as a maximum.

See Also

 $controller VFH \mid match Scans \mid monte Carlo Localization \mid transform Scan$

Introduced in R2019b

plot

Display laser or lidar scan readings

Syntax

```
plot(scan0bj)
plot(____,Name,Value)
linehandle = plot(____)
```

Description

plot(scanObj) plots the lidar scan readings specified in scanObj.

plot(____, Name, Value) provides additional options specified by one or more Name, Value pair arguments.

linehandle = plot(____) returns a column vector of line series handles, using any of the
arguments from previous syntaxes. Use linehandle to modify properties of the line series after it is
created.

Examples

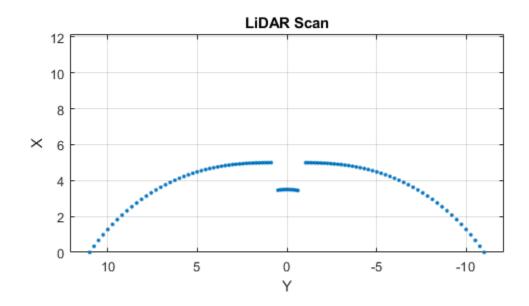
Plot Lidar Scan and Remove Invalid Points

Specify lidar data as vectors of ranges and angles. These values include readings outside of the sensors range.

```
x = linspace(-2,2);
ranges = abs((1.5).*x.^2 + 5);
ranges(45:55) = 3.5;
angles = linspace(-pi/2,pi/2,numel(ranges));
```

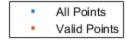
Create a lidar scan by specifying the ranges and angles. Plot all points of the lidar scan.

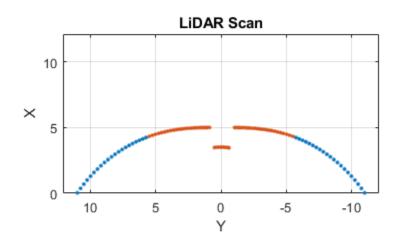
```
scan = lidarScan(ranges,angles);
plot(scan)
```



Remove invalid points based on a specified minimum and maximum range.

```
minRange = 0.1;
maxRange = 7;
scan2 = removeInvalidData(scan,'RangeLimits',[minRange maxRange]);
hold on
plot(scan2)
legend('All Points','Valid Points')
```





Input Arguments

scan0bj — Lidar scan readings

lidarScan object

Lidar scan readings, specified as a lidarScan object.

Name-Value Pair Arguments

Specify optional comma-separated pairs of Name, Value arguments. Name is the argument name and Value is the corresponding value. Name must appear inside quotes. You can specify several name and value pair arguments in any order as Name1, Value1, . . . , NameN, ValueN.

Example: "MaximumRange",5

Parent — Parent of axes

axes object

Parent of axes, specified as the comma-separated pair consisting of "Parent" and an axes object in which the laser scan is drawn. By default, the laser scan is plotted in the currently active axes.

MaximumRange — Range of laser scan

scan.RangeMax (default) | scalar

Range of laser scan, specified as the comma-separated pair consisting of "MaximumRange" and a scalar. When you specify this name-value pair argument, the minimum and maximum x-axis and the

maximum *y*-axis limits are set based on specified value. The minimum *y*-axis limit is automatically determined by the opening angle of the laser scanner.

This name-value pair only works when you input scanMsg as the laser scan.

Outputs

linehandle — One or more chart line objects

scalar | vector

One or more chart line objects, returned as a scalar or a vector. These are unique identifiers, which you can use to query and modify properties of a specific chart line.

See Also

controllerVFH | matchScans | monteCarloLocalization | transformScan

Topics

"Estimate Robot Pose with Scan Matching"

Introduced in R2015a

lidarSLAM

Perform localization and mapping using lidar scans

Description

The lidarSLAM class performs simultaneous localization and mapping (SLAM) for lidar scan sensor inputs. The SLAM algorithm takes in lidar scans and attaches them to a node in an underlying pose graph. The algorithm then correlates the scans using scan matching. It also searches for loop closures, where scans overlap previously mapped regions, and optimizes the node poses in the pose graph.

Creation

Syntax

```
slamObj = lidarSLAM
slamObj = lidarSLAM(mapResolution, maxLidarRange)
slamObj = lidarSLAM(mapResolution, maxLidarRange, maxNumScans)
```

Description

slamObj = lidarSLAM creates a lidar SLAM object. The default occupancy map size is 20 cells per meter. The maximum range for each lidar scan is 8 meters.

slamObj = lidarSLAM(mapResolution, maxLidarRange) creates a lidar SLAM object and sets
the MapResolution and MaxLidarRange properties based on the inputs.

slamObj = lidarSLAM(mapResolution, maxLidarRange, maxNumScans) specifies the upper bound on the number of accepted scans allowed when generating code. maxNumScans is a positive integer. This scan limit is only required when generating code.

Properties

PoseGraph — Underlying pose graph that connects scans

poseGraph object

Underlying pose graph that connects scans, specified as a poseGraph object. Adding scans to lidarSLAM updates this pose graph. When loop closures are found, the pose graph is optimized using OptimizationFcn.

MapResolution — Resolution of occupancy grid map

20 cells per meter (default) | positive integer

Resolution of the occupancy grid map, specified as a positive integer in cells per meter. Specify the map resolution on construction.

MaxLidarRange — Maximum range of lidar sensor

8 meters (default) | positive scalar

Maximum range of the lidar sensor, specified as a positive scalar in meters. Specify the maximum range on construction.

OptimizationFcn — Pose graph optimization function

optimizePoseGraph (default) | function handle

Pose graph optimization function, specified as a function handle. By default, the algorithm calls the <code>optimizePoseGraph</code> function. To specify your own optimization method, the class requires the function signature to be:

[updatedPose,stat] = myOptimizationFcn(poseGraph)

poseGraph is a poseGraph object. updatedPose is an *n*-by-3 vector of [x y theta] poses listed in sequential node ID order. stat is a structure containing a ResidualError field as a positive scalar. Use the stat structure to include other information relevant to your optimization.

LoopClosureThreshold — Threshold for accepting loop closures

100 (default) | positive scalar

Threshold on the score from the scan matching algorithm for accepting loop closures, specified as a positive scalar. Higher thresholds correspond to a better match, but scores vary based on sensor data.

LoopClosureSearchRadius — Search radius for loop closure detection

8 meters (default) | positive scalar

Search radius for loop closure detection, specified as a positive scalar. Increasing this radius affects performance by increasing search time. Tune this distance based on your environment and the expected vehicle trajectory.

${\bf LoopClosure MaxAttempts-Number\ of\ attempts\ at\ finding\ loop\ closures}$

1 (default) | positive integer

Number of attempts at finding looping closures, specified as a positive integer. Increasing the number of attempts affects performance by increasing search time.

LoopClosureAutoRollback — Allow automatic rollback of added loop closures true (default) | false

Allow automatic rollback of added loop closures, specified as true or false. The SLAM object tracks the residual error returned by the OptimizationFcn. If it detects a sudden change in the residual error and this property is true, it rejects (rolls back) the loop closure.

OptimizationInterval — **Number of loop closures accepted to trigger optimization** 1 (default) | positive integer

Number of loop closures accepted to trigger optimization, specified as a positive integer. By default, the PoseGraph is optimized every time lidarSLAM adds a loop closure.

MovementThreshold — Minimum change in pose required to process scans

[0 0] (default) | [translation rotation]

Minimum change in pose required to process scans, specified as a [translation rotation] vector. A relative pose change for a newly added scan is calculated as [x y theta]. If the translation in xy-position or rotation of theta exceeds these thresholds, the lidarSLAM object accepts the scan and adds a pose is added to the PoseGraph.

ScanRegistrationMethod — Scan registration method

```
'BranchAndBound' (default) | 'PhaseCorrelation'
```

Scan registration method, specified as a character vector.

Note Image Processing Toolbox[™] is required for using Phase Correlation method.

Object Functions

addScan Add scan to lidar SLAM map copy Copy lidar SLAM object

removeLoopClosures Remove loop closures from pose graph scansAndPoses Extract scans and corresponding poses

show Plot scans and robot poses

Examples

Perform SLAM Using Lidar Scans

Use a lidarSLAM object to iteratively add and compare lidar scans and build an optimized pose graph of the robot trajectory. To get an occupancy map from the associated poses and scans, use the buildMap function.

Load Data and Set Up SLAM Algorithm

Load a cell array of lidarScan objects. The lidar scans were collected in a parking garage on a Husky® robot from ClearPath Robotics®. Typically, lidar scans are taken at a high frequency and each scan is not needed for SLAM. Therefore, down sample the scans by selecting only every 40th scan.

```
load garage_fll_southend.mat scans
scans = scans(1:40:end);
```

To set up the SLAM algorithm, specify the lidar range, map resolution, loop closure threshold, and search radius. Tune these parameters for your specific robot and environment. Create the lidarSLAM object with these parameters.

```
maxRange = 19.2; % meters
resolution = 10; % cells per meter

slamObj = lidarSLAM(resolution, maxRange);
slamObj.LoopClosureThreshold = 360;
slamObj.LoopClosureSearchRadius = 8;
```

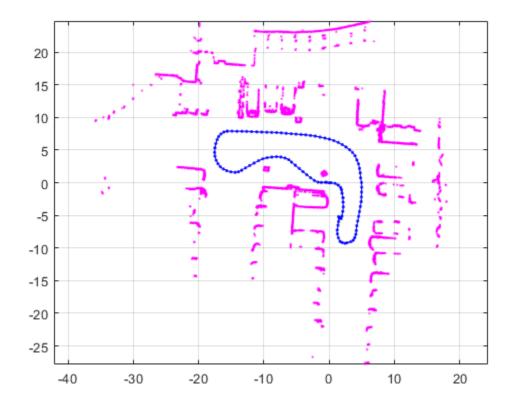
Add Scans Iteratively

Using a for loop, add scans to the SLAM object. The object uses scan matching to compare each added scan to previously added ones. To improve the map, the object optimizes the pose graph whenever it detects a loop closure. Every 10 scans, display the stored poses and scans.

```
for i = 1:numel(scans)

addScan(slamObj,scans{i});
```

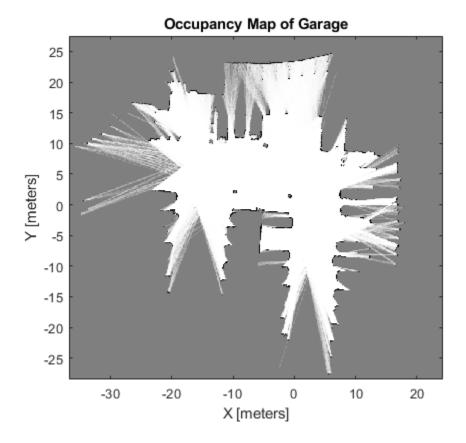
```
if rem(i,10) == 0
          show(slamObj);
end
end
```



View Occupancy Map

After adding all the scans to the SLAM object, build an occupancyMap map by calling buildMap with the scans and poses. Use the same map resolution and max range you used with the SLAM object.

```
[scansSLAM,poses] = scansAndPoses(slamObj);
occMap = buildMap(scansSLAM,poses,resolution,maxRange);
figure
show(occMap)
title('Occupancy Map of Garage')
```



More About

SLAM

Simultaneous localization and mapping (SLAM) is a general concept for algorithms correlating different sensor readings to build a map of a vehicle environment and track pose estimates. Different algorithms use different types of sensors and methods for correlating data.

The lidarSLAM algorithm uses lidar scans and odometry information as sensor inputs. The lidar scans map the environment and are correlated between each other to build an underlying pose graph of the vehicle trajectory. Odometry information is an optional input that gives an initial pose estimate for the scans to aid in the correlation. Scan matching algorithms correlate scans to previously added scans to estimate the relative pose between them and add them to an underlying pose graph.

The pose graph contains nodes connected by edges that represent the relative poses of the vehicle. Edges specify constraints on the node as an information matrix. To correct for drifting pose estimates, the algorithm optimizes over the whole pose graph whenever it detects loop closures.

The algorithm assumes that data comes from a vehicle navigating an environment and incrementally getting laser scans along its path. Therefore, scans are first compared to the most recent scan to identify relative poses and are added to the pose graph incrementally. However, the algorithm also searches for loop closures, which identify when the vehicle scans an area that was previously visited.

When working with SLAM algorithms, the environment and vehicle sensors affect the performance and data correlation quality. Tune your parameters properly for your expected environment or dataset.

References

[1] Hess, Wolfgang, Damon Kohler, Holger Rapp, and Daniel Andor. "Real-Time Loop Closure in 2D LIDAR SLAM." 2016 IEEE International Conference on Robotics and Automation (ICRA). 2016.

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

Use this syntax when constructing lidarSLAM objects for code generation:

slamObj= lidarSLAM(mapResolution, maxLidarRange, maxNumScans) specifies the upper bound on the number of accepted scans allowed when generating code. maxNumScans is a positive integer. This scan limit is only required when generating code.

See Also

optimizePoseGraph | poseGraph

Topics

"Implement Simultaneous Localization And Mapping (SLAM) with Lidar Scans"

Introduced in R2019b

[&]quot;Implement Online Simultaneous Localization And Mapping (SLAM) with Lidar Scans"

addScan

Add scan to lidar SLAM map

Syntax

```
addScan(slamObj,currScan)
addScan(slamObj,currScan,relPoseEst)
[isAccepted,loopClosureInfo,optimInfo] = addScan( )
```

Description

addScan(slam0bj,currScan) adds a lidar scan, currScan, to the lidar SLAM object, slam0bj. The function uses scan matching to correlate this scan to the most recent one, then adds it to the pose graph defined in slam0bj. If the scan is accepted, addScan detects loop closures and optimizes based on settings in slam0bj.

addScan(slamObj,currScan,relPoseEst) also specifies a relative pose to the latest lidar scan pose in slamObj. This relative pose improves the scan matching.

Note The relPoseEst input is ignored when the ScanRegistrationMethod property of lidarSLAM object is set to 'PhaseCorrelation'.

[isAccepted,loopClosureInfo,optimInfo] = addScan(____) outputs detailed information about adding the scan to the SLAM object. isAccepted indicates if the scan is added or rejected. loopClosureInfo and optimInfo indicate if a loop closure is detected or the pose graph is optimized.

Examples

Perform SLAM Using Lidar Scans

Use a lidarSLAM object to iteratively add and compare lidar scans and build an optimized pose graph of the robot trajectory. To get an occupancy map from the associated poses and scans, use the buildMap function.

Load Data and Set Up SLAM Algorithm

Load a cell array of lidarScan objects. The lidar scans were collected in a parking garage on a Husky® robot from ClearPath Robotics®. Typically, lidar scans are taken at a high frequency and each scan is not needed for SLAM. Therefore, down sample the scans by selecting only every 40th scan.

```
load garage_fll_southend.mat scans
scans = scans(1:40:end);
```

To set up the SLAM algorithm, specify the lidar range, map resolution, loop closure threshold, and search radius. Tune these parameters for your specific robot and environment. Create the lidarSLAM object with these parameters.

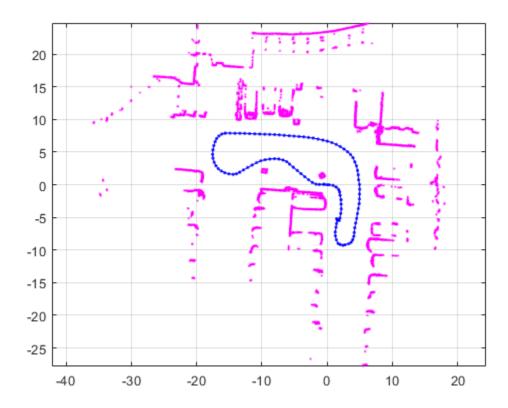
```
maxRange = 19.2; % meters
resolution = 10; % cells per meter

slamObj = lidarSLAM(resolution,maxRange);
slamObj.LoopClosureThreshold = 360;
slamObj.LoopClosureSearchRadius = 8;
```

Add Scans Iteratively

Using a for loop, add scans to the SLAM object. The object uses scan matching to compare each added scan to previously added ones. To improve the map, the object optimizes the pose graph whenever it detects a loop closure. Every 10 scans, display the stored poses and scans.

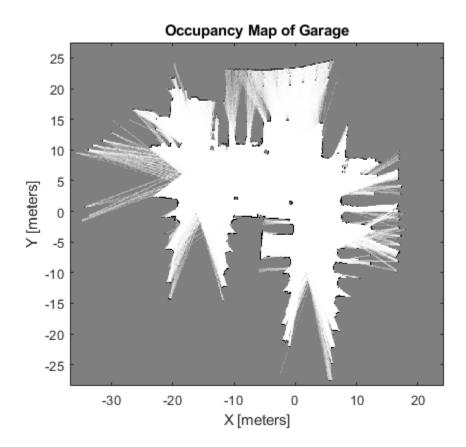
```
for i = 1:numel(scans)
   addScan(slamObj,scans{i});
   if rem(i,10) == 0
       show(slamObj);
   end
end
```



View Occupancy Map

After adding all the scans to the SLAM object, build an occupancyMap map by calling buildMap with the scans and poses. Use the same map resolution and max range you used with the SLAM object.

```
[scansSLAM,poses] = scansAndPoses(slamObj);
occMap = buildMap(scansSLAM,poses,resolution,maxRange);
figure
show(occMap)
title('Occupancy Map of Garage')
```



Input Arguments

slam0bj — Lidar SLAM object

lidarSLAM object

Lidar SLAM object, specified as a lidarSLAM object. The object contains the SLAM algorithm parameters, sensor data, and underlying pose graph used to build the map.

currScan — Lidar scan reading

lidarScan object

Lidar scan reading, specified as a lidarScan object. This scan is correlated to the most recent scan in slamObj using scan matching.

relPoseEst — Relative pose estimate of scan

[x v theta] vector

Relative pose estimate of scan, specified as an $[x \ y \ theta]$ vector. This relative pose improves scan matching.

Output Arguments

isAccepted — Indicates if scan is accepted

true | false

Indicates if scan is accepted, returned as true or false. If the relative pose between scans is below the MovementThreshold property of slamObj, the scan is rejected. By default, all scans are accepted.

loopClosureInfo — Loop closure details

structure

Loop closure details, returned as a structure with these fields:

- EdgeIDs -- IDs of newly connected edges in the pose graph, returned as a vector.
- Edges -- Newly added loop closure edges, returned as an *n*-by-2 matrix of node IDs that each edge connects.
- Scores -- Scores of newly connected edges in the pose graph returned from scan matching, returned as a vector.

Note If the LoopClosureAutoRollback property is set to true in slam0bj, loop closure edges can be removed from the pose graph. This property rejects loops closures if the residual error changes drastically after optimization. Therefore, some of the edge IDs listed in this structure may not exist in the actual pose graph.

optimInfo — Pose graph optimization details

structure

Pose graph optimization details, returned as a structure with these fields:

- IsPerformed -- Boolean indicating if optimization is performed when adding this scan. Optimization performance depends on the OptimizationInterval property in slamObj.
- IsAccepted -- Boolean indicating if optimization was accepted based on ResidualError.
- ResidualError -- Error associated with optimization, returned as a scalar.
- LoopClosureRemoved -- List of IDs of loop closure edges removed during optimization, returned as a vector.

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

Use this syntax when constructing lidarSLAM objects for code generation:

slamObj= lidarSLAM(mapResolution, maxLidarRange, maxNumScans) specifies the upper bound on the number of accepted scans allowed when generating code. maxNumScans is a positive integer. This scan limit is only required when generating code.

See Also

optimizePoseGraph | poseGraph

Topics

"Implement Simultaneous Localization And Mapping (SLAM) with Lidar Scans" "Implement Online Simultaneous Localization And Mapping (SLAM) with Lidar Scans"

Introduced in R2019b

copy

Copy lidar SLAM object

Syntax

newSlamObj = copy(slamObj)

Description

newSlamObj = copy(slamObj) creates a deep copy of slamObj with the same properties. Any
changes made to newSlamObj are not reflected in slamObj.

Input Arguments

slamObj — Lidar SLAM object

lidarSLAM object

Lidar SLAM object, specified as a lidarSLAM object. The object contains the SLAM algorithm parameters, sensor data, and underlying pose graph used to build the map.

Output Arguments

newSlamObj — Lidar SLAM object

lidarSLAM object

Lidar SLAM object, returned as a lidarSLAM object.

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

Use this syntax when constructing lidarSLAM objects for code generation:

slamObj = lidarSLAM(mapResolution, maxLidarRange, maxNumScans) specifies the upper bound on the number of accepted scans allowed when generating code. maxNumScans is a positive integer. This scan limit is only required when generating code.

See Also

optimizePoseGraph | poseGraph

Topics

"Implement Simultaneous Localization And Mapping (SLAM) with Lidar Scans"

Introduced in R2019b

[&]quot;Implement Online Simultaneous Localization And Mapping (SLAM) with Lidar Scans"

removeLoopClosures

Remove loop closures from pose graph

Syntax

```
removeLoopClosures(slamObj)
removeLoopClosures(slamObj,lcEdgeIDs)
```

Description

removeLoopClosures(slamObj) removes all loop closures from the underlying pose graph in slamObj.

removeLoopClosures(slamObj,lcEdgeIDs) removes the loop closure edges with the specified IDs from the underlying pose graph in slamObj.

Input Arguments

slamObj — Lidar SLAM object

lidarSLAM object

Lidar SLAM object, specified as a lidarSLAM object. The object contains the SLAM algorithm parameters, sensor data, and underlying pose graph used to build the map

lcEdgeIDs — Loop closure edge IDs

vector of positive integers

Loop closure edge IDs, specified as a vector of positive integers. To find specific edge IDs, use findEdgeID on the underlying poseGraph object defined in slamObj.

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

Use this syntax when constructing lidarSLAM objects for code generation:

slamObj= lidarSLAM(mapResolution, maxLidarRange, maxNumScans) specifies the upper bound on the number of accepted scans allowed when generating code. maxNumScans is a positive integer. This scan limit is only required when generating code.

See Also

optimizePoseGraph | poseGraph

Topics

- "Implement Simultaneous Localization And Mapping (SLAM) with Lidar Scans"
- "Implement Online Simultaneous Localization And Mapping (SLAM) with Lidar Scans"

Introduced in R2019b

scansAndPoses

Extract scans and corresponding poses

Syntax

```
[scans,poses] = scansAndPoses(slamObj)
[scans,poses] = scansAndPoses(slamObj,nodeIDs)
```

Description

[scans,poses] = scansAndPoses(slamObj) returns the scans used by the lidarSLAM object as lidarScan objects, along with their associated [x y theta] poses from the underlying pose graph of slamObj.

[scans,poses] = scansAndPoses(slamObj,nodeIDs) returns the scans and poses for the specific node IDs. To get the node IDs, see the underlying poseGraph object in slamObj for the node IDs.

Examples

Perform SLAM Using Lidar Scans

Use a lidarSLAM object to iteratively add and compare lidar scans and build an optimized pose graph of the robot trajectory. To get an occupancy map from the associated poses and scans, use the buildMap function.

Load Data and Set Up SLAM Algorithm

Load a cell array of lidarScan objects. The lidar scans were collected in a parking garage on a Husky® robot from ClearPath Robotics®. Typically, lidar scans are taken at a high frequency and each scan is not needed for SLAM. Therefore, down sample the scans by selecting only every 40th scan.

```
load garage_fll_southend.mat scans
scans = scans(1:40:end);
```

To set up the SLAM algorithm, specify the lidar range, map resolution, loop closure threshold, and search radius. Tune these parameters for your specific robot and environment. Create the lidarSLAM object with these parameters.

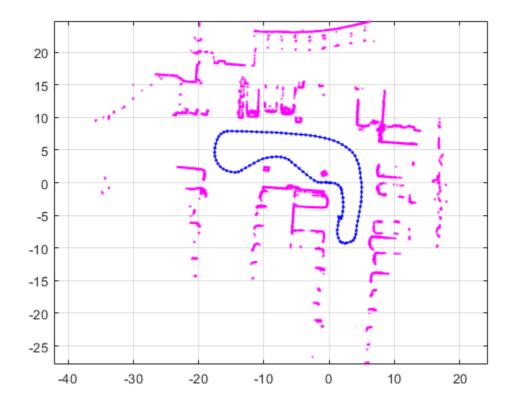
```
maxRange = 19.2; % meters
resolution = 10; % cells per meter

slamObj = lidarSLAM(resolution, maxRange);
slamObj.LoopClosureThreshold = 360;
slamObj.LoopClosureSearchRadius = 8;
```

Add Scans Iteratively

Using a for loop, add scans to the SLAM object. The object uses scan matching to compare each added scan to previously added ones. To improve the map, the object optimizes the pose graph whenever it detects a loop closure. Every 10 scans, display the stored poses and scans.

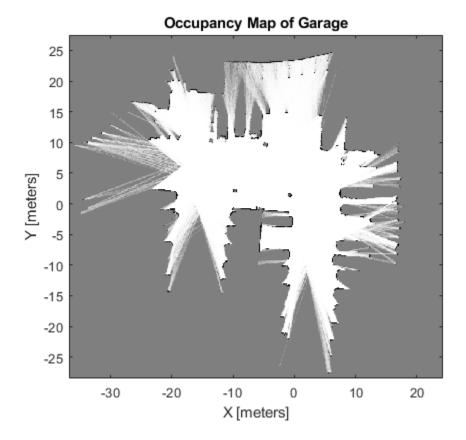
```
for i = 1:numel(scans)
    addScan(slamObj,scans{i});
    if rem(i,10) == 0
        show(slamObj);
    end
end
```



View Occupancy Map

After adding all the scans to the SLAM object, build an occupancyMap map by calling buildMap with the scans and poses. Use the same map resolution and max range you used with the SLAM object.

```
[scansSLAM,poses] = scansAndPoses(slamObj);
occMap = buildMap(scansSLAM,poses,resolution,maxRange);
figure
show(occMap)
title('Occupancy Map of Garage')
```



Input Arguments

slam0bj — Lidar SLAM object

lidarSLAM object

Lidar SLAM object, specified as a lidarSLAM object. The object contains the SLAM algorithm parameters, sensor data, and underlying pose graph used to build the map.

nodeIDs — Node IDs from pose graph

positive integer

Node IDs from pose graph, specified as a positive integer. Nodes are added to the pose graph with sequential ID numbers. To get the node IDs, see the underlying poseGraph object in slamObj for the node IDs.

Output Arguments

scans — Lidar scan readings

lidarScan object

Lidar scan readings, returned as a lidarScan object.

poses — Pose for each scan

n-by-3 matrix | [x y theta] vectors

Pose for each scan, returned as an n-by-3 matrix of [x y theta] vectors. Each row is a pose that corresponds to a scan in scans.

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

Use this syntax when constructing lidarSLAM objects for code generation:

slamObj= lidarSLAM(mapResolution, maxLidarRange, maxNumScans) specifies the upper bound on the number of accepted scans allowed when generating code. maxNumScans is a positive integer. This scan limit is only required when generating code.

See Also

optimizePoseGraph | poseGraph

Topics

"Implement Simultaneous Localization And Mapping (SLAM) with Lidar Scans"

"Implement Online Simultaneous Localization And Mapping (SLAM) with Lidar Scans"

Introduced in R2019b

show

Plot scans and robot poses

Syntax

```
show(slamObj)
show(slamObj,Name,Value)
axes = show( )
```

Description

show(slamObj) plots all the scans added to the input lidarSLAM object overlaid with the lidar poses in its underlying pose graph.

```
show(slamObj, Name, Value) specifies options using Name, Value pair arguments. For example,
"Poses", "off" turns off display of the underlying pose graph in slamObj.
```

axes = show(____) returns the axes handle that the lidar SLAM data is plotted to using any of the
previous syntaxes.

Examples

Perform SLAM Using Lidar Scans

Use a lidarSLAM object to iteratively add and compare lidar scans and build an optimized pose graph of the robot trajectory. To get an occupancy map from the associated poses and scans, use the buildMap function.

Load Data and Set Up SLAM Algorithm

Load a cell array of lidarScan objects. The lidar scans were collected in a parking garage on a Husky® robot from ClearPath Robotics®. Typically, lidar scans are taken at a high frequency and each scan is not needed for SLAM. Therefore, down sample the scans by selecting only every 40th scan.

```
load garage_fll_southend.mat scans
scans = scans(1:40:end);
```

To set up the SLAM algorithm, specify the lidar range, map resolution, loop closure threshold, and search radius. Tune these parameters for your specific robot and environment. Create the lidarSLAM object with these parameters.

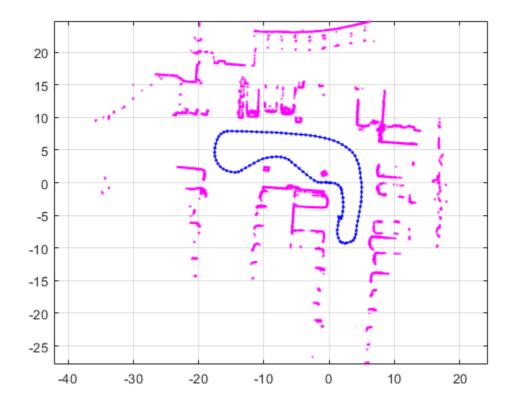
```
maxRange = 19.2; % meters
resolution = 10; % cells per meter

slamObj = lidarSLAM(resolution,maxRange);
slamObj.LoopClosureThreshold = 360;
slamObj.LoopClosureSearchRadius = 8;
```

Add Scans Iteratively

Using a for loop, add scans to the SLAM object. The object uses scan matching to compare each added scan to previously added ones. To improve the map, the object optimizes the pose graph whenever it detects a loop closure. Every 10 scans, display the stored poses and scans.

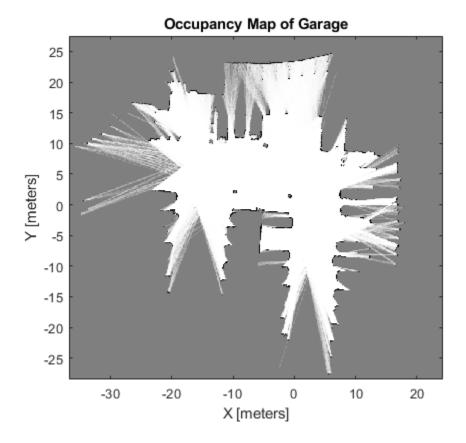
```
for i = 1:numel(scans)
    addScan(slamObj,scans{i});
    if rem(i,10) == 0
        show(slamObj);
    end
end
```



View Occupancy Map

After adding all the scans to the SLAM object, build an occupancyMap map by calling buildMap with the scans and poses. Use the same map resolution and max range you used with the SLAM object.

```
[scansSLAM,poses] = scansAndPoses(slamObj);
occMap = buildMap(scansSLAM,poses,resolution,maxRange);
figure
show(occMap)
title('Occupancy Map of Garage')
```



Input Arguments

slamObj — Lidar SLAM object

lidarSLAM object

Lidar SLAM object, specified as a lidarSLAM object. The object contains the SLAM algorithm parameters, sensor data, and underlying pose graph used to build the map.

Name-Value Pair Arguments

Specify optional comma-separated pairs of Name, Value arguments. Name is the argument name and Value is the corresponding value. Name must appear inside quotes. You can specify several name and value pair arguments in any order as Name1, Value1, . . . , NameN, ValueN.

Example: "Poses", "off"

Parent — Axes used to plot pose graph

Axes object | UIAxes object

Axes used to plot the pose graph, specified as the comma-separated pair consisting of "Parent" and either an Axes or UIAxes object. See axes or uiaxes.

Poses — Display lidar poses

"on" (default) | "off"

Display lidar poses, specified as the comma-separated pair consisting of "Poses" and "on" or "off".

Output Arguments

axes — Axes used to plot the map

Axes object | UIAxes object

Axes used to plot the map, returned as either an Axes or UIAxes object. See axes or uiaxes.

See Also

optimizePoseGraph | poseGraph

Topics

"Implement Simultaneous Localization And Mapping (SLAM) with Lidar Scans"

"Implement Online Simultaneous Localization And Mapping (SLAM) with Lidar Scans"

Introduced in R2019b

likelihoodFieldSensorModel

Create a likelihood field range sensor model

Description

The likelihoodFieldSensor object creates a likelihood field sensor model object for range sensors. This object contains specific sensor model parameters. You can use this object to specify the model parameters in a monteCarloLocalization object.

Creation

Syntax

lf = likelihoodFieldSensorModel

Description

lf = likelihoodFieldSensorModel creates a likelihood field sensor model object for range sensors.

Properties

Map — Occupancy grid representing the map

binaryOccupancyMap object (default)

Occupancy grid representing the map, specified as a binaryOccupancyMap object. This object represents the environment of the vehicle as a grid with binary values indicating obstacles as true (1) and free locations as false (0).

SensorPose — Pose of the range sensor relative to the vehicle

[0 0 0] (default) | three-element vector

Pose of the range sensor relative to the coordinate frame of the vehicle, specified as a three-element vector, [x y theta].

SensorLimits — Minimum and maximum range of sensor

[0 12] (default) | two-element vector

Minimum and maximum range of sensor, specified as a two-element vector in meters.

NumBeams — Number of beams used for likelihood computation

60 (default) | scalar

Number of beams used for likelihood computation, specified as a scalar. The computation efficiency can be improved by specifying a smaller number of beams than the actual number available from the sensor.

MeasurementNoise — Standard deviation for measurement noise

0.2 (default) | scalar

Standard deviation for measurement noise, specified as a scalar.

RandomMeasurementWeight — Weight for probability of random measurement 0.05 (default) | scalar

Weight for probability of random measurement, specified as a scalar. This scalar is the probability that the measurement is not accurate due to random interference.

ExpectedMeasurementWeight — Weight for probability of expected measurement 0.95 (default) | scalar

Weight for probability of expected measurement, specified as a scalar. The weight is the probability of getting a correct range measurement within the noise limits specified in MeasurementNoise property.

MaxLikelihoodDistance — Maximum distance to find nearest obstacles

2.0 (default) | scalar

Maximum distance to find nearest obstacles, specified as a scalar in meters.

Limitations

If you change your sensor model after using it with the monteCarloLocalization object, call release on that object beforehand. For example:

```
mcl = monteCarloLocalization;
[isUpdated,pose,covariance] = mcl(ranges,angles);
release(mcl)
mcl.SensorModel.NumBeams = 120;
```

See Also

monteCarloLocalization | odometryMotionModel

Topics

"Localize TurtleBot Using Monte Carlo Localization"

"Monte Carlo Localization Algorithm"

Introduced in R2019b

magparams

Magnetometer sensor parameters

Description

The magparams class creates a magnetometer sensor parameters object. You can use this object to model a magnetometer when simulating an IMU with imuSensor.

Creation

Syntax

```
params = magarams
params = magparams(Name, Value)
```

Description

params = magarams returns an ideal magnetometer sensor parameters object with default values.

params = magparams(Name, Value) configures magparams object properties using one or more Name, Value pair arguments. Name is a property name and Value is the corresponding value. Name must appear inside single quotes (''). You can specify several name-value pair arguments in any order as Name1, Value1, ..., NameN, ValueN. Any unspecified properties take default values.

Properties

MeasurementRange — Maximum sensor reading (μT)

Inf (default) | real positive scalar

Maximum sensor reading in µT, specified as a real positive scalar.

Data Types: single | double

Resolution — Resolution of sensor measurements (μ T/LSB)

0 (default) | real nonnegative scalar

Resolution of sensor measurements in uT/LSB, specified as a real nonnegative scalar

Data Types: single | double

ConstantBias — Constant sensor offset bias (µT)

```
[0 0 0] (default) | real scalar | real 3-element row vector
```

Constant sensor offset bias in μT , specified as a real scalar or 3-element row vector. Any scalar input is converted into a real 3-element row vector where each element has the input scalar value.

Data Types: single | double

AxesMisalignment — Sensor axes skew (%)

[0 0 0] (default) | real scalar in the range [0,100] | real 3-element row vector in the range [0,100]

Sensor axes skew in %, specified as a real scalar or 3-element row vector with values ranging from 0 to 100. Any scalar input is converted into a real 3-element row vector where each element has the input scalar value.

Data Types: single | double

NoiseDensity — Power spectral density of sensor noise ($\mu T/\sqrt{Hz}$)

[0 0 0] (default) | real scalar | real 3-element row vector

Power spectral density of sensor noise in $\mu T/\sqrt{Hz}$, specified as a real scalar or 3-element row vector. Any scalar input is converted into a real 3-element row vector where each element has the input scalar value.

Data Types: single | double

BiasInstability — Instability of the bias offset (μ T)

[0 0 0] (default) | real scalar | real 3-element row vector

Instability of the bias offset in μT , specified as a real scalar or 3-element row vector. Any scalar input is converted into a real 3-element row vector where each element has the input scalar value.

Data Types: single | double

RandomWalk — Integrated white noise of sensor ($\mu T/\sqrt{Hz}$)

[0 0 0] (default) | real scalar | real 3-element row vector

Integrated white noise of sensor in ($\mu T/\sqrt{Hz}$), specified as a real scalar or 3-element row vector. Any scalar input is converted into a real 3-element row vector where each element has the input scalar value.

Data Types: single | double

TemperatureBias — Sensor bias from temperature (μT/°C)

[0 0 0] (default) | real scalar | real 3-element row vector

Sensor bias from temperature in (μ T/°C), specified as a real scalar or 3-element row vector. Any scalar input is converted into a real 3-element row vector where each element has the input scalar value.

Data Types: single | double

TemperatureScaleFactor — Scale factor error from temperature (%/°C)

[0 0 0] (default) | real scalar in the range [0,100] | real 3-element row vector in the range [0,100]

Scale factor error from temperature in (%/°C), specified as a real scalar or 3-element row vector with values ranging from 0 to 100. Any scalar input is converted into a real 3-element row vector where each element has the input scalar value.

Data Types: single | double

Examples

Generate Magnetometer Data from Stationary Inputs

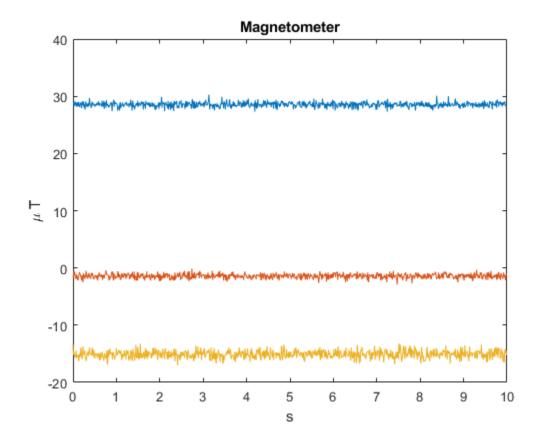
Generate magnetometer data for an imuSensor object from stationary inputs.

Generate a magnetometer parameter object with a maximum sensor reading of 1200 μT and a resolution of 0.1 $\mu T/LSB$. The constant offset bias is 1 μT . The sensor has a power spectral density of $\left(\frac{[0.6\ 0.6\ 0.9]}{\sqrt{100}}\right)\mu T/\sqrt{Hz}$. The bias from temperature is [0.8 0.8 2.4] $\mu T/^0C$. The scale factor error from temperature is 0.1 %/0C.

```
params = magparams('MeasurementRange',1200,'Resolution',0.1,'ConstantBias',1,'NoiseDensity',[0.6
```

Use a sample rate of 100 Hz spaced out over 1000 samples. Create the imuSensor object using the magnetometer parameter object.

```
Fs = 100;
numSamples = 1000;
t = 0:1/Fs:(numSamples-1)/Fs;
imu = imuSensor('accel-mag','SampleRate', Fs, 'Magnetometer', params);
Generate magnetometer data from the imuSensor object.
orient = quaternion.ones(numSamples, 1);
acc = zeros(numSamples, 3);
angvel = zeros(numSamples, 3);
[~, magData] = imu(acc, angvel, orient);
Plot the resultant magnetometer data.
plot(t, magData)
title('Magnetometer')
xlabel('s')
ylabel('\mu T')
```



Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder $^{\text{\tiny TM}}$.

See Also

accelparams|gyroparams|imuSensor

Introduced in R2018b

mapLayer

Create map layer for N-dimensional data

Description

The mapLayer object creates an *N*-dimensional grid map, where the first two dimensions determine the footprint of the map, and all subsequent dimensions dictate the size and layout of the data stored in each cell. For storing scalar binary or probability values for a grid map, use the binaryOccupancyMap or occupancyMap objects instead.

A map layer stores data for grid cells that represent a discretized region of space. To query and update data using world, local, or grid coordinates, use the getMapData and setMapData object functions. Each grid cell in the map can store data of any size from a single a value to a multi-dimensional array. For more information, see the DataSize property.

Layer behavior can also be customized by providing function handles during creation using the GetTransformFcn and SetTransformFcn properties.

Creation

Syntax

```
map = mapLayer
map = mapLayer(p)
map = mapLayer(width,height)
map = mapLayer(rows,cols,'grid')
map = mapLayer(width,height,cellDims)
map = mapLayer(rows,cols,cellDims,'grid')
map = mapLayer(sourceMap)
map = mapLayer(____,Name,Value)
```

Description

map = mapLayer creates an empty map object occupying 10-by-10 meters of space with a resolution
of 1 cell per meter.

map = mapLayer(p) creates a map from the values in the matrix or matrix array p. For 3-D matrix arrays, each cell in the map is filled with the vector of values at each grid location along the third dimension of the array. For an N-by-D matrix array, each cell contains a matrix (N=4) or a matrix array (N>4) of data for that grid location.

map = mapLayer(width,height) creates a map covering the specified width and height with a resolution of 1 cell per meter.

map = mapLayer(rows,cols,'grid') creates a map with a grid size of rows,cols with a
resolution of 1 cell per meter.

map = mapLayer(width,height,cellDims) creates the map where the size of the data stored in each cell is defined by the array of integers cellDims.

map = mapLayer(rows, cols, cellDims, 'grid') creates a map with a grid size of rowscols
where the size of the data stored in each cell is defined by the array of integers cellDims.

map = mapLayer(sourceMap) creates a new object using the layers copied from another
mapLayer object.

For example, mapLayer(___, 'LocalOriginInWorld',[15 20]) sets the local origin to a specific world location.

Properties

DataSize — Size of the N-dimensional data matrix

[10 10] (default) | vector of integers

Size of the *N*-dimensional data matrix, specified as vector of integers. The first two dimensions define the footprint of the map, and all subsequent dimensions dictate the size and layout of the data stored in each cell. The default value assumes a single value is stored for each cell in a 10-by-10 grid.

If the map stores an n-element vector of values in each cell, this property would be [width height n].

If the map stores a 10-by-10 grid with each cell containing a 3-by-3-by-3 matrix array, the data size would be [10 10 3 3 3].

This property is set when you create the object based on the dimensions of the input matrix p or the inputs width, height, and cellDims.

After you create the object, this property is read-only.

Data Types: double

DataType — Data type of the values stored

'double' (default) | character vector

Data type of the values stored in the map, specified as a character vector.

This property is set based on the data type of the input p or the data type of DefaultValue. After you create the object, this property is read-only.

Data Types: char

DefaultValue — Default value for unspecified map locations

0 (default) | numeric scalar

Default value for unspecified map locations including areas outside the map, specified as a numeric scalar.

If you specify the GetTransformFcn or SetTransformFcn property when creating the object, the default value is updated based on that transformation function. If you create the map with a matrix of values p, the transform function modifies the values before storing.

Data Types: double

GetTransformFcn — Applies transformations to retrieved values

function handle

Applies transformations to values retrieved by the getMapData function, specified as a function handle.

This function handle is called inside the **getMapData** object function. It can be used to apply a transformation to values retrieved from the map layer. The function definition must have the following format:

modifiedValues = getTransformFcnHandle(map,values,varargin)

The size of the output modifiedValues must match the size of the input values. The function provides all map data accessed from the getMapData object function to this transform function through the varargin inputs.

You can set this property when you create the object. After you create the object, this property is read-only.

Data Types: function_handle

GridLocationInWorld — Location of the grid in local coordinates

[0 0] (default) | two-element vector | [xWorld yWorld]

Location of the bottom-left corner of the grid in world coordinates, specified as a two-element vector, [xWorld yWorld].

You can set this property when you create the object.

Data Types: double

GridOriginInLocal — Location of the grid in local coordinates

[0 0] (default) | two-element vector | [xLocal yLocal]

Location of the bottom-left corner of the grid in local coordinates, specified as a two-element vector, [xLocal yLocal].

You can set this property when you create the object.

Data Types: double

GridSize — Number of rows and columns in grid

two-element integer-valued vector

Number of rows and columns in grid, stored as a 1-by-2 real-valued vector representing the number of rows and columns, in that order.

This property is set when you create the object based on the first two dimensions of the input matrix p, the inputs width and height, or the inputs row and col.

Data Types: double

LayerName — **Name** of layer

'mapLayer' (default) | character vector | string scalar

Name of map layer, specified as a character vector or string scalar.

You can set this property when you create the object. After you create the object, this property is read-only.

Data Types: double

LocalOriginInWorld — Location of the local frame in world coordinates

```
[0 0] (default) | two-element vector | [xWorld yWorld]
```

Location of the origin of the local frame in world coordinates, specified as a two-element vector, [xLocal yLocal]. Use the move function to shift the local frame as your vehicle moves.

You can set this property when you create the object.

Data Types: double

Resolution — Grid resolution

1 (default) | scalar

This property is read-only.

Grid resolution, stored as a scalar in cells per meter representing the number and size of grid locations.

You can set this property when you create the object. After you create the object, this property is read-only.

Data Types: double

SetTransformFcn — Applies transformations to set values

function handle

Applies transformations to values set by the setMapData function, specified as a function handle.

This function handle is called inside the **setMapData** object function. It can be used to apply a transformation to values set in the map layer. The function must have the following syntax:

```
modifiedValues = setTransformFcnHandle(map,values,varargin)
    if numel(varargin) == 0
        return; %
    else
        % Custom Code
    end
end
```

The size of the output, modifiedValues, must match the size of the input, values. The function provides all map data specified in the setMapData object function to this transform function. When creating this object without starting values, the function is called without additional input arguments, so specify an if-statement to return when the number of elements in varagin is zero.

You can set this property when you create the object. After you create the object, this property is read-only.

Data Types: function handle

XLocalLimits — Minimum and maximum values of x-coordinates in local frame

two-element vector

This property is read-only.

Minimum and maximum values of x-coordinates in local frame, stored as a two-element horizontal vector of the form [min max]. Local frame is defined by LocalOriginInWorld property.

Data Types: double

YLocalLimits — Minimum and maximum values of y-coordinates in local frame

two-element vector

This property is read-only.

Minimum and maximum values of y-coordinates in local frame, stored as a two-element horizontal vector of the form [min_max]. Local frame is defined by LocalOriginInWorld property.

Data Types: double

XWorldLimits — Minimum and maximum world range values of x-coordinates

two-element vector

This property is read-only.

Minimum and maximum world range values of x-coordinates, stored as a 1-by-2 vector representing the minimum and maximum values, in that order.

Data Types: double

YWorldLimits — Minimum and maximum world range values of y-coordinates

two-element vector

This property is read-only.

Minimum and maximum world range values of y-coordinates, stored as a 1-by-2 vector representing the minimum and maximum values, in that order.

Data Types: double

Object Functions

getMapData Retrieve data from map layer

grid2local Convert grid indices to local coordinates Convert grid indices to world coordinates grid2world local2grid Convert local coordinates to grid indices Convert local coordinates to world coordinates local2world

move Move map in world frame Assign data to map layer setMapData

syncWith Sync map with overlapping map

Convert world coordinates to grid indices world2grid world2local Convert world coordinates to local coordinates

Examples

Store and Modify XY Velocities Using A Single Map Layer

Create a map layer that stores two values per grid location as xy-velocities.

Create an m-by-n-by-2 matrix of values. The first element in the third dimension is dx and the second is dy as velocities.

```
dXY = reshape(1:200,10,20);

dXY(:,:,2) = dXY;
```

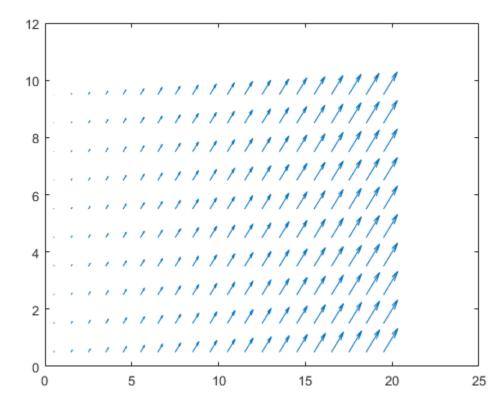
Create a map layer from the matrix. Specify the resolution and layer name.

```
vLayer = mapLayer(dXY, 'Resolution', 1, 'LayerName', 'dXY');
```

Get all the map data out as a matrix. Get the xy-locations of the velocity values by creating arrays that cover the minimum and maximum xy-world limits and is shifted to the grid-center locations. The y-locations are flipped when converting between matrix to world coordinates. Visualize the velocities corresponding to those grid-center locations using the quiver function.

```
v = getMapData(vLayer);

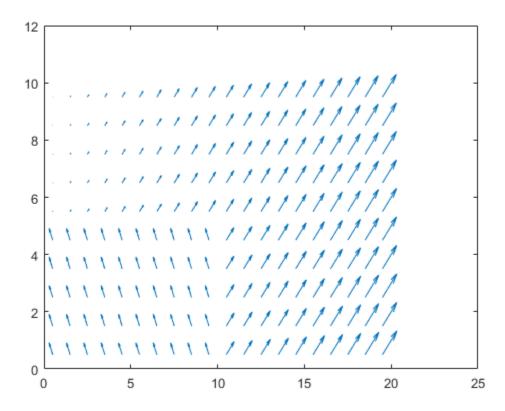
R = 1/(2*vLayer.Resolution);
xLim = vLayer.XWorldLimits;
yLim = vLayer.YWorldLimits;
xLoc = (xLim(1)+R):R*2:(xLim(2)-R);
yLoc = (yLim(2)-R):-R*2:(yLim(1)+R);
quiver(xLoc,yLoc,v(:,:,1),v(:,:,2))
```



Set the bottom-left quadrant to new updated values. Create the values as a matrix and specify the bottom-left corner (0,0) in map coordinates to the setData function.

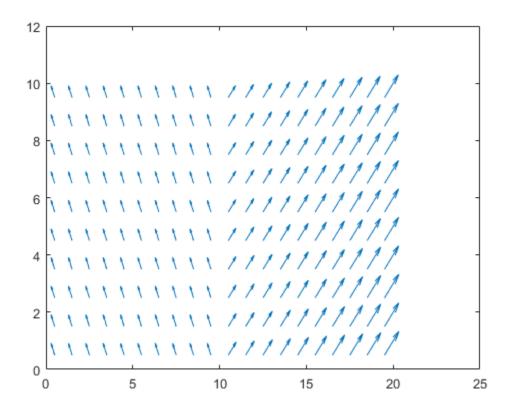
```
updateValues = repmat(reshape([-50,100],[1 1 2]),5,10);
setMapData(vLayer,[0 0],updateValues)
```

```
v = getMapData(vLayer);
quiver(xLoc,yLoc,v(:,:,1),v(:,:,2))
```



Set new values for the top-left quadrant using grid coordinates. For maps, the top-left grid location is (1,1).

```
setMapData(vLayer,[1 1],updateValues,'grid')
v = getMapData(vLayer);
quiver(xLoc,yLoc,v(:,:,1),v(:,:,2))
```



Write Custom Transform Functions for Map Layers

The mapLayer object enables you to apply custom element-wise transformations when setting and getting data in the map. To transform data you set or get from the map, specify function handles for the GetTransfomFcn and SetTransformFcn properties. This example shows how to implement a log-odds probabilitistic map layer by creating a lookup table for probability and log-odds values. The transform functions use these lookup tables to convert between these values when setting or getting data.

Create Lookup Tables

Generate a full lookup table of values that map the probability values to the minimum and maximum limits of int16 values.

Create an array of int16 values from intmin to intmax. Define the probablilty limits.

```
intType = 'int16';
intLinSpace = intmin(intType):intmax(intType);
numOfPoints = length(intLinSpace);
probLimits = [0.001 .999];
```

The exampleHelperProbToLogodds and examplerHelperLogoddsToProb functions covert between the log-odds and probability values. Use the helper functions to get the log-odds limits and

generate the array for looking up log-odds values. Create an interpolated grid for the entire lookup table.

```
logOddsLimits = exampleHelperProbToLogodds([0.001 .999]);
logOddsLookup = single(exampleHelperLogoddsToProb(linspace(logOddsLimits(1),logOddsLimits(2),numlinterpTable = griddedInterpolant(logOddsLookup,single(intLinSpace),'nearest');
```

Specify Transform Function Handles

The transform function handles utilize example helpers that define how to convert between log-odds integer values and the probability values with an applied saturation limit. The probability saturation limits are [0.001 .999] as previously specified. This behavior is similar to the occupancyMap object.

```
getXformFcn = @(obj,logodds,varargin)...
    exampleHelperIntLogoddsToProb(logodds,logOddsLookup(:),intLinSpace);
setXformFcn = @(obj,prob,varargin)...
    exampleHelperProbToIntLogodds(prob,interpTable,logOddsLookup(:),intLinSpace,probLimits);
```

Create Map Layer

Generate an occupancy map layer object from a matrix of probability values. Specify the get and set transform functions.

Notice that when you create the map, the default value is 0.001 instead of 0. This difference is because the SetTransformFcn function has been applied to the default value of 0 when you create the object, which saturates the value to 0.001.

```
disp(occupancyLayer.DefaultValue)
```

Get and Set Map Data

0.0010

The map data matches the matrix you set on creation.

```
extData = getMapData(occupancyLayer)
extData = 10 \times 10
    0.5000
               0.5000
                         0.5000
                                    0.5000
                                               0.5000
                                                          0.5000
                                                                     0.5000
                                                                                0.5000
                                                                                          0.5000
                                               0.5000
              0.5000
                         0.5000
                                                          0.5000
                                                                     0.5000
                                                                                          0.5000
    0.5000
                                    0.5000
                                                                                0.5000
    0.5000
              0.5000
                                               0.5000
                                                                                0.5000
                                                                                          0.5000
                         0.5000
                                    0.5000
                                                          0.5000
                                                                     0.5000
```

0.5000 0.5000 0.5000 0.5000 0.5000 0.5000 0. 0.5000 0.5000 0.5000 0.5000 0.5000 0.5000 0.5000 0.5000 0.5000 0.5000 0.5000 0.5000 0. 0.5000 0.5000 0.5000 0.5000 0.5000 0. 0.5000 0.5000 0.5000 0.5000 0.5000 0.5000 0.5000 0.5000 0.5000 0.5000 0.5000 0.5000 0.5000 0. 0.5000 0.5000 0.5000 0.5000 0.5000 0.5000 0.5000 0.5000 0. 0.5000 0. 0.5000 0.5000 0.5000 0.5000 0.5000 0.5000 0.5000 0.5000 0.5000 0.5000 0.5000 0.5000 0.5000 0.5000 0.5000 0.5000 0.5000 0.5000 0.

Set specific map locations to values that are:

0.

0.

0.

- Outside of the probability saturation limits.
- Higher precision than the resolution of the lookup tables.

```
setMapData(occupancyLayer,[0 0],0.00001)
setMapData(occupancyLayer,[5 5],0.25999)
```

For the first location, the probability is bound to the saturation limits.

```
extData = getMapData(occupancyLayer,[0 0])
extData = 0.0010
```

The second location returns the value closest to the probability value in the lookup table.

```
extData2 = getMapData(occupancyLayer,[5 5])
extData2 = 0.2600
```

The generated map layer can now be used for updating a probability occupany map that are stored as int16 values. To combine this map with other layers or map types, see the multiLayerMap object.

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

- The LayerName property must be fixed at compile-time
- The DataType property must be known at compile-time.

See Also

Objects

binaryOccupancyMap | multiLayerMap | occupancyMap | occupancyMap3D

Functions

getMapData | move | setMapData | syncWith

Topics

"Motion Planning in Urban Environments Using Dynamic Occupancy Grid Map" "Fuse Multiple Lidar Sensors Using Map Layers"

Introduced in R2021a

getMapData

Retrieve data from map layer

Syntax

```
mapData = getMapData(map)
mapData = getMapData(map,xy)
mapData = getMapData(map,xy,'local')
mapData = getMapData(map,ij,'grid')
[mapData,inBounds] = getMapData(____)

mapData = getMapData(map,bottomLeft,mapSize)
mapData = getMapData(map,bottomLeft,mapSize,'local')
mapData = getMapData(map,topLeft,gridSize,'grid')
```

Description

mapData = getMapData(map) returns a matrix of values that contains all the data for the given
map layer map.

mapData = getMapData(map,xy) returns an array of values for the given xy-locations in world coordinates.

mapData = getMapData(map,xy,'local') returns an array of values for the given xy-locations in local coordinates.

mapData = getMapData(map,ij,'grid') returns an array of values for the given ij-locations in grid coordinates. Each row of ij refers to a grid cell index [i j]

 $[mapData, inBounds] = getMapData(____)$ also returns a vector of logical values indicating whether the corresponding input location xy or ij is valid using the previous syntaxes.

mapData = getMapData(map, bottomLeft, mapSize) returns a matrix of values in a subregion of the map layer, map. The subregion starts in the bottom-left xy-position bottomLeft in world coordinates with a given map size mapSize specified as [width height] in meters.

mapData = getMapData(map,bottomLeft,mapSize,'local') specifies the bottom-left corner
of the subregion in local coordinates.

mapData = getMapData(map,topLeft,gridSize,'grid') specifies the top-left corner of the sub region in grid coordinates. The subregion size, gridSize is also given in grid coordinates as [rows cols].

Examples

Store and Modify XY Velocities Using A Single Map Layer

Create a map layer that stores two values per grid location as *xy*-velocities.

Create an m-by-n-by-2 matrix of values. The first element in the third dimension is dx and the second is dy as velocities.

```
dXY = reshape(1:200,10,20);
dXY(:,:,2) = dXY;
```

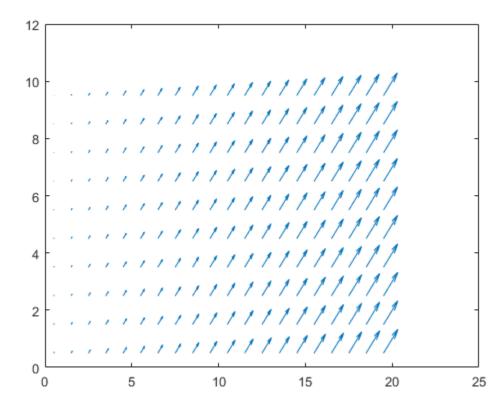
Create a map layer from the matrix. Specify the resolution and layer name.

```
vLayer = mapLayer(dXY, 'Resolution',1, 'LayerName', 'dXY');
```

Get all the map data out as a matrix. Get the xy-locations of the velocity values by creating arrays that cover the minimum and maximum xy-world limits and is shifted to the grid-center locations. The y-locations are flipped when converting between matrix to world coordinates. Visualize the velocities corresponding to those grid-center locations using the quiver function.

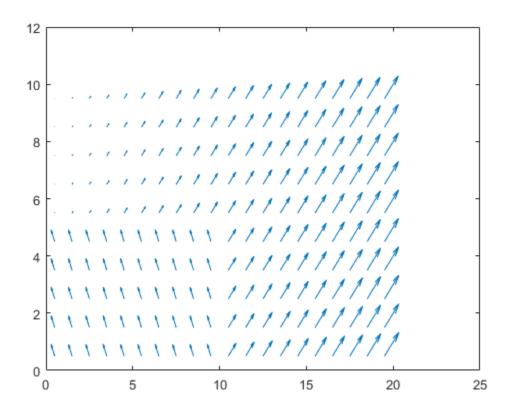
```
v = getMapData(vLayer);

R = 1/(2*vLayer.Resolution);
xLim = vLayer.XWorldLimits;
yLim = vLayer.YWorldLimits;
xLoc = (xLim(1)+R):R*2:(xLim(2)-R);
yLoc = (yLim(2)-R):-R*2:(yLim(1)+R);
quiver(xLoc,yLoc,v(:,:,1),v(:,:,2))
```



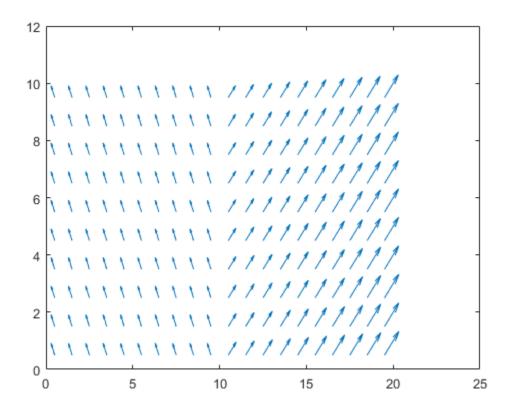
Set the bottom-left quadrant to new updated values. Create the values as a matrix and specify the bottom-left corner (0,0) in map coordinates to the setData function.

```
updateValues = repmat(reshape([-50,100],[1 1 2]),5,10);
setMapData(vLayer,[0 0],updateValues)
v = getMapData(vLayer);
quiver(xLoc,yLoc,v(:,:,1),v(:,:,2))
```



Set new values for the top-left quadrant using grid coordinates. For maps, the top-left grid location is (1,1).

```
setMapData(vLayer,[1 1],updateValues,'grid')
v = getMapData(vLayer);
quiver(xLoc,yLoc,v(:,:,1),v(:,:,2))
```



Write Custom Transform Functions for Map Layers

The mapLayer object enables you to apply custom element-wise transformations when setting and getting data in the map. To transform data you set or get from the map, specify function handles for the GetTransfomFcn and SetTransformFcn properties. This example shows how to implement a log-odds probabilitistic map layer by creating a lookup table for probability and log-odds values. The transform functions use these lookup tables to convert between these values when setting or getting data.

Create Lookup Tables

Generate a full lookup table of values that map the probability values to the minimum and maximum limits of int16 values.

Create an array of int16 values from intmin to intmax. Define the probablilty limits.

```
intType = 'int16';
intLinSpace = intmin(intType):intmax(intType);
numOfPoints = length(intLinSpace);
probLimits = [0.001 .999];
```

The exampleHelperProbToLogodds and examplerHelperLogoddsToProb functions covert between the log-odds and probability values. Use the helper functions to get the log-odds limits and

generate the array for looking up log-odds values. Create an interpolated grid for the entire lookup table.

```
logOddsLimits = exampleHelperProbToLogodds([0.001 .999]);
logOddsLookup = single(exampleHelperLogoddsToProb(linspace(logOddsLimits(1),logOddsLimits(2),numlinterpTable = griddedInterpolant(logOddsLookup,single(intLinSpace),'nearest');
```

Specify Transform Function Handles

The transform function handles utilize example helpers that define how to convert between log-odds integer values and the probability values with an applied saturation limit. The probability saturation limits are [0.001 .999] as previously specified. This behavior is similar to the occupancyMap object.

```
getXformFcn = @(obj,logodds,varargin)...
    exampleHelperIntLogoddsToProb(logodds,logOddsLookup(:),intLinSpace);
setXformFcn = @(obj,prob,varargin)...
    exampleHelperProbToIntLogodds(prob,interpTable,logOddsLookup(:),intLinSpace,probLimits);
```

Create Map Layer

Generate an occupancy map layer object from a matrix of probability values. Specify the get and set transform functions.

Notice that when you create the map, the default value is 0.001 instead of 0. This difference is because the SetTransformFcn function has been applied to the default value of 0 when you create the object, which saturates the value to 0.001.

```
disp(occupancyLayer.DefaultValue)
```

Get and Set Map Data

0.0010

0.5000

0.5000

0.5000

0.5000

0.5000

The map data matches the matrix you set on creation.

0.5000

0.5000

0.5000

0.5000

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0.5000

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0.5000

```
extData = getMapData(occupancyLayer)
extData = 10 \times 10
    0.5000
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                         0.5000
                                    0.5000
                                              0.5000
                                                         0.5000
                                                                    0.5000
                                                                               0.5000
                                                                                         0.5000
                                              0.5000
              0.5000
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```

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Set specific map locations to values that are:

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- Outside of the probability saturation limits.
- Higher precision than the resolution of the lookup tables.

```
setMapData(occupancyLayer,[0 0],0.00001)
setMapData(occupancyLayer,[5 5],0.25999)
```

For the first location, the probability is bound to the saturation limits.

```
extData = getMapData(occupancyLayer,[0 0])
extData = 0.0010
```

The second location returns the value closest to the probability value in the lookup table.

```
extData2 = getMapData(occupancyLayer,[5 5])
extData2 = 0.2600
```

The generated map layer can now be used for updating a probability occupany map that are stored as int16 values. To combine this map with other layers or map types, see the multiLayerMap object.

Input Arguments

map - Map layer

mapLayer object

Map layer, specified as a mapLayer object.

xy — World or local coordinates

n-by-2 matrix

World or local coordinates, specified as an n-by-2 matrix of $[x \ y]$ pairs, where n is the number of coordinates.

Data Types: double

ij - Grid positions

n-by-2 matrix

Grid positions, specified as an n-by-2 matrix of $[i \ j]$ pairs in $[rows \ cols]$ format, where n is the number of grid positions.

Data Types: double

bottomLeft — Location of output matrix in world or local coordinates

```
two-element vector | [xCoord yCoord]
```

Location of bottom left corner of output matrix in world or local coordinates, specified as a twoelement vector, [xCoord yCoord]. Location is in world or local coordinates based on syntax.

Data Types: double

mapSize — Subregion map size

two-element vector | [x y]

Subregion map size, specified as a two-element vector [x y] in world or local coordinates.

Data Types: double

gridSize — Output grid size

two-element vector | [row col]

Output grid size, specified as a two-element vector [row col].

Data Types: double

topLeft — Location of grid

two-element vector | [iCoord jCoord]

Location of top left corner of grid, specified as a two-element vector, [iCoord jCoord].

Data Types: double

Output Arguments

mapData — Data values from map layer

matrix

Data values from map layer, returned as a matrix. By default, the function returns all data on the layer as an M-by-N-by-DataDims matrix. M and N are the grid rows and columns respectively. DataDims are the dimensions of the map data, map.DataSize(3:end).

For other syntaxes, the map data may be returned as an array of values with size *N*-by-*DataDims* or as a subregion of the full matrix.

inBounds — Valid map locations

n-by-1 column vector

Valid map locations, returned as an *n*-by-1 column vector equal in length to xy or ij. Locations inside the map limits return a value of 1. Locations outside the map limits return a value of 0.

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

Objects

binaryOccupancyMap | multiLayerMap | occupancyMap | occupancyMap3D

Functions

move | setMapData | syncWith

Introduced in R2021a

setMapData

Assign data to map layer

Syntax

```
setMapData(map,mapData)
setMapData(map,xy,mapData)
setMapData(map,xy,mapData,'local')
setMapData(map,ij,mapData,'grid')
inBounds = setMapData(____)
setMapData(map,bottomLeft,mapData)
setMapData(map,bottomLeft,mapData,'local')
setMapData(map,topLeft,mapData,'grid')
```

Description

setMapData(map,mapData) overwrites all values in the map layer using a matrix with dimensions that match the map layer data dimensions, map.DataSize.

setMapData(map,xy,mapData) specifies an array of values for the given xy-locations in world coordinates. The mapData input must be an X-by-1-by-DataDims array. DataDims are the dimensions of the map data, map.DataSize(3:end). Locations outside the map boundaries are ignored.

setMapData(map,xy,mapData,'local') specifies locations in local coordinates.

setMapData(map,ij,mapData,'grid') specifies an array of values for the given ij-locations in grid coordinates. Each row of ij refers to a grid cell index $[i\ j]$

inBounds = setMapData(____) also returns a vector of logical values indicating whether the corresponding input location xy or ij is valid using the previous syntaxes.

setMapData(map,bottomLeft,mapData) specifies a matrix of values mapData for a subregion of the map layer, map. The subregion starts in the bottom-left xy-position bottomLeft and updates a subregion based on the size of mapData.

setMapData(map,bottomLeft,mapData,'local') specifies the bottom-left corner of the subregion in local coordinates.

setMapData(map,topLeft,mapData,'grid') specifies the top-left corner of a sub region in grid coordinates. The subregion is updated with values in mapData.

Examples

Store and Modify XY Velocities Using A Single Map Layer

Create a map layer that stores two values per grid location as *xy*-velocities.

Create an m-by-n-by-2 matrix of values. The first element in the third dimension is dx and the second is dy as velocities.

```
dXY = reshape(1:200,10,20);
dXY(:,:,2) = dXY;
```

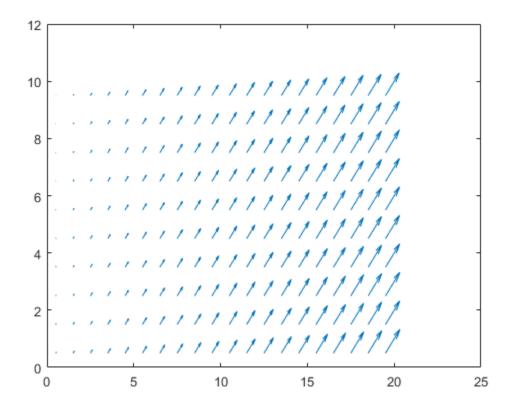
Create a map layer from the matrix. Specify the resolution and layer name.

```
vLayer = mapLayer(dXY, 'Resolution',1, 'LayerName', 'dXY');
```

Get all the map data out as a matrix. Get the xy-locations of the velocity values by creating arrays that cover the minimum and maximum xy-world limits and is shifted to the grid-center locations. The y-locations are flipped when converting between matrix to world coordinates. Visualize the velocities corresponding to those grid-center locations using the quiver function.

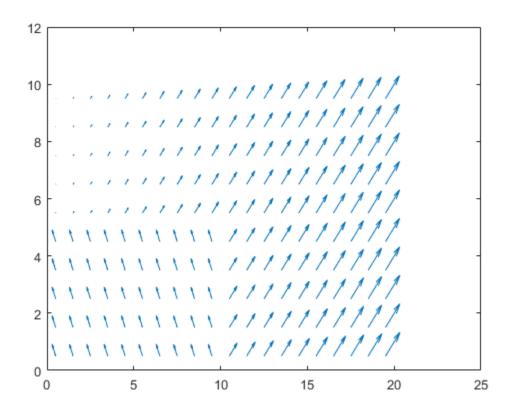
```
v = getMapData(vLayer);

R = 1/(2*vLayer.Resolution);
xLim = vLayer.XWorldLimits;
yLim = vLayer.YWorldLimits;
xLoc = (xLim(1)+R):R*2:(xLim(2)-R);
yLoc = (yLim(2)-R):-R*2:(yLim(1)+R);
quiver(xLoc,yLoc,v(:,:,1),v(:,:,2))
```



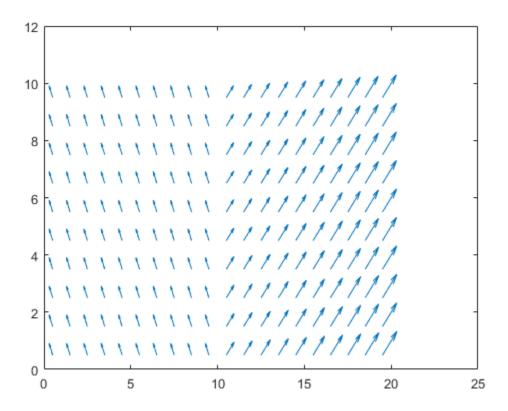
Set the bottom-left quadrant to new updated values. Create the values as a matrix and specify the bottom-left corner (0,0) in map coordinates to the setData function.

```
updateValues = repmat(reshape([-50,100],[1 1 2]),5,10);
setMapData(vLayer,[0 0],updateValues)
v = getMapData(vLayer);
quiver(xLoc,yLoc,v(:,:,1),v(:,:,2))
```



Set new values for the top-left quadrant using grid coordinates. For maps, the top-left grid location is (1,1).

```
setMapData(vLayer,[1 1],updateValues,'grid')
v = getMapData(vLayer);
quiver(xLoc,yLoc,v(:,:,1),v(:,:,2))
```



Write Custom Transform Functions for Map Layers

The mapLayer object enables you to apply custom element-wise transformations when setting and getting data in the map. To transform data you set or get from the map, specify function handles for the GetTransfomFcn and SetTransformFcn properties. This example shows how to implement a log-odds probabilitistic map layer by creating a lookup table for probability and log-odds values. The transform functions use these lookup tables to convert between these values when setting or getting data.

Create Lookup Tables

Generate a full lookup table of values that map the probability values to the minimum and maximum limits of int16 values.

Create an array of int16 values from intmin to intmax. Define the probablilty limits.

```
intType = 'int16';
intLinSpace = intmin(intType):intmax(intType);
numOfPoints = length(intLinSpace);
probLimits = [0.001 .999];
```

The exampleHelperProbToLogodds and examplerHelperLogoddsToProb functions covert between the log-odds and probability values. Use the helper functions to get the log-odds limits and

generate the array for looking up log-odds values. Create an interpolated grid for the entire lookup table.

```
logOddsLimits = exampleHelperProbToLogodds([0.001 .999]);
logOddsLookup = single(exampleHelperLogoddsToProb(linspace(logOddsLimits(1),logOddsLimits(2),numlinterpTable = griddedInterpolant(logOddsLookup,single(intLinSpace),'nearest');
```

Specify Transform Function Handles

The transform function handles utilize example helpers that define how to convert between log-odds integer values and the probability values with an applied saturation limit. The probability saturation limits are [0.001 .999] as previously specified. This behavior is similar to the occupancyMap object.

```
getXformFcn = @(obj,logodds,varargin)...
    exampleHelperIntLogoddsToProb(logodds,logOddsLookup(:),intLinSpace);
setXformFcn = @(obj,prob,varargin)...
    exampleHelperProbToIntLogodds(prob,interpTable,logOddsLookup(:),intLinSpace,probLimits);
```

Create Map Layer

Generate an occupancy map layer object from a matrix of probability values. Specify the get and set transform functions.

Notice that when you create the map, the default value is 0.001 instead of 0. This difference is because the SetTransformFcn function has been applied to the default value of 0 when you create the object, which saturates the value to 0.001.

```
disp(occupancyLayer.DefaultValue)
    0.0010
```

Get and Set Map Data

0.5000 0.5000

0.5000

The map data matches the matrix you set on creation.

0.5000

0.5000

0.5000

0.5000

0.5000

0.5000

```
extData = getMapData(occupancyLayer)
extData = 10 \times 10
    0.5000
               0.5000
                         0.5000
                                    0.5000
                                               0.5000
                                                         0.5000
                                                                    0.5000
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Set specific map locations to values that are:

0.5000

0.5000

0.5000

- Outside of the probability saturation limits.
- Higher precision than the resolution of the lookup tables.

```
setMapData(occupancyLayer,[0 0],0.00001)
setMapData(occupancyLayer,[5 5],0.25999)
```

For the first location, the probability is bound to the saturation limits.

```
extData = getMapData(occupancyLayer,[0 0])
extData = 0.0010
```

The second location returns the value closest to the probability value in the lookup table.

```
extData2 = getMapData(occupancyLayer,[5 5])
extData2 = 0.2600
```

The generated map layer can now be used for updating a probability occupany map that are stored as int16 values. To combine this map with other layers or map types, see the multiLayerMap object.

Input Arguments

map — Map layer

maLayer object

Map layer, specified as a malayer object.

mapData — Data values for setting map layer

matrix

Data values for setting map layer, specified as a matrix. By default, the function sets all data on the layer as an *M*-by-*N*-by-*DataDims* matrix. *M* and *N* are the grid height and width respectively. *DataDims* are the dimensions of the map data, map.DataSize(3,:).

For other syntaxes, the map data may be specified as a matrix with size N-by-DataDims, where N is the number of elements in xy or ij, or as a subregion of the full matrix.

topLeft — Location of grid

```
two-element vector | [iCoord jCoord]
```

Location of top left corner of grid, specified as a two-element vector, [iCoord jCoord].

Data Types: double

${\tt bottomLeft-Location\ of\ output\ matrix\ in\ world\ or\ local\ coordinates}$

```
two-element vector | [xCoord vCoord]
```

Location of bottom left corner of output matrix in world or local coordinates, specified as a twoelement vector, [xCoord yCoord]. Location is in world or local coordinates based on syntax.

Data Types: double

ij - Grid positions

n-by-2 matrix

Grid positions, specified as an n-by-2 matrix of $[i \ j]$ pairs in $[rows \ cols]$ format, where n is the number of grid positions.

Data Types: double

xy — World or local coordinates

n-by-2 matrix

World or local coordinates, specified as an n-by-2 matrix of $[x \ y]$ pairs, where n is the number of coordinates.

Data Types: double

Output Arguments

inBounds — Valid map locations

n-by-1 column vector

Valid map locations, returned as an n-by-1 column vector equal in length to xy or ij. Locations inside the map limits return a value of 1. Locations outside the map limits return a value of 0.

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

Objects

binaryOccupancyMap | multiLayerMap | occupancyMap | occupancyMap3D

Functions

getMapData | move | setMapData | syncWith

Introduced in R2021a

insfilterMARG

Estimate pose from MARG and GPS data

Description

The insfilterMARG object implements sensor fusion of MARG and GPS data to estimate pose in the NED (or ENU) reference frame. MARG (magnetic, angular rate, gravity) data is typically derived from magnetometer, gyroscope, and accelerometer sensors. The filter uses a 22-element state vector to track the orientation quaternion, velocity, position, MARG sensor biases, and geomagnetic vector. The insfilterMARG object uses an extended Kalman filter to estimate these quantities.

Creation

Syntax

```
filter = insfilterMARG
filter = insfilterMARG('ReferenceFrame',RF)
filter = insfilterMARG(____,Name,Value)
```

Description

filter = insfilterMARG creates an insfilterMARG object with default property values.

filter = insfilterMARG('ReferenceFrame', RF) allows you to specify the reference frame, RF, of the filter. Specify RF as 'NED' (North-East-Down) or 'ENU' (East-North-Up). The default value is 'NED'.

filter = insfilterMARG(____, Name, Value) also allows you set properties of the created
filter using one or more name-value pairs. Enclose each property name in single quotes.

Properties

IMUSampleRate — Sample rate of the IMU (Hz)

100 (default) | positive scalar

Sample rate of the inertial measurement unit (IMU) in Hz, specified as a positive scalar.

Data Types: single | double

ReferenceLocation — Reference location (deg, deg, meters)

[0 0 0] (default) | 3-element positive row vector

Reference location, specified as a 3-element row vector in geodetic coordinates (latitude, longitude, and altitude). Altitude is the height above the reference ellipsoid model, WGS84. The reference location units are [degrees degrees meters].

Data Types: single | double

GyroscopeNoise — Multiplicative process noise variance from gyroscope (rad/s)²

1e-9 (default) | scalar | 3-element row vector

Multiplicative process noise variance from the gyroscope in (rad/s)², specified as a scalar or 3-element row vector of positive real finite numbers.

- If GyroscopeNoise is specified as a row vector, the elements correspond to the noise in the *x*, *y*, and *z* axes of the gyroscope, respectively.
- If GyroscopeNoise is specified as a scalar, the single element is applied to the x, y, and z axes of the gyroscope.

Data Types: single | double

GyroscopeBiasNoise — Multiplicative process noise variance from gyroscope bias (rad/s)² 1e-10 (default) | positive scalar | 3-element row vector

Multiplicative process noise variance from the gyroscope bias in (rad/s)², specified as a scalar or 3-element row vector of positive real numbers.

- If GyroscopeBiasNoise is specified as a row vector, the elements correspond to the noise in the x, y, and z axes of the gyroscope bias, respectively.
- If GyroscopeBiasNoise is specified as a scalar, the single element is applied to each axis.

Data Types: single | double

AccelerometerNoise — Multiplicative process noise variance from accelerometer (m/s²)² 1e-4 (default) | scalar | 3-element row vector

Multiplicative process noise variance from the accelerometer in $(m/s^2)^2$, specified as a scalar or 3-element row vector of positive real finite numbers.

- If AccelerometerNoise is specified as a row vector, the elements correspond to the noise in the x, y, and z axes of the accelerometer, respectively.
- If AccelerometerNoise is specified as a scalar, the single element is applied to each axis.

Data Types: single | double

AccelerometerBiasNoise — Multiplicative process noise variance from accelerometer bias $(m/s^2)^2$

1e-4 (default) | positive scalar | 3-element row vector

Multiplicative process noise variance from the accelerometer bias in $(m/s^2)^2$, specified as a scalar or 3-element row vector of positive real numbers.

- If AccelerometerBiasNoise is specified as a row vector, the elements correspond to the noise in the *x*, *y*, and *z* axes of the accelerometer bias, respectively.
- If AccelerometerBiasNoise is specified as a scalar, the single element is applied to each axis.

Data Types: single | double

$\label{eq:GeomagneticVectorNoise} \textbf{--} \textbf{Additive process noise for geomagnetic vector (μT2)}$

1e-6 (default) | positive scalar | 3-element row vector

Additive process noise for geomagnetic vector in μT^2 , specified as a scalar or 3-element row vector of positive real numbers.

- If GeomagneticVectorNoise is specified as a row vector, the elements correspond to the noise in the x, y, and z axes of the geomagnetic vector, respectively.
- If GeomagneticVectorNoise is specified as a scalar, the single element is applied to each axis.

Data Types: single | double

MagnetometerBiasNoise — Additive process noise for magnetometer bias (μT^2)

0.1 (default) | positive scalar | 3-element row vector

Additive process noise for magnetometer bias in μT^2 , specified as a scalar or 3-element row vector.

- If MagnetometerBiasNoise is specified as a row vector, the elements correspond to the noise in the x, y, and z axes of the magnetometer bias, respectively.
- If MagnetometerBiasNoise is specified as a scalar, the single element is applied to each axis.

Data Types: single | double

State — State vector of extended Kalman filter

22-element column vector

State vector of the extended Kalman filter. The state values represent:

State	Units	Index
Orientation (quaternion parts)	N/A	1:4
Position (NED or ENU)	m	5:7
Velocity (NED or ENU)	m/s	8:10
Delta Angle Bias (XYZ)	rad	11:13
Delta Velocity Bias (XYZ)	m/s	14:16
Geomagnetic Field Vector (NED or ENU)	μТ	17:19
Magnetometer Bias (XYZ)	μТ	20:22

Data Types: single | double

StateCovariance — State error covariance for extended Kalman filter

eye(22)*1e-6 (default) | 22-by-22 matrix

State error covariance for the extended Kalman filter, specified as a 22-by-22-element matrix, or real numbers.

Data Types: single | double

Object Functions

correct	Correct states using direct state measurements for insfilterMARG
residual	Residuals and residual covariances from direct state measurements for insfilterMARG
fusegps	Correct states using GPS data for insfilterMARG
residualgps	Residuals and residual covariance from GPS measurements for insfilterMARG
fusemag	Correct states using magnetometer data for insfilterMARG
residualmag	Residuals and residual covariance from magnetometer measurements for
	insfilterMARG
pose	Current orientation and position estimate for insfilterMARG

predict Update states using accelerometer and gyroscope data for insfilterMARG reset Reset internal states for insfilterMARG bisplay state vector information for insfilterMARG tune Tune insfilterMARG parameters to reduce estimation error copy Create copy of insfilterMARG

Examples

Estimate Pose of UAV

This example shows how to estimate the pose of an unmanned aerial vehicle (UAV) from logged sensor data and ground truth pose.

Load the logged sensor data and ground truth pose of an UAV.

```
load uavshort.mat
```

Initialize the insfilterMARG filter object.

```
f = insfilterMARG;
f.IMUSampleRate = imuFs;
f.ReferenceLocation = refloc:
f.AccelerometerBiasNoise = 2e-4:
f.AccelerometerNoise = 2;
f.GyroscopeBiasNoise = 1e-16;
f.GyroscopeNoise = 1e-5;
f.MagnetometerBiasNoise = 1e-10;
f.GeomagneticVectorNoise = 1e-12;
f.StateCovariance = 1e-9*ones(22);
f.State = initstate;
qpsidx = 1;
N = size(accel, 1);
p = zeros(N,3);
q = zeros(N,1,'quaternion');
Fuse accelerometer, gyroscope, magnetometer, and GPS data.
for ii = 1:size(accel,1)
                                        % Fuse IMU
   f.predict(accel(ii,:), gyro(ii,:));
                                        % Fuse magnetometer at 1/2 the IMU rate
   if ~mod(ii,fix(imuFs/2))
       f.fusemag(mag(ii,:),Rmag);
   end
   if ~mod(ii,imuFs)
                                        % Fuse GPS once per second
       f.fusegps(lla(gpsidx,:),Rpos,gpsvel(gpsidx,:),Rvel);
       gpsidx = gpsidx + 1;
   [p(ii,:),q(ii)] = pose(f);
                                         %Log estimated pose
end
Calculate and display RMS errors.
posErr = truePos - p;
qErr = rad2deg(dist(true0rient,q));
```

Algorithms

Note: The following algorithm only applies to an NED reference frame.

insfilterMARG uses a 22-axis extended Kalman filter structure to estimate pose in the NED reference frame. The state is defined as:

```
q_0
                                q_1
                                q_2
                                q_3
                         position<sub>N</sub>
                         position<sub>E</sub>
                         position<sub>D</sub>
                                \nu_{
m N}
                                \nu_{
m E}
                                \nu_{\mathrm{D}}
                           \Delta\thetabias<sub>X</sub>
\chi =
                           \Delta\thetabias<sub>Y</sub>
                           \Delta\thetabias<sub>7</sub>
                           \Delta \nu bias_{\rm X}
                           \Delta \nu bias_{\rm Y}
                           \Delta \nu bias_7
         geomagneticFieldVector_N
         geomagneticFieldVector<sub>E</sub>
         geomagneticFieldVector_D
                         magbias_X
                         magbias<sub>Y</sub>
                         magbias<sub>7</sub>
```

where

- q_0 , q_1 , q_2 , q_3 Parts of orientation quaternion. The orientation quaternion represents a frame rotation from the platform's current orientation to the local NED coordinate system.
- position_N, position_E, position_D -- Position of the platform in the local NED coordinate system.
- $\nu_{\rm N}, \nu_{\rm E}, \nu_{\rm D}$ -- Velocity of the platform in the local NED coordinate system.
- $\Delta\theta bias_X$, $\Delta\theta bias_Y$, $\Delta\theta bias_Z$ Bias in the integrated gyroscope reading.
- $\Delta \nu bias_X$, $\Delta \nu bias_Y$, $\Delta \nu bias_Z$ Bias in the integrated accelerometer reading.
- $geomagneticFieldVector_N$, $geomagneticFieldVector_E$, $geomagneticFieldVector_D$ Estimate of the geomagnetic field vector at the reference location.
- magbias_X, magbias_Y, magbias_Z -- Bias in the magnetometer readings.

Given the conventional formation of the predicted state estimate,

$$x_{k|k-1} = f(\widehat{x}_{k-1|k-1}, u_k)$$

 u_k is controlled by accelerometer and gyroscope data that has been converted to delta velocity and delta angle through trapezoidal integration. The predicted state estimation is:

$$x_{k|k-1} =$$

$$q_0 - q_1 \left(\frac{\Delta\theta_{\rm X} - \Delta\theta bias_{\rm X}}{2}\right) - q_2 \left(\frac{\Delta\theta_{\rm Y} - \Delta\theta bias_{\rm Y}}{2}\right) - q_3 \left(\frac{\Delta\theta_{\rm Z} - \Delta\theta bias_{\rm Z}}{2}\right)$$

$$q_1 + q_0 \left(\frac{\Delta\theta_{\rm X} - \Delta\theta bias_{\rm X}}{2}\right) - q_3 \left(\frac{\Delta\theta_{\rm Y} - \Delta\theta bias_{\rm Y}}{2}\right) + q_2 \left(\frac{\Delta\theta_{\rm Z} - \Delta\theta bias_{\rm Z}}{2}\right)$$

$$q_2 + q_3 \left(\frac{\Delta\theta_{\rm X} - \Delta\theta bias_{\rm X}}{2}\right) + q_0 \left(\frac{\Delta\theta_{\rm Y} - \Delta\theta bias_{\rm Y}}{2}\right) - q_1 \left(\frac{\Delta\theta_{\rm Z} - \Delta\theta bias_{\rm Z}}{2}\right)$$

$$q_3 - q_2 \left(\frac{\Delta\theta_{\rm X} - \Delta\theta bias_{\rm X}}{2}\right) + q_1 \left(\frac{\Delta\theta_{\rm Y} - \Delta\theta bias_{\rm Y}}{2}\right) + q_0 \left(\frac{\Delta\theta_{\rm Z} - \Delta\theta bias_{\rm Z}}{2}\right)$$

$$position_{\rm N} + (\Delta t)(\nu_{\rm N})$$

$$position_{\rm E} + (\Delta t)(\nu_{\rm E})$$

$$position_{\rm D} + (\Delta t)(\nu_{\rm D})$$

$$\nu_{\rm N} + (\Delta t)(g_{\rm N}) + (\Delta\nu_{\rm X} - \Delta\nu bias_{\rm X})\left(q_0^2 + q_1^2 - q_2^2 - q_3^2\right) - 2(\Delta\nu_{\rm Y} - \Delta\nu bias_{\rm Y})(q_0q_3 - q_1q_2) + 2(\Delta\nu_{\rm Z} - \Delta\nu bias_{\rm Z})(q_0q_2 + \nu_{\rm E} + (\Delta t)(g_{\rm E}) + (\Delta\nu_{\rm Y} - \Delta\nu bias_{\rm Y})\left(q_0^2 - q_1^2 + q_2^2 - q_3^2\right) + 2(\Delta\nu_{\rm X} - \Delta\nu bias_{\rm X})(q_0q_3 + q_1q_2) - 2(\Delta\nu_{\rm Z} - \Delta\nu bias_{\rm Z})(q_0q_1 - \nu_{\rm D} + (\Delta t)(g_{\rm D}) + (\Delta\nu_{\rm Z} - \Delta\nu bias_{\rm Z})\left(q_0^2 - q_1^2 - q_2^2 + q_3^2\right) - 2(\Delta\nu_{\rm X} - \Delta\nu bias_{\rm X})(q_0q_2 - q_1q_3) + 2(\Delta\nu_{\rm Y} - 2-3\theta\theta ias_{\rm Y})(q_0q_1 + \Delta\theta bias_{\rm Y})$$

where

- $\Delta\theta_{\rm X}$, $\Delta\theta_{\rm Y}$, $\Delta\theta_{\rm Z}$ Integrated gyroscope reading.
- $\Delta\nu_{\rm X}$, $\Delta\nu_{\rm Y}$, $\Delta\nu_{\rm Z}$ Integrated accelerometer readings.
- Δt -- IMU sample time.
- g_N , g_E , g_D Constant gravity vector in the NED frame.

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

insfilterAsync|insfilterErrorState|insfilterNonholonomic

correct

Correct states using direct state measurements for insfilterMARG

Syntax

correct(FUSE,idx,measurement,measurementCovariance)

Description

correct(FUSE,idx,measurement,measurementCovariance) corrects the state and state estimation error covariance based on the measurement and measurement covariance. The measurement maps directly to the state specified by the indices idx.

Input Arguments

FUSE — insfilterMARG object

object

insfilterMARG, specified as an object.

idx — State vector Index of measurement to correct

N-element vector of increasing integers in the range [1,22]

State vector index of measurement to correct, specified as an N-element vector of increasing integers in the range [1, 22].

The state values represent:

State	Units	Index
Orientation (quaternion parts)		1:4
Position (NED)	m	5:7
Velocity (NED)	m/s	8:10
Delta Angle Bias (XYZ)	rad	11:13
Delta Velocity Bias (XYZ)	m/s	14:16
Geomagnetic Field Vector (NED)) μΤ	17:19
Magnetometer Bias (XYZ)	μТ	20:22

Data Types: single | double

measurement — Direct measurement of state

N-element vector

Direct measurement of state, specified as a N-element vector. N is the number of elements of the index argument, idx.

Data Types: single | double

measurementCovariance — Covariance of measurement

scalar | *N*-element vector | *N*-by-*N* matrix

Covariance of measurement, specified as a scalar, N-element vector, or N-by-N matrix. N is the number of elements of the index argument, idx.

Data Types: single | double

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

insfilter|insfilterMARG

copy

Create copy of insfitlerMARG

Syntax

newFilter = copy(filter)

Description

newFilter = copy(filter) returns a copy of the insfilterMARG, filter, with the exactly same property values.

Input Arguments

filter — Filter to be copied

insfitlerMARG

Filter to be copied, specified as an insfilterMARG object.

Output Arguments

newFilter — New copied filter

insfitlerMARG

New copied filter, returned as an insfilterMARG object.

See Also

insfilterMARG

Introduced in R2020b

fusegps

Correct states using GPS data for insfilterMARG

Syntax

```
[res,resCov] = fusegps(FUSE,position,positionCovariance)
[res,resCov] = fusegps(FUSE,position,positionCovariance,velocity,
velocityCovariance)
```

Description

[res,resCov] = fusegps(FUSE,position,positionCovariance) fuses GPS position data to correct the state estimate.

[res,resCov] = fusegps(FUSE,position,positionCovariance,velocity,
velocityCovariance) fuses GPS position and velocity data to correct the state estimate.

Input Arguments

FUSE — insfilterMARG object

object

insfilterMARG, specified as an object.

position — Position of GPS receiver (LLA)

3-element row vector

Position of GPS receiver in geodetic latitude, longitude, and altitude (LLA) specified as a real finite 3-element row vector. Latitude and longitude are in degrees with north and east being positive. Altitude is in meters.

Data Types: single | double

positionCovariance — Position measurement covariance of GPS receiver (m²)

3-by-3 matrix

Position measurement covariance of GPS receiver in m², specified as a 3-by-3 matrix.

Data Types: single | double

velocity — Velocity of GPS receiver in local NED coordinate system (m/s)

3-element row vector

Velocity of the GPS receiver in the local NED coordinate system in m/s, specified as a 3-element row vector.

Data Types: single | double

velocityCovariance — Velocity measurement covariance of GPS receiver (m/s²)

3-by-3 matrix

Velocity measurement covariance of the GPS receiver in the local NED coordinate system in m/s², specified as a 3-by-3 matrix.

Data Types: single | double

Output Arguments

res — Position and velocity residual

1-by-6 vector of real values

Position and velocity residual, returned as a 1-by-6 vector of real values in m and m/s, respectively.

resCov — Residual covariance

6-by-6 matrix of real values

Residual covariance, returned as a 6-by-6 matrix of real values.

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

insfilter|insfilterMARG

fusemag

Correct states using magnetometer data for insfilterMARG

Syntax

[res,resCov] = fusemag(FUSE,magReadings,magReadingsCovariance)

Description

[res,resCov] = fusemag(FUSE,magReadings,magReadingsCovariance) fuses
magnetometer data to correct the state estimate.

Input Arguments

FUSE — insfilterMARG object

object

insfilterMARG, specified as an object.

magReadings — Magnetometer readings (μT)

3-element row vector

Magnetometer readings in μT , specified as a 3-element row vector of finite real numbers.

Data Types: single | double

magReadingsCovariance — Magnetometer readings error covariance (μT²)

scalar | 3-element row vector | 3-by-3 matrix

Magnetometer readings error covariance in μT^2 , specified as a scalar, 3-element row vector, or 3-by-3 matrix.

Data Types: single | double

Output Arguments

res - Residual

1-by-3 vector of real values

Residual, returned a 1-by-3 vector of real values in µT.

Data Types: single | double

resCov — Residual covariance

3-by-3 matrix of real values

Residual covariance, returned a 3-by-3 matrix of real values in $(\mu T)^2$.

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder $^{\text{\tiny TM}}$.

See Also

 $\verb|insfilter|| \verb|insfilter|| \texttt{MARG}|$

pose

Current orientation and position estimate for insfilterMARG

Syntax

```
[position,orientation,velocity] = pose(FUSE)
[position,orientation,velocity] = pose(FUSE,format)
```

Description

[position, orientation, velocity] = pose(FUSE) returns the current estimate of the pose and velocity.

[position, orientation, velocity] = pose(FUSE, format) returns the current estimate of the pose with orientation in the specified orientation format.

Input Arguments

FUSE — insfilterMARG object

object

insfilterMARG, specified as an object.

format — Output orientation format

```
'quaternion' (default) | 'rotmat'
```

Output orientation format, specified as either 'quaternion' for a quaternion or 'rotmat' for a rotation matrix.

Data Types: char | string

Output Arguments

position — Position estimate in the local NED coordinate system (m)

3-element row vector

Position estimate in the local NED coordinate system in meters, returned as a 3-element row vector.

Data Types: single | double

orientation — Orientation estimate in the local NED coordinate system

quaternion (default) | 3-by-3 rotation matrix

Orientation estimate in the local NED coordinate system, specified as a scalar quaternion or 3-by-3 rotation matrix. The quaternion or rotation matrix represents a frame rotation from the local NED reference frame to the body reference frame.

Data Types: single | double | quaternion

velocity — Velocity estimate in the local NED coordinate system (m/s)

3-element row vector

Velocity estimate in the local NED coordinate system in m/s, returned as a 3-element row vector.

Data Types: single | double

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder $^{\text{\tiny TM}}$.

See Also

insfilter|insfilterMARG

predict

Update states using accelerometer and gyroscope data for insfilterMARG

Syntax

predict(FUSE,accelReadings,gyroReadings)

Description

predict(FUSE,accelReadings,gyroReadings) fuses accelerometer and gyroscope data to update the state estimate.

Input Arguments

FUSE — insfilterMARG object

object

insfilterMARG, specified as an object.

accelReadings — Accelerometer readings in local sensor body coordinate system (m/s²)

3-element row vector

Accelerometer readings in m/s², specified as a 3-element row vector.

Data Types: single | double

gyroReadings — Gyroscope readings in local sensor body coordinate system (rad/s)

3-element row vector

Gyroscope readings in rad/s, specified as a 3-element row vector.

Data Types: single | double

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

insfilter | insfilterMARG

reset

Reset internal states for insfilterMARG

Syntax

reset(FUSE)

Description

reset (FUSE) resets the State, StateCovariance, and internal integrators to their default values.

Input Arguments

FUSE — insfilterMARG object

object

insfilterMARG, specified as an object.

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

insfilter|insfilterMARG

residual

Residuals and residual covariances from direct state measurements for insfilterMARG

Syntax

[res, resCov] = residual(FUSE,idx,measurement,measurementCovariance)

Description

[res, resCov] = residual(FUSE,idx,measurement,measurementCovariance) computes the residual, res, and the residual covariance, resCov, based on the direct state measurement and measurement covariance. The measurement maps directly to the states specified by indices, idx.

Input Arguments

FUSE — insfilterMARG object

object

insfilterMARG, specified as an object.

idx — State vector index of measurement

N-element vector of increasing integers in the range [1,22]

State vector index of measurement, specified as an N-element vector of increasing integers in the range [1, 22].

The state values represent:

State	Units	Index
Orientation (quaternion parts)		1:4
Position (NED)	m	5:7
Velocity (NED)	m/s	8:10
Delta Angle Bias (XYZ)	rad	11:13
Delta Velocity Bias (XYZ)	m/s	14:16
Geomagnetic Field Vector (NED)	μΤ	17:19
Magnetometer Bias (XYZ)	μΤ	20:22

measurement — Direct measurement of state

N-element vector

Direct measurement of state, specified as a N-element vector. N is the number of elements of the index argument, idx.

measurementCovariance — Covariance of measurement

N-by-*N* matrix

Covariance of measurement, specified as an N-by-N matrix. N is the number of elements of the index argument, idx.

Output Arguments

res — Measurement residual

1-by-*N* vector of real values

Measurement residual, returned as a 1-by-N vector of real values.

resCov — Residual covariance

N-by-N matrix of real values

Residual covariance, returned as a N-by-N matrix of real values.

See Also

insfilterMARG

Introduced in R2020a

residualgps

Residuals and residual covariance from GPS measurements for insfilterMARG

Syntax

```
[res,resCov] = residualgps(FUSE,position,positionCovariance)
[res,resCov] = residualgps(FUSE,position,positionCovariance,velocity,velocityCovariance)
```

Description

[res,resCov] = residualgps(FUSE,position,positionCovariance) computes the
residual, res, and the residual covariance, resCov, based on the GPS position measurement and
covariance.

[res,resCov] = residualgps(FUSE,position,positionCovariance,velocity,
velocityCovariance) computes the residual, res, and the residual covariance, resCov, based on
the GPS position measurement and covariance.

Input Arguments

FUSE — insfilterMARG object

object

insfilterMARG, specified as an object.

position — Position of GPS receiver (LLA)

3-element row vector

Position of GPS receiver in geodetic latitude, longitude, and altitude (LLA) specified as a real finite 3-element row vector. Latitude and longitude are in degrees with north and east being positive. Altitude is in meters.

Data Types: single | double

positionCovariance — Position measurement covariance of GPS receiver (m²)

3-by-3 matrix

Position measurement covariance of GPS receiver in m², specified as a 3-by-3 matrix.

Data Types: single | double

velocity — Velocity of GPS receiver in local NED coordinate system (m/s)

3-element row vector

Velocity of the GPS receiver in the local NED coordinate system in m/s, specified as a 3-element row vector.

Data Types: single | double

velocityCovariance — Velocity measurement covariance of GPS receiver (m/s²)

3-by-3 matrix

Velocity measurement covariance of the GPS receiver in the local NED coordinate system in m/s^2 , specified as a 3-by-3 matrix.

Data Types: single | double

Output Arguments

res — Position and velocity residual

1-by-3 vector of real values | 1-by-6 vector of real values

Position and velocity residual, returned as a 1-by-3 vector of real values if the inputs only contain position information, and returned as 1-by-6 vector of real values if the inputs also contain velocity information.

resCov — Residual covariance

3-by-3 matrix of real values | 6-by-6 matrix of real values

Residual covariance, returned as a 3-by-3 matrix of real values if the inputs only contain position information, and a 6-by-6 matrix of real values if the inputs also contain velocity information.

See Also

insfilter | insfilterMARG

Introduced in R2020a

residualmag

Residuals and residual covariance from magnetometer measurements for insfilterMARG

Syntax

[res,resCov] = residualmag(FUSE,magReadings,magReadingsCovariance)

Description

[res,resCov] = residualmag(FUSE,magReadings,magReadingsCovariance) computes the residual, residual, and the residual covariance, resCov, based on the magnetometer readings and the corresponding covariance.

Input Arguments

FUSE — insfilterMARG object

object

insfilterMARG, specified as an object.

magReadings — Magnetometer readings (μT)

3-element row vector

Magnetometer readings in μT , specified as a 3-element row vector of finite real numbers.

Data Types: single | double

magReadingsCovariance — Magnetometer readings error covariance (μ T²)

scalar | 3-element row vector | 3-by-3 matrix

Magnetometer readings error covariance in μT^2 , specified as a scalar, 3-element row vector, or 3-by-3 matrix.

Data Types: single | double

Output Arguments

res — Residual

1-by-3 vector of real values

Residual, returned as a 1-by-3 vector of real values in μT .

Data Types: single | double

resCov — Residual covariance

3-by-3 matrix of real values

Residual covariance, returned a 3-by-3 matrix of real values in $(\mu T)^2$.

See Also

insfilter | insfilterMARG

Introduced in R2020a

stateinfo

Display state vector information for insfilterMARG

Syntax

```
stateinfo(FUSE)
info = stateinfo(FUSE)
```

Description

stateinfo(FUSE) displays the meaning of each index of the State property and the associated units.

info = stateinfo(FUSE) returns a structure with fields containing descriptions of the elements of
the state vector of the filter, FUSE.

Examples

State Information of insfilterMARG

Create an insfilterMARG object.

```
filter = insfilterMARG;
```

Display the state information of the created filter.

stateinfo(filter)

States	Units	Index
Orientation (quaternion parts)		1:4
Position (NAV)	m	5:7
Velocity (NAV)	m/s	8:10
Delta Angle Bias (XYZ)	rad	11:13
Delta Velocity Bias (XYZ)	m/s	14:16
Geomagnetic Field Vector (NAV)	μΤ	17:19
Magnetometer Bias (XYZ)	μΤ	20:22

Output the state information of the filter as a structure.

info = stateinfo(filter)

```
info = struct with fields:
    Orientation: [1 2 3 4]
        Position: [5 6 7]
        Velocity: [8 9 10]
        DeltaAngleBias: [11 12 13]
        DeltaVelocityBias: [14 15 16]
    GeomagneticFieldVector: [17 18 19]
        MagnetometerBias: [20 21 22]
```

Input Arguments

FUSE — insfilterMARG object

object

insfilterMARG, specified as an object.

info — State information

structure

State information, returned as a structure with fields containing descriptions of the elements of the state vector of the filter. The values of each field are the corresponding indices of the state vector.

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

insfilter|insfilterMARG

tune

Tune insfilterMARG parameters to reduce estimation error

Syntax

```
tunedMeasureNoise = tune(filter,measureNoise,sensorData,groundTruth)
tunedMeasureNoise = tune(____,config)
```

Description

tunedMeasureNoise = tune(filter,measureNoise,sensorData,groundTruth) adjusts the properties of the insfilterMARG filter object, filter, and measurement noises to reduce the root-mean-squared (RMS) state estimation error between the fused sensor data and the ground truth. The function also returns the tuned measurement noise, tunedMeasureNoise. The function uses the property values in the filter and the measurement noise provided in the measureNoise structure as the initial estimate for the optimization algorithm.

tunedMeasureNoise = tune(____, config) specifies the tuning configuration based on a tunerconfig object, config.

Examples

Tune insfilterMARG to Optimize Pose Estimate

Load the recorded sensor data and ground truth data.

load('insfilterMARGTuneData.mat');

```
Create tables for the sensor data and the truth data.
sensorData = table(Accelerometer, Gyroscope, ...
Magnetometer, GPSPosition, GPSVelocity);
groundTruth = table(Orientation, Position);
```

Create an insfilterMARG filter object that has a few noise properties.

```
filter = insfilterMARG('State',initialState,...
    'StateCovariance',initialStateCovariance,...
    'AccelerometerBiasNoise',le-7,...
    'GyroscopeBiasNoise',le-7,...
    'MagnetometerBiasNoise',le-7,...
    'GeomagneticVectorNoise',le-7);
```

Create a tuner configuration object for the filter. Set the maximum iterations to eight. Also, set the tunable parameters.

Use the tuner noise function to obtain a set of initial sensor noises used in the filter.

```
measNoise = tunernoise('insfilterMARG')
measNoise = struct with fields:
    MagnetometerNoise: 1
    GPSPositionNoise: 1
    GPSVelocityNoise: 1
```

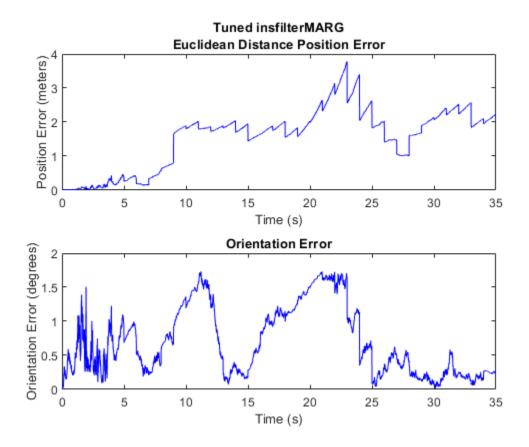
Tune the filter and obtain the tuned parameters.

Iteration	Parameter	Metric
1	AccelerometerNoise	2.5701
1	GPSPositionNoise	2.5446
1	GPSVelocityNoise	2.5279
1	GeomagneticVectorNoise	2.5268
1	GyroscopeNoise	2.5268
1	MagnetometerNoise	2.5204
2	AccelerometerNoise	2.5203
	GPSPositionNoise	2.4908
2 2 2	GPSVelocityNoise	2.4695
2	GeomagneticVectorNoise	2.4684
2	GyroscopeNoise	2.4684
2	MagnetometerNoise	2.4615
3	AccelerometerNoise	2.4615
3	GPSPositionNoise	2.4265
3	GPSVelocityNoise	2.4000
3	GeomagneticVectorNoise	2.3988
2 2 3 3 3 3 3 3	GyroscopeNoise	2.3988
	MagnetometerNoise	2.3911
4	AccelerometerNoise	2.3911
4	GPSPositionNoise	2.3500
4	GPSVelocityNoise	2.3164
4	GeomagneticVectorNoise	2.3153
4	GyroscopeNoise	2.3153
4	MagnetometerNoise	2.3068
5	AccelerometerNoise	2.3068
5	GPSPositionNoise	2.2587
5 5 5	GPSVelocityNoise	2.2166
5	GeomagneticVectorNoise	2.2154
5	GyroscopeNoise	2.2154
5	MagnetometerNoise	2.2063
6	AccelerometerNoise	2.2063
6	GPSPositionNoise	2.1505
6	GPSVelocityNoise	2.0981
6 6	GeomagneticVectorNoise	2.0971 2.0971
6	GyroscopeNoise	2.0971
7	MagnetometerNoise AccelerometerNoise	2.0873
7	GPSPositionNoise	2.0374
7	GPSVelocityNoise	1.9601
7	GeomagneticVectorNoise	1.9594
7	GyroscopeNoise	1.9594
7	MagnetometerNoise	1.9499
,		1.0.00

```
8
                 GPSPositionNoise
                                            1.8802
    8
                 GPSVelocityNoise
                                            1.8035
    8
                 GeomagneticVectorNoise
                                            1.8032
    8
                 GyroscopeNoise
                                            1.8032
    8
                 MagnetometerNoise
                                            1.7959
Fuse the sensor data using the tuned filter.
N = size(sensorData,1);
gEstTuned = guaternion.zeros(N,1);
posEstTuned = zeros(N,3);
for ii=1:N
    predict(filter,Accelerometer(ii,:),Gyroscope(ii,:));
    if all(~isnan(Magnetometer(ii,1)))
        fusemag(filter,Magnetometer(ii,:),...
            tunedParams.MagnetometerNoise);
    end
    if all(~isnan(GPSPosition(ii,1)))
        fusegps(filter,GPSPosition(ii,:),...
            tunedParams.GPSPositionNoise,GPSVelocity(ii,:),...
            tunedParams.GPSVelocityNoise);
    end
    [posEstTuned(ii,:),qEstTuned(ii,:)] = pose(filter);
end
Compute the RMS errors.
orientationErrorTuned = rad2deg(dist(gEstTuned,Orientation));
rmsOrientationErrorTuned = sqrt(mean(orientationErrorTuned.^2))
rmsOrientationErrorTuned = 0.8580
positionErrorTuned = sqrt(sum((posEstTuned - Position).^2,2));
rmsPositionErrorTuned = sqrt(mean(positionErrorTuned.^2))
rmsPositionErrorTuned = 1.7946
Visualize the results.
figure();
t = (0:N-1)./filter.IMUSampleRate;
subplot(2,1,1)
plot(t,positionErrorTuned,'b');
title("Tuned insfilterMARG" + newline + ...
    "Euclidean Distance Position Error")
xlabel('Time (s)');
ylabel('Position Error (meters)')
subplot(2,1,2)
plot(t, orientationErrorTuned, 'b');
title("Orientation Error")
xlabel('Time (s)');
ylabel('Orientation Error (degrees)');
```

AccelerometerNoise

1.9499



Input Arguments

filter — Filter object

infilterMARG object

Filter object, specified as an insfilterMARG object.

measureNoise — Measurement noise

structure

Measurement noise, specified as a structure. The function uses the measurement noise input as the initial guess for tuning the measurement noise. The structure must contain these fields:

Field name	Description
MagnetometerNoise	Variance of magnetometer noise, specified as a scalar in $(\mu T)^2$
GPSPositionNoise	Variance of GPS position noise, specified as a scalar in m ²
GPSVelocityNoise	Variance of GPS velocity noise, specified as a scalar in $(m/s)^2$

sensorData — Sensor data

table

Sensor data, specified as a table. In each row, the sensor data is specified as:

- Accelerometer Accelerometer data, specified as a 1-by-3 vector of scalars in m²/s.
- Gyroscope Gyroscope data, specified as a 1-by-3 vector of scalars in rad/s.
- Magnetometer Magnetometer data, specified as a 1-by-3 vector of scalars in μT.
- GPSPosition GPS position data, specified as a 1-by-3 vector of scalars in meters.
- GPSVelocity GPS velocity data, specified as a 1-by-3 vector of scalars in m/s.

If the GPS sensor does not produce complete measurements, specify the corresponding entry for GPSPosition and/or GPSVelocity as NaN. If you set the Cost property of the tuner configuration input, config, to Custom, then you can use other data types for the sensorData input based on your choice.

groundTruth — Ground truth data

table

Ground truth data, specified as a table. In each row, the table can optionally contain any of these variables:

- Orientation Orientation from the navigation frame to the body frame, specified as a quaternion or a 3-by-3 rotation matrix.
- Position Position in navigation frame, specified as a 1-by-3 vector of scalars in meters.
- Velocity Velocity in navigation frame, specified as a 1-by-3 vector of scalars in m/s.
- DeltaAngleBias Delta angle bias, specified as a 1-by-3 vector of scalars in radians.
- DeltaVelocityBias Delta velocity bias, specified as a 1-by-3 vector of scalars in m/s.
- GeomagneticFieldVector Geomagnetic field vector in navigation frame, specified as a 1-by-3 vector of scalars.
- MagnetometerBias Magnetometer bias in body frame, specified as a 1-by-3 vector of scalars in μT .

The function processes each row of the sensorData and groundTruth tables sequentially to calculate the state estimate and RMS error from the ground truth. State variables not present in groundTruth input are ignored for the comparison. The sensorData and the groundTruth tables must have the same number of rows.

If you set the Cost property of the tuner configuration input, config, to Custom, then you can use other data types for the groundTruth input based on your choice.

config — Tuner configuration

tunerconfig object

Tuner configuration, specified as a tunerconfig object.

Output Arguments

tunedMeasureNoise — Tuned measurement noise

structure

Tuned measurement noise, returned as a structure. The structure contains these fields.

Field name	Description
MagnetometerNoise	Variance of magnetometer noise, specified as a scalar in $(\mu T)^2$
GPSPositionNoise	Variance of GPS position noise, specified as a scalar in m^2
GPSVelocityNoise	Variance of GPS velocity noise, specified as a scalar in (m/s) ²

References

[1] Abbeel, P., Coates, A., Montemerlo, M., Ng, A.Y. and Thrun, S. Discriminative Training of Kalman Filters. In *Robotics: Science and systems*, Vol. 2, pp. 1, 2005.

See Also

tunerconfig|tunernoise

Introduced in R2021a

gnssSensor

Simulate GNSS to generate position and velocity readings

Description

The gnssSensor System object simulates a global navigation satellite system (GNSS) to generate position and velocity readings based on local position and velocity data. The object calculates satellite positions and velocities based on the sensor time and data that specifies the satellite orbital parameters on page 2-541. The object uses only the Global Positioning System (GPS) constellations for calculations. To set the starting positions of the satellites, set the InitialTime property.

To generate GNSS position and velocity readings:

- **1** Create the gnssSensor object and set its properties.
- 2 Call the object with arguments, as if it were a function.

To learn more about how System objects work, see What Are System Objects?.

Calling the object increments the time of the sensor and propagates the satellite position and velocites based on the orbital parameters.

Creation

Syntax

```
GNSS = gnssSensor
GNSS = gnssSensor('ReferenceFrame',frame)
GNSS = gnssSensor(____,Name,Value)
```

Description

GNSS = gnssSensor returns a gnssSensor System object GNSS that computes global navigation satellite system receiver readings based on local position and velocity input.

GNSS = gnssSensor('ReferenceFrame', frame) specifies the reference frame in which the GNSS readings are reported. Specify frame as 'NED' (north-east-down) or 'ENU' (east-north-up). The default value is 'NED'.

GNSS = gnssSensor(____, Name, Value) sets properties using one or more name-value pairs. For example, gnssSensor('SampleRate',2) creates a simulated GNSS with a sample rate of 2 Hz. Enclose each property name in quotes.

Properties

Unless otherwise indicated, properties are *nontunable*, which means you cannot change their values after calling the object. Objects lock when you call them, and the release function unlocks them.

If a property is *tunable*, you can change its value at any time.

For more information on changing property values, see System Design in MATLAB Using System Objects.

SampleRate — Sample rate of GNSS receiver (Hz)

1 (default) | positive scalar

Sample rate of the GNSS receiver, specified as a positive scalar in Hz.

Data Types: single | double

InitialTime — Initial time of GNSS receiver

datetime('now', 'TimeZone', 'UTC') (default) | datetime object

Initial time of the GNSS receiver, specified as a datetime object. The object accounts for leap seconds in the conversion between the UTC and the GNSS time.

ReferenceLocation — Origin of local navigation reference frame

[0 0 0] (default) | three-element row vector of scalars

Origin of the local navigation reference frame, specified as a three-element row vector of scalars in geodetic coordinates (latitude in degrees, longitude in degrees, and altitude in meters). Altitude is the height above the reference ellipsoid model WGS84.

Data Types: single | double

MaskAngle — Elevation mask angle (deg)

10 (default) | scalar in [0, 90]

Elevation mask angle, specified as a scalar in the range of [0, 90] in degrees. Satellites in view but below the mask angle are not used in estimating the position of the receiver.

Tunable: Yes

Data Types: single | double

RangeAccuracy — Standard deviation of measurement noise of pseudorange (m)

1 (default) | nonnegative scalar

Standard deviation of the measurement noise of pseudorange, specified as a nonnegative scalar in meters.

Tunable: Yes

Data Types: single | double

RangeRateAccuracy — Standard deviation of measurement noise of pseudorange rate (m/s)

0.02 (default) | nonnegative scalar

Standard deviation of the measurement noise of pseudorange rate, specified as a nonnegative scalar in meters per second.

Tunable: Yes

Data Types: single | double

RandomStream — Random number source

'Global stream' (default) | 'mt19937ar with seed'

Random number source, specified as one of these options::

- 'Global stream' -- Random numbers are generated using the current global random number stream.
- 'mt19937ar with seed' -- Random numbers are generated using the mt19937ar algorithm with the seed specified by the Seed property.

Data Types: char | string

Seed — Initial seed of mt19937ar random number generator algorithm

67 (default) | nonnegative integer

Initial seed of an mt19937ar random number generator algorithm, specified as a nonnegative integer.

Dependencies

To enable this property, set RandomStream to 'mt19937ar with seed'.

Data Types: integer

Usage

Syntax

[positionReadings, velocityReadings, status] = GNSS(position, velocity)

Description

[positionReadings, velocityReadings, status] = GNSS(position, velocity) computes global navigation satellite system receiver readings from the position and velocity inputs.

Input Arguments

position — Cartesian position of GNSS receiver in local navigation coordinate system (m) N-by-3 matrix of scalar

Cartesian position of the GNSS receiver in the local navigation coordinate system, specified as an *N*-by-3 matrix of scalars in meters. *N* is the number of samples.

The default reference frame is NED (north-east-down). For ENU (east-north-up), set the ReferenceFrame name-value argument to 'ENU' on creation.

Data Types: single | double

velocity — Velocity of GNSS receiver in local navigation coordinate system (m/s)

N-by-3 matrix of scalars

Velocity of the GNSS receiver in the local navigation coordinate system, specified as an N-by-3 matrix in meters per second. N is the number of samples.

Data Types: single | double

The default reference frame is NED (north-east-down). For ENU (east-north-up), set the ReferenceFrame name-value argument to 'ENU' on creation.

Output Arguments

positionReadings — Position readings in LLA coordinate system

N-by-3 matrix of scalar

Position readings of the GNSS receiver in the geodetic latitude, longitude, and altitude (LLA) coordinate system, returned as an N-by-3 matrix of scalars. Altitude is the height above the reference ellipsoid model, WGS84. N is the number of samples in the input argument. Latitude and longitude are in degrees. Altitude is in meters.

Data Types: single | double

velocityReadings — Velocity readings in local navigation coordinate system (m/s)

N-by-3 matrix of scalar

Velocity reading of the GNSS receiver in the local navigation coordinate system in meters per second, returned as an *N*-by-3 matrix of scalars. *N* is the number of samples in the input arguments.

Data Types: single | double

status — Status information of visible satellites

N-element array of structure

Status information of visible satellites, returned as an N-element array of structures. N is the number of samples in the input arguments. Each structure contains these four fields:

Field Name	Description
SatelliteAzimuth	Azimuth angles of visible satellites, returned as an <i>M</i> -element vector of scalars in degrees. <i>M</i> is the number of visible satellites.
SatelliteElevation	Elevation angles of visible satellites, returned as an <i>M</i> -element vector of scalars in degrees. <i>M</i> is the number of visible satellites.
HDOP	Horizontal dilution of precision, returned as a scalar.
VDOP	Vertical dilution of precision, returned as a scalar.

To plot the satellite positions, see the skyplot function.

Object Functions

To use an object function, specify the System object as the first input argument. For example, to release system resources of a System object named obj, use this syntax:

release(obj)

Common to All System Objects

clone Create duplicate System object step Run System object algorithm

release Release resources and allow changes to System object property values and input

characteristics

reset Reset internal states of System object

isDone End-of-data status

Examples

Generate GNSS Position and Velocity Readings

Generate target positions and velocities based on a waypoint trajectory.

```
rng(2020) % For repeatable results
fs = 0.1;
tArrival = 50;
tspan = 0:1/fs:tArrival;
% Create a waypoint trajectory.
trajectory = waypointTrajectory([0,0,0;1,1,1]*500,[0,tArrival]);
[positions,~,velocities] = lookupPose(trajectory,tspan)
positions = 6 \times 3
         0
                   0
            100.0000
  100.0000
                      100.0000
  200.0000
           200.0000
                      200.0000
  300.0000 300.0000
                      300.0000
  400.0000 400.0000
                      400.0000
  500.0000 500.0000 500.0000
velocities = 6 \times 3
   10.0000
             10.0000
                       10.0000
   10.0000
             10.0000
                       10,0000
   10.0000
            10.0000
                       10.0000
   10.0000
            10.0000
                       10,0000
   10.0000
                       10.0000
            10.0000
   10.0000
             10.0000
                       10.0000
```

Create a GNSS System object. Use the LLA position for Natick, MA as the local reference frame origin of the trajectory.

```
refLocNatick = [42.2825 -71.343 53.0352];
gnss = gnssSensor('SampleRate',fs, ...
    'ReferenceLocation',refLocNatick);
```

Generate position and velocity readings based on the GNSS object.

[llaReadings, velocityReadings, status] = gnss(positions, velocities)

```
llaReadings = 6×3

42.2825 -71.3430 53.5746

42.2834 -71.3418 -46.3343

42.2843 -71.3406 -147.0774

42.2852 -71.3394 -245.6328

42.2861 -71.3382 -348.8382

42.2870 -71.3369 -446.5622
```

```
velocityReadings = 6 \times 3
```

SatelliteElevation

```
9.9810
           10.0000
                    10.0532
  10.0125
          10.0150
                    10.0009
  10.0157 10.0172
                     9.9796
          10.0117
   9.9701
                    9.9882
  10.0253
           9.9749
                   10.0887
          10.0183
   9.9720
                     9.9637
status=6×1 struct array with fields:
   SatelliteAzimuth
```

More About

HDOP VDOP

Orbital Parameters

The satellite positions and velocities are defined by orbital parameters from IS-GPS-200K Interface Specification, and are given in the Earth-Centered Earth-Fixed (ECEF) coordinates.

Position calculations use equations from Table 30-II in the same IS-GPS-200K Interface Specification.

Velocity calculations use equations 8.21-8.27 in *Principles of GNSS, Inertial, and Multisensor Integrated Navigation Systems*[1].

References

[1] Groves, Paul D. *Principles of GNSS, Inertial, and Multisensor Integrated Navigation Systems*. 2nd ed, Artech House, 2013.

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

Usage notes and limitations:

See "System Objects in MATLAB Code Generation" (MATLAB Coder).

See Also

Objects

gpsSensor|imuSensor

Functions

gnssconstellation | lookangles | pseudoranges | receiverposition | skyplot

Introduced in R2020b

monteCarloLocalization

Localize robot using range sensor data and map

Description

The monteCarloLocalization System object creates a Monte Carlo localization (MCL) object. The MCL algorithm is used to estimate the position and orientation of a vehicle in its environment using a known map of the environment, lidar scan data, and odometry sensor data.

To localize the vehicle, the MCL algorithm uses a particle filter to estimate the vehicle's position. The particles represent the distribution of likely states for the vehicle, where each particle represents a possible vehicle state. The particles converge around a single location as the vehicle moves in the environment and senses different parts of the environment using a range sensor. An odometry sensor measures the vehicle's motion.

A monteCarloLocalization object takes the pose and lidar scan data as inputs. The input lidar scan sensor data is given in its own coordinate frame, and the algorithm transforms the data according to the SensorModel.SensorPose property that you must specify. The input pose is computed by integrating the odometry sensor data over time. If the change in pose is greater than any of the specified update thresholds, UpdateThresholds, then the particles are updated and the algorithm computes a new state estimate from the particle filter. The particles are updated using this process:

- The particles are propagated based on the change in the pose and the specified motion model, MotionModel.
- The particles are assigned weights based on the likelihood of receiving the range sensor reading for each particle. These likelihood weights are based on the sensor model you specify in SensorModel.
- Based on the ResamplingInterval property, the particles are resampled from the posterior distribution, and the particles of low weight are eliminated. For example, a resampling interval of 2 means that the particles are resampled after every other update.

The outputs of the object are the estimated pose and covariance, and the value of <code>isUpdated</code>. This estimated state is the mean and covariance of the highest weighted cluster of particles. The output pose is given in the map's coordinate frame that is specified in the <code>SensorModel.Map</code> property. If the change in pose is greater than any of the update thresholds, then the state estimate has been updated and <code>isUpdated</code> is <code>true</code>. Otherwise, <code>isUpdated</code> is <code>false</code> and the estimate remains the same. For continuous tracking the best estimate of a robot's state, repeat this process of propagating particles, evaluating their likelihood, and resampling.

To estimate robot pose and covariance using lidar scan data:

- 1 Create the monteCarloLocalization object and set its properties.
- 2 Call the object with arguments, as if it were a function.

To learn more about how System objects work, see What Are System Objects?.

Creation

Syntax

```
mcl = monteCarloLocalization
mcl = monteCarloLocalization(Name, Value)
```

Description

mcl = monteCarloLocalization returns an MCL object that estimates the pose of a vehicle using a map, a range sensor, and odometry data. By default, an empty map is assigned, so a valid map assignment is required before using the object.

mcl = monteCarloLocalization(Name, Value) creates an MCL object with additional options
specified by one or more Name, Value pair arguments.

Name is a property name and Value is the corresponding value. Name must appear inside single quotes (''). You can specify several name-value pair arguments in any order as Name1, Value1, . . . , NameN, ValueN.

Properties

InitialPose — Initial pose of vehicle

[0 0 0] (default) | three-element vector

Initial pose of the vehicle used to start localization, specified as a three-element vector, [x y theta], that indicates the position and heading of the vehicle. Initializing the MCL object with an initial pose estimate enables you to use a smaller value for the maximum number of particles and still converge on a location.

InitialCovariance — Covariance of initial pose

```
diag([1 1 1]) (default) | diagonal matrix | three-element vector | scalar
```

Covariance of the Gaussian distribution for the initial pose, specified as a diagonal matrix. Three-element vector and scalar inputs are converted to a diagonal matrix. This matrix gives an estimate of the uncertainty of the InitialPose.

GlobalLocalization — Flag to start global localization

```
false (default) | true
```

Flag indicating whether to perform global localization, specified as false or true. The default value, false, initializes particles using the InitialPose and InitialCovariance properties. A true value initializes uniformly distributed particles in the entire map and ignores the InitialPose and InitialCovariance properties. Global localization requires a large number of particles to cover the entire workspace. Use global localization only when the initial estimate of vehicle location and orientation is not available.

ParticleLimits — Minimum and maximum number of particles

```
[500 5000] (default) | two-element vector
```

Minimum and maximum number of particles, specified as a two-element vector, [min max].

SensorModel — Likelihood field sensor model

likelihoodFieldSensor object

Likelihood field sensor model, specified as a likelihoodFieldSensor object. The default value uses the default likelihoodFieldSensorModel object. After using the object to get output, call release on the object to make changes to SensorModel. For example:

```
mcl = monteCarloLocalization;
[isUpdated,pose,covariance] = mcl(ranges,angles);
release(mcl)
mcl.SensorModel.NumBeams = 120;
```

MotionModel — Odometry motion model for differential drive

odometryMotionModel object

Odometry motion model for differential drive, specified as an odometryMotionModel object. The default value uses the default odometryMotionModel object. After using the object to get output, call release on the object to make changes to MotionModel. For example:

```
mcl = monteCarloLocalization;
[isUpdated,pose,covariance] = mcl(ranges,angles);
release(mcl)
mcl.MotionModel.Noise = [0.25 0.25 0.4 0.4];
```

UpdateThresholds — Minimum change in states required to trigger update

[0.2 0.2 0.2] (default) | three-element vector

Minimum change in states required to trigger update, specified as a three-element vector. The localization updates the particles if the minimum change in any of the [x y theta] states is met. The pose estimate updates only if the particle filter is updated.

ResamplingInterval — Number of filter updates between resampling of particles

1 (default) | positive integer

Number of filter updates between resampling of particles, specified as a positive integer.

UseLidarScan — Use lidarScan object as scan input

```
false (default) | true
```

Use a lidarScan object as scan input, specified as either false or true.

Usage

Syntax

```
[isUpdated,pose,covariance] = mcl(odomPose,scan)
[isUpdated,pose,covariance] = mcl(odomPose,ranges,angles)
```

Description

[isUpdated, pose, covariance] = mcl(odomPose, scan) estimates the pose and covariance of a vehicle using the MCL algorithm. The estimates are based on the pose calculated from the specified vehicle odometry, odomPose, and the specified lidar scan sensor data, scan. mcl is the

monteCarloLocalization object. isUpdated indicates whether the estimate is updated based on the UpdateThreshold property.

To enable this syntax, you must set the UseLidarScan property to true. For example:

```
mcl = monteCarloLocalization('UseLidarScan',true);
...
[isUpdated,pose,covariance] = mcl(odomPose,scan);
```

[isUpdated,pose,covariance] = mcl(odomPose,ranges,angles) specifies the lidar scan data as ranges and angles.

Input Arguments

odomPose — Pose based on odometry

three-element vector

Pose based on odometry, specified as a three-element vector, $[x \ y \ theta]$. This pose is calculated by integrating the odometry over time.

scan — Lidar scan readings

lidarScan object

Lidar scan readings, specified as a lidarScan object.

Dependencies

To use this argument, you must set the UseLidarScan property to true.

```
mcl.UseLidarScan = true:
```

ranges — Range values from scan data

vector

Range values from scan data, specified as a vector with elements measured in meters. These range values are distances from a laser scan sensor at the specified angles. The ranges vector must have the same number of elements as the corresponding angles vector.

angles — Angle values from scan data

vector

Angle values from scan data, specified as a vector with elements measured in radians. These angle values are the angles at which the specified ranges were measured. The angles vector must be the same length as the corresponding ranges vector.

Output Arguments

isUpdated — Flag for pose update

logical

Flag for pose update, returned as a logical. If the change in pose is more than any of the update thresholds, then the output is true. Otherwise, it is false. A true output means that updated pose and covariance are returned. A false output means that pose and covariance are not updated and are the same as at the last update.

pose — Current pose estimate

three-element vector

Current pose estimate, returned as a three-element vector, [x y theta]. The pose is computed as the mean of the highest-weighted cluster of particles.

covariance — Covariance estimate for current pose

matrix

Covariance estimate for current pose, returned as a matrix. This matrix gives an estimate of the uncertainty of the current pose. The covariance is computed as the covariance of the highest-weighted cluster of particles.

Object Functions

To use an object function, specify the System object as the first input argument. For example, to release system resources of a System object named obj, use this syntax:

```
release(obj)
```

Specific to monteCarloLocalization

getParticles Get particles from localization algorithm

Common to All System Objects

step Run System object algorithm

release Release resources and allow changes to System object property values and input

characteristics

reset Reset internal states of System object

Examples

Estimate Vehicle Pose from Range Sensor Data

Create a monteCarloLocalization object, assign a sensor model, and calculate a pose estimate using the step method.

Note: Starting in R2016b, instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, y = step(obj,x) and y = obj(x) perform equivalent operations.

Create a monteCarloLocalization object. Set the UseLidarScan property to true.

```
mcl = monteCarloLocalization;
mcl.UseLidarScan = true;
```

Assign a sensor model with an occupancy grid map to the object.

```
sm = likelihoodFieldSensorModel;
p = zeros(200,200);
sm.Map = occupancyMap(p,20);
mcl.SensorModel = sm;
Create sample laser scan data input.
ranges = 10*ones(1,300);
```

ranges(1,130:170) = 1.0;

References

- [1] Thrun, Sebatian, Wolfram Burgard, and Dieter Fox. Probabilistic Robotics. MIT Press, 2005.
- [2] Dellaert, F., D. Fox, W. Burgard, and S. Thrun. "Monte Carlo Localization for Mobile Robots." *Proceedings 1999 IEEE International Conference on Robotics and Automation.*

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

lidarScan | likelihoodFieldSensorModel | odometryMotionModel

Topics

"Localize TurtleBot Using Monte Carlo Localization"
"Monte Carlo Localization Algorithm"
Class Attributes
Property Attributes

Introduced in R2019b

getParticles

Get particles from localization algorithm

Syntax

```
[particles,weights] = getParticles(mcl)
```

Description

[particles,weights] = getParticles(mcl) returns the current particles used by the monteCarloLocalization object. particles is an *n*-by-3 matrix that contains the location and orientation of each particle. Each row has a corresponding weight value specified in weights. The number of rows can change with each iteration of the MCL algorithm. Use this method to extract the particles and analyze them separately from the algorithm.

Examples

Get Particles from Monte Carlo Localization Algorithm

Get particles from the particle filter used in the Monte Carlo Localization object.

Create a map and a Monte Carlo localization object.

```
map = binaryOccupancyMap(10,10,20);
mcl = monteCarloLocalization(map);

Create robot data for the range sensor and pose.

ranges = 10*ones(1,300);
ranges(1,130:170) = 1.0;
angles = linspace(-pi/2,pi/2,300);
odometryPose = [0 0 0];

Initialize particles using step.

[isUpdated,estimatedPose,covariance] = step(mcl,odometryPose,ranges,angles);
Get particles from the updated object.

[particles,weights] = getParticles(mcl);
```

Input Arguments

```
mcl — monteCarloLocalization object
```

handle

monteCarloLocalization object, specified as an object handle.

Output Arguments

particles — Estimation particles

n-by-3 vector

Estimation particles, returned as an n-by-3 vector, [x y theta]. Each row corresponds to the position and orientation of a single particle. The length can change with each iteration of the algorithm.

weights — Weights of particles

n-by-1 vector

Weights of particles, returned as a *n*-by-1 vector. Each row corresponds to the weight of the particle in the matching row of particles. These weights are used in the final estimate of the pose of the vehicle. The length can change with each iteration of the algorithm.

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

monteCarloLocalization

Topics

"Monte Carlo Localization Algorithm"

Introduced in R2019b

multiLayerMap

Manage multiple map layers

Description

The multiLayerMap object groups and stores multiple map layers as mapLayer, occupancyMap, or binaryOccupancyMap objects.

Once added to this object, map layers can be modified by either using the multiLayerMap object functions or by performing actions on individual map layers using their object functions or the layer name as input. Any modification to common properties on the multiLayerMap object are reflected across all associated layers.

Creation

Syntax

```
map = multiLayerMap
map = multiLayerMap(maps)
map = multiLayerMap(names,mapData)
map = multiLayerMap(names,width,height)
map = multiLayerMap(names,width,height,cellDims)
map = multiLayerMap(names,rows,cols,'grid')
map = multiLayerMap(names,rows,cols,cellDims,'grid')
map = multiLayerMap(sourceMap)
map = multiLayerMap(____,Name,Value)
```

Description

map = multiLayerMap creates an empty map object occupying 10-by-10 meters of space with a resolution of 1 cell per meter.

map = multiLayerMap(maps) creates a multilayer map from a cell array of mapLayer,
occupancyMap, or binaryOccupancyMap objects. Objects combined into a multilayer map must be
defined with the same resolution and cover the same region in space, but can represent different
categories of information over the shared region.

map = multiLayerMap(names, mapData) creates a multilayer map from the cell array of layer names and associated cell array of map matrices. Matrices must have the same first two dimensions to cover the same shared region. Default resolution is 1 cell per meter.

map = multiLayerMap(names, width, height) creates a multilayer map with the cell array of layer names covering the specified width and height as scalars in meters.

map = multiLayerMap(names, width, height, cellDims) creates a multilayer map where the size of the data stored in each cell of the map is defined by the array of integers, cellDims. For multiple layers, cellDims is a cell array of integer arrays. map = multiLayerMap(names, rows, cols, 'grid') specifies the map width and height as a grid size specified in the rows and cols inputs.

map = multiLayerMap(names, rows, cols, cellDims, 'grid') creates a map with a specified
grid size and the size of the data stored in each cell is defined by the array of integers or cell array of
integer arrays cellDims.

map = multiLayerMap(sourceMap) creates a new object using the layers copied from another
multiLayerMap object.

map = multiLayerMap(____, Name, Value) specifies property values using name-value pairs.

For example, multiLayerMap(__,'LocalOriginInWorld',[15 20]) sets the local origin to a specific world location.

Properties

DataSize — Size of the data in each map layer data array

cell array of integer vectors

Size of the data in each map layer data array, specified as a cell array of integer vectors. In each vector, the first two dimensions define the footprint of the map layer, and all subsequent dimensions dictate the size and layout of the data stored in each cell.

If the map stores an n-element vector of values in each cell, this property would be [width height n].

If the map stores a 10-by-10 grid with each cell containing a 3-by-3-by-3 matrix array, the data size would be [10 10 3 3 3].

After you create the object, this property is read-only.

Data Types: cell | double

DataType — Data type of the values stored

cell array of string scalars

Data type of the values stored in each layer, specified as a cell array of character vectors.

When you create this object, the specified map layers determine each data type. After you create the object, this property is read-only.

Data Types: cell | char

DefaultValue — Default value for unspecified map locations

{0} (default) | cell array of numeric scalars

Default value for unspecified map locations for each layer, specified as a cell array of numeric scalars. This default value is returned for areas outside the map as well.

Data Types: cell | double

GridLocationInWorld — **Location of the grid in local coordinates**

[0 0] (default) | two-element vector | [xWorld yWorld]

Location of the bottom-left corner of the grid in world coordinates, specified as a two-element vector, [xWorld yWorld].

You can set this property when you create the object.

Data Types: double

GridOriginInLocal — Location of the grid in local coordinates

[0 0] (default) | two-element vector | [xLocal yLocal]

Location of the bottom-left corner of the grid in local coordinates, specified as a two-element vector, [xLocal yLocal].

You can set this property when you create the object.

Data Types: double

GridSize — Number of rows and columns in grid

two-element integer-valued vector

This property is read-only.

Number of rows and columns in grid, stored as a 1-by-2 real-valued vector representing the number of rows and columns, in that order.

Data Types: double

LayerNames — **Name of each layer**

cell array of string scalars

Name of each layer, specified as a cell array of string scalars. The order of these names are associated with the order of other properties that are cell arrays.

You can set this property when you create the object. After you create the object, this property is read-only.

Data Types: cell | string

LocalOriginInWorld — Location of the local frame in world coordinates

[0 0] (default) | two-element vector | [xWorld yWorld]

Location of the origin of the local frame in world coordinates, specified as a two-element vector, [xLocal yLocal]. Use the move function to shift the local frame as your vehicle moves.

You can set this property when you create the object.

Data Types: double

NumLayers — Number of map layers

1 (default) | positive integer

This property is read-only.

Number of map layers, stored as a positive integer.

Data Types: double

Resolution — **Grid resolution**

1 (default) | scalar

This property is read-only.

Grid resolution, stored as a scalar in cells per meter representing the number and size of grid locations.

You can set this property when you create the object. After you create the object, this property is read-only.

Data Types: double

XLocalLimits — Minimum and maximum values of x-coordinates in local frame

two-element vector

This property is read-only.

Minimum and maximum values of x-coordinates in local frame, stored as a two-element horizontal vector of the form [min max]. Local frame is defined by LocalOriginInWorld property.

Data Types: double

YLocalLimits — Minimum and maximum values of y-coordinates in local frame

two-element vector

This property is read-only.

Minimum and maximum values of *y*-coordinates in local frame, stored as a two-element horizontal vector of the form [min max]. Local frame is defined by LocalOriginInWorld property.

Data Types: double

XWorldLimits — Minimum and maximum world range values of x-coordinates

two-element vector

This property is read-only.

Minimum and maximum world range values of *x*-coordinates, stored as a 1-by-2 vector representing the minimum and maximum values, in that order.

Data Types: double

YWorldLimits — Minimum and maximum world range values of y-coordinates

two-element vector

This property is read-only.

Minimum and maximum world range values of *y*-coordinates, stored as a 1-by-2 vector representing the minimum and maximum values, in that order.

Data Types: double

Object Functions

getLayer Return individual layers from multilayer map

getMapData Retrieve data from map layers

grid2local Convert grid indices to local coordinates grid2world Convert grid indices to world coordinates local2grid Convert local coordinates to grid indices

local2world Convert local coordinates to world coordinates

move Move map in world frame setMapData Assign data to map layers syncWith Sync map with overlapping map

world2grid Convert world coordinates to grid indices world2local Convert world coordinates to local coordinates

Examples

Create Listeners Using Dependent Map Layers

The multiLayerMap object enables you to group multiple map layers and define behavior for those layers when setting and getting data. Using separate map layers, you can store various map data and specify different behaviors for each. You can also define the SetTransformFcn and GetTransformFcn function handles for a map layer so that dependencies are created between layers. This example shows how to store data in a map layer and implement event listeners which update other maps. These maps store how many times the data is updated or accessed.

Dependent Layers

Create two independent map layers.

```
mapAccessed = mapLayer(zeros(10,10), 'LayerName', 'GetListener');
mapModified = mapLayer(zeros(10,10), 'LayerName', 'SetListener');
```

Specify function handles for the get and set transform functions used in the main map layer. These functions increment the value of a grid location when you get or set map data in the input map mainMap. See Listener Function Handles on page 2-0 for the function implementation.

```
setHookFcn = @(mainMap,values,varargin)exampleHelperSetHookFcn(mapModified,mainMap,values,varargin
getHookFcn = @(mainMap,values,varargin)exampleHelperGetHookFcn(mapAccessed,mainMap,values,varargin)exampleHelperGetHookFcn(mapAccessed,mainMap,values,varargin)exampleHelperGetHookFcn(mapAccessed,mainMap,values,varargin)exampleHelperGetHookFcn(mapAccessed,mainMap,values,varargin)exampleHelperGetHookFcn(mapAccessed,mainMap,values,varargin)exampleHelperGetHookFcn(mapAccessed,mainMap,values,varargin)exampleHelperGetHookFcn(mapAccessed,mainMap,values,varargin)exampleHelperGetHookFcn(mapAccessed,mainMap,values,varargin)exampleHelperGetHookFcn(mapAccessed,mainMap,values,varargin)exampleHelperGetHookFcn(mapAccessed,mainMap,values,varargin)exampleHelperGetHookFcn(mapAccessed,mainMap,values,varargin)exampleHelperGetHookFcn(mapAccessed,mainMap,values,varargin)exampleHelperGetHookFcn(mapAccessed,mainMap,values,varargin)exampleHelperGetHookFcn(mapAccessed,mainMap,values,varargin)exampleHelperGetHookFcn(mapAccessed,mainMap,values,varargin)exampleHelperGetHookFcn(mapAccessed,mainMap,values,varargin)exampleHelperGetHookFcn(mapAccessed,mainMap,values,varargin)exampleHelperGetHookFcn(mapAccessed,mainMap,values,varargin)exampleHelperGetHookFcn(mapAccessed,mainMap,values,varargin)exampleHelperGetHookFcn(mapAccessed,mainMap,values,varargin)exampleHelperGetHookFcn(mapAccessed,mainMap,values,varargin)exampleHelperGetHookFcn(mapAccessed,mainMap,values,varargin)exampleHelperGetHookFcn(mapAccessed,mainMap,values,varargin)exampleHelperGetHookFcn(mapAccessed,mainMap,values,varargin)exampleHelperGetHookFcn(mapAccessed,mainMap,values,varargin)exampleHelperGetHookFcn(mapAccessed,mainMap,values,varargin)exampleHelperGetHookFcn(mapAccessed,mainMap,values,varargin)exampleHelperGetHookFcn(mapAccessed,mainMap,values,varargin)exampleHelperGetHookFcn(mapAccessed,mainMap,values,varargin)exampleHelperGetHookFcn(mapAccessed,mainMap,values,varargin)exampleHelperGetHookFcn(mapAccessed,mainMap,values,varargin)exampleHelperGetHookFcn(mapAccessed,mainMap
```

Create the main map layer with default values of 0.5. Specify the function handles to create the layer depencies.

Add all maps to the same multiLayerMap object.

```
mapLayers = multiLayerMap({map,mapAccessed,mapModified});
```

Set the (0,0) map location with a value of zero using the setMapData object function of map.

```
setMapData(map,[0 0],0)
```

Check that mapModified incremented their value.

```
getMapData(mapModified,[0 0])
```

Get the data you just set to the main map layer. The expected value of zero is returned.

```
getMapData(map,[0 0])
```

ans = 1

```
ans = 0
```

Check that mapAccessed incremented their value.

```
getMapData(mapAccessed,[0 0])
```

ans = 1

Update the entire map with a matrix of values. Access the data as well.

setMapData(map,rand(10,10))
getMapData(map)

alls	=	IUXIU

0.6443	0.2077	0.3111	0.5949	0.0855	0.9631	0.0377	0.1068	0.0305	0.3
0.3786	0.3012	0.9234	0.2622	0.2625	0.5468	0.8852	0.6538	0.7441	0.2
0.8116	0.4709	0.4302	0.6028	0.8010	0.5211	0.9133	0.4942	0.5000	0.8
0.5328	0.2305	0.1848	0.7112	0.0292	0.2316	0.7962	0.7791	0.4799	0.0
0.3507	0.8443	0.9049	0.2217	0.9289	0.4889	0.0987	0.7150	0.9047	0.4
0.9390	0.1948	0.9797	0.1174	0.7303	0.6241	0.2619	0.9037	0.6099	0.3
0.8759	0.2259	0.4389	0.2967	0.4886	0.6791	0.3354	0.8909	0.6177	0.9
0.5502	0.1707	0.1111	0.3188	0.5785	0.3955	0.6797	0.3342	0.8594	0.7
0.6225	0.2277	0.2581	0.4242	0.2373	0.3674	0.1366	0.6987	0.8055	0.5
0.5870	0.4357	0.4087	0.5079	0.4588	0.9880	0.7212	0.1978	0.5767	0.4

Check that ${\tt mapModified}$ and ${\tt mapAccessed}$ incremented their values.

getMapData(mapModified)

ans = 10×10

1	1	1	1	1	1	1	1	1	1
1	1	1	1	1	1	1	1	1	1
1	1	1	1	1	1	1	1	1	1
1	1	1	1	1	1	1	1	1	1
1	1	1	1	1	1	1	1	1	1
1	1	1	1	1	1	1	1	1	1
1	1	1	1	1	1	1	1	1	1
1	1	1	1	1	1	1	1	1	1
1	1	1	1	1	1	1	1	1	1
2	1	1	1	1	1	1	1	1	1

getMapData(mapAccessed)

ans = 10×10

1	1	1	1	1	1	1	1	1	1
1	1	1	1	1	1	1	1	1	1
1	1	1	1	1	1	1	1	1	1
1	1	1	1	1	1	1	1	1	1
1	1	1	1	1	1	1	1	1	1
1	1	1	1	1	1	1	1	1	1
1	1	1	1	1	1	1	1	1	1
1	1	1	1	1	1	1	1	1	1
1	1	1	1	1	1	1	1	1	1
2	1	1	1	1	1	1	1	1	1

The bottom-left location returns two and all other values are one. This confirms the listener functions are working as intended.

Listener Function Handles

These functions implement the get and set example helper functions that update the other map layers.

```
function valuesOut = exampleHelperSetHookFcn(modifiedMap,sourceLayer,valueIn,varargin)
   % Pass output through
   valuesOut = valueIn;
   % If no additional inputs are passed, return immediately.
   if numel(varargin) == 0
        return:
    else
        % Otherwise, increment the value in the modifiedMap.
        if numel(varargin) == 1
            currentValue = getMapData(modifiedMap);
            setMapData(modifiedMap,currentValue+1);
        else
            currentValue = getMapData(modifiedMap,varargin{1},varargin{3:end});
            % setMapData syntax <<<<>>>
            setMapData(modifiedMap,varargin{1},currentValue+1,varargin{3:end});
       end
   end
end
function data = exampleHelperGetHookFcn(accessedMap,sourceLayer,valuesIn,varargin)
   data = valuesIn;
   % If no additional inputs are passed, check if the values in
   if numel(varargin) == 0
        if isequal(size(valuesIn), sourceLayer.DataSize)
            % Increment the depedent map.
            currentValue = getMapData(accessedMap);
            setMapData(accessedMap,currentValue+1);
        end
   else
        currentValue = getMapData(accessedMap,varargin{:});
        setMapData(accessedMap,varargin{1},currentValue+1,varargin{3:end});
    end
end
```

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

Objects

binaryOccupancyMap | mapLayer | occupancyMap | occupancyMap3D

Functions

getMapData | move | setMapData | syncWith

Topics

"Fuse Multiple Lidar Sensors Using Map Layers"

Introduced in R2021a

getLayer

Return individual layers from multilayer map

Syntax

mapLayer = getLayer(map,layerName)

Description

mapLayer = getLayer(map,layerName) returns the individual map layer, specified by the layer
name layerName. For a list of all layer names, see the LayerNames property of the multiLayerMap
object map.

.

Input Arguments

map — Multilayer map

multiLayerMap object

Multilayer map, specified as a multiLayerMap object.

layerName — Name of individual map layer

string scalar | character vector

Name of individual map layer, specified as a string scalar or character vector.

Data Types: char | string

Output Arguments

mapLayer — Individual map layer

binaryOccupancyMap object | occupancyMap object | mapLayer object

Individual map layer, returned as a binaryOccupancyMap, occupancyMap, or mapLayer object as a handle. For more information, see "Handle Object Behavior".

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

Objects

binaryOccupancyMap | mapLayer | occupancyMap | occupancyMap3D

Functions

getMapData | move | setMapData | syncWith

Topics"Fuse Multiple Lidar Sensors Using Map Layers"

Introduced in R2021a

getMapData

Retrieve data from map layers

Syntax

```
mapData = getMapData(map)
mapData = getMapData(map,layername)
mapData = getMapData(map,layername,layerinputs)
```

Description

mapData = getMapData(map) returns a cell array of matrices for the data in each layer of the
specified multiLayerMap object. For binary or occupancy map layers, the values of this function are
passed to the getOccupancy function. mapData is returned as an cell-array of matrices for each
layer.

mapData = getMapData(map,layername) returns all the map data for the specified layer name.
mapData is returned as a matrix equal to the DataSize of the specified layer.

mapData = getMapData(map,layername,layerinputs) takes the layerinputs arguments and passes them to the getMapData object function for the specified map layer name. To access individual cells or blocks of data in the world, local, or grid coordinates, see the syntaxes of getMapData.

Examples

Create Listeners Using Dependent Map Layers

The multiLayerMap object enables you to group multiple map layers and define behavior for those layers when setting and getting data. Using separate map layers, you can store various map data and specify different behaviors for each. You can also define the SetTransformFcn and GetTransformFcn function handles for a map layer so that dependencies are created between layers. This example shows how to store data in a map layer and implement event listeners which update other maps. These maps store how many times the data is updated or accessed.

Dependent Layers

Create two independent map layers.

```
mapAccessed = mapLayer(zeros(10,10), 'LayerName', 'GetListener');
mapModified = mapLayer(zeros(10,10), 'LayerName', 'SetListener');
```

Specify function handles for the get and set transform functions used in the main map layer. These functions increment the value of a grid location when you get or set map data in the input map mainMap. See Listener Function Handles on page 2-0 for the function implementation.

```
set HookFcn = @(mainMap, values, varargin) example HelperSet HookFcn (mapModified, mainMap, values, varargin) example HelperSet HookFcn (mapAccessed, mainMap, values, v
```

Create the main map layer with default values of 0.5. Specify the function handles to create the layer depencies.

```
map = mapLayer(repmat(0.5,10,10),...
                  'GetTransformFcn',getHookFcn,...
'SetTransformFcn',setHookFcn);
Add all maps to the same multiLayerMap object.
mapLayers = multiLayerMap({map,mapAccessed,mapModified});
Set the (0,0) map location with a value of zero using the setMapData object function of map.
setMapData(map,[0 0],0)
Check that mapModified incremented their value.
getMapData(mapModified,[0 0])
ans = 1
Get the data you just set to the main map layer. The expected value of zero is returned.
getMapData(map,[0 0])
ans = 0
Check that mapAccessed incremented their value.
getMapData(mapAccessed,[0 0])
ans = 1
Update the entire map with a matrix of values. Access the data as well.
setMapData(map,rand(10,10))
getMapData(map)
ans = 10 \times 10
    0.6443
               0.2077
                           0.3111
                                      0.5949
                                                 0.0855
                                                            0.9631
                                                                       0.0377
                                                                                  0.1068
                                                                                              0.0305
                                      0.2622
                                                                       0.8852
    0.3786
               0.3012
                          0.9234
                                                 0.2625
                                                            0.5468
                                                                                  0.6538
                                                                                              0.7441
                                                                                  0.4942
               0.4709
                          0.4302
                                                 0.8010
                                                                                              0.5000
    0.8116
                                      0.6028
                                                            0.5211
                                                                       0.9133
    0.5328
               0.2305
                          0.1848
                                      0.7112
                                                 0.0292
                                                            0.2316
                                                                       0.7962
                                                                                  0.7791
                                                                                              0.4799
               0.8443
                          0.9049
                                      0.2217
                                                 0.9289
                                                            0.4889
                                                                       0.0987
                                                                                  0.7150
                                                                                              0.9047
    0.3507
    0.9390
               0.1948
                          0.9797
                                      0.1174
                                                 0.7303
                                                            0.6241
                                                                       0.2619
                                                                                  0.9037
                                                                                              0.6099
                                                                                  0.8909
```

Check that mapModified and mapAccessed incremented their values.

0.2967

0.3188

0.4242

0.5079

0.4886

0.5785

0.2373

0.4588

0.6791

0.3955

0.3674

0.9880

0.3354

0.6797

0.1366

0.7212

0.3342

0.6987

0.1978

0.4389

0.1111

0.2581

0.4087

getMapData(mapModified)

0.2259

0.1707

0.2277

0.4357

0.8759

0.5502

0.6225

0.5870

```
ans = 10 \times 10
      1
               1
                       1
                                1
                                         1
                                                 1
                                                          1
                                                                  1
                                                                           1
                                                                                    1
                        1
                                1
                                         1
                                                 1
                                                          1
```

0.

0.

0.

0.0

0.4

0.

0.9 0.

0.

0.6177

0.8594

0.8055

0.5767

1	1	1	1	1	1	1	1	1	1
1	1	1	1	1	1	1	1	1	1
1	1	1	1	1	1	1	1	1	1
1	1	1	1	1	1	1	1	1	1
1	1	1	1	1	1	1	1	1	1
1	1	1	1	1	1	1	1	1	1
1	1	1	1	1	1	1	1	1	1
2	1	1	1	1	1	1	1	1	1

getMapData(mapAccessed)

```
ans = 10 \times 10
      1
              1
                      1
                              1
                                      1
                                              1
                                                      1
                                                              1
                                                                      1
                                                                              1
      1
              1
                      1
                              1
                                      1
                                              1
                                                      1
                                                              1
                                                                      1
                                                                              1
      1
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              1
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                                      1
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      1
              1
                      1
                              1
                                      1
                                              1
                                                      1
                                                              1
                                                                      1
                                                                              1
      2
                      1
                              1
                                      1
                                              1
                                                      1
                                                                      1
              1
                                                              1
                                                                              1
```

The bottom-left location returns two and all other values are one. This confirms the listener functions are working as intended.

Listener Function Handles

These functions implement the get and set example helper functions that update the other map layers.

```
function valuesOut = exampleHelperSetHookFcn(modifiedMap,sourceLayer,valueIn,varargin)
   % Pass output through
   valuesOut = valueIn;
   % If no additional inputs are passed, return immediately.
   if numel(varargin) == 0
        return;
   else
        % Otherwise, increment the value in the modifiedMap.
        if numel(varargin) == 1
            currentValue = getMapData(modifiedMap);
            setMapData(modifiedMap,currentValue+1);
        else
            currentValue = getMapData(modifiedMap,varargin{1},varargin{3:end});
            % setMapData syntax <<<<>>>>
            setMapData(modifiedMap,varargin{1},currentValue+1,varargin{3:end});
        end
    end
end
function data = exampleHelperGetHookFcn(accessedMap,sourceLayer,valuesIn,varargin)
   data = valuesIn;
```

```
% If no additional inputs are passed, check if the values in
if numel(varargin) == 0
    if isequal(size(valuesIn),sourceLayer.DataSize)
        % Increment the depedent map.
        currentValue = getMapData(accessedMap);
        setMapData(accessedMap,currentValue+1);
    end
else
    currentValue = getMapData(accessedMap,varargin{:});
    setMapData(accessedMap,varargin{1},currentValue+1,varargin{3:end});
end
end
```

Input Arguments

map — Multilayer map

multiLayerMap object

Multilayer map, specified as a multiLayerMap object.

layername — Map layer name

string scalar | character array

Map layer name, specified as a string scalar or character array. Map layers have their name specified when creating the multiLayerMap object.

layerinputs — Variable-length inputs to map layer

varargin

Variable-length inputs to getMapData function of map layer, specified as varargin. To specify individual cells or blocks of data in the world, local, or grid coordinates, see the syntaxes of getMapData.

Output Arguments

mapData — Data values from map layer

matrix

Data values from map layer, returned as a matrix. By default, the function returns all data on the layer as an M-by-N-by-DataDims matrix. M and N are the grid height and width respectively. DataDims are the dimensions of the map data, map.DataSize(3,:).

For other syntaxes, the map data may be given as an array of values with size N-by-DataDims or as a subregion of the full matrix.

See Also

Objects

binaryOccupancyMap|mapLayer|multiLayerMap|occupancyMap|occupancyMap3D

Functions

getMapData | move | setMapData | syncWith

Introduced in R2021a

setMapData

Assign data to map layers

Syntax

```
setMapData(map,layername,layerinputs)
inBounds = setMapData(map,layername,layerinputs)
```

Description

setMapData(map, layername, layerinputs) takes the layerinputs arguments and passes them to the setMapData object function for the specified map layer name. To specify individual cells or blocks of data in the world, local, or grid coordinates, see the syntaxes of setMapData.

inBounds = setMapData(map, layername, layerinputs) returns an array of values for the given locations in the layerinputs input argument.

Examples

Create Listeners Using Dependent Map Layers

The multiLayerMap object enables you to group multiple map layers and define behavior for those layers when setting and getting data. Using separate map layers, you can store various map data and specify different behaviors for each. You can also define the SetTransformFcn and GetTransformFcn function handles for a map layer so that dependencies are created between layers. This example shows how to store data in a map layer and implement event listeners which update other maps. These maps store how many times the data is updated or accessed.

Dependent Layers

Create two independent map layers.

```
mapAccessed = mapLayer(zeros(10,10), 'LayerName', 'GetListener');
mapModified = mapLayer(zeros(10,10), 'LayerName', 'SetListener');
```

Specify function handles for the get and set transform functions used in the main map layer. These functions increment the value of a grid location when you get or set map data in the input map mainMap. See Listener Function Handles on page 2-0 for the function implementation.

```
setHookFcn = @(mainMap,values,varargin)exampleHelperSetHookFcn(mapModified,mainMap,values,vararg.
getHookFcn = @(mainMap,values,varargin)exampleHelperGetHookFcn(mapAccessed,mainMap,values,vararg.
```

Create the main map layer with default values of 0.5. Specify the function handles to create the layer depencies.

Add all maps to the same multiLayerMap object.

```
mapLayers = multiLayerMap({map,mapAccessed,mapModified});
Set the (0,0) map location with a value of zero using the setMapData object function of map.
setMapData(map,[0 0],0)
Check that mapModified incremented their value.
getMapData(mapModified,[0 0])
ans = 1
Get the data you just set to the main map layer. The expected value of zero is returned.
getMapData(map,[0 0])
ans = 0
Check that mapAccessed incremented their value.
getMapData(mapAccessed,[0 0])
ans = 1
Update the entire map with a matrix of values. Access the data as well.
setMapData(map,rand(10,10))
getMapData(map)
ans = 10 \times 10
    0.6443
               0.2077
                          0.3111
                                     0.5949
                                                0.0855
                                                           0.9631
                                                                      0.0377
                                                                                 0.1068
                                                           0.5468
               0.3012
                          0.9234
                                                0.2625
    0.3786
                                     0.2622
                                                                      0.8852
                                                                                 0.6538
               0.4709
                          0.4302
                                                           0.5211
    0.8116
                                     0.6028
                                                0.8010
                                                                      0.9133
                                                                                 0.4942
               0.2305
                                                           0.2316
                                                                      0.7962
                                                                                 0.7791
    0.5328
                          0.1848
                                     0.7112
                                                0.0292
```

0.2217

0.1174

0.2967

0.3188

0.4242

0.5079

0.9289

0.7303

0.4886

0.5785

0.2373

0.4588

0.4889

0.6241

0.6791

0.3955

0.3674

0.9880

0.0987

0.2619

0.3354

0.6797

0.1366

0.7212

0.7150

0.9037

0.8909

0.3342

0.6987

0.1978

0.0305

0.7441

0.5000

0.4799

0.9047

0.6099

0.6177

0.8594

0.8055

0.5767

0.

0.

0.8

0.

0.4

0.

0.

0.

0.

0.4

Check that ${\tt mapModified}$ and ${\tt mapAccessed}$ incremented their values.

0.9049

0.9797

0.4389

0.1111

0.2581

0.4087

getMapData(mapModified)

0.8443

0.1948

0.2259

0.1707

0.2277

0.4357

0.3507

0.9390

0.8759

0.5502

0.6225

0.5870

ans = 10×10 1

getMapData(mapAccessed)

```
ans = 10 \times 10
      1
             1
                     1
                             1
                                     1
                                             1
                                                    1
                                                            1
                                                                    1
                                                                            1
      1
             1
                     1
                             1
                                     1
                                             1
                                                    1
                                                            1
                                                                    1
                                                                            1
      1
             1
                     1
                             1
                                     1
                                             1
                                                    1
                                                            1
                                                                    1
                                                                            1
      1
             1
                     1
                             1
                                     1
                                             1
                                                    1
                                                            1
                                                                    1
                                                                            1
      1
             1
                     1
                             1
                                     1
                                             1
                                                    1
                                                            1
                                                                    1
                                                                            1
      1
             1
                     1
                             1
                                     1
                                             1
                                                    1
                                                            1
                                                                    1
                                                                            1
      1
             1
                     1
                             1
                                     1
                                             1
                                                    1
                                                            1
                                                                    1
                                                                            1
      1
                     1
                             1
             1
                                     1
                                             1
                                                    1
                                                            1
                                                                    1
                                                                            1
      1
             1
                     1
                             1
                                     1
                                             1
                                                    1
                                                            1
                                                                    1
                                                                            1
      2
             1
                     1
                             1
                                     1
                                             1
                                                    1
                                                            1
                                                                    1
                                                                            1
```

The bottom-left location returns two and all other values are one. This confirms the listener functions are working as intended.

Listener Function Handles

These functions implement the get and set example helper functions that update the other map layers.

```
function valuesOut = exampleHelperSetHookFcn(modifiedMap,sourceLayer,valueIn,varargin)
    % Pass output through
   valuesOut = valueIn;
   % If no additional inputs are passed, return immediately.
    if numel(varargin) == 0
        return;
   else
        % Otherwise, increment the value in the modifiedMap.
        if numel(varargin) == 1
            currentValue = getMapData(modifiedMap);
            setMapData(modifiedMap,currentValue+1);
        else
            currentValue = getMapData(modifiedMap,varargin{1},varargin{3:end});
            % setMapData syntax <<<>>>>
            setMapData(modifiedMap,varargin{1},currentValue+1,varargin{3:end});
       end
   end
end
function data = exampleHelperGetHookFcn(accessedMap,sourceLayer,valuesIn,varargin)
   data = valuesIn;
   % If no additional inputs are passed, check if the values in
    if numel(varargin) == 0
        if isequal(size(valuesIn), sourceLayer.DataSize)
            % Increment the depedent map.
            currentValue = getMapData(accessedMap);
            setMapData(accessedMap,currentValue+1);
        end
   else
        currentValue = getMapData(accessedMap,varargin{:});
        setMapData(accessedMap,varargin{1},currentValue+1,varargin{3:end});
```

end end

Input Arguments

map — Multilayer map

multiLayerMap object

Multilayer map, specified as a multiLayerMap object.

layername — Map layer name

string scalar | character array

Map layer name, specified as a string scalar or character array. Map layers have their name specified when creating the multiLayerMap object.

layerinputs — Variable-length inputs to map layer

varargin

Variable-length inputs to setMapData function of the map layer, specified as varargin. To specify individual cells or blocks of data in the world, local, or grid coordinates, see the syntaxes of setMapData.

Output Arguments

inBounds — Valid map locations

n-by-1 column vector

Valid map locations, returned as an n-by-1 column vector equal in length to xy or ij. Locations inside the map limits return a value of 1. Locations outside the map limits return a value of 0.

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

Objects

binaryOccupancyMap | mapLayer | multiLayerMap | occupancyMap | occupancyMap3D

Functions

getMapData | move | setMapData | syncWith

Introduced in R2021a

gpsdev

Connect to a GPS receiver connected to host computer

Description

The gpsdev System object connects to a GPS receiver connected to the host computer.

To connect to a GPS receiver:

- **1** Create the **gpsdev** object and set its properties.
- **2** Call the object with arguments, as if it were a function.

To learn more about how System objects work, see What Are System Objects?.

Creation

Syntax

```
gps0bj = gpsdev(port)
gps0bj = gpsdev(serialobj)
gps0bj = gpsdev(port, ____, Name, Value)
```

Description

```
gpsObj = gpsdev(port) connects to a GPS Receiver at the specified serial port of host computer.
gpsObj = gpsdev(serialobj) connects to a GPS Receiver specified by a serial object.
gpsObj = gpsdev(port, ____, Name, Value) connects to a GPS Receiver on the specified port or specified through a serial object, using one or more name-value pairs.
```

Properties

Unless otherwise indicated, properties are *nontunable*, which means you cannot change their values after calling the object. Objects lock when you call them, and the release function unlocks them.

If a property is *tunable*, you can change its value at any time.

For more information on changing property values, see System Design in MATLAB Using System Objects.

```
BaudRate — Baud rate 9600
```

This property is read-only.

The baud rate for serial communication. The baud rate is set at 9600 bits/sec. The GPS receiver must be configured to work at 9600 bits/sec . If your GPS receiver is configured to some other baud rate, reconfigure it to 9600 bits/sec to use <code>gpsdev</code> function.

ReadMode — Specify which data samples to be returned

```
'latest' (default) | 'oldest'
```

Specify whether to return the latest or the oldest data samples. The number of samples depends on the SamplesPerRead value. The data read from the GPS receiver is stored in the MATLAB buffer.

- latest Provides the latest data samples available in the buffer. All previous data samples in the buffer are discarded. For example, if SamplesPerRead = 3, the latest three data samples read by the GPS receiver are returned.
- oldest Provides the oldest data samples available in the buffer. In this case, no data samples are discarded. For example, if SamplesPerRead = 3, the first three data samples read are returned for the first read, the next three data samples are returned for the second read, and so on.

Tunable: No

Data Types: character vector | string

SamplesRead — Samples read

double

This property is read-only.

Number of samples read from the GPS receiver using the read function, after the object is locked. The gpsdev object gets locked either at the first call of the read function after the object creation or at the first call of the read function after the execution of the release function.

Data Types: double

Samples Available — Samples in the host buffer

double

This property is read-only.

Samples available in the host buffer. When you release the object, SamplesAvailable is set to 0.

Data Types: double

SamplesPerRead — Samples per read

1 (default)

Samples read from the first read, specified as a positive integer in the range [1 10].

Tunable: No

Data Types: double

OutputFormat — Set output format

```
'timetable' (default) | 'matrix'
```

Set the output format of the data returned by executing the read function.

When the OutputFormat is set to timetable, the timetable returned has the following fields:

- LLA (Latitude, Longitude, Altitude)
- · Ground Speed
- · Course over ground
- Dilution of Precisions(DOPs), VDOP, HDOP, PDOP,
- · GPS Receiver Time
- Time System time when the data is read, in datetime or duration format

When the OutputFormat is set to matrix, the data is returned as matrices of Time, LLA, Ground Speed, Course over ground, DOPs, and GPS receiver time. The units for the GPS receiver readings are the same as the timetable format.

Tunable: Yes

Data Types: character vector | string

TimeFormat — Set the format of the time displayed when the GPS data is read

```
'datetime' (default) | 'duration'
```

Set the format of the time displayed when the GPS data is read.

- datetime Displays the date and time at which the data is read.
- duration Displays the time elapsed in seconds after the GPS object is locked. The gpsdev object gets locked either at the first call of the read function after the object creation or at the first call of the read function after the execution of the release function.

Tunable: Yes

Data Types: character vector | string

Object Functions

To use an object function, specify the System object as the first input argument. For example, to release system resources of a System object named obj, use this syntax:

release(obj)

flush Flush all GPS data accumulated in the buffers and reset properties

info Read Update Rate, GPS Lock information and number of satellites in View for the GPS

receiver

read Read data from GPS receiver release Release the GPS object

writeBytes Write raw commands to the GPS receiver

Examples

Create GPS Connection

Connect to a GPS receiver connected to a specific port.

```
gps0bj = gpsdev('COM4')
gps0bj =
```

Create GPS Connection Using Serial Object

Connect to a GPS Receiver on the Specified Port with Additional Name-Value options

More About

GPS Modules

To verify the functionality, the following GPS modules were used:

- Adafruit Ultimate GPS
- Ublox NEO 6M
- Ublox NEO 7M

See Also

nmeaParser

Introduced in R2020b

nmeaParser

Parse data from standard NMEA sentences sent from GNSS receivers

Description

The nmeaParser System object parses data from some of the standard NMEA (National Marine Electronics Association) sentences, which are sent from a GNSS (Global Navigation Satellite System) receiver. The NMEA sentences that need parsing must be compliant with the NMEA 0183® Standard, Version 4.1.

To parse data from NMEA sentences:

- 1 Create the nmeaParser object and set its properties.
- **2** Call the object with arguments, as if it were a function.

To learn more about how System objects work, see What Are System Objects?.

The nmeaParser System object outputs an array of structures corresponding to the values extracted from the specified NMEA sentences.

Creation

Syntax

```
pnmea = nmeaParser
pnmea = nmeaParser('MessageIDs', msgID)
```

Description

pnmea = nmeaParser returns a nmeaParser System object, pnmea, with default properties, that extracts data from these NMEA messages: RMC, GGA, and GSA. The order of structure arrays in the extracted output data is also: RMC, GGA, and GSA.

pnmea = nmeaParser('MessageIDs', msgID) returns a nmeaParser System object, pnmea, that extracts data from the NMEA messages specified using the Message IDs. Specify msgID as "RMC", "GGA", "GSA", "GSV", "VTG", "GLL", "GST", "ZDA", and "HDT", or a combination of these IDs (for example: ["VTG", "GLL", "HDT"]). The order in which you specify the Message IDs determines the order of the structure arrays in the extracted output data. The default value is ["RMC", "GGA", "GSA"].

Properties

Unless otherwise indicated, properties are *nontunable*, which means you cannot change their values after calling the object. Objects lock when you call them, and the release function unlocks them.

If a property is *tunable*, you can change its value at any time.

For more information on changing property values, see System Design in MATLAB Using System Objects.

MessageIDs — Message IDs of NMEA sentences to extract data

["RMC", "GGA", "GSA"] (default) | RMC | GGA | GSA | GSV | VTG | GLL | GST | ZDA | HDT

Message IDs of NMEA sentences, which are compliant with the NMEA 0183 Standard, from which you want to extract data. You can specify multiple message IDs as an array of strings to extract data from NMEA sentences.

Data Types: char | string

Usage

Syntax

[rmcData,ggaData,gsaData,vtgData,gllData,gstData,gsvData,zdaData,hdtData] =
pnmea(rawData)

Description

[rmcData,ggaData,gsaData,vtgData,gllData,gstData,gsvData,zdaData,hdtData] = pnmea(rawData) parses data and returns an array of structures, where each structure corresponds to a single Message ID. The sequence that you specify for the output arguments must be the same sequence that you specified for the Message IDs when creating the nmeaParser System object.

Input Arguments

rawData — NMEA data as obtained from a GNSS receiver

string array

NMEA data, which is compliant with NMEA 0183 Standard, as obtained from a GNSS receiver.

Data Types: string | char

Output Arguments

rmcData — Data extracted from RMC sentence

structure

Data extracted from an RMC sentence. The output structure contains the information parsed from an RMC sentence along with the parsing status. If multiple RMC sentences are found in the input data, then an array of structures is returned. For more details, see "RMC Sentences" on page 2-580.

ggaData — Data extracted from GGA sentence

structure

Data extracted from a GGA sentence. The output structure contains the information parsed from a GGA sentence along with the parsing status. If multiple GGA sentences are found in the input data, then an array of structures is returned. For more details, see "GGA Sentences" on page 2-581.

gsaData — Data extracted from GSA sentence

structure

Data extracted from a GSA sentence. The output structure contains the information parsed from a GSA sentence along with the parsing status. If multiple GSA sentences are found in the input data, then an array of structures is returned. For more details, see "GSA Sentences" on page 2-583.

vtgData — Data extracted from VTG sentence

structure

Data extracted from a VTG sentence. The output structure contains the information parsed from a VTG sentence along with the parsing status. If multiple VTG sentences are found in the input data, then an array of structures is returned. For more details, see "VTG Sentences" on page 2-587.

gllData — Data extracted from GLL sentence

structure

Data extracted from a GLL sentence. The output structure contains the information parsed from a GLL sentence along with the parsing status. If multiple GLL sentences are found in the input data, then an array of structures is returned. For more details, see "GLL Sentences" on page 2-586.

gstData — Data extracted from GST sentence

structure

Data extracted from a GST sentence. The output structure contains the information parsed from a GST sentence along with the parsing status. If multiple GST sentences are found in the input data, then an array of structures is returned. For more details, see "GST Sentences" on page 2-588.

gsvData — Data extracted from GSV sentence

structure

Data extracted from a GSV sentence. The output structure contains the information parsed from a GSV sentence along with the parsing status. The complete satellite information is available in multiple gsvData structures. Each gsvData structure can have a maximum of four satellite information. For more details, see "GSV Sentences" on page 2-584.

zdaData — Data extracted from ZDA sentence

structure

Data extracted from a ZDA sentence. The output structure contains the information parsed from a ZDA sentence along with the parsing status. If multiple ZDA sentences are found in the input data, then an array of structures is returned. For more details, see "ZDA Sentences" on page 2-586.

hdtData — Data extracted from HDT sentence

structure

Data extracted from an HDT sentence. The output structure contains the information parsed from an HDT sentence along with the parsing status. If multiple HDT sentences are found in the input data, then an array of structures is returned. For more details, see "HDT Sentences" on page 2-589.

Object Functions

To use an object function, specify the System object as the first input argument. For example, to release system resources of a System object named obj, use this syntax:

release(obj)

Examples

Extract Data from NMEA Sentences

Extract data from NMEA sentences that are obtained from a GNSS receiver.

Extract Data from RMC Sentence

Create an nmeaParser System Object by specifying the Message ID as "RMC".

```
pnmea = nmeaParser("MessageID","RMC");
```

Provide the RMC sentence obtained from the GNSS receiver as the input and extract data.

```
unparsedRMCLine='$GNRMC,143909.00,A,5107.0020216,N,11402.3294835,W,0.036,348.3,210307,0.0,E,A*31 rmcData = pnmea(unparsedRMCLine)
```

Extract Data from Multiple NMEA Message Types

Provide GGA, GSA, and RMC sentences as the input.

Create a string array to include the three sentences

```
rawNMEAData = [unparsedGGALine ,newline, unparsedGSALine ,newline, unparsedRMCLine]

rawNMEAData =

'$GPGGA,111357.771,5231.364,N,01324.240,E,1,12,1.0,0.0,M,0.0,M,,*69

$GPGSA,A,3,01,02,03,04,05,06,07,08,09,10,11,12,1.0,1.0,1.0*30

$GPRMC,111357.771,A,5231.364,N,01324.240,E,10903,221.5,020620,000.0,W*44'
```

However, consider that you need to extract data only from GGA and GSA sentences. So create the nmeaParser System Object 'pnmea', and specify the 'GGA' and 'GSA' Message IDs as a string array.

```
pnmea=nmeaParser("MessageIDs",["GGA","GSA"]);
```

Specify the output arguments for all the three sentences to extract the data as structures.

```
[ggaData,gsaData] = pnmea(rawNMEAData)
```

```
ggaData = struct with fields:
                          TalkerID: "GP"
                         MessageID: "GGA"
                           UTCTime: 11:13:57.771
                          Latitude: 52.5227
                         Longitude: 13.4040
                  QualityIndicator: 1
                NumSatellitesInUse: 12
                              HDOP: 1
                          Altitude: 0
                   GeoidSeparation: 0
             AgeOfDifferentialData: NaN
   DifferentialReferenceStationID: NaN
                            Status: 0
gsaData = struct with fields:
              TalkerID: "GP"
             MessageID: "GSA"
                  Mode: "A"
               FixType: 3
   SatellitesIDNumber: [1 2 3 4 5 6 7 8 9 10 11 12]
                  PDOP: 1
                  VDOP: 1
                  HDOP: 1
              SystemID: NaN
                Status: 0
```

HD0P

The above output shows that only GGA and GSA sentences are extracted based on the Message IDs specified as input.

Provide another GGA sentence as an additional input, and extract data. In this case, you need not modify the System object as the Message ID has not changed.

```
unparsedGGALine1='$GNGGA,001043.00,4404.14036,N,12118.85961,W,1,12,0.98,1113.0,M,-21.3,M,,*47'
unparsedGGALine1 =
'$GNGGA,001043.00,4404.14036,N,12118.85961,W,1,12,0.98,1113.0,M,-21.3,M,,*47'
rawNMEAData = [unparsedGGALine ,newline, unparsedGSALine ,newline, unparsedGGALine1]
rawNMEAData =
    $GPGGA,111357.771,5231.364,N,01324.240,E,1,12,1.0,0.0,M,0.0,M,,*69
    $GPGSA,A,3,01,02,03,04,05,06,07,08,09,10,11,12,1.0,1.0,1.0*30
    $GNGGA,001043.00,4404.14036,N,12118.85961,W,1,12,0.98,1113.0,M,-21.3,M,,*47
[ggaData,gsaData] = pnmea(rawNMEAData)
ggaData=1×2 struct array with fields:
    TalkerID
   MessageID
   UTCTime
   Latitude
   Longitude
   QualityIndicator
   NumSatellitesInUse
```

```
Altitude
   GeoidSeparation
   AgeOfDifferentialData
   DifferentialReferenceStationID
    Status
gsaData = struct with fields:
              TalkerID: "GP"
             MessageID: "GSA"
                  Mode: "A"
               FixType: 3
    SatellitesIDNumber: [1 2 3 4 5 6 7 8 9 10 11 12]
                  PDOP: 1
                  VDOP: 1
                  HDOP: 1
              SystemID: NaN
                Status: 0
```

A status of **0** indicates that the data was parsed successfully.

Extract Data from GSV Sentence

Create an nmeaParser System Object by specifying the Message ID as "GSV".

```
pnmea = nmeaParser("MessageID", "GSV");
```

Provide the GSV sentence obtained from the GNSS receiver as the input and extract data.

Extract Data from Multiple GSV Sentences

Provide multiple GSV sentences as the input.

```
unparsedGSVLine1 = '$GPGSV,3,1,10,01,,,31,03,28,325,40,10,,,33,12,20,047,30*70';
unparsedGSVLine2 = '$GPGSV,3,2,10,14,88,028,42,22,39,299,48,25,,,25,31,79,289,46*49';
unparsedGSVLine3 = '$GPGSV,3,3,10,32,69,205,41,46,47,215,39*79';

Create a string array to include the three sentences.

CRLF = [char(13),newline];
unparsedGSVLines = [unparsedGSVLine1,CRLF, unparsedGSVLine2, CRLF, unparsedGSVLine3];
```

Create the nmeaParser System Object 'pnmea', specify the 'GSV' Message ID, and extract data.

```
pnmea = nmeaParser("MessageIDs","GSV");
gsvData = pnmea(unparsedGSVLines)

gsvData=1×3 struct array with fields:
    TalkerID
    MessageID
    NumSentences
    SentenceNumber
    SatellitesInView
    SatelliteID
    Elevation
    Azimuth
    SNR
    SignalID
    Status
```

Read Data from NMEA Log

Read data from a sample NMEA log, so that the data can be parsed using the nmeaParser System Object.

The sample log file is nmeaLog.nmea, which is included in this example.

```
f = fopen('nmeaLog.nmea');
unParsedNMEAdata = fread(f);
pnmea = nmeaParser("MessageIDs",["RMC","GGA"]);
[rmcStruct, ggaStruct] = pnmea(unParsedNMEAdata)
rmcStruct=1×9 struct array with fields:
   TalkerID
   MessageID
   FixStatus
   Latitude
   Longitude
   GroundSpeed
   TrueCourseAngle
   UTCDateTime
   MagneticVariation
   ModeIndicator
   NavigationStatus
   Status
ggaStruct=1×9 struct array with fields:
    TalkerID
   MessageID
   UTCTime
   Latitude
   Longitude
   QualityIndicator
   NumSatellitesInUse
   HDOP
   Altitude
   GeoidSeparation
   AgeOfDifferentialData
```

DifferentialReferenceStationID
Status

More About

Status Field

The status field displayed along with the extracted values in each output structure can be used to determine the parsing status:

- Status: 0 Sentence is valid (checksum validation is successful and the extracted data is as per the requested Message ID)
- Status: 1 Checksum of the sentence to be parsed is invalid
- Status: 2 The requested sentence is not found in the input data

Note If a value is not available in the input sentence, the corresponding output value is displayed as "NA" for string values and "NaN" for numeric values.

RMC Sentences

Name of field displayed in the output structure after parsing is complete	Description
TalkerID	Identify the type of device that transmits data. For example, for a GPS receiver, the TalkerID is GP
	Data type: string
MessageID	Type of NMEA message - RMC
	Data type: string
FixStatus	Possible values:
	A - Data is valid
	V - Navigation receiver warning
	Data type: string
Latitude	Latitude in degrees. North is considered positive.
	Data type: double
Longitude	Longitude in degrees. East is considered positive.
	Data type: double
GroundSpeed	Speed over ground in meters per second (m/s)
	Data type: double

Name of field displayed in the output structure after parsing is complete	Description
TrueCourseAngle	Course over ground in degrees.
	Data type: double
UTCDateTime	UTC date and time
	Data type: datetime
MagneticVariation	Magnetic variation value. Direction W is considered as negative
	Data type: double
ModeIndicator	Possible values:
	• N - No fix
	E - Estimated/Dead reckoning fix
	A - Autonomous GNSS fix
	D - Differential GNSS fix
	F - RTK float
	M - Manual input mode
	P - Precision mode
	Data type: string
NavigationStatus	Possible values:
	• S - Safe
	C - Caution
	• U = Unsafe
	V = Navigational Status not valid
	Data type: string

GGA Sentences

Name of field displayed in the output structure after parsing is complete	Description
TalkerID	Identify the type of device that transmits data. For example, for a GPS receiver, the TalkerID is GP
	Data type: string
MessageID	Type of NMEA message – GGA
	Data type: string
UTCTime	UTC Time (hhmmss.ss)
	Data type: datetime

Name of field displayed in the output structure after parsing is complete	Description
Latitude	Latitude in degrees. North is considered positive.
	Data type: double
Longitude	Longitude in degrees. East is considered positive.
	Data type: double
QualityIndicator	Possible values:
	• 0 - No fix
	• 1 - Fix Valid
	2 - Differential GPS, SPS mode fix
	• 4 - RTK fix
	• 5 - RTK float
	6 - Estimated/Dead reckoning fix
	7 - Manual input mode
	8 - Simulator mode
	Data type: uint8
NumSatellitesInUse	Number of satellites used. This could be different from number of satellites in view.
	Data type: uint8
HDOP	Horizontal dilution of precision
	Data type: double
Altitude	Altitude above mean sea level in meters
	Data type: double
GeoidSeparation	Difference between ellipsoid and mean sea level in meters
	Data type: double
AgeOfDifferentialData	Age of differential corrections
	Data type: double
DifferentialReferenceStationID	ID of station providing differential corrections
	Data type: uint16

GSA Sentences

Name of field displayed in the output structure after parsing is complete	Description
TalkerID	Identify the type of device that transmits data. For example, for a GPS receiver, the TalkerID is GP
	Data type: string
MessageID	Type of NMEA message - GSA
	Data type: string
Mode	Possible values:
	• M - Manually set to operate in 2-D or 3-D mode
	A - Automatic switching between 2-D or 3-D mode
	Data type: string
FixType	Possible values:
	• 1 - No fix
	• 2 - 2-D fix
	• 3 - 3-D fix
	Data type: uint8
SatellitesIDNumber	Satellite numbers (array of 12 bytes). Empty fields will be displayed as Nan.
	Data type: uint8
PDOP	Position dilution of precision
	Data type: double
VDOP	Vertical dilution of precision
	Data type: double
HDOP	Horizontal Dilution of Precision
	Data type: double
SystemID	NMEA defined GNSS System ID
	Data type: uint8

GSV Sentences

Name of field displayed in the output structure after parsing is complete	Description
TalkerID	Identify the type of device that transmits data. For example, for a GPS receiver, the TalkerID is GP
	Data type: string
MessageID	Type of NMEA message - GSV
	Data type: string
NumSentences	Total number of sentences. The complete satellite information is available in multiple GSV sentences. This field indicates the total number of gsvData structures containing the complete information per update.
SentenceNumber	Data type: double Sentence number of the currently parsed GSV
Sentencerumber	line
	Data type: double
SatellitesInView	Total number of satellites in view
	Data type: double
SatelliteID	Satellite ID numbers specified as a row vector of size 1-by-N, where N is the number of satellite information available in one sentence. The maximum allowed valued of N is 4.
	Data type: double
Elevation	Elevation in degrees, specified as a row vector of size 1-by-N, where N is the number of satellite information available in one sentence. The maximum allowed valued of N is 4.
	The maximum value of Elevation is 90 degrees.
	Data type: double
Azimuth	Azimuth in degrees, specified as a row vector of size 1-by-N, where N is the number of satellite information available in one sentence. The maximum allowed valued of N is 4.
	The range of Azimuth value is [0-359] degrees.
	Data type: double

Name of field displayed in the output structure after parsing is complete	Description
SNR	Signal-to-noise ratio in dB-Hz, specified as a row vector of size 1-by-N, where N is the number of satellite information available in one sentence. The maximum allowed valued of N is 4. The range of SNR value is [0,99] dB.
	Data type: double
SignalID	Signal ID corresponding to the SatelliteID.
	This value is displayed only if the sentences conform to NMEA 0183 Standard, Version 4.1. Otherwise, the value displayed is NaN.
	Data type: double

The possible values of SignalID and the corresponding Signal Channel are listed in this table.

System	TalkerID displayed in the parsed data	SatelliteID	SignalID	Signal Channel
GPS	GP	• 1 - 32 (for GPS)	0	All signals
		• 33 - 64 (for	1	L1 C/A
		SBAS)	2	L1 P (Y)
			3	L1 M
			4	L2 P (Y)
			5	L2C-M
			6	L2C-L
			7	L5-I
		8	L5-Q	
GLONASS	GLONASS GL	• 33 - 64 (for SBAS)	0	All signals
			1	G1 C/A
	• 65 – 99 (for GLONASS)	2	G1 P	
		3	G2 C/A	
		4	GLONASS (M) G2 P	
GALILEO			0	All signals
		Galileo	1	E5a
	satellites) • 37 - 64 (for Galileo SBAS)	2	E5b	
		3	E5a and E5b	
			4	E6-A
		5	E6-BC	

TalkerID displayed in the parsed data	SatelliteID	SignalID	Signal Channel
		6	L1-A
		7	L1-BC

ZDA Sentences

Name of field displayed in the output structure after parsing is complete	Description
TalkerID	Identify the type of device that transmits data. For example, for a GPS receiver, the TalkerID is GP
	Data type: string
MessageID	Type of NMEA message - ZDA
	Data type: string
UTCTime	UTC Time
	Data type: datetime
UTCDay	UTC Day
	Data type: uint8
UTCMonth	UTC Month
	Data type: uint8
UTCYear	UTC Year
	Data type: uint8
LocalZoneHours	Local zone hours ranging from 00 to +/-13
	Data type: int8
LocalZoneMinutes	Local zone minutes ranging from 00 to 59
	Data type: uint8

GLL Sentences

Name of field displayed in the output structure after parsing is complete	Description
TalkerID	Identify the type of device that transmits data. For example, for a GPS receiver, the TalkerID is GP
	Data type: string

Name of field displayed in the output structure after parsing is complete	Description
MessageID	Type of NMEA message - GLL
	Data type: string
Latitude	Latitude in degrees. North is considered positive.
	Data type: double
Longitude	Longitude in degrees. East is considered positive.
	Data type: double
UTCTime	UTC Time
	Data type: datetime
DataValidity	Data validity status:
	A – Data valid
	V - Data invalid
	Data type: string
PositioningMode	Possible values:
	N - Data not Valid
	E - Estimated/Dead reckoning mode
	A – Autonomous mode
	D - Differential mode
	S - Simulator Mode
	M - Manual input mode
	Data type: string

VTG Sentences

Name of field displayed in the output structure after parsing is complete	Description
TalkerID	Identify the type of device that transmits data. For example, for a GPS receiver, the TalkerID is GP
	Data type: string
MessageID	Type of NMEA message - VTG
	Data type: string
TrueCourseAngle	Course over ground (true) in degrees
	Data type: double

Name of field displayed in the output structure after parsing is complete	Description
MagneticCourseAngle	Course over ground (magnetic) in degrees
	Data type: double
GroundSpeed	Speed over ground in meters per second (m/s)
	Data type: double
ModeIndicator	Possible values:
	• N - No fix
	E - Estimated/Dead reckoning mode
	A - Autonomous mode
	D - Differential mode
	M - Manual input mode
	N - Data not valid
	• P - Precise
	S - Simulator mode
	Data type: string

GST Sentences

Name of field displayed in the output structure after parsing is complete	Description
TalkerID	Identify the type of device that transmits data. For example, for a GPS receiver, the TalkerID is GP
	Data type: string
MessageID	Type of NMEA message - GST
	Data type: string
UTCTime	UTC Time
	Data type: datetime
RMSStdDeviationOfRanges	RMS value of the standard deviation of the ranges in meters.
	Data type: double
StdDeviationSemiMajorAxis	Standard deviation of semi-major axis in meters
	Data type: double
StdDeviationSemiMinorAxis	Standard deviation of semi-minor axis in meters
	Data type: double

Name of field displayed in the output structure after parsing is complete	Description
OrientationSemiMajorAxis	Orientation of semi-major axis, in degrees
	Data type: double
StdDeviationLatitudeError	Standard deviation of latitude error, in meters
	Data type: double
StdDeviationLongitudeError	Standard deviation of longitude error in meters
	Data type: double
StdDeviationAltitudeError	Standard deviation of altitude error in meters
	Data type: double

HDT Sentences

Name of field displayed in the output structure after parsing is complete	Description
TalkerID	Identify the type of device that transmits data. For example, for a GPS receiver, the TalkerID is GP
	Data type: string
MessageID	Type of NMEA message - HDT
	Data type: string
TrueHeadingAngle	Heading in degrees with respect to true north
	Data type: double

See Also

skyplot

Topics

"Plot Position of GNSS Receiver Using Live NMEA Data or NMEA Log File"

Introduced in R2020b

navPath

Planned path

Description

The navPath object stores paths that are typically created by geometric path planners. Path points are stored as states in an associated state space.

Creation

Syntax

```
path = navPath
path = navPath(space)
path = navPath(space, states)
```

Description

path = navPath creates a path object, path, using the SE2 state space with default settings.

path = navPath(space) creates a path object with state space specified by space. The space
input also sets the value of the StateSpace property.

path = navPath(space, states) allows you to initialize the path with state samples given by states. Specify states as a matrix of state samples. States that are outside of the StateBounds of the state space object are reduced to the bounds. The states input also sets the value of the States property.

Properties

StateSpace — State space for path

stateSpaceSE2 (default) | state space object

State space for the path, specified as a state space object. Each state in the path is a sample from the specified state space. You can use objects such as stateSpaceSE2, stateSpaceDubins, or stateSpaceReedsShepp as a state space object. You can also customize a state space object using the nav.StateSpace object.

Data Types: object

States — States of path

zeros(0,StateSpace.NumStateVariables) (default) | real-valued M-by-N matrix

States of the path, specified as a real-valued M-by-N matrix. M is the number of states in the path, and N is the dimension of each state. You can only set this property during object creation or using the append function.

Data Types: double

NumStates — Number of state samples in path

```
0 (default) | nonnegative integer
```

Number of state samples in the path, specified as a nonnegative integer. The number is the same as the number of rows of the state matrix specified in the States property.

Data Types: double

Object Functions

append Add states to end of path copy Create copy of path object interpolate Interpolate points along path

pathLength Length of path

Examples

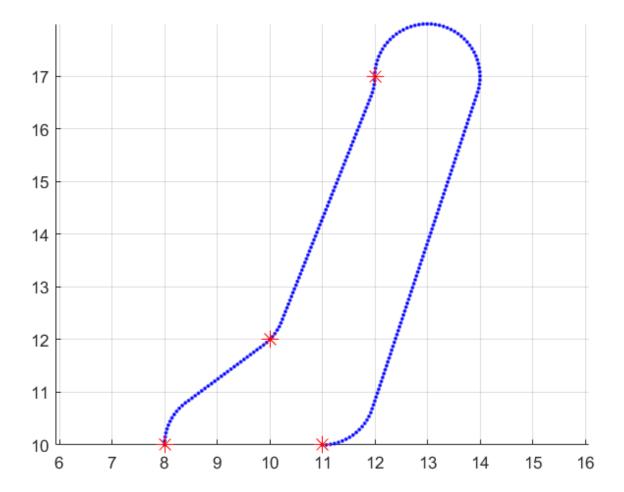
Create navPath Based on Multiple Waypoints

Create a navPath object based on multiple waypoints in a Dubins space.

```
dubinsSpace = stateSpaceDubins([0 25; 0 25; -pi pi])
dubinsSpace =
  stateSpaceDubins with properties:
   SE2 Properties
                 Name: 'SE2 Dubins'
          StateBounds: [3×2 double]
    NumStateVariables: 3
   Dubins Vehicle Properties
     MinTurningRadius: 1
pathobj = navPath(dubinsSpace)
pathobj =
  navPath with properties:
    StateSpace: [1x1 stateSpaceDubins]
        States: [0×3 double]
     NumStates: 0
waypoints = [...
    8 10 pi/2;
    10 12 pi/4;
    12 17 pi/2;
    11 10 -pi];
append(pathobj, waypoints);
Interpolate that path so that it contains exactly 250 points.
interpolate(pathobj, 250)
```

Visualize the interpolated path and the original waypoints.

```
figure;
grid on;
axis equal;
hold on;
plot(pathobj.States(:,1), pathobj.States(:,2), ".b");
plot(waypoints(:,1), waypoints(:,2), "*r", "MarkerSize", 10)
```



Calculate length of path.

```
len = pathLength(pathobj);
disp("Path length = " + num2str(len))
Path length = 19.37
```

See Also

nav.StateSpace|pathmetrics|stateSpaceDubins|stateSpaceReedsShepp| stateSpaceSE2

Introduced in R2019b

append

Add states to end of path

Syntax

```
append(path,states)
```

Description

append(path, states) appends the state samples, states, to the end of the path.

Examples

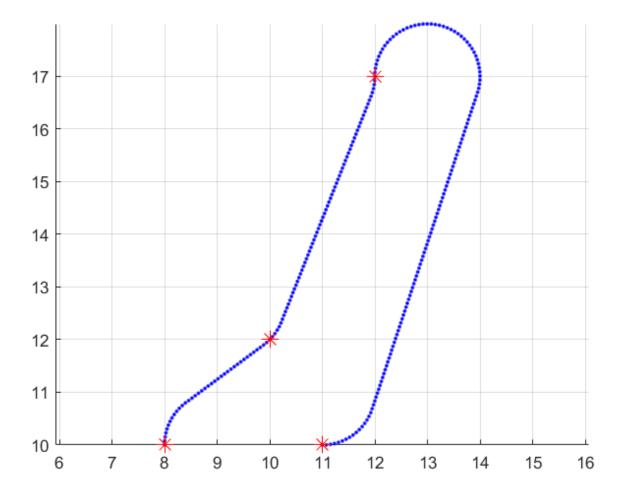
Create navPath Based on Multiple Waypoints

Create a navPath object based on multiple waypoints in a Dubins space.

```
dubinsSpace = stateSpaceDubins([0 25; 0 25; -pi pi])
dubinsSpace =
  stateSpaceDubins with properties:
   SE2 Properties
                 Name: 'SE2 Dubins'
          StateBounds: [3×2 double]
    NumStateVariables: 3
   Dubins Vehicle Properties
     MinTurningRadius: 1
pathobj = navPath(dubinsSpace)
pathobj =
 navPath with properties:
    StateSpace: [1x1 stateSpaceDubins]
        States: [0×3 double]
     NumStates: 0
waypoints = [...
    8 10 pi/2;
    10 12 pi/4;
    12 17 pi/2;
    11 10 -pi];
append(pathobj, waypoints);
Interpolate that path so that it contains exactly 250 points.
interpolate(pathobj, 250)
```

Visualize the interpolated path and the original waypoints.

```
figure;
grid on;
axis equal;
hold on;
plot(pathobj.States(:,1), pathobj.States(:,2), ".b");
plot(waypoints(:,1), waypoints(:,2), "*r", "MarkerSize", 10)
```



Calculate length of path.

```
len = pathLength(pathobj);
disp("Path length = " + num2str(len))
Path length = 19.37
```

Input Arguments

```
path — path object
navPath object
```

Path object, specified as a navPath object.

Data Types: object

states — states of path

real-valued M-by-N matrix

States of the path, specified as a real-valued M-by-N matrix. M is the number of states appended to the path, and N is the dimension of each state. The dimension of each state is governed by the state space defined in the StateSpace property of navPath. States outside of the StateBounds of the state space of path are pruned to the bounds.

Example: [0 0 0; 1 1 1]

Data Types: double

See Also

navPath

Introduced in R2019b

interpolate

Interpolate points along path

Syntax

interpolate(path,numStates)

Description

interpolate(path,numStates) inserts a number of states in the path and ensures the
distribution of all the points in the path to be uniform. The function preserves all the existing states in
the path. The value of numStates must be greater than or equal to the number of existing states in
the path.

Examples

Create navPath Based on Multiple Waypoints

Create a navPath object based on multiple waypoints in a Dubins space.

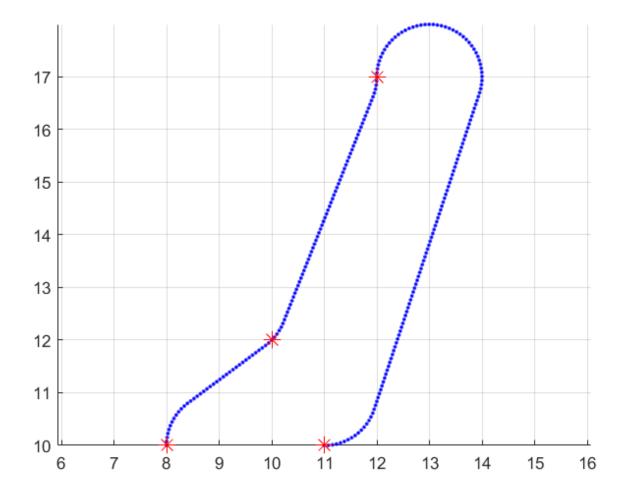
```
dubinsSpace = stateSpaceDubins([0 25; 0 25; -pi pi])
dubinsSpace =
  stateSpaceDubins with properties:
   SE2 Properties
                 Name: 'SE2 Dubins'
          StateBounds: [3×2 double]
    NumStateVariables: 3
   Dubins Vehicle Properties
     MinTurningRadius: 1
pathobj = navPath(dubinsSpace)
pathobj =
  navPath with properties:
    StateSpace: [1x1 stateSpaceDubins]
        States: [0×3 double]
     NumStates: 0
waypoints = [...
    8 10 pi/2;
    10 12 pi/4;
    12 17 pi/2;
    11 10 -pi];
append(pathobj, waypoints);
```

Interpolate that path so that it contains exactly 250 points.

```
interpolate(pathobj, 250)
```

Visualize the interpolated path and the original waypoints.

```
figure;
grid on;
axis equal;
hold on;
plot(pathobj.States(:,1), pathobj.States(:,2), ".b");
plot(waypoints(:,1), waypoints(:,2), "*r", "MarkerSize", 10)
```



Calculate length of path.

```
len = pathLength(pathobj);
disp("Path length = " + num2str(len))
Path length = 19.37
```

Input Arguments

path — Path object

navpath object

Path object, specified as a navPath object.

Data Types: object

numStates — Number of states

nonnegative integer

Number of states inserted in the path, specified as a nonnegative integer. Its value must be greater than or equal to the number of existing states in the path.

Data Types: double

See Also

navPath

Introduced in R2019b

pathLength

Length of path

Syntax

```
len = pathLength(path)
```

Description

len = pathLength(path) returns the total length of path by summing the distances between every sequential pair of states in the path. The function uses the state space object associated with path to calculate the distance between each state pair.

Examples

Create navPath Based on Multiple Waypoints

Create a navPath object based on multiple waypoints in a Dubins space.

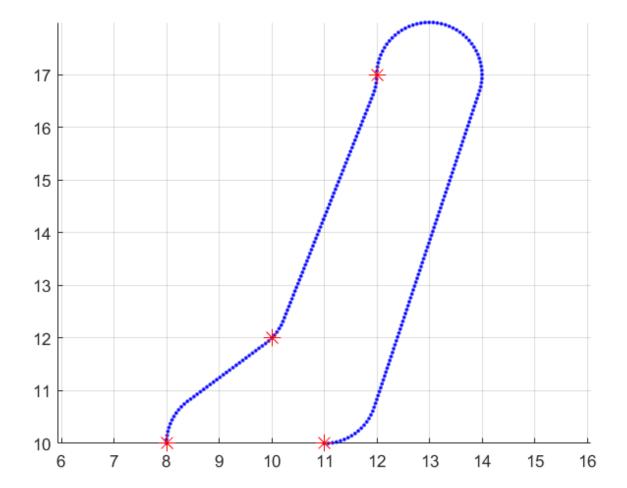
```
dubinsSpace = stateSpaceDubins([0 25; 0 25; -pi pi])
dubinsSpace =
 stateSpaceDubins with properties:
   SE2 Properties
                 Name: 'SE2 Dubins'
          StateBounds: [3×2 double]
   NumStateVariables: 3
   Dubins Vehicle Properties
     MinTurningRadius: 1
pathobj = navPath(dubinsSpace)
pathobj =
 navPath with properties:
    StateSpace: [1x1 stateSpaceDubins]
        States: [0×3 double]
    NumStates: 0
waypoints = [...
    8 10 pi/2;
    10 12 pi/4;
    12 17 pi/2;
    11 10 -pi];
append(pathobj, waypoints);
```

Interpolate that path so that it contains exactly 250 points.

interpolate(pathobj, 250)

Visualize the interpolated path and the original waypoints.

```
figure;
grid on;
axis equal;
hold on;
plot(pathobj.States(:,1), pathobj.States(:,2), ".b");
plot(waypoints(:,1), waypoints(:,2), "*r", "MarkerSize", 10)
```



Calculate length of path.

```
len = pathLength(pathobj);
disp("Path length = " + num2str(len))
Path length = 19.37
```

Input Arguments

path — Path object

navpath object

Path object, specified as a navPath object.

Data Types: object

Output Arguments

len — Length of path

nonnegative scalar

Length of the path, returned as a nonnegative scalar.

See Also

navPath

Introduced in R2019b

nav.StateSpace class

Package: nav

Create state space for path planning

Description

nav.StateSpace is an interface for state spaces used for path planning. Derive from this class if you want to define your own state space. This representation allows for sampling, interpolation, and calculating distances between spaces in the state space.

To create a sample template for generating your own state space class, call createPlanningTemplate. For specific implementations of the state validator class for general application, see **State Spaces** in "Motion Planning".

The nav.StateSpace class is a handle class.

Class Attributes

Abstract true

For information on class attributes, see "Class Attributes".

Creation

Syntax

ss0bj = nav.StateSpace(Name, NumStateVariables, Bounds)

Description

ssObj = nav.StateSpace(Name, NumStateVariables, Bounds) creates a state space object
with a given name and state bounds. NumStateVariables specifies the number of state variables.
This constructor can only be called from a derived class. Create your own class definition using
createPlanningTemplate.

Properties

Public Properties

NumStateVariables — Number of variables in state space

positive numeric scalar

Number of variables in state space, specified as a positive numeric scalar. This property is the dimension of the state space.

Example: 3

Attributes:

SetAccess - immutable

StateBounds — Min and max bounds of state variables

[min max] | *n*-by-2 matrix

Min and max bounds of state variables, specified as a [min max] n-by-2 matrix. This property depends on NumStateVariables, where n is the number of state variables. When specifying on construction, use the Bounds input.

Example: [-10 10; -10 10; -pi pi]

Attributes:

GetAccess public
SetAccess protected
Dependent true

Data Types: double

Protected Properties

Name — Name of state space object

string scalar | character vector

Name of the state space object, specified as a string scalar or character vector.

Example: "customSE2StateSpace"

Attributes:

GetAccess protected SetAccess protected

Methods

Public Methods

copyCopy array of handle objectsdistanceDistance between two statesenforceStateBoundsLimit state to state boundsinterpolateInterpolate between states

sampleGaussian Sample state using Gaussian distribution Sample using uniform distribution

Examples

Create Custom State Space for Path Planning

This example shows how to use the createPlanningTemplate function to generate a template for customizing your own state space definition and sampler to use with path planning algorithms. A simple implementation is provided with the template.

Call the create template function. This function generates a class definition file for you to modify for your own implementation.

createPlanningTemplate

Class and Property Definition

The first part of the template specifies the class definition and any properties for the class. Derive from the nav.StateSpace class. For this example, create a property for the uniform and normal distributions. You can specify any additional user-defined properties here.

```
classdef MyCustomStateSpace < nav.StateSpace & ...
    matlabshared.planning.internal.EnforceScalarHandle
    properties
        UniformDistribution
        NormalDistribution
        % Specify additional properties here
end</pre>
```

Save your custom state space class and ensure your file name matches the class name.

Class Constructor

Use the constructor to set the name of the state space, the number of state variables, and define its boundaries. Alternatively, you can add input arguments to the function and pass the variables in when you create an object.

- For each state variable, define the [min max] values for the state bounds.
- Call the constructor of the base class.
- For this example, you specify the normal and uniform distribution property values using predefined NormalDistribution and UniformDistribution classes.
- Specify any other user-defined property values here.

```
methods
```

Copy Semantics

Specify the copy method definition. Copy all the values of your user-defined variables into a new object, so copy0bj is a deep copy. The default behavior given in this example creates a new copy of the object with the same name, state bounds, and distributions.

```
function copyObj = copy(obj)
   copyObj = feval(class(obj));
   copyObj.StateBounds = obj.StateBounds;
   copyObj.UniformDistribution = obj.UniformDistribution.copy;
   copyObj.NormalDistribution = obj.NormalDistribution.copy;
end
```

Enforce State Bounds

Specify how to ensure states are always within the state bounds. For this example, the state values get saturated at the minimum or maximum values for the state bounds.

```
function boundedState = enforceStateBounds(obj, state)
    nav.internal.validation.validateStateMatrix(state, nan, obj.NumStateVariables, "enfo
    boundedState = state;
    boundedState = min(max(boundedState, obj.StateBounds(:,1)'), ...
        obj.StateBounds(:,2)');
end
```

Sample Uniformly

Specify the behavior for sampling across a uniform distribution. support multiple syntaxes to constrain the uniform distribution to a nearby state within a certain distance and sample multiple states.

```
STATE = sampleUniform(OBJ)
STATE = sampleUniform(OBJ, NUMSAMPLES)
STATE = sampleUniform(OBJ, NEARSTATE, DIST)
STATE = sampleUniform(OBJ, NEARSTATE, DIST, NUMSAMPLES)
```

For this example, use a validation function to process a varargin input that handles the varying input arguments.

```
function state = sampleUniform(obj, varargin)
  narginchk(1,4);
  [numSamples, stateBounds] = obj.validateSampleUniformInput(varargin{:});
  obj.UniformDistribution.RandomVariableLimits = stateBounds;
  state = obj.UniformDistribution.sample(numSamples);
end
```

Sample from Gaussian Distribution

end

Specify the behavior for sampling across a Gaussian distribution. Support multiple syntaxes for sampling a single state or multiple states.

Interpolate Between States

Define how to interpolate between two states in your state space. Use an input, fraction, to determine how to sample along the path between two states. For this example, define a basic linear interpolation method using the difference between states.

```
function interpState = interpolate(obj, state1, state2, fraction)
    narginchk(4,4);
    [state1, state2, fraction] = obj.validateInterpolateInput(state1, state2, fraction);
    stateDiff = state2 - state1;
    interpState = state1 + fraction' * stateDiff;
end
```

Calculate Distance Between States

Specify how to calculate the distance between two states in your state space. Use the state1 and state2 inputs to define the start and end positions. Both inputs can be a single state (row vector) or multiple states (matrix of row vectors). For this example, calculate the distance based on the Euclidean distance between each pair of state positions.

Terminate the methods and class sections.

```
end
end
```

Save your state space class definition. You can now use the class constructor to create an object for your state space.

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

nav.StateValidator|stateSpaceDubins|stateSpaceReedsShepp|stateSpaceSE2

Introduced in R2019b

distance

Class: nav.StateSpace

Package: nav

Distance between two states

Syntax

dist = distance(ss0bj,state1,state2)

Description

dist = distance(ss0bj,state1,state2) calculates the distance between two states.

Input Arguments

ss0bj - State space object

object of a subclass of nav.StateSpace

State space object, specified as an object of a subclass of nav.StateSpace.

state1 — Initial state position

n-element vector | *m*-by-*n* matrix of row vectors

Initial state position, specified as a n-element vector or m-by-n matrix of row vectors. n is the dimension of the state space specified in the NumStateVariables property of ss0bj.

state2 — Final state position

n-element vector | *m*-by-*n* matrix of row vectors

Final state position, specified as a n-element vector or m-by-n matrix of row vectors. n is the dimension of the state space specified in the NumStateVariables property of ss0bj. If specified as a matrix, state1 and state2 should have the same dimensions.

Output Arguments

dist — Distance between two states

numeric scalar | *m*-element vector

Distance between two states, returned as a numeric scalar or m-element vector. This distance calculation is the main component of evaluating costs of paths.

Examples

Create Custom State Space for Path Planning

This example shows how to use the createPlanningTemplate function to generate a template for customizing your own state space definition and sampler to use with path planning algorithms. A simple implementation is provided with the template.

Call the create template function. This function generates a class definition file for you to modify for your own implementation.

createPlanningTemplate

Class and Property Definition

The first part of the template specifies the class definition and any properties for the class. Derive from the nav.StateSpace class. For this example, create a property for the uniform and normal distributions. You can specify any additional user-defined properties here.

```
classdef MyCustomStateSpace < nav.StateSpace & ...
    matlabshared.planning.internal.EnforceScalarHandle
    properties
        UniformDistribution
        NormalDistribution
        % Specify additional properties here
end</pre>
```

Save your custom state space class and ensure your file name matches the class name.

Class Constructor

Use the constructor to set the name of the state space, the number of state variables, and define its boundaries. Alternatively, you can add input arguments to the function and pass the variables in when you create an object.

- For each state variable, define the [min max] values for the state bounds.
- Call the constructor of the base class.
- For this example, you specify the normal and uniform distribution property values using predefined NormalDistribution and UniformDistribution classes.
- Specify any other user-defined property values here.

```
methods
```

Copy Semantics

Specify the copy method definition. Copy all the values of your user-defined variables into a new object, so copyObj is a deep copy. The default behavior given in this example creates a new copy of the object with the same name, state bounds, and distributions.

```
function copyObj = copy(obj)
   copyObj = feval(class(obj));
   copyObj.StateBounds = obj.StateBounds;
   copyObj.UniformDistribution = obj.UniformDistribution.copy;
   copyObj.NormalDistribution = obj.NormalDistribution.copy;
end
```

Enforce State Bounds

Specify how to ensure states are always within the state bounds. For this example, the state values get saturated at the minimum or maximum values for the state bounds.

```
function boundedState = enforceStateBounds(obj, state)
    nav.internal.validation.validateStateMatrix(state, nan, obj.NumStateVariables, "enfo
    boundedState = state;
    boundedState = min(max(boundedState, obj.StateBounds(:,1)'), ...
        obj.StateBounds(:,2)');
end
```

Sample Uniformly

Specify the behavior for sampling across a uniform distribution. support multiple syntaxes to constrain the uniform distribution to a nearby state within a certain distance and sample multiple states.

```
STATE = sampleUniform(OBJ)
STATE = sampleUniform(OBJ, NUMSAMPLES)
STATE = sampleUniform(OBJ, NEARSTATE, DIST)
STATE = sampleUniform(OBJ, NEARSTATE, DIST, NUMSAMPLES)
```

For this example, use a validation function to process a varargin input that handles the varying input arguments.

```
function state = sampleUniform(obj, varargin)
  narginchk(1,4);
  [numSamples, stateBounds] = obj.validateSampleUniformInput(varargin{:});
  obj.UniformDistribution.RandomVariableLimits = stateBounds;
  state = obj.UniformDistribution.sample(numSamples);
end
```

Sample from Gaussian Distribution

Specify the behavior for sampling across a Gaussian distribution. Support multiple syntaxes for sampling a single state or multiple states.

```
[meanState, stdDev, numSamples] = obj.validateSampleGaussianInput(meanState, stdDev,
obj.NormalDistribution.Mean = meanState;
obj.NormalDistribution.Covariance = diag(stdDev.^2);
state = obj.NormalDistribution.sample(numSamples);
state = obj.enforceStateBounds(state);
```

Interpolate Between States

end

Define how to interpolate between two states in your state space. Use an input, fraction, to determine how to sample along the path between two states. For this example, define a basic linear interpolation method using the difference between states.

```
function interpState = interpolate(obj, state1, state2, fraction)
    narginchk(4,4);
    [state1, state2, fraction] = obj.validateInterpolateInput(state1, state2, fraction);
    stateDiff = state2 - state1;
    interpState = state1 + fraction' * stateDiff;
end
```

Calculate Distance Between States

Specify how to calculate the distance between two states in your state space. Use the state1 and state2 inputs to define the start and end positions. Both inputs can be a single state (row vector) or multiple states (matrix of row vectors). For this example, calculate the distance based on the Euclidean distance between each pair of state positions.

Terminate the methods and class sections.

```
end
end
```

Save your state space class definition. You can now use the class constructor to create an object for your state space.

See Also

nav.StateSpace|nav.StateValidator|stateSpaceDubins|stateSpaceReedsShepp| stateSpaceSE2

enforceStateBounds

Class: nav.StateSpace

Package: nav

Limit state to state bounds

Syntax

boundedState = enforceStateBounds(ss0bj,state)

Description

boundedState = enforceStateBounds(ss0bj,state) returns a bounded state that lies inside the state bounds based on the given state. Use this method to define specific bounding behavior like wrapping angular states. The bounds are specified in the StateBounds property of ss0bj.

Input Arguments

ss0bj - State space object

object of a subclass of nav.StateSpace

State space object, specified as an object of a subclass of nav.StateSpace.

state - State position

n-element vector | *m*-by-*n* matrix of row vectors

State position, specified as a n-element vector or an m-by-n matrix of row vectors. n is the dimension of the state space specified in the NumStateVariables property of ss0bj.

Output Arguments

boundedState - State position with enforced state bounds

n-element vector | *m*-by-*n* matrix of row vectors

State position with enforced state bounds, specified as a n-element vector or m-by-n matrix of row vectors. n is the dimension of the state space specified in the NumStateVariables property of ssObj.

Examples

Create Custom State Space for Path Planning

This example shows how to use the createPlanningTemplate function to generate a template for customizing your own state space definition and sampler to use with path planning algorithms. A simple implementation is provided with the template.

Call the create template function. This function generates a class definition file for you to modify for your own implementation.

createPlanningTemplate

Class and Property Definition

The first part of the template specifies the class definition and any properties for the class. Derive from the nav.StateSpace class. For this example, create a property for the uniform and normal distributions. You can specify any additional user-defined properties here.

```
classdef MyCustomStateSpace < nav.StateSpace & ...
    matlabshared.planning.internal.EnforceScalarHandle
    properties
        UniformDistribution
        NormalDistribution
        % Specify additional properties here
end</pre>
```

Save your custom state space class and ensure your file name matches the class name.

Class Constructor

Use the constructor to set the name of the state space, the number of state variables, and define its boundaries. Alternatively, you can add input arguments to the function and pass the variables in when you create an object.

- For each state variable, define the [min max] values for the state bounds.
- Call the constructor of the base class.
- For this example, you specify the normal and uniform distribution property values using predefined NormalDistribution and UniformDistribution classes.
- Specify any other user-defined property values here.

```
methods
```

Copy Semantics

Specify the copy method definition. Copy all the values of your user-defined variables into a new object, so copyObj is a deep copy. The default behavior given in this example creates a new copy of the object with the same name, state bounds, and distributions.

```
function copyObj = copy(obj)
    copyObj = feval(class(obj));
    copyObj.StateBounds = obj.StateBounds;
    copyObj.UniformDistribution = obj.UniformDistribution.copy;
    copyObj.NormalDistribution = obj.NormalDistribution.copy;
end
```

Enforce State Bounds

Specify how to ensure states are always within the state bounds. For this example, the state values get saturated at the minimum or maximum values for the state bounds.

```
function boundedState = enforceStateBounds(obj, state)
    nav.internal.validation.validateStateMatrix(state, nan, obj.NumStateVariables, "enfo
    boundedState = state;
    boundedState = min(max(boundedState, obj.StateBounds(:,1)'), ...
        obj.StateBounds(:,2)');
end
```

Sample Uniformly

Specify the behavior for sampling across a uniform distribution. support multiple syntaxes to constrain the uniform distribution to a nearby state within a certain distance and sample multiple states.

```
STATE = sampleUniform(OBJ)
STATE = sampleUniform(OBJ, NUMSAMPLES)
STATE = sampleUniform(OBJ, NEARSTATE, DIST)
STATE = sampleUniform(OBJ, NEARSTATE, DIST, NUMSAMPLES)
```

For this example, use a validation function to process a varargin input that handles the varying input arguments.

```
function state = sampleUniform(obj, varargin)
  narginchk(1,4);
  [numSamples, stateBounds] = obj.validateSampleUniformInput(varargin{:});
  obj.UniformDistribution.RandomVariableLimits = stateBounds;
  state = obj.UniformDistribution.sample(numSamples);
end
```

Sample from Gaussian Distribution

end

Specify the behavior for sampling across a Gaussian distribution. Support multiple syntaxes for sampling a single state or multiple states.

Interpolate Between States

Define how to interpolate between two states in your state space. Use an input, fraction, to determine how to sample along the path between two states. For this example, define a basic linear interpolation method using the difference between states.

```
function interpState = interpolate(obj, state1, state2, fraction)
    narginchk(4,4);
    [state1, state2, fraction] = obj.validateInterpolateInput(state1, state2, fraction);
    stateDiff = state2 - state1;
    interpState = state1 + fraction' * stateDiff;
end
```

Calculate Distance Between States

Specify how to calculate the distance between two states in your state space. Use the state1 and state2 inputs to define the start and end positions. Both inputs can be a single state (row vector) or multiple states (matrix of row vectors). For this example, calculate the distance based on the Euclidean distance between each pair of state positions.

```
function dist = distance(obj, state1, state2)
    narginchk(3,3);
    nav.internal.validation.validateStateMatrix(state1, nan, obj.NumStateVariables, "distant nav.internal.validation.validateStateMatrix(state2, size(state1,1), obj.NumStateVariables)
    stateDiff = bsxfun(@minus, state2, state1);
    dist = sqrt( sum( stateDiff.^2, 2 ) );
end
```

Terminate the methods and class sections.

```
end
end
```

Save your state space class definition. You can now use the class constructor to create an object for your state space.

See Also

nav.StateSpace|nav.StateValidator|stateSpaceDubins|stateSpaceReedsShepp| stateSpaceSE2

interpolate

Class: nav.StateSpace

Package: nav

Interpolate between states

Syntax

interpStates = interpolate(ss0bj,state1,state2,ratios)

Description

interpStates = interpolate(ss0bj,state1,state2,ratios) interpolates between two
states in your state space based on the given ratios.

Input Arguments

ss0bj — State space object

object of a subclass of nav.StateSpace

State space object, specified as an object of a subclass of nav.StateSpace.

state1 — Initial state position

n-element vector

Initial state position, specified as a n-element vector. n is the dimension of the state space specified in the NumStateVariables property of ss0bj.

state2 — Final state position

n-element vector | *m*-by-*n* matrix of row vectors

Final state position, specified as a n-element vector. n is the dimension of the state space specified in the NumStateVariables property of ss0bj.

ratios — Ratio values for interpolating along path

m-element vector

Ratio values for interpolating along path, specified as an *m*-element vector. These ratios determine how to sample between the two states.

Output Arguments

interpStates — Interpolated states

m-by-*n* matrix of row vectors

Interpolated states, returned as an m-by-n matrix of row vectors. m is the length of ratios and n is the dimension of the state space specified in the NumStateVariables property of ss0bj.

Examples

Create Custom State Space for Path Planning

This example shows how to use the createPlanningTemplate function to generate a template for customizing your own state space definition and sampler to use with path planning algorithms. A simple implementation is provided with the template.

Call the create template function. This function generates a class definition file for you to modify for your own implementation.

createPlanningTemplate

Class and Property Definition

The first part of the template specifies the class definition and any properties for the class. Derive from the nav.StateSpace class. For this example, create a property for the uniform and normal distributions. You can specify any additional user-defined properties here.

Save your custom state space class and ensure your file name matches the class name.

Class Constructor

Use the constructor to set the name of the state space, the number of state variables, and define its boundaries. Alternatively, you can add input arguments to the function and pass the variables in when you create an object.

- For each state variable, define the [min max] values for the state bounds.
- Call the constructor of the base class.
- For this example, you specify the normal and uniform distribution property values using predefined NormalDistribution and UniformDistribution classes.
- Specify any other user-defined property values here.

```
methods
```

Copy Semantics

Specify the copy method definition. Copy all the values of your user-defined variables into a new object, so copyObj is a deep copy. The default behavior given in this example creates a new copy of the object with the same name, state bounds, and distributions.

```
function copyObj = copy(obj)
   copyObj = feval(class(obj));
   copyObj.StateBounds = obj.StateBounds;
   copyObj.UniformDistribution = obj.UniformDistribution.copy;
   copyObj.NormalDistribution = obj.NormalDistribution.copy;
end
```

Enforce State Bounds

Specify how to ensure states are always within the state bounds. For this example, the state values get saturated at the minimum or maximum values for the state bounds.

```
function boundedState = enforceStateBounds(obj, state)
    nav.internal.validation.validateStateMatrix(state, nan, obj.NumStateVariables, "enfo
    boundedState = state;
    boundedState = min(max(boundedState, obj.StateBounds(:,1)'), ...
        obj.StateBounds(:,2)');
end
```

Sample Uniformly

Specify the behavior for sampling across a uniform distribution. support multiple syntaxes to constrain the uniform distribution to a nearby state within a certain distance and sample multiple states.

```
STATE = sampleUniform(OBJ)
STATE = sampleUniform(OBJ, NUMSAMPLES)
STATE = sampleUniform(OBJ, NEARSTATE, DIST)
STATE = sampleUniform(OBJ, NEARSTATE, DIST, NUMSAMPLES)
```

For this example, use a validation function to process a varargin input that handles the varying input arguments.

```
function state = sampleUniform(obj, varargin)
  narginchk(1,4);
  [numSamples, stateBounds] = obj.validateSampleUniformInput(varargin{:});
  obj.UniformDistribution.RandomVariableLimits = stateBounds;
  state = obj.UniformDistribution.sample(numSamples);
end
```

Sample from Gaussian Distribution

Specify the behavior for sampling across a Gaussian distribution. Support multiple syntaxes for sampling a single state or multiple states.

```
[meanState, stdDev, numSamples] = obj.validateSampleGaussianInput(meanState, stdDev,
   obj.NormalDistribution.Mean = meanState;
   obj.NormalDistribution.Covariance = diag(stdDev.^2);
   state = obj.NormalDistribution.sample(numSamples);
   state = obj.enforceStateBounds(state);
end
```

Interpolate Between States

Define how to interpolate between two states in your state space. Use an input, fraction, to determine how to sample along the path between two states. For this example, define a basic linear interpolation method using the difference between states.

```
function interpState = interpolate(obj, state1, state2, fraction)
    narginchk(4,4);
    [state1, state2, fraction] = obj.validateInterpolateInput(state1, state2, fraction);
    stateDiff = state2 - state1;
    interpState = state1 + fraction' * stateDiff;
end
```

Calculate Distance Between States

Specify how to calculate the distance between two states in your state space. Use the state1 and state2 inputs to define the start and end positions. Both inputs can be a single state (row vector) or multiple states (matrix of row vectors). For this example, calculate the distance based on the Euclidean distance between each pair of state positions.

Terminate the methods and class sections.

```
end
end
```

Save your state space class definition. You can now use the class constructor to create an object for your state space.

See Also

nav.StateSpace | nav.StateValidator | stateSpaceDubins | stateSpaceReedsShepp |
stateSpaceSE2

sampleGaussian

Class: nav.StateSpace

Package: nav

Sample state using Gaussian distribution

Syntax

```
states = sampleGaussian(ss0bj,meanState,stdDev)
states = sampleGaussian(ss0bj,meanState,stdDev,numSamples)
```

Description

states = sampleGaussian(ssObj, meanState, stdDev) samples a single state in your state
space from a Gaussian distribution centered on meanState with specified standard deviation.

states = sampleGaussian(ss0bj,meanState,stdDev,numSamples) samples multiple states
based on numSamples.

Input Arguments

ss0bj — State space object

object of a subclass of nav.StateSpace

State space object, specified as an object of a subclass of nav. StateSpace.

meanState — Mean state position

n-element vector

Mean state position, specified as a n-element vector, where n is the dimension of the state space specified in the NumStateVariables property of ss0bj. m is the number of samples specified in numSamples.

stdDev — Standard deviation around mean state

n-element vector

Standard deviation around mean state, specified as an *n*-element vector, where each element corresponds to an element in meanState.

numSamples — Number of samples

positive integer

Number of samples, specified as a positive integer. By default, the function assumes numSamples is 1.

Output Arguments

states — Sampled states from state space

n-element vector | *m*-by-*n* matrix of row vectors

Sampled states from state space, specified as a n-element vector or m-by-n matrix of row vectors. n is the dimension of the state space specified in the NumStateVariables property of ss0bj. m is the number of samples specified in numSamples. All states are sampled within the StateBounds property of ss0bj.

Examples

Create Custom State Space for Path Planning

This example shows how to use the createPlanningTemplate function to generate a template for customizing your own state space definition and sampler to use with path planning algorithms. A simple implementation is provided with the template.

Call the create template function. This function generates a class definition file for you to modify for your own implementation.

createPlanningTemplate

Class and Property Definition

The first part of the template specifies the class definition and any properties for the class. Derive from the nav.StateSpace class. For this example, create a property for the uniform and normal distributions. You can specify any additional user-defined properties here.

```
classdef MyCustomStateSpace < nav.StateSpace & ...
    matlabshared.planning.internal.EnforceScalarHandle
    properties
        UniformDistribution
        NormalDistribution
        % Specify additional properties here
end</pre>
```

Save your custom state space class and ensure your file name matches the class name.

Class Constructor

Use the constructor to set the name of the state space, the number of state variables, and define its boundaries. Alternatively, you can add input arguments to the function and pass the variables in when you create an object.

- For each state variable, define the [min max] values for the state bounds.
- Call the constructor of the base class.
- For this example, you specify the normal and uniform distribution property values using predefined NormalDistribution and UniformDistribution classes.
- Specify any other user-defined property values here.

methods

```
obj@nav.StateSpace(spaceName, numStateVariables, stateBounds);

obj.NormalDistribution = matlabshared.tracking.internal.NormalDistribution(numStateVariable)
obj.UniformDistribution = matlabshared.tracking.internal.UniformDistribution(numStateVariable)
% User-defined property values here
end
```

Copy Semantics

Specify the copy method definition. Copy all the values of your user-defined variables into a new object, so copyObj is a deep copy. The default behavior given in this example creates a new copy of the object with the same name, state bounds, and distributions.

```
function copyObj = copy(obj)
  copyObj = feval(class(obj));
  copyObj.StateBounds = obj.StateBounds;
  copyObj.UniformDistribution = obj.UniformDistribution.copy;
  copyObj.NormalDistribution = obj.NormalDistribution.copy;
end
```

Enforce State Bounds

Specify how to ensure states are always within the state bounds. For this example, the state values get saturated at the minimum or maximum values for the state bounds.

```
function boundedState = enforceStateBounds(obj, state)
    nav.internal.validation.validateStateMatrix(state, nan, obj.NumStateVariables, "enfo
    boundedState = state;
    boundedState = min(max(boundedState, obj.StateBounds(:,1)'), ...
        obj.StateBounds(:,2)');
end
```

Sample Uniformly

Specify the behavior for sampling across a uniform distribution. support multiple syntaxes to constrain the uniform distribution to a nearby state within a certain distance and sample multiple states.

```
STATE = sampleUniform(OBJ)
STATE = sampleUniform(OBJ, NUMSAMPLES)
STATE = sampleUniform(OBJ, NEARSTATE, DIST)
STATE = sampleUniform(OBJ, NEARSTATE, DIST, NUMSAMPLES)
```

For this example, use a validation function to process a varargin input that handles the varying input arguments.

```
function state = sampleUniform(obj, varargin)
  narginchk(1,4);
  [numSamples, stateBounds] = obj.validateSampleUniformInput(varargin{:});
  obj.UniformDistribution.RandomVariableLimits = stateBounds;
  state = obj.UniformDistribution.sample(numSamples);
end
```

Sample from Gaussian Distribution

Specify the behavior for sampling across a Gaussian distribution. Support multiple syntaxes for sampling a single state or multiple states.

Interpolate Between States

Define how to interpolate between two states in your state space. Use an input, fraction, to determine how to sample along the path between two states. For this example, define a basic linear interpolation method using the difference between states.

```
function interpState = interpolate(obj, state1, state2, fraction)
    narginchk(4,4);
    [state1, state2, fraction] = obj.validateInterpolateInput(state1, state2, fraction);
    stateDiff = state2 - state1;
    interpState = state1 + fraction' * stateDiff;
end
```

Calculate Distance Between States

Specify how to calculate the distance between two states in your state space. Use the state1 and state2 inputs to define the start and end positions. Both inputs can be a single state (row vector) or multiple states (matrix of row vectors). For this example, calculate the distance based on the Euclidean distance between each pair of state positions.

Terminate the methods and class sections.

```
end
end
```

Save your state space class definition. You can now use the class constructor to create an object for your state space.

See Also

nav.StateSpace|nav.StateValidator|stateSpaceDubins|stateSpaceReedsShepp| stateSpaceSE2

sampleUniform

Class: nav.StateSpace

Package: nav

Sample state using uniform distribution

Syntax

```
states = sampleUniform(ss0bj)
states = sampleUniform(ss0bj,numSamples)
states = sampleUniform(ss0bj,nearState,distance)
states = sampleUniform(ss0bj,nearState,distance,numSamples)
```

Description

states = sampleUniform(ssObj) samples throughout your entire state space using a uniform
distribution.

states = sampleUniform(ss0bj,numSamples) samples multiple states based on numSamples.

states = sampleUniform(ssObj,nearState,distance) samples near a given state within a
certain distance.

states = sampleUniform(ssObj,nearState,distance,numSamples) samples multiple states
near a given state based on numSamples.

Input Arguments

ss0bj — State space object

object of a subclass of nav.StateSpace

State space object, specified as an object of a subclass of nav.StateSpace.

nearState - Mean state position

n-element vector

Mean state position, specified as a n-element vector, where n is the dimension of the state space specified in the NumStateVariables property of ss0bj. m is the number of samples specified in numSamples.

distance — Max distance from mean state position

n-element vector

Max distance from mean state position, nearState, specified as a *n*-element vector, where nearState defines the center of the sampled region and distance is the maximum distance from nearState allowed in each dimension.

numSamples — Number of samples

positive integer

Number of samples, specified as a positive integer.

Output Arguments

states — Sampled states from state space

n-element vector | *m*-by-*n* matrix of row vectors

Sampled states from state space, specified as a n-element vector or m-by-n matrix of row vectors. n is the dimension of the state space specified in the NumStateVariables property of ss0bj. m is the number of samples specified in numSamples. All states are sampled within the StateBounds property of ss0bj.

Examples

Create Custom State Space for Path Planning

This example shows how to use the createPlanningTemplate function to generate a template for customizing your own state space definition and sampler to use with path planning algorithms. A simple implementation is provided with the template.

Call the create template function. This function generates a class definition file for you to modify for your own implementation.

createPlanningTemplate

Class and Property Definition

The first part of the template specifies the class definition and any properties for the class. Derive from the nav.StateSpace class. For this example, create a property for the uniform and normal distributions. You can specify any additional user-defined properties here.

```
classdef MyCustomStateSpace < nav.StateSpace & ...
    matlabshared.planning.internal.EnforceScalarHandle
    properties
        UniformDistribution
        NormalDistribution
        % Specify additional properties here
end</pre>
```

Save your custom state space class and ensure your file name matches the class name.

Class Constructor

Use the constructor to set the name of the state space, the number of state variables, and define its boundaries. Alternatively, you can add input arguments to the function and pass the variables in when you create an object.

- For each state variable, define the [min max] values for the state bounds.
- Call the constructor of the base class.
- For this example, you specify the normal and uniform distribution property values using predefined NormalDistribution and UniformDistribution classes.
- Specify any other user-defined property values here.

```
methods
    function obj = MyCustomStateSpace
```

Copy Semantics

Specify the copy method definition. Copy all the values of your user-defined variables into a new object, so copyObj is a deep copy. The default behavior given in this example creates a new copy of the object with the same name, state bounds, and distributions.

```
function copyObj = copy(obj)
   copyObj = feval(class(obj));
   copyObj.StateBounds = obj.StateBounds;
   copyObj.UniformDistribution = obj.UniformDistribution.copy;
   copyObj.NormalDistribution = obj.NormalDistribution.copy;
end
```

Enforce State Bounds

Specify how to ensure states are always within the state bounds. For this example, the state values get saturated at the minimum or maximum values for the state bounds.

```
function boundedState = enforceStateBounds(obj, state)
   nav.internal.validation.validateStateMatrix(state, nan, obj.NumStateVariables, "enfo
   boundedState = state;
   boundedState = min(max(boundedState, obj.StateBounds(:,1)'), ...
        obj.StateBounds(:,2)');
end
```

Sample Uniformly

Specify the behavior for sampling across a uniform distribution. support multiple syntaxes to constrain the uniform distribution to a nearby state within a certain distance and sample multiple states.

```
STATE = sampleUniform(OBJ)
STATE = sampleUniform(OBJ, NUMSAMPLES)
STATE = sampleUniform(OBJ, NEARSTATE, DIST)
STATE = sampleUniform(OBJ, NEARSTATE, DIST, NUMSAMPLES)
```

For this example, use a validation function to process a varargin input that handles the varying input arguments.

```
function state = sampleUniform(obj, varargin)
  narginchk(1,4);
  [numSamples, stateBounds] = obj.validateSampleUniformInput(varargin{:});
  obj.UniformDistribution.RandomVariableLimits = stateBounds;
```

```
state = obj.UniformDistribution.sample(numSamples);
end
```

Sample from Gaussian Distribution

Specify the behavior for sampling across a Gaussian distribution. Support multiple syntaxes for sampling a single state or multiple states.

Interpolate Between States

Define how to interpolate between two states in your state space. Use an input, fraction, to determine how to sample along the path between two states. For this example, define a basic linear interpolation method using the difference between states.

```
function interpState = interpolate(obj, state1, state2, fraction)
    narginchk(4,4);
    [state1, state2, fraction] = obj.validateInterpolateInput(state1, state2, fraction);
    stateDiff = state2 - state1;
    interpState = state1 + fraction' * stateDiff;
end
```

Calculate Distance Between States

Specify how to calculate the distance between two states in your state space. Use the state1 and state2 inputs to define the start and end positions. Both inputs can be a single state (row vector) or multiple states (matrix of row vectors). For this example, calculate the distance based on the Euclidean distance between each pair of state positions.

Terminate the methods and class sections.

end end

Save your state space class definition. You can now use the class constructor to create an object for your state space.

See Also

 $\verb|nav.StateSpace| | \verb|nav.StateValidator|| stateSpaceDubins| stateSpaceReedsShepp| stateSpaceSE2$

nav.StateValidator class

Package: nav

Create state validator for path planning

Description

nav.StateValidator is an interface for all state validators used for path planning. Derive from this class if you want to define your own state validator. This representation allows for state and motion validation.

To create a sample template for generating your own state space class, call createPlanningTemplate("StateValidator"). For specific implementations of the state validator class for general application, see **State Validation** in "Motion Planning".

The nav.StateValidator class is a handle class.

Class Attributes

Abstract true

For information on class attributes, see "Class Attributes".

Creation

Syntax

ss0bj = nav.StateValidator(stateSpace)

Description

ss0bj = nav.StateValidator(stateSpace) creates a state validator object that validates
states in the given state space. This constructor can only be called from a derived class. Create your
own class definition using createPlanningTemplate.

Properties

StateSpace — State space definition

object of a subclass from nav.StateSpace

State space definition, specified as an object of a subclass from nav.StateSpace. Specify this property using the stateSpace input on construction. You can also specify any of our predefined objects in the **State Validation** section from "Motion Planning".

Example: stateSpaceSE2

Attributes:

GetAccess public SetAccess immutable

Methods

Public Methods

copy Copy array of handle objects

isMotionValid Check if path between states is valid

isStateValid Check if state is valid

Examples

Create Custom State Space Validator for Path Planning

This example shows how to use the createPlanningTemplate function to generate a template for customizing your own state validation class. State validation is used with path planning algorithms to ensure valid paths. The template function provides a basic implementation for example purposes.

Call the create template function. This function generates a class definition file for you to modify for your own implementation. Save this file.

```
createPlanningTemplate("StateValidator")
```

Class and Property Definition

The first part of the template specifies the class definition and any properties for the class. Derive from the nav.StateValidator class. You can specify any additional user-defined properties here.

```
classdef MyCustomStateValidator < nav.StateValidator & ...
    matlabshared.planning.internal.EnforceScalarHandle
    properties
    % User-defined properties
    end</pre>
```

Save your custom state validator class and ensure your file name matches the class name.

Class Constructor

Use the constructor to set the name of the state space validator and specify the state space object. Set a default value for the state space if one is not provided. Call the constructor of the base class. Initialize any other user-defined properties.

methods

```
function obj = MyCustomStateValidator(space)
    narginchk(0,1)

if nargin == 0
    space = stateSpaceSE2;
end

obj@nav.StateValidator(space);
```

```
\% Initialize user-defined properties \mbox{\it end}
```

Copy Semantics

Specify the copy method definition. Copy all the values of your user-defined variables into a new object, so copyObj is a deep copy. The default behavior given in this example creates a new copy of the object with the same type.

```
function copyObj = copy(obj)
    copyObj = feval(class(obj), obj.StateSpace);
end
```

Check State Validity

Define how a given state is validated. The state input can either be a single row vector, or a matrix of row vectors for multiple states. Customize this function for any special validation behavior for your state space like collision checking against obstacles.

```
function isValid = isStateValid(obj, state)
    narginchk(2,2);
    nav.internal.validation.validateStateMatrix(state, nan, obj.StateSpace.NumStateVarial
        "isStateValid", "state");

bounds = obj.StateSpace.StateBounds';
    inBounds = state >= bounds(1,:) & state <= bounds(2,:);
    isValid = all(inBounds, 2);</pre>
```

end

Check Motion Validity

isValid = true; lastValid = state2;

Define how to generate the motion between states and determine if it is valid. For this example, use linspace to evenly interpolate between states and check if these states are valid using isStateValid. Customize this function to sample between states or consider other analytical methods for determining if a vehicle can move between given states.

```
function [isValid, lastValid] = isMotionValid(obj, state1, state2)
    narginchk(3,3);
    state1 = nav.internal.validation.validateStateVector(state1, ...
        obj.StateSpace.NumStateVariables, "isMotionValid", "state1");
    state2 = nav.internal.validation.validateStateVector(state2, ...
        obj.StateSpace.NumStateVariables, "isMotionValid", "state2");
    if (~obj.isStateValid(state1))
        error("statevalidator:StartStateInvalid", "The start state of the motion is inva-
    end
    % Interpolate at a fixed interval between states and check state validity
    numInterpPoints = 100;
    interpStates = obj.StateSpace.interpolate(state1, state2, linspace(0,1,numInterpPoint)
    interpValid = obj.isStateValid(interpStates);
    % Look for invalid states. Set lastValid state to index-1.
    firstInvalidIdx = find(~interpValid, 1);
    if isempty(firstInvalidIdx)
```

```
else
    isValid = false;
    lastValid = interpStates(firstInvalidIdx-1,:);
end
end
```

Terminate the methods and class sections.

```
end
end
```

Save your state space validator class definition. You can now use the class constructor to create an object for validation of states for a given state space.

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder $^{\text{\tiny TM}}$.

See Also

nav.StateSpace|validatorOccupancyMap|validatorVehicleCostmap

isMotionValid

Class: nav.StateValidator

Package: nav

Check if path between states is valid

Syntax

[isValid,lastValid] = isMotionValid(validatorObj,state1,state2)

Description

[isValid,lastValid] = isMotionValid(validatorObj,state1,state2) determines if the motion between two states is valid by interpolating between states. The function also returns the last valid state along the path.

A default implementation for this method is provided when you call createPlanningTemplate.

Input Arguments

validatorObj — State validator object

object from a subclass of nav.StateValidator

State validator object, specified as an object from a subclass of nav.StateValidator. For provided state validator objects, see validatorOccupancyMap or validatorVehicleCostmap.

state1 — Initial state position

n-element vector | *m*-by-*n* matrix of row vectors

Initial state position, specified as a n-element vector or m-by-n matrix of row vectors. n is the dimension of the state space specified in the state space property in validator0bj.

state2 — Final state position

n-element vector | *m*-by-*n* matrix of row vectors

Final state position, specified as a n-element vector or m-by-n matrix of row vectors. n is the dimension of the state space specified in the state space property in validator0bj.

Output Arguments

isValid — Valid states

m-element vector of 1s and 0s

Valid states, specified as a m-element vector of 1s and 0s.

Data Types: logical

lastValid — Final valid state along path

n-element vector

Final valid state along path, specified as a *n*-element vector. *n* is the dimension of the state space specified in the state space property in validatorObj.

Examples

Create Custom State Space Validator for Path Planning

This example shows how to use the createPlanningTemplate function to generate a template for customizing your own state validation class. State validation is used with path planning algorithms to ensure valid paths. The template function provides a basic implementation for example purposes.

Call the create template function. This function generates a class definition file for you to modify for your own implementation. Save this file.

```
createPlanningTemplate("StateValidator")
```

Class and Property Definition

The first part of the template specifies the class definition and any properties for the class. Derive from the nav.StateValidator class. You can specify any additional user-defined properties here.

Save your custom state validator class and ensure your file name matches the class name.

Class Constructor

Use the constructor to set the name of the state space validator and specify the state space object. Set a default value for the state space if one is not provided. Call the constructor of the base class. Initialize any other user-defined properties.

```
methods
    function obj = MyCustomStateValidator(space)
        narginchk(0,1)

    if nargin == 0
        space = stateSpaceSE2;
    end

    obj@nav.StateValidator(space);

% Initialize user-defined properties
```

Copy Semantics

end

Specify the copy method definition. Copy all the values of your user-defined variables into a new object, so copyObj is a deep copy. The default behavior given in this example creates a new copy of the object with the same type.

```
function copyObj = copy(obj)
    copyObj = feval(class(obj), obj.StateSpace);
end
```

Check State Validity

Define how a given state is validated. The state input can either be a single row vector, or a matrix of row vectors for multiple states. Customize this function for any special validation behavior for your state space like collision checking against obstacles.

```
function isValid = isStateValid(obj, state)
    narginchk(2,2);
    nav.internal.validation.validateStateMatrix(state, nan, obj.StateSpace.NumStateVarial
        "isStateValid", "state");

bounds = obj.StateSpace.StateBounds';
    inBounds = state >= bounds(1,:) & state <= bounds(2,:);
    isValid = all(inBounds, 2);</pre>
```

Check Motion Validity

end

Define how to generate the motion between states and determine if it is valid. For this example, use linspace to evenly interpolate between states and check if these states are valid using isStateValid. Customize this function to sample between states or consider other analytical methods for determining if a vehicle can move between given states.

```
function [isValid, lastValid] = isMotionValid(obj, state1, state2)
    narginchk(3,3);
    state1 = nav.internal.validation.validateStateVector(state1, ...
        obj.StateSpace.NumStateVariables, "isMotionValid", "state1");
    state2 = nav.internal.validation.validateStateVector(state2, ...
        obj.StateSpace.NumStateVariables, "isMotionValid", "state2");
    if (~obj.isStateValid(state1))
        error("statevalidator:StartStateInvalid", "The start state of the motion is inva-
    % Interpolate at a fixed interval between states and check state validity
    numInterpPoints = 100;
    interpStates = obj.StateSpace.interpolate(state1, state2, linspace(0,1,numInterpPointerp)
    interpValid = obj.isStateValid(interpStates);
    % Look for invalid states. Set lastValid state to index-1.
    firstInvalidIdx = find(~interpValid, 1);
    if isempty(firstInvalidIdx)
        isValid = true;
        lastValid = state2;
    else
        isValid = false:
        lastValid = interpStates(firstInvalidIdx-1,:);
    end
```

Terminate the methods and class sections.

end

end end

Save your state space validator class definition. You can now use the class constructor to create an object for validation of states for a given state space.

See Also

nav.StateSpace|nav.StateValidator|validatorOccupancyMap|
validatorVehicleCostmap

isStateValid

Class: nav.StateValidator

Package: nav

Check if state is valid

Syntax

isValid = isStateValid(validatorObj,states)

Description

isValid = isStateValid(validatorObj, states) determines if the states are valid.

Input Arguments

validator0bj — State validator object

object from a subclass of nav.StateValidator

State validator object, specified as an object from a subclass of nav.StateValidator. For provided state validator objects, see validatorOccupancyMap or validatorVehicleCostmap.

states — State positions

n-element vector | *m*-by-*n* matrix of row vectors

Initial state position, specified as a n-element vector or m-by-n matrix of row vectors. n is the dimension of the state space specified in validator0bj. m is the number of states to validate.

Output Arguments

isValid — Valid states

m-element vector of 1s and 0s

Valid states, specified as a *m*-element vector of 1s and 0s.

Examples

Create Custom State Space Validator for Path Planning

This example shows how to use the createPlanningTemplate function to generate a template for customizing your own state validation class. State validation is used with path planning algorithms to ensure valid paths. The template function provides a basic implementation for example purposes.

Call the create template function. This function generates a class definition file for you to modify for your own implementation. Save this file.

createPlanningTemplate("StateValidator")

Class and Property Definition

The first part of the template specifies the class definition and any properties for the class. Derive from the nav.StateValidator class. You can specify any additional user-defined properties here.

Save your custom state validator class and ensure your file name matches the class name.

Class Constructor

Use the constructor to set the name of the state space validator and specify the state space object. Set a default value for the state space if one is not provided. Call the constructor of the base class. Initialize any other user-defined properties.

```
methods
```

```
function obj = MyCustomStateValidator(space)
    narginchk(0,1)

if nargin == 0
        space = stateSpaceSE2;
    end

    obj@nav.StateValidator(space);

% Initialize user-defined properties
end
```

Copy Semantics

Specify the copy method definition. Copy all the values of your user-defined variables into a new object, so copyObj is a deep copy. The default behavior given in this example creates a new copy of the object with the same type.

```
function copyObj = copy(obj)
  copyObj = feval(class(obj), obj.StateSpace);
end
```

Check State Validity

Define how a given state is validated. The state input can either be a single row vector, or a matrix of row vectors for multiple states. Customize this function for any special validation behavior for your state space like collision checking against obstacles.

```
function isValid = isStateValid(obj, state)
    narginchk(2,2);
    nav.internal.validation.validateStateMatrix(state, nan, obj.StateSpace.NumStateVarial
        "isStateValid", "state");

bounds = obj.StateSpace.StateBounds';
    inBounds = state >= bounds(1,:) & state <= bounds(2,:);
    isValid = all(inBounds, 2);</pre>
```

end

Check Motion Validity

Define how to generate the motion between states and determine if it is valid. For this example, use linspace to evenly interpolate between states and check if these states are valid using isStateValid. Customize this function to sample between states or consider other analytical methods for determining if a vehicle can move between given states.

```
function [isValid, lastValid] = isMotionValid(obj, state1, state2)
    narginchk(3,3);
    state1 = nav.internal.validation.validateStateVector(state1, ...
        obj.StateSpace.NumStateVariables, "isMotionValid", "state1");
    state2 = nav.internal.validation.validateStateVector(state2, ...
        obj.StateSpace.NumStateVariables, "isMotionValid", "state2");
    if (~obj.isStateValid(state1))
        error("statevalidator:StartStateInvalid", "The start state of the motion is inva-
    % Interpolate at a fixed interval between states and check state validity
    numInterpPoints = 100;
    interpStates = obj.StateSpace.interpolate(state1, state2, linspace(0,1,numInterpPoint)
    interpValid = obj.isStateValid(interpStates);
    % Look for invalid states. Set lastValid state to index-1.
    firstInvalidIdx = find(~interpValid, 1);
    if isempty(firstInvalidIdx)
        isValid = true;
        lastValid = state2;
        isValid = false:
        lastValid = interpStates(firstInvalidIdx-1,:);
    end
end
```

Terminate the methods and class sections.

```
end
end
```

Save your state space validator class definition. You can now use the class constructor to create an object for validation of states for a given state space.

See Also

nav.StateSpace | nav.StateValidator | validatorOccupancyMap |
validatorVehicleCostmap

insfilterNonholonomic

Estimate pose with nonholonomic constraints

Description

The insfilterNonholonomic object implements sensor fusion of inertial measurement unit (IMU) and GPS data to estimate pose in the NED (or ENU) reference frame. IMU data is derived from gyroscope and accelerometer data. The filter uses a 16-element state vector to track the orientation quaternion, velocity, position, and IMU sensor biases. The insfilterNonholonomic object uses an extended Kalman filter to estimate these quantities.

Creation

Syntax

```
filter = insfilterNonholonomic
filter = insfilterNonholonomic('ReferenceFrame',RF)
filter = insfilterNonholonomic(____,Name,Value)
```

Description

filter = insfilterNonholonomic creates an insfilterErrorState object with default property values.

filter = insfilterNonholonomic('ReferenceFrame',RF) allows you to specify the reference frame, RF, of the filter. Specify RF as 'NED' (North-East-Down) or 'ENU' (East-North-Up). The default value is 'NED'.

filter = insfilterNonholonomic(____, Name, Value) also allows you set properties of the created filter using one or more name-value pairs. Enclose each property name in single quotes.

Properties

IMUSampleRate — Sample rate of the IMU (Hz)

100 (default) | positive scalar

Sample rate of the IMU in Hz, specified as a positive scalar.

Data Types: single | double

ReferenceLocation — Reference location (deg, deg, meters)

[0 0 0] (default) | 3-element positive row vector

Reference location, specified as a 3-element row vector in geodetic coordinates (latitude, longitude, and altitude). Altitude is the height above the reference ellipsoid model, WGS84. The reference location units are [degrees degrees meters].

Data Types: single | double

DecimationFactor — Decimation factor for kinematic constraint correction

2 (default) | positive integer scalar

Decimation factor for kinematic constraint correction, specified as a positive integer scalar.

Data Types: single | double

GyroscopeNoise — Multiplicative process noise variance from gyroscope $(rad/s)^2$

[4.8e-6 4.8e-6] (default) | scalar | 3-element row vector

Multiplicative process noise variance from the gyroscope in (rad/s)², specified as a scalar or 3element row vector of positive real finite numbers.

- If GyroscopeNoise is specified as a row vector, the elements correspond to the noise in the x, y, and z axes of the gyroscope, respectively.
- If GyroscopeNoise is specified as a scalar, the single element is applied to the x, y, and z axes of the gyroscope.

Data Types: single | double

GyroscopeBiasNoise — Multiplicative process noise variance from gyroscope bias (rad/s)² [4e-14 4e-14] (default) | scalar | 3-element row vector

Multiplicative process noise variance from the gyroscope bias in (rad/s)², specified as a scalar or 3element row vector of positive real finite numbers. Gyroscope bias is modeled as a lowpass filtered white noise process.

- If GyroscopeBiasNoise is specified as a row vector, the elements correspond to the noise in the x, y, and z axes of the gyroscope, respectively.
- If GyroscopeBiasNoise is specified as a scalar, the single element is applied to the x, y, and z axes of the gyroscope.

Data Types: single | double

GyroscopeBiasDecayFactor — Decay factor for gyroscope bias

0.999 (default) | scalar in the range [0,1]

Decay factor for gyroscope bias, specified as a scalar in the range [0,1]. A decay factor of 0 models gyroscope bias as a white noise process. A decay factor of 1 models the gyroscope bias as a random walk process.

Data Types: single | double

AccelerometerNoise — Multiplicative process noise variance from accelerometer (m/s²)2 [4.8e-2 4.8e-2 4.8e-2] (default) | scalar | 3-element row vector

Multiplicative process noise variance from the accelerometer in (m/s²)², specified as a scalar or 3element row vector of positive real finite numbers.

- If AccelerometerNoise is specified as a row vector, the elements correspond to the noise in the x, y, and z axes of the accelerometer, respectively.
- If AccelerometerNoise is specified as a scalar, the single element is applied to each axis.

Data Types: single | double

AccelerometerBiasNoise — Multiplicative process noise variance from accelerometer bias $(m/s^2)^2$

[4e-14 4e-14] (default) | positive scalar | 3-element row vector

Multiplicative process noise variance from the accelerometer bias in $(m/s^2)^2$, specified as a scalar or 3-element row vector of positive real numbers. Accelerometer bias is modeled as a lowpass filtered white noise process.

- If AccelerometerBiasNoise is specified as a row vector, the elements correspond to the noise in the *x*, *y*, and *z* axes of the accelerometer, respectively.
- If AccelerometerBiasNoise is specified as a scalar, the single element is applied to each axis.

AccelerometerBiasDecayFactor — Decay factor for accelerometer bias

0.9999 (default) | scalar in the range [0,1]

Decay factor for accelerometer bias, specified as a scalar in the range [0,1]. A decay factor of 0 models accelerometer bias as a white noise process. A decay factor of 1 models the accelerometer bias as a random walk process.

Data Types: single | double

State — State vector of extended Kalman filter

[1; zeros(15,1)] | 16-element column vector

State vector of the extended Kalman filter. The state values represent:

State	Units	Index
Orientation (quaternion parts)	N/A	1:4
Gyroscope Bias (XYZ)	rad/s	5:7
Position (NED or ENU)	m	8:10
Velocity (NED or ENU)	m/s	11:13
Accelerometer Bias (XYZ)	m/s ²	14:16

Data Types: single | double

StateCovariance — State error covariance for extended Kalman filter

eye(16) (default) | 16-by-16 matrix

State error covariance for the extended Kalman filter, specified as a 16-by-16-element matrix, or real numbers.

Data Types: single | double

ZeroVelocityConstraintNoise — Velocity constraints noise (m/s)²

1e-2 (default) | nonnegative scalar

Velocity constraints noise in $(m/s)^2$, specified as a nonnegative scalar.

Data Types: single | double

Object Functions

correct Correct states using direct state measurements for insfilterNonholonomic

residual Residuals and residual covariances from direct state measurements for

insfilterNonholonomic

fusegps Correct states using GPS data for insfilterNonholonomic

residualgps Residuals and residual covariance from GPS measurements for insfilterNonholonomic

pose Current orientation and position estimate for insfilterNonholonomic

predict Update states using accelerometer and gyroscope data for insfilterNonholonomic

reset Reset internal states for insfilterNonholonomic

stateinfo Display state vector information for insfilterNonholonomic

tune Tune insfilterNonholonomic parameters to reduce estimation error

copy Create copy of insfitlerNonholonomic

Examples

Estimate Pose of Ground Vehicle

This example shows how to estimate the pose of a ground vehicle from logged IMU and GPS sensor measurements and ground truth orientation and position.

Load the logged data of a ground vehicle following a circular trajectory.

Initialize the insfilterNonholonomic object.

```
filt = insfilterNonholonomic;
filt.IMUSampleRate = imuFs;
filt.ReferenceLocation = localOrigin;
filt.State = initialState;
filt.StateCovariance = initialStateCovariance;
imuSamplesPerGPS = imuFs/gpsFs;
```

Log data for final metric computation. Use the predict object function to estimate filter state based on accelerometer and gyroscope data. Then correct the filter state according to GPS data.

```
numIMUSamples = size(accelData,1);
estOrient = quaternion.ones(numIMUSamples,1);
estPos = zeros(numIMUSamples,3);

gpsIdx = 1;

for idx = 1:numIMUSamples
    predict(filt,accelData(idx,:),gyroData(idx,:)); %Predict filter state

    if (mod(idx,imuSamplesPerGPS) == 0) %Correct filter state
        fusegps(filt,gpsLLA(gpsIdx,:),Rpos,gpsVel(gpsIdx,:),Rvel);
        gpsIdx = gpsIdx + 1;
    end

    [estPos(idx,:),estOrient(idx,:)] = pose(filt); %Log estimated pose
end
```

Calculate and display RMS errors.

```
posd = estPos - truePos;
quatd = rad2deg(dist(estOrient,trueOrient));
msep = sqrt(mean(posd.^2));
fprintf('Position RMS Error\n\tX: %.2f, Y: %.2f, Z: %.2f (meters)\n\n',msep(1),msep(2),msep(3));
Position RMS Error
    X: 0.15, Y: 0.11, Z: 0.01 (meters)
fprintf('Quaternion Distance RMS Error\n\t%.2f (degrees)\n\n',sqrt(mean(quatd.^2)));
Quaternion Distance RMS Error
    0.26 (degrees)
```

Algorithms

Note: The following algorithm only applies to an NED reference frame.

insfilterNonholonomic uses a 16-axis error state Kalman filter structure to estimate pose in the NED reference frame. The state is defined as:

```
q_0
             q_1
             q_2
             q_3
       gyrobias_X
       gyrobiasy
       gyrobias<sub>7</sub>
       position_N
\chi =
        position<sub>E</sub>
        position<sub>D</sub>
            \nu_N
             \nu_E
             \nu_D
       accelbiasx
       accelbiasy
       accelbias_Z
```

where

- q_0 , q_1 , q_2 , q_3 -- Parts of orientation quaternion. The orientation quaternion represents a frame rotation from the platform's current orientation to the local NED coordinate system.
- $gyrobias_X$, $gyrobias_Y$, $gyrobias_Z$ Bias in the gyroscope reading.
- $position_N$, $position_E$, $position_D$ -- Position of the platform in the local NED coordinate system.
- $\nu_{\rm N}$, $\nu_{\rm E}$, $\nu_{\rm D}$ -- Velocity of the platform in the local NED coordinate system.

• $\mathit{accelbias}_X$, $\mathit{accelbias}_Y$, $\mathit{accelbias}_Z$ — Bias in the accelerometer reading.

Given the conventional formulation of the state transition function,

$$x_{k|k-1} = f(\widehat{x}_{k-1|k-1})$$

the predicted state estimate is:

```
x_{k|k-1} =
```

```
q_0 + \Delta t * q_1(gyrobias_X/2 - gyro_X/2) + \Delta t * q_2 * (gyrobias_Y/2 - gyro_Y/2) + \Delta t * q_3 * (gyrobias_Z/2 - gyro_Z/2)
q_1 - \Delta t * q_0(gyrobias_X/2 - gyro_X/2) + \Delta t * q_3 * (gyrobias_Y/2 - gyro_Y/2) - \Delta t * q_2 * (gyrobias_Z/2 - gyro_Z/2)
q_2 - \Delta t * q_3(gyrobias_X/2 - gyro_X/2) - \Delta t * q_0 * (gyrobias_Y/2 - gyro_Y/2) + \Delta t * q_1 * (gyrobias_Z/2 - gyro_Z/2)
q_3 + \Delta t * q_2(gyrobias_X/2 - gyro_X/2) - \Delta t * q_1 * (gyrobias_Y/2 - gyro_Y/2) - \Delta t * q_0 * (gyrobias_Z/2 - gyro_Z/2)
                                                                                                          -gryobias_X * (\Delta t * \lambda_{gyro} - 1)
                                                                                                           -gryobias_Y * (\Delta t * \lambda_{gyro} - 1)
                                                                                                           -gryobias_Z * (\Delta t * \lambda_{gyro} - 1)
                                                                                                                        position_N + \Delta t * v_N
                                                                                                                        position_E + \Delta t * v_E
                                                                                                                        position_D + \Delta t * v_D
                             q_1*(q_1*(accelbias_X - accel_X) + q_2*(accelbias_Y - accel_Y) + q_3*(accelbias_Z - accel_Z)) - q_1*(accelbias_X - accel_X) + q_2*(accelbias_Y - accel_Y) + q_3*(accelbias_X - accel_X))
                             \left\lfloor q_3*(q_3*(accelbias_X-accel_X)+q_0*(accelbias_Y-accel_Y)-q_1*(accelbias_Z-accel_Z) \right) 
                             [q_0*(q_3*(accelbias_X-accel_X)+q_0*(accelbias_Y-accel_Y)-q_1*(accelbias_Z-accel_Z))-g_E-q_1*(accelbias_Z-accel_Z)]
                              q_1*(q_1*(accelbias_Y-accel_Y)-q_2*(accelbias_X-accel_X)+q_0*(accelbias_Z-accel_Z))+q_0*(accelbias_Z-accel_Z))+q_0*(accelbias_Z-accel_Z))+q_0*(accelbias_Z-accel_Z))+q_0*(accelbias_Z-accel_Z))+q_0*(accelbias_Z-accel_Z))+q_0*(accelbias_Z-accel_Z))+q_0*(accelbias_Z-accel_Z))+q_0*(accelbias_Z-accel_Z))+q_0*(accelbias_Z-accel_Z))+q_0*(accelbias_Z-accel_Z))+q_0*(accelbias_Z-accel_Z))+q_0*(accelbias_Z-accel_Z))+q_0*(accelbias_Z-accel_Z))+q_0*(accelbias_Z-accel_Z))+q_0*(accelbias_Z-accel_Z))+q_0*(accelbias_Z-accel_Z))+q_0*(accelbias_Z-accel_Z))+q_0*(accelbias_Z-accel_Z))+q_0*(accelbias_Z-accel_Z))+q_0*(accelbias_Z-accel_Z))+q_0*(accelbias_Z-accel_Z))+q_0*(accelbias_Z-accel_Z))+q_0*(accelbias_Z-accel_Z))+q_0*(accelbias_Z-accel_Z))+q_0*(accelbias_Z-accel_Z))+q_0*(accelbias_Z-accel_Z))+q_0*(accelbias_Z-accel_Z))+q_0*(accelbias_Z-accel_Z))+q_0*(accelbias_Z-accel_Z))+q_0*(accelbias_Z-accel_Z))+q_0*(accelbias_Z-accel_Z))+q_0*(accelbias_Z-accel_Z))+q_0*(accelbias_Z-accel_Z))+q_0*(accelbias_Z-accel_Z))+q_0*(accelbias_Z-accel_Z))+q_0*(accelbias_Z-accel_Z))+q_0*(accelbias_Z-accel_Z))+q_0*(accelbias_Z-accel_Z))+q_0*(accelbias_Z-accel_Z))+q_0*(accelbias_Z-accel_Z))+q_0*(accelbias_Z-accel_Z))+q_0*(accelbias_Z-accel_Z))+q_0*(accelbias_Z-accel_Z))+q_0*(accelbias_Z-accel_Z))+q_0*(accelbias_Z-accel_Z)+q_0*(accelbias_Z-accel_Z)+q_0*(accelbias_Z-accel_Z)+q_0*(accelbias_Z-accel_Z)+q_0*(accelbias_Z-accel_Z)+q_0*(accelbias_Z-accel_Z)+q_0*(accelbias_Z-accel_Z)+q_0*(accelbias_Z-accel_Z)+q_0*(accelbias_Z-accel_Z)+q_0*(accelbias_Z-accel_Z)+q_0*(accelbias_Z-accel_Z)+q_0*(accelbias_Z-accel_Z)+q_0*(accelbias_Z-accel_Z)+q_0*(accelbias_Z-accel_Z)+q_0*(accelbias_Z-accel_Z)+q_0*(accelbias_Z-accel_Z)+q_0*(accelbias_Z-accel_Z)+q_0*(accelbias_Z-accel_Z)+q_0*(accelbias_Z-accel_Z)+q_0*(accelbias_Z-accel_Z)+q_0*(accelbias_Z-accel_Z)+q_0*(accelbias_Z-accel_Z)+q_0*(accelbias_Z-accel_Z)+q_0*(accelbias_Z-accel_Z)+q_0*(accelbias_Z-accel_Z)+q_0*(accelbias_Z-accel_Z)+q_0*(accelbias_Z-accel_Z)+q_0*(accelbias_Z-accel_Z)+q_0*(accelbias_Z-accel_Z)+q_0*(accelbias_Z-a
                              q_2*(q_1*(accelbias_X-accel_X)+q_2*(accelbias_Y-accel_Y)+q_3*(accelbias_Z-accel_Z))+\\
```

where

- Δt -- IMU sample time.
- $g_{\rm N}$, $g_{\rm E}$, $g_{\rm D}$ -- Constant gravity vector in the NED frame.
- *accel*_X, *accel*_Y, *accel*_Z -- Acceleration vector in the body frame.
- λ_{accel} -- Accelerometer bias decay factor.
- λ_{gyro} -- Gyroscope bias decay factor.

References

[1] Munguía, R. "A GPS-Aided Inertial Navigation System in Direct Configuration." *Journal of applied research and technology.* Vol. 12, Number 4, 2014, pp. 803 – 814.

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

insfilterAsync|insfilterErrorState|insfilterMARG

correct

Correct states using direct state measurements for insfilterNonholonomic

Syntax

correct(FUSE,idx,measurement,measurementCovariance)

Description

correct(FUSE,idx,measurement,measurementCovariance) corrects the state and state estimation error covariance based on the measurement and measurement covariance. The measurement maps directly to the state specified by the indices idx.

Input Arguments

FUSE — insfilterNonholonomic object

object

insfilterNonholonomic, specified as an object.

idx — State vector Index of measurement to correct

N-element vector of increasing integers in the range [1,16]

State vector index of measurement to correct, specified as an N-element vector of increasing integers in the range [1,16].

The state values represent:

State	Units	Index
Orientation (quaternion parts)		1:4
Gyroscope bias (XYZ)	rad/s	5:7
Position (NED)	m	8:10
Velocity (NED)	m/s	11:13
Accelerometer Bias (XYZ)	m/s ²	14:16

Data Types: single | double

measurement — Direct measurement of state

N-element vector

Direct measurement of state, specified as a N-element vector. N is the number of elements of the index argument, idx.

Data Types: single | double

measurementCovariance — Covariance of measurement

scalar | N-element vector | N-by-N matrix

Covariance of measurement, specified as a scalar, N-element vector, or N-by-N matrix. N is the number of elements of the index argument, idx.

Data Types: single | double

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

insfilter|insfilterNonholonomic

copy

Create copy of insfitlerNonholonomic

Syntax

newFilter = copy(filter)

Description

newFilter = copy(filter) returns a copy of the insfilterNonholonomic, filter, with the
exactly same property values.

Input Arguments

filter — Filter to be copied

insfitlerNonholonomic

Filter to be copied, specified as an insfilterNonholonomic object.

Output Arguments

newFilter — New copied filter

insfitlerNonholonomic

New copied filter, returned as an insfilterNonholonomic object.

See Also

insfilterNonholonomic

Introduced in R2020b

fusegps

Correct states using GPS data for insfilterNonholonomic

Syntax

```
[res,resCov] = fusegps(FUSE,position,positionCovariance)
[res,resCov] = fusegps(FUSE,position,positionCovariance,velocity,
velocityCovariance)
```

Description

[res,resCov] = fusegps(FUSE,position,positionCovariance) fuses GPS position data to correct the state estimate.

[res,resCov] = fusegps(FUSE,position,positionCovariance,velocity,
velocityCovariance) fuses GPS position and velocity data to correct the state estimate.

Input Arguments

FUSE — insfilterNonholonomic object

object

insfilterNonholonomic, specified as an object.

position — Position of GPS receiver (LLA)

3-element row vector

Position of GPS receiver in geodetic latitude, longitude, and altitude (LLA) specified as a real finite 3-element row vector. Latitude and longitude are in degrees with north and east being positive. Altitude is in meters.

Data Types: single | double

positionCovariance — Position measurement covariance of GPS receiver (m²)

3-by-3 matrix

Position measurement covariance of GPS receiver in m², specified as a 3-by-3 matrix.

Data Types: single | double

velocity — Velocity of GPS receiver in local NED coordinate system (m/s)

3-element row vector

Velocity of the GPS receiver in the local NED coordinate system in m/s, specified as a 3-element row vector.

Data Types: single | double

velocityCovariance — Velocity measurement covariance of GPS receiver (m/s²)

3-by-3 matrix

Velocity measurement covariance of the GPS receiver in the local NED coordinate system in m/s², specified as a 3-by-3 matrix.

Data Types: single | double

Output Arguments

res — Position and course residual

1-by-4 vector of real values

Position and course residual, returned as a 1-by-6 vector of real values in m and rad/s, respectively.

resCov — Residual covariance

4-by-4 matrix of real values

Residual covariance, returned as a 4-by-4 matrix of real values.

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

insfilter|insfilterNonholonomic

pose

Current orientation and position estimate for insfilterNonholonomic

Syntax

```
[position,orientation,velocity] = pose(FUSE)
[position,orientation,velocity] = pose(FUSE,format)
```

Description

[position, orientation, velocity] = pose(FUSE) returns the current estimate of the pose.

[position, orientation, velocity] = pose(FUSE, format) returns the current estimate of the pose with orientation in the specified orientation format.

Input Arguments

FUSE — NHConstrainedIMUGPSFuser object

object

insfilterNonholonomic, specified as an object.

format — Output orientation format

```
'quaternion' (default) | 'rotmat'
```

Output orientation format, specified as either 'quaternion' for a quaternion or 'rotmat' for a rotation matrix.

Data Types: char | string

Output Arguments

position — Position estimate in the local NED coordinate system (m)

3-element row vector

Position estimate in the local NED coordinate system in meters, returned as a 3-element row vector.

Data Types: single | double

orientation — Orientation estimate in the local NED coordinate system

quaternion (default) | 3-by-3 rotation matrix

Orientation estimate in the local NED coordinate system, specified as a scalar quaternion or 3-by-3 rotation matrix. The quaternion or rotation matrix represents a frame rotation from the local NED reference frame to the body reference frame.

Data Types: single | double | quaternion

velocity — Velocity estimate in local NED coordinate system (m/s)

3-element row vector

Velocity estimate in the local NED coordinate system in m/s, returned as a 3-element row vector.

Data Types: single | double

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder $^{\text{\tiny TM}}$.

See Also

insfilter|insfilterNonholonomic

predict

Update states using accelerometer and gyroscope data for insfilterNonholonomic

Syntax

predict(FUSE,accelReadings,gyroReadings)

Description

predict(FUSE,accelReadings,gyroReadings) fuses accelerometer and gyroscope data to update the state estimate.

Input Arguments

FUSE — insfilterNonholonomic object

object

insfilterNonholonomic, specified as an object.

accelReadings — Accelerometer readings in local sensor body coordinate system (m/s²)

3-element row vector

Accelerometer readings in m/s², specified as a 3-element row vector.

Data Types: single | double

gyroReadings — Gyroscope readings in local sensor body coordinate system (rad/s)

3-element row vector

Gyroscope readings in rad/s, specified as a 3-element row vector.

Data Types: single | double

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

insfilter|insfilterNonholonomic

reset

Reset internal states for insfilterNonholonomic

Syntax

reset(FUSE)

Description

reset (FUSE) resets the State, StateCovariance, and internal integrators to their default values.

Input Arguments

FUSE — insfilterNonholonomic object

object

insfilterNonholonomic, specified as an object.

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

insfilter|insfilterNonholonomic

residual

Residuals and residual covariances from direct state measurements for insfilterNonholonomic

Syntax

[res, resCov] = residual(FUSE,idx,measurement,measurementCovariance)

Description

[res, resCov] = residual(FUSE,idx,measurement,measurementCovariance) computes the residual, res, and the residual covariance, resCov, based on the direct state measurement and measurement covariance. The measurement maps directly to the states specified by indices, idx.

Input Arguments

FUSE — insfilterNonholonomic object

object

insfilterNonholonomic, specified as an object.

idx — State vector Index of measurement to correct

N-element vector of increasing integers in the range [1,16]

State vector index of measurement to correct, specified as an N-element vector of increasing integers in the range [1,16].

The state values represent:

State	Units	Index
Orientation (quaternion parts)		1:4
Gyroscope bias (XYZ)	rad/s	5:7
Position (NED)	m	8:10
Velocity (NED)	m/s	11:13
Accelerometer Bias (XYZ)	m/s ²	14:16

Data Types: single | double

measurement — Direct measurement of state

N-element vector

Direct measurement of state, specified as a N-element vector. N is the number of elements of the index argument, idx.

measurementCovariance — Covariance of measurement

N-by-*N* matrix

Covariance of measurement, specified as an N-by-N matrix. N is the number of elements of the index argument, idx.

Output Arguments

res — Measurement residual

1-by-*N* vector of real values

Measurement residual, returned as a 1-by-*N* vector of real values.

resCov — Residual covariance

N-by-N matrix of real values

Residual covariance, returned as a *N*-by-*N* matrix of real values.

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

insfilter|insfilterNonholonomic

Introduced in R2020a

residualgps

Residuals and residual covariance from GPS measurements for insfilterNonholonomic

Syntax

```
[res,resCov] = residualgps(FUSE,position,positionCovariance)
[res,resCov] = residualgps(FUSE,position,positionCovariance,velocity,velocityCovariance)
```

Description

[res,resCov] = residualgps(FUSE,position,positionCovariance) computes the
residual, res, and the residual covariance, resCov, based on the GPS position measurement and
covariance.

[res,resCov] = residualgps(FUSE,position,positionCovariance,velocity,
velocityCovariance) computes the residual, res, and the residual covariance, resCov, based on
the GPS position measurement and covariance.

Input Arguments

FUSE — insfilterNonholonomic object

object

insfilterNonholonomic, specified as an object.

position — Position of GPS receiver (LLA)

3-element row vector

Position of GPS receiver in geodetic latitude, longitude, and altitude (LLA) specified as a real finite 3-element row vector. Latitude and longitude are in degrees with north and east being positive. Altitude is in meters.

Data Types: single | double

positionCovariance — Position measurement covariance of GPS receiver (m²)

3-by-3 matrix

Position measurement covariance of GPS receiver in m², specified as a 3-by-3 matrix.

Data Types: single | double

velocity — Velocity of GPS receiver in local NED coordinate system (m/s)

3-element row vector

Velocity of the GPS receiver in the local NED coordinate system in m/s, specified as a 3-element row vector.

Data Types: single | double

velocityCovariance — Velocity measurement covariance of GPS receiver (m/s²)

3-by-3 matrix

Velocity measurement covariance of the GPS receiver in the local NED coordinate system in m/s^2 , specified as a 3-by-3 matrix.

Data Types: single | double

Output Arguments

res — Position and course residual

1-by-3 vector of real values | 1-by-4 vector of real values

Position and course residual, returned as a 1-by-3 vector of real values the inputs only contain position information, and returned as a 1-by-4 vector of real values if the inputs also contain velocity information.

resCov — Residual covariance

3-by-3 matrix of real values | 4-by-4 matrix of real values

Residual covariance, returned as a 3-by-3 matrix of real values if the inputs only contain position information, and a 4-by-4 vector of real values if the inputs also contain velocity information.

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

insfilterNonholonomic

Introduced in R2020a

stateinfo

Display state vector information for insfilterNonholonomic

Syntax

```
stateinfo(FUSE)
info = stateinfo(FUSE)
```

Description

stateinfo(FUSE) displays the meaning of each index of the State property and the associated units.

info = stateinfo(FUSE) returns a structure with fields containing descriptions of the elements of
the state vector of the filter, FUSE.

Examples

State information of insfilterNonholonomic

Create an insfilterNonholonomic object.

```
filter = insfilterErrorState;
```

Display the state information of the created filter.

stateinfo(filter)

```
Index
                                   Units
States
Orientation (quaternion parts)
                                            1:4
                                             5:7
Position (NAV)
Velocity (NAV)
                                   m/s
                                            8:10
Gyroscope Bias (XYZ)
                                   rad/s
                                            11:13
Accelerometer Bias (XYZ)
                                   m/s^2
                                            14:16
Visual Odometry Scale
                                             17
```

Output the state information of the filter as a structure.

```
info = stateinfo(filter)
```

Input Arguments

FUSE — insfilterNonholonomic object

object

 $\verb"insfilterNonholonomic", specified as an object.$

Output Arguments

info — State information

structure

State information, returned as a structure with fields containing descriptions of the elements of the state vector of the filter. The values of each field are the corresponding indices of the state vector.

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

insfilter|insfilterNonholonomic

tune

Tune insfilterNonholonomic parameters to reduce estimation error

Syntax

Description

tunedMeasureNoise = tune(filter, measureNoise, sensorData, groundTruth) adjusts the properties of the insfilterNonholonomic filter object, filter, and measurement noises to reduce the root-mean-squared (RMS) state estimation error between the fused sensor data and the ground truth. The function also returns the tuned measurement noise, tunedMeasureNoise. The function uses the property values in the filter and the measurement noise provided in the measureNoise structure as the initial estimate for the optimization algorithm.

tunedMeasureNoise = tune(____, config) specifies the tuning configuration based on a tunerconfig object, config.

Examples

Tune insfilterNonholonomic to Optimize Pose Estimate

Load the recorded sensor data and ground truth data.

GPSVelocityNoise: 1

Tune the filter and obtain the tuned measurement noise.

tunedNoise = tune(filter,measNoise,sensorData,groundTruth,config);

Iteration	Parameter	Metric
1	GyroscopeNoise	3.4877
1	AccelerometerNoise	3.3961
1	GyroscopeBiasNoise	3.3961
1	GyroscopeBiasDecayFactor	3.3961
1	AccelerometerBiasNoise	3.3961
1	AccelerometerBiasDecayFactor	3.3961
1	ZeroVelocityConstraintNoise	3.3935
1	GPSPositionNoise	3.2848
1	GPSVelocityNoise	3.2798
2	GyroscopeNoise	3.2641
2 2	AccelerometerNoise	3.1715
2	GyroscopeBiasNoise	3.1715
2	GyroscopeBiasDecayFactor	2.9661
2	AccelerometerBiasNoise	2.9661
2	AccelerometerBiasDecayFactor	2.9661
2	ZeroVelocityConstraintNoise	2.9617
2	GPSPositionNoise	2.8438
2	GPSVelocityNoise	2.8384
3	GyroscopeNoise	2.8373
3	AccelerometerNoise	2.7382
3	GyroscopeBiasNoise	2.7382
3	GyroscopeBiasDecayFactor	2.7382
3	AccelerometerBiasNoise	2.7382
2 2 2 2 2 3 3 3 3 3 3 3 3 3	AccelerometerBiasDecayFactor	2.7382
3	ZeroVelocityConstraintNoise	2.7335
3	GPSPositionNoise	2.6105
4	GPSVelocityNoise	2.6045
4	GyroscopeNoise	2.6023 2.5001
4	AccelerometerNoise GyroscopeBiasNoise	2.5001
4	GyroscopeBiasDecayFactor	2.5001
4	AccelerometerBiasNoise	2.5001
4	AccelerometerBiasDecayFactor	2.5001
4	ZeroVelocityConstraintNoise	2.4953
4	GPSPositionNoise	2.3692
4	GPSVelocityNoise	2.3626
5	GyroscopeNoise	2.3595
5	AccelerometerNoise	2.2561
5	GyroscopeBiasNoise	2.2561
	GyroscopeBiasDecayFactor	2.2508
5	AccelerometerBiasNoise	2.2508
5	AccelerometerBiasDecayFactor	2.2508
5 5 5 5 5	ZeroVelocityConstraintNoise	2.2469
5	GPSPositionNoise	2.1265
5	GPSVelocityNoise	2.1191
6	GyroscopeNoise	2.1148
6	AccelerometerNoise	2.0150
6	GyroscopeBiasNoise	2.0150
6	GyroscopeBiasDecayFactor	2.0150

6	A 7 . B: N :	0.150
6	AccelerometerBiasNoise	2.0150
6	AccelerometerBiasDecayFactor	2.0150
6	ZeroVelocityConstraintNoise	2.0116
6	GPSPositionNoise	
		1.8970
6	GPSVelocityNoise	1.8888
7	GyroscopeNoise	1.8847
7	AccelerometerNoise	1.7921
7	GyroscopeBiasNoise	1.7921
7	GyroscopeBiasDecayFactor	1.7845
7	AccelerometerBiasNoise	1.7845
7	AccelerometerBiasDecayFactor	1.7845
7	ZeroVelocityConstraintNoise	1.7815
7	GPSPositionNoise	1.6794
7		
	GPSVelocityNoise	1.6708
8	GyroscopeNoise	1.6679
8	AccelerometerNoise	1.5886
8	GyroscopeBiasNoise	1.5886
8	GyroscopeBiasDecayFactor	1.5866
8		
	AccelerometerBiasNoise	1.5866
8	AccelerometerBiasDecayFactor	1.5866
8	ZeroVelocityConstraintNoise	1.5850
8	GPSPositionNoise	1.5057
8	GPSVelocityNoise	1.4965
9		1.4950
	GyroscopeNoise	
9	AccelerometerNoise	1.4364
9	GyroscopeBiasNoise	1.4364
9	GyroscopeBiasDecayFactor	1.4364
9	AccelerometerBiasNoise	1.4364
9	AccelerometerBiasDecayFactor	1.4364
9	ZeroVelocityConstraintNoise	1.4355
9	GPSPositionNoise	1.3894
9	GPSVelocityNoise	1.3790
10	GyroscopeNoise	1.3773
10	AccelerometerNoise	1.3422
10	GyroscopeBiasNoise	1.3422
10	GyroscopeBiasDecayFactor	1.3421
10	AccelerometerBiasNoise	1.3421
10	AccelerometerBiasDecayFactor	1.3421
10	ZeroVelocityConstraintNoise	1.3399
10	GPSPositionNoise	1.3319
10	GPSVelocityNoise	1.3190
11	GyroscopeNoise	1.3159
11	AccelerometerNoise	1.3102
11	GyroscopeBiasNoise	1.3102
11	GyroscopeBiasDecayFactor	1.3100
11	AccelerometerBiasNoise	1.3100
11	AccelerometerBiasDecayFactor	1.3100
11	ZeroVelocityConstraintNoise	1.3069
11	GPSPositionNoise	1.2964
11	GPSVelocityNoise	1.2762
12	GyroscopeNoise	1.2740
12	AccelerometerNoise	1.2655
12	GyroscopeBiasNoise	1.2655
12	GyroscopeBiasDecayFactor	1.2641
12	AccelerometerBiasNoise	1.2641
12	AccelerometerBiasDecayFactor	1.2641
12	ZeroVelocityConstraintNoise	1.2631
12	GPSPositionNoise	1.2511

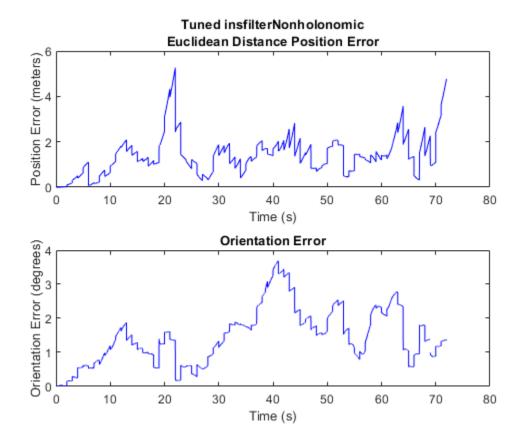
12	GPSVelocityNoise	1.2198
13	GyroscopeNoise	1.2184
13	AccelerometerNoise	1.2058
13	GyroscopeBiasNoise	1.2058
13	GyroscopeBiasDecayFactor	1.2029
13	AccelerometerBiasNoise	1.2029
13	AccelerometerBiasDecayFactor	1.2029
13	ZeroVelocityConstraintNoise	1.2029
13	GPSPositionNoise	1.1874
13	GPSVelocityNoise	1.1408
14		1.1403
	GyroscopeNoise	
14	AccelerometerNoise	1.1236
14		
	GyroscopeBiasNoise	1.1236
14	GyroscopeBiasDecayFactor	1.1186
14		1.1186
	AccelerometerBiasNoise	
14	AccelerometerBiasDecayFactor	1.1186
14		
	ZeroVelocityConstraintNoise	1.1183
14	GPSPositionNoise	1.0975
14	GPSVelocityNoise	1.0348
15	GyroscopeNoise	1.0347
15	AccelerometerNoise	1.0155
15	GyroscopeBiasNoise	1.0155
15	GyroscopeBiasDecayFactor	1.0081
15	AccelerometerBiasNoise	1.0081
15	AccelerometerBiasDecayFactor	1.0081
15	ZeroVelocityConstraintNoise	1.0076
15	GPSPositionNoise	0.9813
15	GPSVelocityNoise	0.9078
16	GyroscopeNoise	0.9074
16	AccelerometerNoise	0.8926
16	GyroscopeBiasNoise	0.8926
16	GyroscopeBiasDecayFactor	0.8823
16	AccelerometerBiasNoise	0.8823
16	AccelerometerBiasDecayFactor	0.8823
16	ZeroVelocityConstraintNoise	0.8815
16	GPSPositionNoise	0.8526
16	GPSVelocityNoise	0.7926
17	GyroscopeNoise	0.7920
17	AccelerometerNoise	0.7870
17	GyroscopeBiasNoise	0.7870
17		0.7742
1/	GyroscopeBiasDecayFactor	
17	AccelerometerBiasNoise	0.7742
17		0.7742
	AccelerometerBiasDecayFactor	
17	ZeroVelocityConstraintNoise	0.7730
17	GPSPositionNoise	
		0.7665
17	GPSVelocityNoise	0.7665
18	-	
	GyroscopeNoise	0.7662
18	AccelerometerNoise	0.7638
18	GyroscopeBiasNoise	0.7638
18	GyroscopeBiasDecayFactor	0.7495
18	AccelerometerBiasNoise	0.7495
18	AccelerometerBiasDecayFactor	0.7495
18		0.7482
	ZeroVelocityConstraintNoise	
18	GPSPositionNoise	0.7482
18	GPSVelocityNoise	0.7475
19	GyroscopeNoise	0.7474
19	AccelerometerNoise	0.7474
19	GyroscopeBiasNoise	0.7474

19	GyroscopeBiasDecayFactor	0.7474
19	AccelerometerBiasNoise	0.7474
19	AccelerometerBiasDecayFactor	0.7474
19	ZeroVelocityConstraintNoise	0.7453
19	GPSPositionNoise	0.7416
19	GPSVelocityNoise	0 7202
	GPSVeloCilyNoise	0.7382
20	GyroscopeNoise	0.7378
	·	
20	AccelerometerNoise	0.7370
20	GyroscopeBiasNoise	0.7370
20	GyroscopeBiasDecayFactor	0.7370
20	AccelerometerBiasNoise	0.7370
20	AccelerometerBiasDecayFactor	0.7370
20	ZeroVelocityConstraintNoise	0.7345
20	GPSPositionNoise	0.7345
20	GPSVelocityNoise	0.7345
21	GyroscopeNoise	0.7334
21	AccelerometerNoise	0.7334
21		
	GyroscopeBiasNoise	0.7334
21	GyroscopeBiasDecayFactor	0.7334
21	AccelerometerBiasNoise	0.7334
21		
	AccelerometerBiasDecayFactor	0.7334
21	ZeroVelocityConstraintNoise	0.7306
	-	
21	GPSPositionNoise	0.7279
21		
	GPSVelocityNoise	0.7268
22	GyroscopeNoise	0.7248
22	AccelerometerNoise	0.7247
22	GyroscopeBiasNoise	0.7247
22	GyroscopeBiasDecayFactor	0.7234
22	AccelerometerBiasNoise	0.7234
22	AccelerometerBiasDecayFactor	0.7234
22	ZeroVelocityConstraintNoise	0.7207
22	GPSPositionNoise	0.7206
22	GPSVelocityNoise	0.7170
23	GyroscopeNoise	0.7138
23	AccelerometerNoise	0.7134
23	GyroscopeBiasNoise	0.7134
23	GyroscopeBiasDecayFactor	0.7134
23	AccelerometerBiasNoise	0.7134
23	AccelerometerBiasDecayFactor	0.7134
23	ZeroVelocityConstraintNoise	0.7122
23	GPSPositionNoise	0.7122
23	GPSVelocityNoise	0.7122
24	GyroscopeNoise	0.7081
24	AccelerometerNoise	0.7080
24	GyroscopeBiasNoise	0.7080
24	GyroscopeBiasDecayFactor	0.7080
24	AccelerometerBiasNoise	0.7080
24	AccelerometerBiasDecayFactor	0.7080
24	ZeroVelocityConstraintNoise	0.7080
24	GPSPositionNoise	0.7080
24		
	GPSVelocityNoise	0.7072
25	GyroscopeNoise	0.7009
25	AccelerometerNoise	0.7009
25	GyroscopeBiasNoise	0.7009
25	GyroscopeBiasDecayFactor	0.7007
25	AccelerometerBiasNoise	0.7007
25	AccelerometerBiasDecayFactor	0.7007
25	ZeroVelocityConstraintNoise	0.7005

```
25
             GPSPositionNoise
                                               0.6997
25
             GPSVelocityNoise
                                               0.6997
26
             GyroscopeNoise
                                               0.6912
26
             AccelerometerNoise
                                               0.6906
26
             GyroscopeBiasNoise
                                               0.6906
26
             GyroscopeBiasDecayFactor
                                               0.6906
26
             AccelerometerBiasNoise
                                               0.6906
26
             AccelerometerBiasDecayFactor
                                               0.6906
26
             ZeroVelocityConstraintNoise
                                               0.6896
26
             GPSPositionNoise
                                               0.6896
26
             GPSVelocityNoise
                                               0.6896
27
             GyroscopeNoise
                                               0.6840
27
             AccelerometerNoise
                                               0.6831
27
                                               0.6831
             GyroscopeBiasNoise
27
             GyroscopeBiasDecayFactor
                                               0.6831
27
                                               0.6831
             AccelerometerBiasNoise
27
             AccelerometerBiasDecayFactor
                                               0.6831
27
             ZeroVelocityConstraintNoise
                                               0.6818
27
             GPSPositionNoise
                                               0.6816
27
             GPSVelocityNoise
                                               0.6816
28
             GyroscopeNoise
                                               0.6816
28
             AccelerometerNoise
                                               0.6809
28
             GyroscopeBiasNoise
                                               0.6809
28
                                               0.6809
             GyroscopeBiasDecayFactor
28
             AccelerometerBiasNoise
                                               0.6809
28
             AccelerometerBiasDecayFactor
                                               0.6809
28
             ZeroVelocityConstraintNoise
                                               0.6804
28
             GPSPositionNoise
                                               0.6802
28
             GPSVelocityNoise
                                               0.6802
29
             GyroscopeNoise
                                               0.6793
29
             AccelerometerNoise
                                               0.6785
29
             GyroscopeBiasNoise
                                               0.6785
29
             GyroscopeBiasDecayFactor
                                               0.6785
29
             AccelerometerBiasNoise
                                               0.6785
29
             AccelerometerBiasDecayFactor
                                               0.6785
29
             ZeroVelocityConstraintNoise
                                               0.6778
29
             GPSPositionNoise
                                               0.6773
29
             GPSVelocityNoise
                                               0.6773
30
             GyroscopeNoise
                                               0.6773
30
             AccelerometerNoise
                                               0.6769
30
             GyroscopeBiasNoise
                                               0.6769
30
             GyroscopeBiasDecayFactor
                                               0.6769
30
             AccelerometerBiasNoise
                                               0.6769
30
             AccelerometerBiasDecayFactor
                                               0.6769
30
             ZeroVelocityConstraintNoise
                                               0.6769
30
             GPSPositionNoise
                                               0.6769
30
                                               0.6769
             GPSVelocityNoise
```

Fuse the sensor data using the tuned filter. Obtain estimated pose and orientation.

```
tunedNoise.GPSVelocityNoise);
    end
    [posEstTuned(ii,:),qEstTuned(ii,:)] = pose(filter);
end
Compute the RMS errors.
orientationErrorTuned = rad2deg(dist(qEstTuned,Orientation));
rmsOrientationErrorTuned = sqrt(mean(orientationErrorTuned.^2))
rmsOrientationErrorTuned = 1.6857
positionErrorTuned = sqrt(sum((posEstTuned-Position).^2,2));
rmsPositionErrorTuned = sqrt(mean(positionErrorTuned.^2))
rmsPositionErrorTuned = 1.6667
Visualize the results.
figure;
t = (0:N-1)./filter.IMUSampleRate;
subplot(2,1,1)
plot(t,positionErrorTuned,'b');
title("Tuned insfilterNonholonomic" + newline + ...
    "Euclidean Distance Position Error")
xlabel('Time (s)');
ylabel('Position Error (meters)')
subplot(2,1,2)
plot(t,orientationErrorTuned,'b');
title("Orientation Error")
xlabel('Time (s)');
ylabel('Orientation Error (degrees)');
```



Input Arguments

filter — Filter object

infilterAsync object

 $Filter\ object,\ specified\ as\ an\ \verb"insfilterNonholonomic"\ object.$

measureNoise — Measurement noise

structure

Measurement noise, specified as a structure. The function uses the measurement noise input as the initial guess for tuning the measurement noise. The structure must contain these fields:

Field name	Description
GPSPositionNoise	Variance of GPS position noise, specified as a scalar in m ²
GPSVelocityNoise	Variance of GPS velocity noise, specified as a scalar in (m/s) ²

Data Types: struct

sensorData — Sensor data

table

Sensor data, specified as a table. In each row, the sensor data is specified as:

- Accelerometer Accelerometer data, specified as a 1-by-3 vector of scalars in m²/s.
- Gyroscope Gyroscope data, specified as a 1-by-3 vector of scalars in rad/s.
- GPSPosition GPS position data, specified as a 1-by-3 vector of scalars in meters.
- GPSVelocity GPS velocity data, specified as a 1-by-3 vector of scalars in m/s.

If the GPS sensor does not produce complete measurements, specify the corresponding entry for GPSPosition and/or GPSVelocity as NaN. If you set the Cost property of the tuner configuration input, config, to Custom, then you can use other data types for the sensorData input based on your choice.

Data Types: table

groundTruth — Ground truth data

table

Ground truth data, specified as a table. In each row, the table can optionally contain any of these variables:

- Orientation Orientation from the navigation frame to the body frame, specified as a quaternion or a 3-by-3 rotation matrix.
- Position Position in navigation frame, specified as a 1-by-3 vector of scalars in meters.
- Velocity Velocity in navigation frame, specified as a 1-by-3 vector of scalars in m/s.
- GyroscopeBias Gyroscope delta angle bias in body frame, specified as a 1-by-3 vector of scalars in rad/s.
- AccelerometerBias Accelerometer delta angle bias in body frame, specified as a 1-by-3 vector of scalars in m²/s.

The function processes each row of the sensorData and groundTruth tables sequentially to calculate the state estimate and RMS error from the ground truth. State variables not present in groundTruth input are ignored for the comparison. The sensorData and the groundTruth tables must have the same number of rows.

If you set the Cost property of the tuner configuration input, config, to Custom, then you can use other data types for the groundTruth input based on your choice.

Data Types: table

config — Tuner configuration

tunerconfig object

Tuner configuration, specified as a tunerconfig object.

Output Arguments

tunedMeasureNoise — Tuned measurement noise

structure

Tuned measurement noise, returned as a structure. The structure contains these fields.

Field name	Description
	Variance of GPS position noise, specified as a scalar in m ²
GPSVelocityNoise	Variance of GPS velocity noise, specified as a scalar in $(m/s)^2$

Data Types: struct

References

[1] Abbeel, Pieter, et al. "Discriminative Training of Kalman Filters." Robotics: Science and Systems I, Robotics: Science and Systems Foundation, 2005. DOI.org (Crossref), doi:10.15607/RSS.2005.I.038.

See Also

insfilterNonholonomic|tunerconfig|tunernoise

Introduced in R2020b

occupancyMap

Create occupancy map with probabilistic values

Description

occupancyMap creates a 2-D occupancy grid map object. Each cell in the occupancy grid has a value representing the probability of the occupancy of that cell. Values close to 1 represent a high probability that the cell contains an obstacle. Values close to 0 represent a high probability that the cell is not occupied and obstacle free.

Occupancy maps are used in navigation algorithms such as path planning (see plannerRRT). They are also used in mapping applications for finding collision-free paths, performing collision avoidance, and calculating localization (see monteCarloLocalization). You can modify your occupancy map to fit your specific application.

The occupancyMap objects support local coordinates, world coordinates, and grid indices. The first grid location with index (1,1) begins in the top-left corner of the grid.

Use the occupancyMap class to create 2-D maps of an environment with probability values representing different obstacles in your world. You can specify exact probability values of cells or include observations from sensors such as laser scanners.

Probability values are stored using a binary Bayes filter to estimate the occupancy of each grid cell. A log-odds representation is used, with values stored as int16 to reduce the map storage size and allow for real-time applications.

Creation

Syntax

```
map = occupancyMap(width,height)
map = occupancyMap(width,height,resolution)
map = occupancyMap(rows,cols,resolution,'grid')
map = occupancyMap(p)
map = occupancyMap(p,resolution)
map = occupancyMap(sourcemap)
map = occupancyMap(sourcemap,resolution)
```

Description

map = occupancyMap(width,height) creates a 2-D occupancy map object representing a world space of width and height in meters. The default grid resolution is 1 cell per meter.

map = occupancyMap(width, height, resolution) creates an occupancy map with a specified
grid resolution in cells per meter. resolution sets the "Resolution" on page 2-0 property.

map = occupancyMap(rows,cols,resolution,'grid') creates an occupancy map with the
specified number of rows and columns and with the resolution in cells per meter. The values of rows
and cols sets the "GridSize" on page 2-0 property.

map = occupancyMap(p) creates an occupancy map from the values in matrix p. The grid size matches the size of the matrix, with each cell probability value interpreted from the matrix location.

map = occupancyMap(p,resolution) creates an occupancy map from the specified matrix and resolution in cells per meter.

map = occupancyMap(sourcemap) creates an object using values from another occupancyMap
object.

map = occupancyMap(sourcemap, resolution) creates an object using values from another
occupancyMap object, but resamples the matrix to have the specified resolution.

Input Arguments

width — Map width

scalar

Map width, specified as a scalar in meters.

height — Map height

scalar

Map height, specified as a scalar in meters.

resolution — Grid resolution

1 (default) | scalar

Grid resolution, specified as a scalar in cells per meter.

rows — Number of rows in grid

positive scalar integer

Number of rows in grid, specified as a positive scalar integer.

cols — Number of columns in grid

positive scalar integer

Number of columns in grid, specified as a positive scalar integer.

p — Input occupancy grid

matrix of probability values from 0 to 1

Input occupancy grid, specified as a matrix of probability values from 0 to 1. The size of the grid matches the size of the matrix. Each matrix element corresponds to the probability of the grid cell location being occupied. Values close to 1 represent a high certainty that the cell contains an obstacle. Values close to 0 represent certainty that the cell is not occupied and obstacle free.

sourcemap — Occupancy map object

occupancyMap object

Occupancy map object, specified as a occupancyMap object.

Properties

FreeThreshold — Threshold below which cells are considered obstacle-free

scalar between 0 and 1

Threshold below which cells are considered obstacle-free, specified as a scalar between 0 and 1 inclusive. Cells with probability values below this threshold are considered obstacle free. This property also defines the free locations for path planning when using objects like plannerRRT.

Data Types: double

OccupiedThreshold — Threshold above which cells are considered occupied

scalar

Threshold above which cells are considered occupied, specified as a scalar. Cells with probability values above this threshold are considered occupied.

Data Types: double

ProbabilitySaturation — Saturation limits for probability

[0.001 0.999] (default) | two-element real-valued vector

Saturation limits for probability, specified as a 1-by-2 real-valued vector representing the minimum and maximum values, in that order. Values above or below these saturation values are set to the minimum and maximum values. This property reduces oversaturating of cells when incorporating multiple observations.

Data Types: double

GridSize — Number of rows and columns in grid

two-element integer-valued vector

This property is read-only.

Number of rows and columns in grid, stored as a 1-by-2 real-valued vector representing the number of rows and columns, in that order.

Data Types: double

Resolution — **Grid resolution**

1 (default) | scalar

This property is read-only.

Grid resolution, stored as a scalar in cells per meter representing the number and size of grid locations.

Data Types: double

XLocalLimits — Minimum and maximum values of x-coordinates in local frame

two-element vector

This property is read-only.

Minimum and maximum values of x-coordinates in local frame, stored as a two-element horizontal vector of the form [min max]. Local frame is defined by LocalOriginInWorld property.

Data Types: double

YLocalLimits — Minimum and maximum values of y-coordinates in local frame

two-element vector

This property is read-only.

Minimum and maximum values of *y*-coordinates in local frame, stored as a two-element horizontal vector of the form [min max]. Local frame is defined by LocalOriginInWorld property.

Data Types: double

XWorldLimits — Minimum and maximum world range values of x-coordinates

two-element vector

This property is read-only.

Minimum and maximum world range values of *x*-coordinates, stored as a 1-by-2 vector representing the minimum and maximum values, in that order.

Data Types: double

YWorldLimits — Minimum and maximum world range values of y-coordinates

two-element vector

This property is read-only.

Minimum and maximum world range values of *y*-coordinates, stored as a 1-by-2 vector representing the minimum and maximum values, in that order.

Data Types: double

GridLocationInWorld — [x y] world coordinates of grid

[0 0] (default) | two-element vector

[x,y] world coordinates of the bottom-left corner of the grid, specified as a 1-by-2 vector.

Data Types: double

LocalOriginInWorld — Location of the local frame in world coordinates

[0 0] (default) | two-element vector | [xWorld yWorld]

Location of the origin of the local frame in world coordinates, specified as a two-element vector, [xLocal yLocal]. Use the move function to shift the local frame as your vehicle moves.

Data Types: double

GridOriginInLocal — Location of the grid in local coordinates

[0 0] (default) | two-element vector | [xLocal yLocal]

Location of the bottom-left corner of the grid in local coordinates, specified as a two-element vector, [xLocal yLocal].

Data Types: double

DefaultValue — Default value for unspecified map locations

0.5 (default) | scalar between 0 and 1

Default value for unspecified map locations including areas outside the map, specified as a scalar between θ and 1 inclusive.

Data Types: double

Object Functions

checkOccupancy Check locations for free, occupied, or unknown values

copy Create copy of occupancy grid getOccupancy Get occupancy value of locations

grid2local Convert grid indices to local coordinates
grid2world Convert grid indices to world coordinates
inflate Inflate each occupied grid location
insertRay Insert ray from laser scan observation
local2grid Convert local coordinates to grid indices
local2world Convert local coordinates to world coordinates

move Move map in world frame

occupancyMatrix Convert occupancy grid to double matrix

raycast Compute cell indices along a ray

rayIntersection Find intersection points of rays and occupied map cells

setOccupancy Set occupancy value of locations show Show grid values in a figure syncWith Sync map with overlapping map

updateOccupancy Integrate probability observations at locations world2grid Convert world coordinates to grid indices Convert world coordinates to local coordinates

Examples

Insert Laser Scans into Occupancy Map

```
Create an empty occupancy grid map.
```

```
map = occupancyMap(10, 10, 20);
```

Input pose of the vehicle, ranges, angles, and the maximum range of the laser scan.

```
pose = [5,5,0];
ranges = 3*ones(100,1);
angles = linspace(-pi/2,pi/2,100);
maxrange = 20;
```

Create a lidarScan object with the specified ranges and angles.

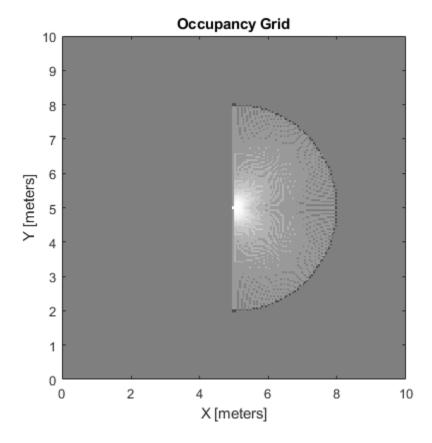
```
scan = lidarScan(ranges,angles);
```

Insert the laser scan data into the occupancy map.

```
insertRay(map,pose,scan,maxrange);
```

Show the map to see the results of inserting the laser scan.

```
show(map)
```



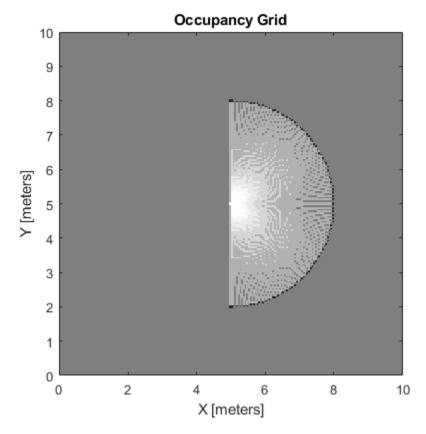
Check the occupancy of the spot directly in front of the vehicle.

```
getOccupancy(map,[8 5])
```

ans = 0.7000

Add a second reading and view the update to the occupancy values. The additional reading increases the confidence in the readings. The free and occupied values become more distinct.

insertRay(map,pose,scan,maxrange);
show(map)



getOccupancy(map,[8 5])

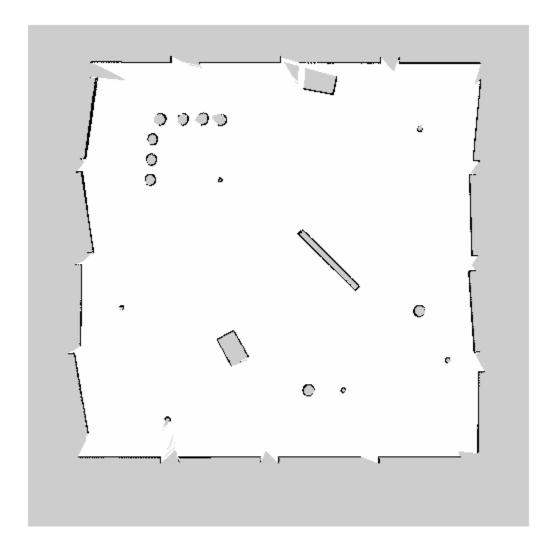
ans = 0.8448

Convert PGM Image to Map

Convert a portable graymap (PGM) file containing a ROS map into an occupancyMap for use in MATLAB.

Import the image using imread. Crop the image to the playpen area.

```
image = imread('playpen_map.pgm');
imageCropped = image(750:1250,750:1250);
imshow(imageCropped)
```

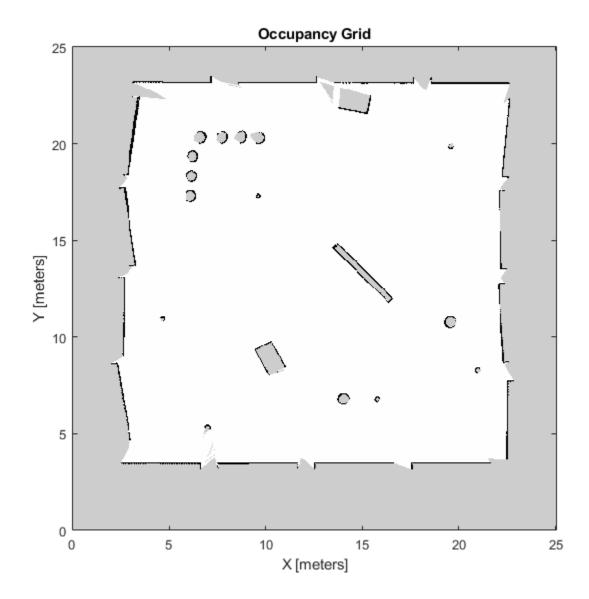


PGM values are expressed from 0 to 255 as uint8. Normalize these values by converting the cropped image to double and dividing each cell by 255. This image shows obstacles as values close to 0. Subtract the normalized image from 1 to get occupancy values with 1 representing occupied space.

```
imageNorm = double(imageCropped)/255;
imageOccupancy = 1 - imageNorm;
```

Create the occupancyMap object using an adjusted map image. The imported map resolution is 20 cells per meter.

```
map = occupancyMap(imageOccupancy,20);
show(map)
```



Limitations

Occupancy values have a limited resolution of ± 0.001 . The values are stored as int16 using a logodds representation. This data type limits resolution, but saves memory when storing large maps in MATLAB. When calling setOccupancy and then getOccupancy, the value returned might not equal the value you set. For more information, see the log-odds representations section in "Occupancy Grids".

If memory size is a limitation, consider using binaryOccupancyMap instead. The binary occupancy map uses less memory with binary values, but still works with Navigation Toolbox $^{\text{\tiny TM}}$ algorithms and other applications.

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

binaryOccupancyMap | controllerPurePursuit | mobileRobotPRM | readOccupancyGrid | writeOccupancyGrid

Topics

"Create Egocentric Occupancy Maps Using Range Sensors"

"Build Occupancy Map from Lidar Scans and Poses"
"Occupancy Grids"

checkOccupancy

Check locations for free, occupied, or unknown values

Syntax

```
i0ccval = checkOccupancy(map,xy)
i0ccval = checkOccupancy(map,xy,'local')
i0ccval = checkOccupancy(map,ij,'grid')
[i0ccval,validPts] = checkOccupancy(____)

occMatrix = checkOccupancy(map)
occMatrix = checkOccupancy(map,bottomLeft,matSize)
occMatrix = checkOccupancy(map,bottomLeft,matSize,'local')
occMatrix = checkOccupancy(map,topLeft,matSize,'grid')
```

Description

iOccval = checkOccupancy(map,xy) returns an array of occupancy values at the xy locations. Each row is a separate xy location in the grid. Occupancy values can be obstacle free (0), occupied (1), or unknown (-1) based on the OccupiedThreshold and FreeThreshold properties of the map object.

i0ccval = check0ccupancy(map,xy,'local') returns an array of occupancy values at the xy
locations in the local frame. The local frame is based on the LocalOriginInWorld property of the
map.

i0ccval = checkOccupancy(map,ij,'grid') specifies ij grid cell indices instead of xy
locations.

[iOccval,validPts] = checkOccupancy(____) also outputs an n-element vector of logical values indicating whether input coordinates are within the map limits.

occMatrix = checkOccupancy(map) returns a matrix that contains the occupancy status of each location. Obstacle-free cells return 0, occupied cells return 1. Unknown locations, including outside the map, return -1.

occMatrix = checkOccupancy(map,bottomLeft,matSize) returns a matrix of occupancy values by specifying the bottom-left corner location in world coordinates and the matrix size in meters.

occMatrix = checkOccupancy(map,bottomLeft,matSize,'local') returns a matrix of occupancy values by specifying the bottom-left corner location in local coordinates and the matrix size in meters.

occMatrix = checkOccupancy(map,topLeft,matSize,'grid') returns a matrix of occupancy values by specifying the top-left corner location in grid coordinates and the grid size.

Examples

Get Occupancy Values and Check Occupancy Status

Access occupancy values and check their occupancy status based on the occupied and free thresholds of the occupancyMap object.

Create a matrix and populate it with values. Use this matrix to create an occupancy map.

```
p = 0.5*ones(20,20);

p(11:20,11:20) = 0.75*ones(10,10);

map = occupancyMap(p,10);
```

Get the occupancy of different locations and check their occupancy statuses. The occupancy status returns 0 for free space and 1 for occupied space. Unknown values return -1.

```
pocc = get0ccupancy(map,[1.5 1])
pocc = 0.7500

occupied = check0ccupancy(map,[1.5 1])
occupied = 1

pocc2 = get0ccupancy(map,[5 5],'grid')
pocc2 = 0.5000
occupied2 = check0ccupancy(map,[5 5],'grid')
occupied2 = -1
```

Input Arguments

map — Map representation

occupancyMap object

Map representation, specified as a occupancyMap object. This object represents the environment of the vehicle. The object contains a matrix grid with values representing the probability of the occupancy of that cell. Values close to 1 represent a high certainty that the cell contains an obstacle. Values close to 0 represent certainty that the cell is not occupied and obstacle free.

xy — World coordinates

n-by-2 matrix

World coordinates, specified as an n-by-2 matrix of $[x \ y]$ pairs, where n is the number of world coordinates.

Data Types: double

ij - Grid positions

n-by-2 matrix

Grid positions, specified as an n-by-2 matrix of $[i \ j]$ pairs in $[rows \ cols]$ format, where n is the number of grid positions.

Data Types: double

bottomLeft — Location of output matrix in world or local

two-element vector | [xCoord yCoord]

Location of bottom left corner of output matrix in world or local coordinates, specified as a twoelement vector, [xCoord yCoord]. Location is in world or local coordinates based on syntax.

Data Types: double

matSize — Output matrix size

two-element vector | [xLength yLength] | [gridRow gridCol]

Output matrix size, specified as a two-element vector, [xLength yLength], or [gridRow gridCol]. Size is in world, local, or grid coordinates based on syntax.

Data Types: double

topLeft — Location of grid

two-element vector | [iCoord jCoord]

Location of top left corner of grid, specified as a two-element vector, [iCoord jCoord].

Data Types: double

Output Arguments

iOccval — Interpreted occupancy values

n-by-1 column vector

Interpreted occupancy values, returned as an *n*-by-1 column vector equal in length to xy or ij.

Occupancy values can be obstacle free (0), occupied (1), or unknown (-1). These values are determined from the actual probability values and the OccupiedThreshold and FreeThreshold properties of the map object.

validPts — Valid map locations

n-by-1 column vector

Valid map locations, returned as an n-by-1 column vector equal in length to xy or ij. Locations inside the map return a value of 1. Locations outside the map limits return a value of 0.

occMatrix — Matrix of occupancy values

matrix

Matrix of occupancy values, returned as matrix with size equal to matSize or the size of your map. Occupancy values can be obstacle free (0), occupied (1), or unknown (-1).

See Also

binaryOccupancyMap | getOccupancy | occupancyMap

copy

Create copy of occupancy grid

Syntax

```
copyMap = copy(map)
```

Description

copyMap = copy(map) creates a deep copy of the occupancyMap object with the same properties.

Examples

Copy Occupancy Grid Map

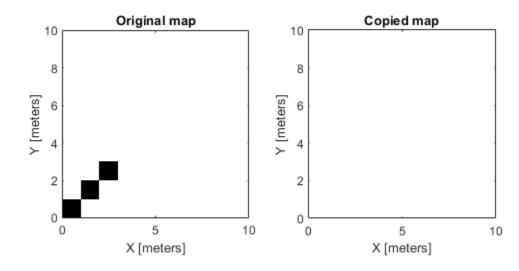
Copy an occupancy grid map object. Once copied, the original object can be modified without affecting the copied map.

Create an occupancy grid with zeros for an empty map.

```
p = zeros(10);
map = occupancyMap(p);
```

Copy the occupancy grid map. Modify the original map. The copied map is not modified. Plot the two maps side by side.

```
mapCopy = copy(map);
setOccupancy(map,[1:3;1:3]',ones(3,1));
subplot(1,2,1)
show(map)
title('Original map')
subplot(1,2,2)
show(mapCopy)
title('Copied map')
```



Input Arguments

map — Map representation

occupancyMap object

Map representation, specified as a occupancyMap object. This object represents the environment of the vehicle. The object contains a matrix grid with values representing the probability of the occupancy of that cell. Values close to 1 represent a high probability that the cell contains an obstacle. Values close to 0 represent a high probability that the cell is not occupied and obstacle free.

Output Arguments

copyMap — Copied map representation

occupancyMap object

Map representation, specified as a occupancyMap object. The properties are the same as the input object, map, but the copy has a different object handle.

See Also

binaryOccupancyMap | getOccupancy | occupancyMap | occupancyMatrix

Topics

"Occupancy Grids"

getOccupancy

Get occupancy value of locations

Syntax

```
occVal = get0ccupancy(map,xy)
occVal = get0ccupancy(map,xy,'local')
occVal = get0ccupancy(map,ij,'grid')
[occVal,validPts] = get0ccupancy(____)

occMatrix = get0ccupancy(map)
occMatrix = get0ccupancy(map,bottomLeft,matSize)
occMatrix = get0ccupancy(map,bottomLeft,matSize,'local')
occMatrix = get0ccupancy(map,topLeft,matSize,'grid')
```

Description

occVal = getOccupancy(map,xy) returns an array of probability occupancy values at the xy locations in the world frame. Values close to 1 represent a high probability that the cell contains an obstacle. Values close to 0 represent a high probability that the cell is not occupied and obstacle free. Unknown locations, including outside the map, return map.DefaultValue.

occVal = getOccupancy(map,xy,'local') returns an array of occupancy values at the xy
locations in the local frame.

```
occVal = getOccupancy(map,ij,'grid') specifies ij grid cell indices instead of xy locations.
```

[occVal,validPts] = getOccupancy(____) additionally outputs an n-element vector of logical values indicating whether input coordinates are within the map limits.

occMatrix = getOccupancy(map) returns all occupancy values in the map as a matrix.

occMatrix = getOccupancy(map,bottomLeft,matSize) returns a matrix of occupancy values by specifying the bottom-left corner location in world coordinates and the matrix size in meters.

occMatrix = getOccupancy(map,bottomLeft,matSize,'local') returns a matrix of occupancy values by specifying the bottom-left corner location in local coordinates and the matrix size in meters.

occMatrix = getOccupancy(map,topLeft,matSize,'grid') returns a matrix of occupancy values by specifying the top-left corner location in grid indices and the matrix size.

Examples

Insert Laser Scans into Occupancy Map

```
Create an empty occupancy grid map.
```

```
map = occupancyMap(10, 10, 20);
```

Input pose of the vehicle, ranges, angles, and the maximum range of the laser scan.

```
pose = [5,5,0];
ranges = 3*ones(100,1);
angles = linspace(-pi/2,pi/2,100);
maxrange = 20;
```

Create a lidarScan object with the specified ranges and angles.

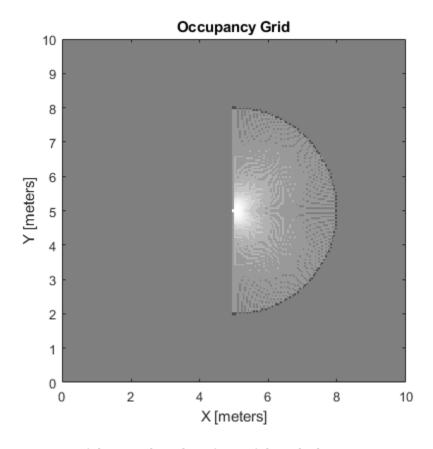
```
scan = lidarScan(ranges,angles);
```

Insert the laser scan data into the occupancy map.

```
insertRay(map,pose,scan,maxrange);
```

Show the map to see the results of inserting the laser scan.

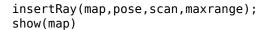
show(map)

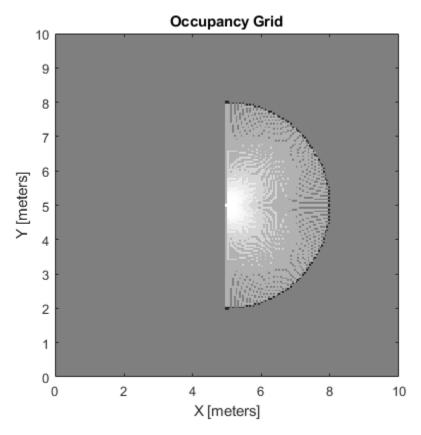


Check the occupancy of the spot directly in front of the vehicle.

```
get0ccupancy(map,[8 5])
ans = 0.7000
```

Add a second reading and view the update to the occupancy values. The additional reading increases the confidence in the readings. The free and occupied values become more distinct.





getOccupancy(map,[8 5])

ans = 0.8448

Get Occupancy Values and Check Occupancy Status

Access occupancy values and check their occupancy status based on the occupied and free thresholds of the occupancyMap object.

Create a matrix and populate it with values. Use this matrix to create an occupancy map.

```
p = 0.5*ones(20,20);

p(11:20,11:20) = 0.75*ones(10,10);

map = occupancyMap(p,10);
```

Get the occupancy of different locations and check their occupancy statuses. The occupancy status returns 0 for free space and 1 for occupied space. Unknown values return -1.

```
pocc = get0ccupancy(map,[1.5 1])
pocc = 0.7500
occupied = check0ccupancy(map,[1.5 1])
```

```
occupied = 1

pocc2 = get0ccupancy(map,[5 5],'grid')

pocc2 = 0.5000

occupied2 = check0ccupancy(map,[5 5],'grid')
occupied2 = -1
```

Input Arguments

map — Map representation

occupancyMap object

Map representation, specified as a occupancyMap object. This object represents the environment of the vehicle. The object contains a matrix grid with values representing the probability of the occupancy of that cell. Values close to 1 represent a high probability that the cell contains an obstacle. Values close to 0 represent a high probability that the cell is not occupied and obstacle free.

xy — World coordinates

n-by-2 matrix

World coordinates, specified as an n-by-2 matrix of $[x \ y]$ pairs, where n is the number of world coordinates.

Data Types: double

ij — Grid positions

n-by-2 matrix

Grid positions, specified as an n-by-2 matrix of $[i \ j]$ pairs in $[rows \ cols]$ format, where n is the number of grid positions.

Data Types: double

bottomLeft — Location of output matrix in world or local

two-element vector | [xCoord yCoord]

Location of bottom left corner of output matrix in world or local coordinates, specified as a twoelement vector, [xCoord yCoord]. Location is in world or local coordinates based on syntax.

Data Types: double

matSize — Output matrix size

two-element vector | [xLength yLength] | [gridRow gridCol]

Output matrix size, specified as a two-element vector, [xLength yLength] or [gridRow gridCol]. Size is in world, local, or grid coordinates based on syntax.

Data Types: double

topLeft — Location of grid

two-element vector | [iCoord jCoord]

Location of top left corner of grid, specified as a two-element vector, [iCoord jCoord].

Data Types: double

Output Arguments

occVal — Probability occupancy values

column vector

Probability occupancy values, returned as a column vector the same length as either xy or ij.

Values close to 0 represent a high probability that the cell is not occupied and obstacle free.

validPts — Valid map locations

n-by-1 column vector

Valid map locations, returned as an n-by-1 column vector equal in length to xy or ij. Locations inside the map return a value of 1. Locations outside the map limits return a value of 0.

occMatrix — Matrix of occupancy values

matrix

Matrix of occupancy values, returned as matrix with size equal to matSize or the size of map.

Values close to 0 represent a high probability that the cell is not occupied and obstacle free.

Limitations

Occupancy values have a limited resolution of ± 0.001 . The values are stored as int16 using a logodds representation. This data type limits resolution, but saves memory when storing large maps in MATLAB. When calling setOccupancy and then getOccupancy, the value returned might not equal the value you set. For more information, see the log-odds representations section in "Occupancy Grids".

See Also

checkOccupancy | occupancyMap

Topics

"Occupancy Grids" (Robotics System Toolbox)

grid2local

Convert grid indices to local coordinates

Syntax

xy = grid2local(map,ij)

Description

xy = grid2local(map,ij) converts a [row col] array of grid indices, ij, to an array of local
coordinates, xy.

Input Arguments

map — Map representation

occupancyMap object | mapLayer object | multiLayerMap object

Map representation, specified as a occupancyMap, mapLayer, or multiLayerMap object.

ij - Grid positions

n-by-2 vertical array

Grid positions, specified as an n-by-2 vertical array of [i j] pairs in [rows cols] format, where n is the number of grid positions.

Output Arguments

xy — Local coordinates

n-by-2 vertical array

Local coordinates, specified as an n-by-2 vertical array of $[x \ y]$ pairs, where n is the number of local coordinates

See Also

grid2world|occupancyMap

grid2world

Convert grid indices to world coordinates

Syntax

xy = grid2world(map,ij)

Description

xy = grid2world(map,ij) converts a [row col] array of grid indices, ij, to an array of world
coordinates, xy.

Input Arguments

map — Map representation

occupancyMap object | mapLayer object | multiLayerMap object

Map representation, specified as a occupancyMap, mapLayer, or multiLayerMap object.

ij - Grid positions

n-by-2 matrix

Grid positions, specified as an n-by-2 matrix of $[i \ j]$ pairs in $[rows \ cols]$ format, where n is the number of grid positions. The grid cell locations are counted from the top left corner of the grid.

Data Types: double

Output Arguments

xy — World coordinates

n-by-2 matrix

World coordinates, returned as an n-by-2 matrix of $[x \ y]$ pairs, where n is the number of world coordinates.

Data Types: double

See Also

binaryOccupancyMap | grid2local | occupancyMap | world2grid

Topics

"Occupancy Grids"

inflate

Inflate each occupied grid location

Syntax

```
inflate(map, radius)
inflate(map, gridradius, 'grid')
```

Description

inflate(map, radius) inflates each occupied position of the specified map by the radius, specified in meters. Occupied location values are based on the map.OccupiedThreshold property. radius is rounded up to the nearest equivalent cell based on the resolution of the map. Values are modified using grayscale inflation to inflate higher probability values across the grid. This inflation increases the size of the occupied locations in the map.

inflate(map,gridradius,'grid') inflates each occupied position by the gridradius, specified
in number of cells.

Examples

Create and Modify Occupancy Map

Create an empty map of 10-by-10 meters in size.

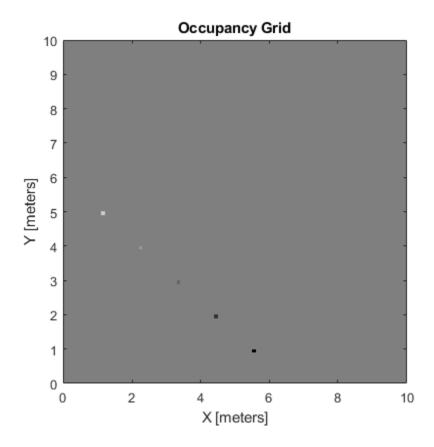
```
map = occupancyMap(10,10,10);
```

Update the occupancy of specific world locations with new probability values and display the map.

```
x = [1.2; 2.3; 3.4; 4.5; 5.6];
y = [5.0; 4.0; 3.0; 2.0; 1.0];

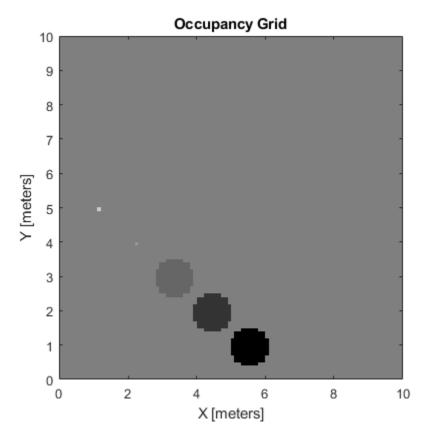
pvalues = [0.2; 0.4; 0.6; 0.8; 1];

updateOccupancy(map,[x y],pvalues)
figure
show(map)
```



Inflate the occupied areas by a radius of $0.5\ m$. The larger occupancy values overwrite the smaller values.

inflate(map,0.5)
figure
show(map)

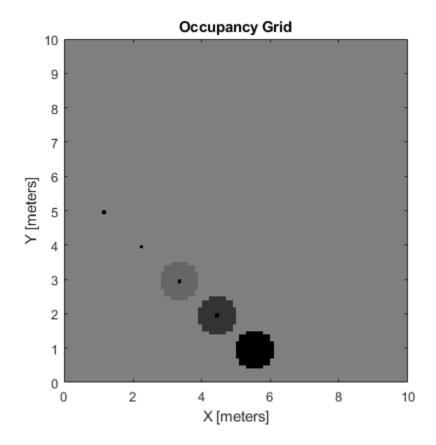


Get the grid locations from the world locations.

```
ij = world2grid(map,[x y]);
```

Set occupancy values for the grid locations.

```
setOccupancy(map,ij,ones(5,1),'grid')
figure
show(map)
```



Input Arguments

map — Map representation

occupancyMap object

Map representation, specified as a occupancyMap object. This object represents the environment of the vehicle. The object contains a matrix grid with values representing the probability of the occupancy of that cell. Values close to 1 represent a high probability that the cell contains an obstacle. Values close to 0 represent a high probability that the cell is not occupied and obstacle free.

radius — Dimension that defines by how much to inflate occupied locations scalar

Dimension that defines by how much to inflate occupied locations, specified as a scalar in meters. radius is rounded up to the nearest equivalent cell value.

Data Types: double

gridradius — Number of cells by which to inflate the occupied locations positive integer scalar

Number of cells by which to inflate the occupied locations, specified as a positive integer scalar.

Data Types: double

More About

Grayscale Inflation

In *grayscale inflation*, the strel function creates a circular structuring element using the inflation radius. The grayscale inflation of A(x, y) by B(x, y) is defined as:

$$(A \oplus B)(x, y) = \max \{A(x - x', y' - y') + B(x', y') \mid (x', y') \in D_B\}.$$

 D_B is the domain of the probability values in the structuring element B. A(x,y) is assumed to be $+\infty$ outside the domain of the grid.

Grayscale inflation acts as a local maximum operator and finds the highest probability values for nearby cells. The inflate method uses this definition to inflate the higher probability values throughout the grid. This inflation increases the size of any occupied locations and creates a buffer zone for vehicles to use as they navigate.

See Also

binaryOccupancyMap | getOccupancy | occupancyMap

Topics

"Occupancy Grids"

insertRay

Insert ray from laser scan observation

Syntax

```
insertRay(map,pose,scan,maxrange)
insertRay(map,pose,ranges,angles,maxrange)
insertRay(map,startpt,endpoints)
insertRay(____,invModel)
```

Description

insertRay(map,pose,scan,maxrange) inserts one or more lidar scan sensor observations in the occupancy grid, map, using the input lidarScan object, scan, to get ray endpoints. The ray endpoints are considered free space if the input scan ranges are below maxrange. Cells observed as occupied are updated with an observation of 0.7. All other points along the ray are treated as obstacle free and updated with an observation of 0.4. Endpoints above maxrange are not updated. NaN values are ignored. This behavior correlates to the inverse sensor model.

insertRay(map,pose,ranges,angles,maxrange) specifies the range readings as vectors defined by the input ranges and angles.

insertRay(map, startpt, endpoints) inserts observations between the line segments from the start point to the end points. The endpoints are updated with a probability observation of 0.7. Cells along the line segments are updated with an observation of 0.4.

insertRay(____, invModel) inserts rays with updated probabilities given in the two-element
vector, invModel, that corresponds to obstacle-free and occupied observations. Use any of the
previous syntaxes to input the rays.

Examples

Insert Laser Scans into Occupancy Map

Create an empty occupancy grid map.

```
map = occupancyMap(10, 10, 20);
```

Input pose of the vehicle, ranges, angles, and the maximum range of the laser scan.

```
pose = [5,5,0];
ranges = 3*ones(100,1);
angles = linspace(-pi/2,pi/2,100);
maxrange = 20;
```

Create a lidarScan object with the specified ranges and angles.

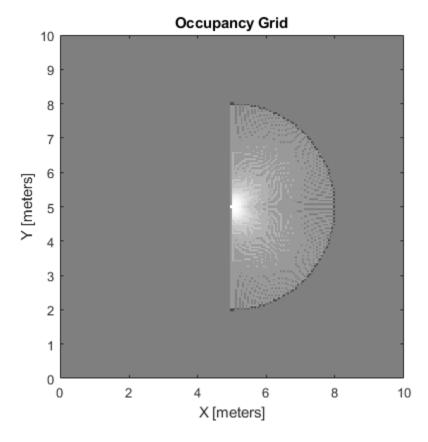
```
scan = lidarScan(ranges,angles);
```

Insert the laser scan data into the occupancy map.

insertRay(map,pose,scan,maxrange);

Show the map to see the results of inserting the laser scan.

show(map)



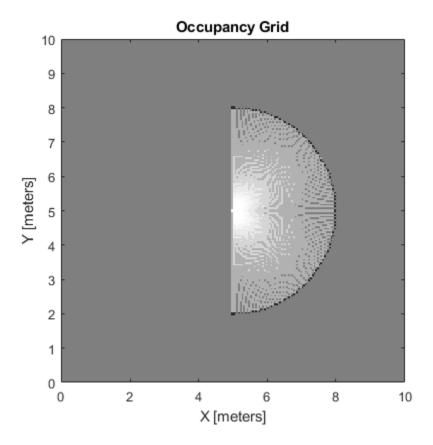
Check the occupancy of the spot directly in front of the vehicle.

getOccupancy(map,[8 5])

ans = 0.7000

Add a second reading and view the update to the occupancy values. The additional reading increases the confidence in the readings. The free and occupied values become more distinct.

insertRay(map,pose,scan,maxrange);
show(map)



getOccupancy(map,[8 5])

ans = 0.8448

Input Arguments

map — Map representation

occupancyMap object

Map representation, specified as a occupancyMap object. This object represents the environment of the vehicle. The object contains a matrix grid with values representing the probability of the occupancy of that cell. Values close to 1 represent a high probability that the cell contains an obstacle. Values close to 0 represent a high probability that the cell is not occupied and obstacle free.

pose — Position and orientation of vehicle

three-element vector

Position and orientation of vehicle, specified as an $[x \ y \ theta]$ vector. The vehicle pose is an x and y position with angular orientation theta (in radians) measured from the x-axis.

scan — Lidar scan readings

lidarScan object

Lidar scan readings, specified as a lidarScan object.

ranges - Range values from scan data

vector

Range values from scan data, specified as a vector of elements measured in meters. These range values are distances from a sensor at given angles. The vector must be the same length as the corresponding angles vector.

angles - Angle values from scan data

vector

Angle values from scan data, specified as a vector of elements measured in radians. These angle values correspond to the given ranges. The vector must be the same length as the corresponding ranges vector.

maxrange — Maximum range of sensor

scalar

Maximum range of laser range sensor, specified as a scalar in meters. Range values greater than or equal to maxrange are considered free along the whole length of the ray, up to maxrange.

startpt — Start point for rays

two-element vector

Start point for rays, specified as a two-element vector, $[x \ y]$, in the world coordinate frame. All rays are line segments that originate at this point.

endpoints — Endpoints for rays

n-by-2 matrix

Endpoints for rays, specified as an n-by-2 matrix of $[x \ y]$ pairs in the world coordinate frame, where n is the length of ranges or angles. All rays are line segments that originate at startpt.

invModel — Inverse sensor model values

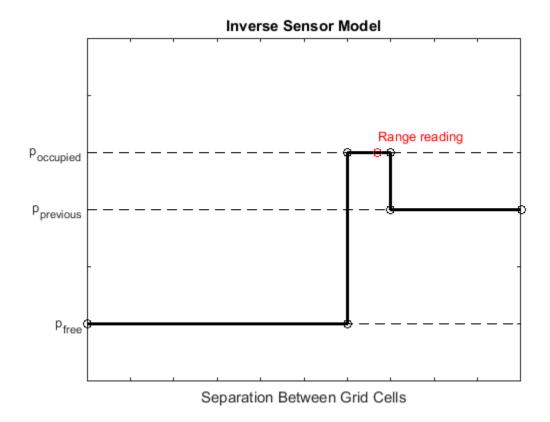
two-element vector

Inverse sensor model values, specified as a two-element vector corresponding to obstacle-free and occupied probabilities. Points along the ray are updated according to the inverse sensor model and the specified range readings. NaN range values are ignored. Range values greater than maxrange are not updated. See "Inverse Sensor Model" on page 2-705.

More About

Inverse Sensor Model

The inverse sensor model determines how values are set along a ray from a range sensor reading to the obstacles in the map. You can customize this model by specifying different probabilities for free and occupied locations in the <code>invModel</code> argument. NaN range values are ignored. Range values greater than <code>maxrange</code> are not updated.



Grid locations that contain range readings are updated with the occupied probability. Locations before the reading are updated with the free probability. All locations after the reading are not updated.

See Also

binaryOccupancyMap|lidarScan|occupancyMap|raycast

Topics

"Occupancy Grids"

local2grid

Convert local coordinates to grid indices

Syntax

ij = local2grid(map,xy)

Description

ij = local2grid(map,xy) converts an array of local coordinates, xy, to an array of grid indices,
ij in [row col] format.

Input Arguments

map — Map representation

occupancyMap object | mapLayer object | multiLayerMap object

Map representation, specified as a occupancyMap, mapLayer, or multiLayerMap object.

xy — Local coordinates

n-by-2 matrix

Local coordinates, specified as an n-by-2 matrix of $[x \ y]$ pairs, where n is the number of local coordinates.

Output Arguments

ij — Grid positions

n-by-2 matrix

Grid positions, returned as an n-by-2 matrix of $[i \ j]$ pairs in $[row \ col]$ format, where n is the number of grid positions. The grid cell locations start at (1,1) and are counted from the top left corner of the grid.

See Also

binaryOccupancyMap | grid2world | occupancyMap

Topics

"Occupancy Grids"

local2world

Convert local coordinates to world coordinates

Syntax

xyWorld = local2world(map,xy)

Description

xyWorld = local2world(map,xy) converts an array of local coordinates to world coordinates

Input Arguments

map — Map representation

occupancyMap object | mapLayer object | multiLayerMap object

Map representation, specified as a occupancyMap, mapLayer, or multiLayerMap object.

xy — Local coordinates

n-by-2 matrix

Local coordinates, specified as an n-by-2 matrix of $[x \ y]$ pairs, where n is the number of world coordinates.

Data Types: double

Output Arguments

xyWorld — World coordinates

n-by-2 matrix

World coordinates, specified as an n-by-2 matrix of $[x \ y]$ pairs, where n is the number of world coordinates.

Data Types: double

See Also

grid2world|occupancyMap|world2local

Topics

"Occupancy Grids"

move

Move map in world frame

Syntax

```
move(map, moveValue)
move(map, moveValue, Name, Value)
```

Description

move(map, moveValue) moves the local origin of the map to an absolute location, moveValue, in the world frame, and updates the map limits. Move values are truncated based on the resolution of the map. By default, newly revealed regions are set to map.DefaultValue.

move(map, moveValue, Name, Value) specifies additional options specified by one or more name-value pair arguments.

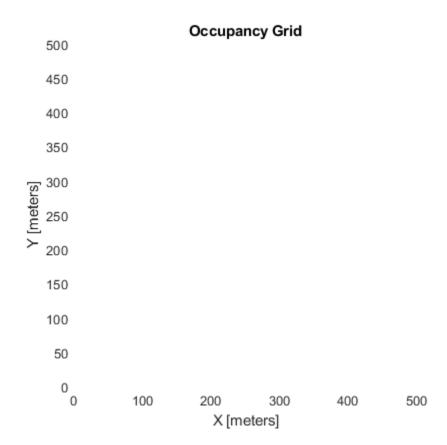
Examples

Move Local Map and Sync with World Map

This example shows how to move a local egocentric map and sync it with a larger world map. This process emulates a vehicle driving in an environment and getting updates on obstacles in the new areas.

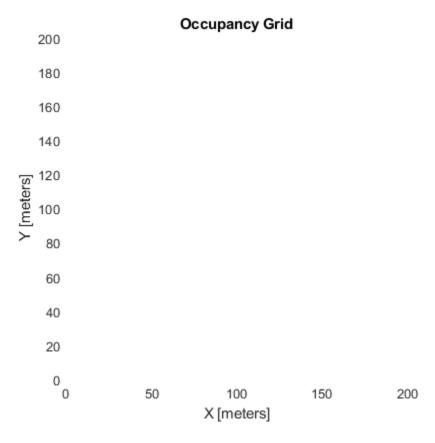
Load example maps. Create an occupancy map from the ternaryMap.

```
load exampleMaps.mat
map = occupancyMap(ternaryMap);
show(map)
```



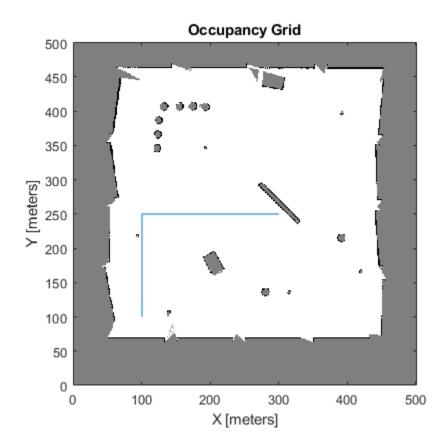
Create a smaller local map.

```
mapLocal = occupancyMap(ternaryMap(end-200:end,1:200));
show(mapLocal)
```

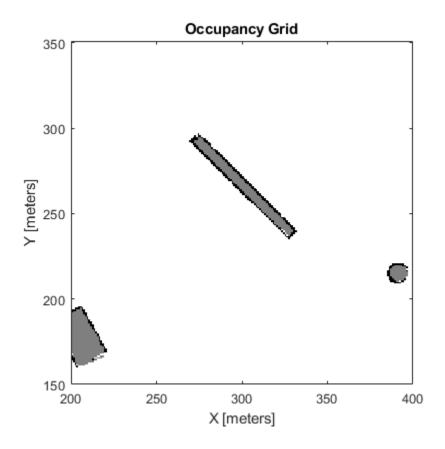


Follow a path planned in the world map and update the local map as you move your local frame.

Specify path locations and plot on the map.



Create a loop for moving between points by the map resolution. Divide the difference between points by the map resolution to see how many incremental moves you can make.



Input Arguments

map — Map representation

occupancyMap object | mapLayer object | multiLayerMap object

Map representation, specified as a occupancyMap, mapLayer, or multiLayerMap object.

moveValue — Local map origin move value

[x y] vector

Local map origin move value, specified as an $[x \ y]$ vector. By default, the value is an absolute location to move the local origin to in the world frame. Use the MoveType name-value pair to specify a relative move.

Name-Value Pair Arguments

Specify optional comma-separated pairs of Name, Value arguments. Name is the argument name and Value is the corresponding value. Name must appear inside quotes. You can specify several name and value pair arguments in any order as Name1, Value1, . . . , NameN, ValueN.

Example: 'MoveType', 'relative'

MoveType — Type of move

'absolute' (default) | 'relative'

Type of move, specified as 'absolute' or 'relative'. For relative moves, specify a relative [x y] vector for moveValue based on your current local frame.

FillValue — Fill value for revealed locations

0 (default) | 1

Fill value for revealed locations because of the shifted map limits, specified as 0 or 1.

SyncWith — Secondary map to sync with

occupancyMap object

Secondary map to sync with, specified as a occupancyMap object. Any revealed locations based on the move are updated with values in this map using the world coordinates.

See Also

Objects

binaryOccupancyMap|mapLayer|multiLayerMap|occupancyMap

Functions

occupancyMatrix

occupancyMatrix

Convert occupancy grid to double matrix

Syntax

```
mat = occupancyMatrix(map)
mat = occupancyMatrix(map, 'ternary')
```

Description

mat = occupancyMatrix(map) returns probability values stored in the occupancy grid object as a
matrix.

mat = occupancyMatrix(map, 'ternary') returns the occupancy status of each grid cell as a matrix. The OccupiedThreshold and FreeThreshold properties on the occupancy grid determine the obstacle free cells (0) and occupied cells (1). Unknown values are returned as -1.

Input Arguments

map — Map representation

occupancyMap object

Map representation, specified as a occupancyMap object. This object represents the environment of the vehicle. The object contains a matrix grid with values representing the probability of the occupancy of that cell. Values close to 1 represent a high probability that the cell contains an obstacle. Values close to 0 represent a high probability that the cell is not occupied and obstacle free.

Output Arguments

mat — Occupancy grid values

matrix

Occupancy grid values, returned as an h-by-w matrix, where h and w are defined by the two elements of the GridSize property of the occupancy grid object.

Data Types: double

See Also

binaryOccupancyMap | getOccupancy | occupancyMap | show

Topics

"Occupancy Grids"

raycast

Compute cell indices along a ray

Syntax

```
[endpoints,midpoints] = raycast(map,pose,range,angle)
[endpoints,midpoints] = raycast(map,p1,p2)
```

Description

[endpoints, midpoints] = raycast(map, pose, range, angle) returns cell indices of the specified map for all cells traversed by a ray originating from the specified pose at the specified angle and range values. endpoints contains all indices touched by the end of the ray, with all other points included in midpoints.

[endpoints, midpoints] = raycast(map,p1,p2) returns the cell indices of the line segment between the two specified points.

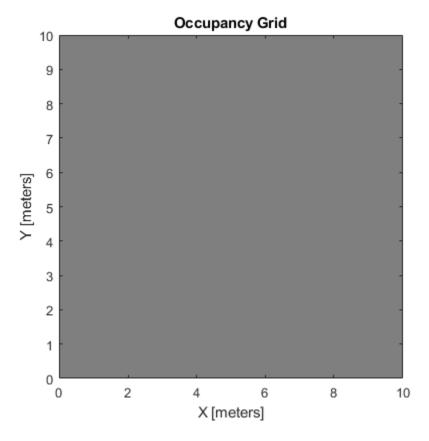
Examples

Get Grid Cells Along A Ray

Use the raycast method to generate cell indices for all cells traversed by a ray.

Create an empty map. A low-resolution map is used to illustrate the effected grid locations.

```
map = occupancyMap(10,10,1);
show(map)
```

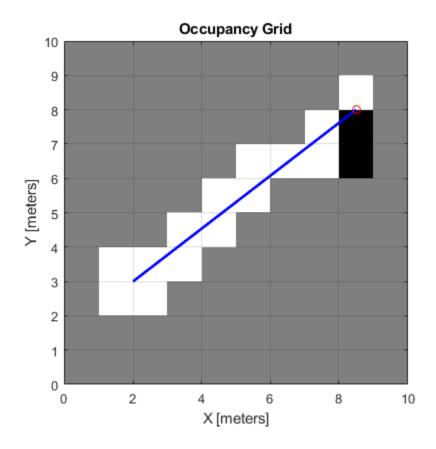


Get the grid indices of the midpoints and end points of a ray from [2 3] to [8.5 8]. Set occupancy values for these grid indices. Midpoints are treated as open space. Update endpoints with an occupied observation.

```
p1 = [2 3];
p2 = [8.5 8];
[endPts,midPts] = raycast(map,p1,p2);
setOccupancy(map,midPts,zeros(length(midPts),1),'grid');
setOccupancy(map,endPts,ones(length(endPts),1),'grid');
```

Plot the original ray over the map. Each grid cell touched by the line is updated. The starting point overlaps multiple cells, and the line touches the edge of certain cells, but all the cells are still updated.

```
show(map)
hold on
plot([p1(1) p2(1)],[p1(2) p2(2)],'-b','LineWidth',2)
plot(p2(1),p2(2),'or')
grid on
```



Input Arguments

map — Map representation

occupancyMap object

Map representation, specified as a occupancyMap object. This object represents the environment of the sensor. The object contains a matrix grid with values representing the probability of the occupancy of that cell. Values close to 1 represent a high probability that the cell contains an obstacle. Values close to 0 represent a high probability that the cell is not occupied and obstacle free.

pose — Position and orientation of sensor

three-element vector

Position and orientation of sensor, specified as an $[x \ y \ theta]$ vector. The sensor pose is an x and y position with angular orientation *theta* (in radians) measured from the x-axis.

range - Range of ray

scalar

Range of ray, specified as a scalar in meters.

angle — Angle of ray

scalar

Angle of ray, specified as a scalar in radians. The angle value is for the corresponding range.

p1 — Starting point of ray

two-element vector

Starting point of ray, specified as an $[x \ y]$ two-element vector. The point is defined in the world frame.

p2 — Endpoint of ray

two-element vector

Endpoint of ray, specified as an $[x \ y]$ two-element vector. The point is defined in the world frame.

Output Arguments

endpoints — Endpoint grid indices

n-by-2 matrix

Endpoint indices, returned as an n-by-2 matrix of $[i \ j]$ pairs, where n is the number of grid indices. The endpoints are where the range value hits at the specified angle. Multiple indices are returned when the endpoint lies on the boundary of multiple cells.

midpoints — Midpoint grid indices

n-by-2 matrix

Midpoint indices, returned as an n-by-2 matrix of $[i \ j]$ pairs, where n is the number of grid indices. This argument includes all grid indices the ray intersects, excluding the endpoint.

See Also

occupancyMap

Topics

"Occupancy Grids"

Introduced in R2019b

rayIntersection

Find intersection points of rays and occupied map cells

Syntax

```
intersectionPts = rayIntersection(map,pose,angles,maxrange)
intersectionPts = rayIntersection(map,pose,angles,maxrange,threshold)
```

Description

intersectionPts = rayIntersection(map,pose,angles,maxrange) returns intersection points of rays and occupied cells in the specified map. Rays emanate from the specified pose and angles. Intersection points are returned in the world coordinate frame. If there is no intersection up to the specified maxrange, [NaN NaN] is returned. By default, the OccupiedThreshold property is used to determine occupied cells.

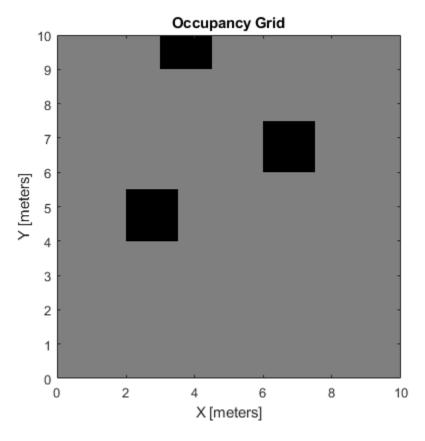
intersectionPts = rayIntersection(map,pose,angles,maxrange,threshold) returns intersection points based on the specified threshold for the occupancy values. Values greater than or equal to the threshold are considered occupied.

Examples

Get Ray Intersection Points on Occupancy Map

Create an occupancy grid map. Add obstacles and inflate them. A lower resolution map is used to illustrate the importance of using grid cells. Show the map.

```
map = occupancyMap(10,10,2);
obstacles = [4 10; 3 5; 7 7];
setOccupancy(map,obstacles,ones(length(obstacles),1))
inflate(map,0.25)
show(map)
```

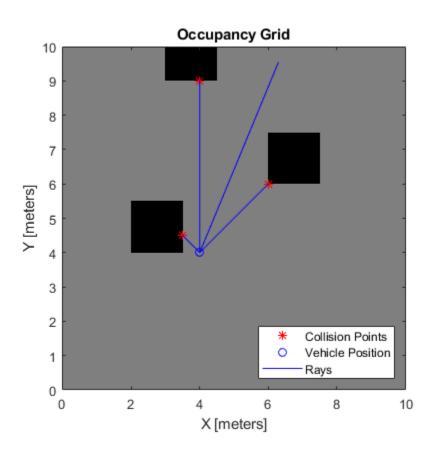


Find the intersection points of occupied cells and rays that emit from the given vehicle pose. Specify the max range and angles for these rays. The last ray does not intersect with an obstacle within the max range, so it has no collision point.

```
maxrange = 6;
angles = [pi/4,-pi/4,0,-pi/8];
vehiclePose = [4,4,pi/2];
intsectionPts = rayIntersection(map,vehiclePose,angles,maxrange,0.7)
intsectionPts = 4×2
    3.5000     4.5000
    6.0000     6.0000
    4.0000     9.0000
    NaN     NaN
```

Plot the intersection points and rays from the pose.

```
hold on
plot(intsectionPts(:,1),intsectionPts(:,2),'*r') % Intersection points
plot(vehiclePose(1),vehiclePose(2),'ob') % Vehicle pose
for i = 1:3
    plot([vehiclePose(1),intsectionPts(i,1)],...
        [vehiclePose(2),intsectionPts(i,2)],'-b') % Plot intersecting rays
end
plot([vehiclePose(1),vehiclePose(1)-6*sin(angles(4))],...
    [vehiclePose(2),vehiclePose(2)+6*cos(angles(4))],'-b') % No intersection ray
```



legend('Collision Points','Vehicle Position','Rays','Location','SouthEast')

Input Arguments

map — Map representation

occupancyMap object

Map representation, specified as a occupancyMap object. This object represents the environment of the sensor. The object contains a matrix grid with values representing the probability of the occupancy of that cell. Values close to 1 represent a high probability that the cell contains an obstacle. Values close to 0 represent a high probability that the cell is not occupied and obstacle free.

pose — Position and orientation of sensor

three-element vector

Position and orientation of sensor, specified as an $[x \ y \ theta]$ vector. The sensor pose is an x and y position with angular orientation *theta* (in radians) measured from the x-axis.

angles — Ray angles emanating from sensor

vector

Ray angles emanating from the sensor, specified as a vector with elements in radians. These angles are relative to the specified sensor pose.

maxrange — Maximum range of sensor

scalar

Maximum range of laser range sensor, specified as a scalar in meters. Range values greater than or equal to maxrange are considered free along the whole length of the ray, up to maxrange.

threshold — Threshold for occupied cells

scalar from 0 to 1

Threshold for occupied cells, specified as a scalar from 0 to 1. Occupancy values greater than or equal to the threshold are treated as occupied cells to trigger intersections.

Output Arguments

intersectionPts — Intersection points

n-by-2 matrix

Intersection points, returned as n-by-2 matrix of $[x \ y]$ pairs in the world frame, where n is the length of angles.

See Also

binaryOccupancyMap | occupancyMap | raycast | updateOccupancy

Topics

"Occupancy Grids"

Introduced in R2019b

setOccupancy

Set occupancy value of locations

Syntax

```
setOccupancy(map,xy,occval)
setOccupancy(map,xy,occval,'local')
setOccupancy(map,ij,occval,'grid')
validPts = setOccupancy(____)
setOccupancy(map,bottomLeft,inputMatrix)
setOccupancy(map,bottomLeft,inputMatrix,'local')
setOccupancy(map,topLeft,inputMatrix,'grid')
```

Description

setOccupancy(map,xy,occval) assigns the occupancy values to each coordinate specified in xy. occval can be a column vector the same size of xy or a scalar, which is applied to all coordinates.

setOccupancy(map,xy,occval,'local') assigns occupancy values, occval, to the input array of local coordinates, xy, as local coordinates.

setOccupancy(map,ij,occval,'grid') assigns occupancy values, occval, to the input array of
grid indices, ij, as [rows cols].

validPts = setOccupancy(____) outputs an n-element vector of logical values indicating
whether input coordinates are within the map limits.

setOccupancy(map,bottomLeft,inputMatrix) assigns a matrix of occupancy values by specifying the bottom-left corner location in world coordinates.

setOccupancy(map,bottomLeft,inputMatrix,'local') assigns a matrix of occupancy values by specifying the bottom-left corner location in local coordinates.

setOccupancy(map,topLeft,inputMatrix,'grid') assigns a matrix of occupancy values by specifying the top-left cell index in grid indices and the matrix size.

Examples

Create and Modify Occupancy Map

Create an empty map of 10-by-10 meters in size.

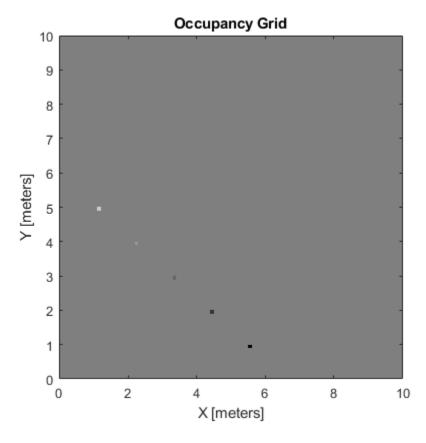
```
map = occupancyMap(10,10,10);
```

Update the occupancy of specific world locations with new probability values and display the map.

```
x = [1.2; 2.3; 3.4; 4.5; 5.6];

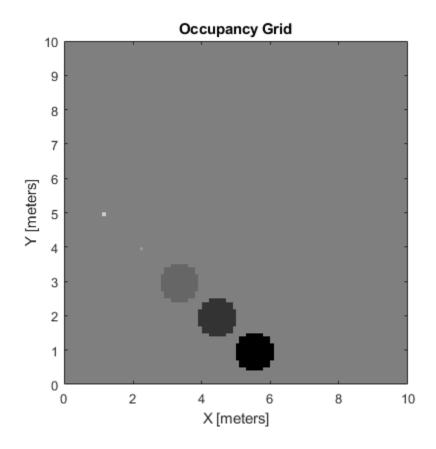
y = [5.0; 4.0; 3.0; 2.0; 1.0];
```

```
pvalues = [0.2; 0.4; 0.6; 0.8; 1];
updateOccupancy(map,[x y],pvalues)
figure
show(map)
```



Inflate the occupied areas by a radius of $0.5\ m$. The larger occupancy values overwrite the smaller values.

inflate(map,0.5)
figure
show(map)

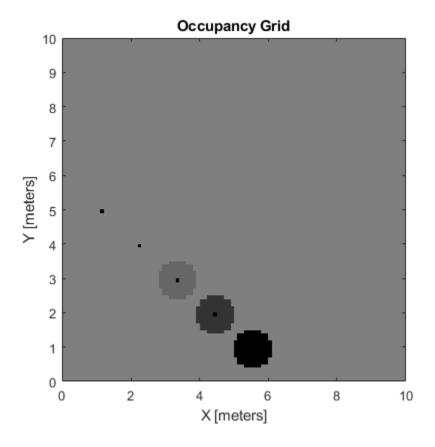


Get the grid locations from the world locations.

```
ij = world2grid(map,[x y]);
```

Set occupancy values for the grid locations.

```
setOccupancy(map,ij,ones(5,1),'grid')
figure
show(map)
```



Input Arguments

map — Map representation

occupancyMap object

Map representation, specified as a occupancyMap object. This object represents the environment of the vehicle. The object contains a matrix grid with values representing the probability of the occupancy of that cell. Values close to 1 represent a high probability that the cell contains an obstacle. Values close to 0 represent a high probability that the cell is not occupied and obstacle free.

xy — World coordinates

n-by-2 matrix

World coordinates, specified as an n-by-2 matrix of $[x \ y]$ pairs, where n is the number of world coordinates.

Data Types: double

ij - Grid positions

n-by-2 matrix

Grid positions, specified as an n-by-2 matrix of $[i \ j]$ pairs in $[rows \ cols]$ format, where n is the number of grid positions.

Data Types: double

occval — Probability occupancy values

scalar | column vector

Probability occupancy values, specified as a scalar or a column vector the same size as either xy or ij. A scalar input is applied to all coordinates in either xy or ij.

Values close to 0 represent a high probability that the cell is not occupied and obstacle free.

inputMatrix — Occupancy values

matrix

Occupancy values, specified as a matrix. Values are given between 0 and 1 inclusively.

bottomLeft — Location of output matrix in world or local

two-element vector | [xCoord yCoord]

Location of bottom left corner of output matrix in world or local coordinates, specified as a twoelement vector, [xCoord yCoord]. Location is in world or local coordinates based on syntax.

Data Types: double

topLeft — Location of grid

two-element vector | [iCoord jCoord]

Location of top left corner of grid, specified as a two-element vector, [iCoord jCoord].

Data Types: double

Output Arguments

validPts — Valid map locations

n-by-1 column vector

Valid map locations, returned as an n-by-1 column vector equal in length to xy or ij. Locations inside the map return a value of 1. Locations outside the map limits return a value of 0.

Limitations

Occupancy values have a limited resolution of ± 0.001 . The values are stored as int16 using a logodds representation. This data type limits resolution, but saves memory when storing large maps in MATLAB. When calling setOccupancy and then getOccupancy, the value returned might not equal the value you set. For more information, see the log-odds representations section in "Occupancy Grids".

See Also

binaryOccupancyMap | getOccupancy | occupancyMap

Topics

"Occupancy Grids"

Introduced in R2019b

show

Show grid values in a figure

Syntax

```
show(map)
show(map,'local')
show(map,'grid')
show(____,Name,Value)
mapImage = show(____)
```

Description

show(map) displays the occupancy grid map in the current axes, with the axes labels representing the world coordinates.

show(map, 'local') displays the occupancy grid map in the current axes, with the axes labels
representing the local coordinates instead of world coordinates.

 ${\sf show(map,'grid')}$ displays the occupancy grid ${\sf map}$ in the current axes, with the axes labels representing the grid coordinates.

show(____, Name, Value) specifies additional options specified by one or more name-value pair arguments.

mapImage = show() returns the handle to the image object created by show.

Examples

Create and Modify Occupancy Map

Create an empty map of 10-by-10 meters in size.

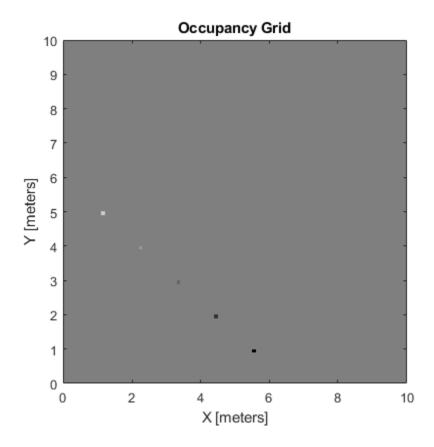
```
map = occupancyMap(10,10,10);
```

Update the occupancy of specific world locations with new probability values and display the map.

```
x = [1.2; 2.3; 3.4; 4.5; 5.6];
y = [5.0; 4.0; 3.0; 2.0; 1.0];

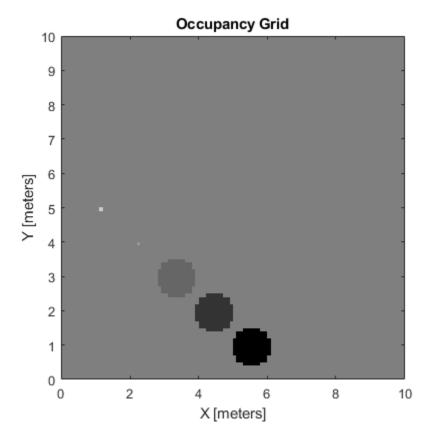
pvalues = [0.2; 0.4; 0.6; 0.8; 1];

updateOccupancy(map,[x y],pvalues)
figure
show(map)
```



Inflate the occupied areas by a radius of $0.5\ m$. The larger occupancy values overwrite the smaller values.

inflate(map,0.5)
figure
show(map)

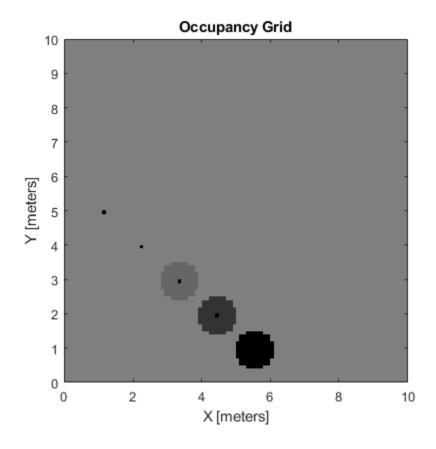


Get the grid locations from the world locations.

```
ij = world2grid(map,[x y]);
```

Set occupancy values for the grid locations.

```
setOccupancy(map,ij,ones(5,1),'grid')
figure
show(map)
```

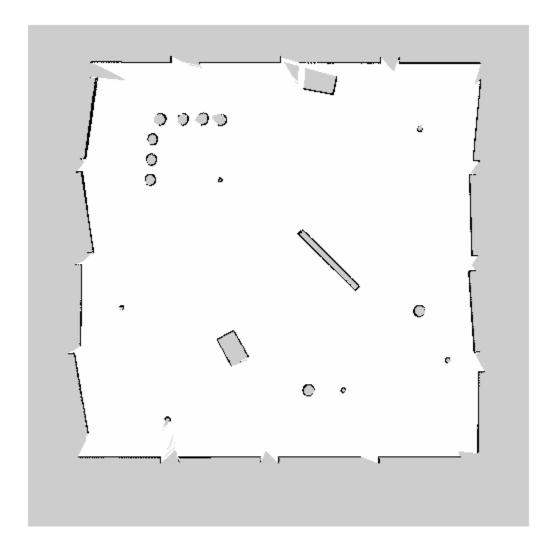


Convert PGM Image to Map

Convert a portable graymap (PGM) file containing a ROS map into an occupancyMap for use in MATLAB.

Import the image using imread. Crop the image to the playpen area.

```
image = imread('playpen_map.pgm');
imageCropped = image(750:1250,750:1250);
imshow(imageCropped)
```

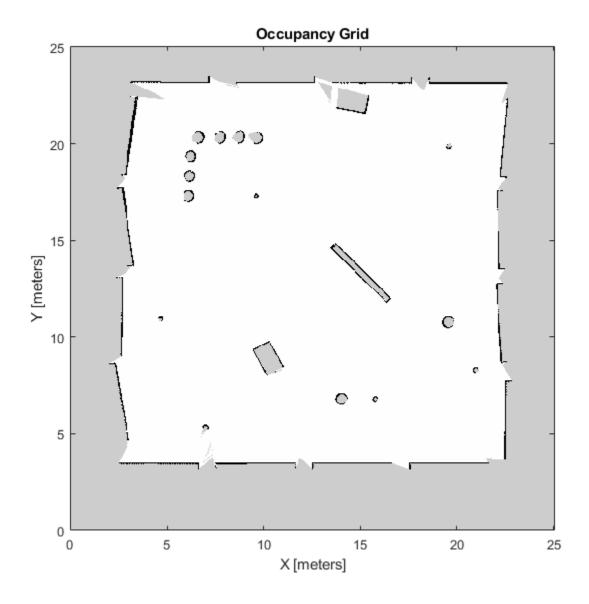


PGM values are expressed from 0 to 255 as uint8. Normalize these values by converting the cropped image to double and dividing each cell by 255. This image shows obstacles as values close to 0. Subtract the normalized image from 1 to get occupancy values with 1 representing occupied space.

```
imageNorm = double(imageCropped)/255;
imageOccupancy = 1 - imageNorm;
```

Create the occupancyMap object using an adjusted map image. The imported map resolution is 20 cells per meter.

```
map = occupancyMap(imageOccupancy,20);
show(map)
```



Input Arguments

map — Map representation

occupancyMap object

Map representation, specified as a occupancyMap object. This object represents the environment of the vehicle. The object contains a matrix grid with values representing the probability of the occupancy of that cell. Values close to 1 represent a high probability that the cell contains an obstacle. Values close to 0 represent a high probability that the cell is not occupied and obstacle free.

Name-Value Pair Arguments

Specify optional comma-separated pairs of Name, Value arguments. Name is the argument name and Value is the corresponding value. Name must appear inside quotes. You can specify several name and value pair arguments in any order as Name1, Value1, . . . , NameN, ValueN.

Example: 'Parent', axHandle

Parent — Axes to plot the map

Axes object | UIAxes object

Axes to plot the map specified as either an Axes or UIAxes object. See axes or uiaxes.

FastUpdate — Update existing map plot

0 (default) | 1

Update existing map plot, specified as 0 or 1. If you previously plotted your map on your figure, set to 1 for a faster update to the figure. This is useful for updating the figure in a loop for fast animations.

Outputs

mapImage — Map image

object handle

Map image, specified as an object handle.

See Also

axes | binaryOccupancyMap | occupancyMap | occupancyMatrix

Introduced in R2019b

syncWith

Sync map with overlapping map

Syntax

```
mat = syncWith(map,sourcemap)
```

Description

mat = syncWith(map, sourcemap) updates map with data from another occupancyMap object, sourcemap. Locations in map that are also found in sourcemap are updated. All other cells in map retain their current values.

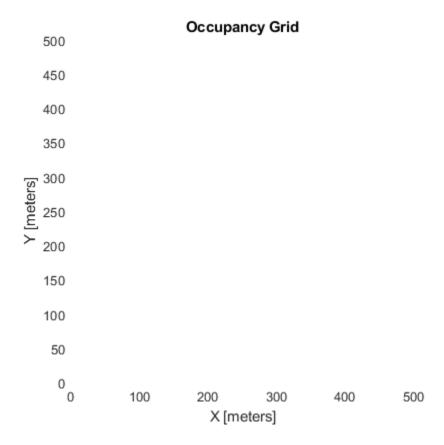
Examples

Move Local Map and Sync with World Map

This example shows how to move a local egocentric map and sync it with a larger world map. This process emulates a vehicle driving in an environment and getting updates on obstacles in the new areas.

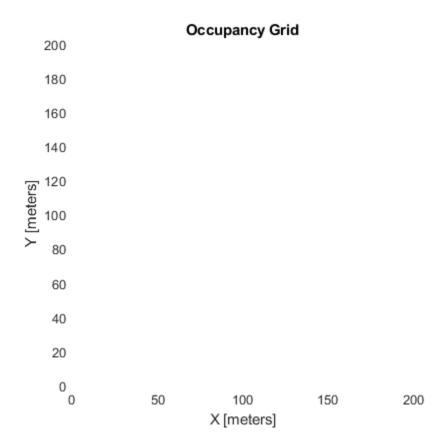
Load example maps. Create an occupancy map from the ternaryMap.

```
load exampleMaps.mat
map = occupancyMap(ternaryMap);
show(map)
```



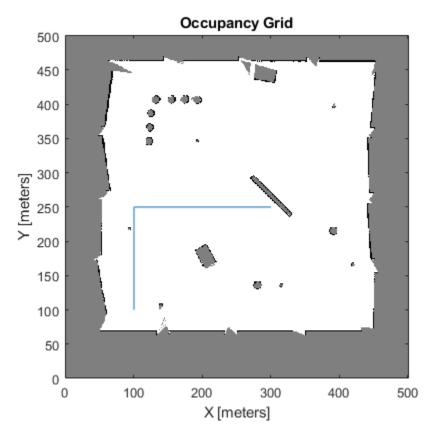
Create a smaller local map.

mapLocal = occupancyMap(ternaryMap(end-200:end,1:200));
show(mapLocal)

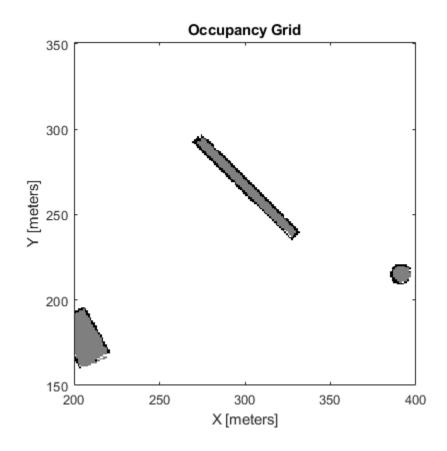


Follow a path planned in the world map and update the local map as you move your local frame.

Specify path locations and plot on the map.



Create a loop for moving between points by the map resolution. Divide the difference between points by the map resolution to see how many incremental moves you can make.



Input Arguments

map — Map representation

occupancyMap object | mapLayer object | multiLayerMap object

Map representation, specified as a occupancyMap, mapLayer, or multiLayerMap object.

sourcemap — Source map data

occupancyMap object | mapLayer object | multiLayerMap object

Source map data, specified as a occupancyMap, mapLayer, or multiLayerMap object.

See Also

binaryOccupancyMap | occupancyMap

Topics

"Occupancy Grids"

Introduced in R2019b

updateOccupancy

Integrate probability observations at locations

Syntax

```
updateOccupancy(map,occMatrix)

updateOccupancy(map,locations,obs)
updateOccupancy(map,xy,obs,'world')
updateOccupancy(map,xy,obs,'local')
updateOccupancy(map,ij,obs,'grid')

updateOccupancy(map,bottomLeft,obsMatrix)
updateOccupancy(map,bottomLeft,obsMatrix,'world')
updateOccupancy(map,bottomLeft,obsMatrix,'local')
updateOccupancy(map,topLeft,obsMatrix,'grid')
```

Description

updateOccupancy(map,occMatrix) probabilistically integrates a matrix of occupancy values, occMatrix, with the current occupancy matrix of the occupancyMap object map. The size of the matrix must be equal to the GridSize property of map.

updateOccupancy (map, locations, obs) probabilistically integrates observation values, obs, into the occupancy map cells corresponding to the n-by-2 matrix of world coordinates locations. Observation values are determined based on the "Inverse Sensor Model" on page 2-746.

updateOccupancy(map,xy,obs,'world') probabilistically integrates observation values, obs, into the cells corresponding to the n-by-2 matrix of world coordinates xy.

updateOccupancy(map,xy,obs,'local') probabilistically integrates observation values, obs, into the cells corresponding to the *n*-by-2 matrix of local coordinates xy.

updateOccupancy(map,ij,obs,'grid') probabilistically integrates observation values, obs, into the cells corresponding to the n-by-2 matrix of grid indices ij.

updateOccupancy(map,bottomLeft,obsMatrix) probabilistically integrates an m-by-n matrix of observation values, obsMatrix, into a subregion in the map. Specify the bottom-left corner of the subregion as a world position, bottomLeft. The subregion extends m rows up and n columns to the right from the specified position.

updateOccupancy(map,bottomLeft,obsMatrix,'world') probabilistically integrates an m-by-n matrix of observation values, obsMatrix, into a subregion in the map. Specify the bottom-left corner of the subregion as a world position, bottomLeft. The subregion extends m rows up and n columns to the right from the specified position.

updateOccupancy(map,bottomLeft,obsMatrix,'local') probabilistically integrates an m-by-n matrix of observation values, obsMatrix, into a subregion in the map. Specify the bottom-left corner of the subregion as a local position, bottomLeft. The subregion extends m rows up and n columns to the right from the specified position.

updateOccupancy(map,topLeft,obsMatrix,'grid') probabilistically integrates an m-by-n matrix of observation values, obsMatrix, into a subregion in the map. Specify the top-left corner of the subregion as a grid index, topLeft. The subregion extends m rows down and n columns to the right from the specified index.

Examples

Create and Modify Occupancy Map

Create an empty map of 10-by-10 meters in size.

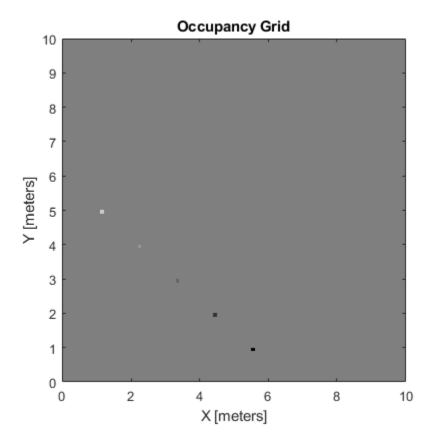
```
map = occupancyMap(10, 10, 10);
```

Update the occupancy of specific world locations with new probability values and display the map.

```
x = [1.2; 2.3; 3.4; 4.5; 5.6];
y = [5.0; 4.0; 3.0; 2.0; 1.0];

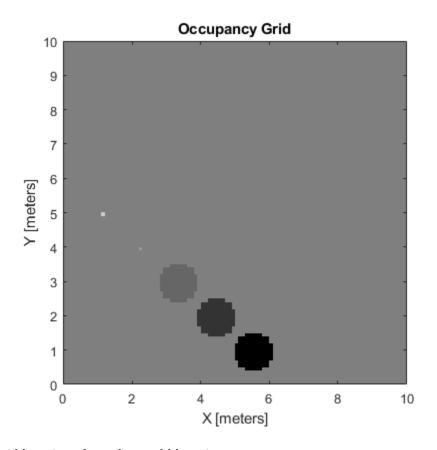
pvalues = [0.2; 0.4; 0.6; 0.8; 1];

updateOccupancy(map,[x y],pvalues)
figure
show(map)
```



Inflate the occupied areas by a radius of $0.5\ m$. The larger occupancy values overwrite the smaller values.

inflate(map,0.5)
figure
show(map)

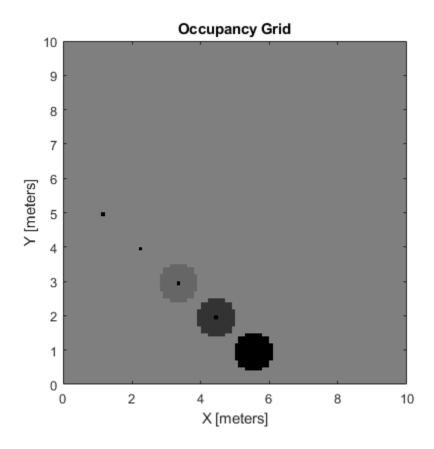


Get the grid locations from the world locations.

```
ij = world2grid(map,[x y]);
```

Set occupancy values for the grid locations.

```
setOccupancy(map,ij,ones(5,1),'grid')
figure
show(map)
```



Input Arguments

map — Map representation

occupancyMap object

Map representation, specified as an occupancyMap object. This object represents the environment of the vehicle. The object contains a matrix grid with each value representing the probability of the occupancy of that cell. Values close to 1 represent a high probability that the cell contains an obstacle. Values close to θ represent a high probability that the cell is not occupied and contains no obstacles.

occMatrix — Matrix of occupancy values

numeric matrix | logical matrix

Matrix of occupancy values, specified as a matrix. The size of the matrix must be equal to the GridSize property of map.

The occupancy values can be of any numeric type, with values between 0 and 1. If the matrix is logical, the default occupancy values of 0.7 (true) and 0.4 (false) are used.

Example: updateOccupancy(map,ones(map.GridSize)*0.6)

Data Types: single | double | logical

locations — Cell locations in world coordinates

n-by-2 matrix

Cell locations in world coordinates, specified as an n-by-2 matrix with rows of the form [x y], where n is the number of world coordinates. The function ignores locations outside of the map boundaries.

```
Example: updateOccupancy(map,[1 1; 3 3; 5 5],false)
```

Data Types: single | double

bottomLeft — Location of bottom-left corner of observation matrix

two-element vector

Location of the bottom-left corner of the observation matrix, specified as a two-element vector of the form [xCoord yCoord]. The location is in world or local coordinates, based on the syntax.

```
Example: updateOccupancy(map, [2 2], [0.2 0.4; 0.6 0.8], 'world')
```

Data Types: single | double

topLeft - Location of top-left corner of grid

two-element vector

Location of the top-left corner of the grid, specified as a two-element vector of form [iCoord jCoord].

```
Example: updateOccupancy(map,[2 2],[0.2 0.4; 0.6 0.8],'grid')
```

Data Types: single | double

xy — World or local coordinates

n-by-2 matrix

World or local coordinates, specified as an n-by-2 matrix with rows of the form $[x \ y]$, where n is the number of coordinates.

```
Example: updateOccupancy(map, [2 2; 4 4; 6 6], [0.2; 0.4; 0.6], 'world')
```

Data Types: single | double

ij — Grid positions

n-by-2 matrix

Grid positions, specified as an n-by-2 matrix with rows of the form $[i \ j]$ in $[rows \ cols]$ format, where n is the number of grid positions.

```
Example: updateOccupancy(map,[2 2; 4 4; 6 6],[0.2; 0.4; 0.6],'grid')
```

Data Types: single | double

obs — Probability observation values

n-element numeric column vector | n-element logical column vector | numeric scalar | logical scalar

Probability observation values, specified as a numeric or logical scalar or a numeric or logical *n*-element column vector the same size as either locations, xy, or ij.

obs values can be any value from 0 to 1, but if obs is a logical vector, the default observation values of 0.7 (true) and 0.4 (false) are used. If obs is a numeric or a logical scalar, the value is applied to all coordinates in locations, xy, or ij. These values correlate to the "Inverse Sensor Model" on page 2-746 for ray casting.

```
Example: updateOccupancy(map,[2 2; 4 4; 6 6],[0.2; 0.4; 0.6],'local')
```

Data Types: single | double | logical

obsMatrix — Matrix of probability observation values

m-by-*n* numeric matrix | *m*-by-*n* logical matrix

Matrix of probability observation values, specified as an *m*-by-*n* numeric or logical matrix.

The observation values can be of any numeric type with value between 0 and 1. If the matrix is logical, the default observation values of 0.7 (true) and 0.4 (false) are used.

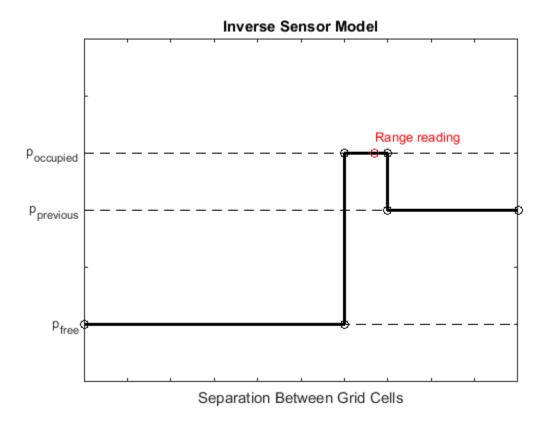
Example: updateOccupancy(map,[2 2],[0.2 0.4; 0.6 0.8])

Data Types: single | double | logical

More About

Inverse Sensor Model

The inverse sensor model determines how values are set along a ray from a range sensor reading to the obstacles in the map. NaN range values are ignored. Range values greater than maxrange are not updated.



Grid locations that contain range readings are updated with the occupied probability. Locations before the reading are updated with the free probability. All locations after the reading are not updated.

See Also

binaryOccupancyMap|occupancyMap|setOccupancy

Topics "Occupancy Grids"

Introduced in R2019b

world2grid

Convert world coordinates to grid indices

Syntax

```
ij = world2grid(map,xy)
```

Description

```
ij = world2grid(map,xy) converts an array of world coordinates, xy, to an array of grid indices,
ij in [row col] format.
```

Examples

Create and Modify Occupancy Map

Create an empty map of 10-by-10 meters in size.

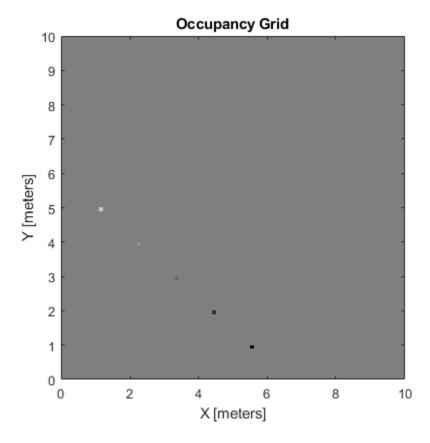
```
map = occupancyMap(10,10,10);
```

Update the occupancy of specific world locations with new probability values and display the map.

```
x = [1.2; 2.3; 3.4; 4.5; 5.6];
y = [5.0; 4.0; 3.0; 2.0; 1.0];

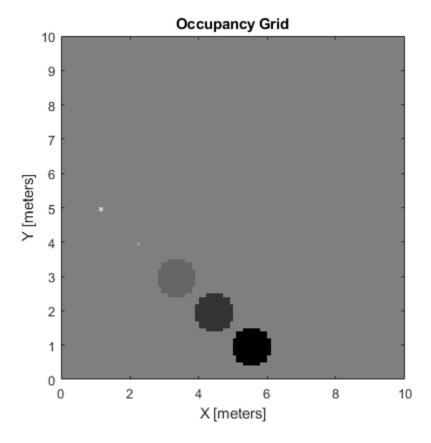
pvalues = [0.2; 0.4; 0.6; 0.8; 1];

updateOccupancy(map,[x y],pvalues)
figure
show(map)
```



Inflate the occupied areas by a radius of $0.5\ m$. The larger occupancy values overwrite the smaller values.

inflate(map,0.5)
figure
show(map)

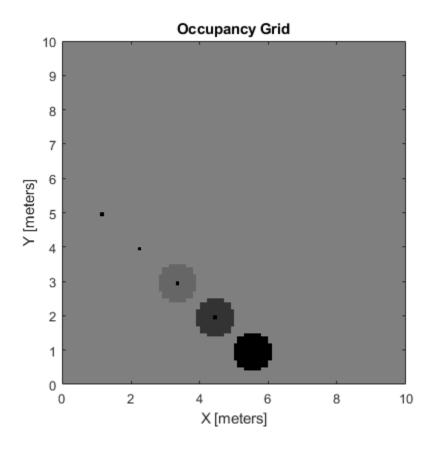


Get the grid locations from the world locations.

```
ij = world2grid(map,[x y]);
```

Set occupancy values for the grid locations.

```
setOccupancy(map,ij,ones(5,1),'grid')
figure
show(map)
```



Input Arguments

map — Map representation

occupancyMap object | mapLayer object | multiLayerMap object

Map representation, specified as a occupancyMap, mapLayer, or multiLayerMap object.

xy — World coordinates

n-by-2 matrix

World coordinates, specified as an n-by-2 matrix of $[x \ y]$ pairs, where n is the number of world coordinates.

Data Types: double

Output Arguments

ij — Grid indices

n-by-2 matrix

Grid indices, returned as an n-by-2 matrix of $[i \ j]$ pairs in $[row \ col]$ format, where n is the number of grid positions. The grid cell locations are counted from the top left corner of the grid.

Data Types: double

See Also

Objects

binaryOccupancyMap | mapLayer | multiLayerMap | occupancyMap

Functions

grid2world

Topics "Occupancy Grids"

Introduced in R2019b

rangeSensor

Simulate range-bearing sensor readings

Description

The rangeSensor System object is a range-bearing sensor that is capable of outputting range and angle measurements based on the given sensor pose and occupancy map. The range-bearing readings are based on the obstacles in the occupancy map.

To simulate a range-bearing sensor using this object:

- **1** Create the rangeSensor object and set its properties.
- **2** Call the object with arguments, as if it were a function.

To learn more about how System objects work, see What Are System Objects?.

Creation

Syntax

```
rbsensor = rangeSensor
rbsensor = rangeSensor(Name, Value)
```

Description

rbsensor = rangeSensor returns a rangeSensor System object, rbsensor. The sensor is capable of outputting range and angle measurements based on the sensor pose and an occupancy map.

rbsensor = rangeSensor(Name, Value) sets properties for the sensor using one or more namevalue pairs. Unspecified properties have default values. Enclose each property name in quotes.

Properties

Unless otherwise indicated, properties are *nontunable*, which means you cannot change their values after calling the object. Objects lock when you call them, and the release function unlocks them.

If a property is *tunable*, you can change its value at any time.

For more information on changing property values, see System Design in MATLAB Using System Objects.

Range — Minimum and maximum detectable range

[0 20] (default) | 1-by-2 positive real-valued vector

The minimum and maximum detectable range, specified as a 1-by-2 positive real-valued vector. Units are in meters.

Example: [1 15]

Tunable: Yes

Data Types: single | double

HorizontalAngle — Minimum and maximum horizontal detection angle

[-pi pi] (default) | 1-by-2 real-valued vector

Minimum and maximum horizontal detection angle, specified as a 1-by-2 real-valued vector. Units are in radians.

Example: [-pi/3 pi/3]
Data Types: single | double

Horizontal Angle Resolution — Resolution of horizontal angle readings

0.0244 (default) | positive scalar

Resolution of horizontal angle readings, specified as a positive scalar. The resolution defines the angular interval between two consecutive sensor readings. Units are in radians.

Example: 0.01

Data Types: single | double

RangeNoise — Standard deviation of range noise

0 (default) | positive scalar

The standard deviation of range noise, specified as a positive scalar. The range noise is modeled as a zero-mean white noise process with the specified standard deviation. Units are in meters.

Example: 0.01

Tunable: Yes

Data Types: single | double

HorizontalAngleNoise — Standard deviation of horizontal angle noise

0 (default) | positive scalar

The standard deviation of horizontal angle noise, specified as a positive scalar. The range noise is modeled as a zero-mean white noise process with the specified standard deviation. Units are in radians.

Example: 0.01

Tunable: Yes

Data Types: single | double

NumReadings — Number of output readings

258 (default) | positive integer

This property is read-only.

Number of output readings for each pose of the sensor, specified as a positive integer. This property depends on the HorizonalAngle and HorizontalAngleResolution properties.

Data Types: single | double

Usage

Syntax

[ranges,angles] = rbsensor(pose,map)

Description

[ranges,angles] = rbsensor(pose,map) returns the range and angle readings from the 2-D pose information and the ground-truth map.

Input Arguments

pose — Pose of sensor in map

N-by-3 real-valued matrix

Poses of the sensor in the 2-D map, specified as an N-by-3 real-valued matrix, where N is the number of poses to simulate the sensor. Each row of the matrix corresponds to a pose of the sensor in the order of $[x, y, \theta]$. x and y represent the position of the sensor in the map frame. The units of x and y are in meters. θ is the heading angle of the sensor with respect to the positive x-direction of the map frame. The units of θ are in radians.

map — Ground-truth map

occupancyMap object | binaryOccupancyMap object

Ground-truth map, specified as an occupancyMap or a binaryOccupancyMap object. For the occupancyMap input, the range-bearing sensor considers a cell as occupied and returns a range reading if the occupancy probability of the cell is greater than the value specified by the OccupiedThreshold property of the occupancy map.

Output Arguments

ranges — Range readings

R-by-*N* real-valued matrix

Range readings, specified as an R-by-N real-valued matrix. N is the number of poses for which the sensor is simulated, and R is the number of sensor readings per pose of the sensor. R is same as the value of the NumReadings property.

angles — Angle readings

R-by-1 real-valued vector

Angle readings, specified as an R-by-1 real-valued vector. R is the number of sensor readings per pose of the sensor. R is same as the value of the NumReadings property.

Object Functions

To use an object function, specify the System object as the first input argument. For example, to release system resources of a System object named obj, use this syntax:

release(obj)

Common to All System Objects

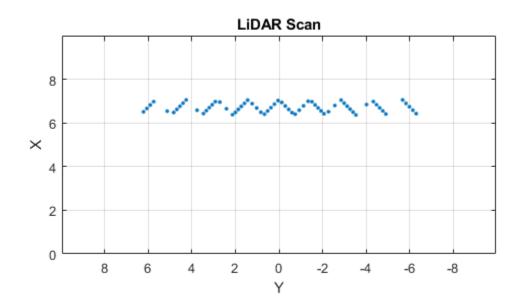
step Run System object algorithm clone Create duplicate System object

Examples

plot(scan)

Obtain Range and Bearing Readings

```
Create a range-bearing sensor.
  rbsensor = rangeSensor;
Specify the pose of the sensor and the ground-truth map.
truePose = [0 0 pi/4];
trueMap = binaryOccupancyMap(eye(10));
Generate the sensor readings.
[ranges, angles] = rbsensor(truePose, trueMap);
Visualize the results using lidarScan.
scan = lidarScan(ranges, angles);
figure
```



Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

Usage notes and limitations:

• See "System Objects in MATLAB Code Generation" (MATLAB Coder).

See Also

binaryOccupancyMap|lidarScan|occupancyMap

world2local

Convert world coordinates to local coordinates

Syntax

xyLocal = world2local(map,xy)

Description

xyLocal = world2local(map,xy) converts an array of world coordinates to local coordinates.

Input Arguments

map — Map representation

occupancyMap object | mapLayer object | multiLayerMap object

Map representation, specified as a occupancyMap, mapLayer, or multiLayerMap object.

xy — World coordinates

n-by-2 vertical array

World coordinates, specified as an n-by-2 vertical array of $[x \ y]$ pairs, where n is the number of world coordinates.

Output Arguments

xyLocal — Local coordinates

n-by-2 vertical array

Local coordinates, specified as an n-by-2 vertical array of $[x \ y]$ pairs, where n is the number of local coordinates.

See Also

Objects

binaryOccupancyMap | mapLayer | multiLayerMap | occupancyMap

Functions

grid2world|local2world

occupancyMap3D

Create 3-D occupancy map

Description

The occupancyMap3D class stores a 3-D map and map information. The map is stored as probabilistic values in an octree data structure on page 2-763. The class handles arbitrary environments and expands its size dynamically based on observation inputs. You can add observations as point clouds or as specific *xyz* locations. These observations update the probability values. Probabilistic values represent the occupancy of locations. The octree data structure trims data appropriately to remain efficient both in memory and on disk.

Creation

Syntax

```
omap = occupancyMap3D
omap = occupancyMap3D(res)
omap = occupancyMap3D(res,Name,Value)
```

Description

omap = occupancyMap3D creates an empty 3-D occupancy map with no observations and default property values.

omap = occupancyMap3D(res) specifies a map resolution in cells/meter and sets the Resolution
property.

omap = occupancyMap3D(res,Name,Value) creates an object with additional options specified by one or more Name, Value pair arguments. For example, 'FreeThreshold',0.25 sets the threshold to consider cells obstacle-free as a probability value of 0.25. Enclose each property name in quotes.

Properties

Resolution — Grid resolution

1 (default) | positive scalar

Grid resolution in cells per meter, specified as a scalar. Specify resolution on construction. Inserting observations with precisions higher than this value are rounded down and applied at this resolution.

FreeThreshold — Threshold to consider cells as obstacle-free

0.2 (default) | positive scalar

Threshold to consider cells as obstacle-free, specified as a positive scalar. Probability values below this threshold are considered obstacle-free.

OccupiedThreshold — Threshold to consider cells as occupied

```
0.65 (default) | positive scalar
```

Threshold to consider cells as occupied, specified as a positive scalar. Probability values above this threshold are considered occupied.

ProbabilitySaturation — Saturation limits on probability values

```
[0.001 0.999] (default) | [min max] vector
```

Saturation limits on probability values, specified as a [min max] vector. Values above or below these saturation values are set to the min or max values. This property reduces oversaturating of cells when incorporating multiple observations.

Object Functions

checkOccupancy Check if locations are free or occupied getOccupancy Get occupancy probability of locations

inflate Inflate map

insertPointCloud Insert 3-D points or point cloud observation into map rayIntersection Find intersection points of rays and occupied map cells

setOccupancy Set occupancy probability of locations

show Show occupancy map

updateOccupancy Update occupancy probability at locations

Examples

Create 3-D Occupancy Map and Inflate Points

The occupancyMap3D object stores obstacles in 3-D space, using sensor observations to map an environment. Create a map and add points from a point cloud to identify obstacles. Then inflate the obstacles in the map to ensure safe operating space around obstacles.

Create an occupancyMap3D object with a map resolution of 10 cells/meter.

```
map3D = occupancyMap3D(10);
```

Define a set of 3-D points as an observation from a pose [x y z qw qx qy qz]. This pose is for the sensor that observes these points and is centered on the origin. Define two sets of points to insert multiple observations.

```
pose = [000100];

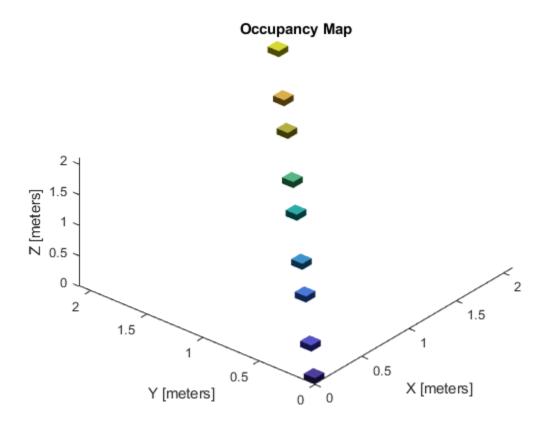
points = repmat((0:0.25:2)', 1, 3);

points2 = [(0:0.25:2)' (2:-0.25:0)' (0:0.25:2)'];

maxRange = 5;
```

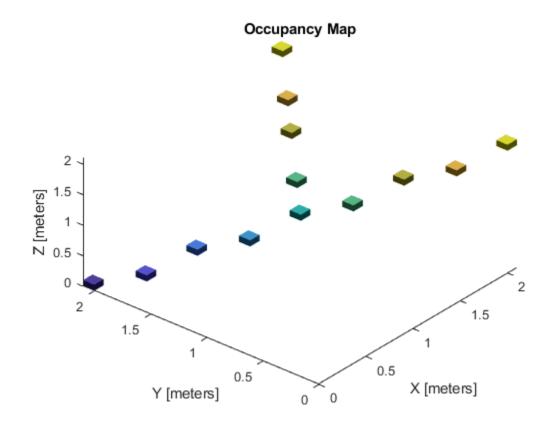
Insert the first set of points using insertPointCloud. The function uses the sensor pose and the given points to insert observations into the map. The colors displayed correlate to the height of the point only for illustrative purposes.

```
insertPointCloud(map3D,pose,points,maxRange)
show(map3D)
```



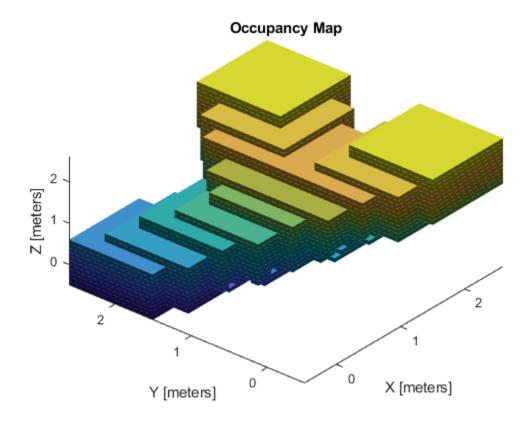
Insert the second set of points. The ray between the sensor pose (origin) and these points overlap points from the previous insertion. Therefore, the free space between the sensor and the new points are updated and marked as free space.

insertPointCloud(map3D,pose,points2,maxRange)
show(map3D)



Inflate the map to add a buffer zone for safe operation around obstacles. Define the vehicle radius and safety distance and use the sum of these values to define the inflation radius for the map.

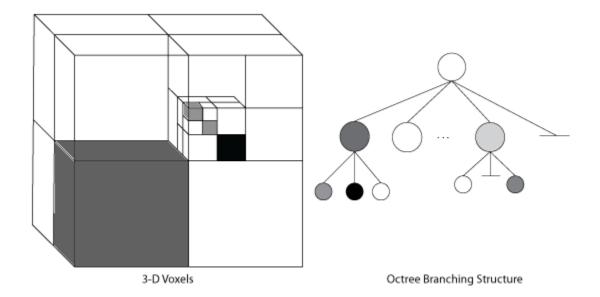
```
vehicleRadius = 0.2;
safetyRadius = 0.3;
inflationRadius = vehicleRadius + safetyRadius;
inflate(map3D, inflationRadius);
show(map3D)
```



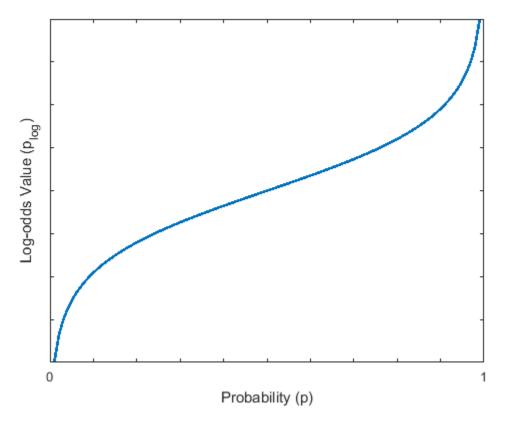
Algorithms

Octree Data Structure

The octree data structure is a hierarchical structure used for subdivision of an environment into cubic volumes called voxels. For a given map volume, the space is recursively subdivided into eight voxels until achieving a desired map resolution (voxel size) is achieved. This subdivision can be represented as a tree, which stores probability values for locations in the map.



The probability values in the tree have a log-odds representation. Using this representation, locations easily recover from dynamic observations and numerical errors due to small probabilities are reduced. To remain efficient in memory, lower branches of the tree are pruned in the structure if they share the same occupancy values using this log-odds representation.



The class internally handles the organization of this data structure, including the pruning of branches. Specify all observations as spatial coordinates when using functions such as setOccupancy, getOccupancy, or insertPointCloud. Insertions into the tree, and navigation through the tree, is determined based on the spatial coordinates and the resolution of the map.

References

[1] Hornung, Armin, Kai M. Wurm, Maren Bennewitz, Cyrill Stachniss, and Wolfram Burgard.

"OctoMap: an efficient probabilistic 3D mapping framework based on octrees." *Autonomous Robots*, Vol. 34, No. 3, 2013, pp. 189–206.. doi:10.1007/s10514-012-9321-0.

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

Classes

binaryOccupancyMap | occupancyMap

Functions

inflate | insertPointCloud | readOccupancyMap3D | setOccupancy | show

checkOccupancy

Check if locations are free or occupied

Syntax

i0ccval = check0ccupancy(map3D,xyz)

Description

iOccval = checkOccupancy(map3D,xyz) returns an array of occupancy values specified at the xyz locations using the OccupiedThreshold and FreeThreshold properties of the input occupancyMap3D object. Each row is a separate xyz location in the map to check the occupancy of. Occupancy values can be obstacle-free (0), occupied (1), or unknown (-1).

Input Arguments

map3D — 3-D occupancy map

occupancyMap3D object

3-D occupancy map, specified as an occupancyMap3D object.

xyz — World coordinates

n-by-3 matrix

World coordinates, specified as an n-by-3 matrix of [x y z] points, where n is the number of world coordinates.

Output Arguments

iOccval — Interpreted occupancy values

column vector

Interpreted occupancy values, returned as a column vector with the same length as xyz.

Occupancy values can be obstacle-free (0), occupied (1), or unknown (-1). These values are determined from the actual probability values and the OccupiedThreshold and FreeThreshold properties of the map3D object.

See Also

Classes

lidarSLAM | occupancyMap | occupancyMap3D

Functions

inflate | insertPointCloud | setOccupancy | show

getOccupancy

Get occupancy probability of locations

Syntax

occval = getOccupancy(map3D,xyz)

Description

occval = get0ccupancy(map3D, xyz) returns an array of probability occupancy values at the specified xyz locations in the occupancyMap3D object. Values close to 1 represent a high certainty that the cell contains an obstacle. Values close to 0 represent certainty that the cell is not occupied and obstacle-free.

Input Arguments

map3D — 3-D occupancy map

occupancyMap3D object

3-D occupancy map, specified as an occupancyMap3D object.

xyz — World coordinates

n-by-3 matrix

World coordinates, specified as an n-by-3 matrix of $[x \ y \ z]$ points, where n is the number of world coordinates.

Output Arguments

occval — Probability occupancy values

column vector

Probability occupancy values, returned as a column vector with the same length as xyz.

Values close to 0 represent certainty that the cell is not occupied and obstacle-free.

See Also

Classes

lidarSLAM | occupancyMap | occupancyMap3D

Functions

inflate | insertPointCloud | setOccupancy | show

inflate

Inflate map

Syntax

inflate(map3D, radius)

Description

inflate(map3D, radius) inflates each occupied position of the specified in the input
occupancyMap3D object by the radius specified in meters. radius is rounded up to the nearest
equivalent cell based on the resolution of the map. This inflation increases the size of the occupied
locations in the map.

Input Arguments

map3D — 3-D occupancy map

occupancyMap3D object

3-D occupancy map, specified as an occupancyMap3D object.

radius — Amount to inflate occupied locations

scalar

Amount to inflate occupied locations, specified as a scalar. radius is rounded up to the nearest cell value.

See Also

Classes

lidarSLAM | occupancyMap | occupancyMap3D

Functions

insertPointCloud | setOccupancy | show

insertPointCloud

Insert 3-D points or point cloud observation into map

Syntax

insertPointCloud(map3D,pose,points,maxrange)
insertPointCloud(map3D,pose,ptcloud,maxrange)

Description

insertPointCloud(map3D, pose, points, maxrange) inserts one or more sensor observations at the given points in the occupancy map, map3D. Occupied points are updated with an observation of 0.7. All other points between the sensor pose and points are treated as obstacle-free and updated with an observation of 0.4. Points outside maxrange are not updated. NaN values are ignored.

insertPointCloud(map3D, pose, ptcloud, maxrange) inserts a ptcloud object into the map.

Input Arguments

map3D — 3-D occupancy map

occupancyMap3D object

3-D occupancy map, specified as a occupancyMap3D object.

points — Points of point cloud

n-by-3 matrix

Points of point cloud in sensor coordinates, specified as an n-by-3 matrix of [x y z] points, where n is the number of points in the point cloud.

ptcloud — Point cloud reading

pointCloud object

Point cloud reading, specified as a pointCloud object.

Note Using pointCloud objects requires Computer Vision Toolbox.

pose — Position and orientation of vehicle

```
[x y z qw qx qy qz] vector
```

Position and orientation of vehicle, specified as an $[x \ y \ z \ qw \ qx \ qy \ qz]$ vector. The vehicle pose is an xyz-position vector with a quaternion orientation vector specified as $[qw \ qx \ qy \ qz]$.

maxrange — Maximum range of sensor

scalar

Maximum range of point cloud sensor, specified as a scalar. Points outside this range are ignored.

See Also

Classes

lidarSLAM|occupancyMap|occupancyMap3D

Functions

inflate|setOccupancy|show

rayIntersection

Find intersection points of rays and occupied map cells

Syntax

```
[intersectionPts,isOccupied] = rayIntersection(map3D,sensorPose,directions,
maxrange)
[intersectionPts,isOccupied] = rayIntersection(map3D,sensorPose,directions,
maxrange,ignoreUnknown)
```

Description

[intersectionPts,isOccupied] = rayIntersection(map3D,sensorPose,directions,maxrange) returns intersection points of rays in the specified map, map3D. Rays emanate from the specified sensorPose at the given orientations, directions. Intersection points are returned in the world coordinate frame. Use isOccupied to determine if the intersection point is at the sensor max range or if it intersects an obstacle.

[intersectionPts,isOccupied] = rayIntersection(map3D,sensorPose,directions,maxrange,ignoreUnknown) additionally accepts optional arguments for the sensors max range and whether to ignore unknown values. By default, the rays extend to the map boundary and unknown values are ignored.

Input Arguments

map3D — 3-D occupancy map

occupancyMap3D object

3-D occupancy map, specified as a occupancyMap3D object.

sensorPose — Position and orientation of sensor

```
[x y z qw qx qy qz] vector
```

Position and orientation of sensor, specified as an $[x \ y \ z \ qw \ qx \ qy \ qz]$ vector. The vehicle pose is an xyz-position vector with a quaternion orientation vector specified as $[qw \ qx \ qy \ qz]$.

directions — Orientation of rays emanating from sensor

```
n-by-3 [dx dy dz] matrix | n-by-2 [az el] matrix
```

Orientation of rays emanating from the sensor relative to the sensor coordinate frame, specified as an n-by-3 [dx dy dz] matrix or n-by-2 [az el] matrix.

- [dx dy dz] is a directional vector in *xyz*-coordinates.
- [az el] is a vector with azimuth angle, az, measured from the positive x direction to the positive y direction, and elevation angle from the xy-plane to the positive z-direction in sensor coordinate frame.

maxrange — Maximum range of sensor

scalar

Maximum range of laser range sensor, specified as a scalar in meters. Range values greater than or equal to maxrange are considered free along the whole length of the ray, up to maxrange.

ignoreUnknown — Interpret unknown values as free or occupied $1 \ (default) \mid 0$

Interpret unknown values in the map as free or occupied specified as 1 or 0. Set this value to 0 to assume unknown values are occupied.

Output Arguments

intersectionPts — Intersection points

n-by-3 matrix

Intersection points, returned as n-by-3 matrix of $[x \ y \ z]$ points in the world frame, where n is the length of directions.

isOccupied — Occupancy status of ray end points

vector of zeroes and ones

Occupancy status of ray end points, returned as a vector of zeroes and ones. Use isOccupied to determine if the intersection point is at the sensor max range or if it intersects an obstacle.

See Also

Classes

lidarSLAM | occupancyMap | occupancyMap3D

Functions

inflate | insertPointCloud | setOccupancy | show

Introduced in R2020a

setOccupancy

Set occupancy probability of locations

Syntax

setOccupancy(map3D,xyz,occval)

Description

setOccupancy(map3D,xyz,occval) assigns the occupancy values to each specified xyz coordinate in the 3-D occupancy map.

Input Arguments

map3D — 3-D occupancy map

occupancyMap3D object

3-D occupancy map, specified as an occupancyMap3D object.

xyz — World coordinates

n-by-3 matrix

World coordinates, specified as an n-by-3 matrix of [x y z] points, where n is the number of world coordinates.

occval — Probability occupancy values

scalar | column vector

Probability occupancy values, specified as a scalar or a column vector with the same length as xyz. A scalar input is applied to all coordinates in xyz.

Values close to 0 represent certainty that the cell is not occupied and obstacle-free.

See Also

Classes

lidarSLAM | occupancyMap | occupancyMap3D

Functions

inflate | insertPointCloud | setOccupancy | show

show

Show occupancy map

Syntax

```
axes = show(map3D)
show(map3D, "Parent", parent)
```

Description

axes = show(map3D) displays the occupancy map, map3D, in the current axes, with the axes labels
representing the world coordinates.

The function displays the 3-D environment using 3-D voxels for areas with occupancy values greater than the <code>OccupiedThreshold</code> property value specified in <code>map3D</code>. The color of the 3-D plot is strictly height-based.

show(map3D, "Parent", parent) displays the occupancy map in the axes handle specified by
parent.

Input Arguments

map3D — 3-D occupancy map

occupancyMap3D object

3-D occupancy map, specified as an occupancyMap3D object.

parent — Axes used to plot the map

Axes object | UIAxes object

Axes used to plot the map, specified as either an Axes or UIAxes object. See axes or uiaxes.

Output Arguments

axes — Axes handle for map

Axes object | UIAxes object

Axes handle for map, returned as either an Axes or UIAxesobject. See axes or uiaxes.

See Also

Classes

lidarSLAM | occupancyMap | occupancyMap3D

Functions

insertPointCloud | setOccupancy | show

updateOccupancy

Update occupancy probability at locations

Syntax

updateOccupancy(map3D,xyz,obs)

Description

updateOccupancy(map3D,xyz,obs) probabilistically integrates the observation values, obs, to each specified xyz coordinate in the occupancyMap3D object, map3D.

Input Arguments

map3D — 3-D occupancy map

occupancyMap3D object

3-D occupancy map, specified as an occupancyMap3D object.

xyz — World coordinates

n-by-3 matrix

World coordinates, specified as an n-by-3 matrix of [x y z] points, where n is the number of world coordinates.

obs — Probability observation values

numeric scalar | logical scalar | *n*-by-1 column vector

Probability observation values, specified as a numeric or logical scalar, or as an n-by-1 column vector with the same size as xyz.

obs values can be from 0 to 1, but if obs is a logical array, the function uses the default observation values of 0.7 (true) and 0.4 (false). If obs is a numeric or logical scalar, the value is applied to all coordinates in xyz.

See Also

Classes

lidarSLAM | occupancyMap | occupancyMap3D

Functions

inflate | insertPointCloud | setOccupancy | show

odometryMotionModel

Create an odometry motion model

Description

odometryMotionModel creates an odometry motion model object for differential drive vehicles. This object contains specific motion model parameters. You can use this object to specify the motion model parameters in the monteCarloLocalization object.

This motion model assumes that the vehicle makes pure rotation and translation motions to travel from one location to the other. The model propagates points for either forward or backwards motion based on these motion patterns. The elements of the Noise property refer to the variance in the motion. To see the effect of changing the noise parameters, use showNoiseDistribution.

Creation

Syntax

omm = odometryMotionModel

Description

omm = odometryMotionModel creates an odometry motion model object for differential drive vehicles.

Properties

Noise — Gaussian noise for vehicle motion

[0.2 0.2 0.2 0.2] (default) | 4-element vector

Gaussian noise for vehicle motion, specified as a 4-element vector. This property represents the variance parameters for Gaussian noise applied to vehicle motion. The elements of the vector correspond to the following errors in order:

- Rotational error due to rotational motion
- · Rotational error due to translational motion
- Translational error due to translation motion
- · Translational error due to rotational motion

Type — Type of the odometry motion model

'DifferentialDrive' (default)

This property is read-only.

Type of the odometry motion model, returned as 'DifferentialDrive'. This read-only property indicates the type of odometry motion model being used by the object.

Object Functions

showNoiseDistribution Display noise parameter effects

Examples

Predict Poses Based On An Odometry Motion Model

This example shows how to use the odometryMotionModel class to predict the pose of a vehicle. An odometryMotionModel object contains the motion model parameters for a differential drive vehicle. Use the object to predict the pose of a vehicle based on its current and previous poses and the motion model parameters.

Create odometry motion model object.

```
motionModel = odometryMotionModel;
```

Define previous poses and the current odometry reading. Each pose prediction corresponds to a row in previousPoses vector.

```
previousPoses = rand(10,3);
currentOdom = [0.1 0.1 0.1];
```

The first call to the object initializes values and returns the previous poses as the current poses.

```
currentPoses = motionModel(previousPoses, currentOdom);
```

Subsequent calls to the object with updated odometry poses returns the predicted poses based on the motion model.

```
current0dom = current0dom + [0.1 0.1 0.05];
predPoses = motionModel(previousPoses, current0dom);
```

Show Noise Distribution Effects for Odometry Motion Model

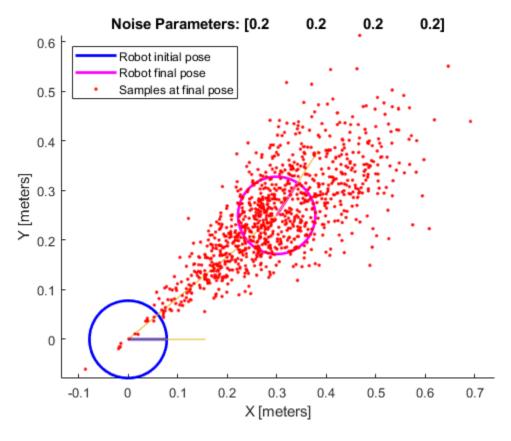
This example shows how to visualize the effect of different noise parameters on the odometryMotionModel class. An odometryMotionModel object contains the motion model noise parameters for a differential drive vehicle. Use showNoiseDistribution to visualize how changing these values affect the distribution of predicted poses.

Create a motion model object.

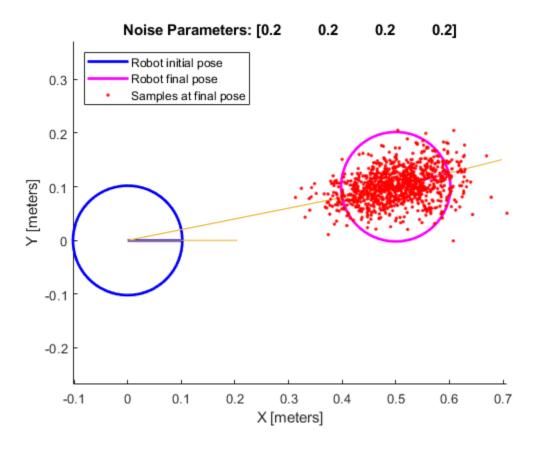
```
motionModel = odometryMotionModel;
```

Show the distribution of particles with the existing noise parameters. Each particle is a hypothesis for the predicted pose.

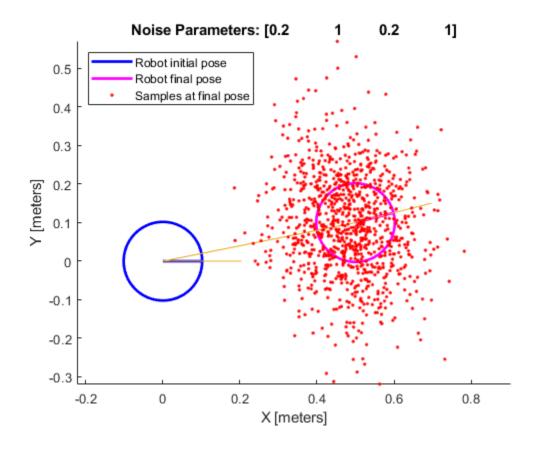
```
showNoiseDistribution(motionModel);
```



Show the distribution with a specified odometry pose change and number of samples. The change in odometry is used as the final pose with hypotheses distributed around based on the Noise parameters.



Change the \mbox{Noise} parameters and visualize the effects. Use the same odometry pose change and number of samples.



Limitations

If you make changes to your motion model after using it with the monteCarloLocalization object, call release on that object beforehand. For example:

```
mcl = monteCarloLocalization;
[isUpdated,pose,covariance] = mcl(ranges,angles);
release(mcl)
mcl.MotionModel.Noise = [0.25 0.25 0.4 0.4];
```

References

[1] Thrun, Sebatian, Wolfram Burgard, and Dieter Fox. Probabilistic Robotics. MIT Press, 2005.

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

likelihoodFieldSensorModel|monteCarloLocalization

Topics "Localize TurtleBot Using Monte Carlo Localization"

showNoiseDistribution

Display noise parameter effects

Syntax

```
showNoiseDistribution(ommObj)
showNoiseDistribution(ommObj)
showNoiseDistribution(ommObj,Name,Value)
```

Description

showNoiseDistribution(ommObj) shows the noise distribution for a default odometry pose update, number of samples and the current noise parameters on the input object.

axes = showNoiseDistribution(ommObj) shows the noise distribution and returns the axes handle.

showNoiseDistribution(ommObj,Name,Value) provides additional options specified by one or more Name, Value pairs. Name is the property name and Value is the corresponding value. Name must appear inside single quotes (' '). You can specify several name-value pair arguments in any order as Name1, Value1,...,NameN,ValueN. Properties not specified retain their default values.

Examples

Show Noise Distribution Effects for Odometry Motion Model

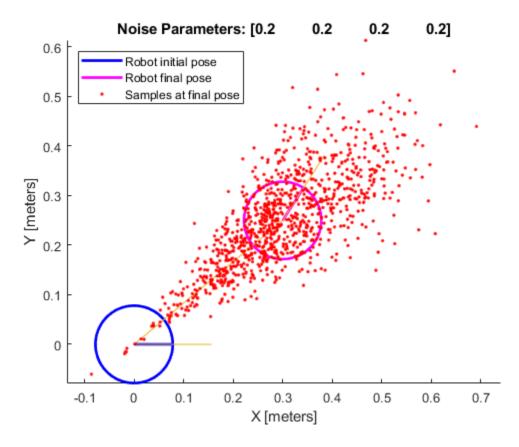
This example shows how to visualize the effect of different noise parameters on the odometryMotionModel class. An odometryMotionModel object contains the motion model noise parameters for a differential drive vehicle. Use showNoiseDistribution to visualize how changing these values affect the distribution of predicted poses.

Create a motion model object.

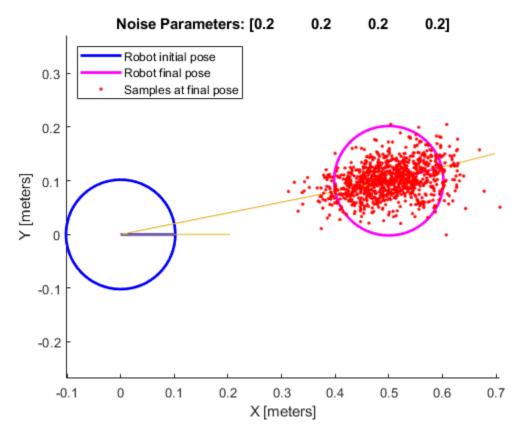
```
motionModel = odometryMotionModel;
```

Show the distribution of particles with the existing noise parameters. Each particle is a hypothesis for the predicted pose.

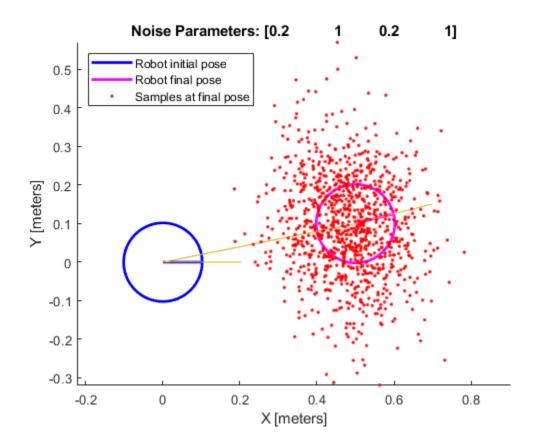
```
showNoiseDistribution(motionModel);
```



Show the distribution with a specified odometry pose change and number of samples. The change in odometry is used as the final pose with hypotheses distributed around based on the Noise parameters.



Change the \mbox{Noise} parameters and visualize the effects. Use the same odometry pose change and number of samples.



Input Arguments

ommObj — odometryMotionModel object

handle

odometryMotionModel object, specified as a handle. Create this object using odometryMotionModel.

Name-Value Pair Arguments

Specify optional comma-separated pairs of Name, Value arguments. Name is the argument name and Value is the corresponding value. Name must appear inside quotes. You can specify several name and value pair arguments in any order as Name1, Value1, . . . , NameN, ValueN.

Example: 'OdometryPoseChange',[1 1 pi]

OdometryPoseChange — Change in odometry

three-element vector

Change in odometry of the robot, specified as a comma-separated pair consisting of 'OdometryPoseChange' and a three-element vector, [x y theta].

NumSamples — Number of particles to display

scalar

Number of particles to display, specified as a comma-separated pair consisting of 'NumSamples' and a scalar.

Parent — Axes to plot the map

Axes object | UIAxes object

Axes to plot the map, specified as a comma-separated pair consisting of 'Parent' and either an Axes or UIAxes object. See axes or uiaxes.

See Also

likelihoodFieldSensorModel | monteCarloLocalization | odometryMotionModel

pathmetrics

Information for path metrics

Description

The pathmetrics object holds information for computing path metrics. Use object functions to calculate smoothness, clearance, and path validity based on a set of poses and the associated map environment.

Creation

Syntax

```
pathMetricsObj = pathmetrics(path)
pathMetricsObj = pathmetrics(path,validator)
```

Description

pathMetricsObj = pathmetrics(path) creates an object based on the input navPath object.
The state validator is assumed to be a validatorOccupancyMap object. The path input sets the
value of the "Path" on page 2-0 property.

pathMetricsObj = pathmetrics(path,validator) creates an object based on the input
navPath object and associated state validator for checking the path validity. The validator input
sets the value of the "StateValidator" on page 2-0 property.

Properties

Path — Path data structure

navPath object

Path data structure, specified as a navPath object is the path whose metric is to be calculated.

StateValidator — Validator for states on path

validatorOccupancyMap(stateSpaceSE2,binaryOccupancyMap(10)) (default) |
validatorOccupancyMap object | validatorVehicleCostmap object

Validator for states on path, specified either as a validatorOccupancyMap or validatorVehicleCostmap object.

Object Functions

clearance Minimum clearance of path

isPathValid Determine if planned path is obstacle free show Visualize path metrics in map environment

smoothness Smoothness of path

Examples

Compute Path Metrics

Compute smoothness, clearance, and validity of a planned path based on a set of poses and the associated map environment.

Load and Assign Map to State Validator

[path,solutionInfo] = plan(planner,start,goal);

Create an occupancy map from an example map and set the map resolution.

```
load exampleMaps.mat; % simpleMap
mapResolution = 1; % cells/meter
map = occupancyMap(simpleMap,mapResolution);
Create a Dubins state space.
statespace = stateSpaceDubins;
Create a state validator based on occupancy map to store the parameters and states in the Dubins
state space.
statevalidator = validatorOccupancyMap(statespace);
Assign the map to the validator.
statevalidator.Map = map;
Set the validation distance for the validator.
statevalidator.ValidationDistance = 0.01;
Update the state space bounds to be the same as the map limits.
statespace.StateBounds = [map.XWorldLimits;map.YWorldLimits;[-pi pi]];
Plan Path
Create an RRT* path planner and allow further optimization.
planner = plannerRRTStar(statespace, statevalidator);
planner.ContinueAfterGoalReached = true;
Reduce the maximum number of iterations and increase the maximum connection distance.
planner.MaxIterations = 2500;
planner.MaxConnectionDistance = 0.3;
Define start and goal states for the path planner as [x, y, theta] vectors. x and y are the Cartesian
coordinates, and theta is the orientation angle.
start = [2.5, 2.5, 0]; % [meters, meters, radians]
goal = [22.5, 8.75, 0];
Plan a path from the start state to the goal state. The plan function returns a navPath object.
rng(100, 'twister') % repeatable result
```

Compute and Visualize Path Metrics

Create a path metrics object.

```
pathMetricsObj = pathmetrics(path,statevalidator);
```

Check path validity. The result is 1 (true) if the planned path is obstacle free. 0 (false) indicates an invalid path.

```
isPathValid(pathMetricsObj)
```

```
ans = logical
```

Calculate the minimum clearance of the path.

```
clearance(pathMetricsObj)
```

```
ans = 1.4142
```

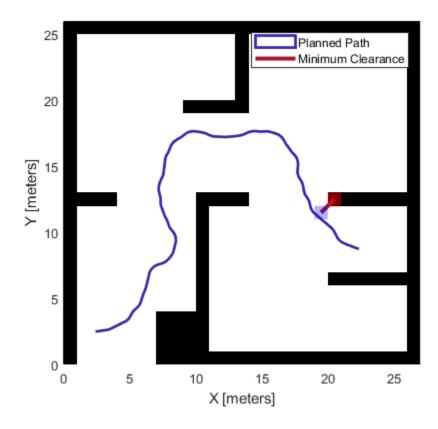
Evaluate the smoothness of the path. Values close to θ indicate a smoother path. Straight-line paths return a value of θ .

```
smoothness(pathMetricsObj)
```

```
ans = 1.7318
```

Visualize the minimum clearance of the path.

```
show(pathMetricsObj)
legend('Planned Path','Minimum Clearance')
```



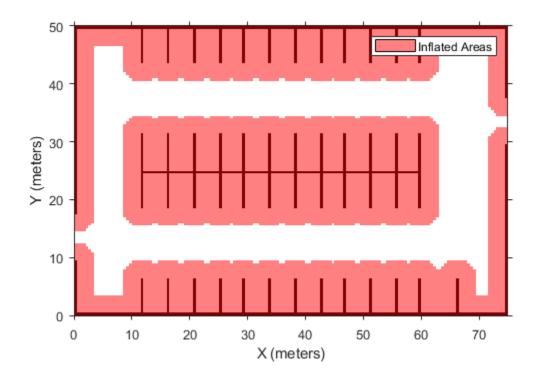
Vehicle Path Planning and Metrics Computation in a 2-D Costmap Environment

Plan a vehicle path through a parking lot using the RRT* algorithm. Compute and visualize the smoothness, clearance, and validity of the planned path.

Load and Assign Map to State Validator

Load a costmap of a parking lot. Plot the costmap to see the parking lot and the inflated areas that the vehicle should avoid.

```
load parkingLotCostmap.mat;
costmap = parkingLotCostmap;
plot(costmap)
xlabel('X (meters)')
ylabel('Y (meters)')
```



Create a stateSpaceDubins object and increase the minimum turing radius to 4 meters.

```
statespace = stateSpaceDubins;
statespace.MinTurningRadius = 4; % meters
```

Create a validatorVehicleCostmap object using the created state space.

```
statevalidator = validatorVehicleCostmap(statespace);
```

Assign the parking lot costmap to the state validator object.

```
statevalidator.Map = costmap;
```

Plan Path

Define start and goal poses for the vehicle as $[x, y, \theta]$ vectors. World units for the (x,y) locations are in meters. World units for the orientation angles θ are in degrees.

```
startPose = [5, 5, 90]; % [meters, meters, degrees]
goalPose = [40, 38, 180]; % [meters, meters, degrees]
```

Use a pathPlannerRRT (Automated Driving Toolbox) object and the plan (Automated Driving Toolbox) function to plan the vehicle path from the start pose to the goal pose.

```
planner = pathPlannerRRT(costmap);
refPath = plan(planner, startPose, goalPose);
```

Interpolate along the path at every one meter. Convert the orientation angles from degrees to radians.

```
poses = zeros(size(refPath.PathSegments,2)+1,3);
poses(1,:) = refPath.StartPose;
for i = 1:size(refPath.PathSegments,2)
    poses(i+1,:) = refPath.PathSegments(i).GoalPose;
end
poses(:,3) = deg2rad(poses(:,3));
```

Create a navPath object using the Dubins state space object and the states specified by poses.

```
path = navPath(statespace,poses);
```

Compute and Visualize Path Metrics

Create a pathmetrics object.

```
pathMetricsObj = pathmetrics(path, statevalidator);
```

Check path validity. The result is 1 (true) if the planned path is obstacle free. 0 (false) indicates an invalid path.

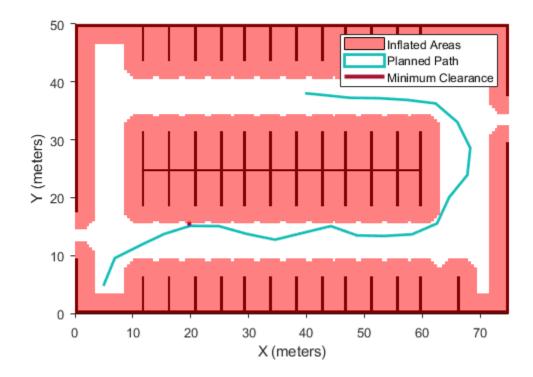
```
isPathValid(pathMetricsObj)
```

```
ans = logical
1
```

Compute and visualize the minimum clearance of the path.

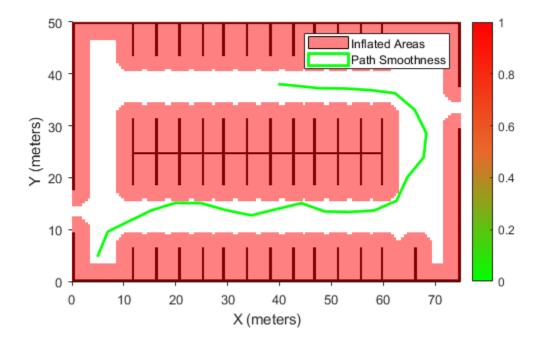
```
clearance(pathMetricsObj)
```

```
ans = 0.5000
show(pathMetrics0bj)
legend('Inflated Areas','Planned Path','Minimum Clearance')
xlabel('X (meters)')
ylabel('Y (meters)')
```



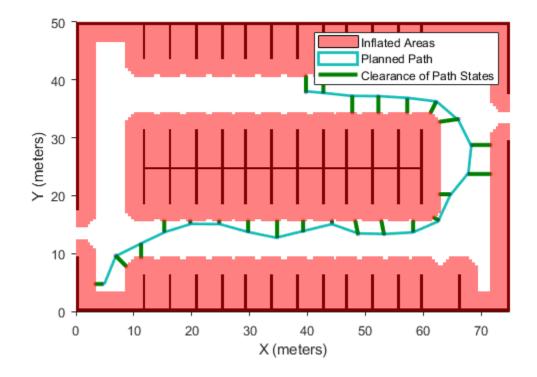
Compute and visualize the smoothness of the path. Values close to 0 indicate a smoother path. Straight-line paths return a value of 0.

```
smoothness(pathMetricsObj)
ans = 0.0842
show(pathMetricsObj,'Metrics',{'Smoothness'})
legend('Inflated Areas','Path Smoothness')
xlabel('X (meters)')
ylabel('Y (meters)')
```



Visualize the clearance for each state of the path.

```
show(pathMetricsObj,'Metrics',{'StatesClearance'})
legend('Inflated Areas','Planned Path','Clearance of Path States')
xlabel('X (meters)')
ylabel('Y (meters)')
```



See AlsooccupancyMap | occupancyMap3D | plannerRRTStar

Introduced in R2019b

clearance

Minimum clearance of path

Syntax

```
clearance(pathMetricsObj)
clearance(pathMetricsObj,'Type','states')
```

Description

clearance(pathMetricsObj) returns the minimum clearance of the path. Clearance is measured as the minimum distance between grid cell centers of states on the path and obstacles in the specified map environment.

Note The computed clearance is accurate up to sqrt(2) times grid map cell size.

clearance(pathMetricsObj,'Type','states') returns the set of minimum distances for each state of the path, in the form of an n-by-1 vector, where n is the number of states.

Examples

Compute Path Metrics

Compute smoothness, clearance, and validity of a planned path based on a set of poses and the associated map environment.

Load and Assign Map to State Validator

Set the validation distance for the validator.

Create an occupancy map from an example map and set the map resolution.

```
load exampleMaps.mat; % simpleMap
mapResolution = 1; % cells/meter
map = occupancyMap(simpleMap,mapResolution);

Create a Dubins state space.

statespace = stateSpaceDubins;

Create a state validator based on occupancy map to store the parameters and states in the Dubins state space.

statevalidator = validatorOccupancyMap(statespace);

Assign the map to the validator.

statevalidator.Map = map;
```

```
statevalidator.ValidationDistance = 0.01;
```

Update the state space bounds to be the same as the map limits.

```
statespace.StateBounds = [map.XWorldLimits;map.YWorldLimits;[-pi pi]];
```

Plan Path

Create an RRT* path planner and allow further optimization.

```
planner = plannerRRTStar(statespace,statevalidator);
planner.ContinueAfterGoalReached = true;
```

Reduce the maximum number of iterations and increase the maximum connection distance.

```
planner.MaxIterations = 2500;
planner.MaxConnectionDistance = 0.3;
```

Define start and goal states for the path planner as [x, y, theta] vectors. x and y are the Cartesian coordinates, and theta is the orientation angle.

```
start = [2.5, 2.5, 0]; % [meters, meters, radians]
goal = [22.5, 8.75, 0];
```

Plan a path from the start state to the goal state. The plan function returns a navPath object.

```
rng(100,'twister') % repeatable result
[path,solutionInfo] = plan(planner,start,goal);
```

Compute and Visualize Path Metrics

Create a path metrics object.

```
pathMetricsObj = pathmetrics(path, statevalidator);
```

Check path validity. The result is 1 (true) if the planned path is obstacle free. 0 (false) indicates an invalid path.

```
isPathValid(pathMetricsObj)
```

```
ans = logical
```

Calculate the minimum clearance of the path.

```
clearance(pathMetricsObj)
```

```
ans = 1.4142
```

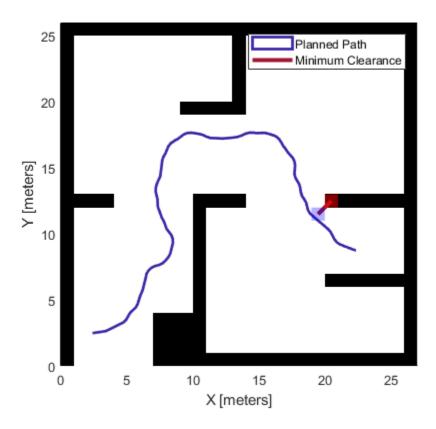
Evaluate the smoothness of the path. Values close to θ indicate a smoother path. Straight-line paths return a value of θ .

```
smoothness(pathMetricsObj)
```

```
ans = 1.7318
```

Visualize the minimum clearance of the path.

```
show(pathMetricsObj)
legend('Planned Path','Minimum Clearance')
```



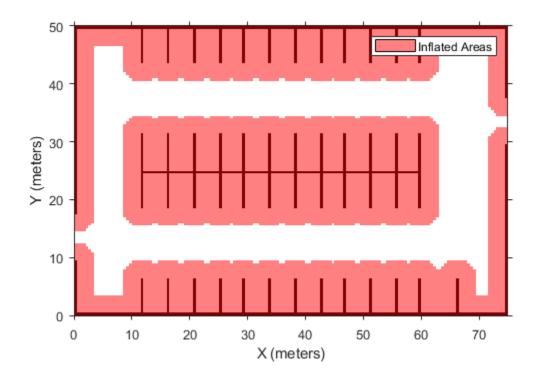
Vehicle Path Planning and Metrics Computation in a 2-D Costmap Environment

Plan a vehicle path through a parking lot using the RRT* algorithm. Compute and visualize the smoothness, clearance, and validity of the planned path.

Load and Assign Map to State Validator

Load a costmap of a parking lot. Plot the costmap to see the parking lot and the inflated areas that the vehicle should avoid.

```
load parkingLotCostmap.mat;
costmap = parkingLotCostmap;
plot(costmap)
xlabel('X (meters)')
ylabel('Y (meters)')
```



Create a stateSpaceDubins object and increase the minimum turing radius to 4 meters.

```
statespace = stateSpaceDubins;
statespace.MinTurningRadius = 4; % meters
```

Create a validatorVehicleCostmap object using the created state space.

```
statevalidator = validatorVehicleCostmap(statespace);
```

Assign the parking lot costmap to the state validator object.

```
statevalidator.Map = costmap;
```

Plan Path

Define start and goal poses for the vehicle as $[x, y, \theta]$ vectors. World units for the (x,y) locations are in meters. World units for the orientation angles θ are in degrees.

```
startPose = [5, 5, 90]; % [meters, meters, degrees]
goalPose = [40, 38, 180]; % [meters, meters, degrees]
```

Use a pathPlannerRRT (Automated Driving Toolbox) object and the plan (Automated Driving Toolbox) function to plan the vehicle path from the start pose to the goal pose.

```
planner = pathPlannerRRT(costmap);
refPath = plan(planner, startPose, goalPose);
```

Interpolate along the path at every one meter. Convert the orientation angles from degrees to radians.

```
poses = zeros(size(refPath.PathSegments,2)+1,3);
poses(1,:) = refPath.StartPose;
for i = 1:size(refPath.PathSegments,2)
     poses(i+1,:) = refPath.PathSegments(i).GoalPose;
end
poses(:,3) = deg2rad(poses(:,3));
```

Create a navPath object using the Dubins state space object and the states specified by poses.

```
path = navPath(statespace,poses);
```

Compute and Visualize Path Metrics

Create a pathmetrics object.

```
pathMetricsObj = pathmetrics(path, statevalidator);
```

Check path validity. The result is 1 (true) if the planned path is obstacle free. 0 (false) indicates an invalid path.

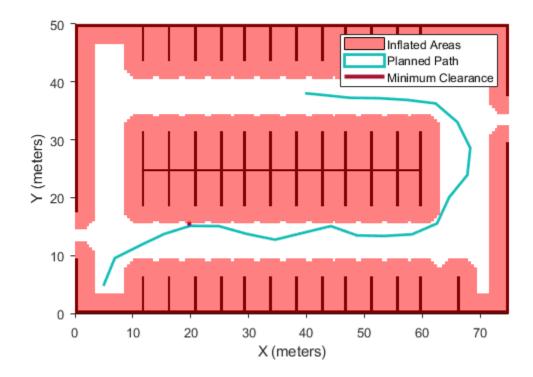
```
isPathValid(pathMetricsObj)
```

```
ans = logical
```

Compute and visualize the minimum clearance of the path.

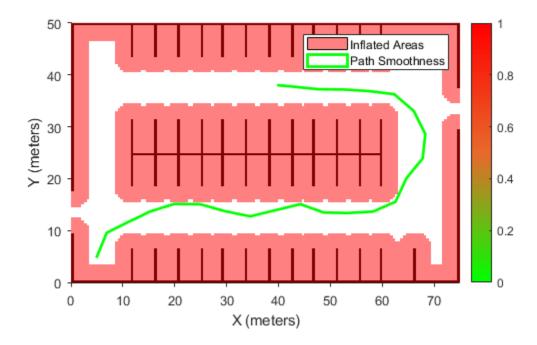
```
clearance(pathMetricsObj)
```

```
ans = 0.5000
show(pathMetrics0bj)
legend('Inflated Areas','Planned Path','Minimum Clearance')
xlabel('X (meters)')
ylabel('Y (meters)')
```



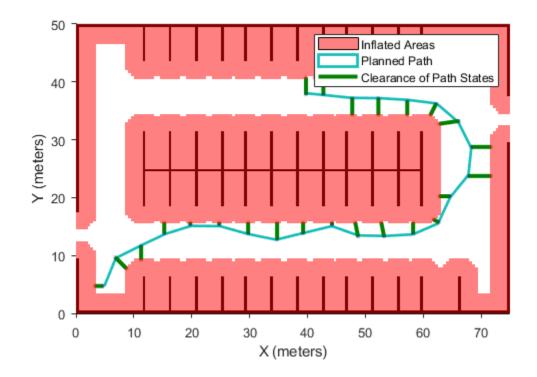
Compute and visualize the smoothness of the path. Values close to 0 indicate a smoother path. Straight-line paths return a value of 0.

```
smoothness(pathMetricsObj)
ans = 0.0842
show(pathMetricsObj,'Metrics',{'Smoothness'})
legend('Inflated Areas','Path Smoothness')
xlabel('X (meters)')
ylabel('Y (meters)')
```



Visualize the clearance for each state of the path.

```
show(pathMetricsObj,'Metrics',{'StatesClearance'})
legend('Inflated Areas','Planned Path','Clearance of Path States')
xlabel('X (meters)')
ylabel('Y (meters)')
```



Input Arguments

${\tt pathMetrics0bj-Information\ for\ path\ metrics}$

pathmetrics object

Information for path metrics, specified as a pathmetrics object.

See Also

Objects

pathmetrics

Functions

isPathValid|show|smoothness

Introduced in R2019b

isPathValid

Determine if planned path is obstacle free

Syntax

isPathValid(pathMetricsObj)

Description

isPathValid(pathMetricsObj) returns either a logical 1 (true) if the planned path is obstacle
free or a logical 0 (false) if the path is invalid.

Examples

Compute Path Metrics

Compute smoothness, clearance, and validity of a planned path based on a set of poses and the associated map environment.

Load and Assign Map to State Validator

Create an occupancy map from an example map and set the map resolution.

```
load exampleMaps.mat; % simpleMap
mapResolution = 1; % cells/meter
map = occupancyMap(simpleMap, mapResolution);

Create a Dubins state space.
statespace = stateSpaceDubins;

Create a state validator based on occupancy map to store the parameters and states in the Dubins state space.
statevalidator = validatorOccupancyMap(statespace);

Assign the map to the validator.
statevalidator.Map = map;

Set the validation distance for the validator.
statevalidator.ValidationDistance = 0.01;

Update the state space bounds to be the same as the map limits.
statespace.StateBounds = [map.XWorldLimits;map.YWorldLimits;[-pi pi]];
```

Plan Path

Create an RRT* path planner and allow further optimization.

```
planner = plannerRRTStar(statespace,statevalidator);
planner.ContinueAfterGoalReached = true;
```

Reduce the maximum number of iterations and increase the maximum connection distance.

```
planner.MaxIterations = 2500;
planner.MaxConnectionDistance = 0.3;
```

Define start and goal states for the path planner as [x, y, theta] vectors. x and y are the Cartesian coordinates, and theta is the orientation angle.

```
start = [2.5, 2.5, 0]; % [meters, meters, radians]
goal = [22.5, 8.75, 0];
```

Plan a path from the start state to the goal state. The plan function returns a navPath object.

```
rng(100,'twister') % repeatable result
[path,solutionInfo] = plan(planner,start,goal);
```

Compute and Visualize Path Metrics

Create a path metrics object.

```
pathMetricsObj = pathmetrics(path,statevalidator);
```

Check path validity. The result is 1 (true) if the planned path is obstacle free. 0 (false) indicates an invalid path.

```
isPathValid(pathMetricsObj)
```

```
ans = logical
1
```

Calculate the minimum clearance of the path.

```
clearance(pathMetricsObj)
```

```
ans = 1.4142
```

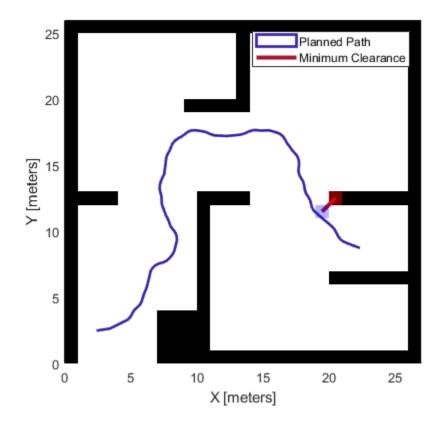
Evaluate the smoothness of the path. Values close to 0 indicate a smoother path. Straight-line paths return a value of 0.

```
smoothness(pathMetricsObj)
```

```
ans = 1.7318
```

Visualize the minimum clearance of the path.

```
show(pathMetricsObj)
legend('Planned Path','Minimum Clearance')
```



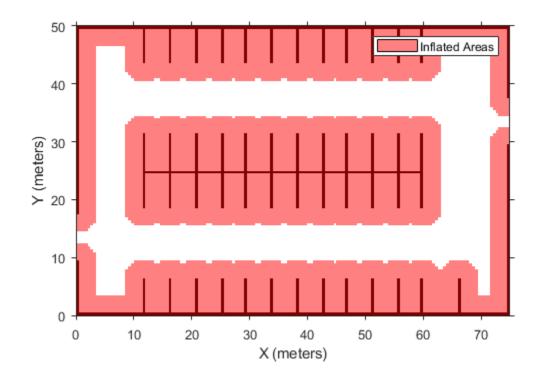
Vehicle Path Planning and Metrics Computation in a 2-D Costmap Environment

Plan a vehicle path through a parking lot using the RRT* algorithm. Compute and visualize the smoothness, clearance, and validity of the planned path.

Load and Assign Map to State Validator

Load a costmap of a parking lot. Plot the costmap to see the parking lot and the inflated areas that the vehicle should avoid.

```
load parkingLotCostmap.mat;
costmap = parkingLotCostmap;
plot(costmap)
xlabel('X (meters)')
ylabel('Y (meters)')
```



Create a stateSpaceDubins object and increase the minimum turing radius to 4 meters.

```
statespace = stateSpaceDubins;
statespace.MinTurningRadius = 4; % meters
```

Create a validatorVehicleCostmap object using the created state space.

```
statevalidator = validatorVehicleCostmap(statespace);
```

Assign the parking lot costmap to the state validator object.

```
statevalidator.Map = costmap;
```

Plan Path

Define start and goal poses for the vehicle as $[x, y, \theta]$ vectors. World units for the (x,y) locations are in meters. World units for the orientation angles θ are in degrees.

```
startPose = [5, 5, 90]; % [meters, meters, degrees]
goalPose = [40, 38, 180]; % [meters, meters, degrees]
```

Use a pathPlannerRRT (Automated Driving Toolbox) object and the plan (Automated Driving Toolbox) function to plan the vehicle path from the start pose to the goal pose.

```
planner = pathPlannerRRT(costmap);
refPath = plan(planner, startPose, goalPose);
```

Interpolate along the path at every one meter. Convert the orientation angles from degrees to radians.

```
poses = zeros(size(refPath.PathSegments,2)+1,3);
poses(1,:) = refPath.StartPose;
for i = 1:size(refPath.PathSegments,2)
     poses(i+1,:) = refPath.PathSegments(i).GoalPose;
end
poses(:,3) = deg2rad(poses(:,3));
```

Create a navPath object using the Dubins state space object and the states specified by poses.

```
path = navPath(statespace,poses);
```

Compute and Visualize Path Metrics

Create a pathmetrics object.

```
pathMetricsObj = pathmetrics(path,statevalidator);
```

Check path validity. The result is 1 (true) if the planned path is obstacle free. 0 (false) indicates an invalid path.

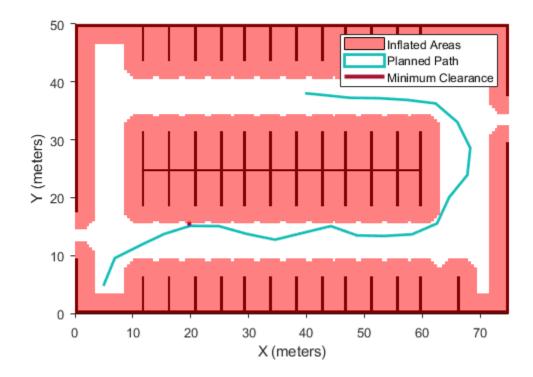
```
isPathValid(pathMetricsObj)
```

```
ans = logical
```

Compute and visualize the minimum clearance of the path.

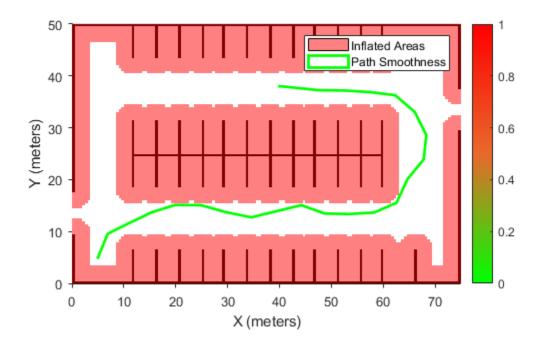
```
clearance(pathMetricsObj)
```

```
ans = 0.5000
show(pathMetrics0bj)
legend('Inflated Areas','Planned Path','Minimum Clearance')
xlabel('X (meters)')
ylabel('Y (meters)')
```



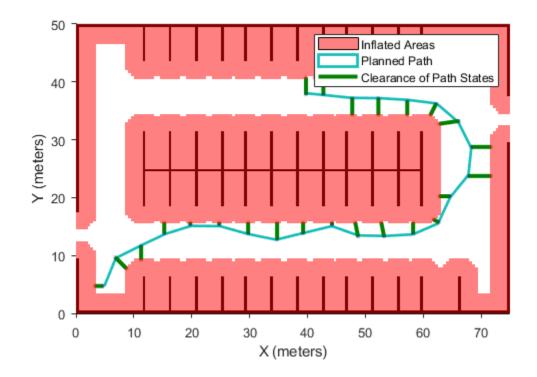
Compute and visualize the smoothness of the path. Values close to 0 indicate a smoother path. Straight-line paths return a value of 0.

```
smoothness(pathMetricsObj)
ans = 0.0842
show(pathMetricsObj,'Metrics',{'Smoothness'})
legend('Inflated Areas','Path Smoothness')
xlabel('X (meters)')
ylabel('Y (meters)')
```



Visualize the clearance for each state of the path.

```
show(pathMetricsObj,'Metrics',{'StatesClearance'})
legend('Inflated Areas','Planned Path','Clearance of Path States')
xlabel('X (meters)')
ylabel('Y (meters)')
```



Input Arguments

${\tt pathMetrics0bj-Information\ for\ path\ metrics}$

pathmetrics object

Information for path metrics, specified as a pathmetrics object.

See Also

Objects

pathmetrics

Functions

clearance|show|smoothness

Introduced in R2019b

show

Visualize path metrics in map environment

Syntax

```
show(pathMetricsObj)
show(pathMetricsObj,Name,Value)
axHandle = show(pathMetricsObj)
```

Description

show(pathMetricsObj) plots the path in the map environment with the minimum clearance.

show(pathMetricsObj,Name,Value) specifies additional options using one or more name-value
pair arguments.

axHandle = show(pathMetricsObj) outputs the axes handle of the figure used to plot the path.

Examples

Compute Path Metrics

Compute smoothness, clearance, and validity of a planned path based on a set of poses and the associated map environment.

Load and Assign Map to State Validator

Create an occupancy map from an example map and set the map resolution.

```
load exampleMaps.mat; % simpleMap
mapResolution = 1; % cells/meter
map = occupancyMap(simpleMap,mapResolution);

Create a Dubins state space.

statespace = stateSpaceDubins;

Create a state validator based on occupancy map to store the parameters and states in the Dubins state space.

statevalidator = validatorOccupancyMap(statespace);

Assign the map to the validator.

statevalidator.Map = map;

Set the validation distance for the validator.

statevalidator.ValidationDistance = 0.01;
```

Update the state space bounds to be the same as the map limits.

```
statespace.StateBounds = [map.XWorldLimits;map.YWorldLimits;[-pi pi]];
```

Plan Path

Create an RRT* path planner and allow further optimization.

```
planner = plannerRRTStar(statespace,statevalidator);
planner.ContinueAfterGoalReached = true;
```

Reduce the maximum number of iterations and increase the maximum connection distance.

```
planner.MaxIterations = 2500;
planner.MaxConnectionDistance = 0.3;
```

Define start and goal states for the path planner as [x, y, theta] vectors. x and y are the Cartesian coordinates, and theta is the orientation angle.

```
start = [2.5, 2.5, 0]; % [meters, meters, radians]
goal = [22.5, 8.75, 0];
```

Plan a path from the start state to the goal state. The plan function returns a navPath object.

```
rng(100,'twister') % repeatable result
[path,solutionInfo] = plan(planner,start,goal);
```

Compute and Visualize Path Metrics

Create a path metrics object.

```
pathMetricsObj = pathmetrics(path,statevalidator);
```

Check path validity. The result is 1 (true) if the planned path is obstacle free. 0 (false) indicates an invalid path.

```
isPathValid(pathMetricsObj)
```

```
ans = logical
```

Calculate the minimum clearance of the path.

```
clearance(pathMetricsObj)
```

```
ans = 1.4142
```

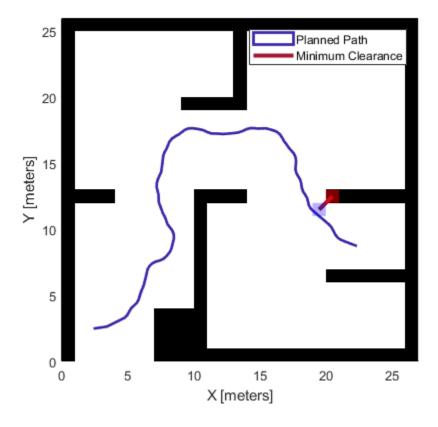
Evaluate the smoothness of the path. Values close to θ indicate a smoother path. Straight-line paths return a value of θ .

```
smoothness(pathMetricsObj)
```

```
ans = 1.7318
```

Visualize the minimum clearance of the path.

```
show(pathMetricsObj)
legend('Planned Path','Minimum Clearance')
```



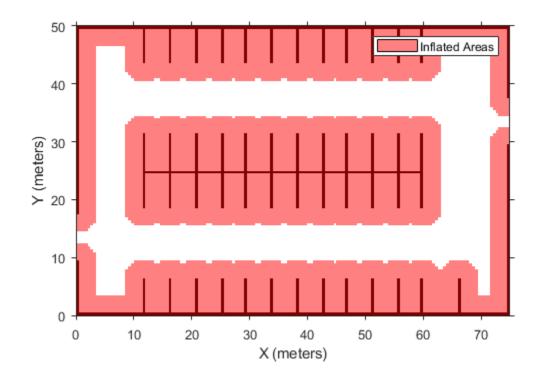
Vehicle Path Planning and Metrics Computation in a 2-D Costmap Environment

Plan a vehicle path through a parking lot using the RRT* algorithm. Compute and visualize the smoothness, clearance, and validity of the planned path.

Load and Assign Map to State Validator

Load a costmap of a parking lot. Plot the costmap to see the parking lot and the inflated areas that the vehicle should avoid.

```
load parkingLotCostmap.mat;
costmap = parkingLotCostmap;
plot(costmap)
xlabel('X (meters)')
ylabel('Y (meters)')
```



Create a stateSpaceDubins object and increase the minimum turing radius to 4 meters.

```
statespace = stateSpaceDubins;
statespace.MinTurningRadius = 4; % meters
```

Create a validatorVehicleCostmap object using the created state space.

```
statevalidator = validatorVehicleCostmap(statespace);
```

Assign the parking lot costmap to the state validator object.

```
statevalidator.Map = costmap;
```

Plan Path

Define start and goal poses for the vehicle as $[x, y, \theta]$ vectors. World units for the (x,y) locations are in meters. World units for the orientation angles θ are in degrees.

```
startPose = [5, 5, 90]; % [meters, meters, degrees]
goalPose = [40, 38, 180]; % [meters, meters, degrees]
```

Use a pathPlannerRRT (Automated Driving Toolbox) object and the plan (Automated Driving Toolbox) function to plan the vehicle path from the start pose to the goal pose.

```
planner = pathPlannerRRT(costmap);
refPath = plan(planner,startPose,goalPose);
```

Interpolate along the path at every one meter. Convert the orientation angles from degrees to radians.

```
poses = zeros(size(refPath.PathSegments,2)+1,3);
poses(1,:) = refPath.StartPose;
for i = 1:size(refPath.PathSegments,2)
     poses(i+1,:) = refPath.PathSegments(i).GoalPose;
end
poses(:,3) = deg2rad(poses(:,3));
```

Create a navPath object using the Dubins state space object and the states specified by poses.

```
path = navPath(statespace,poses);
```

Compute and Visualize Path Metrics

Create a pathmetrics object.

```
pathMetricsObj = pathmetrics(path,statevalidator);
```

Check path validity. The result is 1 (true) if the planned path is obstacle free. 0 (false) indicates an invalid path.

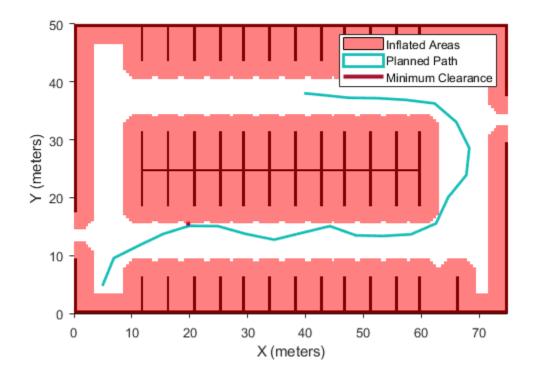
```
isPathValid(pathMetricsObj)
```

```
ans = logical
1
```

Compute and visualize the minimum clearance of the path.

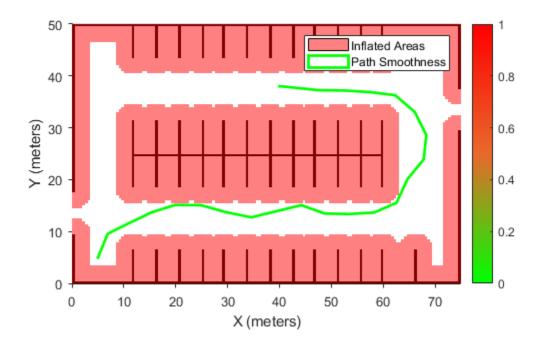
```
clearance(pathMetricsObj)
```

```
ans = 0.5000
show(pathMetrics0bj)
legend('Inflated Areas','Planned Path','Minimum Clearance')
xlabel('X (meters)')
ylabel('Y (meters)')
```



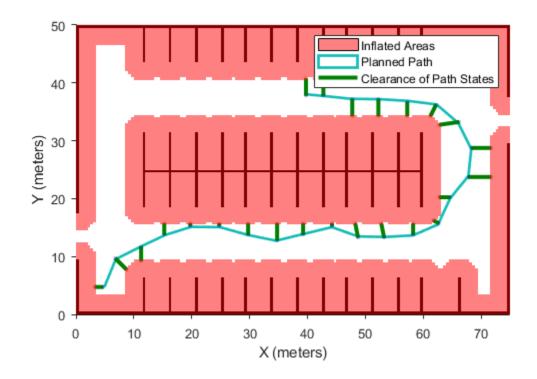
Compute and visualize the smoothness of the path. Values close to 0 indicate a smoother path. Straight-line paths return a value of 0.

```
smoothness(pathMetricsObj)
ans = 0.0842
show(pathMetricsObj,'Metrics',{'Smoothness'})
legend('Inflated Areas','Path Smoothness')
xlabel('X (meters)')
ylabel('Y (meters)')
```



Visualize the clearance for each state of the path.

```
show(pathMetricsObj,'Metrics',{'StatesClearance'})
legend('Inflated Areas','Planned Path','Clearance of Path States')
xlabel('X (meters)')
ylabel('Y (meters)')
```



Input Arguments

pathMetricsObj — Information for path metrics

pathmetrics object

Information for path metrics, specified as a pathmetrics object.

Name-Value Pair Arguments

Specify optional comma-separated pairs of Name, Value arguments. Name is the argument name and Value is the corresponding value. Name must appear inside quotes. You can specify several name and value pair arguments in any order as Name1, Value1, ..., NameN, ValueN.

Example: 'Parent', axHandle

Parent — Axes used to plot path

Axes object | UIAxes object

Axes used to plot path, specified as the comma-separated pair consisting of 'Parent' and either an axes or uiaxes object. If you do not specify Parent, a new figure is created.

Example: show(pathMetricsObj, 'Parent', axHandle)

Metrics — Display metrics option

cell array of strings

Display metrics option, specified as the comma-separated pair consisting of 'Metrics' and a cell array with any combination of these values:

- 'MinClearance' Display minimum clearance of path.
- 'StatesClearance' Display clearance of path states.
- 'Smoothness' Display path smoothness.

```
Example: show(pathMetricsObj,'Metrics',{'Smoothness','StatesClearance'})
Data Types: cell
```

Output Arguments

axHandle — Axes used to plot path

Axes object | UIAxes object

Axes used to plot path, returned as either an axes or uiaxes object.

See Also

Objects

pathmetrics

Functions

clearance|isPathValid|smoothness

Introduced in R2019b

smoothness

Smoothness of path

Syntax

```
smoothness(pathMetricsObj)
smoothness(pathMetricsObj,'Type','segments')
```

Description

smoothness(pathMetricsObj) evaluates the smoothness of the planned path. Values close to 0
indicate a smoother path. Straight-line paths return a value of 0.

smoothness (pathMetricsObj, 'Type', 'segments') returns individual smoothness calculations between each set of three poses on the path, in the form of a (n-2)-element vector, where n is the number of poses.

Examples

Compute Path Metrics

Compute smoothness, clearance, and validity of a planned path based on a set of poses and the associated map environment.

Load and Assign Map to State Validator

Create an occupancy map from an example map and set the map resolution.

Update the state space bounds to be the same as the map limits.

```
load exampleMaps.mat; % simpleMap
mapResolution = 1; % cells/meter
map = occupancyMap(simpleMap,mapResolution);

Create a Dubins state space.

statespace = stateSpaceDubins;

Create a state validator based on occupancy map to store the parameters and states in the Dubins state space.

statevalidator = validatorOccupancyMap(statespace);

Assign the map to the validator.

statevalidator.Map = map;

Set the validation distance for the validator.

statevalidator.ValidationDistance = 0.01;
```

```
statespace.StateBounds = [map.XWorldLimits;map.YWorldLimits;[-pi pi]];
```

Plan Path

Create an RRT* path planner and allow further optimization.

```
planner = plannerRRTStar(statespace, statevalidator);
planner.ContinueAfterGoalReached = true;
```

Reduce the maximum number of iterations and increase the maximum connection distance.

```
planner.MaxIterations = 2500;
planner.MaxConnectionDistance = 0.3;
```

Define start and goal states for the path planner as [x, y, theta] vectors. x and y are the Cartesian coordinates, and theta is the orientation angle.

```
start = [2.5, 2.5, 0]; % [meters, meters, radians]
goal = [22.5, 8.75, 0];
```

Plan a path from the start state to the goal state. The plan function returns a navPath object.

```
rng(100,'twister') % repeatable result
[path,solutionInfo] = plan(planner,start,goal);
```

Compute and Visualize Path Metrics

Create a path metrics object.

```
pathMetricsObj = pathmetrics(path,statevalidator);
```

Check path validity. The result is 1 (true) if the planned path is obstacle free. 0 (false) indicates an invalid path.

```
isPathValid(pathMetricsObj)
```

```
ans = logical
```

Calculate the minimum clearance of the path.

```
clearance(pathMetricsObj)
```

```
ans = 1.4142
```

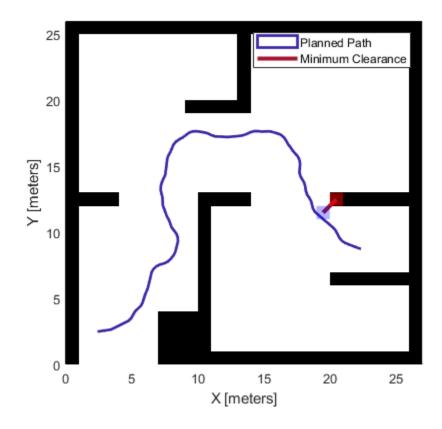
Evaluate the smoothness of the path. Values close to θ indicate a smoother path. Straight-line paths return a value of θ .

```
smoothness(pathMetricsObj)
```

```
ans = 1.7318
```

Visualize the minimum clearance of the path.

```
show(pathMetricsObj)
legend('Planned Path','Minimum Clearance')
```



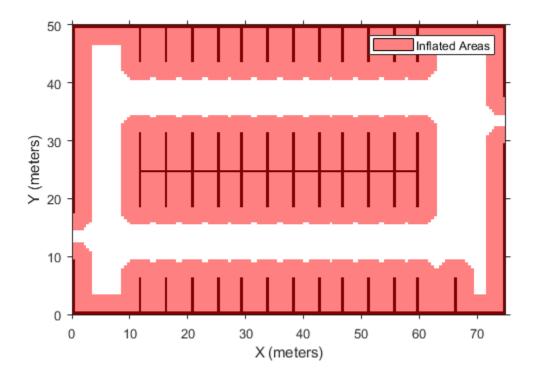
Vehicle Path Planning and Metrics Computation in a 2-D Costmap Environment

Plan a vehicle path through a parking lot using the RRT* algorithm. Compute and visualize the smoothness, clearance, and validity of the planned path.

Load and Assign Map to State Validator

Load a costmap of a parking lot. Plot the costmap to see the parking lot and the inflated areas that the vehicle should avoid.

```
load parkingLotCostmap.mat;
costmap = parkingLotCostmap;
plot(costmap)
xlabel('X (meters)')
ylabel('Y (meters)')
```



Create a stateSpaceDubins object and increase the minimum turing radius to 4 meters.

```
statespace = stateSpaceDubins;
statespace.MinTurningRadius = 4; % meters
```

Create a validatorVehicleCostmap object using the created state space.

```
statevalidator = validatorVehicleCostmap(statespace);
```

Assign the parking lot costmap to the state validator object.

```
statevalidator.Map = costmap;
```

Plan Path

Define start and goal poses for the vehicle as $[x, y, \theta]$ vectors. World units for the (x,y) locations are in meters. World units for the orientation angles θ are in degrees.

```
startPose = [5, 5, 90]; % [meters, meters, degrees]
goalPose = [40, 38, 180]; % [meters, meters, degrees]
```

Use a pathPlannerRRT (Automated Driving Toolbox) object and the plan (Automated Driving Toolbox) function to plan the vehicle path from the start pose to the goal pose.

```
planner = pathPlannerRRT(costmap);
refPath = plan(planner, startPose, goalPose);
```

Interpolate along the path at every one meter. Convert the orientation angles from degrees to radians.

```
poses = zeros(size(refPath.PathSegments,2)+1,3);
poses(1,:) = refPath.StartPose;
for i = 1:size(refPath.PathSegments,2)
        poses(i+1,:) = refPath.PathSegments(i).GoalPose;
end
poses(:,3) = deg2rad(poses(:,3));
```

Create a navPath object using the Dubins state space object and the states specified by poses.

```
path = navPath(statespace,poses);
```

Compute and Visualize Path Metrics

Create a pathmetrics object.

```
pathMetricsObj = pathmetrics(path,statevalidator);
```

Check path validity. The result is 1 (true) if the planned path is obstacle free. 0 (false) indicates an invalid path.

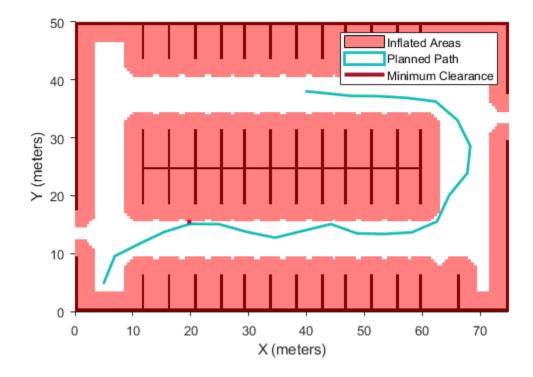
```
isPathValid(pathMetricsObj)
ans = logical
```

1

Compute and visualize the minimum clearance of the path.

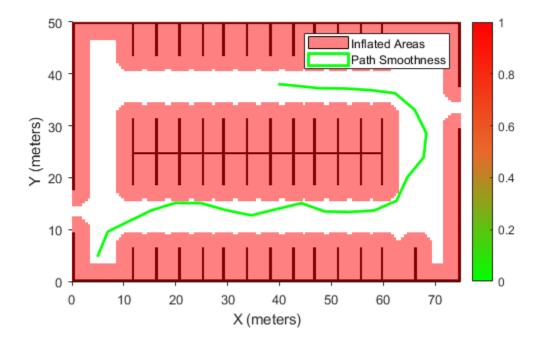
```
clearance(pathMetricsObj)
```

```
ans = 0.5000
show(pathMetrics0bj)
legend('Inflated Areas','Planned Path','Minimum Clearance')
xlabel('X (meters)')
ylabel('Y (meters)')
```



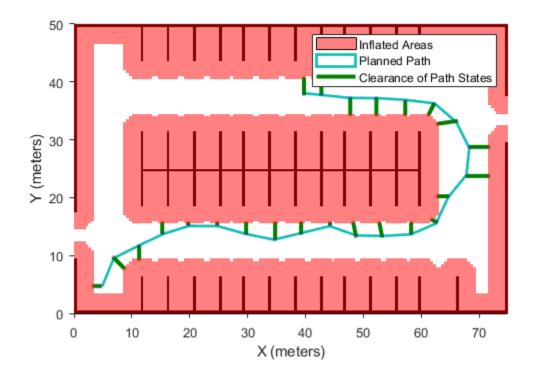
Compute and visualize the smoothness of the path. Values close to 0 indicate a smoother path. Straight-line paths return a value of 0.

```
smoothness(pathMetricsObj)
ans = 0.0842
show(pathMetricsObj,'Metrics',{'Smoothness'})
legend('Inflated Areas','Path Smoothness')
xlabel('X (meters)')
ylabel('Y (meters)')
```



Visualize the clearance for each state of the path.

```
show(pathMetricsObj,'Metrics',{'StatesClearance'})
legend('Inflated Areas','Planned Path','Clearance of Path States')
xlabel('X (meters)')
ylabel('Y (meters)')
```



Input Arguments

pathMetricsObj — Information for path metrics

pathmetrics object

Information for path metrics, specified as a pathmetrics object.

References

[1] Lindemann, Stephen R., and Steven M. LaValle. "Simple and efficient algorithms for computing smooth, collision-free feedback laws over given cell decompositions." *The International Journal of Robotics Research 28, no. 5.* 2009, pp. 600-621.

See Also

Objects

pathmetrics

Functions

clearance|isPathValid|show

Introduced in R2019b

plannerAStarGrid

A* path planner for grid map

Description

The plannerAStarGrid object creates an A* path planner. The planner performs an A* search on an occupancy map and finds shortest obstacle-free path between the specified start and goal grid locations as determined by heuristic cost.

Creation

Syntax

```
planner = plannerAStarGrid
planner = plannerAStarGrid(map)
planner = plannerAStarGrid(____, Name, Value)
```

Description

planner = plannerAStarGrid creates a plannerAStarGrid object with a
binaryOccupancyMap object using a width and height of 10 meters and grid resolution of 1 cell per
meter.

planner = plannerAStarGrid(map) creates a plannerAStarGrid object using the specified map object map. Specify map as either a binaryOccupancyMap or occupancyMap object. The map input sets the value of the Map property.

planner = plannerAStarGrid(____, Name, Value) sets properties using one or more name-value pairs. Unspecified properties have default values. Enclose each property name in quotes.

For example, plannerAStarGrid(map, 'GCost', 'Manhattan') creates an A* path planner object using the Manhattan cost function.

Properties

Map — Map representation

binaryOccupancyMap object (default) | occupancyMap object

Map representation, specified as either a binaryOccupancyMap or occupancyMap object. This object represents the environment of the robot as an occupancy grid. The value of each grid cell indicates the occupancy of the associated location in the map.

```
Example: planner.Map = binaryOccupancyMap(zeros(50,50));
```

GCost — General cost of moving between any two points in grid

```
'Euclidean' (default) | 'Chebyshev' | 'EulideanSquared' | 'Manhattan'
```

The general cost of moving between any two points in a grid, specified as one of the following predefined cost functions 'Chebyshev', 'Euclidean', 'EulideanSquared', or 'Manhattan'.

Note You can either use the predefined cost functions or a custom cost function. To use a custom cost function, see GCostFcn property.

```
Example: planner = plannerAStarGrid(map, 'GCost', 'Manhattan');
Example: planner.GCost = 'Chebyshev';
Data Types: string | char
```

GCostFcn — Custom GCost function

function handle

Custom GCost function, specified as a function handle. The function handle must accept two pose inputs as a [row column] vectors and return a scalar of type double.

Note You can either use the predefined cost functions or a custom cost function. To use the predefined cost functions, see GCost property.

```
Example: planner = plannerAStarGrid(map, 'GCostFcn',@(pose1,pose2)sum(abs(pose1-pose2),2));
Example: planner.GCostFcn = @(pose1,pose2)sum(abs(pose1-pose2),2);
Data Types: function_handle
```

HCost — Heuristic cost between point and goal in grid

```
'Euclidean' (default) | 'Chebyshev' | 'EulideanSquared' | 'Manhattan'
```

The heuristic cost between a point and the goal in a grid, specified as one of the following predefined cost functions 'Chebyshev', 'Euclidean', 'EulideanSquared', or 'Manhattan'.

Note You can either use the predefined cost functions or a custom cost function. To use a custom cost function, see HCostFcn property.

```
Example: planner = plannerAStarGrid(map, 'HCost', 'Manhattan');
Example: planner.HCost = 'Chebyshev';
Data Types: string | char
```

HCostFcn — Custom HCost function

function handle

Custom HCost function, specified as a function handle. The function handle must accept two pose inputs as a [row column] vectors and return a scalar of type double.

Note You can either use the predefined cost functions or a custom cost function. To use the predefined cost functions, see HCost property.

```
Example: planner = plannerAStarGrid(map, 'HCostFcn',@(pose1,pose2)sum(abs(pose1-pose2),2));
Example: planner.HCostFcn = @(pose1,pose2)sum(abs(pose1-pose2),2);
Data Types: function handle
```

TieBreaker - Toggle tiebreaker mode

```
'off' (default) | 'on'
```

Toggle tiebreaker mode, specified as either 'on' or 'off'.

When you enable the TieBreaker property, the A* path planner chooses between multiple paths of the same length by adjusting the heuristic cost value.

```
Example: planner = plannerAStarGrid(map, 'TieBreaker', 'on');
Example: planner.TieBreaker = 'off';
Data Types: string | char
```

Object Functions

plan Find shortest obstacle-free path between two points show Plot and visualize A* explored nodes and planned path

Examples

Plan Obstacle-Free Path in Grid Map Using A-Star Path Planner

Plan the shortest collision-free path through an obstacle grid map using the A* path planning algorithm.

Generate a binaryOccupancyMap object with randomly scattered obstacles using the mapClutter function.

```
rng('default');
map = mapClutter;

Use the map to create a plannerAStarGrid object.

planner = plannerAStarGrid(map);

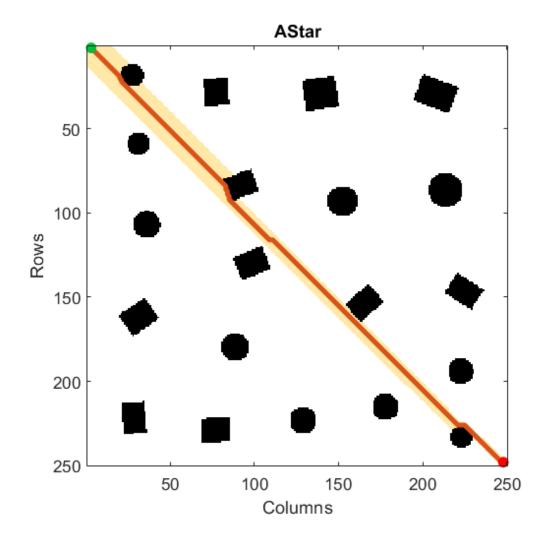
Define the start and goal points.

start = [2 3];
goal = [248 248];

Plan a path from the start point to the goal point.

plan(planner, start, goal);

Visualize the path and the explored nodes using the show object function.
show(planner)
```



Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

 $\label{lem:binaryOccupancyMap|plannerHybridAStar|plannerRRT|plannerRRTStar} binaryOccupancyMap|plannerHybridAStar|plannerRRTStar$

Introduced in R2020b

plan

Find shortest obstacle-free path between two points

Syntax

```
path = plan(planner,start,goal)
path = plan(planner,start,goal,'world')
[path,debugInfo] = plan( )
```

Description

path = plan(planner, start, goal) finds the shortest obstacle-free path, path, between a specified start point, start, and goal point, goal, specified as [row column] in grid frame with origin at top-left corner, using the specified A* path planner planner.

path = plan(planner, start, goal, 'world') finds the shortest obstacle-free path, path,
between a specified start point, start, and goal point, goal, specified as [x y] in world coordinate
frame with origin at bottom-left corner, using the specified A* path planner planner.

[path,debugInfo] = plan(____) also returns debugInfo that contains the path cost, number of nodes explored, and GCost for each explored node.

Examples

Plan Obstacle-Free Path in Grid Map Using A-Star Path Planner

Plan the shortest collision-free path through an obstacle grid map using the A* path planning algorithm.

Generate a binaryOccupancyMap object with randomly scattered obstacles using the mapClutter function.

```
rng('default');
map = mapClutter;

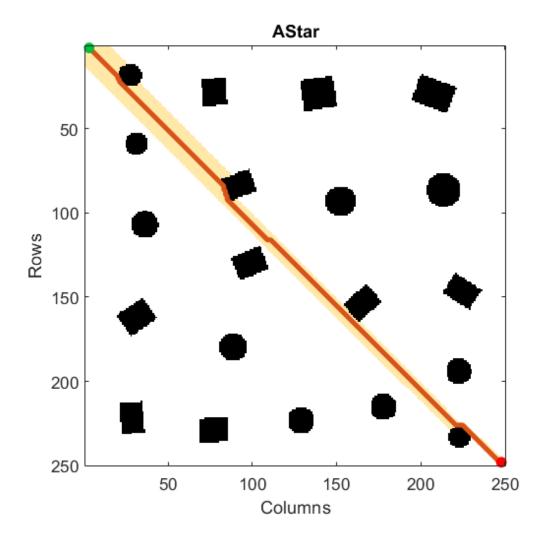
Use the map to create a plannerAStarGrid object.
planner = plannerAStarGrid(map);

Define the start and goal points.

start = [2 3];
goal = [248 248];

Plan a path from the start point to the goal point.
plan(planner, start, goal);

Visualize the path and the explored nodes using the show object function.
show(planner)
```



Input Arguments

planner — A* path planner for grid map

plannerAStarGrid object

A* path planner for a grid map, specified as a plannerAStarGrid object.

start — Start position in grid or world

two-element vector

Start position in the grid or world, specified as a two-element vector of the form [$row\ column$], or [x y]. The location is in grid positions or world coordinates based on syntax.

Example: [2 3]
Data Types: double

goal — Goal position in grid or world

two-element vector

Goal position in the grid or world, specified as a two-element vector of the form [$row\ column$], or [x y]. The location is in grid positions or world coordinates based on syntax.

Example: [28 46]
Data Types: double

Output Arguments

path — Shortest obstacle-free path

n-by-2 matrix

Shortest obstacle-free path, returned as an n-by-2 matrix. n is the number of waypoints in the path. Each row represents the [$row\ column$], or [$x\ y$] location of a waypoint along the solved path from the start location to the goal. The location is in grid positions or world coordinates based on syntax.

Data Types: double

debugInfo — Debugging information for path result

structure

Debugging information for the path result, returned as a structure with these fields:

- PathCost Cost of the path
- $\bullet \quad {\tt NumNodesExplored} {\tt Number} \ {\tt of} \ {\tt nodes} \ {\tt explored} \\$
- GCostMatrix GCost for each explored node

Data Types: struct

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

plannerAStarGrid | show

Introduced in R2020b

show

Plot and visualize A* explored nodes and planned path

Syntax

```
show(planner)
axHandle = show(planner)
[____] = show(____,Name,Value)
```

Description

show(planner) plots and visualizes the A* explored nodes and the planned path in the associated map.

axHandle = show(planner) returns the axes handle of the figure used to plot the path.

[___] = show(___, Name, Value) specifies options using one or more name-value pair arguments in addition to any of the arguments from previous syntaxes. Enclose argument name inside single quotes ('').

For example, 'ExploredNodes', 'off' plots and visualizes the planned path without displaying the explored nodes.

Examples

Plan Obstacle-Free Path in Grid Map Using A-Star Path Planner

Plan the shortest collision-free path through an obstacle grid map using the A* path planning algorithm.

Generate a binaryOccupancyMap object with randomly scattered obstacles using the mapClutter function.

```
rng('default');
map = mapClutter;

Use the map to create a plannerAStarGrid object.
planner = plannerAStarGrid(map);

Define the start and goal points.

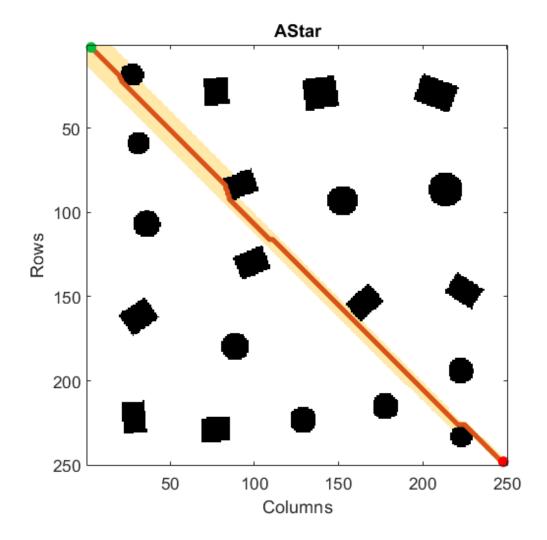
start = [2 3];
goal = [248 248];
```

Plan a path from the start point to the goal point.

```
plan(planner,start,goal);
```

Visualize the path and the explored nodes using the show object function.

show(planner)



Input Arguments

planner — A* path planner for grid map

plannerAStarGrid object

A* path planner for a grid map, specified as a plannerAStarGrid object.

Name-Value Pair Arguments

Specify optional comma-separated pairs of Name, Value arguments. Name is the argument name and Value is the corresponding value. Name must appear inside quotes. You can specify several name and value pair arguments in any order as Name1, Value1, . . . , NameN, ValueN.

Example: 'ExploredNodes', 'off' plots and visualizes the planned path without displaying the explored nodes.

Parent — Axes used to plot path

Axes object | UIAxes object

Axes used to plot path, specified as the comma-separated pair consisting of 'Parent' and either an Axes or UIAxes object. If you do not specify Parent, a new figure is created.

Example: 'Parent', axHandle

ExploredNodes — Display explored nodes

'on' (default) | 'off'

Display the explored nodes, specified as the comma-separated pair consisting of 'ExploredNodes' and either 'on' or 'off'.

Example: 'ExploredNodes','off'

Data Types: string | char

Output Arguments

axHandle — Axes used to plot path

Axes object | UIAxes object

Axes used to plot the path, returned as an Axes or UIAxes object.

See Also

plan | plannerAStarGrid

Introduced in R2020b

plannerBiRRT

Create bidirectional RRT planner for geometric planning

Description

The plannerBiRRT object is a single-query planner that uses the bidirectional rapidly exploring random tree (RRT) algorithm with an optional connect heuristic for increased speed.

The bidirectional RRT planner creates one tree with a root node at the specified start state and another tree with a root node at the specified goal state. To extend each tree, the planner generates a random state and, if valid, takes a step from the nearest node based on the MaxConnectionDistance property. The start and goal trees alternate this extension process until both trees are connected. If the EnableConnectHeuristic property is enabled, the extension process ignores the MaxConnectionDistance property. Invalid states or connections that collide with the environment are not added to the tree.

Creation

Syntax

planner = plannerBiRRT(stateSpace, stateVal)

Description

planner = plannerBiRRT(stateSpace, stateVal) creates a bidirectional RRT planner from a state space object, stateSpace, and a state validator object, stateVal. The state space of stateVal must be the same as stateSpace. The stateSpace and stateVal arguments also set the StateSpace and StateValidator properties, respectively, of the planner.

Properties

StateSpace — State space for planner

state space object

State space for the planner, specified as a state space object. You can use state space objects such as stateSpaceSE2, stateSpaceDubins, and stateSpaceReedsShepp. You can also customize a state space object using the nav.StateSpace class.

StateValidator — State validator for planner

state validator object

State validator for the planner, specified as a state validator object. You can use state validator objects such as validatorOccupancyMap and validatorVehicleCostmap.

MaxConnectionDistance — Maximum length between planned configurations

0.1 (default) | positive scalar

Maximum length between planned configurations, specified as a positive scalar.

If the EnableConnectHeuristic property is set to true, the object ignores this distance when connecting the two trees during the connect stage.

Data Types: single | double

MaxIterations — Maximum number of iterations

1e4 (default) | positive integer

Maximum number of iterations, specified as a positive integer.

Data Types: single | double

MaxNumTreeNodes — Maximum number of nodes in search tree

1e4 (default) | positive integer

Maximum number of nodes in the search tree, specified as a positive integer.

Data Types: single | double

EnableConnectHeuristic — Directly join trees during connect phase

false or 0 (default) | true or 1

Directly join trees during the connect phase of the planner, specified as a logical 0 (false) or 1 (true).

Setting this property to true causes the object to ignore the MaxConnectionDistance property when attempting to connect the two trees together.

Data Types: logical

Object Functions

plan Plan path between two states copy Create deep copy of planner object

Examples

Plan Path Between Two States Using Bidirectional RRT

Use the plannerBiRRT object to plan a path between two states in an environment with obstacles. Visualize the planned path with interpolated states.

Create a state space.

```
ss = stateSpaceSE2;
```

Create an occupancyMap-based state validator using the created state space.

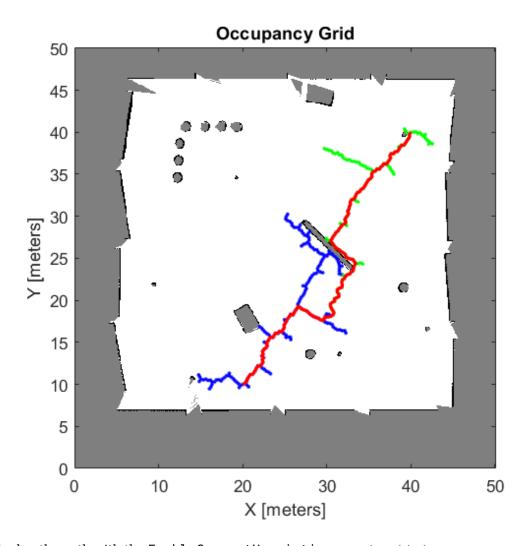
```
sv = validatorOccupancyMap(ss);
```

Create an occupancy map from an example map and set map resolution as 10 cells per meter.

```
load exampleMaps
map = occupancyMap(ternaryMap,10);
sv.Map = map;
```

Set the validation distance for the validator.

```
sv.ValidationDistance = 0.01;
Update the state space bounds to be the same as the map limits.
ss.StateBounds = [map.XWorldLimits; map.YWorldLimits; [-pi pi]];
Create the path planner and increase the maximum connection distance.
planner = plannerBiRRT(ss,sv);
planner.MaxConnectionDistance = 0.3;
Specify the start and goal states.
start = [20 \ 10 \ 0];
qoal = [40 \ 40 \ 0];
Plan a path. Due to the randomness of the RRT algorithm, set the rng seed for repeatability.
rng(100,'twister')
[pthObj,solnInfo] = plan(planner,start,goal);
Display the number of iterations taken for the tree to converge.
fprintf('Number of iterations: %d\n',solnInfo.NumIterations)
Number of iterations: 346
Visualize the results.
show(map)
hold on
 \verb|plot(solnInfo.StartTreeData(:,1),solnInfo.StartTreeData(:,2),'.-','color','b')| % Start tree expansion of the expansion 
plot(pthObj.States(:,1),pthObj.States(:,2),'r-','LineWidth',2) % draw path
hold off
```



Replan the path with the EnableConnectHeuristic property set to true.

fprintf('Number of iterations: %d\n',solnInfo.NumIterations)

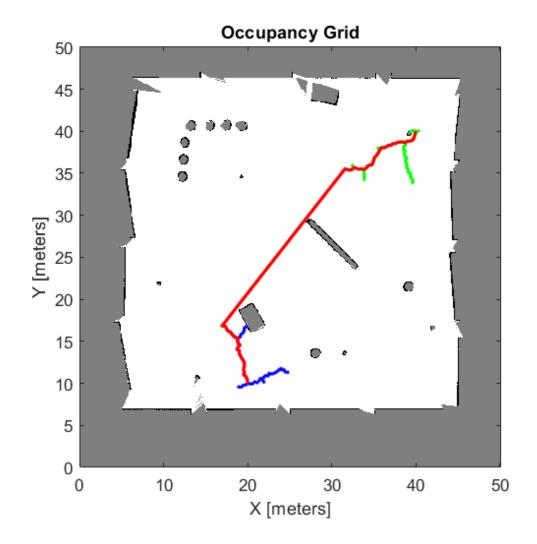
```
planner.EnableConnectHeuristic = true;
[pth0bj,solnInfo] = plan(planner,start,goal);
```

Number of iterations: 135

Display the number of iterations taken for the tree to converge. Observe that the planner requires significantly fewer iterations compared to when the <code>EnableConnectHeuristic</code> property is set to false.

```
Visualize the results.

figure 
show(map) 
hold on 
plot(solnInfo.StartTreeData(:,1),solnInfo.StartTreeData(:,2),'.-','color','b') % Start tree expa 
plot(solnInfo.GoalTreeData(:,1),solnInfo.GoalTreeData(:,2),'.-','color','g') % Goal tree expansion 
plot(pthObj.States(:,1),pthObj.States(:,2),'r-','LineWidth',2) % draw path
```



References

[1] Kuffner, J. J., and S. M. LaValle. "RRT-Connect: An Efficient Approach to Single-Query Path Planning." In *Proceedings 2000 ICRA*. *Millennium Conference*. *IEEE International Conference on Robotics and Automation*. *Symposia Proceedings (Cat. No.00CH37065)*, 2:995–1001. San Francisco, CA, USA: IEEE, 2000. https://doi:10.1109/ROBOT.2000.844730.

See Also

Objects

plannerRRT | plannerRRTStar

Functions

copy | plan

Introduced in R2021a

copy

Create deep copy of planner object

Syntax

plannerCopy = copy(planner)

Description

plannerCopy = copy(planner) creates a deep copy of the planner object with the same
properties.

Input Arguments

planner — Path planner

plannerBiRRT object

Path planner, specified as a plannerBiRRT object.

Output Arguments

plannerCopy — Copy of path planner

plannerBiRRT object

Copy of path planner, returned as a plannerBiRRT object.

See Also

Objects

plannerBiRRT

Functions

plan

Introduced in R2021a

plan

Plan path between two states

Syntax

```
path = plan(planner,startState,goalState)
[path,solnInfo] = plan(planner,startState,goalState)
```

Description

path = plan(planner, startState, goalState) returns a bidirectional rapidly exploring random tree (RRT) path from the start state to the goal state as a navPath object.

[path,solnInfo] = plan(planner,startState,goalState) also returns the solution
information from path planning.

Examples

Plan Path Between Two States Using Bidirectional RRT

Use the plannerBiRRT object to plan a path between two states in an environment with obstacles. Visualize the planned path with interpolated states.

```
Create a state space.

ss = stateSpaceSE2;

Create an occupancyMap-based state validator using the created state space.

sv = validatorOccupancyMap(ss);

Create an occupancy map from an example map and set map resolution as 10 cells per meter.

load exampleMaps
map = occupancyMap(ternaryMap,10);
sv.Map = map;

Set the validation distance for the validator.

sv.ValidationDistance = 0.01;

Update the state space bounds to be the same as the map limits.

ss.StateBounds = [map.XWorldLimits; map.YWorldLimits; [-pi pi]];

Create the path planner and increase the maximum connection distance.

planner = plannerBiRRT(ss,sv);
planner.MaxConnectionDistance = 0.3;
```

Specify the start and goal states.

```
start = [20 10 0];
goal = [40 40 0];
```

Plan a path. Due to the randomness of the RRT algorithm, set the rng seed for repeatability.

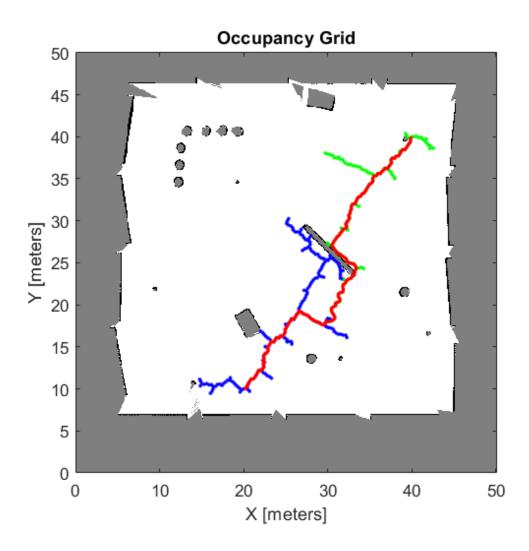
```
rng(100, 'twister')
[pth0bj,solnInfo] = plan(planner,start,goal);
```

Display the number of iterations taken for the tree to converge.

```
fprintf('Number of iterations: %d\n', solnInfo.NumIterations)
Number of iterations: 346
```

Visualize the results.

```
show(map)
hold on
plot(solnInfo.StartTreeData(:,1),solnInfo.StartTreeData(:,2),'.-','color','b') % Start tree expansion
plot(solnInfo.GoalTreeData(:,1),solnInfo.GoalTreeData(:,2),'.-','color','g') % Goal tree expansion
plot(pthObj.States(:,1),pthObj.States(:,2),'r-','LineWidth',2) % draw path
hold off
```



Replan the path with the EnableConnectHeuristic property set to true.

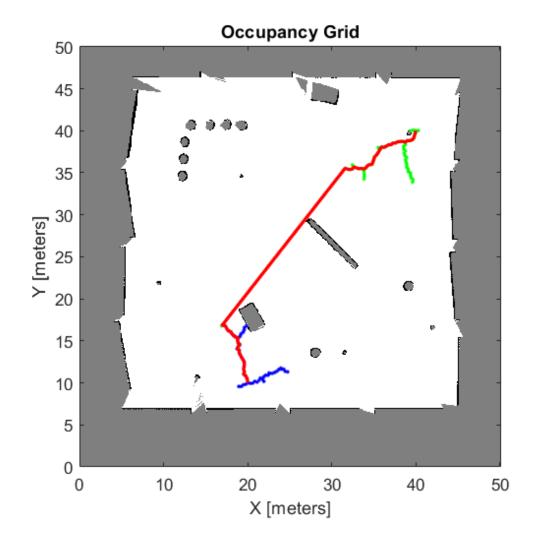
```
planner.EnableConnectHeuristic = true;
[pthObj,solnInfo] = plan(planner,start,goal);
```

Display the number of iterations taken for the tree to converge. Observe that the planner requires significantly fewer iterations compared to when the <code>EnableConnectHeuristic</code> property is set to false.

```
fprintf('Number of iterations: %d\n',solnInfo.NumIterations)
Number of iterations: 135
```

Visualize the results.

```
figure
show(map)
hold on
plot(solnInfo.StartTreeData(:,1),solnInfo.StartTreeData(:,2),'.-','color','b') % Start tree expansion
plot(solnInfo.GoalTreeData(:,1),solnInfo.GoalTreeData(:,2),'.-','color','g') % Goal tree expansion
plot(pthObj.States(:,1),pthObj.States(:,2),'r-','LineWidth',2) % draw path
```



Input Arguments

planner — Path planner

plannerBiRRT object

Path planner, specified as a plannerBiRRT object.

startState — Start state of path

N-element real-valued vector

Start state of the path, specified as an N-element real-valued vector. N is the number of dimensions in the state space.

Example: [1 1 pi/6]

Data Types: single | double

goalState — Goal state of path

N-element real-valued vector

Goal state of the path, specified as an N-element real-valued vector. N is the number of dimensions in the state space.

Example: [2 2 pi/3]

Data Types: single | double

Output Arguments

path — Planned path information

navPath object

Planned path information, returned as a navPath object.

solnInfo — Solution Information

structure

Solution Information, returned as a structure. The structure contains these fields:

Field	Description
IsPathFound	Indicates whether a path is found. It returns 1 (true) if a path is found. Otherwise, it returns 0 (false).
ExitFlag	Indicates the termination cause of the planner, returned as: • 1 — The planner reaches the goal. • 2 — The planner reaches the maximum
	number of iterations.
	3 — The planner reaches the maximum number of nodes.

Field	Description
StartTreeNumNodes	Number of nodes in the start search tree when the planner terminates, excluding the root node.
GoalTreeNumNodes	Number of nodes in the goal search tree when the planner terminates, excluding the root node.
NumIterations	Number of combined iterations by both the start tree and goal tree.
StartTreeData	Collection of explored states that reflect the status of the start search tree when the planner terminates. Note that NaN values are inserted as delimiters to separate each individual edge.
GoalTreeData	Collection of explored states that reflect the status of the goal search tree when the planner terminates. Note that NaN values are inserted as delimiters to separate each individual edge.

Data Types: structure

See Also

Objects navPath | plannerBiRRT

Functions

сору

Introduced in R2021a

plannerHybridAStar

Hybrid A* path planner

Description

The Hybrid A* path planner object generates a smooth path in a given 2-D space for vehicles with nonholonomic constraints.

Note The Hybrid A* planner checks for collisions in the map by interpolating the motion primitives and analytic expansion based on the ValidationDistance property of the stateValidator object. If the ValidationDistance property is set to Inf, the object interpolates based on the cell size of the map specified in the state validator. Inflate the occupancy map before assigning it to the planner to account for the vehicle size.

Creation

Syntax

```
planner = plannerHybridAStar(validator)
planner = plannerHybridAStar(validator,Name,Value)
```

Description

planner = plannerHybridAStar(validator) creates a path planner object using the Hybrid A* algorithm. Specify the validator input as a validatorOccupancyMap or validatorVehicleCostmap object. The validator input sets the value of the "StateValidator" on page 2-0 property.

planner = plannerHybridAStar(validator,Name,Value) sets "Properties" on page 2-851 of the path planner by using one or more name-value pair arguments. Enclose each property name inside single quotes ('').

Properties

StateValidator — State validator for planning

validatorOccupancyMap object | validatorVehicleCostmap object

State validator for planning, specified either as a validatorOccupancyMap or validatorVehicleCostmap object based on SE(2) state space.

MotionPrimitiveLength — Length of motion primitives to be generated

ceil(sqrt(2)*map_CellSize) (default) | positive scalar

Length of motion primitives to be generated, specified as the comma-separated pair consisting of 'MotionPrimitiveLength' and a positive scalar in meters. Increase the length for large maps or sparse environments. Decrease the length for dense environments.

Note 'MotionPrimitiveLength' cannot exceed one-fourth the length of the circumference of a circle based on the 'MinTurningRadius'.

Data Types: double

MinTurningRadius — Minimum turning radius of vehicle

(2*motion primitive length)/pi (default) | positive scalar

Minimum turning radius of vehicle, specified as the comma-separated pair consisting of 'MinTurningRadius' and a positive scalar in meters.

Note The value of 'MinTurningRadius' is set such that the 'MotionPrimitiveLength' cannot exceed one-fourth the length of the circumference of a circle based on it.

Data Types: double

NumMotionPrimitives — Number of motion primitives to be generated

5 (default) | positive odd integer scalar

Number of motion primitives to be generated, specified as the comma-separated pair consisting of 'NumMotionPrimitives' and a positive odd integer scalar.

ForwardCost — Cost multiplier to travel in forward direction

1 (default) | positive scalar

Cost multiplier to travel in forward direction, specified as the comma-separated pair consisting of 'ForwardCost' and a positive scalar. Increase the cost value to penalize forward motion.

Data Types: double

ReverseCost — Cost multiplier to travel in reverse direction

3 (default) | positive scalar

Cost multiplier to travel in reverse direction, specified as the comma-separated pair consisting of 'ReverseCost' and a positive scalar. Increase the cost value to penalize reverse motion.

Data Types: double

DirectionSwitchingCost — Additive cost for switching direction of motion

0 (default) | positive scalar

Additive cost for switching direction of motion, specified as the comma-separated pair consisting of 'DirectionSwitchingCost' and a positive scalar. Increase the cost value to penalize direction switching.

Data Types: double

AnalyticExpansionInterval — Interval for attempting analytic expansion from lowest cost node available

5 (default) | positive integer scalar

Interval for attempting analytic expansion from the lowest cost node available at that instance, specified as the comma-separated pair consisting of 'AnalyticExpansionInterval' and a positive integer scalar.

The Hybrid A* path planner expands the motion primitives from the nodes with the lowest cost available at that instance:

- The number of nodes to be expanded depends upon the number of primitives to be generated in both the direction and their validity, the cycle repeats until 'AnalyticExpansionInterval' is reached.
- The planner then attempts an analytic expansion to reach the goal pose from the tree using a Reeds-Shepp model. If the attempt fails, the planner repeats the cycle.

Improve the algorithm performance by reducing the interval to increase the number of checks for a Reeds-Shepp connection to the final goal.

InterpolationDistance — Distance between interpolated poses in output path 1 (default) | positive scalar

Distance between interpolated poses in output path, specified as the comma-separated pair consisting of 'InterpolationDistance' and a positive scalar in meters.

Data Types: double

Object Functions

plan Find obstacle-free path between two poses show Visualize the planned path

Examples

Obstacle-Free Path Planning Using Hybrid A Star

Plan a collision-free path for a vehicle through a parking lot by using the Hybrid A* algorithm.

Create and Assign Map to State Validator

Load the cost values of cells in the vehicle costmap of a parking lot.

```
load parkingLotCostVal.mat % costVal
```

Create a binaryOccupancyMap with cost values.

```
map = binaryOccupancyMap(costVal);
```

Create a state validator object for collision checking.

```
validator = validatorOccupancyMap;
```

Assign the map to the state validator object.

```
validator.Map = map;
```

Plan and Visualize Path

Initialize the plannerHybridAStar object with the state validator object. Specify the MinTurningRadius and MotionPrimitiveLength properties of the planner.

```
planner = plannerHybridAStar(validator, 'MinTurningRadius', 4, 'MotionPrimitiveLength', 6);
```

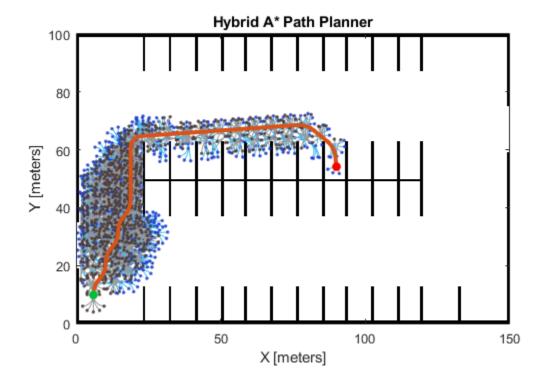
Define start and goal poses for the vehicle as [x, y, theta] vectors. x and y specify the position in meters, and theta specifies the orientation angle in radians.

```
startPose = [6 10 pi/2]; % [meters, meters, radians]
goalPose = [90 54 -pi/2];
Plan a path from the start pose to the goal pose.
```

refpath = plan(planner,startPose,goalPose);

Visualize the path using show function.

show(planner)



References

- [1] Dolgov, Dmitri, Sebastian Thrun, Michael Montemerlo, and James Diebel. *Practical Search Techniques in Path Planning for Autonomous Driving*. American Association for Artificial Intelligence, 2008.
- [2] Petereit, Janko, Thomas Emter, Christian W. Frey, Thomas Kopfstedt, and Andreas Beutel.

 "Application of Hybrid A* to an Autonomous Mobile Robot for Path Planning in Unstructured Outdoor Environments." *ROBOTIK 2012: 7th German Conference on Robotics*. 2012, pp. 1-6.

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

navPath | validatorOccupancyMap | validatorVehicleCostmap

Introduced in R2019b

plan

Find obstacle-free path between two poses

Syntax

```
path = plan(planner, start, goal)
```

Description

path = plan(planner, start, goal) computes an obstacle-free path between start and goal
poses, specified as [x y theta] vectors, using the input plannerHybridAStar object.

Examples

Obstacle-Free Path Planning Using Hybrid A Star

Plan a collision-free path for a vehicle through a parking lot by using the Hybrid A* algorithm.

Create and Assign Map to State Validator

Load the cost values of cells in the vehicle costmap of a parking lot.

```
load parkingLotCostVal.mat % costVal
```

Create a binaryOccupancyMap with cost values.

```
map = binaryOccupancyMap(costVal);
```

Create a state validator object for collision checking.

```
validator = validatorOccupancyMap;
```

Assign the map to the state validator object.

```
validator.Map = map;
```

Plan and Visualize Path

Initialize the plannerHybridAStar object with the state validator object. Specify the MinTurningRadius and MotionPrimitiveLength properties of the planner.

```
planner = plannerHybridAStar(validator, 'MinTurningRadius', 4, 'MotionPrimitiveLength', 6);
```

Define start and goal poses for the vehicle as [x, y, theta] vectors. x and y specify the position in meters, and theta specifies the orientation angle in radians.

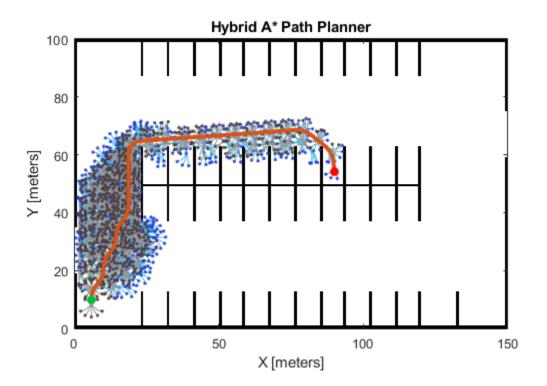
```
startPose = [6 10 pi/2]; % [meters, meters, radians]
goalPose = [90 54 -pi/2];
```

Plan a path from the start pose to the goal pose.

```
refpath = plan(planner,startPose,goalPose);
```

Visualize the path using show function.

show(planner)



Input Arguments

planner — Hybrid A* path planner

plannerHybridAStar object

Hybrid A* path planner, specified as a plannerHybridAStar object.

start — Start location of path

three-element vector

Start location of path, specified as a 1-by-3 vector in the form $[x \ y \ theta]$. x and y specify the position in meters, and theta specifies the orientation angle in radians.

Example: [5 5 pi/2]
Data Types: double

goal — Final location of path

three-element vector

Final location of path, specified as a 1-by-3 vector in the form $[x \ y \ theta]$. x and y specify the position in meters, and theta specifies the orientation angle in radians.

Example: [45 45 pi/4] Data Types: double

Output Arguments

path — Obstacle-free path

navPath object

Obstacle-free path, returned as a navPath object.

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder $^{\text{\tiny TM}}$.

See Also

navPath | validatorOccupancyMap | validatorVehicleCostmap

Introduced in R2019b

show

Visualize the planned path

Syntax

```
show(planner)
show(planner,Name,Value)
axHandle = show(planner)
```

Description

show(planner) plots the Hybrid A* expansion tree and the planned path in the map.

show(planner, Name, Value) specifies additional options using one or more name-value pair arguments.

axHandle = show(planner) outputs the axes handle of the figure used to plot the path.

Examples

Obstacle-Free Path Planning Using Hybrid A Star

Plan a collision-free path for a vehicle through a parking lot by using the Hybrid A* algorithm.

Create and Assign Map to State Validator

Load the cost values of cells in the vehicle costmap of a parking lot.

```
load parkingLotCostVal.mat % costVal
```

Create a binaryOccupancyMap with cost values.

```
map = binaryOccupancyMap(costVal);
```

Create a state validator object for collision checking.

```
validator = validatorOccupancyMap;
```

Assign the map to the state validator object.

```
validator.Map = map;
```

Plan and Visualize Path

Initialize the plannerHybridAStar object with the state validator object. Specify the MinTurningRadius and MotionPrimitiveLength properties of the planner.

```
planner = plannerHybridAStar(validator, 'MinTurningRadius', 4, 'MotionPrimitiveLength', 6);
```

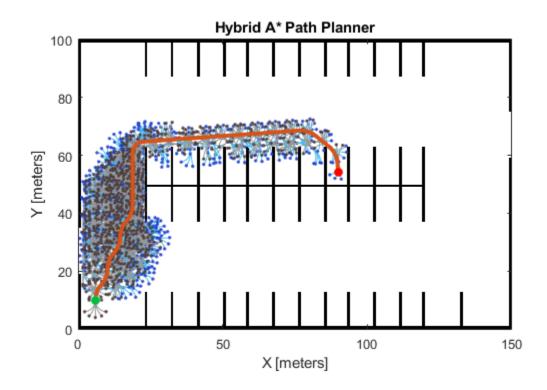
Define start and goal poses for the vehicle as [x, y, theta] vectors. x and y specify the position in meters, and theta specifies the orientation angle in radians.

```
startPose = [6 10 pi/2]; % [meters, meters, radians]
goalPose = [90 54 -pi/2];

Plan a path from the start pose to the goal pose.

refpath = plan(planner, startPose, goalPose);

Visualize the path using show function.
show(planner)
```



Input Arguments

planner — Hybrid A* path planner

plannerHybridAStar object

Hybrid A* path planner, specified as a plannerHybridAStar object.

Name-Value Pair Arguments

Specify optional comma-separated pairs of Name, Value arguments. Name is the argument name and Value is the corresponding value. Name must appear inside quotes. You can specify several name and value pair arguments in any order as Name1, Value1, . . . , NameN, ValueN.

```
Example: 'Positions', 'none'
```

Parent — Axes used to plot path

Axes object | UIAxes object

Axes used to plot path, specified as the comma-separated pair consisting of 'Parent' and either an axes or uiaxes object. If you do not specify 'Parent', a new figure is created.

Tree — Display expansion tree

```
'on' (default) | 'off'
```

Display expansion tree option, specified as the comma-separated pair consisting of 'Tree' and either 'on' or 'off'.

```
Example: show(planner, 'Tree', 'off')
Data Types: string
```

Path — Display planned path

```
'on' (default) | 'off'
```

Display planned path option, specified as the comma-separated pair consisting of 'Path' and either 'on' or 'off'.

```
Example: show(planner, 'Path', 'off')
Data Types: string
```

Positions — Display start and goal points

```
'both' (default) | 'start' | 'goal' | 'none'
```

Display the start and goal points, specified as the comma-separated pair consisting of 'Positions' and one of the following:

- 'start' Display the start point.
- 'goal' Display the goal point.
- 'both' Display the start and goal points.
- 'none' Do not display any points.

```
Example: show(planner, 'Positions', 'start')
Data Types: string
```

Output Arguments

axHandle — Axes used to plot path

Axes object | UIAxes object

Axes used to plot path, returned as either an axes or uiaxes object.

See Also

navPath | validatorOccupancyMap | validatorVehicleCostmap

plannerRRT

Create an RRT planner for geometric planning

Description

The plannerRRT object creates a rapidly-exploring random tree (RRT) planner for solving geometric planning problems. RRT is a tree-based motion planner that builds a search tree incrementally from samples randomly drawn from a given state space. The tree eventually spans the search space and connects the start state to the goal state. The general tree growing process is as follows:

- **1** The planner samples a random state x_{rand} in the state space.
- The planner finds a state x_{near} that is already in the search tree and is closest (based on the distance definition in the state space) to x_{rand} .
- **3** The planner expands from x_{near} towards x_{rand} , until a state x_{new} is reached.
- **4** Then new state x_{new} is added to the search tree.

For geometric RRT, the expansion and connection between two states can be found analytically without violating the constraints specified in the state space of the planner object.

Creation

Syntax

planner = plannerRRT(stateSpace,stateVal)

Description

planner = plannerRRT(stateSpace, stateVal) creates an RRT planner from a state space object, stateSpace, and a state validator object, stateVal. The state space of stateVal must be the same as stateSpace. stateSpace and stateVal also sets the StateSpace and StateValidator properties of the planner.

Properties

StateSpace — State space for the planner

state space object

State space for the planner, specified as a state space object. You can use state space objects such as stateSpaceSE2, stateSpaceDubins, and stateSpaceReedsShepp. You can also customize a state space object using the nav.StateSpace object.

StateValidator — State validator for the planner

state validator object

State validator for the planner, specified as a state validator object. You can use state validator objects such as validatorOccupancyMap and validatorVehicleCostmap.

MaxNumTreeNodes — Maximum number of nodes in the search tree

1e4 (default) | positive integer

Maximum number of nodes in the search tree (excluding the root node), specified as a positive integer.

Data Types: single | double

MaxIterations — Maximum number of iterations

1e4 (default) | positive integer

Maximum number of iterations, specified as a positive integer.

Data Types: single | double

MaxConnectionDistance — Maximum length of motion

0.1 (default) | positive scalar

Maximum length of a motion allowed in the tree, specified as a scalar.

Data Types: single | double

GoalReachedFcn — Callback function to evaluate whether goal is reached

@nav.algs.checkIfGoalIsReached | function handle

Callback function to evaluate whether the goal is reached, specified as a function handle. You can create your own goal reached function. The function must follow this syntax:

function isReached = myGoalReachedFcn(planner,currentState,goalState)

where:

- planner The created planner object, specified as plannerRRT object.
- currentState The current state, specified as a three element real vector.
- goalState The goal state, specified as a three element real vector.
- isReached A boolean variable to indicate whether the current state has reached the goal state, returned as true or false.

Data Types: function handle

GoalBias — Probability of choosing goal state during state sampling

0.05 (default) | real scalar in [0,1]

Probability of choosing the goal state during state sampling, specified as a real scalar in [0,1]. The property defines the probability of choosing the actual goal state during the process of randomly selecting states from the state space. You can start by setting the probability to a small value such as 0.05.

Data Types: single | double

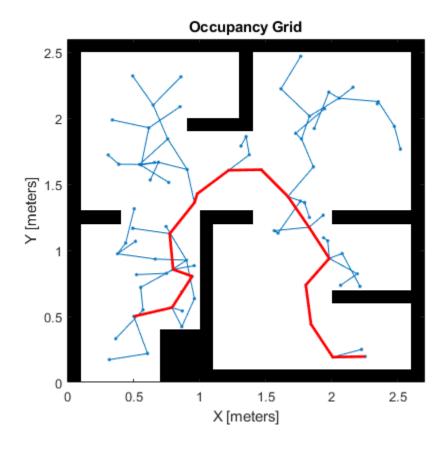
Object Functions

plan Plan path between two states copy Create copy of planner object

Examples

Plan Path Between Two States

```
Create a state space.
ss = stateSpaceSE2;
Create an occupanyMap-based state validator using the created state space.
sv = validatorOccupancyMap(ss);
Create an occupany map from an example map and set map resolution as 10 cells/meter.
load exampleMaps
map = occupancyMap(simpleMap,10);
sv.Map = map;
Set validation distance for the validator.
sv.ValidationDistance = 0.01;
Update state space bounds to be the same as map limits.
ss.StateBounds = [map.XWorldLimits; map.YWorldLimits; [-pi pi]];
Create the path planner and increase max connection distance.
planner = plannerRRT(ss,sv);
planner.MaxConnectionDistance = 0.3;
Set the start and goal states.
start = [0.5, 0.5, 0];
goal = [2.5, 0.2, 0];
Plan a path with default settings.
rng(100, 'twister'); % for repeatable result
[pthObj,solnInfo] = plan(planner,start,goal);
Visualize the results.
show(map)
hold on
plot(solnInfo.TreeData(:,1),solnInfo.TreeData(:,2),'.-'); % tree expansion
plot(pth0bj.States(:,1),pth0bj.States(:,2),'r-','LineWidth',2) % draw path
```



References

[1] S.M. Lavalle and J.J. Kuffner. "Randomized Kinodynamic Planning." *The International Journal of Robotics Research.* Vol. 20, Number 5, 2001, pp. 378 – 400.

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

navPath | plannerRRTStar | stateSpaceDubins | stateSpaceReedsShepp | stateSpaceSE2

plannerRRTStar

Create an optimal RRT path planner (RRT*)

Description

The plannerRRTStar object creates an asymptotically-optimal RRT planner, RRT*. The RRT* algorithm converges to an optimal solution in terms of the state space distance. Also, its runtime is a constant factor of the runtime of the RRT algorithm. RRT* is used to solve geometric planning problems. A geometric planning problem requires that any two random states drawn from the state space can be connected.

Creation

Syntax

planner = plannerRRTStar(stateSpace, stateVal)

Description

planner = plannerRRTStar(stateSpace, stateVal) creates an RRT* planner from a state space object, stateSpace, and a state validator object, stateVal. The state space of stateVal must be the same as stateSpace. stateSpace and stateVal also sets the StateSpace and StateValidator properties of the planner object.

Properties

BallRadiusConstant — **Constant used to estimate the near neighbors search radius** 100 (default) | positive scalar

Constant used to estimate the near neighbors search radius, specified as a positive scalar. With a larger ball radius, the searching radius reduces slower as the number of nodes in the tree increases. The radius is estimated as following:

$$r = \min\left(\left\{\frac{\gamma \ln(n)}{nV_d}\right\}^{1/d}, \eta\right)$$

where:

- *d* Dimension of the state space
- n Number of nodes in the search tree
- η The value of the MaxConnectionDistance property
- V_d Volume of the unit ball in the *d*th dimension

Data Types: single | double

ContinueAfterGoalReached — Continue to optimize after goal is reached

false (default) | true

Decide if the planner continues to optimize after the goal is reached, specified as false or true. The planner also terminates regardless of the value of this property if the maximum number of iterations or maximum number of tree nodes is reached.

Data Types: logical

StateSpace — State space for the planner

state space object

State space for the planner, specified as a state space object. You can use state space objects such as stateSpaceSE2, stateSpaceDubins, and stateSpaceReedsShepp. You can also customize a state space object using the nav.StateSpace object.

StateValidator — **State validator for the planner**

state validator object

State validator for the planner, specified as a state validator object. You can use state validator objects such as validatorOccupancyMap and validatorVehicleCostmap.

MaxNumTreeNodes — Maximum number of nodes in the search tree

1e4 (default) | positive integer

Maximum number of nodes in the search tree (excluding the root node), specified as a positive integer.

Data Types: single | double

MaxIterations — Maximum number of iterations

1e4 (default) | positive integer

Maximum number of iterations, specified as a positive integer.

Data Types: single | double

MaxConnectionDistance — Maximum length of motion

0.1 (default) | positive scalar

Maximum length of a motion allowed in the tree, specified as a scalar.

Data Types: single | double

GoalReachedFcn — Callback function to determine whether goal is reached

@nav.algs.checkIfGoalIsReached | function handle

Callback function to determine whether the goal is reached, specified as a function handle. You can create your own goal reached function. The function must follow this syntax:

function isReached = myGoalReachedFcn(planner,currentState,goalState)

where:

- planner The created planner object, specified as plannerRRTStar object.
- currentState The current state, specified as a three element real vector.
- goalState The goal state, specified as a three element real vector.
- isReached A boolean variable to indicate whether the current state has reached the goal state, returned as true or false.

Data Types: function handle

GoalBias — Probability of choosing goal state during state sampling

```
0.05 (default) | real scalar in [0,1]
```

Probability of choosing the goal state during state sampling, specified as a real scalar in [0,1]. The property defines the probability of choosing the actual goal state during the process of randomly selecting states from the state space. You can start by setting the probability to a small value such as 0.05.

Data Types: single | double

Object Functions

plan Plan path between two states copy Create copy of planner object

Examples

Plan Optimal Path Between Two States

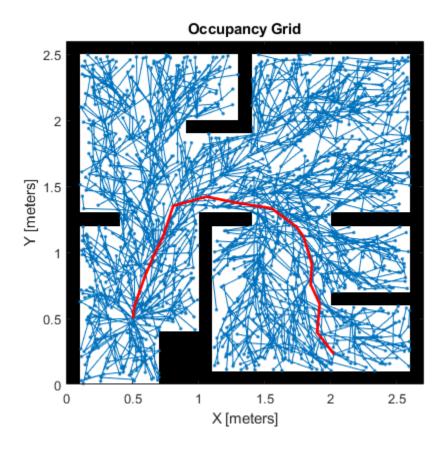
```
Create a state space.
ss = stateSpaceSE2;
Create a occupancyMap-based state validator using the created state space.
sv = validatorOccupancyMap(ss);
Create an occupany map from an example map and set map resolution as 10 cells/meter.
load exampleMaps.mat
map = occupancyMap(simpleMap, 10);
sv.Map = map;
Set validation distance for the validator.
sv.ValidationDistance = 0.01:
Update state space bounds to be the same as map limits.
ss.StateBounds = [map.XWorldLimits; map.YWorldLimits; [-pi pi]];
Create RRT* path planner and allow further optimization after goal is reached.
planner = plannerRRTStar(ss,sv);
planner.ContinueAfterGoalReached = true;
Reduce max iterations and increase max connection distance.
planner.MaxIterations = 2500;
planner.MaxConnectionDistance = 0.3;
Set the start and goal states.
start = [0.5, 0.5 0];
goal = [2.5, 0.2, 0];
```

Plan a path with default settings.

```
rng(100, 'twister') % repeatable result
[pth0bj, solnInfo] = plan(planner, start, goal);

Visualize the results.

map.show;
hold on;
plot(solnInfo.TreeData(:,1), solnInfo.TreeData(:,2), '.-'); % tree expansion
plot(pth0bj.States(:,1), pth0bj.States(:,2), 'r-', 'LineWidth',2); % draw path
```



References

[1] Karaman, S. and E. Frazzoli. "Sampling-Based Algorithms for Optimal Motion Planning." *The International Journal of Robotics Research.* Vol. 30, Number 7, 2011, pp 846 – 894.

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

navPath | plannerRRT | stateSpaceDubins | stateSpaceReedsShepp | stateSpaceSE2

plan

Plan path between two states

Syntax

```
path = plan(planner,startState,goalState)
[path,solutionInfo] = plan(planner,startState,goalState)
```

Description

path = plan(planner, startState, goalState) returns a path from the start state to the goal state.

[path, solutionInfo] = plan(planner, startState, goalState) also returns solInfo that contains the solution information of the path planning.

Input Arguments

planner — Path planner

plannerRRT object | plannerRRTStar object

Path planner, specified as a plannerRRT object or a plannerRRTStar object.

startState - Start state of the path

N-element real-valued vector

Start state of the path, specified as an N-element real-valued vector. N is the dimension of the state space.

Example: [1 1 pi/6]

Data Types: single | double

goalState — Goal state of the path

N-element real-valued vector

Goal state of the path, specified as an N-element real-valued vector. N is the dimension of the state space.

Example: [2 2 pi/3]

Data Types: single | double

Output Arguments

path — Object that holds planned path information

navPath object

An object that holds the planned path information, returned as a navPath object.

solutionInfo — Solution Information

structure

Solution Information, returned as a structure. The fields of the structure are:

Fields of solutionInfo

Fields	Description
IsPathFound	Indicates whether a path is found. It returns as 1 if a path is found. Otherwise, it returns 0 .
ExitFlag	Indicates the terminate status of the planner, returned as
	• 1 — if the goal is reached
	2 — if the maximum number of iterations is reached
	3 — if the maximum number of nodes is reached
NumNodes	Number of nodes in the search tree when the planner terminates (excluding the root node).
NumIterations	Number of "extend" routines executed.
TreeData	A collection of explored states that reflects the status of the search tree when planner terminates. Note that NaN values are inserted as delimiters to separate each individual edge.
PathCosts	Contains the cost of the path at each iteration. Value for iterations when path has not reached the goal is denoted by a NaN. Size of the array is NumIterations-by-1. Last element contains the cost of the final path.
	Note This field is applicable only for plannerRRTStar object.

Data Types: structure

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

navPath | plannerRRT | plannerRRTStar | stateSpaceDubins | stateSpaceReedsShepp |
stateSpaceSE2

copy

Create copy of planner object

Syntax

planner2 = copy(planner1)

Description

planner2 = copy(planner1) creates a planner object, planner2, form a planner object, planner1.

Input Arguments

planner1 — Path planner

plannerRRT object | plannerRRTStar object

Path planner, specified as a plannerRRT object or a plannerRRTStar object.

Output Arguments

planner2 — Path planner

plannerRRT object | plannerRRTStar object

Path planner, returned as a plannerRRT object or a plannerRRTStar object.

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

navPath|plannerRRT|plannerRRTStar|stateSpaceDubins|stateSpaceReedsShepp| stateSpaceSE2

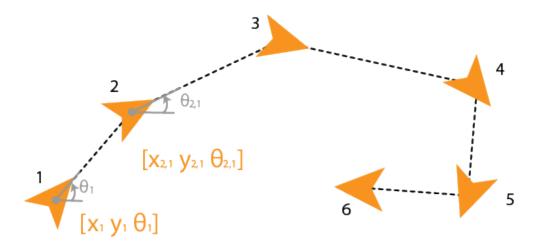
poseGraph

Create 2-D pose graph

Description

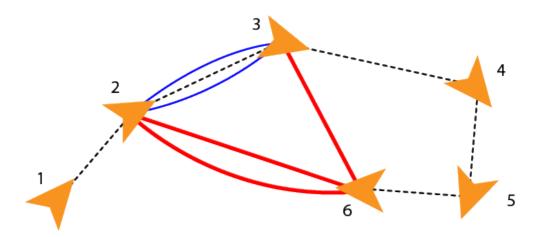
A poseGraph object stores information for a 2-D pose graph representation. A pose graph contains nodes connected by edges. Each node estimate is connected to the graph by edge constraints that define the relative pose between nodes and the uncertainty on that measurement.

To construct a pose graph iteratively, use the addRelativePose function to add relative pose estimates and connect them to an existing node with specified edge constraints. Pose nodes must be specified relative to a pose node. Specify the uncertainty of the measurement using an information matrix.



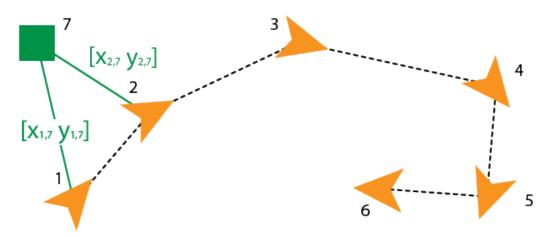
Pose Node Estimates

Adding an edge between two nonsequential nodes creates a *loop closure* in the graph. Multiple edges or *multiedges* between node pairs are also supported, which includes loop closures. To add additional edge constraints or loop closures, specify the node IDs using the addRelativePose function. When optimizing the pose graph, the optimizePoseGraph function finds a solution to satisfy all these edge constraints.



Loop closures and multiedges

To add landmark point nodes, use the addPointLandmark function. This function specifies nodes as xy-points without orientation estimates. Landmarks must be specified relative to a pose node.



Point landmarks

The lidarSLAM object performs lidar-based simultaneous localization and mapping, which is based around the optimization of a 2-D pose graph.

For 3-D pose graphs, see the poseGraph3D object or the "Landmark SLAM Using AprilTag Markers" example.

Creation

Syntax

```
poseGraph = poseGraph('MaxNumEdges', maxEdges, 'MaxNumNodes', maxNodes)
```

Description

poseGraph = poseGraph creates a 2-D pose graph object. Add poses using addRelativePose to construct a pose graph iteratively.

poseGraph = poseGraph('MaxNumEdges', maxEdges,'MaxNumNodes', maxNodes) specifies an upper bound on the number of edges and nodes allowed in the pose graph when generating code. This syntax is only required when generating code.

Properties

NumNodes — Number of nodes in pose graph

1 (default) | positive integer

This property is read-only.

Number of nodes in pose graph, specified as a positive integer. Each node represents a pose measurement or a point landmark measurement. To specify relative poses between nodes, use addRelativePose. To specify a landmark pose, use addLandmarkPose. To get a list of all nodes, use edgeNodePairs.

NumEdges — Number of edges in pose graph

0 (default) | nonnegative integer

This property is read-only.

Number of edges in pose graph, specified as a nonnegative integer. Each edge connects two nodes in the pose graph. Loop closure edges and landmark edges are included.

NumLoopClosureEdges — Number of loop closures

0 (default) | nonnegative integer

This property is read-only.

Number of loop closures in pose graph, specified as a nonnegative integer. To get the edge IDs of the loop closures, use the LoopClosureEdgeIDs property.

LoopClosureEdgeIDs — Loop closure edge IDs

vector

This property is read-only.

Loop closure edges IDs, specified as a vector of edge IDs.

LandmarkNodeIDs — Landmark node IDs

vector

This property is read-only.

Landmark node IDs, specified as a vector of IDs for each node.

Object Functions

addPointLandmark Add landmark point node to pose graph addRelativePose Add relative pose to pose graph Create copy of pose graph copy edgeNodePairs Edge node pairs in pose graph edgeConstraints Edge constraints in pose graph edgeResidualErrors Compute pose graph edge residual errors findEdgeID Find edge ID of edge nodeEstimates Poses of nodes in pose graph

removeEdges Remove loop closure edges from graph

show Plot pose graph

Examples

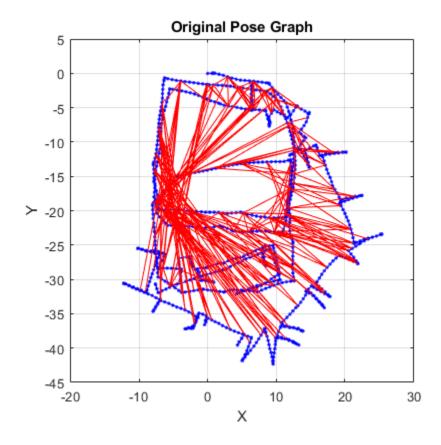
Optimize a 2-D Pose Graph

Optimize a pose graph based on the nodes and edge constraints. The pose graph used in this example is from the Intel Research Lab Dataset and was generated from collecting wheel odometry and a laser range finder sensor information in an indoor lab.

Load the Intel data set that contains a 2-D pose graph. Inspect the poseGraph object to view the number of nodes and loop closures.

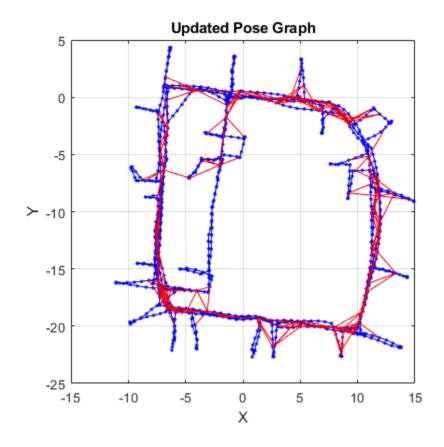
Plot the pose graph with IDs off. Red lines indicate loop closures identified in the dataset.

```
show(pg,'IDs','off');
title('Original Pose Graph')
```



Optimize the pose graph. Nodes are adjusted based on the edge constraints and loop closures. Plot the optimized pose graph to see the adjustment of the nodes with loop closures.

```
updatedPG = optimizePoseGraph(pg);
figure
show(updatedPG,'IDs','off');
title('Updated Pose Graph')
```



References

[1] Grisetti, G., R. Kummerle, C. Stachniss, and W. Burgard. "A Tutorial on Graph-Based SLAM." *IEEE Intelligent Transportation Systems Magazine*. Vol. 2, No. 4, 2010, pp. 31-43. doi:10.1109/mits.2010.939925.

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

Use this syntax when constructing poseGraph objects for code generation: poseGraph = poseGraph('MaxNumEdges', maxEdges, 'MaxNumNodes', maxNodes) specifies an upper bound on the number of edges and nodes allowed in the pose graph when generating code. This limit is only required when generating code.

See Also

Functions

addPointLandmark | addRelativePose | optimizePoseGraph | show

Objects

lidarSLAM|poseGraph3D

Topics

"Implement Simultaneous Localization And Mapping (SLAM) with Lidar Scans" "Implement Online Simultaneous Localization And Mapping (SLAM) with Lidar Scans"

"Landmark SLAM Using AprilTag Markers"

addPointLandmark

Add landmark point node to pose graph

Syntax

```
addPointLandmark(poseGraph, measurement)
addPointLandmark(poseGraph, measurement, infoMat)
addPointLandmark(poseGraph, measurement, infoMat, poseNodeID)
addPointLandmark(poseGraph, measurement, infoMat, poseNodeID, pointNodeID)
[nodePair,edgeID] = addPointLandmark( )
```

Description

addPointLandmark(poseGraph, measurement) adds a landmark point node, based on the input position measurement that connects to the last pose node in the pose graph. To add pose measurement nodes, see the addRelativePose function.

addPointLandmark(poseGraph, measurement, infoMat) also specifies the information matrix as part of the edge constraint, which represents the uncertainty of the landmark measurement.

addPointLandmark(poseGraph, measurement, infoMat, poseNodeID) adds a new landmark point node and connects it to the pose node specified by poseNodeID.

addPointLandmark(poseGraph, measurement, infoMat, poseNodeID, pointNodeID) creates an edge by specifying a point measurement between existing nodes, specified by poseNodeID and pointNodeID. If the node pair already exists, the function appends the new measurement.

[nodePair,edgeID] = addPointLandmark(____) returns the newly added edge and edge ID using any combination of inputs from the previous syntaxes.

Input Arguments

poseGraph — Pose graph

poseGraph object | poseGraph3D object

Pose graph, specified as a poseGraph or poseGraph3D object.

measurement — Position of landmark point

two-element vector of form [x y] | three-element vector of form [x y z]

Position of landmark point, specified as one of the following:

For poseGraph (2-D), the pose is a two-element vector of form of the form [x y], which defines an xy-position for the landmark.

For poseGraph3D, the pose is a three-element vector of the form $[x \ y \ z]$, which defines an xyz-position for the landmark.

infoMat — Information matrix for landmark

three-element vector | six-element vector

Information matrix for the landmark, specified as a three-element or six-element vector.

Each vector is the compact form of the upper triangle of the square information matrix. An information matrix represents the uncertainty of the measurement. The matrix is calculated as the inverse of the covariance. If the measurement is an $[x \ y]$ vector, the covariance matrix is a 2-by-2 matrix of pairwise covariance calculations. Typically, the uncertainty is determined by the sensor model.

For poseGraph (2-D), each information matrix is a three-element vector. The default is [1 1 0].

For poseGraph3D, each information matrix is a six-element vector. The default is [1 0 0 1 0 1].

poseNodeID — Pose node to attach from

positive integer

Pose node to attach from, specified as a positive integer. This integer corresponds to the node ID of a pose node in poseGraph. When specified without the pointNodeID input, addPointLandmark creates a new landmark point node and adds an edge between the new node and the poseNodeID node.

pointNodeID — Landmark point node to attach to

positive integer

Landmark point node to attach to, specified as a positive integer. This integer corresponds to the ID of a landmark node in the pose graph. See the LandmarkNodeIDs property of the pose graph.

Output Arguments

nodePair - Edge node pair in pose graph

two-element vector

Edge node pair in the pose graph, returned as a two-element vector that lists the IDs of the two nodes that the edge connects. Multiple edges may exist between the same pair of nodes.

edgeID — ID of added edge

positive integer

ID of added edge, returned as a positive integer.

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

Use this syntax when constructing poseGraph or poseGraph3D objects for code generation:

poseGraph = poseGraph('MaxNumEdges', maxEdges, 'MaxNumNodes', maxNodes) specifies an upper bound on the number of edges and nodes allowed in the pose graph when generating code. This limit is only required when generating code.

poseGraph = poseGraph3D('MaxNumEdges', maxEdges, 'MaxNumNodes', maxNodes)

See Also

Functions

edgeConstraints|edgeNodePairs|findEdgeID|nodeEstimates|optimizePoseGraph|
removeEdges

Objects

lidarSLAM | poseGraph | poseGraph3D

Topics

"Implement Simultaneous Localization And Mapping (SLAM) with Lidar Scans"

"Implement Online Simultaneous Localization And Mapping (SLAM) with Lidar Scans"

"Landmark SLAM Using AprilTag Markers"

Introduced in R2021a

addRelativePose

Add relative pose to pose graph

Syntax

```
addRelativePose(poseGraph, measurement)
addRelativePose(poseGraph, measurement, infoMat)
addRelativePose(poseGraph, measurement, infoMat, fromNodeID)
addRelativePose(poseGraph, measurement, infoMat, fromNodeID, toNodeID)
[nodePair,edgeID] = addRelativePose(____)
```

Description

addRelativePose(poseGraph, measurement) creates a node based on the input measurement that connects to the last pose node in the pose graph. To add landmark nodes, see the addPointLandmark function.

addRelativePose(poseGraph, measurement, infoMat) also specifies the information matrix as part of the edge constraint, which represents the uncertainty of the pose measurement.

addRelativePose(poseGraph, measurement, infoMat, fromNodeID) creates a new pose node and connects it to the specific node specified by fromNodeID.

addRelativePose(poseGraph, measurement, infoMat, fromNodeID, toNodeID) creates an edge by specifying a relative pose measurement between existing nodes specified by fromNodeID and toNodeID. This edge is called a loop closure. If a loop closure already exists, the function appends the new measurement. Calling the optimizePoseGraph function combines multiple appended measurements into a single edge. This syntax does not support adding edges to a landmark node.

[nodePair,edgeID] = addRelativePose(____) returns the newly added edge and edge ID
using any of the previous syntaxes.

Input Arguments

poseGraph — Pose graph

poseGraph object | poseGraph3D object

Pose graph, specified as a poseGraph or poseGraph3D object.

measurement — Relative pose between nodes

```
[x y theta] vector | [x y z qw qx qy qz] vector
```

Relative pose between nodes, specified as one of the following:

For poseGraph (2-D), the pose is a [x y theta] vector, which defines a xy-position and orientation angle, theta.

For poseGraph3D, the pose is a $[x \ y \ z \ qw \ qx \ qy \ qz]$ vector, which defines by an xyz-position and quaternion orientation, $[qw \ qx \ qy \ qz]$

Note Many other sources for 3-D pose graphs, including .g2o formats, specify the quaternion orientation in a different order, for example, [qx qy qz qw]. Check the source of your pose graph data before adding nodes to your poseGraph3D object.

infoMat — Information matrix

6-element vector | 21-element vector

Information matrices, specified in compact form as a 6-element vector or 21-element vector.

Each row is the upper triangle of the square information matrix. An information matrix represents the uncertainty of the measurement. The matrix is calculated as the inverse of the covariance. If the measurement is an [x y theta] vector, the covariance matrix is a 3-by-3 of pairwise covariance calculations. Typically, the uncertainty is determined by the sensor model.

For poseGraph (2-D), each information matrix is a six-element vector. The default is [1 0 0 1 0 1]. For landmark nodes, the last three elements are returned as NaN.

For poseGraph3D, each information matrix is a 21-element vector. The default is $[1 \ 0 \ 0 \ 0 \ 0 \ 1 \ 0 \ 0 \ 0 \ 1 \]$.

fromNodeID — Node to attach from

positive integer

Node to attach from, specified as a positive integer. This integer corresponds to the node ID of a node in poseGraph. When specified without toNodeID, addRelativePose creates a new node and adds an edge between the new node and the fromNodeID node.

toNodeID — Node to attach to

positive integer

Node to attach to, specified as a positive integer. This integer corresponds to the node ID of a node in poseGraph. addRelativePose adds an edge between this node and the fromNodeID node.

Output Arguments

nodePair — Edge node pair in pose graph

two-element vector

Edge node pairs in pose graph, returned as two-element vector that lists the IDs of the two nodes that each edge connects. Multiple edges may exist between the same pair of nodes.

edgeID — ID of added edge

positive integer

ID of added edge, returned as a positive integer.

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

Use this syntax when constructing poseGraph or poseGraph3D objects for code generation:

poseGraph = poseGraph('MaxNumEdges', maxEdges, 'MaxNumNodes', maxNodes) specifies an upper bound on the number of edges and nodes allowed in the pose graph when generating code. This limit is only required when generating code.

poseGraph = poseGraph3D('MaxNumEdges', maxEdges, 'MaxNumNodes', maxNodes)

See Also

Functions

 $\verb|edgeConstraints|| edgeNodePairs|| findEdgeID|| nodeEstimates|| optimizePoseGraph|| removeEdges$

Objects

lidarSLAM | poseGraph | poseGraph3D

Topics

- "Implement Simultaneous Localization And Mapping (SLAM) with Lidar Scans"
- "Implement Online Simultaneous Localization And Mapping (SLAM) with Lidar Scans"
- "Landmark SLAM Using AprilTag Markers"

copy

Create copy of pose graph

Syntax

poseGraph2 = copy(poseGraph1)

Description

poseGraph2 = copy(poseGraph1) creates a deep copy of the pose graph object with the same properties.

Examples

Input Arguments

poseGraph1 — Pose graph

poseGraph object | poseGraph3D object

Pose graph, specified as a poseGraph or poseGraph3D object.

Output Arguments

poseGraph2 — Copy of pose graph

poseGraph object | poseGraph3D object

Copy of pose graph, returned as a poseGraph or poseGraph3D object.

See Also

poseGraph | poseGraph3D

edgeConstraints

Edge constraints in pose graph

Syntax

```
measurements = edgeConstraints(poseGraph)
[measurements,infoMats] = edgeConstraints(poseGraph)
[measurements,infoMats] = edgeConstraints(poseGraph,edgeIDs)
```

Description

measurements = edgeConstraints(poseGraph) lists all edge constraints in the specified pose graph as a relative pose.

[measurements,infoMats] = edgeConstraints(poseGraph) also returns the information matrices for each edge. The information matrix is the inverse of the covariance of the pose measurement.

[measurements,infoMats] = edgeConstraints(poseGraph,edgeIDs) returns edge constraints for the specified edge IDs.

Input Arguments

poseGraph — Pose graph

poseGraph object | poseGraph3D object

Pose graph, specified as a poseGraph or poseGraph3D object.

edgeIDs — Edge IDs

vector of positive integers

Edge IDs, specified as a vector of positive integers.

Output Arguments

measurements — Measurements between nodes

n-by-3 matrix | *n*-by-7 matrix

Measurements between nodes, returned as an *n*-by-3 matrix or *n*-by-7 matrix.

For poseGraph (2-D), each row is an [x y theta] vector, which defines the relative xy-position and orientation angle, theta, of a pose in the graph. For landmark positions, theta is returned as NaN.

For poseGraph3D, each row is an [x y z qw qx qy qz] vector, which defines the relative xyz-position and quaternion orientation, [qw qx qy qz], of a pose in the graph.

Note Many other sources for 3-D pose graphs, including .g2o formats, specify the quaternion orientation in a different order, for example, [qx qy qz qw]. Check the source of your pose graph data before adding nodes to your poseGraph3D object.

infoMats — Information matrices

n-by-6 matrix | *n*-by-21 matrix

Information matrices, specified in compact form as a n-by-6 or n-by-21 matrix, where n is the number of poses in the pose graph.

Each row is the upper triangle of the square information matrix. An information matrix represents the uncertainty of the measurement. The matrix is calculated as the inverse of the covariance. If the measurement is an [x y theta] vector, the covariance matrix is a 3-by-3 of pairwise covariance calculations. Typically, the uncertainty is determined by the sensor model.

For poseGraph (2-D), each information matrix is a six-element vector. The default is [1 0 0 1 0 1]. For landmark nodes, the last three elements are returned as NaN.

For poseGraph3D, each information matrix is a 21-element vector. The default is [1 0 0 0 0 1 0 0 0 1 0 0 1 0 1].

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

Use this syntax when constructing poseGraph or poseGraph3D objects for code generation:

poseGraph = poseGraph('MaxNumEdges', maxEdges, 'MaxNumNodes', maxNodes) specifies an upper bound on the number of edges and nodes allowed in the pose graph when generating code. This limit is only required when generating code.

See Also

Functions

 $add Relative Pose \mid edge Node Pairs \mid find Edge ID \mid node Estimates \mid optimize Pose Graph \mid remove Edges$

Objects

lidarSLAM | poseGraph | poseGraph3D

Topics

"Implement Simultaneous Localization And Mapping (SLAM) with Lidar Scans"

[&]quot;Implement Online Simultaneous Localization And Mapping (SLAM) with Lidar Scans"

edgeNodePairs

Edge node pairs in pose graph

Syntax

```
nodePairs = edgeNodePairs(poseGraph)
nodePairs = edgeNodePairs(poseGraph,edgeIDs)
```

Description

nodePairs = edgeNodePairs(poseGraph) returns all edges in the specified pose graph as a list of node ID pairs. Each row of the edges output is a pair of nodes that form an edge. Multiple edges may exist between the same pair of nodes.

nodePairs = edgeNodePairs(poseGraph,edgeIDs) returns edges corresponding to the
specified edge IDs. Each edge in the pose graph has a unique ID even if the node pairs are the same.

Input Arguments

poseGraph — Pose graph

poseGraph object | poseGraph3D object

Pose graph, specified as a poseGraph or poseGraph3D object.

edgeIDs — Edge IDs

vector of positive integers

Edge IDs, specified as a vector of positive integers.

Output Arguments

nodePairs - Edge node pairs in pose graph

n-by-2 matrix

Edge node pairs in pose graph, returned as n-by-2 matrix that lists the IDs of the two nodes that each edge connects. Each row is a pair of nodes that form an edge. Multiple edges may exist between the same pair of nodes, so the matrix may contain duplicate entries.

Compatibility Considerations

edgeNodePairs was renamed

Behavior change in future release

The edgeNodePairs object function was renamed from edges. Use edgeNodePairs when calling the function.

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

Use this syntax when constructing poseGraph or poseGraph3D objects for code generation:

poseGraph = poseGraph('MaxNumEdges', maxEdges, 'MaxNumNodes', maxNodes) specifies an upper bound on the number of edges and nodes allowed in the pose graph when generating code. This limit is only required when generating code.

See Also

Functions

addRelativePose | edgeConstraints | findEdgeID | nodeEstimates | optimizePoseGraph |
removeEdges

Objects

lidarSLAM | poseGraph | poseGraph3D

Topics

"Implement Simultaneous Localization And Mapping (SLAM) with Lidar Scans"

"Implement Online Simultaneous Localization And Mapping (SLAM) with Lidar Scans"

edgeResidualErrors

Compute pose graph edge residual errors

Syntax

```
resErrorVec = edgeResidualErrors(poseGraphObj)
```

Description

resErrorVec = edgeResidualErrors(poseGraphObj) returns the residual errors for each edge in the pose graph with the current pose node estimates. The residual errors order matches the order of edge IDs in poseGraph.

Examples

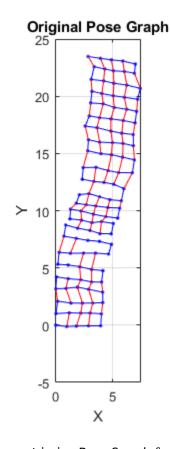
Optimize and Trim Loop Closures For 2-D Pose Graphs

Optimize a pose graph based on the nodes and edge constraints. Trim loop closed based on their edge residual errors.

Load the data set that contains a 2-D pose graph. Inspect the poseGraph object to view the number of nodes and loop closures.

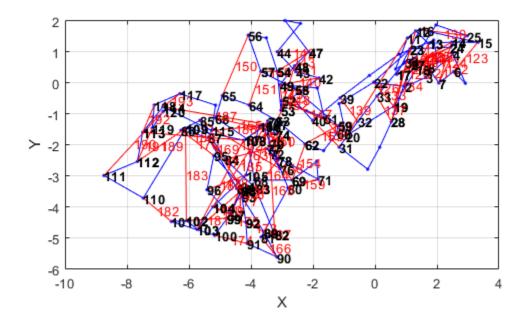
Plot the pose graph with IDs off. Red lines indicate loop closures identified in the dataset. The poses in the graph should follow a grid pattern, but show evidence of drift over time.

```
show(pg,'IDs','off');
title('Original Pose Graph')
```



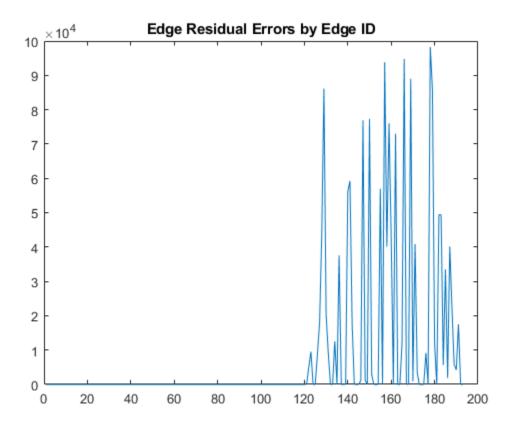
Optimize the pose grap using the optimizePoseGraph function. By default, this function uses the "builtin-trust-region" solver. Because the pose graph contains some bad loop closures, the resulting pose graph is actual not desirable.

```
pgOptim = optimizePoseGraph(pg);
figure;
show(pgOptim);
```



Look at the edge residual errors for the original pose graph. Large outlier error values at the end indicate bad loop closures.

```
resErrorVec = edgeResidualErrors(pg);
plot(resErrorVec);
title('Edge Residual Errors by Edge ID')
```



Certain loop closures should be trimmed from the pose graph based on their residual error. Use the trimLoopClosures function to trim therse bad loop closures. Set the maximum and truncation threshold for the trimmer parameters. This threshold is set based on the measurement accuracy and should be tuned for your system.

```
trimParams.MaxIterations = 100;
trimParams.TruncationThreshold = 25;
solverOptions = poseGraphSolverOptions;
```

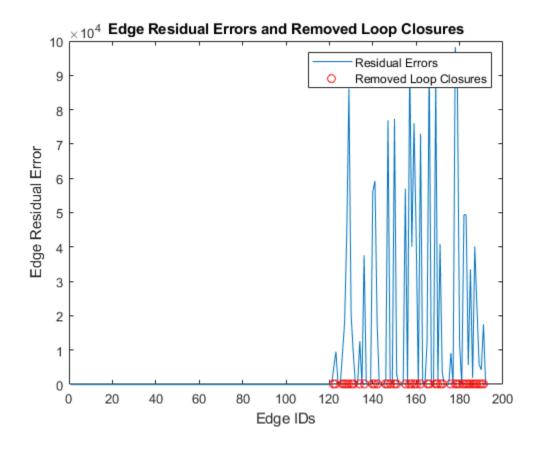
Use the trimLoopClosures function with the trimmer parameters and solver options.

```
[pgNew, trimInfo, debugInfo] = trimLoopClosures(pg,trimParams,solverOptions);
```

From the trimInfo output, plot the loop closures removed from the optimized pose graph. By plotting with the residual errors plot before, you can see the large error loop closures were removed.

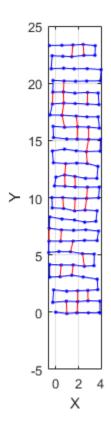
removedLCs = trimInfo.LoopClosuresToRemove;

```
hold on
plot(removedLCs,zeros(length(removedLCs)),'or')
title('Edge Residual Errors and Removed Loop Closures')
legend('Residual Errors', 'Removed Loop Closures')
xlabel('Edge IDs')
ylabel('Edge Residual Error')
hold off
```



Show the new pose graph with the bad loop closures trimmed.

show(pgNew,"IDs","off");



Input Arguments

poseGraphObj - Pose graph

poseGraph object | poseGraph3D object

Pose graph, specified as a poseGraph or poseGraph3D object.

Output Arguments

resErrorVec - Edge residual errors for pose graph

vector of positive scalars

Edge residual errors for pose graph, specified as a vector of positive scalars.

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

Use this syntax when constructing poseGraph or poseGraph3D objects for code generation:

poseGraph = poseGraph('MaxNumEdges', maxEdges, 'MaxNumNodes', maxNodes) specifies an upper bound on the number of edges and nodes allowed in the pose graph when generating code. This limit is only required when generating code.

See Also

Functions

addRelativePose | edgeNodePairs | findEdgeID | nodeEstimates | optimizePoseGraph |
removeEdges

Objects

lidarSLAM | poseGraph | poseGraph3D

Introduced in R2020b

findEdgeID

Find edge ID of edge

Syntax

edgeID = findEdgeID(poseGraph,nodePairs)

Description

edgeID = findEdgeID(poseGraph, nodePairs) finds the edge ID for a specified edge. Edges are
defined by the IDs of the two nodes that connect them.

Input Arguments

poseGraph - Pose graph

poseGraph object | poseGraph3D object

Pose graph, specified as a poseGraph or poseGraph3D object.

nodePairs - Edge node pairs in pose graph

two-element vector

Edge node pairs in pose graph, specified as a two-element vector that lists the IDs of the two nodes that the edge connects.

Output Arguments

edgeID — Edge ID

positive integer | vector

Edge IDs, returned as a positive integer or vector of positive integers. The pose graph can contain multiple edges between each node pair, so multiple edge IDs may be returned for a single edge ID.

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

Use this syntax when constructing poseGraph or poseGraph3D objects for code generation:

poseGraph = poseGraph('MaxNumEdges',maxEdges,'MaxNumNodes',maxNodes) specifies an upper bound on the number of edges and nodes allowed in the pose graph when generating code. This limit is only required when generating code.

See Also

Functions

addRelativePose | edgeConstraints | edgeNodePairs | nodeEstimates |
optimizePoseGraph | removeEdges

Objects

lidarSLAM | poseGraph | poseGraph3D

Topics

"Implement Simultaneous Localization And Mapping (SLAM) with Lidar Scans"

"Implement Online Simultaneous Localization And Mapping (SLAM) with Lidar Scans"

Introduced in R2019b

nodeEstimates

Poses of nodes in pose graph

Syntax

```
measurements = nodeEstimates(poseGraph)
measurements = nodeEstimates(poseGraph,nodeIDs)
```

Description

measurements = nodeEstimates(poseGraph) lists all poses in the specified pose graph.

measurements = nodeEstimates(poseGraph, nodeIDs) lists the poses with the specified node IDs.

Input Arguments

poseGraph — Pose graph

poseGraph object | poseGraph3D object

Pose graph, specified as a poseGraph or poseGraph3D object.

nodeIDs — Node IDs

positive integer | vector of positive integers

Node IDs, specified as a positive integer or vector of positive integers. Each node added gets an ID sequentially in the graph.

Output Arguments

measurements — Measurements between nodes

n-by-3 matrix | *n*-by-7 matrix

Measurements between nodes, returned as an *n*-by-3 matrix or *n*-by-7 matrix.

For poseGraph (2-D), each row is an [x y theta] vector, which defines the relative xy-position and orientation angle, theta, of a pose in the graph. For landmark positions, theta is returned as NaN.

For poseGraph3D, each row is an $[x \ y \ z \ qw \ qx \ qy \ qz]$ vector, which defines the relative xyz-position and quaternion orientation, $[qw \ qx \ qy \ qz]$, of a pose in the graph.

Note Many other sources for 3-D pose graphs, including .g2o formats, specify the quaternion orientation in a different order, for example, [qx qy qz qw]. Check the source of your pose graph data before adding nodes to your poseGraph3D object.

Compatibility Considerations

nodeEstimates was renamed

Behavior change in future release

The nodeEstimates object function was renamed from nodes. Use nodeEstimates when calling the function.

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

Use this syntax when constructing poseGraph or poseGraph3D objects for code generation:

poseGraph = poseGraph('MaxNumEdges', maxEdges,'MaxNumNodes', maxNodes) specifies an upper bound on the number of edges and nodes allowed in the pose graph when generating code. This limit is only required when generating code.

See Also

Functions

addRelativePose | edgeConstraints | edgeNodePairs | findEdgeID | optimizePoseGraph |
removeEdges

Objects

lidarSLAM | poseGraph | poseGraph3D

Topics

"Implement Simultaneous Localization And Mapping (SLAM) with Lidar Scans"

Introduced in R2019b

[&]quot;Implement Online Simultaneous Localization And Mapping (SLAM) with Lidar Scans"

removeEdges

Remove loop closure edges from graph

Syntax

removeEdges(poseGraph,edgeIDs)

Description

removeEdges (poseGraph, edgeIDs) removes loop closure edges, landmark edges, or duplicate incremental edges from the pose graph.

Input Arguments

poseGraph — Pose graph

poseGraph object | poseGraph3D object

Pose graph, specified as a poseGraph or poseGraph3D object.

edgeIDs — Edge IDs

vector of positive integers

Edge IDs, specified as a vector of positive integers. To get edge IDs based on node pairs, see the findEdgeID function.

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

Use this syntax when constructing poseGraph or poseGraph3D objects for code generation:

poseGraph = poseGraph('MaxNumEdges', maxEdges, 'MaxNumNodes', maxNodes) specifies an upper bound on the number of edges and nodes allowed in the pose graph when generating code. This limit is only required when generating code.

See Also

Functions

addRelativePose | edgeConstraints | edgeNodePairs | findEdgeID | nodeEstimates |
optimizePoseGraph

Objects

lidarSLAM | poseGraph | poseGraph3D

Topics

- "Implement Simultaneous Localization And Mapping (SLAM) with Lidar Scans"
- "Implement Online Simultaneous Localization And Mapping (SLAM) with Lidar Scans"

Introduced in R2019b

show

Plot pose graph

Syntax

```
show(poseGraph)
show(poseGraph,Name,Value)
axes = show(____)
```

Description

show(poseGraph) plots the specified pose graph in a figure.

show(poseGraph,Name,Value) specifies options using Name,Value pair arguments. For example,
'IDs','on' plots all node and edge IDs of the pose graph.

axes = show(____) returns the axes handle that the pose graph is plotted to using any of previous
syntaxes.

Examples

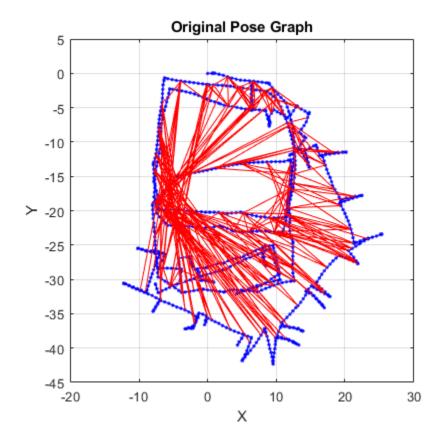
Optimize a 2-D Pose Graph

Optimize a pose graph based on the nodes and edge constraints. The pose graph used in this example is from the Intel Research Lab Dataset and was generated from collecting wheel odometry and a laser range finder sensor information in an indoor lab.

Load the Intel data set that contains a 2-D pose graph. Inspect the poseGraph object to view the number of nodes and loop closures.

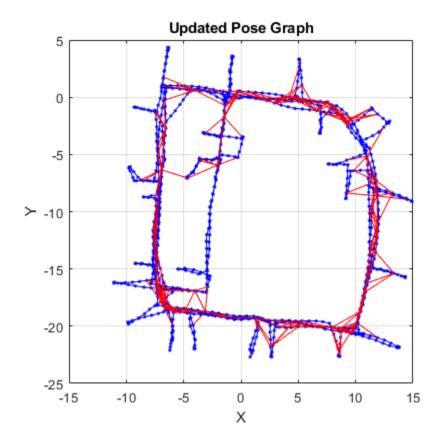
Plot the pose graph with IDs off. Red lines indicate loop closures identified in the dataset.

```
show(pg,'IDs','off');
title('Original Pose Graph')
```



Optimize the pose graph. Nodes are adjusted based on the edge constraints and loop closures. Plot the optimized pose graph to see the adjustment of the nodes with loop closures.

```
updatedPG = optimizePoseGraph(pg);
figure
show(updatedPG,'IDs','off');
title('Updated Pose Graph')
```



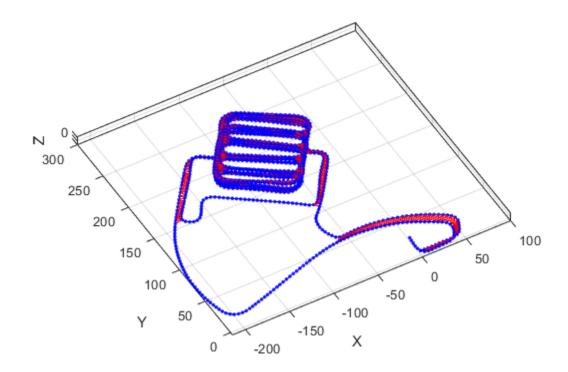
Optimize a 3-D Pose Graph

Optimize a pose graph based on the nodes and edge constraints. The pose graph used in this example is taken from the MIT Dataset and was generated using information extracted from a parking garage.

Load the pose graph from the MIT dataset. Inspect the poseGraph3D object to view the number of nodes and loop closures.

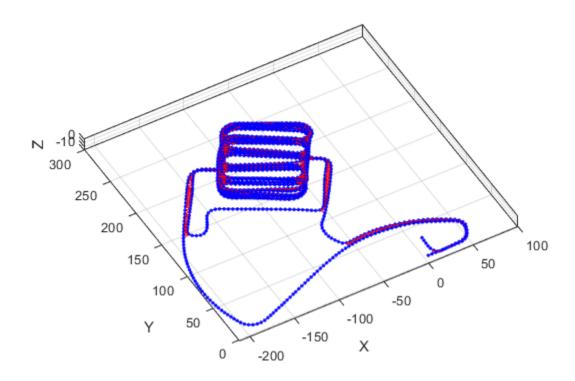
Plot the pose graph with IDs off. Red lines indicate loop closures identified in the dataset.

```
title('Original Pose Graph')
show(pg,'IDs','off');
view(-30,45)
```



Optimize the pose graph. Nodes are adjusted based on the edge constraints and loop closures. Plot the optimized pose graph to see the adjustment of the nodes with loop closures.

```
updatedPG = optimizePoseGraph(pg);
figure
title('Updated Pose Graph')
show(updatedPG,'IDs','off');
view(-30,45)
```



Input Arguments

poseGraph — Pose graph

poseGraph object | poseGraph3D object

Pose graph, specified as a poseGraph or poseGraph3D object.

Name-Value Pair Arguments

Specify optional comma-separated pairs of Name, Value arguments. Name is the argument name and Value is the corresponding value. Name must appear inside quotes. You can specify several name and value pair arguments in any order as Name1, Value1, . . . , NameN, ValueN.

Example: 'IDs', 'off'

Parent — Axes used to plot pose graph

Axes object | UIAxes object

Axes used to plot the pose graph, specified as the comma-separated pair consisting of 'Parent' and either an Axes or UIAxesobject. See axes or uiaxes.

IDs — Display of IDs on pose graph

'loopclosures' (default) | 'all' | 'nodes' | 'landmarks' | 'off'

Display of IDs on pose graph, specified as the comma-separated pair consisting of 'IDs' and one of the following:

- 'all' Plot all node and edge IDs.
- 'nodes' Plot all node IDs and loop closure IDs.
- 'loopclosures' Plot only loop closure edge IDs.
- 'landmarks' Plot landmark edge IDs.
- 'off' Do not plot any IDs.

Output Arguments

axes — Axes used to plot the map

Axes object | UIAxes object

Axes used to plot the map, returned as either an Axes or UIAxes object. See axes or uiaxes.

See Also

Functions

addRelativePose|optimizePoseGraph

Objects

lidarSLAM | poseGraph | poseGraph3D

Topics

"Implement Simultaneous Localization And Mapping (SLAM) with Lidar Scans"

"Implement Online Simultaneous Localization And Mapping (SLAM) with Lidar Scans"

Introduced in R2019b

[&]quot;Landmark SLAM Using AprilTag Markers"

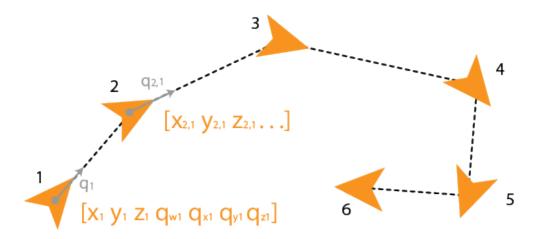
poseGraph3D

Create 3-D pose graph

Description

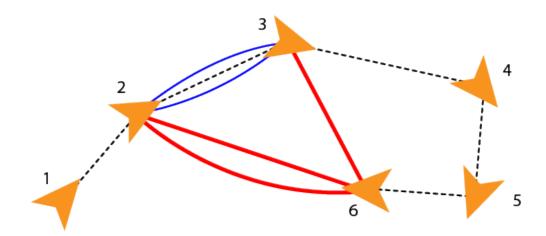
A poseGraph3D object stores information for a 3-D pose graph representation. A pose graph contains nodes connected by edges. Each node estimate is connected to the graph by edge constraints that define the relative pose between nodes and the uncertainty on that measurement.

To construct a pose graph iteratively, use the addRelativePose function to add relative pose estimates and connect them to an existing node with specified edge constraints. Pose nodes must be specified relative to a pose node. Specify the uncertainty of the measurement using an information matrix.



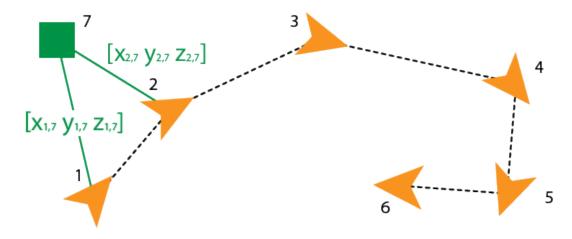
Pose Node Estimates

Adding an edge between two nonsequential nodes creates a *loop closure* in the graph. Multiple edges or *multiedges* between node pairs are also supported, which includes loop closures. To add additional edge constraints or loop closures, specify the node IDs using the addRelativePose function. When optimizing the pose graph, the optimizePoseGraph function finds a solution to satisfy all these edge constraints.



Loop closures and multiedges

To add landmark point nodes, use the addPointLandmark function. This function specifies nodes as xyz-points without orientation estimates. Landmarks must be specified relative to a pose node.



Point landmarks

For 2-D pose graphs, see poseGraph.

For an example that builds and optimizes a 3-D pose graph from real-world sensor data, see "Landmark SLAM Using AprilTag Markers".

Creation

Syntax

```
poseGraph = poseGraph3D
poseGraph = poseGraph3D('MaxNumEdges', maxEdges, 'MaxNumNodes', maxNodes)
```

Description

poseGraph = poseGraph3D creates a 3-D pose graph object. Add poses using addRelativePose
to construct a pose graph iteratively.

poseGraph = poseGraph3D('MaxNumEdges', maxEdges, 'MaxNumNodes', maxNodes) specifies
an upper bound on the number of edges and nodes allowed in the pose graph when generating code.
This limit is only required when generating code.

Properties

NumNodes — Number of nodes in pose graph

1 (default) | positive integer

This property is read-only.

Number of nodes in pose graph, specified as a positive integer. Each node represents a pose measurement or a point landmark measurement. To specify relative poses between nodes, use addRelativePose. To specify a landmark pose, use addLandmarkPose. To get a list of all nodes, use edgeNodePairs.

NumEdges — Number of edges in pose graph

0 (default) | nonnegative integer

This property is read-only.

Number of edges in pose graph, specified as a nonnegative integer. Each edge connects two nodes in the pose graph. Loop closure edges and landmark edges are included.

NumLoopClosureEdges — Number of loop closures

0 (default) | nonnegative integer

This property is read-only.

Number of loop closures in pose graph, specified as a nonnegative integer. To get the edge IDs of the loop closures, use the LoopClosureEdgeIDs property.

LoopClosureEdgeIDs — Loop closure edge IDs

vector

This property is read-only.

Loop closure edges IDs, specified as a vector of edge IDs.

LandmarkNodeIDs — Landmark node IDs

vector

This property is read-only.

Landmark node IDs, specified as a vector of IDs for each node.

Object Functions

addPointLandmarkAdd landmark point node to pose graph addRelativePose Add relative pose to pose graph Create copy of pose graph copy Edge node pairs in pose graph edgeNodePairs edgeConstraints Edge constraints in pose graph Compute pose graph edge residual errors edgeResidualErrors findEdgeID Find edge ID of edge nodeEstimates Poses of nodes in pose graph removeEdges Remove loop closure edges from graph show Plot pose graph

111113

Examples

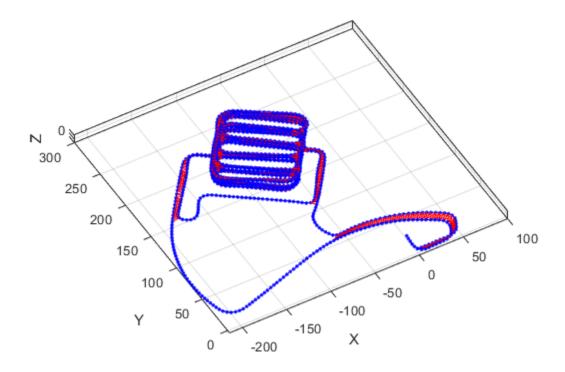
Optimize a 3-D Pose Graph

Optimize a pose graph based on the nodes and edge constraints. The pose graph used in this example is taken from the MIT Dataset and was generated using information extracted from a parking garage.

Load the pose graph from the MIT dataset. Inspect the poseGraph3D object to view the number of nodes and loop closures.

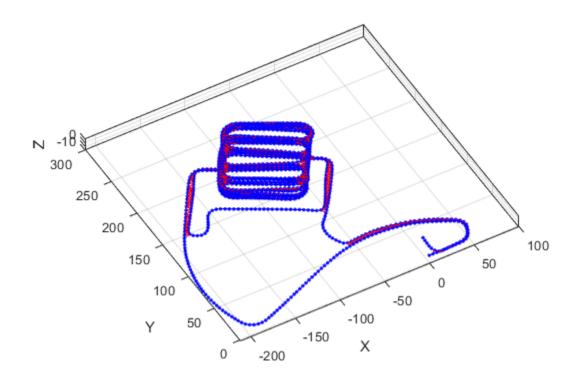
Plot the pose graph with IDs off. Red lines indicate loop closures identified in the dataset.

```
title('Original Pose Graph')
show(pg,'IDs','off');
view(-30,45)
```



Optimize the pose graph. Nodes are adjusted based on the edge constraints and loop closures. Plot the optimized pose graph to see the adjustment of the nodes with loop closures.

```
updatedPG = optimizePoseGraph(pg);
figure
title('Updated Pose Graph')
show(updatedPG,'IDs','off');
view(-30,45)
```



References

[1] Carlone, Luca, Roberto Tron, Kostas Daniilidis, and Frank Dellaert. "Initialization Techniques for 3D SLAM: a Survey on Rotation Estimation and its Use in Pose Graph Optimization." 2015 IEEE International Conference on Robotics and Automation (ICRA). 2015, pp. 4597–4604.

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

Use this syntax when constructing poseGraph3D objects for code generation:

 $poseGraph = poseGraph3D('MaxNumEdges', maxEdges, 'MaxNumNodes', maxNodes) \ specifies \\ an upper bound on the number of edges and nodes allowed in the pose graph when generating code. \\ This limit is only required when generating code.$

See Also

Functions

addPointLandmark | addRelativePose | optimizePoseGraph

Objects

lidarSLAM | poseGraph

Topics"Landmark SLAM Using AprilTag Markers"

Introduced in R2019b

quaternion

Create a quaternion array

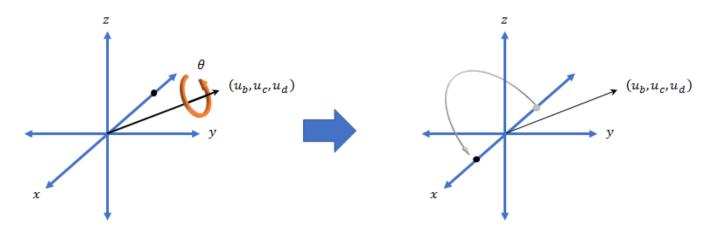
Description

A quaternion is a four-part hyper-complex number used in three-dimensional rotations and orientations.

A quaternion number is represented in the form a + bi + cj + dk, where a, b, c, and d parts are real numbers, and i, j, and k are the basis elements, satisfying the equation: $i^2 = j^2 = k^2 = ijk = -1$.

The set of quaternions, denoted by \mathbf{H} , is defined within a four-dimensional vector space over the real numbers, \mathbf{R}^4 . Every element of \mathbf{H} has a unique representation based on a linear combination of the basis elements, i, j, and k.

All rotations in 3-D can be described by an axis of rotation and angle about that axis. An advantage of quaternions over rotation matrices is that the axis and angle of rotation is easy to interpret. For example, consider a point in \mathbf{R}^3 . To rotate the point, you define an axis of rotation and an angle of rotation.



The quaternion representation of the rotation may be expressed as $q = \cos(\theta/2) + \sin(\theta/2)(u_b i + u_c j + u_d k)$, where θ is the angle of rotation and $[u_b, u_c, and u_d]$ is the axis of rotation.

Creation

Syntax

```
quat = quaternion()
quat = quaternion(A,B,C,D)
quat = quaternion(matrix)
quat = quaternion(RV,'rotvec')
```

```
quat = quaternion(RV,'rotvecd')
quat = quaternion(RM,'rotmat',PF)
quat = quaternion(E,'euler',RS,PF)
quat = quaternion(E,'eulerd',RS,PF)
```

Description

quat = quaternion() creates an empty quaternion.

quat = quaternion(A,B,C,D) creates a quaternion array where the four quaternion parts are taken from the arrays A, B, C, and D. All the inputs must have the same size and be of the same data type.

quat = quaternion(matrix) creates an N-by-1 quaternion array from an N-by-4 matrix, where each column becomes one part of the quaternion.

quat = quaternion(RV, 'rotvec') creates an N-by-1 quaternion array from an N-by-3 matrix of rotation vectors, RV. Each row of RV represents a rotation vector in radians.

quat = quaternion(RV, 'rotvecd') creates an N-by-1 quaternion array from an N-by-3 matrix of rotation vectors, RV. Each row of RV represents a rotation vector in degrees.

quat = quaternion(RM, 'rotmat', PF) creates an N-by-1 quaternion array from the 3-by-3-by-N array of rotation matrices, RM. PF can be either 'point' if the Euler angles represent point rotations or 'frame' for frame rotations.

quat = quaternion(E, 'euler', RS, PF) creates an N-by-1 quaternion array from the N-by-3 matrix, E. Each row of E represents a set of Euler angles in radians. The angles in E are rotations about the axes in sequence RS.

quat = quaternion(E, 'eulerd', RS, PF) creates an N-by-1 quaternion array from the N-by-3 matrix, E. Each row of E represents a set of Euler angles in degrees. The angles in E are rotations about the axes in sequence RS.

Input Arguments

A,B,C,D — Quaternion parts

comma-separated arrays of the same size

Parts of a quaternion, specified as four comma-separated scalars, matrices, or multi-dimensional arrays of the same size.

```
Example: quat = quaternion(1,2,3,4) creates a quaternion of the form 1 + 2i + 3j + 4k.

Example: quat = quaternion([1,5],[2,6],[3,7],[4,8]) creates a 1-by-2 quaternion array where quat(1,1) = 1 + 2i + 3j + 4k and quat(1,2) = 5 + 6i + 7j + 8k

Data Types: single | double
```

matrix — Matrix of quaternion parts

N-by-4 matrix

Matrix of quaternion parts, specified as an *N*-by-4 matrix. Each row represents a separate quaternion. Each column represents a separate quaternion part.

Example: quat = quaternion(rand(10,4)) creates a 10-by-1 quaternion array.

Data Types: single | double

RV — Matrix of rotation vectors

N-by-3 matrix

Matrix of rotation vectors, specified as an *N*-by-3 matrix. Each row of RV represents the [X Y Z] elements of a rotation vector. A rotation vector is a unit vector representing the axis of rotation scaled by the angle of rotation in radians or degrees.

To use this syntax, specify the first argument as a matrix of rotation vectors and the second argument as the 'rotvec' or 'rotvecd'.

```
Example: quat = quaternion(rand(10,3),'rotvec') creates a 10-by-1 quaternion array. Data Types: single | double
```

RM — Rotation matrices

3-by-3 matrix | 3-by-3-by-*N* array

Array of rotation matrices, specified by a 3-by-3 matrix or 3-by-3-by-*N* array. Each page of the array represents a separate rotation matrix.

```
Example: quat = quaternion(rand(3),'rotmat','point')
Example: quat = quaternion(rand(3),'rotmat','frame')
Data Types: single | double
```

PF — Type of rotation matrix

```
'point'|'frame'
```

Type of rotation matrix, specified by 'point' or 'frame'.

```
Example: quat = quaternion(rand(3),'rotmat','point')
Example: quat = quaternion(rand(3),'rotmat','frame')
Data Types: char | string
```

E — Matrix of Euler angles

N-by-3 matrix

Matrix of Euler angles, specified by an N-by-3 matrix. If using the 'euler' syntax, specify E in radians. If using the 'eulerd' syntax, specify E in degrees.

```
Example: quat = quaternion(E, 'euler', 'YZY', 'point')
Example: quat = quaternion(E, 'euler', 'XYZ', 'frame')
Data Types: single | double
```

RS — Rotation sequence

character vector | scalar string

Rotation sequence, specified as a three-element character vector:

- 'YZY'
- 'YXY'
- 'ZYZ'

- 'ZXZ'
- 'XYX'
- 'XZX'
- 'XYZ'
- 'YZX'
- 'ZXY'
- 'XZY'
- 'ZYX'
- 'YXZ'

Assume you want to determine the new coordinates of a point when its coordinate system is rotated using frame rotation. The point is defined in the original coordinate system as:

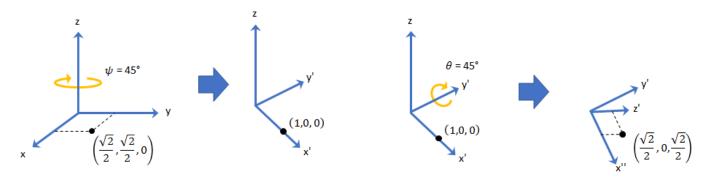
```
point = [sqrt(2)/2, sqrt(2)/2, 0];
```

In this representation, the first column represents the *x*-axis, the second column represents the *y*-axis, and the third column represents the *z*-axis.

You want to rotate the point using the Euler angle representation [45,45,0]. Rotate the point using two different rotation sequences:

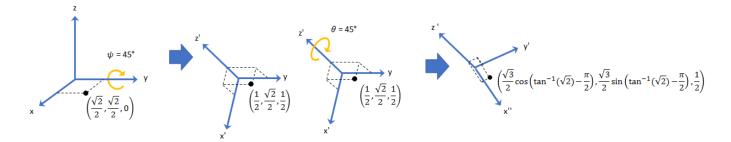
• If you create a quaternion rotator and specify the 'ZYX' sequence, the frame is first rotated 45° around the *z*-axis, then 45° around the new *y*-axis.

```
quatRotator = quaternion([45,45,0],'eulerd','ZYX','frame');
newPointCoordinate = rotateframe(quatRotator,point)
newPointCoordinate =
    0.7071   -0.0000    0.7071
```



• If you create a quaternion rotator and specify the 'YZX' sequence, the frame is first rotated 45° around the *y*-axis, then 45° around the new *z*-axis.

```
quatRotator = quaternion([45,45,0],'eulerd','YZX','frame');
newPointCoordinate = rotateframe(quatRotator,point)
newPointCoordinate =
    0.8536    0.1464    0.5000
```



Data Types: char | string

Object Functions

angvel Angular velocity from quaternion array

classUnderlying Class of parts within quaternion

compact Convert quaternion array to N-by-4 matrix

conj Complex conjugate of quaternion

ctranspose, ' Complex conjugate transpose of quaternion array

dist Angular distance in radians

euler Convert quaternion to Euler angles (radians) eulerd Convert quaternion to Euler angles (degrees)

exp Exponential of quaternion array ldivide, .\ Element-wise quaternion left division Natural logarithm of quaternion array

meanrot Quaternion mean rotation minus, - Quaternion subtraction mtimes, * Quaternion multiplication

norm Quaternion norm

normalize Quaternion normalization

ones Create quaternion array with real parts set to one and imaginary parts set to zero

parts Extract quaternion parts

power, .^ Element-wise quaternion power prod Product of a quaternion array

randrot Uniformly distributed random rotations rdivide, ./ Element-wise guaternion right division

rotateframe Quaternion frame rotation rotatepoint Quaternion point rotation

rotmat Convert quaternion to rotation matrix

rotvec Convert quaternion to rotation vector (radians) rotvecd Convert quaternion to rotation vector (degrees)

slerp Spherical linear interpolation

times, .* Element-wise quaternion multiplication

transpose, ' Transpose a quaternion array uminus, - Quaternion unary minus

zeros Create quaternion array with all parts set to zero

Examples

Create Empty Quaternion

quat = quaternion()

```
quat =
    0x0 empty quaternion array
By default, the underlying class of the quaternion is a double.
classUnderlying(quat)
ans =
'double'
```

Create Quaternion by Specifying Individual Quaternion Parts

You can create a quaternion array by specifying the four parts as comma-separated scalars, matrices, or multidimensional arrays of the same size.

Define quaternion parts as scalars.

Define quaternion parts as column vectors.

Define quaternion parts as matrices.

Define quaternion parts as three dimensional arrays.

```
A = randn(2,2,2);
B = zeros(2,2,2);
C = zeros(2,2,2);
D = zeros(2,2,2);
quatMultiDimArray = quaternion(A,B,C,D)
quatMultiDimArray = 2x2x2 quaternion array
quatMultiDimArray(:,:,1) =
     0.53767 +
                     0i +
                                 0j +
                                            0 k
                                                   -2.2588 +
                                                                    0i +
                                                                                0j +
                                                                                           0k
      1.8339 +
                     0i +
                                 0j +
                                            0k
                                                   0.86217 +
                                                                    0i +
                                                                                0i +
                                                                                           0k
quatMultiDimArray(:,:,2) =
     0.31877 +
                                                                    0i +
                     0i +
                                 0j +
                                                   -0.43359 +
                                                                                0j +
                                                                                           0k
                                            0 k
     -1.3077 +
                     0i +
                                 0j +
                                                   0.34262 +
                                                                    0i +
                                                                                0j +
                                                                                           0k
                                            0 k
```

Create Quaternion by Specifying Quaternion Parts Matrix

You can create a scalar or column vector of quaternions by specify an N-by-4 matrix of quaternion parts, where columns correspond to the quaternion parts A, B, C, and D.

Create a column vector of random quaternions.

```
quatParts = rand(3,4)
quatParts = 3 \times 4
   0.8147
              0.9134
                        0.2785
                                  0.9649
   0.9058
              0.6324
                        0.5469
                                  0.1576
   0.1270
              0.0975
                        0.9575
                                  0.9706
quat = quaternion(quatParts)
quat=3×1 quaternion array
     0.81472 + 0.91338i + 0.2785j + 0.96489k
     0.90579 + 0.63236i + 0.54688j + 0.15761k
     0.12699 + 0.09754i + 0.95751j + 0.97059k
```

To retrieve the quatParts matrix from quaternion representation, use compact.

```
retrievedquatParts = compact(quat)
```

```
retrievedquatParts = 3×4

0.8147  0.9134  0.2785  0.9649

0.9058  0.6324  0.5469  0.1576

0.1270  0.0975  0.9575  0.9706
```

Create Quaternion by Specifying Rotation Vectors

You can create an N-by-1 quaternion array by specifying an N-by-3 matrix of rotation vectors in radians or degrees. Rotation vectors are compact spatial representations that have a one-to-one relationship with normalized quaternions.

Rotation Vectors in Radians

Create a scalar quaternion using a rotation vector and verify the resulting quaternion is normalized.

You can convert from quaternions to rotation vectors in radians using the rotvec function. Recover the rotationVector from the quaternion, quat.

```
rotvec(quat) ans = 1 \times 3 0.3491 0.6283 0.3491
```

Rotation Vectors in Degrees

Create a scalar quaternion using a rotation vector and verify the resulting quaternion is normalized.

You can convert from quaternions to rotation vectors in degrees using the rotvecd function. Recover the rotationVector from the quaternion, quat.

```
rotvecd(quat)
ans = 1×3
20.0000 36.0000 20.0000
```

Create Quaternion by Specifying Rotation Matrices

You can create an N-by-1 quaternion array by specifying a 3-by-3-by-N array of rotation matrices. Each page of the rotation matrix array corresponds to one element of the quaternion array.

Create a scalar quaternion using a 3-by-3 rotation matrix. Specify whether the rotation matrix should be interpreted as a frame or point rotation.

You can convert from quaternions to rotation matrices using the rotmat function. Recover the rotationMatrix from the quaternion, quat.

Create Quaternion by Specifying Euler Angles

You can create an *N*-by-1 quaternion array by specifying an *N*-by-3 array of Euler angles in radians or degrees.

Euler Angles in Radians

Use the euler syntax to create a scalar quaternion using a 1-by-3 vector of Euler angles in radians. Specify the rotation sequence of the Euler angles and whether the angles represent a frame or point rotation.

```
E = [pi/2,0,pi/4];
quat = quaternion(E,'euler','ZYX','frame')

quat = quaternion
    0.65328 + 0.2706i + 0.2706j + 0.65328k
```

You can convert from quaternions to Euler angles using the euler function. Recover the Euler angles, E, from the quaternion, quat.

```
euler(quat, 'ZYX', 'frame') ans = 1 \times 3
1.5708 0 0.7854
```

Euler Angles in Degrees

Use the eulerd syntax to create a scalar quaternion using a 1-by-3 vector of Euler angles in degrees. Specify the rotation sequence of the Euler angles and whether the angles represent a frame or point rotation.

```
E = [90,0,45];
quat = quaternion(E,'eulerd','ZYX','frame')

quat = quaternion
     0.65328 + 0.2706i + 0.2706j + 0.65328k
```

You can convert from quaternions to Euler angles in degrees using the eulerd function. Recover the Euler angles, E, from the quaternion, quat.

```
eulerd(quat,'ZYX','frame')
ans = 1×3
90.0000 0 45.0000
```

Quaternion Algebra

Quaternions form a noncommutative associative algebra over the real numbers. This example illustrates the rules of quaternion algebra.

Addition and Subtraction

Quaternion addition and subtraction occur part-by-part, and are commutative:

```
Q1 = quaternion(1,2,3,4)
Q1 = quaternion
    1 + 2i + 3j + 4k

Q2 = quaternion(9,8,7,6)
Q2 = quaternion
    9 + 8i + 7j + 6k

Q1plusQ2 = Q1 + Q2

Q1plusQ2 = quaternion
    10 + 10i + 10j + 10k

Q2plusQ1 = Q2 + Q1

Q2plusQ1 = quaternion
    10 + 10i + 10j + 10k
Q1minusQ2 = Q1 - Q2
```

```
QlminusQ2 = quaternion

-8 - 6i - 4j - 2k

Q2minusQ1 = Q2 - Q1

Q2minusQ1 = quaternion

8 + 6i + 4j + 2k
```

You can also perform addition and subtraction of real numbers and quaternions. The first part of a quaternion is referred to as the *real* part, while the second, third, and fourth parts are referred to as the *vector*. Addition and subtraction with real numbers affect only the real part of the quaternion.

```
Q1plusRealNumber = Q1 + 5
Q1plusRealNumber = quaternion
6 + 2i + 3j + 4k

Q1minusRealNumber = Q1 - 5
Q1minusRealNumber = quaternion
-4 + 2i + 3j + 4k
```

Multiplication

Quaternion multiplication is determined by the products of the basis elements and the distributive law. Recall that multiplication of the basis elements, i, j, and k, are not commutative, and therefore quaternion multiplication is not commutative.

You can also multiply a quaternion by a real number. If you multiply a quaternion by a real number, each part of the quaternion is multiplied by the real number individually:

```
Q1times5 = Q1*5

Q1times5 = quaternion
5 + 10i + 15j + 20k
```

Multiplying a quaternion by a real number is commutative.

```
isequal(Q1*5,5*Q1)
ans = logical
1
```

Conjugation

The complex conjugate of a quaternion is defined such that each element of the vector portion of the quaternion is negated.

```
Q1 = quaternion

1 + 2i + 3j + 4k

conj(Q1)

ans = quaternion

1 - 2i - 3j - 4k
```

Multiplication between a quaternion and its conjugate is commutative:

```
isequal(Q1*conj(Q1),conj(Q1)*Q1)
ans = logical
1
```

Quaternion Array Manipulation

You can organize quaternions into vectors, matrices, and multidimensional arrays. Built-in MATLAB® functions have been enhanced to work with quaternions.

Concatenate

Quaternions are treated as individual objects during concatenation and follow MATLAB rules for array manipulation.

Indexing

To access or assign elements in a quaternion array, use indexing.

```
qLoc2 = qMultiDimensionalArray(2)
qLoc2 = quaternion
    -1 - 2i - 3j - 4k
```

Replace the quaternion at index two with a quaternion one.

Reshape

To reshape quaternion arrays, use the reshape function.

```
qMatReshaped = reshape(qMatrix,4,1)
qMatReshaped=4×1 quaternion array
    1 + 2i + 3j + 4k
    -1 - 2i - 3j - 4k
    9 + 8i + 7j + 6k
    -9 - 8i - 7j - 6k
```

Transpose

To transpose quaternion vectors and matrices, use the transpose function.

```
qMatTransposed = transpose(qMatrix)
```

Permute

To permute quaternion vectors, matrices, and multidimensional arrays, use the permute function.

qMultiDimensionalArray

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

Topics

[&]quot;Rotations, Orientation, and Quaternions"

[&]quot;Lowpass Filter Orientation Using Quaternion SLERP"

Introduced in R2019b

angvel

Angular velocity from quaternion array

Syntax

```
AV = angvel(Q,dt,'frame')
AV = angvel(Q,dt,'point')
[AV,qf] = angvel(0,dt,fp,qi)
```

Description

AV = angvel(Q,dt,'frame') returns the angular velocity array from an array of quaternions, Q. The quaternions in Q correspond to frame rotation. The initial quaternion is assumed to represent zero rotation.

AV = angvel(Q,dt,'point') returns the angular velocity array from an array of quaternions, Q. The quaternions in Q correspond to point rotation. The initial quaternion is assumed to represent zero rotation.

[AV,qf] = angvel(Q,dt,fp,qi) allows you to specify the initial quaternion, qi, and the type of rotation, fp. It also returns the final quaternion, qf.

Examples

Generate Angular Velocity From Quaternion Array

Create an array of quaternions.

0

0

(-)

0

0

```
eulerAngles = [(0:10:90).', zeros(numel(0:10:90),2)];
q = quaternion(eulerAngles, 'eulerd', 'ZYX', 'frame');
Specify the time step and generate the angular velocity array.
av = angvel(q,dt,'frame') % units in rad/s
av = 10 \times 3
          0
                     0
          0
                     0
                          0.1743
                     0
                          0.1743
          0
                     0
                          0.1743
```

0.1743

0.1743

0.1743

0.1743

0.1743

0.1743

0

0

0

0

0

(-)

Input Arguments

Q — Quaternions

N-by-1 vector of quaternions

Quaternions, specified as an *N*-by-1 vector of quaternions.

Data Types: quaternion

dt - Time step

nonnegative scalar

Time step, specified as a nonnegative scalar.

Data Types: single | double

fp — Type of rotation

'frame'|'point'

Type of rotation, specified as 'frame' or 'point'.

qi — Initial quaternion

quaternion

Initial quaternion, specified as a quaternion.

Data Types: quaternion

Output Arguments

AV — Angular velocity

N-by-3 real matrix

Angular velocity, returned as an N-by-3 real matrix. N is the number of quaternions given in the input Q. Each row of the matrix corresponds to an angular velocity vector.

qf — Final quaternion

quaternion

Final quaternion, returned as a quaternion. qf is the same as the last quaternion in the Q input.

Data Types: quaternion

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

quaternion

Topics

"Rotations, Orientation, and Quaternions"

Introduced in R2020a

classUnderlying

Class of parts within quaternion

Syntax

```
underlyingClass = classUnderlying(quat)
```

Description

underlyingClass = classUnderlying(quat) returns the name of the class of the parts of the
quaternion quat.

Examples

Get Underlying Class of Quaternion

A quaternion is a four-part hyper-complex number used in three-dimensional representations. The four parts of the quaternion are of data type single or double.

Create two quaternions, one with an underlying data type of single, and one with an underlying data type of double. Verify the underlying data types by calling classUnderlying on the quaternions.

You can separate quaternions into their parts using the parts function. Verify the parts of each quaternion are the correct data type. Recall that double is the default MATLAB® type.

```
[aS,bS,cS,dS] = parts(qSingle)
aS = single
```

```
bS = single
2
cS = single
3
dS = single
4

[aD,bD,cD,dD] = parts(qDouble)
aD = 1
bD = 2
cD = 3
dD = 4
```

Quaternions follow the same implicit casting rules as other data types in MATLAB. That is, a quaternion with underlying data type single that is combined with a quaternion with underlying data type double results in a quaternion with underlying data type single. Multiply qDouble and qSingle and verify the resulting underlying data type is single.

```
q = qDouble*qSingle;
classUnderlying(q)
ans =
'single'
```

Input Arguments

quat — Quaternion to investigate

scalar | vector | matrix | multi-dimensional array

Quaternion to investigate, specified as a quaternion or array of quaternions.

Data Types: quaternion

Output Arguments

underlyingClass — Underlying class of quaternion object

```
'single'|'double'
```

Underlying class of quaternion, returned as the character vector 'single' or 'double'.

Data Types: char

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

Functions

compact | parts

Objects

quaternion

Topics "Rotations, Orientation, and Quaternions"

compact

Convert quaternion array to N-by-4 matrix

Syntax

```
matrix = compact(quat)
```

Description

matrix = compact(quat) converts the quaternion array, quat, to an N-by-4 matrix. The columns are made from the four quaternion parts. The ith row of the matrix corresponds to quat(i).

Examples

Convert Quaternion Array to Compact Representation of Parts

Create a scalar quaternion with random parts. Convert the parts to a 1-by-4 vector using compact.

```
randomParts = randn(1,4)
randomParts = 1×4
    0.5377    1.8339   -2.2588    0.8622

quat = quaternion(randomParts)
quat = quaternion
    0.53767 + 1.8339i - 2.2588j + 0.86217k

quatParts = compact(quat)
quatParts = 1×4
    0.5377    1.8339   -2.2588    0.8622
```

Create a 2-by-2 array of quaternions, then convert the representation to a matrix of quaternion parts. The output rows correspond to the linear indices of the quaternion array.

Τ	2	3	4
5	6	7	8
9	10	11	12
13	14	15	16

Input Arguments

quat — Quaternion to convert

scalar | vector | matrix | multidimensional array

Quaternion to convert, specified as scalar, vector, matrix, or multidimensional array of quaternions.

Data Types: quaternion

Output Arguments

matrix — Quaternion in matrix form

N-by-4 matrix

Quaternion in matrix form, returned as an N-by-4 matrix, where N = numel(quat).

Data Types: single | double

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

Functions

classUnderlying|parts

Objects

quaternion

Tonics

"Rotations, Orientation, and Quaternions"

conj

Complex conjugate of quaternion

Syntax

```
quatConjugate = conj(quat)
```

Description

```
quatConjugate = conj(quat) returns the complex conjugate of the quaternion, quat.
```

If q = a + bi + cj + dk, the complex conjugate of q is $q^* = a - bi - cj - dk$. Considered as a rotation operator, the conjugate performs the opposite rotation. For example,

Examples

Complex Conjugate of Quaternion

Create a quaternion scalar and get the complex conjugate.

Verify that a quaternion multiplied by its conjugate returns a quaternion one.

q*qConj

```
ans = quaternion
1 + 0i + 0j + 0k
```

Input Arguments

quat — Quaternion

scalar | vector | matrix | multidimensional array

Quaternion to conjugate, specified as a scalar, vector, matrix, or array of quaternions.

Data Types: quaternion

Output Arguments

quatConjugate — Quaternion conjugate

scalar | vector | matrix | multidimensional array

Quaternion conjugate, returned as a quaternion or array of quaternions the same size as quat.

Data Types: quaternion

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

Functions

norm|times, .*

Objects

quaternion

Topics

"Rotations, Orientation, and Quaternions"

ctranspose, '

Complex conjugate transpose of quaternion array

Syntax

```
quatTransposed = quat'
```

Description

quatTransposed = quat' returns the complex conjugate transpose of the quaternion, quat.

Examples

Vector Complex Conjugate Transpose

Create a vector of quaternions and compute its complex conjugate transpose.

```
quatTransposed=1×4 quaternion array
0.53767 - 0.31877i - 3.5784j - 0.7254k 1.8339 + 1.3077i - 2.7694j + 0.063055
```

Matrix Complex Conjugate Transpose

3.5784 +

Create a matrix of quaternions and compute its complex conjugate transpose.

```
quat = [quaternion(randn(2,4)),quaternion(randn(2,4))]
```

0.53767 + 2.2588i - 0.31877j + 0.43359k

1.3499i - 0.7254j - 0.71474k

1.8339 - 0.86217i + 1.3077j - 0.3426

2.7694 - 3.0349i + 0.063055j + 0.2049

Input Arguments

quat — Quaternion to transpose

scalar | vector | matrix

Quaternion to transpose, specified as a vector or matrix or quaternions. The complex conjugate transpose is defined for 1-D and 2-D arrays.

Data Types: quaternion

Output Arguments

quatTransposed — Conjugate transposed quaternion

scalar | vector | matrix

Conjugate transposed quaternion, returned as an N-by-M array, where quat was specified as an M-by-N array.

Data Types: quaternion

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

Functions

transpose, '

Objects

quaternion

Topics

"Rotations, Orientation, and Quaternions"

dist

Angular distance in radians

Syntax

```
distance = dist(quatA, quatB)
```

Description

distance = dist(quatA, quatB) returns the angular distance in radians between two
quaternions, quatA and quatB.

Examples

Calculate Quaternion Distance

Calculate the quaternion distance between a single quaternion and each element of a vector of quaternions. Define the quaternions using Euler angles.

```
q = quaternion([0,0,0],'eulerd','zyx','frame')
q = quaternion
    1 + 0i + 0j + 0k
qArray = quaternion([0,45,0;0,90,0;0,180,0;0,-90,0;0,-45,0],'eulerd','zyx','frame')
qArray=5×1 quaternion array
                 0i +
                               0.38268j +
                                                  0k
      0.92388 +
       0.70711 +
                        0i +
                               0.70711j +
                                                  0k
   6.1232e-17 +
                        0i +
                                                  0k
                                      1j +
                        0i -
       0.70711 +
                               0.70711j +
                                                  0k
      0.92388 +
                       0i -
                               0.38268j +
                                                  0k
quaternionDistance = rad2deg(dist(q,qArray))
quaternionDistance = 5 \times 1
   45.0000
   90.0000
  180.0000
   90.0000
   45.0000
```

If both arguments to dist are vectors, the quaternion distance is calculated between corresponding elements. Calculate the quaternion distance between two quaternion vectors.

```
angles1 = [30,0,15; ... 30,5,15; ...
```

```
30,10,15; ...
30,15,15];

angles2 = [30,6,15; ...
31,11,15; ...
30,16,14; ...
30.5,21,15.5];

qVector1 = quaternion(angles1,'eulerd','zyx','frame');
qVector2 = quaternion(angles2,'eulerd','zyx','frame');
rad2deg(dist(qVector1,qVector2))

ans = 4×1
6.0000
6.0827
6.0827
6.0827
6.0287
```

Note that a quaternion represents the same rotation as its negative. Calculate a quaternion and its negative.

Find the distance between the quaternion and its negative.

```
dist(qPositive,qNegative)
ans = 0
```

The components of a quaternion may look different from the components of its negative, but both expressions represent the same rotation.

Input Arguments

quatA, quatB — Quaternions to calculate distance between

```
scalar | vector | matrix | multidimensional array
```

Quaternions to calculate distance between, specified as comma-separated quaternions or arrays of quaternions. quatA and quatB must have compatible sizes:

```
    size(quatA) == size(quatB), or
    numel(quatA) == 1, or
    numel(quatB) == 1, or
```

• if [Adim1,...,AdimN] = size(quatA) and [Bdim1,...,BdimN] = size(quatB), then for i = 1:N, either Adimi==Bdimi or Adim==1 or Bdim==1.

If one of the quaternion arguments contains only one quaternion, then this function returns the distances between that quaternion and every quaternion in the other argument.

Data Types: quaternion

Output Arguments

distance — Angular distance (radians)

scalar | vector | matrix | multidimensional array

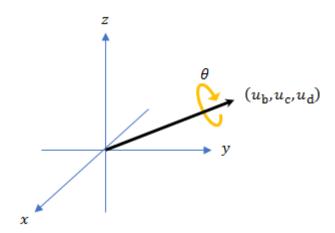
Angular distance in radians, returned as an array. The dimensions are the maximum of the union of size(quatA) and size(quatB).

Data Types: single | double

Algorithms

The dist function returns the angular distance between two quaternions.

A quaternion may be defined by an axis (u_b, u_c, u_d) and angle of rotation θ_q : $q = \cos(\theta q/2) + \sin(\theta q/2)(u_b i + u_c j + u_d k)$.



Given a quaternion in the form, q = a + bi + cj + dk, where a is the real part, you can solve for the angle of q as $\theta_q = 2\cos^{-1}(a)$.

Consider two quaternions, p and q, and the product $z = p * \operatorname{conjugate}(q)$. As p approaches q, the angle of z goes to 0, and z approaches the unit quaternion.

The angular distance between two quaternions can be expressed as $\theta_z = 2\cos^{-1}(\text{real}(z))$.

Using the quaternion data type syntax, the angular distance is calculated as:

angularDistance = 2*acos(abs(parts(p*conj(q))));

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder $^{\text{\tiny TM}}$.

See Also

Functions

conj | parts

Objects

quaternion

Topics

"Rotations, Orientation, and Quaternions"

euler

Convert guaternion to Euler angles (radians)

Syntax

eulerAngles = euler(quat,rotationSequence,rotationType)

Description

eulerAngles = euler(quat, rotationSequence, rotationType) converts the quaternion, quat, to an N-by-3 matrix of Euler angles.

Examples

Convert Quaternion to Euler Angles in Radians

Convert a quaternion frame rotation to Euler angles in radians using the 'ZYX' rotation sequence.

```
quat = quaternion([0.7071 0.7071 0 0]);
eulerAnglesRandians = euler(quat,'ZYX','frame')
eulerAnglesRandians = 1\times3
0 0 1.5708
```

Input Arguments

quat — Quaternion to convert to Euler angles

scalar | vector | matrix | multidimensional array

Quaternion to convert to Euler angles, specified as a scalar, vector, matrix, or multidimensional array of quaternions.

Data Types: quaternion

```
rotationSequence — Rotation sequence
'ZYX' | 'ZYZ' | 'ZXY' | 'ZXZ' | 'YXZ' | 'YXY' | 'YZX' | 'XYZ' | 'XYX' | 'XZY' | 'XZX'
```

Rotation sequence of Euler representation, specified as a character vector or string.

The rotation sequence defines the order of rotations about the axes. For example, if you specify a rotation sequence of 'YZX':

- **1** The first rotation is about the y-axis.
- **2** The second rotation is about the new z-axis.
- **3** The third rotation is about the new x-axis.

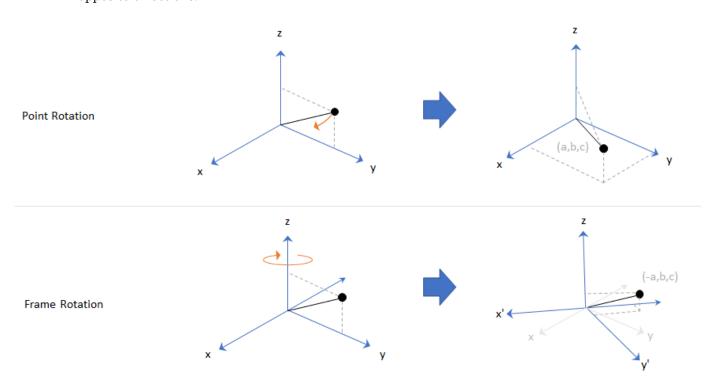
Data Types: char | string

rotationType — Type of rotation

'point'|'frame'

Type of rotation, specified as 'point' or 'frame'.

In a point rotation, the frame is static and the point moves. In a frame rotation, the point is static and the frame moves. Point rotation and frame rotation define equivalent angular displacements but in opposite directions.



Data Types: char | string

Output Arguments

eulerAngles — Euler angle representation (radians)

N-by-3 matrix

Euler angle representation in radians, returned as a N-by-3 matrix. N is the number of quaternions in the quat argument.

For each row of eulerAngles, the first element corresponds to the first axis in the rotation sequence, the second element corresponds to the second axis in the rotation sequence, and the third element corresponds to the third axis in the rotation sequence.

The data type of the Euler angles representation is the same as the underlying data type of quat.

Data Types: single | double

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

Functions

eulerd|rotateframe|rotatepoint

Objects

quaternion

Topics

"Rotations, Orientation, and Quaternions"

eulerd

Convert quaternion to Euler angles (degrees)

Syntax

eulerAngles = eulerd(quat,rotationSequence,rotationType)

Description

eulerAngles = eulerd(quat, rotationSequence, rotationType) converts the quaternion, quat, to an N-by-3 matrix of Euler angles in degrees.

Examples

Convert Quaternion to Euler Angles in Degrees

Convert a quaternion frame rotation to Euler angles in degrees using the 'ZYX' rotation sequence.

Input Arguments

quat — Quaternion to convert to Euler angles

scalar | vector | matrix | multidimensional array

Quaternion to convert to Euler angles, specified as a scalar, vector, matrix, or multidimensional array of quaternions.

Data Types: quaternion

```
rotationSequence — Rotation sequence
'ZYX' | 'ZYZ' | 'ZXY' | 'ZXZ' | 'YXZ' | 'YXY' | 'YZX' | 'XYZ' | 'XYX' | 'XZY' | 'XZX'
```

Rotation sequence of Euler angle representation, specified as a character vector or string.

The rotation sequence defines the order of rotations about the axes. For example, if you specify a rotation sequence of 'YZX':

- **1** The first rotation is about the *y*-axis.
- **2** The second rotation is about the new z-axis.
- **3** The third rotation is about the new x-axis.

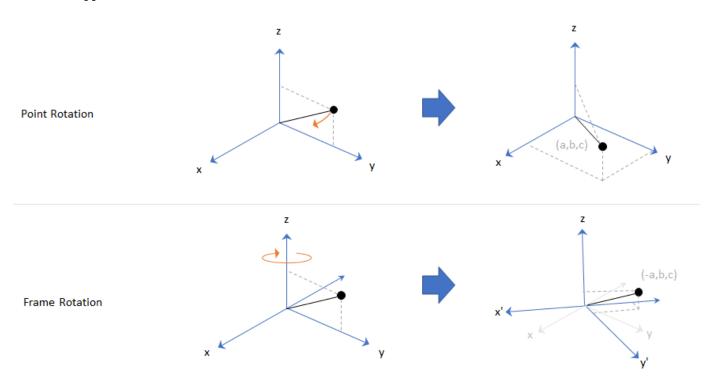
Data Types: char | string

rotationType — Type of rotation

'point'|'frame'

Type of rotation, specified as 'point' or 'frame'.

In a point rotation, the frame is static and the point moves. In a frame rotation, the point is static and the frame moves. Point rotation and frame rotation define equivalent angular displacements but in opposite directions.



Data Types: char | string

Output Arguments

eulerAngles — Euler angle representation (degrees)

N-by-3 matrix

Euler angle representation in degrees, returned as a N-by-3 matrix. N is the number of quaternions in the quat argument.

For each row of eulerAngles, the first column corresponds to the first axis in the rotation sequence, the second column corresponds to the second axis in the rotation sequence, and the third column corresponds to the third axis in the rotation sequence.

The data type of the Euler angles representation is the same as the underlying data type of quat.

Data Types: single | double

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

Functions

euler | rotateframe | rotatepoint

Objects

quaternion

Topics

"Rotations, Orientation, and Quaternions"

exp

Exponential of quaternion array

Syntax

```
B = exp(A)
```

Description

 $B = \exp(A)$ computes the exponential of the elements of the quaternion array A.

Examples

Exponential of Quaternion Array

Create a 4-by-1 quaternion array A.

```
A = quaternion(magic(4))
```

Compute the exponential of A.

```
B = \exp(A)
```

```
B=4×1 quaternion array
5.3525e+06 + 1.0516e+06i + 1.5774e+06j + 6.8352e+06k
-57.359 - 89.189i - 81.081j - 64.865k
-6799.1 + 2039.1i + 1747.8j + 3495.6k
-6.66 + 36.931i + 39.569j + 2.6379k
```

Input Arguments

A — Input quaternion

scalar | vector | matrix | multidimensional array

Input quaternion, specified as a scalar, vector, matrix, or multidimensional array.

Data Types: quaternion

Output Arguments

B - Result

scalar | vector | matrix | multidimensional array

Result of quaternion exponential, returned as a scalar, vector, matrix, or multidimensional array. Data Types: quaternion

Algorithms

Given a quaternion $A = a + bi + cj + dk = a + \overline{v}$, the exponential is computed by

$$\exp(A) = e^a \left(\cos \lVert \bar{v} \rVert + \frac{\bar{v}}{\lVert \bar{v} \rVert} \sin \lVert \bar{v} \rVert \right)$$

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

Functions

log|power, .^

Objects

quaternion

Topics

"Rotations, Orientation, and Quaternions"

Idivide, .\

Element-wise quaternion left division

Syntax

 $C = A.\B$

Description

 $C = A \cdot B$ performs quaternion element-wise division by dividing each element of quaternion B by the corresponding element of quaternion A.

Examples

Divide a Quaternion Array by a Real Scalar

Create a 2-by-1 quaternion array, and divide it element-by-element by a real scalar.

```
A = quaternion([1:4;5:8])

A=2×1 quaternion array
    1 + 2i + 3j + 4k
    5 + 6i + 7j + 8k

B = 2;
C = A.\B

C=2×1 quaternion array
    0.066667 - 0.13333i - 0.2j - 0.26667k
    0.057471 - 0.068966i - 0.08046j - 0.091954k
```

Divide a Quaternion Array by Another Quaternion Array

Create a 2-by-2 quaternion array, and divide it element-by-element by another 2-by-2 quaternion array.

```
B=2\times 2 quaternion array 
 16+2i+3j+13k 9+7i+6j+12k 
 5+11i+10j+8k 4+14i+15j+1k
```

$C = A.\B$

```
C=2×2 quaternion array
2.7 - 1.9i - 0.9j - 1.7k 1.5159 - 0.37302i - 0.15079j - 0.0238
2.2778 + 0.46296i - 0.57407j + 0.092593k 1.2471 + 0.91379i - 0.33908j - 0.1092
```

Input Arguments

A - Divisor

scalar | vector | matrix | multidimensional array

Divisor, specified as a quaternion, an array of quaternions, a real scalar, or an array of real numbers.

A and B must have compatible sizes. In the simplest cases, they can be the same size or one can be a scalar. Two inputs have compatible sizes if, for every dimension, the dimension sizes of the inputs are the same or one of the dimensions is 1.

Data Types: quaternion | single | double

B — Dividend

scalar | vector | matrix | multidimensional array

Dividend, specified as a quaternion, an array of quaternions, a real scalar, or an array of real numbers.

A and B must have compatible sizes. In the simplest cases, they can be the same size or one can be a scalar. Two inputs have compatible sizes if, for every dimension, the dimension sizes of the inputs are the same or one of the dimensions is 1.

Data Types: quaternion | single | double

Output Arguments

C — Result

scalar | vector | matrix | multidimensional array

Result of quaternion division, returned as a scalar, vector, matrix, or multidimensional array.

Data Types: quaternion

Algorithms

Quaternion Division

Given a quaternion $A = a_1 + a_2i + a_3j + a_4k$ and a real scalar p,

$$C = p \cdot A = \frac{a_1}{p} + \frac{a_2}{p}i + \frac{a_3}{p}j + \frac{a_4}{p}k$$

Note For a real scalar p, $A./p = A. \ p$.

Quaternion Division by a Quaternion Scalar

Given two quaternions A and B of compatible sizes, then

$$C = A \cdot \backslash B = A^{-1} \cdot *B = \left(\frac{conj(A)}{norm(A)^2}\right) \cdot *B$$

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

Functions

conj | norm | rdivide, ./|times, .*

Objects

quaternion

Topics

"Rotations, Orientation, and Quaternions"

log

Natural logarithm of quaternion array

Syntax

```
B = log(A)
```

Description

B = log(A) computes the natural logarithm of the elements of the quaternion array A.

Examples

Logarithmic Values of Quaternion Array

Create a 3-by-1 quaternion array A.

```
A = quaternion(randn(3,4))
```

```
A=3×1 quaternion array

0.53767 + 0.86217i - 0.43359j + 2.7694k

1.8339 + 0.31877i + 0.34262j - 1.3499k

-2.2588 - 1.3077i + 3.5784j + 3.0349k
```

Compute the logarithmic values of A.

```
B = log(A)
```

```
B=3×1 quaternion array

1.0925 + 0.40848i - 0.20543j + 1.3121k

0.8436 + 0.14767i + 0.15872j - 0.62533k

1.6807 - 0.53829i + 1.473j + 1.2493k
```

Input Arguments

A — Input array

```
scalar | vector | matrix | multidimensional array
```

Input array, specified as a scalar, vector, matrix, or multidimensional array.

Data Types: quaternion

Output Arguments

B — Logarithm values

```
scalar | vector | matrix | multidimensional array
```

 $Quaternion\ natural\ logarithm\ values,\ returned\ as\ a\ scalar,\ vector,\ matrix,\ or\ multidimensional\ array.$

Data Types: quaternion

Algorithms

Given a quaternion $A = a + \overline{v} = a + bi + cj + dk$, the logarithm is computed by

$$\log(A) = \log||A|| + \frac{\overline{v}}{\|\overline{v}\|} \arccos \frac{a}{\|A\|}$$

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

Functions

exp|power, .^

Objects

quaternion

Topics

"Rotations, Orientation, and Quaternions"

meanrot

Quaternion mean rotation

Syntax

```
quatAverage = meanrot(quat)
quatAverage = meanrot(quat,dim)
quatAverage = meanrot( ,nanflag)
```

Description

quatAverage = meanrot(quat) returns the average rotation of the elements of quat along the first array dimension whose size not does equal 1.

- If quat is a vector, meanrot(quat) returns the average rotation of the elements.
- If quat is a matrix, meanrot(quat) returns a row vector containing the average rotation of each column.
- If quat is a multidimensional array, then mearot(quat) operates along the first array dimension whose size does not equal 1, treating the elements as vectors. This dimension becomes 1 while the sizes of all other dimensions remain the same.

The meanrot function normalizes the input quaternions, quat, before calculating the mean.

quatAverage = meanrot(quat,dim) return the average rotation along dimension dim. For
example, if quat is a matrix, then meanrot(quat,2) is a column vector containing the mean of each
row

quatAverage = meanrot(____, nanflag) specifies whether to include or omit NaN values from the calculation for any of the previous syntaxes. meanrot(quat, 'includenan') includes all NaN values in the calculation while mean(quat, 'omitnan') ignores them.

Examples

Quaternion Mean Rotation

Create a matrix of quaternions corresponding to three sets of Euler angles.

Determine the average rotation represented by the quaternions. Convert the average rotation to Euler angles in degrees for readability.

```
quatAverage = meanrot(quat)
```

```
quatAverage = quaternion
     0.88863 - 0.062598i + 0.27822j + 0.35918k

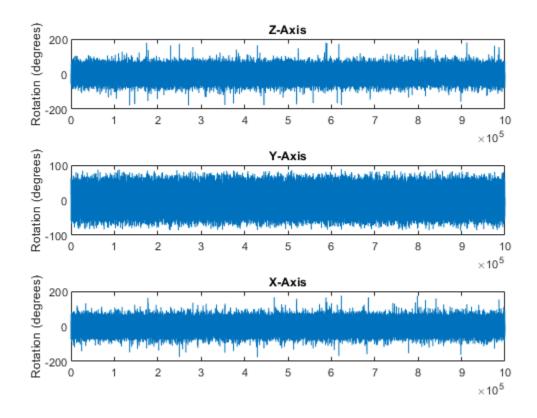
eulerAverage = eulerd(quatAverage,'ZYX','frame')
eulerAverage = 1×3
     45.7876     32.6452     6.0407
```

Average Out Rotational Noise

Use meanrot over a sequence of quaternions to average out additive noise.

Create a vector of 1e6 quaternions whose distance, as defined by the dist function, from quaternion(1,0,0,0) is normally distributed. Plot the Euler angles corresponding to the noisy quaternion vector.

```
nrows = 1e6;
ax = 2*rand(nrows,3) - 1;
ax = ax./sqrt(sum(ax.^2,2));
ang = 0.5*randn(size(ax,1),1);
q = quaternion(ax.*ang ,'rotvec');
noisyEulerAngles = eulerd(q,'ZYX','frame');
figure(1)
subplot(3,1,1)
plot(noisyEulerAngles(:,1))
title('Z-Axis')
ylabel('Rotation (degrees)')
hold on
subplot(3,1,2)
plot(noisyEulerAngles(:,2))
title('Y-Axis')
ylabel('Rotation (degrees)')
hold on
subplot(3,1,3)
plot(noisyEulerAngles(:,3))
title('X-Axis')
ylabel('Rotation (degrees)')
hold on
```



Use $\tt meanrot$ to determine the average quaternion given the vector of quaternions. Convert to Euler angles and plot the results.

```
qAverage = meanrot(q);

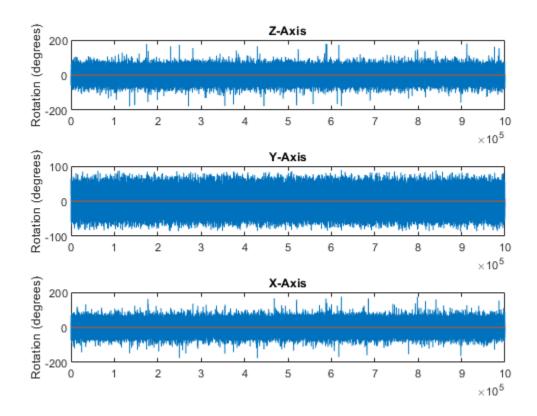
qAverageInEulerAngles = eulerd(qAverage,'ZYX','frame');

figure(1)

subplot(3,1,1)
plot(ones(nrows,1)*qAverageInEulerAngles(:,1))
title('Z-Axis')

subplot(3,1,2)
plot(ones(nrows,1)*qAverageInEulerAngles(:,2))
title('Y-Axis')

subplot(3,1,3)
plot(ones(nrows,1)*qAverageInEulerAngles(:,3))
title('X-Axis')
```



The meanrot Algorithm and Limitations

The meanrot Algorithm

The meanrot function outputs a quaternion that minimizes the squared Frobenius norm of the difference between rotation matrices. Consider two quaternions:

- q0 represents no rotation.
- **q90** represents a 90 degree rotation about the *x*-axis.

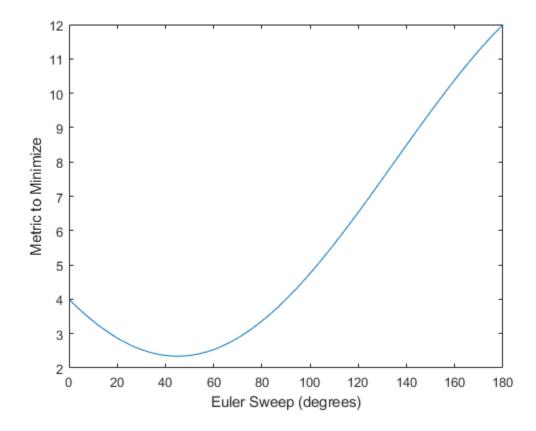
```
q0 = quaternion([0 0 0], 'eulerd', 'ZYX', 'frame');
q90 = quaternion([0 0 90], 'eulerd', 'ZYX', 'frame');
```

Create a quaternion sweep, qSweep, that represents rotations from 0 to 180 degrees about the *x*-axis.

```
eulerSweep = (0:1:180)';
qSweep = quaternion([zeros(numel(eulerSweep),2),eulerSweep], ...
    'eulerd','ZYX','frame');
```

Convert q0, q90, and qSweep to rotation matrices. In a loop, calculate the metric to minimize for each member of the quaternion sweep. Plot the results and return the value of the Euler sweep that corresponds to the minimum of the metric.

```
r0 = rotmat(q0,'frame');
r90 = rotmat(q90,'frame');
```



```
[~,eulerIndex] = min(metricToMinimize);
eulerSweep(eulerIndex)
```

```
ans = 45
```

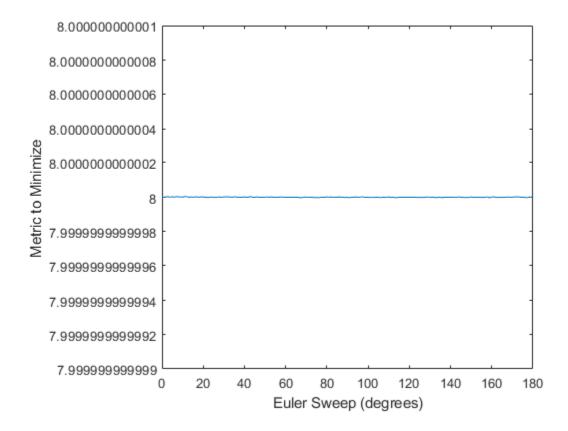
The minimum of the metric corresponds to the Euler angle sweep at 45 degrees. That is, meanrot defines the average between quaterion([0 0 0],'ZYX','frame') and quaternion([0 0 90],'ZYX','frame') as quaternion([0 0 45],'ZYX','frame'). Call meanrot with q0 and q90 to verify the same result.

```
eulerd(meanrot([q0,q90]),'ZYX','frame')
ans = 1×3
```

```
0 0 45.0000
```

Limitations

The metric that meanrot uses to determine the mean rotation is not unique for quaternions significantly far apart. Repeat the experiment above for quaternions that are separated by 180 degrees.



```
[~,eulerIndex] = min(metricToMinimize);
eulerSweep(eulerIndex)
ans = 159
```

Quaternion means are usually calculated for rotations that are close to each other, which makes the edge case shown in this example unlikely in real-world applications. To average two quaternions that are significantly far apart, use the slerp function. Repeat the experiment using slerp and verify that the quaternion mean returned is more intuitive for large distances.

Input Arguments

quat — Quaternion

scalar | vector | matrix | multidimensional array

Quaternion for which to calculate the mean, specified as a scalar, vector, matrix, or multidimensional array of quaternions.

Data Types: quaternion

dim — Dimension to operate along

positive integer scalar

Dimension to operate along, specified as a positive integer scalar. If no value is specified, then the default is the first array dimension whose size does not equal 1.

Dimension dim indicates the dimension whose length reduces to 1. The size(quatAverage,dim) is 1, while the sizes of all other dimensions remain the same.

Data Types: double | single

nanflag — NaN condition

```
'includenan' (default) | 'omitnan'
```

NaN condition, specified as one of these values:

- 'includenan' -- Include NaN values when computing the mean rotation, resulting in NaN.
- 'omitnan' -- Ignore all NaN values in the input.

Data Types: char | string

Output Arguments

quatAverage — Quaternion average rotation

```
scalar | vector | matrix | multidimensional array
```

Quaternion average rotation, returned as a scalar, vector, matrix, or multidimensional array.

```
Data Types: single | double
```

Algorithms

meanrot determines a quaternion mean, \bar{q} , according to [1]. \bar{q} is the quaternion that minimizes the squared Frobenius norm of the difference between rotation matrices:

$$\bar{q} = \arg \min_{q \in S^3} \sum_{i=1}^n ||A(q) - A(q_i)||_F^2$$

References

[1] Markley, F. Landis, Yang Chen, John Lucas Crassidis, and Yaakov Oshman. "Average Quaternions." Journal of Guidance, Control, and Dynamics. Vol. 30, Issue 4, 2007, pp. 1193-1197.

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

Functions

dist|slerp

Objects

quaternion

Topics

"Rotations, Orientation, and Quaternions"

minus, -

Quaternion subtraction

Syntax

```
C = A - B
```

Description

C = A - B subtracts quaternion B from quaternion A using quaternion subtraction. Either A or B may be a real number, in which case subtraction is performed with the real part of the quaternion argument.

Examples

Subtract a Quaternion from a Quaternion

Quaternion subtraction is defined as the subtraction of the corresponding parts of each quaternion. Create two quaternions and perform subtraction.

```
Q1 = quaternion([1,0,-2,7]);
Q2 = quaternion([1,2,3,4]);
Q1minusQ2 = Q1 - Q2
Q1minusQ2 = quaternion
    0 - 2i - 5j + 3k
```

Subtract a Real Number from a Quaternion

Addition and subtraction of real numbers is defined for quaternions as acting on the real part of the quaternion. Create a quaternion and then subtract 1 from the real part.

Input Arguments

A — Input

scalar | vector | matrix | multidimensional array

Input, specified as a quaternion, array of quaternions, real number, or array of real numbers.

Data Types: quaternion | single | double

B - Input

scalar | vector | matrix | multidimensional array

Input, specified as a quaternion, array of quaternions, real number, or array of real numbers.

Data Types: quaternion | single | double

Output Arguments

C - Result

scalar | vector | matrix | multidimensional array

Result of quaternion subtraction, returned as a scalar, vector, matrix, or multidimensional array of quaternions.

Data Types: quaternion

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

Functions

```
mtimes, * | times, .* | uminus, -
```

Objects

quaternion

Topics

"Rotations, Orientation, and Quaternions"

mtimes, *

Quaternion multiplication

Syntax

```
quatC = A*B
```

Description

quatC = A*B implements quaternion multiplication if either A or B is a quaternion. Either A or B must be a scalar.

You can use quaternion multiplication to compose rotation operators:

- To compose a sequence of frame rotations, multiply the quaternions in the order of the desired sequence of rotations. For example, to apply a p quaternion followed by a q quaternion, multiply in the order pq. The rotation operator becomes $(pq)^*v(pq)$, where v represents the object to rotate specified in quaternion form. * represents conjugation.
- To compose a sequence of point rotations, multiply the quaternions in the reverse order of the desired sequence of rotations. For example, to apply a p quaternion followed by a q quaternion, multiply in the reverse order, qp. The rotation operator becomes $(qp)v(qp)^*$.

Examples

Multiply Quaternion Scalar and Quaternion Vector

Create a 4-by-1 column vector, A, and a scalar, b. Multiply A times b.

```
A = quaternion(randn(4,4))
```

```
A=4×1 quaternion array

0.53767 + 0.31877i + 3.5784j + 0.7254k

1.8339 - 1.3077i + 2.7694j - 0.063055k

-2.2588 - 0.43359i - 1.3499j + 0.71474k

0.86217 + 0.34262i + 3.0349j - 0.20497k

b = quaternion

-0.12414 + 1.4897i + 1.409j + 1.4172k
```

C = A*b

```
C=4×1 quaternion array

-6.6117 + 4.8105i + 0.94224j - 4.2097k

-2.0925 + 6.9079i + 3.9995j - 3.3614k

1.8155 - 6.2313i - 1.336j - 1.89k

-4.6033 + 5.8317i + 0.047161j - 2.791k
```

Input Arguments

A - Input

scalar | vector | matrix | multidimensional array

Input to multiply, specified as a quaternion, array of quaternions, real scalar, or array of real scalars.

If B is nonscalar, then A must be scalar.

Data Types: quaternion | single | double

B — Input

scalar | vector | matrix | multidimensional array

Input to multiply, specified as a quaternion, array of quaternions, real scalar, or array of real scalars.

If A is nonscalar, then B must be scalar.

Data Types: quaternion | single | double

Output Arguments

quatC — Quaternion product

scalar | vector | matrix | multidimensional array

Quaternion product, returned as a quaternion or array of quaternions.

Data Types: quaternion

Algorithms

Quaternion Multiplication by a Real Scalar

Given a quaternion

$$q = a_{\mathsf{q}} + b_{\mathsf{q}}\mathbf{i} + c_{\mathsf{q}}\mathbf{j} + d_{\mathsf{q}}\mathbf{k},$$

the product of q and a real scalar β is

$$\beta q = \beta a_{q} + \beta b_{q}i + \beta c_{q}j + \beta d_{q}k$$

Quaternion Multiplication by a Quaternion Scalar

The definition of the basis elements for quaternions,

$$i^2 = j^2 = k^2 = ijk = -1$$
,

can be expanded to populate a table summarizing quaternion basis element multiplication:

	1	i	j	k
1	1	i	j	k
i	i	-1	k	- j

j	j	-k	-1	i
k	k	j	-i	-1

When reading the table, the rows are read first, for example: ij = k and ji = -k.

Given two quaternions, $q = a_q + b_q i + c_q j + d_q k$, and $p = a_p + b_p i + c_p j + d_p k$, the multiplication can be expanded as:

$$z = pq = (a_{p} + b_{p}i + c_{p}j + d_{p}k)(a_{q} + b_{q}i + c_{q}j + d_{q}k)$$

$$= a_{p}a_{q} + a_{p}b_{q}i + a_{p}c_{q}j + a_{p}d_{q}k$$

$$+ b_{p}a_{q}i + b_{p}b_{q}i^{2} + b_{p}c_{q}ij + b_{p}d_{q}ik$$

$$+ c_{p}a_{q}j + c_{p}b_{q}ji + c_{p}c_{q}j^{2} + c_{p}d_{q}jk$$

$$+ d_{p}a_{q}k + d_{p}b_{q}ki + d_{p}c_{q}kj + d_{p}d_{q}k^{2}$$

You can simplify the equation using the guaternion multiplication table:

$$\begin{split} z &= pq = a_{\rm p} a_{\rm q} + a_{\rm p} b_{\rm q} {\rm i} + a_{\rm p} c_{\rm q} {\rm j} + a_{\rm p} d_{\rm q} {\rm k} \\ &+ b_{\rm p} a_{\rm q} {\rm i} - b_{\rm p} b_{\rm q} + b_{\rm p} c_{\rm q} {\rm k} - b_{\rm p} d_{\rm q} {\rm j} \\ &+ c_{\rm p} a_{\rm q} {\rm j} - c_{\rm p} b_{\rm q} {\rm k} - c_{\rm p} c_{\rm q} + c_{\rm p} d_{\rm q} {\rm i} \\ &+ d_{\rm p} a_{\rm q} k + d_{\rm p} b_{\rm q} {\rm j} - d_{\rm p} c_{\rm q} {\rm i} - d_{\rm p} d_{\rm q} \end{split}$$

References

[1] Kuipers, Jack B. *Quaternions and Rotation Sequences: A Primer with Applications to Orbits, Aerospace, and Virtual Reality.* Princeton, NJ: Princeton University Press, 2007.

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

Functions

times, .*

Objects

quaternion

Topics

"Rotations, Orientation, and Quaternions"

norm

Quaternion norm

Syntax

```
N = norm(quat)
```

Description

N = norm(quat) returns the norm of the quaternion, quat.

Given a quaternion of the form $Q = a + b\mathbf{i} + c\mathbf{j} + d\mathbf{k}$, the norm of the quaternion is defined as $\operatorname{norm}(Q) = \sqrt{a^2 + b^2 + c^2 + d^2}$.

Examples

Calculate Quaternion Norm

Create a scalar quaternion and calculate its norm.

```
quat = quaternion(1,2,3,4);
norm(quat)
ans = 5.4772
```

The quaternion norm is defined as the square root of the sum of the quaternion parts squared. Calculate the quaternion norm explicitly to verify the result of the norm function.

```
[a,b,c,d] = parts(quat);
sqrt(a^2+b^2+c^2+d^2)
ans = 5.4772
```

Input Arguments

quat — Quaternion

```
scalar | vector | matrix | multidimensional array
```

Quaternion for which to calculate the norm, specified as a scalar, vector, matrix, or multidimensional array of quaternions.

Data Types: quaternion

Output Arguments

N — Quaternion norm

scalar | vector | matrix | multidimensional array

Quaternion norm. If the input quat is an array, the output is returned as an array the same size as quat. Elements of the array are real numbers with the same data type as the underlying data type of the quaternion, quat.

Data Types: single | double

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

Functions

conj | normalize | parts

Objects

quaternion

Topics

"Rotations, Orientation, and Quaternions"

normalize

Quaternion normalization

Syntax

```
quatNormalized = normalize(quat)
```

Description

```
quatNormalized = normalize(quat) normalizes the quaternion.
```

Given a quaternion of the form $Q = a + b\mathbf{i} + c\mathbf{j} + d\mathbf{k}$, the normalized quaternion is defined as $Q/\sqrt{a^2 + b^2 + c^2 + d^2}$.

Examples

Normalize Elements of Quaternion Vector

Quaternions can represent rotations when normalized. You can use normalize to normalize a scalar, elements of a matrix, or elements of a multi-dimensional array of quaternions. Create a column vector of quaternions, then normalize them.

Input Arguments

quat — Quaternion to normalize

```
scalar | vector | matrix | multidimensional array
```

Quaternion to normalize, specified as a scalar, vector, matrix, or multidimensional array of quaternions.

Data Types: quaternion

Output Arguments

```
quatNormalized — Normalized quaternion
```

scalar | vector | matrix | multidimensional array

Normalized quaternion, returned as a quaternion or array of quaternions the same size as quat.

Data Types: quaternion

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder $^{\text{\tiny TM}}$.

See Also

Functions

conj | norm | times, .*

Objects

quaternion

Topics

"Rotations, Orientation, and Quaternions"

ones

Create quaternion array with real parts set to one and imaginary parts set to zero

Syntax

```
quatOnes = ones('quaternion')
quatOnes = ones(n,'quaternion')
quatOnes = ones(sz,'quaternion')
quatOnes = ones(sz1,...,szN,'quaternion')
quatOnes = ones(____,'like',prototype,'quaternion')
```

Description

quatOnes = ones('quaternion') returns a scalar quaternion with the real part set to 1 and the imaginary parts set to 0.

```
Given a quaternion of the form Q = a + bi + cj + dk, a quaternion one is defined as Q = 1 + 0i + 0j + 0k.
```

quatOnes = ones(n, 'quaternion') returns an n-by-n quaternion matrix with the real parts set to 1 and the imaginary parts set to 0.

quatOnes = ones(sz,'quaternion') returns an array of quaternion ones where the size vector, sz, defines size(qOnes).

Example: ones([1,4,2],'quaternion') returns a 1-by-4-by-2 array of quaternions with the real parts set to 1 and the imaginary parts set to θ .

quatOnes = ones(sz1,...,szN,'quaternion') returns a sz1-by-...-by-szN array of ones where sz1,...,szN indicates the size of each dimension.

quatOnes = ones(____, 'like',prototype,'quaternion') specifies the underlying class of the returned quaternion array to be the same as the underlying class of the quaternion prototype.

Examples

Quaternion Scalar One

Create a quaternion scalar one.

```
quat0nes = ones('quaternion')
quat0nes = quaternion
    1 + 0i + 0j + 0k
```

Square Matrix of Quaternion Ones

Create an n-by-n matrix of quaternion ones.

```
\begin{array}{l} n = 3;\\ \text{quatOnes} = \text{ones(n,'quaternion')} \\ \\ \text{quatOnes} = 3 \times 3 \ \textit{quaternion array} \\ \\ 1 + 0i + 0j + 0k & 1 + 0i + 0j + 0k & 1 + 0i + 0j + 0k \\ \\ 1 + 0i + 0j + 0k & 1 + 0i + 0j + 0k & 1 + 0i + 0j + 0k \\ \\ 1 + 0i + 0j + 0k & 1 + 0i + 0j + 0k & 1 + 0i + 0j + 0k \end{array}
```

Multidimensional Array of Quaternion Ones

Create a multidimensional array of quaternion ones by defining array dimensions in order. In this example, you create a 3-by-1-by-2 array. You can specify dimensions using a row vector or commaseparated integers. Specify the dimensions using a row vector and display the results:

```
dims = [3,1,2];
quatOnesSyntax1 = ones(dims, 'quaternion')

quatOnesSyntax1 = 3x1x2 quaternion array
quatOnesSyntax1(:,:,1) =

    1 + 0i + 0j + 0k
    1 + 0i + 0j + 0k
    1 + 0i + 0j + 0k

quatOnesSyntax1(:,:,2) =

    1 + 0i + 0j + 0k
    1 + 0i + 0j + 0k
```

Specify the dimensions using comma-separated integers, and then verify the equivalency of the two syntaxes:

```
quatOnesSyntax2 = ones(3,1,2,'quaternion');
isequal(quatOnesSyntax1,quatOnesSyntax2)
ans = logical
1
```

Underlying Class of Quaternion Ones

A quaternion is a four-part hyper-complex number used in three-dimensional rotations and orientations. You can specify the underlying data type of the parts as single or double. The default is double.

Create a quaternion array of ones with the underlying data type set to single.

Verify the underlying class using the classUnderlying function.

classUnderlying(quatOnes)

```
ans =
'single'
```

Input Arguments

n — Size of square quaternion matrix

integer value

Size of square quaternion matrix, specified as an integer value.

If n is zero or negative, then quatOnes is returned as an empty matrix.

Example: ones (4, 'quaternion') returns a 4-by-4 matrix of quaternions with the real parts set to 1 and the imaginary parts set to 0.

Data Types: single | double | int8 | int16 | int32 | int64 | uint8 | uint16 | uint32 | uint64

sz — Output size

row vector of integer values

Output size, specified as a row vector of integer values. Each element of sz indicates the size of the corresponding dimension in quatOnes. If the size of any dimension is 0 or negative, then quatOnes is returned as an empty array.

Data Types: single | double | int8 | int16 | int32 | int64 | uint8 | uint16 | uint32 | uint64

prototype — Quaternion prototype

variable

Quaternion prototype, specified as a variable.

Example: ones(2, 'like', quat, 'quaternion') returns a 2-by-2 matrix of quaternions with the same underlying class as the prototype quaternion, quat.

Data Types: quaternion

sz1,...,szN — Size of each dimension

two or more integer values

Size of each dimension, specified as two or more integers. If the size of any dimension is 0 or negative, then quatOnes is returned as an empty array.

Example: ones(2,3,'quaternion') returns a 2-by-3 matrix of quaternions with the real parts set to 1 and the imaginary parts set to 0.

Data Types: single | double | int8 | int16 | int32 | int64 | uint8 | uint16 | uint32 | uint64

Output Arguments

quat0nes — Quaternion ones

scalar | vector | matrix | multidimensional array

Quaternion ones, returned as a scalar, vector, matrix, or multidimensional array of quaternions.

Given a quaternion of the form Q = a + bi + cj + dk, a quaternion one is defined as Q = 1 + 0i + 0j + 0k.

Data Types: quaternion

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

Functions

zeros

Objects

quaternion

Topics

"Rotations, Orientation, and Quaternions"

parts

Extract quaternion parts

Syntax

```
[a,b,c,d] = parts(quat)
```

Description

[a,b,c,d] = parts(quat) returns the parts of the quaternion array as arrays, each the same size as quat.

Examples

Convert Quaternion to Matrix of Quaternion Parts

Convert a quaternion representation to parts using the parts function.

Create a two-element column vector of quaternions by specifying the parts.

```
quat = quaternion([1:4;5:8])
quat=2×1 quaternion array
    1 + 2i + 3j + 4k
    5 + 6i + 7j + 8k
```

Recover the parts from the quaternion matrix using the parts function. The parts are returned as separate output arguments, each the same size as the input 2-by-1 column vector of quaternions.

4

8

Input Arguments

quat — Quaternion

scalar | vector | matrix | multidimensional array

Quaternion, specified as a quaternion or array of quaternions.

Data Types: quaternion

Output Arguments

[a,b,c,d] — Quaternion parts

scalar | vector | matrix | multidimensional array

Quaternion parts, returned as four arrays: a, b, d, and d. Each part is the same size as quat.

Data Types: single | double

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder $^{\text{\tiny TM}}$.

See Also

Functions

classUnderlying | compact

Objects

quaternion

Topics

"Rotations, Orientation, and Quaternions"

power, .^

Element-wise quaternion power

Syntax

$$C = A.^b$$

Description

 $C = A.^b$ raises each element of A to the corresponding power in b.

Examples

Raise a Quaternion to a Real Scalar Power

Create a quaternion and raise it to a real scalar power.

```
A = quaternion(1,2,3,4)
A = quaternion
    1 + 2i + 3j + 4k

b = 3;
C = A.^b

C = quaternion
    -86 - 52i - 78j - 104k
```

Raise a Quaternion Array to Powers from a Multidimensional Array

Create a 2-by-1 quaternion array and raise it to powers from a 2-D array.

 $C = A.^b$

Input Arguments

A — Base

scalar | vector | matrix | multidimensional array

Base, specified as a scalar, vector, matrix, or multidimensional array.

Data Types: quaternion | single | double

b — Exponent

scalar | vector | matrix | multidimensional array

Exponent, specified as a real scalar, vector, matrix, or multidimensional array.

Data Types: single | double

Output Arguments

C — Result

scalar | vector | matrix | multidimensional array

Each element of quaternion A raised to the corresponding power in b, returned as a scalar, vector, matrix, or multidimensional array.

Data Types: quaternion

Algorithms

The polar representation of a quaternion A = a + bi + cj + dk is given by

$$A = ||A||(\cos\theta + \widehat{u}\sin\theta)$$

where θ is the angle of rotation, and \hat{u} is the unit quaternion.

Quaternion A raised by a real exponent b is given by

$$P = A \cdot \hat{b} = ||A||^b (\cos(b\theta) + \widehat{u}\sin(b\theta))$$

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

Functions

exp | log

Objects quaternion

Topics

"Rotations, Orientation, and Quaternions"

prod

Product of a quaternion array

Syntax

```
quatProd = prod(quat)
quatProd = prod(quat,dim)
```

Description

```
quatProd = prod(quat) returns the quaternion product of the elements of the array.
quatProd = prod(quat,dim) calculates the quaternion product along dimension dim.
```

Examples

Product of Quaternions in Each Column

Create a 3-by-3 array whose elements correspond to their linear indices.

```
A = reshape(quaternion(randn(9,4)),3,3)
```

Find the product of the quaternions in each column. The length of the first dimension is 1, and the length of the second dimension matches size(A,2).

```
B = prod(A)
```

```
B=1×3 quaternion array
-19.837 - 9.1521i + 15.813j - 19.918k -5.4708 - 0.28535i + 3.077j - 1.2295k
```

Product of Specified Dimension of Quaternion Array

You can specify which dimension of a quaternion array to take the product of.

```
Create a 2-by-2-by-2 quaternion array.
```

```
A = reshape(quaternion(randn(8,4)),2,2,2);
```

Find the product of the elements in each page of the array. The length of the first dimension matches size(A,1), the length of the second dimension matches size(A,2), and the length of the third dimension is 1.

Input Arguments

quat — Quaternion

scalar | vector | matrix | multidimensional array

Quaternion, specified as scalar, vector, matrix, or multidimensional array of quaternions.

Example: qProd = prod(quat) calculates the quaternion product along the first non-singleton dimension of quat.

Data Types: quaternion

dim — Dimension

first non-singleton dimension (default) | positive integer

Dimension along which to calculate the quaternion product, specified as a positive integer. If dim is not specified, prod operates along the first non-singleton dimension of quat.

Data Types: single | double | int8 | int16 | int32 | int64 | uint8 | uint16 | uint32 | uint64

Output Arguments

quatProd — Quaternion product

positive integer

Quaternion product, returned as quaternion array with one less non-singleton dimension than quat.

For example, if quat is a 2-by-2-by-5 array,

- prod(quat,1) returns a 1-by-2-by-5 array.
- prod(quat,2) returns a 2-by-1-by-5 array.
- prod(quat,3) returns a 2-by-2 array.

Data Types: quaternion

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

Functions

```
mtimes, *|times, .*
```

Objects quaternion

Topics

"Rotations, Orientation, and Quaternions"

rdivide, ./

Element-wise quaternion right division

Syntax

C = A./B

Description

C = A./B performs quaternion element-wise division by dividing each element of quaternion A by the corresponding element of quaternion B.

Examples

Divide a Quaternion Array by a Real Scalar

Create a 2-by-1 quaternion array, and divide it element-by-element by a real scalar.

```
A = quaternion([1:4;5:8])
A=2×1 quaternion array
    1 + 2i + 3j + 4k
    5 + 6i + 7j + 8k

B = 2;
C = A./B

C=2×1 quaternion array
    0.5 + 1i + 1.5j + 2k
    2.5 + 3i + 3.5j + 4k
```

Divide a Quaternion Array by Another Quaternion Array

Create a 2-by-2 quaternion array, and divide it element-by-element by another 2-by-2 quaternion array.

C = A./B

```
C=2×2 quaternion array
2.7 - 0.1i - 2.1j - 1.7k 2.2778 + 0.092593i - 0.46296j - 0.5740
1.8256 - 0.081395i + 0.45349j - 0.24419k 1.4524 - 0.5i + 1.0238j - 0.2619
```

Input Arguments

A — Dividend

scalar | vector | matrix | multidimensional array

Dividend, specified as a quaternion, an array of quaternions, a real scalar, or an array of real numbers.

A and B must have compatible sizes. In the simplest cases, they can be the same size or one can be a scalar. Two inputs have compatible sizes if, for every dimension, the dimension sizes of the inputs are the same or one of the dimensions is 1.

Data Types: quaternion | single | double

B — Divisor

scalar | vector | matrix | multidimensional array

Divisor, specified as a quaternion, an array of quaternions, a real scalar, or an array of real numbers.

A and B must have compatible sizes. In the simplest cases, they can be the same size or one can be a scalar. Two inputs have compatible sizes if, for every dimension, the dimension sizes of the inputs are the same or one of the dimensions is 1.

Data Types: quaternion | single | double

Output Arguments

C — Result

scalar | vector | matrix | multidimensional array

Result of quaternion division, returned as a scalar, vector, matrix, or multidimensional array.

Data Types: quaternion

Algorithms

Quaternion Division

Given a quaternion $A = a_1 + a_2i + a_3j + a_4k$ and a real scalar p,

$$C = A \cdot /p = \frac{a_1}{p} + \frac{a_2}{p}i + \frac{a_3}{p}j + \frac{a_4}{p}k$$

Note For a real scalar p, $A./p = A. \ p$.

Quaternion Division by a Quaternion Scalar

Given two quaternions A and B of compatible sizes,

$$C = A \cdot /B = A \cdot *B^{-1} = A \cdot *\left(\frac{conj(B)}{norm(B)^{2}}\right)$$

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

Functions

conj|ldivide, .\|norm|times, .*

Objects

quaternion

Topics

"Rotations, Orientation, and Quaternions"

randrot

Uniformly distributed random rotations

Syntax

```
R = randrot
R = randrot(m)
R = randrot(m1,...,mN)
R = randrot([m1,...,mN])
```

Description

R = randrot returns a unit quaternion drawn from a uniform distribution of random rotations.

R = randrot(m) returns an m-by-m matrix of unit quaternions drawn from a uniform distribution of random rotations.

R = randrot(m1, ..., mN) returns an m1-by-...-by-mN array of random unit quaternions, where m1, ..., mN indicate the size of each dimension. For example, randrot(3,4) returns a 3-by-4 matrix of random unit quaternions.

R = randrot([m1,...,mN]) returns an m1-by-...-by-mN array of random unit quaternions, where m1,...,mN indicate the size of each dimension. For example, randrot([3,4]) returns a 3-by-4 matrix of random unit quaternions.

Examples

Matrix of Random Rotations

Generate a 3-by-3 matrix of uniformly distributed random rotations.

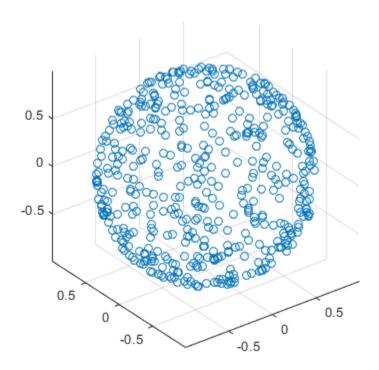
```
r = randrot(3)
```

Create Uniform Distribution of Random Rotations

Create a vector of 500 random quaternions. Use rotatepoint on page 2-1003 to visualize the distribution of the random rotations applied to point (1, 0, 0).

```
q = randrot(500,1);
pt = rotatepoint(q, [1 0 0]);
```

```
figure
scatter3(pt(:,1), pt(:,2), pt(:,3))
axis equal
```



Input Arguments

m — Size of square matrix

integer

Size of square quaternion matrix, specified as an integer value. If m is θ or negative, then R is returned as an empty matrix.

Data Types: single | double | int8 | int16 | int32 | int64 | uint8 | uint16 | uint32 | uint64

$m1, \ldots, mN$ — Size of each dimension

two or more integer values

Size of each dimension, specified as two or more integer values. If the size of any dimension is θ or negative, then R is returned as an empty array.

Example: randrot(2,3) returns a 2-by-3 matrix of random quaternions.

Data Types: single | double | int8 | int16 | int32 | int64 | uint8 | uint16 | uint32 | uint64

[m1,...,mN] — Vector of size of each dimension

row vector of integer values

Vector of size of each dimension, specified as a row vector of two or more integer values. If the size of any dimension is θ or negative, then R is returned as an empty array.

Example: randrot([2,3]) returns a 2-by-3 matrix of random quaternions.

Data Types: single | double | int8 | int16 | int32 | int64 | uint8 | uint16 | uint32 | uint64

Output Arguments

R — Random quaternions

scalar | vector | matrix | multidimensional array

Random quaternions, returned as a quaternion or array of quaternions.

Data Types: quaternion

References

[1] Shoemake, K. "Uniform Random Rotations." *Graphics Gems III* (K. David, ed.). New York: Academic Press, 1992.

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

quaternion

Topics

"Rotations, Orientation, and Quaternions"

rotateframe

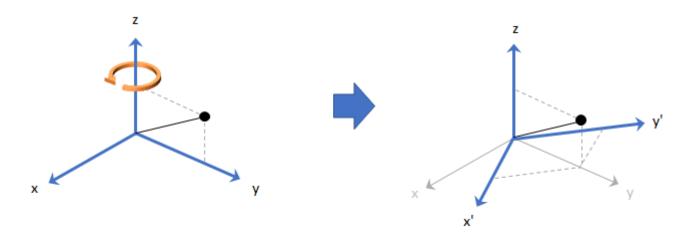
Quaternion frame rotation

Syntax

rotationResult = rotateframe(quat,cartesianPoints)

Description

rotationResult = rotateframe(quat, cartesianPoints) rotates the frame of reference for the Cartesian points using the quaternion, quat. The elements of the quaternion are normalized before use in the rotation.

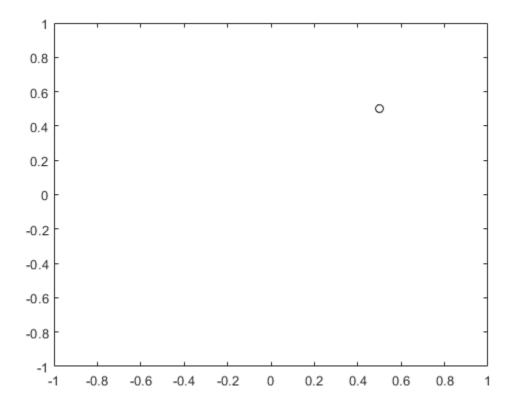


Examples

Rotate Frame Using Quaternion Vector

Define a point in three dimensions. The coordinates of a point are always specified in the order x, y, and z. For convenient visualization, define the point on the x-y plane.

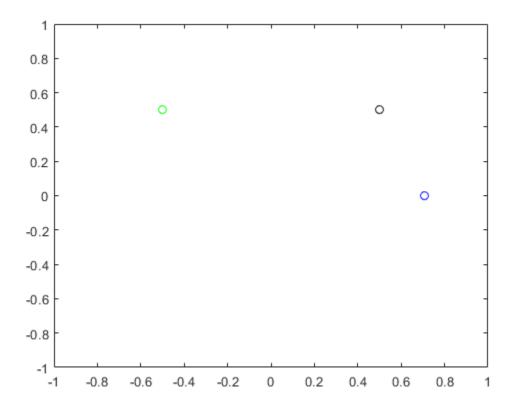
```
x = 0.5;
y = 0.5;
z = 0;
plot(x,y,'ko')
hold on
axis([-1 1 -1 1])
```



Create a quaternion vector specifying two separate rotations, one to rotate the frame 45 degrees and another to rotate the point -90 degrees about the z-axis. Use rotateframe to perform the rotations.

Plot the rereferenced points.

```
plot(rereferencedPoint(1,1), rereferencedPoint(1,2), 'bo')
plot(rereferencedPoint(2,1), rereferencedPoint(2,2), 'go')
```



Rereference Group of Points using Quaternion

Define two points in three-dimensional space. Define a quaternion to rereference the points by first rotating the reference frame about the z-axis 30 degrees and then about the new y-axis 45 degrees.

```
a = [1,0,0];
b = [0,1,0];
quat = quaternion([30,45,0],'eulerd','ZYX','point');
```

Use rotateframe to reference both points using the quaternion rotation operator. Display the result.

```
rP = rotateframe(quat,[a;b])

rP = 2\times3

0.6124 -0.3536 0.7071

0.5000 0.8660 -0.0000
```

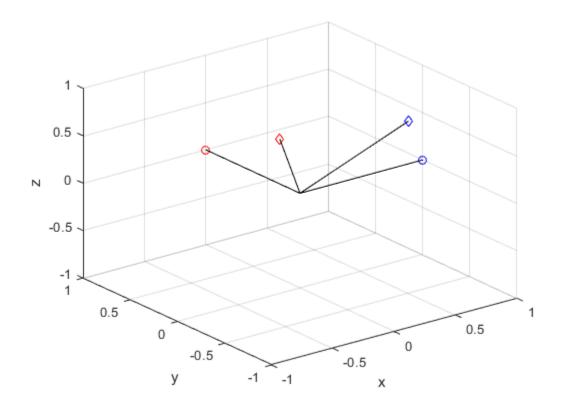
Visualize the original orientation and the rotated orientation of the points. Draw lines from the origin to each of the points for visualization purposes.

```
plot3(a(1),a(2),a(3),'bo');
hold on
```

```
grid on
axis([-1 1 -1 1 -1 1])
xlabel('x')
ylabel('y')
zlabel('z')

plot3(b(1),b(2),b(3),'ro');
plot3(rP(1,1),rP(1,2),rP(1,3),'bd')
plot3(rP(2,1),rP(2,2),rP(2,3),'rd')

plot3([0;rP(1,1)],[0;rP(1,2)],[0;rP(1,3)],'k')
plot3([0;rP(2,1)],[0;rP(2,2)],[0;rP(2,3)],'k')
plot3([0;a(1)],[0;a(2)],[0;a(3)],'k')
plot3([0;b(1)],[0;b(2)],[0;b(3)],'k')
```



Input Arguments

quat — Quaternion that defines rotation

scalar | vector

Quaternion that defines rotation, specified as a scalar quaternion or vector of quaternions.

Data Types: quaternion

cartesianPoints — Three-dimensional Cartesian points

1-by-3 vector | N-by-3 matrix

Three-dimensional Cartesian points, specified as a 1-by-3 vector or *N*-by-3 matrix.

Data Types: single | double

Output Arguments

rotationResult — Re-referenced Cartesian points

vector | matrix

Cartesian points defined in reference to rotated reference frame, returned as a vector or matrix the same size as cartesianPoints.

The data type of the re-referenced Cartesian points is the same as the underlying data type of quat.

Data Types: single | double

Algorithms

Quaternion frame rotation re-references a point specified in \mathbf{R}^3 by rotating the original frame of reference according to a specified quaternion:

$$L_q(u) = q * uq$$

where q is the quaternion, * represents conjugation, and u is the point to rotate, specified as a quaternion.

For convenience, the rotateframe function takes a point in \mathbb{R}^3 and returns a point in \mathbb{R}^3 . Given a function call with some arbitrary quaternion, q = a + bi + cj + dk, and arbitrary coordinate, [x,y,z],

the rotateframe function performs the following operations:

1 Converts point [x,y,z] to a quaternion:

$$u_a = 0 + xi + yj + zk$$

2 Normalizes the quaternion, q:

$$q_n = \frac{q}{\sqrt{a^2 + b^2 + c^2 + d^2}}$$

3 Applies the rotation:

$$v_a = q * u_a q$$

4 Converts the quaternion output, v_a , back to \mathbf{R}^3

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

Functions

rotatepoint

Objects

quaternion

Topics "Rotations, Orientation, and Quaternions"

rotatepoint

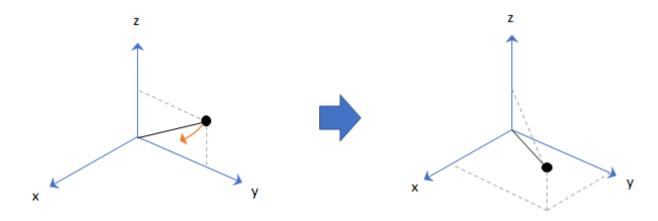
Quaternion point rotation

Syntax

rotationResult = rotatepoint(quat,cartesianPoints)

Description

rotationResult = rotatepoint(quat, cartesianPoints) rotates the Cartesian points using
the quaternion, quat. The elements of the quaternion are normalized before use in the rotation.

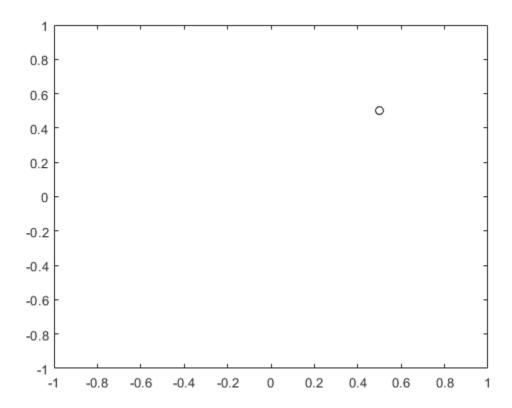


Examples

Rotate Point Using Quaternion Vector

Define a point in three dimensions. The coordinates of a point are always specified in order x, y, z. For convenient visualization, define the point on the x-y plane.

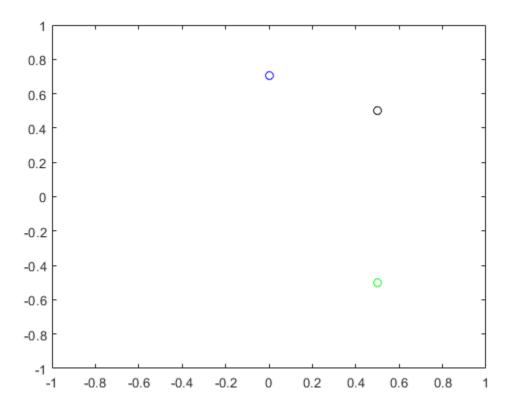
```
x = 0.5;
y = 0.5;
z = 0;
plot(x,y,'ko')
hold on
axis([-1 1 -1 1])
```



Create a quaternion vector specifying two separate rotations, one to rotate the point 45 and another to rotate the point -90 degrees about the z-axis. Use rotatepoint to perform the rotation.

Plot the rotated points.

```
plot(rotatedPoint(1,1),rotatedPoint(1,2),'bo')
plot(rotatedPoint(2,1),rotatedPoint(2,2),'go')
```



Rotate Group of Points Using Quaternion

Define two points in three-dimensional space. Define a quaternion to rotate the point by first rotating about the z-axis 30 degrees and then about the new y-axis 45 degrees.

```
a = [1,0,0];
b = [0,1,0];
quat = quaternion([30,45,0],'eulerd','ZYX','point');
```

Use rotatepoint to rotate both points using the quaternion rotation operator. Display the result.

```
rP = rotatepoint(quat,[a;b])
rP = 2×3
0.6124 0.5000 -0.6124
-0.3536 0.8660 0.3536
```

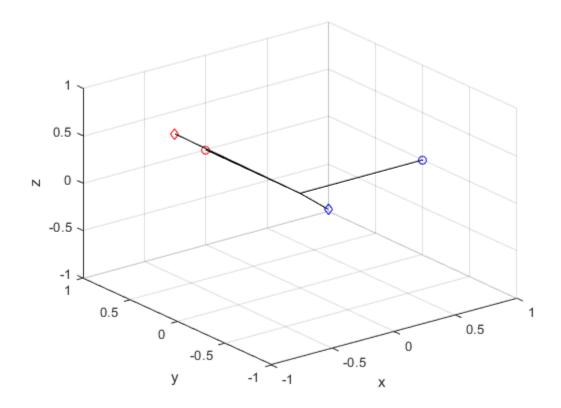
Visualize the original orientation and the rotated orientation of the points. Draw lines from the origin to each of the points for visualization purposes.

```
plot3(a(1),a(2),a(3),'bo');
hold on
```

```
grid on
axis([-1 1 -1 1 -1 1])
xlabel('x')
ylabel('y')
zlabel('z')

plot3(b(1),b(2),b(3),'ro');
plot3(rP(1,1),rP(1,2),rP(1,3),'bd')
plot3(rP(2,1),rP(2,2),rP(2,3),'rd')

plot3([0;rP(1,1)],[0;rP(1,2)],[0;rP(1,3)],'k')
plot3([0;rP(2,1)],[0;rP(2,2)],[0;rP(2,3)],'k')
plot3([0;a(1)],[0;a(2)],[0;a(3)],'k')
plot3([0;b(1)],[0;b(2)],[0;b(3)],'k')
```



Input Arguments

quat — Quaternion that defines rotation

scalar | vector

Quaternion that defines rotation, specified as a scalar quaternion, row vector of quaternions, or column vector of quaternions.

Data Types: quaternion

cartesianPoints — Three-dimensional Cartesian points

1-by-3 vector | N-by-3 matrix

Three-dimensional Cartesian points, specified as a 1-by-3 vector or *N*-by-3 matrix.

Data Types: single | double

Output Arguments

rotationResult — Repositioned Cartesian points

vector | matrix

Rotated Cartesian points defined using the quaternion rotation, returned as a vector or matrix the same size as cartesianPoints.

Data Types: single | double

Algorithms

Quaternion point rotation rotates a point specified in \mathbb{R}^3 according to a specified quaternion:

$$L_q(u) = quq^*$$

where q is the quaternion, * represents conjugation, and u is the point to rotate, specified as a quaternion.

For convenience, the rotatepoint function takes in a point in \mathbf{R}^3 and returns a point in \mathbf{R}^3 . Given a function call with some arbitrary quaternion, $q = a + b\mathbf{i} + c\mathbf{j} + d\mathbf{k}$, and arbitrary coordinate, [x,y,z], for example,

rereferencedPoint = rotatepoint(q,[x,y,z])

the rotatepoint function performs the following operations:

1 Converts point [x,y,z] to a quaternion:

$$u_a = 0 + xi + yj + zk$$

2 Normalizes the quaternion, *q*:

$$q_n = \frac{q}{\sqrt{a^2 + b^2 + c^2 + d^2}}$$

3 Applies the rotation:

$$v_a = qu_a q^*$$

4 Converts the quaternion output, v_a , back to \mathbf{R}^3

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

Functions

rotateframe

Objects

quaternion

Topics "Rotations, Orientation, and Quaternions"

rotmat

Convert quaternion to rotation matrix

Syntax

```
rotationMatrix = rotmat(quat,rotationType)
```

Description

rotationMatrix = rotmat(quat, rotationType) converts the quaternion, quat, to an
equivalent rotation matrix representation.

Examples

Convert Quaternion to Rotation Matrix for Point Rotation

Define a quaternion for use in point rotation.

Convert the quaternion to a rotation matrix.

rotationMatrixVerification = rx*ry

To verify the rotation matrix, directly create two rotation matrices corresponding to the rotations about the y- and x-axes. Multiply the rotation matrices and compare to the output of rotmat.

```
rotationMatrixVerification = 3\times3

0.7071 0 0.7071

0.3536 0.8660 -0.3536

-0.6124 0.5000 0.6124
```

Convert Quaternion to Rotation Matrix for Frame Rotation

Define a quaternion for use in frame rotation.

Convert the quaternion to a rotation matrix.

```
rotationMatrix = rotmat(quat,'frame')
rotationMatrix = 3×3

0.7071  -0.0000  -0.7071
0.3536   0.8660   0.3536
0.6124  -0.5000   0.6124
```

To verify the rotation matrix, directly create two rotation matrices corresponding to the rotations about the *y*- and *x*-axes. Multiply the rotation matrices and compare to the output of rotmat.

```
theta = 45;
gamma = 30;
ry = [cosd(theta)
                   0
                               -sind(theta) ; ...
                   1
                               0 ; ...
     0
    sind(theta)
                              cosd(theta)];
rx = [1]
                                                  . . .
     0
                   cosd(gamma) sind(gamma) ;
                                                 . . .
                   -sind(gamma) cosd(gamma)];
rotationMatrixVerification = rx*ry
rotationMatrixVerification = 3 \times 3
   0.7071
                  0
                     -0.7071
   0.3536 0.8660 0.3536
   0.6124 -0.5000 0.6124
```

Convert Quaternion Vector to Rotation Matrices

Create a 3-by-1 normalized quaternion vector.

```
gVec = normalize(quaternion(randn(3,4)));
```

Convert the quaternion array to rotation matrices. The pages of rotmatArray correspond to the linear index of qVec.

```
rotmatArray = rotmat(qVec, 'frame');
```

Assume qVec and rotmatArray correspond to a sequence of rotations. Combine the quaternion rotations into a single representation, then apply the quaternion rotation to arbitrarily initialized Cartesian points.

```
loc = normalize(randn(1,3));
quat = prod(qVec);
rotateframe(quat,loc)
ans = 1×3
0.9524 0.5297 0.9013
```

Combine the rotation matrices into a single representation, then apply the rotation matrix to the same initial Cartesian points. Verify the quaternion rotation and rotation matrix result in the same orientation.

```
totalRotMat = eye(3);
for i = 1:size(rotmatArray,3)
    totalRotMat = rotmatArray(:,:,i)*totalRotMat;
end
totalRotMat*loc'
ans = 3×1
    0.9524
    0.5297
    0.9013
```

Input Arguments

quat — Quaternion to convert

```
scalar | vector | matrix | multidimensional array
```

Quaternion to convert, specified as a scalar, vector, matrix, or multidimensional array.

Data Types: quaternion

```
{\bf rotation Type} - {\bf Type} \ {\bf or} \ {\bf rotation}
```

```
'frame'|'point'
```

Type of rotation represented by the rotationMatrix output, specified as 'frame' or 'point'.

```
Data Types: char | string
```

Output Arguments

rotationMatrix — Rotation matrix representation

3-by-3 matrix | 3-by-3-by-*N* multidimensional array

Rotation matrix representation, returned as a 3-by-3 matrix or 3-by-3-by-N multidimensional array.

- If quat is a scalar, rotationMatrix is returned as a 3-by-3 matrix.
- If quat is non-scalar, rotationMatrix is returned as a 3-by-3-by-N multidimensional array, where rotationMatrix(:,:,i) is the rotation matrix corresponding to quat(i).

The data type of the rotation matrix is the same as the underlying data type of quat.

Data Types: single | double

Algorithms

Given a quaternion of the form

$$q = a + bi + cj + dk$$
,

the equivalent rotation matrix for frame rotation is defined as

$$\begin{bmatrix} 2a^2 - 1 + 2b^2 & 2bc + 2ad & 2bd - 2ac \\ 2bc - 2ad & 2a^2 - 1 + 2c^2 & 2cd + 2ab \\ 2bd + 2ac & 2cd - 2ab & 2a^2 - 1 + 2d^2 \end{bmatrix}.$$

The equivalent rotation matrix for point rotation is the transpose of the frame rotation matrix:

$$\begin{bmatrix} 2a^2 - 1 + 2b^2 & 2bc - 2ad & 2bd + 2ac \\ 2bc + 2ad & 2a^2 - 1 + 2c^2 & 2cd - 2ab \\ 2bd - 2ac & 2cd + 2ab & 2a^2 - 1 + 2d^2 \end{bmatrix}.$$

References

[1] Kuipers, Jack B. *Quaternions and Rotation Sequences: A Primer with Applications to Orbits, Aerospace, and Virtual Reality.* Princeton, NJ: Princeton University Press, 2007.

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

Functions

euler | eulerd | rotvec | rotvecd

Objects

quaternion

Topics

"Rotations, Orientation, and Quaternions"

rotvec

Convert quaternion to rotation vector (radians)

Syntax

```
rotationVector = rotvec(quat)
```

Description

rotationVector = rotvec(quat) converts the quaternion array, quat, to an N-by-3 matrix of equivalent rotation vectors in radians. The elements of quat are normalized before conversion.

Examples

Convert Quaternion to Rotation Vector in Radians

Convert a random quaternion scalar to a rotation vector in radians

```
quat = quaternion(randn(1,4));
rotvec(quat)
ans = 1\times3
1.6866 -2.0774 0.7929
```

Input Arguments

quat — Quaternion to convert

```
scalar | vector | matrix | multidimensional array
```

Quaternion to convert, specified as scalar quaternion, vector, matrix, or multidimensional array of quaternions.

Data Types: quaternion

Output Arguments

rotationVector — Rotation vector (radians)

```
N-by-3 matrix
```

Rotation vector representation, returned as an N-by-3 matrix of rotations vectors, where each row represents the [X Y Z] angles of the rotation vectors in radians. The ith row of rotationVector corresponds to the element quat(i).

The data type of the rotation vector is the same as the underlying data type of quat.

```
Data Types: single | double
```

Algorithms

All rotations in 3-D can be represented by a three-element axis of rotation and a rotation angle, for a total of four elements. If the rotation axis is constrained to be unit length, the rotation angle can be distributed over the vector elements to reduce the representation to three elements.

Recall that a quaternion can be represented in axis-angle form

$$q = \cos(\theta/2) + \sin(\theta/2)(xi + yj + zk),$$

where θ is the angle of rotation and [x,y,z] represent the axis of rotation.

Given a quaternion of the form

$$q = a + bi + cj + dk,$$

you can solve for the rotation angle using the axis-angle form of quaternions:

$$\theta = 2\cos^{-1}(a)$$
.

Assuming a normalized axis, you can rewrite the quaternion as a rotation vector without loss of information by distributing θ over the parts b, c, and d. The rotation vector representation of q is

$$q_{\rm rv} = \frac{\theta}{\sin(\theta/2)} [b, c, d].$$

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder $^{\text{\tiny TM}}$.

See Also

Functions

euler | eulerd | rotvecd

Objects

quaternion

Topics

"Rotations, Orientation, and Quaternions"

rotvecd

Convert quaternion to rotation vector (degrees)

Syntax

```
rotationVector = rotvecd(quat)
```

Description

rotationVector = rotvecd(quat) converts the quaternion array, quat, to an N-by-3 matrix of equivalent rotation vectors in degrees. The elements of quat are normalized before conversion.

Examples

Convert Quaternion to Rotation Vector in Degrees

Convert a random quaternion scalar to a rotation vector in degrees.

```
quat = quaternion(randn(1,4));
rotvecd(quat)
ans = 1\times3
96.6345 -119.0274 45.4312
```

Input Arguments

quat — Quaternion to convert

```
scalar | vector | matrix | multidimensional array
```

Quaternion to convert, specified as scalar, vector, matrix, or multidimensional array of quaternions.

Data Types: quaternion

Output Arguments

rotationVector — Rotation vector (degrees)

N-by-3 matrix

Rotation vector representation, returned as an N-by-3 matrix of rotation vectors, where each row represents the $[x\ y\ z]$ angles of the rotation vectors in degrees. The ith row of rotationVector corresponds to the element quat(i).

The data type of the rotation vector is the same as the underlying data type of quat.

```
Data Types: single | double
```

Algorithms

All rotations in 3-D can be represented by four elements: a three-element axis of rotation and a rotation angle. If the rotation axis is constrained to be unit length, the rotation angle can be distributed over the vector elements to reduce the representation to three elements.

Recall that a quaternion can be represented in axis-angle form

$$q = \cos(\theta/2) + \sin(\theta/2)(xi + yj + zk),$$

where θ is the angle of rotation in degrees, and [x,y,z] represent the axis of rotation.

Given a quaternion of the form

$$q = a + bi + cj + dk,$$

you can solve for the rotation angle using the axis-angle form of quaternions:

$$\theta = 2\cos^{-1}(a)$$
.

Assuming a normalized axis, you can rewrite the quaternion as a rotation vector without loss of information by distributing θ over the parts b, c, and d. The rotation vector representation of q is

$$q_{\rm rv} = \frac{\theta}{\sin(\theta/2)} [b, c, d].$$

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder $^{\text{\tiny TM}}$.

See Also

Functions

euler | eulerd | rotvec

Objects

quaternion

Topics

"Rotations, Orientation, and Quaternions"

slerp

Spherical linear interpolation

Syntax

```
q0 = slerp(q1,q2,T)
```

Description

q0 = slerp(q1,q2,T) spherically interpolates between q1 and q2 by the interpolation coefficient T.

Examples

Interpolate Between Two Quaternions

Create two quaternions with the following interpretation:

```
1  a = 45 degree rotation around the z-axis
2  c = -45 degree rotation around the z-axis
a = quaternion([45,0,0],'eulerd','ZYX','frame');
c = quaternion([-45,0,0],'eulerd','ZYX','frame');
```

Call slerp with the quaternions a and c and specify an interpolation coefficient of 0.5.

```
interpolationCoefficient = 0.5;
b = slerp(a,c,interpolationCoefficient);
```

The output of slerp, b, represents an average rotation of a and c. To verify, convert b to Euler angles in degrees.

```
averageRotation = eulerd(b,'ZYX','frame') averageRotation = 1 \times 3
0 0 0
```

The interpolation coefficient is specified as a normalized value between θ and 1, inclusive. An interpolation coefficient of θ corresponds to the a quaternion, and an interpolation coefficient of 1 corresponds to the c quaternion. Call slerp with coefficients θ and 1 to confirm.

```
b = slerp(a,c,[0,1]);
eulerd(b,'ZYX','frame')
ans = 2×3
45,0000 0 0
```

```
-45.0000 0 0
```

You can create smooth paths between quaternions by specifying arrays of equally spaced interpolation coefficients.

```
path = 0:0.1:1;
interpolatedQuaternions = slerp(a,c,path);
```

For quaternions that represent rotation only about a single axis, specifying interpolation coefficients as equally spaced results in quaternions equally spaced in Euler angles. Convert interpolatedQuaternions to Euler angles and verify that the difference between the angles in the path is constant.

```
k = eulerd(interpolatedQuaternions, 'ZYX', 'frame');
abc = abs(diff(k))
abc = 10 \times 3
    9.0000
                      0
                                 0
    9.0000
                      0
                                  0
    9.0000
                      0
                                  0
    9.0000
                      0
    9.0000
                      0
    9.0000
                      0
                                 0
    9.0000
                      0
                                 (-)
    9.0000
                      0
                                 (-)
    9.0000
                      0
                                 0
    9.0000
                      (-)
                                  (-)
```

Alternatively, you can use the dist function to verify that the distance between the interpolated quaternions is consistent. The dist function returns angular distance in radians; convert to degrees for easy comparison.

```
 \begin{aligned} & \mathsf{def} = \mathsf{rad2deg}(\mathsf{dist}(\mathsf{interpolatedQuaternions}(2 : \mathsf{end}), \mathsf{interpolatedQuaternions}(1 : \mathsf{end-1}))) \\ & \mathsf{def} = 1 \times 10 \\ & 9.0000 \quad 9.0000 \\ \end{aligned}
```

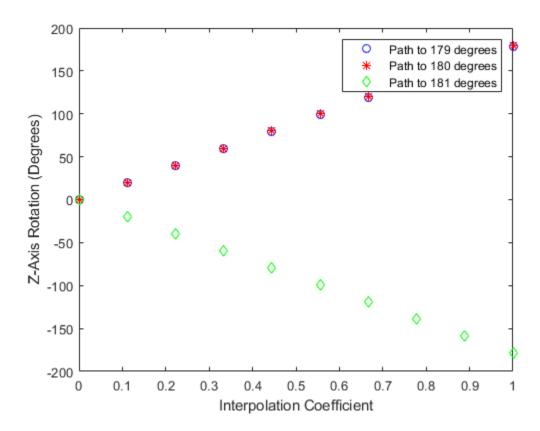
SLERP Minimizes Great Circle Path

The SLERP algorithm interpolates along a great circle path connecting two quaternions. This example shows how the SLERP algorithm minimizes the great circle path.

Define three quaternions:

- 1 q0 quaternion indicating no rotation from the global frame
- **2** q179 quaternion indicating a 179 degree rotation about the *z*-axis
- **3** q180 quaternion indicating a 180 degree rotation about the z-axis

```
q181 - quaternion indicating a 181 degree rotation about the z-axis
q0 = ones(1, 'quaternion');
q179 = quaternion([179,0,0], 'eulerd', 'ZYX', 'frame');
q180 = quaternion([180,0,0], 'eulerd', 'ZYX', 'frame');
q181 = quaternion([181,0,0],'eulerd','ZYX','frame');
Use slerp to interpolate between q0 and the three quaternion rotations. Specify that the paths are
traveled in 10 steps.
T = linspace(0,1,10);
q179path = slerp(q0,q179,T);
q180path = slerp(q0,q180,T);
q181path = slerp(q0,q181,T);
Plot each path in terms of Euler angles in degrees.
q179pathEuler = eulerd(q179path,'ZYX','frame');
q180pathEuler = eulerd(q180path,'ZYX','frame');
q181pathEuler = eulerd(q181path,'ZYX','frame');
T,q181pathEuler(:,1),'gd');
legend('Path to 179 degrees', ...
        'Path to 180 degrees', ...
       'Path to 181 degrees')
xlabel('Interpolation Coefficient')
ylabel('Z-Axis Rotation (Degrees)')
```



The path between q0 and q179 is clockwise to minimize the great circle distance. The path between q0 and q181 is counterclockwise to minimize the great circle distance. The path between q0 and q180 can be either clockwise or counterclockwise, depending on numerical rounding.

Input Arguments

q1 — Quaternion

scalar | vector | matrix | multidimensional array

Quaternion to interpolate, specified as a scalar, vector, matrix, or multidimensional array of quaternions.

q1, q2, and T must have compatible sizes. In the simplest cases, they can be the same size or any one can be a scalar. Two inputs have compatible sizes if, for every dimension, the dimension sizes of the inputs are either the same or one of them is 1.

Data Types: quaternion

q2 — Quaternion

scalar | vector | matrix | multidimensional array

Quaternion to interpolate, specified as a scalar, vector, matrix, or multidimensional array of quaternions.

q1, q2, and T must have compatible sizes. In the simplest cases, they can be the same size or any one can be a scalar. Two inputs have compatible sizes if, for every dimension, the dimension sizes of the inputs are either the same or one of the dimension sizes is 1.

Data Types: quaternion

T — Interpolation coefficient

scalar | vector | matrix | multidimensional array

Interpolation coefficient, specified as a scalar, vector, matrix, or multidimensional array of numbers with each element in the range [0,1].

q1, q2, and T must have compatible sizes. In the simplest cases, they can be the same size or any one can be a scalar. Two inputs have compatible sizes if, for every dimension, the dimension sizes of the inputs are either the same or one of the dimension sizes is 1.

Data Types: single | double

Output Arguments

q0 — Interpolated quaternion

scalar | vector | matrix | multidimensional array

Interpolated quaternion, returned as a scalar, vector, matrix, or multidimensional array.

Data Types: quaternion

Algorithms

Quaternion spherical linear interpolation (SLERP) is an extension of linear interpolation along a plane to spherical interpolation in three dimensions. The algorithm was first proposed in [1]. Given two quaternions, q_1 and q_2 , SLERP interpolates a new quaternion, q_0 , along the great circle that connects q_1 and q_2 . The interpolation coefficient, T, determines how close the output quaternion is to either q_1 and q_2 .

The SLERP algorithm can be described in terms of sinusoids:

$$q_0 = \frac{\sin((1-T)\theta)}{\sin(\theta)}q_1 + \frac{\sin(T\theta)}{\sin(\theta)}q_2$$

where q_1 and q_2 are normalized quaternions, and θ is half the angular distance between q_1 and q_2 .

References

[1] Shoemake, Ken. "Animating Rotation with Quaternion Curves." *ACM SIGGRAPH Computer Graphics* Vol. 19, Issue 3, 1985, pp. 345–354.

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

Functions

dist|meanrot

Objects

quaternion

Topics

"Lowpass Filter Orientation Using Quaternion SLERP"
"Rotations, Orientation, and Quaternions"

times, .*

Element-wise quaternion multiplication

Syntax

```
quatC = A.*B
```

Description

quatC = A.*B returns the element-by-element quaternion multiplication of quaternion arrays.

You can use quaternion multiplication to compose rotation operators:

- To compose a sequence of frame rotations, multiply the quaternions in the same order as the desired sequence of rotations. For example, to apply a p quaternion followed by a q quaternion, multiply in the order pq. The rotation operator becomes $(pq)^*v(pq)$, where v represents the object to rotate in quaternion form. * represents conjugation.
- To compose a sequence of point rotations, multiply the quaternions in the reverse order of the desired sequence of rotations. For example, to apply a p quaternion followed by a q quaternion, multiply in the reverse order, qp. The rotation operator becomes $(qp)v(qp)^*$.

Examples

Multiply Two Quaternion Vectors

Create two vectors, A and B, and multiply them element by element.

Multiply Two Quaternion Arrays

Create two 3-by-3 arrays, A and B, and multiply them element by element.

```
A = reshape(quaternion(randn(9,4)),3,3);

B = reshape(quaternion(randn(9,4)),3,3);

C = A.*B

C=3×3 quaternion array

0.60169 + 2.4332i - 2.5844j + 0.51646k -0.49513 + 1.1722i + 4.4401j - 1.217k

-4.2329 + 2.4547i + 3.7768j + 0.77484k -0.65232 - 0.43112i - 1.4645j - 0.90073k
```

```
-4.4159 + 2.1926i + 1.9037j - 4.0303k -2.0232 + 0.4205i - 0.17288j + 3.8529k
```

Note that quaternion multiplication is not commutative:

```
isequal(C,B.*A)
ans = logical
0
```

Multiply Quaternion Row and Column Vectors

Create a row vector **a** and a column vector **b**, then multiply them. The 1-by-3 row vector and 4-by-1 column vector combine to produce a 4-by-3 matrix with all combinations of elements multiplied.

```
a = [zeros('quaternion'),ones('quaternion'),quaternion(randn(1,4))]
a=1×3 quaternion array
                                0j +
                                           0k
                                                                  0i +
                                                                              0j +
           0 +
                     0i +
                                                        1 + 
                                                                                         0k
b = quaternion(randn(4,4))
b=4×1 quaternion array
      0.31877 +
                 3.5784i +
                              0.7254i -
                                         0.12414k
      -1.3077 +
                 2.7694i - 0.063055i +
                                         1.4897k
     -0.43359 -
                 1.3499i + 0.71474i +
                                          1.409k
      0.34262 +
                 3.0349i - 0.20497j +
                                          1.4172k
a.*b
ans=4×3 quaternion array
            0 +
                                   0i +
                                               0k
                                                       0.31877 +
                                                                    3.5784i +
                                                                                0.7254i -
                                                                                           0.1241
                      0i +
            0 +
                       0i +
                                   0i +
                                               0k
                                                       -1.3077 +
                                                                    2.7694i - 0.063055j +
                                                                                            1.489
            0 +
                       0i +
                                   0j +
                                               0 k
                                                       -0.43359 -
                                                                   1.3499i + 0.71474j +
                                                                                             1.40
            0 +
                       0i +
                                   0j +
                                               0k
                                                       0.34262 +
                                                                   3.0349i - 0.20497j +
                                                                                            1.417
```

Input Arguments

A — Array to multiply

scalar | vector | matrix | multidimensional array

Array to multiply, specified as a quaternion, an array of quaternions, a real scalar, or an array of real numbers.

A and B must have compatible sizes. In the simplest cases, they can be the same size or one can be a scalar. Two inputs have compatible sizes if, for every dimension, the dimension sizes of the inputs are the same or one of them is 1.

Data Types: quaternion | single | double

B — Array to multiply

scalar | vector | matrix | multidimensional array

Array to multiply, specified as a quaternion, an array of quaternions, a real scalar, or an array of real numbers.

A and B must have compatible sizes. In the simplest cases, they can be the same size or one can be a scalar. Two inputs have compatible sizes if, for every dimension, the dimension sizes of the inputs are the same or one of them is 1.

Data Types: quaternion | single | double

Output Arguments

quatC — Quaternion product

scalar | vector | matrix | multidimensional array

Quaternion product, returned as a scalar, vector, matrix, or multidimensional array.

Data Types: quaternion

Algorithms

Quaternion Multiplication by a Real Scalar

Given a quaternion,

$$q = a_{\alpha} + b_{\alpha}i + c_{\alpha}j + d_{\alpha}k,$$

the product of q and a real scalar β is

$$\beta q = \beta a_{q} + \beta b_{q}i + \beta c_{q}j + \beta d_{q}k$$

Quaternion Multiplication by a Quaternion Scalar

The definition of the basis elements for quaternions,

$$i^2 = i^2 = k^2 = iik = -1$$

can be expanded to populate a table summarizing quaternion basis element multiplication:

	1	i	j	k
1	1	i	j	k
i	i	-1	k	- ј
j	j	-k	-1	i
k	k	j	-i	-1

When reading the table, the rows are read first, for example: ij = k and ji = -k.

Given two quaternions, $q = a_q + b_q i + c_q j + d_q k$, and $p = a_p + b_p i + c_p j + d_p k$, the multiplication can be expanded as:

$$z = pq = (a_{p} + b_{p}i + c_{p}j + d_{p}k)(a_{q} + b_{q}i + c_{q}j + d_{q}k)$$

$$= a_{p}a_{q} + a_{p}b_{q}i + a_{p}c_{q}j + a_{p}d_{q}k$$

$$+ b_{p}a_{q}i + b_{p}b_{q}i^{2} + b_{p}c_{q}ij + b_{p}d_{q}ik$$

$$+ c_{p}a_{q}j + c_{p}b_{q}ji + c_{p}c_{q}j^{2} + c_{p}d_{q}jk$$

$$+ d_{p}a_{q}k + d_{p}b_{q}ki + d_{p}c_{q}kj + d_{p}d_{q}k^{2}$$

You can simplify the equation using the quaternion multiplication table.

$$\begin{split} z &= pq = a_{\rm p}a_{\rm q} + a_{\rm p}b_{\rm q}{\rm i} + a_{\rm p}c_{\rm q}{\rm j} + a_{\rm p}d_{\rm q}{\rm k} \\ &+ b_{\rm p}a_{\rm q}{\rm i} - b_{\rm p}b_{\rm q} + b_{\rm p}c_{\rm q}{\rm k} - b_{\rm p}d_{\rm q}{\rm j} \\ &+ c_{\rm p}a_{\rm q}{\rm j} - c_{\rm p}b_{\rm q}{\rm k} - c_{\rm p}c_{\rm q} + c_{\rm p}d_{\rm q}{\rm i} \\ &+ d_{\rm p}a_{\rm q}k + d_{\rm p}b_{\rm q}{\rm j} - d_{\rm p}c_{\rm q}{\rm i} - d_{\rm p}d_{\rm q} \end{split}$$

References

[1] Kuipers, Jack B. *Quaternions and Rotation Sequences: A Primer with Applications to Orbits, Aerospace, and Virtual Reality.* Princeton, NJ: Princeton University Press, 2007.

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

Functions

mtimes, *|prod

Objects

quaternion

Topics

"Rotations, Orientation, and Quaternions"

transpose, .'

Transpose a quaternion array

Syntax

```
Y = quat.'
```

Description

Y = quat.' returns the non-conjugate transpose of the quaternion array, quat.

Examples

Vector Transpose

Create a vector of quaternions and compute its nonconjugate transpose.

```
quat = quaternion(randn(4,4))
quat=4×1 quaternion array
     0.53767 + 0.31877i +
                            3.5784j + 0.7254k
                           2.7694j - 0.063055k
      1.8339 -
               1.3077i +
     -2.2588 - 0.43359i -
                            1.3499j + 0.71474k
     0.86217 + 0.34262i + 3.0349j - 0.20497k
quatTransposed = quat.'
```

```
quatTransposed=1×4 quaternion array
     0.53767 + 0.31877i + 3.5784j + 0.7254k
                                                 1.8339 - 1.3077i + 2.7694j - 0.06305
```

Matrix Transpose

quat=2×2 quaternion array

Create a matrix of quaternions and compute its nonconjugate transpose.

```
quat = [quaternion(randn(2,4)),quaternion(randn(2,4))]
```

```
0.53767 - 2.2588i + 0.31877j - 0.43359k
                                                        3.5784 - 1.3499i + 0.7254j + 0.71476
      1.8339 + 0.86217i - 1.3077j + 0.34262k
                                                        2.7694 + 3.0349i - 0.063055j - 0.2049
quatTransposed = quat.'
quatTransposed=2×2 quaternion array
      0.53767 - 2.2588i + 0.31877j - 0.43359k
3.5784 - 1.3499i + 0.7254j + 0.71474k
                                                        1.8339 + 0.86217i - 1.3077j + 0.3426
```

2.7694 + 3.0349i - 0.063055j - 0.2049

Input Arguments

quat — Quaternion array to transpose

vector | matrix

Quaternion array to transpose, specified as a vector or matrix of quaternions. transpose is defined for 1-D and 2-D arrays. For higher-order arrays, use permute.

Data Types: quaternion

Output Arguments

Y — Transposed quaternion array

vector | matrix

Transposed quaternion array, returned as an N-by-M array, where quat was specified as an M-by-N array.

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

Functions

ctranspose, '

Objects

quaternion

Topics

"Rotations, Orientation, and Quaternions"

uminus, -

Quaternion unary minus

Syntax

```
mQuat = -quat
```

Description

mQuat = -quat negates the elements of quat and stores the result in mQuat.

Examples

Negate Elements of Quaternion Matrix

Unary minus negates each part of a the quaternion. Create a 2-by-2 matrix, Q.

```
Q = quaternion(randn(2), randn(2), randn(2), randn(2))
```

Negate the parts of each quaternion in Q.

```
R = -Q
```

Input Arguments

quat — Quaternion array

```
scalar | vector | matrix | multidimensional array
```

Quaternion array, specified as a scalar, vector, matrix, or multidimensional array.

Data Types: quaternion

Output Arguments

mQuat — Negated quaternion array

```
scalar | vector | matrix | multidimensional array
```

Negated quaternion array, returned as the same size as quat.

Data Types: quaternion

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder $^{\text{\tiny TM}}$.

See Also

Functions

minus, -

Objects

quaternion

Topics

"Rotations, Orientation, and Quaternions"

zeros

Create quaternion array with all parts set to zero

Syntax

```
quatZeros = zeros('quaternion')
quatZeros = zeros(n,'quaternion')
quatZeros = zeros(sz,'quaternion')
quatZeros = zeros(sz1,...,szN,'quaternion')
quatZeros = zeros(____,'like',prototype,'quaternion')
```

Description

```
quatZeros = zeros('quaternion') returns a scalar quaternion with all parts set to zero.
quatZeros = zeros(n, 'quaternion') returns an n-by-n matrix of quaternions.
quatZeros = zeros(sz, 'quaternion') returns an array of quaternions where the size vector, sz, defines size(quatZeros).
quatZeros = zeros(sz1,...,szN, 'quaternion') returns a sz1-by-...-by-szN array of quaternions where sz1,...,szN indicates the size of each dimension.
quatZeros = zeros(____, 'like',prototype, 'quaternion') specifies the underlying class of the returned quaternion array to be the same as the underlying class of the quaternion prototype.
```

Examples

Quaternion Scalar Zero

Create a quaternion scalar zero.

```
quatZeros = zeros('quaternion')
quatZeros = quaternion
0 + 0i + 0j + 0k
```

Square Matrix of Quaternions

Create an n-by-n array of quaternion zeros.

```
n = 3;
quatZeros = zeros(n,'quaternion')
quatZeros=3×3 quaternion array
    0 + 0i + 0j + 0k     0 + 0i + 0j + 0k
```

```
0 + 0i + 0j + 0k 0 + 0i + 0j + 0k
```

Multidimensional Array of Quaternion Zeros

Create a multidimensional array of quaternion zeros by defining array dimensions in order. In this example, you create a 3-by-1-by-2 array. You can specify dimensions using a row vector or commaseparated integers.

Specify the dimensions using a row vector and display the results:

Specify the dimensions using comma-separated integers, and then verify the equivalence of the two syntaxes:

```
quatZerosSyntax2 = zeros(3,1,2,'quaternion');
isequal(quatZerosSyntax1,quatZerosSyntax2)
ans = logical
1
```

Underlying Class of Quaternion Zeros

A quaternion is a four-part hyper-complex number used in three-dimensional representations. You can specify the underlying data type of the parts as single or double. The default is double.

Create a quaternion array of zeros with the underlying data type set to single.

Verify the underlying class using the classUnderlying function.

classUnderlying(quatZeros)

```
ans =
'single'
```

Input Arguments

n — Size of square quaternion matrix

integer value

Size of square quaternion matrix, specified as an integer value. If n is 0 or negative, then quatZeros is returned as an empty matrix.

Example: zeros(4, 'quaternion') returns a 4-by-4 matrix of quaternion zeros.

Data Types: single | double | int8 | int16 | int32 | int64 | uint8 | uint16 | uint32 | uint64

sz - Output size

row vector of integer values

Output size, specified as a row vector of integer values. Each element of sz indicates the size of the corresponding dimension in quatZeros. If the size of any dimension is 0 or negative, then quatZeros is returned as an empty array.

Example: zeros([1,4,2], 'quaternion') returns a 1-by-4-by-2 array of quaternion zeros.

Data Types: single | double | int8 | int16 | int32 | int64 | uint8 | uint16 | uint32 | uint64

prototype — Quaternion prototype

variable

Quaternion prototype, specified as a variable.

Example: zeros(2, 'like', quat, 'quaternion') returns a 2-by-2 matrix of quaternions with the same underlying class as the prototype quaternion, quat.

Data Types: quaternion

sz1, ..., szN - Size of each dimension

two or more integer values

Size of each dimension, specified as two or more integers.

- If the size of any dimension is 0, then quatZeros is returned as an empty array.
- If the size of any dimension is negative, then it is treated as 0.

Example: zeros(2,3,'quaternion') returns a 2-by-3 matrix of quaternion zeros.

Data Types: single | double | int8 | int16 | int32 | int64 | uint8 | uint16 | uint32 | uint64

Output Arguments

quatZeros — Quaternion zeros

scalar | vector | matrix | multidimensional array

Quaternion zeros, returned as a quaternion or array of quaternions.

Given a quaternion of the form $Q = a + b\mathbf{i} + c\mathbf{j} + d\mathbf{k}$, a quaternion zero is defined as $Q = 0 + 0\mathbf{i} + 0\mathbf{j} + 0\mathbf{k}$.

Data Types: quaternion

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

Functions

ones

Objects

quaternion

Topics

"Rotations, Orientation, and Quaternions"

rateControl

Execute loop at fixed frequency

Description

The rateControl object enables you to run a loop at a fixed frequency. It also collects statistics about the timing of the loop iterations. Use waitfor in the loop to pause code execution until the next time step. The loop operates every <code>DesiredPeriod</code> seconds, unless the enclosed code takes longer to operate. The object uses the <code>OverrunAction</code> property to determine how it handles longer loop operation times. The default setting, 'slip', immediately executes the loop if <code>LastPeriod</code> is greater than <code>DesiredPeriod</code>. Using 'drop' causes the <code>waitfor</code> method to wait until the next multiple of <code>DesiredPeriod</code> is reached to execute the next loop.

Tip The scheduling resolution of your operating system and the level of other system activity can affect rate execution accuracy. As a result, accurate rate timing is limited to 100 Hz for execution of MATLAB code. To improve performance and execution speeds, use code generation.

Creation

Syntax

rateObj = rateControl(desiredRate)

Description

rateObj = rateControl(desiredRate) creates an object that operates loops at a fixed-rate
based on your system time and directly sets the DesireRate property.

Properties

DesiredRate — Desired execution rate

scalar

Desired execution rate of loop, specified as a scalar in Hz. When using waitfor, the loop operates every DesiredRate seconds, unless the loop takes longer. It then begins the next loop based on the specified OverrunAction.

DesiredPeriod — Desired time period between executions

scalar

Desired time period between executions, specified as a scalar in seconds. This property is equal to the inverse of DesiredRate.

TotalElapsedTime — Elapsed time since construction or reset

scalar

Elapsed time since construction or reset, specified as a scalar in seconds.

LastPeriod — Elapsed time between last two calls to waitfor

NaN (default) | scalar

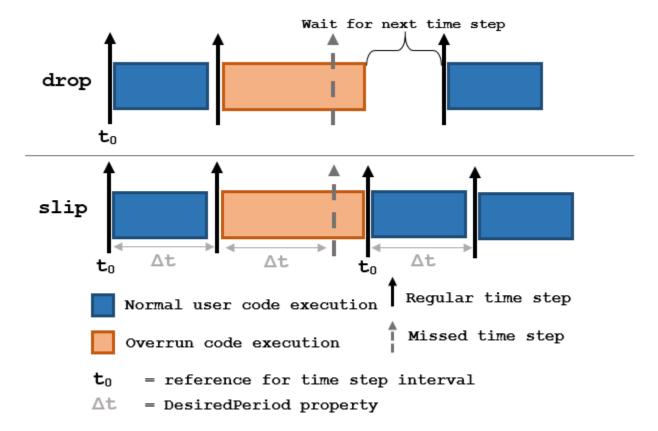
Elapsed time between last two calls to waitfor, specified as a scalar. By default, LastPeriod is set to NaN until waitfor is called for the first time. After the first call, LastPeriod equals TotalElapsedTime.

OverrunAction — Method for handling overruns

'slip' (default) | 'drop'

Method for handling overruns, specified as one of these character vectors:

- 'drop' waits until the next time interval equal to a multiple of DesiredPeriod
- 'slip' immediately executes the loop again



Each code section calls waitfor at the end of execution.

Object Functions

waitfor Pause code execution to achieve desired execution rate

statistics Statistics of past execution periods

reset Reset Rate object

Examples

Run Loop at Fixed Rate

Create a rate object that runs at 1 Hz.

```
r = rateControl(1);
```

Start a loop using the rateControl object inside to control the loop execution. Reset the object prior to the loop execution to reset timer. Print the iteration and time elapsed.

```
reset(r)
for i = 1:10
    time = r.TotalElapsedTime;
    fprintf('Iteration: %d - Time Elapsed: %f\n',i,time)
   waitfor(r);
end
Iteration: 1 - Time Elapsed: 0.002345
Iteration: 2 - Time Elapsed: 1.000594
Iteration: 3 - Time Elapsed: 2.000562
Iteration: 4 - Time Elapsed: 3.000690
Iteration: 5 - Time Elapsed: 4.000886
Iteration: 6 - Time Elapsed: 5.000637
Iteration: 7 - Time Elapsed: 6.000167
Iteration: 8 - Time Elapsed: 7.000496
Iteration: 9 - Time Elapsed: 8.000213
Iteration: 10 - Time Elapsed: 9.000539
```

Each iteration executes at a 1-second interval.

Get Statistics From Rate Object Execution

```
Create a rateControl object for running at 20 Hz.
```

```
r = rateControl(20);
```

Start a loop and control operation using the rateControl object.

```
for i = 1:30
   % Your code goes here
   waitfor(r);
end
```

Get Rate object statistics after loop operation.

Run Loop At Fixed Rate and Reset Rate Object

Create a rateControl object for running at 20 Hz.

```
r = rateControl(2);
Start a loop and control operation using the Rate object.
for i = 1:30
    % Your code goes here
    waitfor(r);
end
Display the rateControl object properties after loop operation.
disp(r)
  rateControl with properties:
         DesiredRate: 2
       DesiredPeriod: 0.5000
       OverrunAction: 'slip'
    TotalElapsedTime: 15.0093
          LastPeriod: 0.4998
Reset the object to restart the time statistics.
reset(r);
disp(r)
  rateControl with properties:
         DesiredRate: 2
       DesiredPeriod: 0.5000
       OverrunAction: 'slip'
    TotalElapsedTime: 0.0029
          LastPeriod: NaN
```

Compatibility Considerations

rateControl was renamed

Behavior change in future release

The rateControl object was renamed from robotics.Rate. Use rateControl for all object creation.

See Also

```
reset | rosrate | statistics | waitfor
```

Topics

"Execute Code at a Fixed-Rate"

Introduced in R2016a

reset

Reset Rate object

Syntax

reset(rate)

Description

reset(rate) resets the state of the Rate object, including the elapsed time and all statistics about previous periods. reset is useful if you want to run multiple successive loops at the same rate, or if the object is created before the loop is executed.

Input Arguments

```
rate — Rate object
```

handle

Rate object, specified as a handle. This object contains the information for the desired rate and other information about the execution. See rateControl for more information.

Examples

Run Loop At Fixed Rate and Reset Rate Object

```
Create a rateControl object for running at 20 Hz.
```

```
r = rateControl(2);
```

Start a loop and control operation using the Rate object.

```
for i = 1:30
   % Your code goes here
   waitfor(r);
end
```

Display the rateControl object properties after loop operation.

```
disp(r)
```

```
rateControl with properties:

DesiredRate: 2
DesiredPeriod: 0.5000
OverrunAction: 'slip'
TotalElapsedTime: 15.0093
LastPeriod: 0.4998
```

Reset the object to restart the time statistics.

reset(r); disp(r)

rateControl with properties:

DesiredRate: 2
DesiredPeriod: 0.5000
OverrunAction: 'slip'
TotalElapsedTime: 0.0029
LastPeriod: NaN

See Also

rateControl|waitfor

Topics

"Execute Code at a Fixed-Rate"

Introduced in R2016a

statistics

Statistics of past execution periods

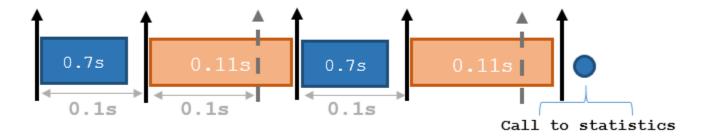
Syntax

stats = statistics(rate)

Description

stats = statistics(rate) returns statistics of previous periods of code execution. stats is a struct with these fields: Periods, NumPeriods, AveragePeriod, StandardDeviation, and NumOverruns.

Here is a sample execution graphic using the default setting, 'slip', for the OverrunAction property in the Rate object. See OverrunAction for more information on overrun code execution.



The output of statistics is:

stats =

Periods: [0.7 0.11 0.7 0.11]
NumPeriods: 4
AveragePeriod: 0.09
StandardDeviation: 0.0231
NumOverruns: 2

Input Arguments

rate — Rate object

handle

Rate object, specified as an object handle. This object contains the information for the DesiredRate and other info about the execution. See rateControl for more information.

Output Arguments

stats — Time execution statistics

structure

Time execution statistics, returned as a structure. This structure contains the following fields:

- Period All time periods (returned in seconds) used to calculate statistics as an indexed array. stats.Period(end) is the most recent period.
- NumPeriods Number of elements in Periods
- AveragePeriod Average time in seconds
- StandardDeviation Standard deviation of all periods in seconds, centered around the mean stored in AveragePeriod
- NumOverruns Number of periods with overrun

Examples

Get Statistics From Rate Object Execution

```
Create a rateControl object for running at 20 Hz.
```

```
r = rateControl(20);
```

Start a loop and control operation using the rateControl object.

```
for i = 1:30
   % Your code goes here
   waitfor(r);
end
```

Get Rate object statistics after loop operation.

See Also

rateControl|waitfor

Topics

"Execute Code at a Fixed-Rate"

Introduced in R2016a

waitfor

Package: robotics

Pause code execution to achieve desired execution rate

Syntax

```
waitfor(rate)
numMisses = waitfor(rate)
```

Description

waitfor(rate) pauses execution until the code reaches the desired execution rate. The function accounts for the time that is spent executing code between waitfor calls.

numMisses = waitfor(rate) returns the number of iterations missed while executing code
between calls.

Examples

Run Loop at Fixed Rate

Create a rate object that runs at 1 Hz.

```
r = rateControl(1);
```

Start a loop using the rateControl object inside to control the loop execution. Reset the object prior to the loop execution to reset timer. Print the iteration and time elapsed.

```
reset(r)
for i = 1:10
   time = r.TotalElapsedTime;
    fprintf('Iteration: %d - Time Elapsed: %f\n',i,time)
   waitfor(r):
end
Iteration: 1 - Time Elapsed: 0.002345
Iteration: 2 - Time Elapsed: 1.000594
Iteration: 3 - Time Elapsed: 2.000562
Iteration: 4 - Time Elapsed: 3.000690
Iteration: 5 - Time Elapsed: 4.000886
Iteration: 6 - Time Elapsed: 5.000637
Iteration: 7 - Time Elapsed: 6.000167
Iteration: 8 - Time Elapsed: 7.000496
Iteration: 9 - Time Elapsed: 8.000213
Iteration: 10 - Time Elapsed: 9.000539
```

Each iteration executes at a 1-second interval.

Input Arguments

rate — Rate object

handle

Rate object, specified as a handle. This object contains the information for the desired rate and other information about the execution. See rateControl for more information.

Output Arguments

numMisses — Number of missed task executions

scalar

Number of missed task executions, returned as a scalar waitfor returns the number of times the task was missed in the Rate object based on the LastPeriod time. For example, if the desired rate is 1 Hz and the last period was 3.2 seconds, numMisses returns 3.

See Also

rateControl

Topics

"Execute Code at a Fixed-Rate"

Introduced in R2016a

reedsSheppConnection

Reeds-Shepp path connection type

Description

The reedSheppConnection object holds information for computing a reedsSheppPathSegment object to connect between poses. A Reeds-Shepp path segment connects two poses as a sequence of five motions. The motion options are:

- Straight
- Left turn at maximum steer
- · Right turn at maximum steer
- · No movement

A Reeds-Shepp path segment supports both forward and backward motion.

Use this connection object to define parameters for a vehicle motion model, including the minimum turning radius and options for path types. To generate a path segment between poses using this connection type, call the connect function.

Creation

Syntax

```
reedsConnObj = reedsSheppConnection
reedsConnObj = reedsSheppConnection(Name, Value)
```

Description

reedsConnObj = reedsSheppConnection creates an object using default property values.

reedsConnObj = reedsSheppConnection(Name, Value) specifies property values using name-value pairs. To set multiple properties, specify multiple name-value pairs.

Properties

MinTurningRadius — Minimum turning radius

1 (default) | positive scalar in meters

Minimum turning radius for the vehicle, specified as a positive scalar in meters. The minimum turning radius is for the smallest circle the vehicle can make with maximum steer in a single direction.

Data Types: double

DisabledPathTypes — Path types to disable

{} (default) | vector of string scalars | cell array of character vectors

Path types to disable, specified as a vector of string scalars or cell array of character vectors.

Motion Type	Description
"Sp","Sn"	Straight (p = forward, n = reverse)
"Lp","Ln"	Left turn at the maximum steering angle of the vehicle $(p = forward, n = reverse)$
"Rp","Rn"	Right turn at the maximum steering angle of the vehicle ($p = forward$, $n = reverse$)
"N"	No motion

If a path segment has fewer than five motion types, the remaining elements are "N" (no motion).

To see all available path types, see the AllPathTypes property.

Example: ["LpSnLp", "LnSnRpSn", "LnSnRpSnLp"]

Data Types: cell

AllPathTypes — All possible path types

cell array of character vectors

This property is read-only.

All possible path types, specified as a cell array of character vectors. This property lists all types. To disable certain types, specify types from this list in DisabledPathTypes.

For Reeds-Shepp connections, there are 44 possible combinations of motion types.

Data Types: cell

ForwardCost — Cost multiplier to travel forward

1 (default) | positive numeric scalar

Cost multiple to travel forward, specified as a positive numeric scalar. Increase this property to penalize forward motion.

Data Types: double

ReverseCost — Cost multiplier to travel in reverse

1 (default) | positive numeric scalar

Cost multiple to travel in reverse, specified as a positive numeric scalar. Increase this property to penalize reverse motion.

Data Types: double

Object Functions

connect Connect poses for given connection type

Examples

Connect Poses Using ReedsShepp Connection Path

```
Create a reedsSheppConnection object.
```

```
reedsConnObj = reedsSheppConnection;
```

Define start and goal poses as [x y theta] vectors.

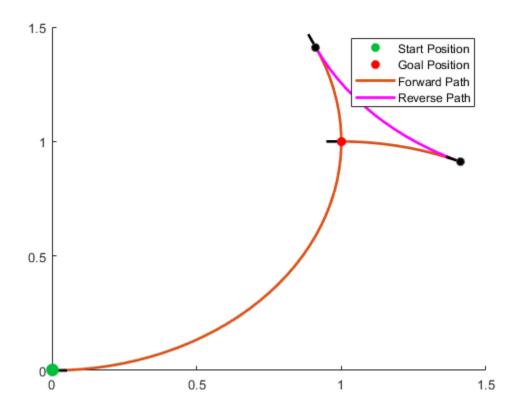
```
startPose = [0 0 0];
goalPose = [1 1 pi];
```

Calculate a valid path segment to connect the poses.

```
[pathSegObj,pathCosts] = connect(reedsConnObj,startPose,goalPose);
```

Show the generated path.

show(pathSegObj{1})



Modify Connection Types for Reeds-Shepp Path

Create a reedsSheppConnection object.

reedsConnObj = reedsSheppConnection;

Define start and goal poses as $[x \ y \ theta]$ vectors.

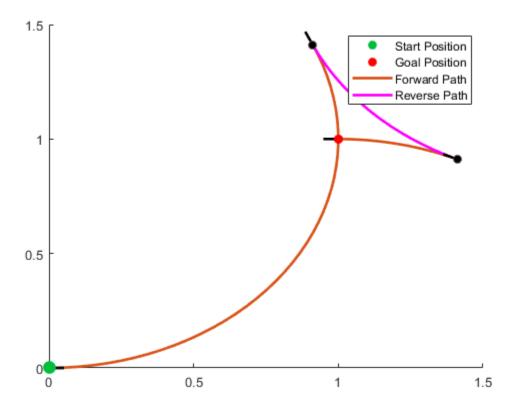
```
startPose = [0 0 0];
goalPose = [1 1 pi];
```

Calculate a valid path segment to connect the poses.

```
[pathSegObj,pathCosts] = connect(reedsConnObj,startPose,goalPose);
```

Show the generated path. Notice the direction of the turns.

show(pathSegObj{1})



pathSegObj{1}.MotionTypes

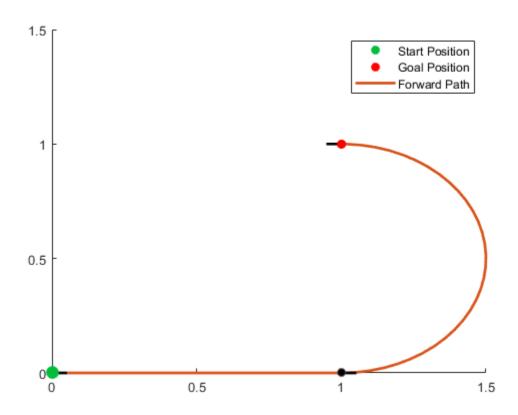
ans =
$$1x5$$
 cell {'L'} {'R'} {'L'} {'N'} {'N'}

pathSegObj{1}.MotionDirections

ans =
$$1 \times 5$$

1 -1 1 1 1

Disable this specific motion sequence in a new connection object. Reduce the MinTurningRadius if the robot is more maneuverable. Increase the reverse cost to reduce the likelihood of reverse directions being used. Connect the poses again to get a different path.



Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

Objects

dubinsConnection | dubinsPathSegment | reedsSheppPathSegment

Functions

connect|interpolate|show

Introduced in R2019b

reedsSheppPathSegment

Reeds-Shepp path segment connecting two poses

Description

The reedSheppPathSegment object holds information for a Reeds-Shepp path segment to connect between poses. A Reeds-Shepp path segment connects two poses as a sequence of five motion types. The motion options are:

- Straight
- · Left turn at maximum steer
- · Right turn at maximum steer
- No movement

Creation

To generate a reedSheppPathSegment object, use the connect function with a reedsSheppConnection object:

reedsPathSegObj = connect(connectionObj,start,goal) connects the start and goal poses
using the specified connection type object.

To specifically define a path segment:

reedsPathSegObj =

reedsSheppPathSegment(connectionObj, start, goal, motionLengths, motionTypes) specifies the Reeds-Shepp connection type, the start and goal poses, and the corresponding motion lengths and types. These values are set to the corresponding properties in the object.

Properties

MinTurningRadius — Minimum turning radius of vehicle

positive scalar

This property is read-only.

Minimum turning radius of the vehicle, specified as a positive scalar in meters. This value corresponds to the radius of the turning circle at the maximum steering angle of the vehicle.

Data Types: double

StartPose — Initial pose of vehicle

 $[x, y, \Theta]$ vector

This property is read-only.

Initial pose of the vehicle at the start of the path segment, specified as an $[x, y, \Theta]$ vector. x and y are in meters. Θ is in radians.

Data Types: double

GoalPose — **Goal pose of vehicle**

[x, y, Θ] vector

This property is read-only.

Goal pose of the vehicle at the end of the path segment, specified as an $[x, y, \Theta]$ vector. x and y are in meters. Θ is in radians.

Data Types: double

MotionLengths — Length of each motion

five-element numeric vector

This property is read-only.

Length of each motion in the path segment, specified as a five-element numeric vector in meters. Each motion length corresponds to a motion type specified in MotionTypes.

Data Types: double

MotionTypes — Type of each motion

five-element string cell array

This property is read-only.

Type of each motion in the path segment, specified as a five-element string cell array.

Motion Type	Description
"S"	Straight (forward, p or reverse, n)
"L"	Left turn at the maximum steering angle of the vehicle (forward, p or reverse, n)
"R"	Right turn at the maximum steering angle of the vehicle (forward, p or reverse, n)
"N"	No motion

If a path segment has fewer than five motion types, the remaining elements are "N" (no motion).

```
Example: {"L", "S", "R", "L", "R"}
```

Data Types: cell

MotionDirections — Direction of each motion

five-element vector of 1s (forward motion) and -1s (reverse motion)

This property is read-only.

Direction of each motion in the path segment, specified as a five-element vector of 1s (forward motion) and -1s (reverse motion). Each motion direction corresponds to a motion length specified in MotionLengths and a motion type specified in MotionTypes.

When no motion occurs, that is, when a MotionTypes value is "N", then the corresponding MotionDirections element is 1.

```
Example: [-1 1 -1 1 1]
```

Data Types: double

Length — Length of path segment

positive scalar

This property is read-only.

Length of the path segment, specified as a positive scalar in meters. This length is just a sum of the elements in MotionLengths.

Data Types: double

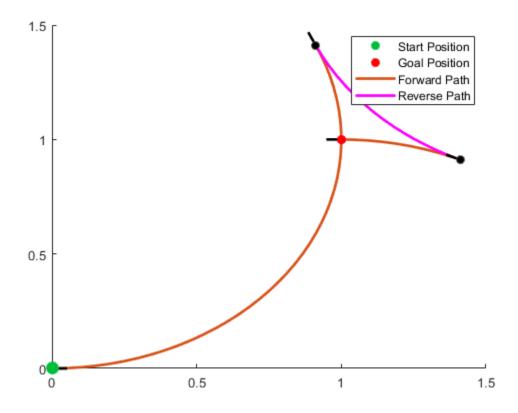
Object Functions

show Visualize path segment

Examples

Connect Poses Using ReedsShepp Connection Path

```
Create a reedsSheppConnection object.
reedsConnObj = reedsSheppConnection;
Define start and goal poses as [x y theta] vectors.
startPose = [0 0 0];
goalPose = [1 1 pi];
Calculate a valid path segment to connect the poses.
[pathSegObj,pathCosts] = connect(reedsConnObj,startPose,goalPose);
Show the generated path.
show(pathSegObj{1})
```



References

[1] Reeds, J. A., and L. A. Shepp. "Optimal Paths for a Car That Goes Both Forwards and Backwards." *Pacific Journal of Mathematics*. Vol. 145, Number 2, 1990, pp. 367–393.

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder $^{\text{\tiny TM}}$.

See Also

Objects

dubinsConnection | dubinsPathSegment | reedsSheppConnection

Functions

connect | interpolate | show

Introduced in R2019b

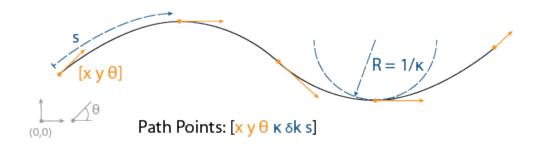
referencePathFrenet

Smooth reference path fit to waypoints

Description

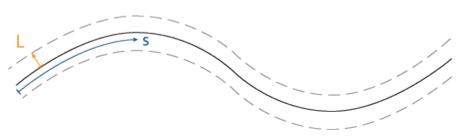
The referencePathFrenet object fits a smooth, piecewise, continuous curve to a set of waypoints given as [x y] or [x y theta]. After fitting, points along the curve, the path points are expressed as [x y theta kappa dkappa s], where:

- x y and theta— SE(2) state expressed in global coordinates, with x and y in meters and theta in radians
- kappa Curvature, or inverse of the radius, in meters
- dkappa Derivative of curvature with respect to arc length in meters per second
- s Arc length, or distance along path from path origin, in meters



Using this object, convert trajectories between global and Frenet coordinate systems, interpolate states along the path based on arc length, and query the closest point on a path from a global state.

The object expresses Frenet states as a vector of form [S dS ddS L dL ddL], where S is the arc length and L is the perpendicular deviation from the direction of the reference path. Derivatives of S are relative to time. Derivatives of L are relative to the arc length, S.



Frenet States: [s δs δ²s L δL δ²L]

Creation

Syntax

```
refPathObj = referencePathFrenet(waypoints)
refPathObj = referencePathFrenet(
waypoints,'DiscretizationDistance',discretionDist)
```

Description

refPathObj = referencePathFrenet(waypoints) fits a piecewise, continuous set of curves to the specified waypoints. The waypoints argument sets the Waypoints property.

```
refPathObj = referencePathFrenet(
waypoints, 'DiscretizationDistance', discretionDist) fits a piecewise, continuous set of
curves to waypoints using the specified distance between interpolated path points. The
discretionDist argument sets the DiscretizationDistance property.
```

Properties

DiscretizationDistance — Arc length between interpolated path points

0.05 (default) | positive scalar

Arc length between interpolated path points, specified as a positive scalar in meters. The object uses interpolated path points to accelerate performance of the transformation functions frenet2global and global2frenet. A smaller discretization distance can improve accuracy at the expense of memory and computational efficiency.

Data Types: single | double

Waypoints — Presampled points along path

P-by-2 numeric matrix | *P*-by-3 numeric matrix

Presampled points along the path, specified as a P-by-2 matrix with rows of form [x y] or P-by-3 matrix with rows of form [x y theta]. Specify x and y in meters and theta in radians. P is the number of presampled points, and must be greater than or equal to two

Data Types: single | double

Object Functions

closestPoint Find closest point on reference path to global point

frenet2global Convert Frenet states to global states global2frenet Convert global states to Frenet states

interpolate Interpolate reference path at provided arc lengths

show Display reference path in figure

Examples

Generate Alternative Trajectories for Reference Path

Generate alternative trajectories for a reference path using Frenet coordinates. Specify different initial and terminal states for your trajectories. Tune your states based on the generated trajectories.

Generate a reference path from a set of waypoints. Create a trajectoryGeneratorFrenet object from the reference path.

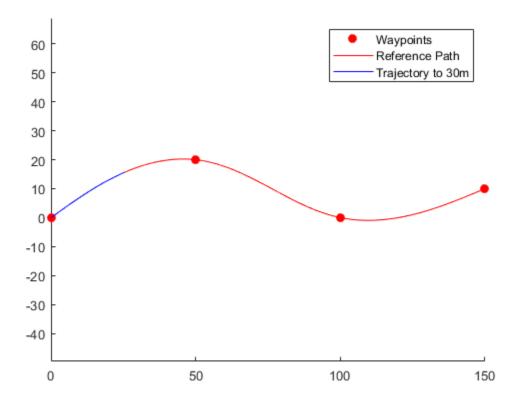
```
waypoints = [0 0; ...
50 20; ...
100 0; ...
150 10];
refPath = referencePathFrenet(waypoints);
connector = trajectoryGeneratorFrenet(refPath);
```

Generate a five-second trajectory between the path origin and a point 30 m down the path as Frenet states.

```
initState = [0 0 0 0 0 0]; % [S ds ddS L dL ddL]
termState = [30 0 0 0 0 0]; % [S ds ddS L dL ddL]
[~,trajGlobal] = connect(connector,initState,termState,5);
```

Display the trajectory in global coordinates.

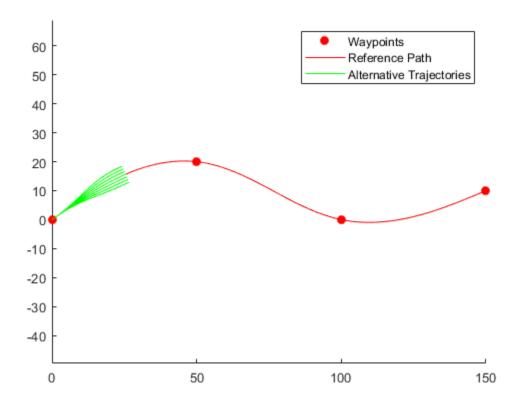
```
show(refPath);
hold on
axis equal
plot(trajGlobal.Trajectory(:,1),trajGlobal.Trajectory(:,2),'b')
legend(["Waypoints","Reference Path","Trajectory to 30m"])
```



Create a matrix of terminal states with lateral deviations between -3 m and 3 m. Generate trajectories that cover the same arc length in 10 seconds, but deviate laterally from the reference path. Display the new alternative paths.

```
termStateDeviated = termState + ([-3:3]' * [0 0 0 1 0 0]);
[~,trajGlobal] = connect(connector,initState,termStateDeviated,5);

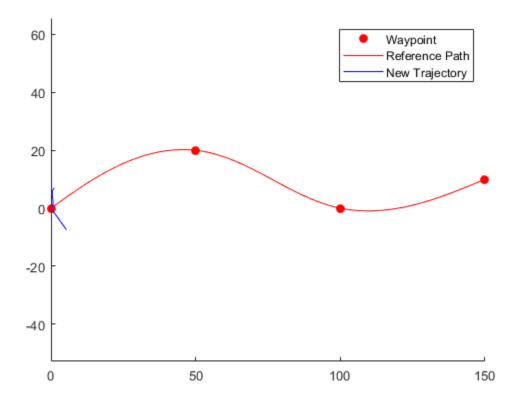
clf
show(refPath);
hold on
axis equal
for i = 1:length(trajGlobal)
    plot(trajGlobal(i).Trajectory(:,1),trajGlobal(i).Trajectory(:,2),'g')
end
legend(["Waypoints","Reference Path","Alternative Trajectories"])
hold off
```



Specify a new terminal state to generate a new trajectory. This trajectory is not desirable because it requires reverse motion to achieve a lateral velocity of 10 m/s.

```
newTermState = [5 10 0 5 0 0];
[~,newTrajGlobal] = connect(connector,initState,newTermState,3);

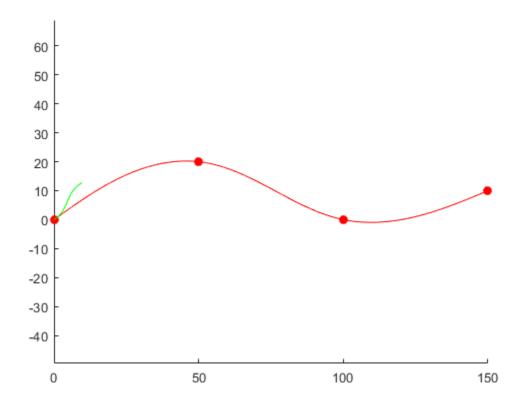
clf
show(refPath);
hold on
axis equal
plot(newTrajGlobal.Trajectory(:,1),newTrajGlobal.Trajectory(:,2),'b');
legend(["Waypoint","Reference Path","New Trajectory"])
hold off
```



Relax the restriction on the longitudinal state by specifying an arc length of NaN. Generate and display the trajectory again. The new position shows a good alternative trajectory that deviates off the reference path.

```
relaxedTermState = [NaN 10 0 5 0 0];
[~,trajGlobalRelaxed] = connect(connector,initState,relaxedTermState,3);

clf
show(refPath);
hold on
axis equal
plot(trajGlobalRelaxed.Trajectory(:,1),trajGlobalRelaxed.Trajectory(:,2),'g');
hold off
```



Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

Objects

navPath | trajectoryGeneratorFrenet

Functions

closestPoint | frenet2global | global2frenet | interpolate | show

Topics

"Highway Trajectory Planning Using Frenet Reference Path"

Introduced in R2020b

closestPoint

Find closest point on reference path to global point

Syntax

pathPoints = closestPoint(refPath,points)

Description

pathPoints = closestPoint(refPath, points) finds the closest point on the reference path to each of the specified (x,y)-positions points.

Input Arguments

refPath — Reference path

referencePathFrenet object

Reference path, specified as a referencePathFrenet object.

points — Global points

P-by-2 numeric matrix

Global points, specified as a P-by-2 numeric matrix with rows of the form [x y]. P is the number of points. Positions are in meters.

Output Arguments

pathPoints — Closest points on reference path

N-by-6 numeric matrix

Closest points on the reference path, returned as an N-by-6 numeric matrix with rows of form [x y theta kappa dkappa s], where:

- x y and theta— SE(2) state expressed in global coordinates, with x and y in meters and theta in radians
- kappa Curvature, or inverse of the radius, in meters
- dkappa Derivative of curvature with respect to arc length in meters per second
- s Arc length, or distance along path from path origin, in meters

N is the number of points sampled along the reference path.

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

Objects

navPath | referencePathFrenet | trajectoryGeneratorFrenet

Functions

frenet2global | global2frenet | interpolate | show

Topics

"Highway Trajectory Planning Using Frenet Reference Path"

Introduced in R2020b

frenet2global

Convert Frenet states to global states

Syntax

globalState = frenet2global(refPath, frenetState)

Description

globalState = frenet2global(refPath, frenetState) converts Frenet trajectory states to
global states.

Input Arguments

refPath - Reference path

referencePathFrenet object

Reference path, specified as a referencePathFrenet object.

frenetState — Trajectory in Frenet coordinate frame

P-by-6 numeric matrix

Trajectory in the Frenet coordinate frame, specified as a *P*-by-6 numeric matrix with rows of form [S dS ddS L dL ddL], where S is the arc length and L is the perpendicular deviation from the direction of the reference path. Derivatives of S are relative to time. Derivatives of L are relative to the arc length, S. *P* is the number of Frenet states specified.

Output Arguments

globalState — Trajectory in global coordinate frame

P-by-6 numeric matrix

Trajectories in the global coordinate frame, returned as a P-by-6 numeric matrix with rows of form [x y theta kappa speed accel], where:

- x y and theta -- SE(2) state expressed in global coordinates, with x and y in meters and theta in radians
- kappa -- Curvature, or inverse of the radius, in meters
- speed -- Speed in the theta direction in m/s
- accel -- Acceleration in the theta direction in m/s²

P is the number of Frenet trajectories converted to global trajectories.

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

Objects

navPath | referencePathFrenet | trajectoryGeneratorFrenet

Functions

closestPoint|global2frenet|interpolate|show

Topics

"Highway Trajectory Planning Using Frenet Reference Path"

Introduced in R2020b

global2frenet

Convert global states to Frenet states

Syntax

frenetState = global2frenet(refPath,globalState)

Description

frenetState = global2frenet(refPath,globalState) converts global states to Frenet
trajectory states.

Input Arguments

refPath - Reference path

referencePathFrenet object

Reference path, specified as a referencePathFrenet object.

globalState — Trajectory in global coordinate frame

P-by-6 numeric matrix

Trajectories in the global coordinate frame, specified as a P-by-6 numeric matrix with rows of form [x y theta kappa speed accel], where:

- x y and theta -- SE(2) state expressed in global coordinates, with x and y in meters and theta
 in radians
- kappa -- Curvature, or inverse of the radius, in meters
- speed -- Speed in the theta direction in m/s
- accel -- Acceleration in the theta direction in m/s²

P is the number of Frenet trajectories converted to global trajectories.

Output Arguments

frenetState — Trajectory in Frenet coordinate frame

P-by-6 numeric matrix

Trajectory in the Frenet coordinate frame, returned as a *P*-by-6 numeric matrix with rows of form [S dS ddS L dL ddL], where S is the arc length and L is the perpendicular deviation from the direction of the reference path. Derivatives of S are relative to time. Derivatives of L are relative to the arc length, S. *P* is the number of Frenet states specified.

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

Objects

navPath | referencePathFrenet | trajectoryGeneratorFrenet

Functions

closestPoint | frenet2global | global2frenet | interpolate | show

Topics

"Highway Trajectory Planning Using Frenet Reference Path"

Introduced in R2020b

interpolate

Interpolate reference path at provided arc lengths

Syntax

pathPoints = interpolate(refPath,arclengths)

Description

pathPoints = interpolate(refPath, arclengths) interpolates the reference path at the provided arc lengths and returns the interpolated points on the path in global coordinates.

Input Arguments

refPath — Reference path

referencePathFrenet object

Reference path, specified as a referencePathFrenet object.

arclengths — Distances along reference path

N-element vector

Distances along the reference path, specified as an N-element vector. N is the number of arc lengths at which to sample points. Each distance is in meters.

Output Arguments

pathPoints — Points on reference path

N-by-6 numeric matrix

Points on the reference path, returned as an N-by-6 numeric matrix with rows of form [x y theta kappa dkappa s], where:

- x y and theta— SE(2) state expressed in global coordinates, with x and y in meters and theta in radians
- kappa Curvature, or inverse of the radius, in meters
- dkappa Derivative of curvature with respect to arc length in meters per second
- s Arc length, or distance along path from path origin, in meters

N is the number of points sampled along the reference path.

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

Objects

navPath | referencePathFrenet | trajectoryGeneratorFrenet

Functions

closestPoint|frenet2global|global2frenet|show

Topics

"Highway Trajectory Planning Using Frenet Reference Path"

Introduced in R2020b

show

Display reference path in figure

Syntax

```
show(refPath)
show(refPath,'Parent',parentAx)
ax = show(____)
```

Description

show(refPath) displays the reference path and its lateral states in the current figure.

show(refPath, 'Parent', parentAx) displays the reference path on the specified axes. parentAx is specified as an Axes handle.

ax = show(____) displays the reference path using any of the previous input combinations and returns the axes handle on which the reference path is plotted.

Input Arguments

refPath - Reference path

referencePathFrenet object

Reference path, specified as a referencePathFrenet object.

Output Arguments

ax — Axes on which the reference path is plotted

Axes handle

Axes on which the reference path is plotted, returned as an Axes handle.

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

Objects

navPath | referencePathFrenet | trajectoryGeneratorFrenet

Functions

closestPoint | frenet2global | global2frenet | interpolate

Topics

"Highway Trajectory Planning Using Frenet Reference Path"

Introduced in R2020b

resamplingPolicyPF

Create resampling policy object with resampling settings

Description

The resamplingPolicyPF object stores settings for when resampling should occur when using a particle filter for state estimation. The object contains the method that triggers resampling and the relevant threshold for this resampling. Use this object as the ResamplingPolicy property of the stateEstimatorPF object.

Creation

Syntax

policy = resamplingPolicyPF

Description

policy = resamplingPolicyPF creates a resamplingPolicyPF object policy, which contains
properties to be modified to control when resampling should be triggered. Use this object as the
ResamplingPolicy property of the stateEstimatorPF object.

Properties

TriggerMethod — Method for determining if resampling should occur

'ratio' (default) | character vector

Method for determining if resampling should occur, specified as a character vector. Possible choices are 'ratio' and 'interval'. The 'interval' method triggers resampling at regular intervals of operating the particle filter. The 'ratio' method triggers resampling based on the ratio of effective total particles.

SamplingInterval — Fixed interval between resampling

1 (default) | scalar

Fixed interval between resampling, specified as a scalar. This interval determines during which correction steps the resampling is executed. For example, a value of 2 means the resampling is executed every second correction step. A value of inf means that resampling is never executed.

This property only applies with the TriggerMethod is set to 'interval'.

MinEffectiveParticleRatio — Minimum desired ratio of effective to total particles 0.5 (default) | scalar

Minimum desired ratio of effective to total particles, specified as a scalar. The effective number of particles is a measure of how well the current set of particles approximates the posterior distribution. A lower effective particle ratio means less particles are contributing to the estimation and resampling

might be required. If the ratio of effective particles to total particles falls below the MinEffectiveParticleRatio, a resampling step is triggered.

See Also

correct|stateEstimatorPF

Introduced in R2019b

SkyPlotChart Properties

Sky plot chart appearance and behavior

Description

The SkyPlotChart properties control the appearance of a sky plot chart generated using the skyplot function. To modify the chart appearance, use dot notation on the SkyPlotChart object:

```
h = skyplot;
h.AzimuthData = [45 120 295];
h.ElevationData = [10 45 60];
h.Labels = ["G1" "G4" "G11"];
```

Properties

Sky Plot Properties

AzimuthData — Azimuth angles for visible satellite positions

n-element vector of angles

Azimuth angles for visible satellite positions, specified as an n-element vector of angles. n is the number of visible satellite positions in the plot. Angles are measured in degrees, clockwise-positive from the North direction.

```
Example: [25 45 182 356]
Data Types: double
```

ElevationData — Elevation angles for visible satellite positions

n-element vector of angles

Elevation angles for visible satellite positions, specified as an n-element vector of angles. n is the number of visible satellite positions in the plot. Angles are measured from the horizon line with 90 degrees being directly up.

```
Example: [45 90 27 74]
Data Types: double
```

LabelData — Labels for visible satellite positions

n-element string array

Labels for visible satellite positions, specified as an n-element string array. n is the number of visible satellite positions in the plot.

```
Example: ["G1" "G11" "G7" "G3"]
Data Types: string
```

GroupData — Group for each satellite position

```
categorical array
```

Group for each satellite position, specified as a categorical array. Each group has a different color label defined by the ColorOrder property.

Example: [GPS GPS Galileo Galileo]

Data Types: double

ColorOrder — Color order

seven predefined colors (default) | three-column matrix of RGB triplets

Color order, specified as a three-column matrix of RGB triplets. This property defines the palette of colors MATLAB uses to create plot objects such as Line, Scatter, and Bar objects. Each row of the array is an RGB triplet. An RGB triplet is a three-element vector whose elements specify the intensities of the red, green, and blue components of a color. The intensities must be in the range [0, 1]. This table lists the default colors.

Colors	Color0rder Matrix
	[0 0.4470 0.7410 0.8500 0.3250 0.0980 0.9290 0.6940 0.1250 0.4940 0.1840 0.5560 0.4660 0.6740 0.1880 0.3010 0.7450 0.9330 0.6350 0.0780 0.1840]

MATLAB assigns colors to objects according to their order of creation. For example, when plotting lines, the first line uses the first color, the second line uses the second color, and so on. If there are more lines than colors, then the cycle repeats.

You can also set the color order using the colororder function.

Label Properties

LabelFontSize — Font size of labels

scalar numeric value

Font size of labels, specified as a scalar numeric value. The default font depends on the specific operating system and locale.

```
Example: h = skyplot(__,'LabelFontSize',12)
Example: h.LabelFontSize = 12
```

LabelFontSizeMode — Selection mode for font size of labels

```
'auto' (default) | 'manual'
```

Selection mode for the font size of labels, specified as one of these values:

- 'auto' Font size specified by MATLAB. If you resize the axes to be smaller than the default size, the font size can scale down to improve readability and layout.
- 'manual' Font size specified manually. MATLAB does not scale the font size as the axes size changes. To specify the font size, set the LabelFontSize property.

Chart Properties

HandleVisibility — Visibility of object handle

```
'on' (default) | 'off' | 'callback'
```

Visibility of the SkyPlotChart object handle in the Children property of the parent, specified as one of these values:

- 'on' Object handle is always visible.
- 'off' Object handle is invisible at all times. This option is useful for preventing unintended changes to the UI by another function. To temporarily hide the handle during the execution of that function, set the HandleVisibility to 'off'.
- 'callback' Object handle is visible from within callbacks or functions invoked by callbacks, but not from within functions invoked from the command line. This option blocks access to the object at the command line, but allows callback functions to access it.

If the object is not listed in the Children property of the parent, then functions that obtain object handles by searching the object hierarchy or querying handle properties cannot return it. This includes get, findobj, gca, gcf, gco, newplot, cla, clf, and close.

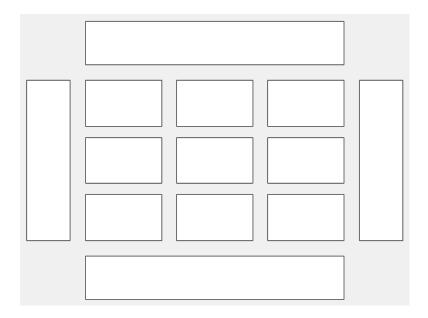
Hidden object handles are still valid. Set the root ShowHiddenHandles property to 'on' to list all object handles, regardless of their HandleVisibility property setting.

Layout — Layout options

empty LayoutOptions array (default) | TiledChartLayoutOptions object | GridLayoutOptions
object

Layout options, specified as a TiledChartLayoutOptions or GridLayoutOptions object. This property is useful when the chart is either in a tiled chart layout or a grid layout.

To position the chart within the grid of a tiled chart layout, set the Tile and TileSpan properties on the TiledChartLayoutOptions object. For example, consider a 3-by-3 tiled chart layout. The layout has a grid of tiles in the center, and four tiles along the outer edges. In practice, the grid is invisible and the outer tiles do not take up space until you populate them with axes or charts.



This code places the chart c in the third tile of the grid..

c.Layout.Tile = 3;

To make the chart span multiple tiles, specify the TileSpan property as a two-element vector. For example, this chart spans 2 rows and 3 columns of tiles.

```
c.Layout.TileSpan = [2 3];
```

To place the chart in one of the surrounding tiles, specify the Tile property as 'north', 'south', 'east', or 'west'. For example, setting the value to 'east' places the chart in the tile to the right of the grid.

```
c.Layout.Tile = 'east';
```

To place the chart into a layout within an app, specify this property as a GridLayoutOptions object. For more information about working with grid layouts in apps, see uigridlayout.

If the chart is not a child of either a tiled chart layout or a grid layout (for example, if it is a child of a figure or panel) then this property is empty and has no effect.

Parent — **Parent container**

Figure object | Panel object | Tab object | TiledChartLayout object | GridLayout object

Parent container, specified as a Figure, Panel, Tab, TiledChartLayout, or GridLayout object.

Marker Properties

MarkerEdgeAlpha — Marker edge transparency

```
1 (default) | scalar in range [0,1] | 'flat'
```

Marker edge transparency, specified as a scalar in the range [0,1] or 'flat'. A value of 1 is opaque and 0 is completely transparent. Values between 0 and 1 are semitransparent.

To set the edge transparency to a different value for each point in the plot, set the AlphaData property to a vector the same size as the XData property, and set the MarkerEdgeAlpha property to 'flat'.

MarkerEdgeColor — Marker outline color

```
'flat' (default) | 'auto' | RGB triplet | hexadecimal color code | 'r' | 'g' | 'b' | ...
```

Marker outline color, specified as 'auto', an RGB triplet, a hexadecimal color code, a color name, or a short name. The value of 'auto' uses the same color as the Color property.

For a custom color, specify an RGB triplet or a hexadecimal color code.

- An RGB triplet is a three-element row vector whose elements specify the intensities of the red, green, and blue components of the color. The intensities must be in the range [0,1]. For example, [0.4 0.6 0.7].
- A hexadecimal color code is a character vector or a string scalar that starts with a hash symbol (#) followed by three or six hexadecimal digits, which can range from 0 to F. The values are not case sensitive. Thus, the color codes '#FF8800', '#ff8800', '#F80', and '#f80' are equivalent.

Alternatively, you can specify some common colors by name. This table lists the named color options, the equivalent RGB triplets, and the hexadecimal color codes.

Color Name	Short Name	RGB Triplet	Hexadecimal Color Code	Appearance
'red'	'r'	[1 0 0]	'#FF0000'	
'green'	'g'	[0 1 0]	'#00FF00'	
'blue'	'b'	[0 0 1]	'#0000FF'	
'cyan'	'c'	[0 1 1]	'#00FFFF'	
'magenta'	'm'	[1 0 1]	'#FF00FF'	
'yellow'	'y'	[1 1 0]	'#FFFF00'	
'black'	'k'	[0 0 0]	'#000000'	
'white'	'w'	[1 1 1]	'#FFFFFF'	
'none'	Not applicable	Not applicable	Not applicable	No color

This table shows the RGB triplets and hexadecimal color codes for the default colors MATLAB uses in many types of plots.

RGB Triplet	Hexadecimal Color Code	Appearance
[0 0.4470 0.7410]	'#0072BD'	
[0.8500 0.3250 0.0980]	'#D95319'	
[0.9290 0.6940 0.1250]	'#EDB120'	
[0.4940 0.1840 0.5560]	'#7E2F8E'	
[0.4660 0.6740 0.1880]	'#77AC30'	
[0.3010 0.7450 0.9330]	'#4DBEEE'	
[0.6350 0.0780 0.1840]	'#A2142F'	

MarkerFaceAlpha — Marker face transparency

0.6 (default) | scalar in range [0,1] | 'flat'

Marker face transparency, specified as a scalar in the range [0,1] or 'flat'. A value of 1 is opaque and 0 is completely transparent. Values between 0 and 1 are partially transparent.

To set the marker face transparency to a different value for each point, set the AlphaData property to a vector the same size as the XData property, and set the MarkerFaceAlpha property to 'flat'.

MarkerFaceColor — Marker fill color

```
'flat' (default) | 'auto' | 'none' | RGB triplet | hexadecimal color code | 'r' | 'g' | 'b' | ...
```

Marker fill color, specified as 'flat', 'auto', an RGB triplet, a hexadecimal color code, a color name, or a short name. The 'flat' option uses the CData values. The 'auto' option uses the same color as the Color property for the axes.

For a custom color, specify an RGB triplet or a hexadecimal color code.

• An RGB triplet is a three-element row vector whose elements specify the intensities of the red, green, and blue components of the color. The intensities must be in the range [0,1]; for example, [0.4 0.6 0.7].

• A hexadecimal color code is a character vector or a string scalar that starts with a hash symbol (#) followed by three or six hexadecimal digits, which can range from 0 to F. The values are not case sensitive. Thus, the color codes '#FF8800', '#ff8800', '#F80', and '#f80' are equivalent.

Alternatively, you can specify some common colors by name. This table lists the named color options, the equivalent RGB triplets, and hexadecimal color codes.

Color Name	Short Name	RGB Triplet	Hexadecimal Color Code	Appearance
'red'	'r'	[1 0 0]	'#FF0000'	
'green'	'g'	[0 1 0]	'#00FF00'	
'blue'	'b'	[0 0 1]	'#0000FF'	
'cyan'	'c'	[0 1 1]	'#00FFFF'	
'magenta'	'm'	[1 0 1]	'#FF00FF'	
'yellow'	'y'	[1 1 0]	'#FFFF00'	
'black'	'k'	[0 0 0]	'#000000'	
'white'	'w'	[1 1 1]	'#FFFFFF'	
'none'	Not applicable	Not applicable	Not applicable	No color

Here are the RGB triplets and hexadecimal color codes for the default colors MATLAB uses in many types of plots.

RGB Triplet	Hexadecimal Color Code	Appearance
[0 0.4470 0.7410]	'#0072BD'	
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[0.9290 0.6940 0.1250]	'#EDB120'	
[0.4940 0.1840 0.5560]	'#7E2F8E'	
[0.4660 0.6740 0.1880]	'#77AC30'	
[0.3010 0.7450 0.9330]	'#4DBEEE'	
[0.6350 0.0780 0.1840]	'#A2142F'	

Example: [0.3 0.2 0.1]

Example: 'green'
Example: '#D2F9A7'

MarkerSizeData — Marker size

100 (default) | positive scalar | vector of positive values

Marker size, specified as a positive scalar or vector of positive values in points, where one point = 1/72 of an inch. If specified as a vector, the vector must be of the same length as AzimuthData.

Position

PositionConstraint — Position to hold constant

'outerposition'|'innerposition'

Position property to hold constant when adding, removing, or changing decorations, specified as one of the following values:

- 'outerposition' The OuterPosition property remains constant when you add, remove, or change decorations such as a title or an axis label. If any positional adjustments are needed, MATLAB adjusts the InnerPosition property.
- 'innerposition' The InnerPosition property remains constant when you add, remove, or change decorations such as a title or an axis label. If any positional adjustments are needed, MATLAB adjusts the OuterPosition property.

Note Setting this property has no effect when the parent container is a TiledChartLayout.

OuterPosition — Outer size and location

[0 0 1 1] (default) | four-element vector

Outer size and location of the skyplot within the parent container (typically a figure, panel, or tab), specified as a four-element vector of the form [left bottom width height]. The outer position includes the colorbar, title, and axis labels.

- The left and bottom elements define the distance from the lower-left corner of the container to the lower-left corner of the skyplot.
- The width and height elements are the skyplot dimensions, which include the skyplot cells, plus
 a margin for the surrounding text and colorbar.

The default value of $[0\ 0\ 1\ 1]$ covers the whole interior of the container. The units are normalized relative to the size of the container. To change the units, set the Units property.

Note Setting this property has no effect when the parent container is a TiledChartLayout.

InnerPosition — Inner size and location

[0.1300 0.1100 0.7750 0.8114] (default) | four-element vector

Inner size and location of the skyplot within the parent container (typically a figure, panel, or tab), specified as a four-element vector of the form [left bottom width height]. The inner position does not include the colorbar, title, or axis labels.

- The left and bottom elements define the distance from the lower-left corner of the container to the lower-left corner of the skyplot.
- The width and height elements are the skyplot dimensions, which include only the skyplot cells.

Note Setting this property has no effect when the parent container is a TiledChartLayout.

Position — Inner size and location

four-element vector

Inner size and location of the skyplot within the parent container (typically a figure, panel, or tab), specified as a four-element vector of the form [left bottom width height]. This property is equivalent to the InnerPosition property.

Note Setting this property has no effect when the parent container is a TiledChartLayout.

Units — Position units

'normalized' (default) | 'inches' | 'centimeters' | 'points' | 'pixels' | 'characters'

Position units, specified as one of these values.

Units	Description
'normalized' (default)	Normalized with respect to the container, which is typically the figure or a panel. The lower left corner of the container maps to $(0,0)$, and the upper right corner maps to $(1,1)$.
'inches'	Inches.
'centimeters'	Centimeters.
'characters'	Based on the default uicontrol font of the graphics root object: • Character width = width of letter x.
	Character height = distance between the baselines of two lines of text.
'points'	Typography points. One point equals 1/72 inch.
'pixels'	Pixels. Starting in R2015b, distances in pixels are independent of your system resolution on Windows® and Macintosh systems: On Windows systems, a pixel is 1/96th of an inch. On Macintosh systems, a pixel is 1/72nd of an inch. On Linux® systems, the size of a pixel is determined by your system resolution.

When specifying the units as a name-value argument during object creation, you must set the Units property before specifying the properties that you want to use these units, such as OuterPosition.

Visible — State of visibility

'on' (default) | on/off logical value

State of visibility, specified as 'on' or 'off', or as numeric or logical 1 (true) or 0 (false). A value of 'on' is equivalent to true, and 'off' is equivalent to false. Thus, you can use the value of this property as a logical value. The value is stored as an on/off logical value of type matlab.lang.OnOffSwitchState.

- 'on' Display the skyplot.
- ' off' Hide the skyplot without deleting it. You can still access the properties of an invisible SkyPlotChart object.

See Also

Functions polarscatter | skyplot

Objects gnssSensor|nmeaParser

Introduced in R2021a

stateEstimatorPF

Create particle filter state estimator

Description

The stateEstimatorPF object is a recursive, Bayesian state estimator that uses discrete particles to approximate the posterior distribution of the estimated state.

The particle filter algorithm computes the state estimate recursively and involves two steps: prediction and correction. The prediction step uses the previous state to predict the current state based on a given system model. The correction step uses the current sensor measurement to correct the state estimate. The algorithm periodically redistributes, or resamples, the particles in the state space to match the posterior distribution of the estimated state.

The estimated state consists of state variables. Each particle represents a discrete state hypothesis of these state variables. The set of all particles is used to help determine the final state estimate.

You can apply the particle filter to arbitrary nonlinear system models. Process and measurement noise can follow arbitrary non-Gaussian distributions.

For more information on the particle filter workflow and setting specific parameters, see:

- "Particle Filter Workflow"
- "Particle Filter Parameters"

Creation

Syntax

pf = stateEstimatorPF

Description

pf = stateEstimatorPF creates an object that enables the state estimation for a simple system
with three state variables. Use the initialize method to initialize the particles with a known mean
and covariance or uniformly distributed particles within defined bounds. To customize the particle
filter's system and measurement models, modify the StateTransitionFcn and
MeasurementLikelihoodFcn properties.

After you create the object, use initialize to initialize the NumStateVariables and NumParticles properties. The initialize function sets these two properties based on your inputs.

Properties

NumStateVariables — Number of state variables

3 (default) | scalar

This property is read-only.

Number of state variables, specified as a scalar. This property is set based on the inputs to the initialize method. The number of states is implicit based on the specified matrices for initial state and covariance.

NumParticles — Number of particles used in the filter

1000 (default) | scalar

This property is read-only.

Number of particles using in the filter, specified as a scalar. You can specify this property only by calling the initialize method.

StateTransitionFcn — Callback function for determining the state transition between particle filter steps

function handle

Callback function for determining the state transition between particle filter steps, specified as a function handle. The state transition function evolves the system state for each particle. The function signature is:

function predictParticles = stateTransitionFcn(pf,prevParticles,varargin)

The callback function accepts at least two input arguments: the stateEstimatorPF object, pf, and the particles at the previous time step, prevParticles. These specified particles are the predictParticles returned from the previous call of the object. predictParticles and prevParticles are the same size: NumParticles-by-NumStateVariables.

You can also use varargin to pass in a variable number of arguments from the predict function. When you call:

predict(pf,arg1,arg2)

MATLAB essentially calls stateTranstionFcn as:

stateTransitionFcn(pf,prevParticles,arg1,arg2)

MeasurementLikelihoodFcn — Callback function calculating the likelihood of sensor measurements

function handle

Callback function calculating the likelihood of sensor measurements, specified as a function handle. Once a sensor measurement is available, this callback function calculates the likelihood that the measurement is consistent with the state hypothesis of each particle. You must implement this function based on your measurement model. The function signature is:

function likelihood = measurementLikelihoodFcn(PF,predictParticles,measurement,varargin)

The callback function accepts at least three input arguments:

- 1 pf The associated stateEstimatorPF object
- predictParticles The particles that represent the predicted system state at the current time step as an array of size NumParticles-by-NumStateVariables
- **3** measurement The state measurement at the current time step

You can also use varargin to pass in a variable number of arguments. These arguments are passed by the correct function. When you call:

```
correct(pf,measurement,arg1,arg2)
```

MATLAB essentially calls measurementLikelihoodFcn as:

```
measurementLikelihoodFcn(pf,predictParticles,measurement,arg1,arg2)
```

The callback needs to return exactly one output, likelihood, which is the likelihood of the given measurement for each particle state hypothesis.

IsStateVariableCircular — **Indicator** if state variables have a circular distribution [0 0 0] (default) | logical array

Indicator if state variables have a circular distribution, specified as a logical array. Circular (or angular) distributions use a probability density function with a range of [-pi,pi]. If the object has multiple state variables, then IsStateVariableCircular is a row vector. Each vector element indicates if the associated state variable is circular. If the object has only one state variable, then IsStateVariableCircular is a scalar.

ResamplingPolicy — **Policy settings that determine when to trigger resampling** object

Policy settings that determine when to trigger resampling, specified as an object. You can trigger resampling either at fixed intervals, or you can trigger it dynamically, based on the number of effective particles. See resamplingPolicyPF for more information.

ResamplingMethod — Method used for particle resampling

```
'multinomial' (default) | 'residual' | 'stratified' | 'systematic'
```

Method used for particle resampling, specified as 'multinomial', 'residual', 'stratified', and 'systematic'.

StateEstimationMethod — Method used for state estimation

```
'mean' (default) | 'maxweight'
```

Method used for state estimation, specified as 'mean' and 'maxweight'.

Particles — Array of particle values

NumParticles-by-NumStateVariables matrix

Array of particle values, specified as a NumParticles-by-NumStateVariables matrix. Each row corresponds to the state hypothesis of a single particle.

Weights — Particle weights

NumParticles-by-1 vector

Particle weights, specified as a NumParticles-by-1 vector. Each weight is associated with the particle in the same row in the Particles property.

State — Best state estimate

vector

This property is read-only.

Best state estimate, returned as a vector with length NumStateVariables. The estimate is extracted based on the StateEstimationMethod property.

State Covariance — Corrected system covariance

```
N-by-N matrix | []
```

This property is read-only.

Corrected system variance, returned as an N-by-N matrix, where N is equal to the NumStateVariables property. The corrected state is calculated based on the StateEstimationMethod property and the MeasurementLikelihoodFcn. If you specify a state estimate method that does not support covariance, then the property is set to [].

Object Functions

initialize Initialize the state of the particle filter

predict Predict state of robot in next time step

correct Adjust state estimate based on sensor measurement

Examples

Particle Filter Prediction and Correction

Create a stateEstimatorPF object, and execute a prediction and correction step for state estimation. The particle filter gives a predicted state estimate based on the return value of StateTransitionFcn. It then corrects the state based on a given measurement and the return value of MeasurementLikelihoodFcn.

Create a particle filter with the default three states.

Specify the mean state estimation method and systematic resampling method.

```
pf.StateEstimationMethod = 'mean';
pf.ResamplingMethod = 'systematic';
```

Initialize the particle filter at state [4 1 9] with unit covariance (eye(3)). Use 5000 particles.

```
initialize(pf,5000,[4 1 9],eye(3));
```

Assuming a measurement [4.2 0.9 9], run one predict and one correct step.

```
[statePredicted,stateCov] = predict(pf);
[stateCorrected,stateCov] = correct(pf,[4.2 0.9 9]);
```

Get the best state estimate based on the StateEstimationMethod algorithm.

```
stateEst = getStateEstimate(pf)

stateEst = 1 \times 3

4.1562 0.9185 9.0202
```

Estimate Robot Position in a Loop Using Particle Filter

Use the stateEstimatorPF object to track a robot as it moves in a 2-D space. The measured position has random noise added. Using predict and correct, track the robot based on the measurement and on an assumed motion model.

Initialize the particle filter and specify the default state transition function, the measurement likelihood function, and the resampling policy.

```
pf = stateEstimatorPF;
pf.StateEstimationMethod = 'mean';
pf.ResamplingMethod = 'systematic';
```

Sample 1000 particles with an initial position of [0 0] and unit covariance.

```
initialize(pf,1000,[0 0],eye(2));
```

Prior to estimation, define a sine wave path for the dot to follow. Create an array to store the predicted and estimated position. Define the amplitude of noise.

```
t = 0:0.1:4*pi;
dot = [t; sin(t)]';
robotPred = zeros(length(t),2);
robotCorrected = zeros(length(t),2);
noise = 0.1;
```

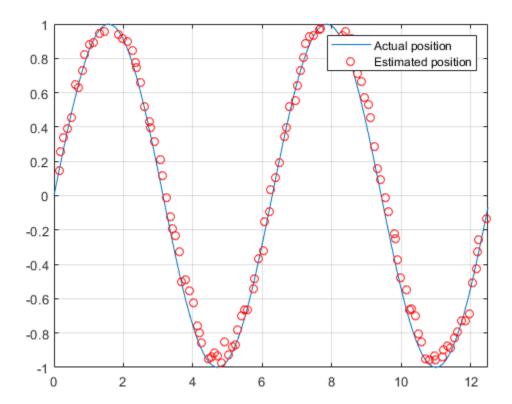
Begin the loop for predicting and correcting the estimated position based on measurements. The resampling of particles occurs based on the Resampling Policy property. The robot moves based on a sine wave function with random noise added to the measurement.

```
for i = 1:length(t)
  % Predict next position. Resample particles if necessary.
  [robotPred(i,:),robotCov] = predict(pf);
  % Generate dot measurement with random noise. This is
  % equivalent to the observation step.
  measurement(i,:) = dot(i,:) + noise*(rand([1 2])-noise/2);
  % Correct position based on the given measurement to get best estimation.
```

```
% Actual dot position is not used. Store corrected position in data array.
[robotCorrected(i,:),robotCov] = correct(pf,measurement(i,:));
end
```

Plot the actual path versus the estimated position. Actual results may vary due to the randomness of particle distributions.

```
plot(dot(:,1),dot(:,2),robotCorrected(:,1),robotCorrected(:,2),'or')
xlim([0 t(end)])
ylim([-1 1])
legend('Actual position','Estimated position')
grid on
```



The figure shows how close the estimate state matches the actual position of the robot. Try tuning the number of particles or specifying a different initial position and covariance to see how it affects tracking over time.

Compatibility Considerations

stateEstimatorPF was renamed

Behavior change in future release

The stateEstimatorPF object was renamed from robotics.ParticleFilter. Use stateEstimatorPF for all object creation.

References

- [1] Arulampalam, M.S., S. Maskell, N. Gordon, and T. Clapp. "A Tutorial on Particle Filters for Online Nonlinear/Non-Gaussian Bayesian Tracking." *IEEE Transactions on Signal Processing*. Vol. 50, No. 2, Feb 2002, pp. 174-188.
- [2] Chen, Z. "Bayesian Filtering: From Kalman Filters to Particle Filters, and Beyond." *Statistics*. Vol. 182, No. 1, 2003, pp. 1-69.

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

correct | getStateEstimate | initialize | predict | resamplingPolicyPF

Topics

"Track a Car-Like Robot Using Particle Filter" (Robotics System Toolbox)

"Particle Filter Parameters"

"Particle Filter Workflow"

Introduced in R2016a

copy

Create copy of particle filter

Syntax

b = copy(a)

Description

b = copy(a) copies each element in the array of handles, a, to the new array of handles, b.

The copy method does not copy dependent properties. MATLAB does not call copy recursively on any handles contained in property values. MATLAB also does not call the class constructor or property-set methods during the copy operation.

Input Arguments

a — Object array

handle

Object array, specified as a handle.

Output Arguments

b — Object array containing copies of the objects in a

handle

Object array containing copies of the object in **a**, specified as a handle.

b has the same number of elements and is the same size and class of a. b is the same class as a. If a is empty, b is also empty. If a is heterogeneous, b is also heterogeneous. If a contains deleted handles, then copy creates deleted handles of the same class in b. Dynamic properties and listeners associated with objects in a are not copied to objects in b.

See Also

correct | getStateEstimate | initialize | predict | resamplingPolicyPF |
stateEstimatorPF

Topics

"Track a Car-Like Robot Using Particle Filter" (Robotics System Toolbox)

"Particle Filter Parameters"

"Particle Filter Workflow"

Introduced in R2016a

correct

Adjust state estimate based on sensor measurement

Syntax

```
[stateCorr,stateCov] = correct(pf,measurement)
[stateCorr,stateCov] = correct(pf,measurement,varargin)
```

Description

[stateCorr, stateCov] = correct(pf, measurement) calculates the corrected system state and its associated uncertainty covariance based on a sensor measurement at the current time step. correct uses the MeasurementLikelihoodFcn property from the particle filter object, pf, as a function to calculate the likelihood of the sensor measurement for each particle. The two inputs to the MeasurementLikelihoodFcn function are:

- 1 pf The stateEstimatorPF object, which contains the particles of the current iteration
- 2 measurement The sensor measurements used to correct the state estimate

The MeasurementLikelihoodFcn function then extracts the best state estimate and covariance based on the setting in the StateEstimationMethod property.

[stateCorr, stateCov] = correct(pf, measurement, varargin) passes all additional arguments in varargin to the underlying MeasurementLikelihoodFcn after the first three required inputs.

Examples

Particle Filter Prediction and Correction

Create a stateEstimatorPF object, and execute a prediction and correction step for state estimation. The particle filter gives a predicted state estimate based on the return value of StateTransitionFcn. It then corrects the state based on a given measurement and the return value of MeasurementLikelihoodFcn.

Create a particle filter with the default three states.

```
pf = stateEstimatorPF

pf =
    stateEstimatorPF with properties:

        NumStateVariables: 3
              NumParticles: 1000
        StateTransitionFcn: @nav.algs.gaussianMotion
        MeasurementLikelihoodFcn: @nav.algs.fullStateMeasurement
        IsStateVariableCircular: [0 0 0]
        ResamplingPolicy: [1x1 resamplingPolicyPF]
        ResamplingMethod: 'multinomial'
        StateEstimationMethod: 'mean'
```

```
StateOrientation: 'row'
Particles: [1000x3 double]
Weights: [1000x1 double]
State: 'Use the getStateEstimate function to see the value.'
StateCovariance: 'Use the getStateEstimate function to see the value.'
```

Specify the mean state estimation method and systematic resampling method.

```
pf.StateEstimationMethod = 'mean';
pf.ResamplingMethod = 'systematic';
```

Initialize the particle filter at state [4 1 9] with unit covariance (eye(3)). Use 5000 particles.

```
initialize(pf,5000,[4 1 9],eye(3));
```

Assuming a measurement [4.2 0.9 9], run one predict and one correct step.

```
[statePredicted,stateCov] = predict(pf);
[stateCorrected,stateCov] = correct(pf,[4.2 0.9 9]);
```

Get the best state estimate based on the StateEstimationMethod algorithm.

```
stateEst = getStateEstimate(pf)

stateEst = 1 \times 3

4.1562 0.9185 9.0202
```

Input Arguments

pf — stateEstimatorPF object

handle

stateEstimatorPF object, specified as a handle. See stateEstimatorPF for more information.

measurement — Sensor measurements

array

Sensor measurements, specified as an array. This input is passed directly into the MeasurementLikelihoodFcn property of pf. It is used to calculate the likelihood of the sensor measurement for each particle.

varargin — Variable-length input argument list

comma-separated list

Variable-length input argument list, specified as a comma-separated list. This input is passed directly into the MeasurementLikelihoodFcn property of pf. It is used to calculate the likelihood of the sensor measurement for each particle. When you call:

```
correct(pf,measurement,arg1,arg2)
```

MATLAB essentially calls measurementLikelihoodFcn as:

```
measurementLikelihoodFcn(pf,measurement,arg1,arg2)
```

Output Arguments

stateCorr — Corrected system state

vector with length NumStateVariables

Corrected system state, returned as a row vector with length NumStateVariables. The corrected state is calculated based on the StateEstimationMethod algorithm and the MeasurementLikelihoodFcn.

stateCov — Corrected system covariance

N-by-N matrix | []

Corrected system variance, returned as an N-by-N matrix, where N is the value of NumStateVariables property from pf. The corrected state is calculated based on the StateEstimationMethod algorithm and the MeasurementLikelihoodFcn. If you specify a state estimate method that does not support covariance, then the function returns stateCov as [].

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

correct | getStateEstimate | initialize | predict | resamplingPolicyPF |
stateEstimatorPF

Topics

"Track a Car-Like Robot Using Particle Filter" (Robotics System Toolbox)

"Particle Filter Parameters"

"Particle Filter Workflow"

Introduced in R2016a

getStateEstimate

Extract best state estimate and covariance from particles

Syntax

```
stateEst = getStateEstimate(pf)
[stateEst,stateCov] = getStateEstimate(pf)
```

Description

stateEst = getStateEstimate(pf) returns the best state estimate based on the current set of
particles. The estimate is extracted based on the StateEstimationMethod property from the
stateEstimatorPF object, pf.

[stateEst,stateCov] = getStateEstimate(pf) also returns the covariance around the state estimate. The covariance is a measure of the uncertainty of the state estimate. Not all state estimate methods support covariance output. In this case, getStateEstimate returns stateCov as [].

Examples

Particle Filter Prediction and Correction

Create a stateEstimatorPF object, and execute a prediction and correction step for state estimation. The particle filter gives a predicted state estimate based on the return value of StateTransitionFcn. It then corrects the state based on a given measurement and the return value of MeasurementLikelihoodFcn.

Create a particle filter with the default three states.

```
pf = stateEstimatorPF
pf =
 stateEstimatorPF with properties:
           NumStateVariables: 3
                NumParticles: 1000
          StateTransitionFcn: @nav.algs.gaussianMotion
   MeasurementLikelihoodFcn: @nav.algs.fullStateMeasurement
     IsStateVariableCircular: [0 0 0]
            ResamplingPolicy: [1x1 resamplingPolicyPF]
            ResamplingMethod: 'multinomial'
       StateEstimationMethod: 'mean'
            StateOrientation: 'row'
                   Particles: [1000x3 double]
                     Weights: [1000x1 double]
                       State: 'Use the getStateEstimate function to see the value.'
             StateCovariance: 'Use the getStateEstimate function to see the value.'
```

Specify the mean state estimation method and systematic resampling method.

```
pf.StateEstimationMethod = 'mean';
pf.ResamplingMethod = 'systematic';
Initialize the particle filter at state [4 1 9] with unit covariance (eye(3)). Use 5000 particles.
initialize(pf,5000,[4 1 9],eye(3));
Assuming a measurement [4.2 0.9 9], run one predict and one correct step.
[statePredicted,stateCov] = predict(pf);
[stateCorrected,stateCov] = correct(pf,[4.2 0.9 9]);
Get the best state estimate based on the StateEstimationMethod algorithm.
stateEst = getStateEstimate(pf)
stateEst = 1×3
4.1562 0.9185 9.0202
```

Input Arguments

pf — stateEstimatorPF object

handle

stateEstimatorPF object, specified as a handle. See stateEstimatorPF for more information.

Output Arguments

stateEst — Best state estimate

vector

Best state estimate, returned as a row vector with length NumStateVariables. The estimate is extracted based on the StateEstimationMethod algorithm specified in pf.

stateCov — Corrected system covariance

```
N-by-N matrix | []
```

Corrected system variance, returned as an N-by-N matrix, where N is the value of NumStateVariables property from pf. The corrected state is calculated based on the StateEstimationMethod algorithm and the MeasurementLikelihoodFcn. If you specify a state estimate method that does not support covariance, then the function returns stateCov as [].

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder[™].

See Also

correct | getStateEstimate | initialize | predict | resamplingPolicyPF |
stateEstimatorPF

Topics"Track a Car-Like Robot Using Particle Filter" (Robotics System Toolbox)
"Particle Filter Parameters"
"Particle Filter Workflow"

Introduced in R2016a

initialize

Initialize the state of the particle filter

Syntax

```
initialize(pf,numParticles,mean,covariance)
initialize(pf,numParticles,stateBounds)
initialize(____,Name,Value)
```

Description

initialize(pf,numParticles,mean,covariance) initializes the particle filter object, pf, with a specified number of particles, numParticles. The initial states of the particles in the state space are determined by sampling from the multivariate normal distribution with the specified mean and covariance.

initialize(pf,numParticles,stateBounds) determines the initial location of the particles by sample from the multivariate uniform distribution within the specified stateBounds.

initialize(____, Name, Value) initializes the particles with additional options specified by one or more Name, Value pair arguments.

Examples

Particle Filter Prediction and Correction

Create a stateEstimatorPF object, and execute a prediction and correction step for state estimation. The particle filter gives a predicted state estimate based on the return value of StateTransitionFcn. It then corrects the state based on a given measurement and the return value of MeasurementLikelihoodFcn.

Create a particle filter with the default three states.

```
pf = stateEstimatorPF
```

```
StateCovariance: 'Use the getStateEstimate function to see the value.'
```

Specify the mean state estimation method and systematic resampling method.

```
pf.StateEstimationMethod = 'mean';
pf.ResamplingMethod = 'systematic';
Initialize the particle filter at state [4 1 9] with unit covariance (eye(3)). Use 5000 particles.
initialize(pf,5000,[4 1 9],eye(3));
Assuming a measurement [4.2 0.9 9], run one predict and one correct step.
[statePredicted,stateCov] = predict(pf);
[stateCorrected,stateCov] = correct(pf,[4.2 0.9 9]);
Get the best state estimate based on the StateEstimationMethod algorithm.
stateEst = getStateEstimate(pf)
```

Input Arguments

 $stateEst = 1 \times 3$

4.1562

pf — stateEstimatorPF object

0.9185

handle

stateEstimatorPF object, specified as a handle. See stateEstimatorPF for more information.

numParticles — Number of particles used in the filter

9.0202

scalar

Number of particles used in the filter, specified as a scalar.

mean — Mean of particle distribution

vector

Mean of particle distribution, specified as a vector. The NumStateVariables property of pf is set based on the length of this vector.

covariance - Covariance of particle distribution

N-by-*N* matrix

Covariance of particle distribution, specified as an N-by-N matrix, where N is the value of NumStateVariables property from pf.

stateBounds — Bounds of state variables

n-by-2 matrix

Bounds of state variables, specified as an n-by-2 matrix. The NumStateVariables property of pf is set based on the value of n. Each row corresponds to the lower and upper limit of the corresponding state variable.

Name-Value Pair Arguments

Specify optional comma-separated pairs of Name, Value arguments. Name is the argument name and Value is the corresponding value. Name must appear inside quotes. You can specify several name and value pair arguments in any order as Name1, Value1, . . . , NameN, ValueN.

Example: "CircularVariables",[0 0 1]

Circular Variables — Circular variables

logical vector

Circular variables, specified as a logical vector. Each state variable that uses circular or angular coordinates is indicated with a 1. The length of the vector is equal to the NumStateVariables property of pf.

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

correct | getStateEstimate | initialize | predict | resamplingPolicyPF |
stateEstimatorPF

Topics

"Track a Car-Like Robot Using Particle Filter" (Robotics System Toolbox)

"Particle Filter Parameters"

"Particle Filter Workflow"

Introduced in R2016a

predict

Predict state of robot in next time step

Syntax

```
[statePred,stateCov] = predict(pf)
[statePred,stateCov] = predict(pf,varargin)
```

Description

[statePred, stateCov] = predict(pf) calculates the predicted system state and its associated uncertainty covariance. predict uses the StateTransitionFcn property of stateEstimatorPF object, pf, to evolve the state of all particles. It then extracts the best state estimate and covariance based on the setting in the StateEstimationMethod property.

[statePred, stateCov] = predict(pf, varargin) passes all additional arguments specified in varargin to the underlying StateTransitionFcn property of pf. The first input to StateTransitionFcn is the set of particles from the previous time step, followed by all arguments in varargin.

Examples

Particle Filter Prediction and Correction

Create a stateEstimatorPF object, and execute a prediction and correction step for state estimation. The particle filter gives a predicted state estimate based on the return value of StateTransitionFcn. It then corrects the state based on a given measurement and the return value of MeasurementLikelihoodFcn.

Create a particle filter with the default three states.

Specify the mean state estimation method and systematic resampling method.

```
pf.StateEstimationMethod = 'mean';
pf.ResamplingMethod = 'systematic';
Initialize the particle filter at state [4 1 9] with unit covariance (eye(3)). Use 5000 particles.
initialize(pf,5000,[4 1 9],eye(3));
Assuming a measurement [4.2 0.9 9], run one predict and one correct step.
[statePredicted,stateCov] = predict(pf);
[stateCorrected,stateCov] = correct(pf,[4.2 0.9 9]);
Get the best state estimate based on the StateEstimationMethod algorithm.
stateEst = getStateEstimate(pf)
stateEst = 1×3
4.1562 0.9185 9.0202
```

Input Arguments

pf — stateEstimatorPF object

handle

stateEstimatorPF object, specified as a handle. See stateEstimatorPF for more information.

varargin — Variable-length input argument list

comma-separated list

Variable-length input argument list, specified as a comma-separated list. This input is passed directly into the StateTransitionFcn property of pf to evolve the system state for each particle. When you call:

```
predict(pf,arg1,arg2)
MATLAB essentially calls the stateTranstionFcn as:
stateTransitionFcn(pf,prevParticles,arg1,arg2)
```

Output Arguments

statePred — Predicted system state

vector

Predicted system state, returned as a vector with length NumStateVariables. The predicted state is calculated based on the StateEstimationMethod algorithm.

stateCov — Corrected system covariance

```
N-bv-N matrix | []
```

Corrected system variance, returned as an N-by-N matrix, where N is the value of NumStateVariables property from pf. The corrected state is calculated based on the

StateEstimationMethod algorithm and the MeasurementLikelihoodFcn. If you specify a state estimate method that does not support covariance, then the function returns stateCov as [].

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

correct | getStateEstimate | initialize | predict | resamplingPolicyPF |
stateEstimatorPF

Topics

"Track a Car-Like Robot Using Particle Filter" (Robotics System Toolbox)

"Particle Filter Parameters"

"Particle Filter Workflow"

Introduced in R2016a

stateSpaceSE2

SE(2) state space

Description

The stateSpaceSE2 object stores parameters and states in the SE(2) state space, which is composed of state vectors represented by $[x, y, \theta]$. x and y are Cartesian coordinates, and θ is the orientation angle. The object uses Euclidean distance to calculate distance and uses linear interpolation to calculate translation and rotation of the state.

Creation

Syntax

```
space = stateSpaceSE2
space = stateSpaceSE2(bounds)
```

Description

space = stateSpaceSE2 creates an SE(2) state space object with default state bounds for x, y, and θ .

space = stateSpaceSE2(bounds) specifies the bounds for x, y, and θ . The state values beyond the bounds are truncated to the bounds. The input, bounds, allows you to set the value of the StateBounds property.

Properties

Name — Name of state space

```
'SE2' (default) | string
```

Name of state space, specified as a string.

NumStateVariables — Dimension of the state space

3 (default) | positive integer

This property is read-only.

Dimension of the state space, specified as a positive integer.

StateBounds — Bounds of state variables

```
[-100 100; -100 100; -3.1416 3.1416] (default) | 3-by-2 real-valued matrix
```

Bounds of state variables, specified as a 3-by-2 real-valued matrix.

- The first row specifies the lower and upper bounds of the x state in meters.
- The second row specifies the lower and upper bounds of the *y* state in meters.

• The third row specifies the lower and upper bounds of the θ state in radians.

Data Types: double

WeightXY — Weight applied to x and y distance calculation

1 (default) | nonnegative real scalar

Weight applied to x and y distance calculation, specified as a nonnegative real scalar.

In the object, the distance calculated as:

$$d = \sqrt{\left(w_{xy}(d_x^2 + d_y^2)\right) + w_\theta d_\theta^2}$$

 w_{xy} is weight applied to x and y coordinates, and w_{θ} is the weight applied to the θ coordinate. d_x , d_y , and d_{θ} are the distances in the x, y, and θ direction, respectively.

Data Types: double

WeightTheta — Weight applied to theta distance calculation

0.1 (default) | nonnegative real scalar

Weight applied to θ distance calculation, specified as a nonnegative real scalar.

In the object, the distance calculated as:

$$d = \sqrt{\left(w_{xy}(d_x^2 + d_y^2)\right) + w_\theta d_\theta^2}$$

 w_{xy} is weight applied to x and y coordinates, and w_{θ} is the weight applied to the θ coordinate. d_x , d_y , and d_{θ} are the distances in the x, y, and θ direction, respectively.

Data Types: double

Object Functions

copy Create deep copy of state space object

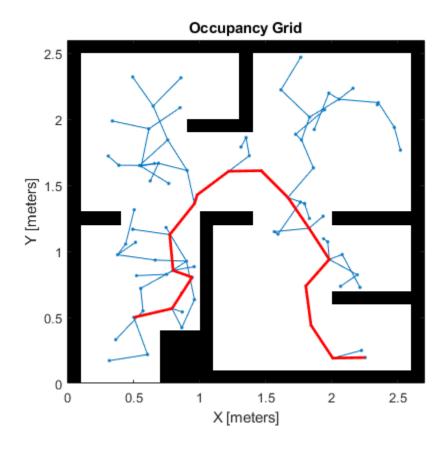
distance Distance between two states enforceStateBounds interpolate Reduce state to state bounds Interpolate between states

sampleGaussian Sample state using Gaussian distribution Sample using uniform distribution

Examples

Plan Path Between Two SE(2) States

```
Create an SE(2) state space.
ss = stateSpaceSE2;
Create an occupancyMap-based state validator using the created state space.
sv = validatorOccupancyMap(ss);
Create an occupancy map from an example map and set map resolution as 10 cells/meter.
load exampleMaps
map = occupancyMap(simpleMap,10);
sv.Map = map;
Set validation distance for the validator.
sv.ValidationDistance = 0.01;
Update state space bounds to be the same as map limits.
ss.StateBounds = [map.XWorldLimits; map.YWorldLimits; [-pi pi]];
Create the path planner and increase maximum connection distance.
planner = plannerRRT(ss,sv);
planner.MaxConnectionDistance = 0.3;
Set the start and goal states.
start = [0.5, 0.5, 0];
goal = [2.5, 0.2, 0];
Plan a path with default settings.
rng(100,'twister'); % for repeatable result
[pthObj,solnInfo] = planner.plan(start,goal);
Visualize the results.
map.show; hold on;
plot(solnInfo.TreeData(:,1),solnInfo.TreeData(:,2),'.-'); % tree expansion
plot(pthObj.States(:,1), pthObj.States(:,2),'r-','LineWidth',2) % draw path
```



Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder $^{\text{\tiny TM}}$.

See Also

stateSpaceDubins|stateSpaceReedsShepp

Introduced in R2019b

stateSpaceSE3

SE(3) state space

Description

The stateSpaceSE3 object stores parameters and states in the SE(3) state space, which is composed of state vectors represented by [x, y, z, qw, qx, qy, qz]. x, y, and z are Cartesian coordinates. qw, qx, qy, and qz represent the orientation in a quaternion. The object uses Euclidean distance calculation and linear interpolation for the translation component of the state. The object uses quaternion distance calculation and spherical linear interpolation for the rotation component of the state.

Creation

Syntax

```
space = stateSpaceSE3
space = stateSpaceSE3(bounds)
```

Description

space = stateSpaceSE3 creates an SE(3) state space object with default state bounds for x, y, and z. The state variables qw, qx, qy, and qz corresponding to orientation are not bounded.

space = stateSpaceSE3 (bounds) creates an SE(3) state space object with state bounds specified as a 7-by-2 matrix. Each row specifies the minimum and maximum value for a dimension of the state in the order x, y, z, qw, qx, qy, and qz. The input bounds sets the StateBounds property.

Properties

Name — Name of state space

'SE3' (default) | character vector

This property is read-only.

Name of state space, specified as a character vector.

Data Types: char

NumStateVariables — Number of state space dimensions

7 (default) | positive integer

This property is read-only.

Number of state space dimensions, specified dimensions, returned as a positive integer.

Data Types: double

StateBounds — Bounds of state variables

[-100 100; -100 100; -100 100; Inf Inf; Inf Inf; Inf Inf; Inf Inf] (default) \mid 7-by-2 matrix of real values

Bounds of state variables, specified as a 7-by-2 matrix of real values.

- The first row specifies the lower and upper bounds of the x state in meters.
- The second row specifies the lower and upper bounds of the y state in meters.
- The third row specifies the lower and upper bounds of the *z* state in meters.
- The fourth through the seventh rows specify the lower and upper bounds of the state variables *qw*, *qx*, *qy*, and *qz* respectively, corresponding to orientation as a quaternion.

Note The StateBounds property only affect the Cartesian components of the state. The state variables corresponding to orientation are not bounded.

```
Example: stateSpaceSE3([-10 10; -10 10; -10 10; Inf Inf; Inf Inf; Inf Inf])
```

Example: space.StateBounds = [-10 10; -10 10; -10 10; Inf Inf; Inf Inf; Inf Inf; Inf Inf]

Data Types: double

WeightXYZ — Weight applied to x, y, and z distance calculation

1 (default) | positive real scalar

Weight applied to the x, y, and z distance calculation, specified as a positive real scalar. By default, the weight for translation is chosen to be greater than the weight for rotation.

The object calculates distance as:

$$d = \sqrt{w_{xyz}(d_x^2 + d_y^2 + d_z^2) + w_a d_a^2}$$

,

where w_{xyz} is the weight applied to x, y, and z coordinates, and w_q is the weight applied to the orientation in quaternion. d_x , d_y , and d_z are the distances in the x, y, and z directions, respectively. d_q is the quaternion distance.

Example: space.WeightXYZ = 2

Data Types: double

WeightQuaternion — Weight applied to quaternion distance calculation

0.1 (default) | positive real scalar

Weight applied to quaternion distance calculation, specified as a positive real scalar. By default, the weight for rotation is chosen to be less than the weight for translation.

The object calculates distance as:

$$d = \sqrt{w_{xyz}(d_x^2 + d_y^2 + d_z^2) + w_q d_q^2}$$

,

where w_{xyz} is weight applied to x, y, and z coordinates, and w_q is the weight applied to the orientation in quaternion. d_x , d_y , and d_z are the distances in the x, y, and z direction, respectively. d_q is the quaternion distance.

```
Example: space.WeightQuaternion = 0.5
Data Types: double
```

Object Functions

copy Create deep copy of state space object

distance Distance between two states enforceStateBounds Reduce state to state bounds interpolate Interpolate between states

sampleUniform Sample state using uniform distribution

Examples

Validate Path Through 3-D Occupancy Map Environment

Create a 3-D occupancy map and associated state validator. Plan, validate, and visualize a path through the occupancy map.

Load and Assign Map to State Validator

Load a 3-D occupancy map of a city block into the workspace. Specify a threshold for which cells to consider as obstacle-free.

```
mapData = load('dMapCityBlock.mat');
omap = mapData.omap;
omap.FreeThreshold = 0.5;
```

Inflate the occupancy map to add a buffer zone for safe operation around the obstacles.

```
inflate(omap,5)
```

Create an SE(3) state space object with bounds for state variables.

```
ss = stateSpaceSE3([-20 220;
    -20 220;
    -10 100;
    inf inf;
    inf inf;
    inf inf;
    inf inf);
```

Create a 3-D occupancy map state validator using the created state space.

```
sv = validatorOccupancyMap3D(ss);
```

Assign the occupancy map to the state validator object. Specify the sampling distance interval.

```
sv.Map = omap;
sv.ValidationDistance = 0.1;
```

Plan and Visualize Path

Create a path planner with increased maximum connection distance. Reduce the maximum number of iterations.

```
planner = plannerRRT(ss,sv);
planner.MaxConnectionDistance = 50;
planner.MaxIterations = 1000;
```

Create a user-defined evaluation function for determining whether the path reaches the goal. Specify

```
the probability of choosing the goal state during sampling.
planner.GoalReachedFcn = @(\sim,x,y)(norm(x(1:3)-y(1:3))<5);
planner.GoalBias = 0.1;
Set the start and goal states.
start = [40 180 25 0.7 0.2 0 0.1];
goal = [150 33 35 0.3 0 0.1 0.6];
Plan a path using the specified start, goal, and planner.
[pthObj,solnInfo] = plan(planner,start,goal);
Check that the points of the path are valid states.
isValid = isStateValid(sv,pth0bj.States)
isValid = 6x1 logical array
   1
   1
   1
   1
   1
   1
```

Check that the motion between each sequential path state is valid.

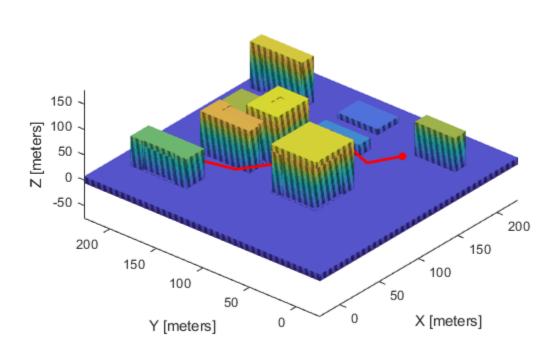
```
isPathValid = zeros(size(pthObj.States,1)-1,1,'logical');
for i = 1:size(pth0bj.States,1)-1
    [isPathValid(i),~] = isMotionValid(sv,pthObj.States(i,:),...
        pthObj.States(i+1,:));
end
isPathValid
isPathValid = 5x1 logical array
   1
   1
   1
   1
   1
```

Visualize the results.

```
show(omap)
hold on
```

scatter3(start(1,1),start(1,2),start(1,3),'g','filled') % draw start state
scatter3(goal(1,1),goal(1,2),goal(1,3),'r','filled') % draw goal state
plot3(pth0bj.States(:,1),pth0bj.States(:,2),pth0bj.States(:,3),...
'r-','LineWidth',2) % draw path

Occupancy Map



Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

stateSpaceSE2 | validatorOccupancyMap3D

Introduced in R2020b

stateSpaceDubins

State space for Dubins vehicles

Description

The stateSpaceDubins object stores parameters and states in the Dubins state space, which is composed of state vectors represented by $[x, y, \theta]$. x and y are Cartesian coordinates, and θ is the orientation angle. The Dubins state space has a lower limit on the turning radius (specified by the MinTurningRadius property in the object) for navigating between states and uses the shortest feasible curve to connect states.

Creation

Syntax

```
space = stateSpaceDubins
space = stateSpaceDubins(bounds)
```

Description

space = stateSpaceDubins creates a Dubins state space object with default state bounds for x, y, and θ .

space = stateSpaceDubins(bounds) specifies the bounds for x, y, and θ . The state values beyond the bounds are truncated to the bounds. The input, bounds, allows you to set the value of the StateBounds property.

Properties

Name — Name of state space

```
'SE2 Dubins' (default) | string
```

Name of state space, specified as a string.

NumStateVariables — Dimension of the state space

3 (default) | positive integer

This property is read-only.

Dimension of the state space, specified as a positive integer.

StateBounds — Bounds of state variables

```
[-100 100; -100 100; -3.1416 3.1416] (default) | 3-by-2 real-valued matrix
```

Bounds of state variables, specified as a 3-by-2 real-valued matrix.

• The first row specifies the lower and upper bounds for the *x* state in meters.

- The second row specifies the lower and upper bounds for the *y* state in meters.
- The third row specifies the lower and upper bounds for the θ state in radians.

Data Types: double

MinTurningRadius — Minimum turning radius

```
1 (default) | positive scalar
```

Minimum turning radius in meters, specified as a positive scalar. The minimum turning radius is for the smallest circle the vehicle can make with maximum steer in a single direction.

Object Functions

copy Create deep copy of state space object

distance Distance between two states enforceStateBounds interpolate Distance between two states leading to state bounds interpolate Distance between two states leading to state between states leading to state between two states leading to state leading to state between two states leading to state leading to

sampleGaussian Sample state using Gaussian distribution sampleUniform Sample state using uniform distribution

Examples

Plan Path Between Two States in Dubins State Space

Create a Dubins state space and set the minimum turing radius to 0.2.

```
ss = stateSpaceDubins;
ss.MinTurningRadius = 0.2;
```

Create an occupancyMap-based state validator using the created state space.

```
sv = validatorOccupancyMap(ss);
```

Create an occupancy map from an example map and set map resolution as 10 cells/meter.

```
load exampleMaps
map = occupancyMap(simpleMap,10);
sv.Map = map;
```

Set validation distance for the validator.

```
sv.ValidationDistance = 0.01;
```

Update state space bounds to be the same as map limits.

```
ss.StateBounds = [map.XWorldLimits; map.YWorldLimits; [-pi pi]];
```

Create the path planner and increase max connection distance.

```
planner = plannerRRT(ss,sv);
planner.MaxConnectionDistance = 0.3;
Set the start and goal states.
```

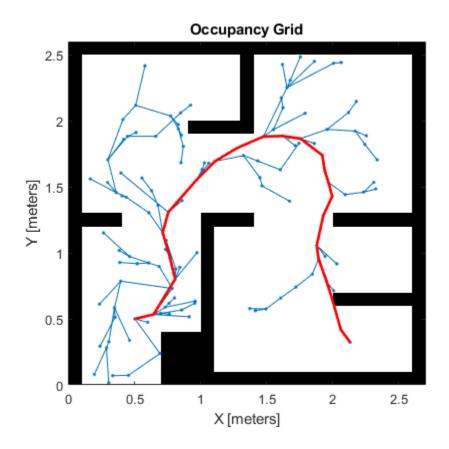
```
start = [0.5, 0.5, 0];
goal = [2.5, 0.2, 0];
```

Plan a path with default settings.

```
rng(100,'twister'); % repeatable result
[pth0bj,solnInfo] = planner.plan(start,goal);

Visualize the results.

show(map);
hold on;
plot(solnInfo.TreeData(:,1),solnInfo.TreeData(:,2),'.-'); % tree expansion
plot(pth0bj.States(:,1), pth0bj.States(:,2),'r-','LineWidth',2) % draw path
```



Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder $^{\text{\tiny TM}}$.

See Also

dubinsConnection|stateSpaceReedsShepp|stateSpaceSE2

stateSpaceReedsShepp

State space for Reeds-Shepp vehicles

Description

The stateSpaceReedsShepp object stores parameters and states in the ReedsShepp state space, which is composed of state vectors represented by $[x, y, \theta]$. x and y are Cartesian coordinates, and θ is the orientation angle. The Reeds-Shepp state space has a lower limit on the turning radius (specified by the MinTurningRadius property in the object) and forward and reverse costs (specified by the ForwardCost and ReverseCost properties in the object) for navigating between states.

Creation

Syntax

```
space = stateSpaceReedsShepp
sapce = stateSpaceReedsShepp(bounds)
```

Description

space = stateSpaceReedsShepp creates a Reeds-Shepp state space object with default state bounds for x, y, and θ .

sapce = stateSpaceReedsShepp(bounds) specifies the bounds for x, y, and θ . The state values beyond the bounds are truncated to the bounds. The input, bounds, sets the value of the StateBounds property.

Properties

Name — Name of state space

'SE2 Dubins' (default) | string

Name of state space, specified as a string.

NumStateVariables — Dimension of the state space

3 (default) | positive integer

This property is read-only.

Dimension of the state space, specified as a positive integer.

StateBounds — Bounds of state variables

```
[-100 100; -100 100; -3.1416 3.1416] (default) | 3-by-2 real-valued matrix
```

Bounds of state variables, specified as a 3-by-2 real-valued matrix.

- The first row specifies the lower and upper bounds for the *x* state in meters.
- The second row specifies the lower and upper bounds for the *y* state in meters.
- The third row specifies the lower and upper bounds for the θ state in radians.

Data Types: double

MinTurningRadius — Minimum turning radius

1 (default) | positive scalar

Minimum turning radius in meters, specified as a positive scalar. The minimum turning radius is for the smallest circle the vehicle can make with maximum steer in a single direction.

ForwardCost — Cost multiplier for forward motion

1 (default) | positive scalar

Cost multiplier for forward motion, specified as a positive scalar. Increase the cost to penalize forward motion.

ReverseCost — Cost multiplier for reverse motion

1 (default) | positive scalar

Cost multiplier for reverse motion, specified as a positive scalar. Increase the cost to penalize reverse motion.

Object Functions

copy Create deep copy of state space object

distance Distance between two states enforceStateBounds interpolate Reduce state to state bounds Interpolate between states

sampleGaussian Sample state using Gaussian distribution Sample using uniform distribution

Examples

Plan Path Between Two States in ReedsShepp State Space

Create a ReedsShepp state space.

```
ss = stateSpaceReedsShepp;
```

Create an occupanyMap-based state validator using the created state space.

```
sv = validatorOccupancyMap(ss);
```

Create an occupany map from an example map and set map resolution as 10 cells/meter.

```
load exampleMaps
map = occupancyMap(simpleMap,10);
sv.Map = map;
```

Set validation distance for the validator.

```
sv.ValidationDistance = 0.01;
```

```
Update state space bounds to be the same as map limits.
```

```
ss.StateBounds = [map.XWorldLimits; map.YWorldLimits; [-pi pi]];
```

Create the path planner and increase max connection distance.

```
planner = plannerRRT(ss,sv);
planner.MaxConnectionDistance = 0.3;
```

Set the start and goal states.

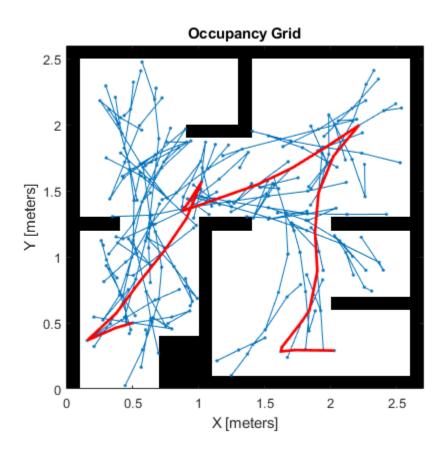
```
start = [0.5, 0.5, 0];
goal = [2.5, 0.2, 0];
```

Plan a path with default settings.

```
rng(100,'twister'); % repeatable result
[pth0bj,solnInfo] = planner.plan(start,goal);
```

Visualize the results.

```
show(map);
hold on;
plot(solnInfo.TreeData(:,1),solnInfo.TreeData(:,2),'.-'); % tree expansion
plot(pthObj.States(:,1), pthObj.States(:,2),'r-','LineWidth',2) % draw path
```



Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

reedsSheppConnection|stateSpaceDubins|stateSpaceSE2

distance

Distance between two states

Syntax

```
dist = distance(space, states1, states2)
```

Description

dist = distance(space, states1, states2) returns the distance between states1 and
states2 in the specified state space space.

Examples

Calculate Distance Between Two States in SE3

Calculate distance between two states.

```
dist = distance(space,[2 10 3 0.2 0 0 0.8],[0 -2.5 4 0.7 0.3 0 0])

dist = 12.7269
```

Calculate Euclidean distance between two states.

```
space.WeightQuaternion = 0; distEuc = distance(space,[2 10 3 0.2 0 0 0.8; 4 5 2 1 2 4 2],[62 5 33 0.2 0 0 0.8; 9 9 3 3 1 3.1 distEuc = 2 \times 1
```

```
67.2681
6.4807
```

Input Arguments

space — State space object

stateSpaceSE2 object | stateSpaceSE3 object | stateSpaceDubins object |
stateSpaceReedsShepp object

State space object, specified as a stateSpaceSE2, stateSpaceSE3, stateSpaceDubins, or stateSpaceReedsShepp object.

states1 — Initial states for distance calculation

n-by-3 matrix of real values | *n*-by-7 matrix of real values

Initial states for distance calculation, specified as an n-by-3 or n-by-7 matrix of real values. n is the number of specified states.

For the 2-D state space objects stateSpaceSE2, stateSpaceDubins, and stateSpaceReedsShepp, each row is of form [x y theta], which defines the xy-position and orientation angle theta of a state in the state space.

For the 3-D state space object stateSpaceSE3, each row is of form [x y z qw qx qy qz], which defines the xyz-position and quaternion orientation [qw qx qy qz] of a state in the state space.

The function supports following combinations for distance calculation:

• n-to-n number of states in states1 and n number of states in states2.

```
For example, distance(space, rand(10,7), rand(10,7))
```

• 1-to-n-1 state in states 1 and n number of states in states 2.

```
For example, distance(space, rand(1,7), rand(10,7))
```

• n-to-1 — n number of states in states1 and 1 state in states2.

```
For example, distance(space, rand(10,7), rand(1,7))
```

Data Types: single | double

states2 — Final states for distance calculation

n-by-3 matrix of real values | *n*-by-7 matrix of real values

Final states for distance calculation, specified as an n-by-3 or n-by-7 matrix of real values. n is the number of specified states.

For the 2-D state space objects stateSpaceSE2, stateSpaceDubins, and stateSpaceReedsShepp, each row is of form [x y theta], which defines the xy-position and orientation angle theta of a state in the state space.

For the 3-D state space object stateSpaceSE3, each row is of form $[x \ y \ z \ qw \ qx \ qz]$, which defines the xyz-position and quaternion orientation $[qw \ qx \ qy \ qz]$ of a state in the state space.

The function supports following combinations for distance calculation:

• n-to-n number of states in states1 and n number of states in states2.

```
For example, distance(space, rand(10,7), rand(10,7))
```

• 1-to-n-1 state in states1 and n number of states in states2.

For example, distance(space, rand(1,7), rand(10,7))

• n-to-1 — n number of states in states1 and 1 state in states2.

For example, distance(space, rand(10,7), rand(1,7))

Data Types: single | double

Output Arguments

dist - Distance between states

n-element column vector

Distance between states, returned as an n-element column vector. n is the number of specified states.

The function supports following combinations for distance calculation:

- n-to-n number of states in states1 and n number of states in states2.
- 1-to-n-1 state in states1 and n number of states in states2.
- n-to-1 n number of states in states1 and 1 state in states2.

Data Types: single | double

See Also

stateSpaceDubins | stateSpaceReedsShepp | stateSpaceSE2 | stateSpaceSE3

interpolate

Interpolate between states

Syntax

```
interpStates = interpolate(space, state1, state2, ratio)
```

Description

interpStates = interpolate(space, state1, state2, ratio) interpolates states between the
specified start state state1 and end state state2 based on the specified interpolation ratio.

Examples

Interpolate Between States in SE(2)

Create an SE(2) state space with default properties.

```
space = stateSpaceSE2
space =
  stateSpaceSE2 with properties:
                  Name: 'SE2'
          StateBounds: [3×2 double]
    NumStateVariables: 3
             WeightXY: 1
          WeightTheta: 0.1000
Create a pair of states in 2-D space.
state1 = [2 10 -pi];
state2 = [0 -2.5 -pi/4];
Interpolate halfway between two states.
state = interpolate(space, state1, state2, 0.5)
state = 1 \times 3
    1.0000
               3.7500 -1.9635
Interpolate multiple points with a fixed interval.
states = interpolate(space, state1, state2, 0:0.02:1)
states = 51 \times 3
    2.0000 10.0000 -3.1416
    1.9600 9.7500 -3.0945
```

```
9.5000
                    -3.0473
1.9200
1.8800
          9.2500
                    -3.0002
1.8400
          9.0000
                    -2.9531
1.8000
          8.7500
                    -2.9060
1.7600
          8.5000
                    -2.8588
          8.2500
1.7200
                    -2.8117
1.6800
          8.0000
                    -2.7646
1.6400
          7.7500
                    -2.7175
```

Interpolate Between States in SE(3)

Create an SE(3) state space with default properties.

Create a pair of states in 3-D space.

```
state1 = [2 10 3 0.2 0 0 0.8];
state2 = [0 -2.5 4 0.7 0.3 0 0];
```

Interpolate halfway between two states.

```
state = interpolate(space, state1, state2, 0.5)
state = 1×7
```

1 3.75 3.5 0.7428 0.25188 0 0.62033

Interpolate multiple points with a fixed interval.

```
states = interpolate(space, state1, state2, 0:0.02:1)
```

states = 51×7 3 2 10 0.24254 0 0.97014 9.75 3.02 0.010877 1.96 0.26633 0 0.96382 9.5 1.92 3.04 0.28994 0.021745 0 0.9568 1.88 9.25 3.06 0.31333 0.032598 0 0.94908 1.84 9 3.08 0.3365 0.043428 0 0.94068 8.75 3.1 0 1.8 0.35943 0.054225 0.9316 8.5 0 1.76 3.12 0.38209 0.064984 0.92184 1.72 8.25 3.14 0.40448 0.075695 0 0.91141 1.68 8 3.16 0.42657 0.086352 (-) 0.90032 1.64 7.75 3.18 0.44835 0.096946 0 0.88858

Input Arguments

space — State space object

stateSpaceSE2 object | stateSpaceSE3 object | stateSpaceDubins object |
stateSpaceReedsShepp object

State space object, specified as a stateSpaceSE2, stateSpaceSE3, stateSpaceDubins, or stateSpaceReedsShepp object.

state1 — Start state for interpolation

three-element vector of real values | seven-element vector of real values

Start state for interpolation, specified as a three-element or seven-element vector of real values.

For the 2-D state space objects stateSpaceSE2, stateSpaceDubins, and stateSpaceReedsShepp, the state is a vector of form [x y theta], which defines the xy-position and orientation angle theta of a state in the state space.

For the 3-D state space object stateSpaceSE3, the state is a vector of form $[x \ y \ z \ qw \ qx \ qy \ qz]$, which defines the xyz-position and quaternion orientation $[qw \ qx \ qy \ qz]$ of a state in the state space.

Data Types: single | double

state2 — End state for interpolation

three-element vector of real values | seven-element vector of real values

End state for interpolation, specified as a three-element or seven-element vector of real values.

For the 2-D state space objects stateSpaceSE2, stateSpaceDubins, and stateSpaceReedsShepp, the state is a vector of form [x y theta], which defines the xy-position and orientation angle theta of a state in the state space.

For the 3-D state space object stateSpaceSE3, the state is a vector of form $[x \ y \ z \ qw \ qx \ qy \ qz]$, which defines the xyz-position and quaternion orientation $[qw \ qx \ qy \ qz]$ of a state in the state space.

Data Types: single | double

ratio — Interpolation ratio

scalar in range [0, 1] | *n*-element column vector of values in the range [0, 1]

Interpolation ratio, specified as a scalar in the range of [0, 1], or an n-element column vector of values in the range [0, 1]. n is the number of desired interpolation points.

Data Types: single | double

Output Arguments

interpStates — Interpolated states

n-by-3 matrix of real values | n-by-7 matrix of real values

Interpolated states, returned as an n-by-3 or n-by-7 matrix of real values. n is the number of interpolation points specified by the ratio input argument.

For the 2-D state space objects stateSpaceSE2, stateSpaceDubins, and stateSpaceReedsShepp, each row is of form [x y theta], which defines the xy-position and orientation angle theta of the interpolated states.

For the 3-D state space object stateSpaceSE3, each row is of form [x y z qw qx qy qz], which defines the xyz-position and quaternion orientation [qw qx qy qz] of the interpolated states.

Data Types: single | double

See Also

stateSpaceDubins | stateSpaceReedsShepp | stateSpaceSE2 | stateSpaceSE3

enforceStateBounds

Reduce state to state bounds

Syntax

boundedStates = enforceStateBounds(space, states)

Description

boundedStates = enforceStateBounds(space, states) reduces the specified states states to the state bounds in the StateBounds property of the specified state space object space.

Examples

Enforce State Bounds for SE(3) States

```
Create an SE(3) state space object.
```

```
space = stateSpaceSE3([-1 1; ...
    -2 2; ...
    -10 10; ...
    -inf inf; ...
    -inf inf; ...
    -inf inf; ...
    -inf inf])
space =
  stateSpaceSE3 with properties:
                  Name: 'SE3'
          StateBounds: [7x2 double]
    NumStateVariables: 7
            WeightXYZ: 1
     WeightQuaternion: 0.1000
Create a pair of states in 3-D space.
state1 = [2 10 3 2 0 0 0.8];
state2 = [223 100 3 2 2 12 5];
Enforce state bounds for a single state.
boundedState = enforceStateBounds(space,state1)
boundedState = 1 \times 7
```

2.0000

0

0

0.8000

Enforce state bounds for multiple states.

2.0000

3.0000

1.0000

boundedStates = enforceStateBounds(space,[state1; state2])

boundedStates = 2×7

1.0000	2.0000	3.0000	2.0000	0	0	0.8000
1.0000	2.0000	3.0000	2.0000	2.0000	12.0000	5.0000

Input Arguments

space — State space object

stateSpaceSE2 object | stateSpaceSE3 object | stateSpaceDubins object |
stateSpaceReedsShepp object

State space object, specified as a stateSpaceSE2, stateSpaceSE3, stateSpaceDubins, or stateSpaceReedsShepp object.

states — Unbounded states

n-by-3 matrix of real values | *n*-by-7 matrix of real values

Unbounded states, specified as an *n*-by-3 or *n*-by-7 matrix of real values.

For the 2-D state space objects stateSpaceSE2, stateSpaceDubins, and stateSpaceReedsShepp, each row is of form [x y theta], which defines the xy-position and orientation angle theta of a state in the state space.

For the 3-D state space object stateSpaceSE3, each row is of form [x y z qw qx qy qz], which defines the xyz-position and quaternion orientation [qw qx qy qz] of a state in the state space.

Data Types: single | double

Output Arguments

boundedStates — Bounded states

n-by-3 matrix of real values | *n*-by-7 matrix of real values

Bounded states, returned as an n-by-3 or n-by-7 matrix of real values. The value of n is same as for states input argument.

The function truncates each of the specified unbounded states to the bounds specified in the StateBounds property of the state space object space.

For the 2-D state space objects stateSpaceSE2, stateSpaceDubins, and stateSpaceReedsShepp, each row is of form [x y theta], which defines the xy-position and orientation angle theta of the bounded states.

For the 3-D state space object stateSpaceSE3, each row is of form [x y z qw qx qy qz], which defines the xyz-position and quaternion orientation [qw qx qy qz] of the bounded states.

Data Types: single | double

See Also

stateSpaceDubins | stateSpaceReedsShepp | stateSpaceSE2 | stateSpaceSE3

copy

Create deep copy of state space object

Syntax

```
space2 = copy(space1)
```

Description

space2 = copy(space1) creates a deep copy of the specified state space object.

Examples

Create Deep Copy of SE(3) State Space Object

```
Create a default SE(3) state space object.
```

```
space = stateSpaceSE3;
```

Specify weight for the quaternion distance in state space calculation.

```
space.WeightQuaternion = 2/3
space =
```

WeightQuaternion: 0.6667

Create a deep copy of the state space object.

Verify that the WeightQuaternion property values of the two state space objects are equal.

```
isequal(space.WeightQuaternion,space2.WeightQuaternion)
```

```
ans = logical
```

Input Arguments

space1 — State space object

stateSpaceSE2 object | stateSpaceSE3 object | stateSpaceDubins object |
stateSpaceReedsShepp object

State space object, specified as a stateSpaceSE2, stateSpaceSE3, stateSpaceDubins, or stateSpaceReedsShepp object.

Output Arguments

space2 — State space object

stateSpaceSE2 object | stateSpaceSE3 object | stateSpaceDubins object |
stateSpaceReedsShepp object

State space object, returned as a stateSpaceSE2, stateSpaceSE3, stateSpaceDubins, or stateSpaceReedsShepp object.

See Also

stateSpaceDubins | stateSpaceReedsShepp | stateSpaceSE2 | stateSpaceSE3

sampleGaussian

Sample state using Gaussian distribution

Syntax

```
state = sampleGaussian(space, meanState, stdDev)
state = sampleGaussian(space, meanState, stdDev, numSamples)
```

Description

state = sampleGaussian(space, meanState, stdDev) returns a sample state of the state space
based on a Gaussian (normal) distribution with specified mean, meanState, and standard deviation,
stdDev.

state = sampleGaussian(space, meanState, stdDev, numSamples) returns a number of state
samples. The number is equal to numSamples.

Input Arguments

space — State space object

spaceSE2 object | spaceDubins object | spaceReedsShepp object

State space object, specified as a stateSpaceSE2, a stateSpaceDubins, or a stateSpaceReedsShepp object.

Data Types: object

meanState — Mean state

3-element vector of real values

Mean state of the Gaussian distribution for sampling, specified as a 3-element vector of real values.

Example: [5 5 pi/3]

Data Types: single | double

stdDev — Standard deviation

3-element vector of nonnegative values

Standard deviation of the Gaussian distribution for sampling, specified as a 3-element vector of nonnegative values.

Example: [0.1 0.1 pi/18]
Data Types: single | double

numSamples — Number of samples

positive integer

Number of samples, specified as a positive integer.

Data Types: single | double

Output Arguments

state — State samples

N-by-3 real-valued matrix

State samples, returned as an N-by-3 real-valued matrix. N is the number of samples. Each row of the matrix corresponds to one incidence of state in the state space.

Data Types: single | double

See Also

stateSpaceDubins | stateSpaceReedsShepp | stateSpaceSE2

sampleUniform

Sample state using uniform distribution

Syntax

```
state = sampleUniform(space)
state = sampleUniform(space,numSamples)
state = sampleUniform(space,nearState,distVector,numSamples)
```

Description

state = sampleUniform(space) samples a state within the bounds in the StateBounds property
of the specified state space object space using a uniform probability distribution. For a
stateSpaceSE3 object, the state variables corresponding to orientation are bound to a unit
quaternion using a uniform distribution of random rotations.

state = sampleUniform(space, numSamples) returns a specified number of state samples
numSamples within the bounds of the state space object.

state = sampleUniform(space,nearState,distVector,numSamples) samples states in a
specified subregion of the bounds of the state space object. Specify the center of the sampling region
nearState and the distance from the center of the sampling region to its boundaries distVector.

Note The stateSpaceSE3 object does not support this syntax.

Examples

Sample State Using Uniform Distribution in SE(3)

```
Create an SE(3) state space.
```

Sample 3 states within full state bounds.

```
state = sampleUniform(space,3)
state = 3×7
```

6.2945	8.1158	-7.4603	0.6316	0.3078	-0.6921	-0.1654
8.2675	2.6472	-8.0492	-0.0834	-0.9448	0.2709	0.1641
-4.4300	0.9376	9.1501	0.5771	-0.5458	-0.5490	-0.2601

Input Arguments

space — State space object

stateSpaceSE2 object | stateSpaceSE3 object | stateSpaceDubins object |
stateSpaceReedsShepp object

State space object, specified as a stateSpaceSE2, stateSpaceSE3, stateSpaceDubins, or stateSpaceReedsShepp object.

numSamples — **Number of samples**

positive integer

Number of samples, specified as a positive integer.

Data Types: single | double

nearState — Center of sampling region

three-element vector of real values

Center of the sampling region, specified as a three-element vector of real values.

For the 2-D state space objects stateSpaceSE2, stateSpaceDubins, and stateSpaceReedsShepp, the state is a vector of form [x y theta], which defines the xy-position and orientation angle theta of a state in the state space.

Note The stateSpaceSE3 object does not support this argument.

Data Types: single | double

distVector — Distance of sampling region boundary from center

three-element vector of positive numbers

Distance of sampling region boundary from the center, specified as a three-element vector of positive numbers.

For the 2-D state space objects stateSpaceSE2, stateSpaceDubins, and stateSpaceReedsShepp, the state is a vector of form [x y theta], which defines the xy-position and orientation angle theta of a state in the state space.

Note The stateSpaceSE3 object does not support this argument.

Data Types: single | double

Output Arguments

state — State samples

n-by-3 matrix of real values | *n*-by-7 matrix of real values

State samples, returned as an *n*-by-3 or *n*-by-7 matrix of real values. *n* is the number of samples.

For the 2-D state space objects stateSpaceSE2, stateSpaceDubins, and stateSpaceReedsShepp, each row is of form [x y theta], which defines the xy-position and orientation angle theta of the sampled states.

For the 3-D state space object stateSpaceSE3, each row is of form $[x \ y \ z \ qw \ qx \ qz]$, which defines the xyz-position and quaternion orientation $[qw \ qx \ qy \ qz]$ of the sampled states.

Data Types: single | double

See Also

stateSpaceDubins | stateSpaceReedsShepp | stateSpaceSE2 | stateSpaceSE3

trajectoryGeneratorFrenet

Find optimal trajectory along reference path

Description

The trajectoryGeneratorFrenet object generates alternate trajectories using fourth or fifthorder polynomials relative to a given reference path. Each trajectory defines a motion between Frenet states over a specified time span.

Frenet states describe their position, velocity and acceleration relative to a static reference path, specified as a referencePathFrenet object.

The object expresses Frenet states as a vector of form [S dS ddS L dL ddL], where S is the arc length and L is the perpendicular deviation from the direction of the reference path. Derivatives of S are relative to time. Derivatives of L are relative to the arc length, S.



Frenet States: [s $\delta s \delta^2 s L \delta L \delta^2 L$]

To generate alternative trajectories, specify the initial and terminal frenet states with a given time span to the connect object function.

Creation

Syntax

connectorFrenet = trajectoryGeneratorFrenet(refPath)
connectorFrenet = trajectoryGeneratorFrenet(
refPath,'TimeResolution',timeValue)

Description

connectorFrenet = trajectoryGeneratorFrenet(refPath) generates trajectories between initial and terminal states relative to a reference path refPath specified as a referencePathFrenet object. The refPath input argument sets the ReferencePath property.

```
connectorFrenet = trajectoryGeneratorFrenet(
refPath,'TimeResolution',timeValue) specifies the time interval for discretization. The
timeValue argument sets the TimeResolution property.
```

Properties

TimeResolution — Discretization time interval between sampled Frenet states

```
0.1 (default) | positive scalar in seconds
```

Discretization time interval between sampled Frenet states, specified as a positive scalar in seconds. When using the connect object function, this property determines the resolution of the Times field of the generated trajectory structures, frenetTrajectory and globalTrajectory.

Data Types: double

ReferencePath — Reference path in Frenet coordinates

referencePathFrenet

Reference path in Frenet coordinates, specified as a referencePathFrenet object.

Object Functions

connect Connect initial and terminal Frenet states

Examples

Generate Alternative Trajectories for Reference Path

Generate alternative trajectories for a reference path using Frenet coordinates. Specify different initial and terminal states for your trajectories. Tune your states based on the generated trajectories.

Generate a reference path from a set of waypoints. Create a trajectoryGeneratorFrenet object from the reference path.

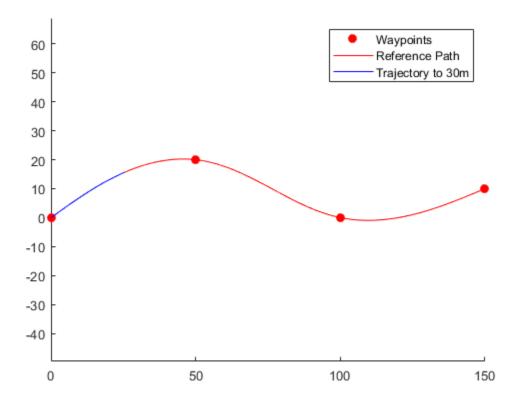
```
waypoints = [0 0; ...
50 20; ...
100 0; ...
150 10];
refPath = referencePathFrenet(waypoints);
connector = trajectoryGeneratorFrenet(refPath);
```

Generate a five-second trajectory between the path origin and a point 30 m down the path as Frenet states.

```
initState = [0 0 0 0 0 0]; % [S ds ddS L dL ddL]
termState = [30 0 0 0 0 0]; % [S ds ddS L dL ddL]
[~,trajGlobal] = connect(connector,initState,termState,5);
```

Display the trajectory in global coordinates.

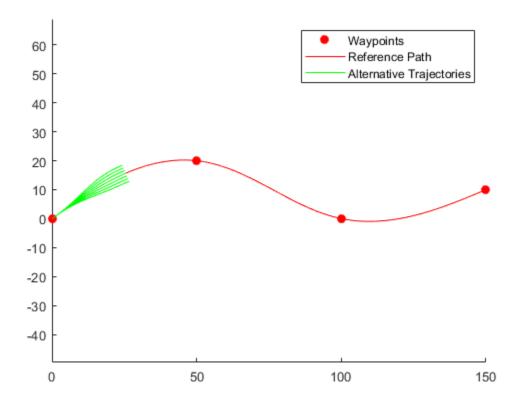
```
show(refPath);
hold on
axis equal
plot(trajGlobal.Trajectory(:,1),trajGlobal.Trajectory(:,2),'b')
legend(["Waypoints","Reference Path","Trajectory to 30m"])
```



Create a matrix of terminal states with lateral deviations between -3 m and 3 m. Generate trajectories that cover the same arc length in 10 seconds, but deviate laterally from the reference path. Display the new alternative paths.

```
termStateDeviated = termState + ([-3:3]' * [0 0 0 1 0 0]);
[~,trajGlobal] = connect(connector,initState,termStateDeviated,5);

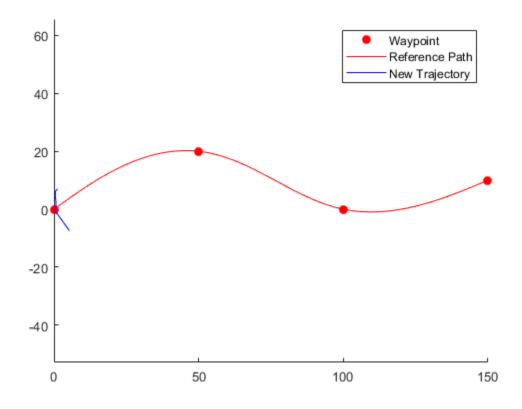
clf
show(refPath);
hold on
axis equal
for i = 1:length(trajGlobal)
    plot(trajGlobal(i).Trajectory(:,1),trajGlobal(i).Trajectory(:,2),'g')
end
legend(["Waypoints","Reference Path","Alternative Trajectories"])
hold off
```



Specify a new terminal state to generate a new trajectory. This trajectory is not desirable because it requires reverse motion to achieve a lateral velocity of 10 m/s.

```
newTermState = [5 10 0 5 0 0];
[~,newTrajGlobal] = connect(connector,initState,newTermState,3);

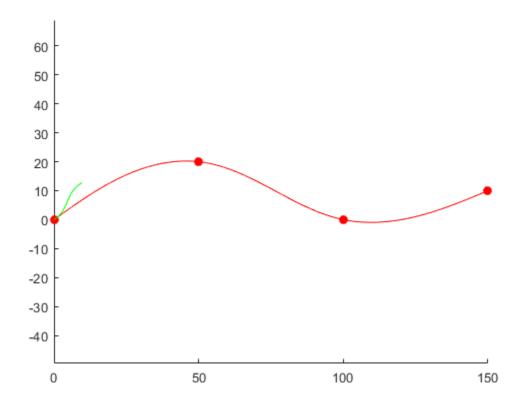
clf
show(refPath);
hold on
axis equal
plot(newTrajGlobal.Trajectory(:,1),newTrajGlobal.Trajectory(:,2),'b');
legend(["Waypoint","Reference Path","New Trajectory"])
hold off
```



Relax the restriction on the longitudinal state by specifying an arc length of NaN. Generate and display the trajectory again. The new position shows a good alternative trajectory that deviates off the reference path.

```
relaxedTermState = [NaN 10 0 5 0 0];
[~,trajGlobalRelaxed] = connect(connector,initState,relaxedTermState,3);

clf
show(refPath);
hold on
axis equal
plot(trajGlobalRelaxed.Trajectory(:,1),trajGlobalRelaxed.Trajectory(:,2),'g');
hold off
```



Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

Objects

referencePathFrenet

Functions

closestPoint | connect | frenet2global | global2frenet | interpolate | show

Topics

"Highway Trajectory Planning Using Frenet Reference Path"

Introduced in R2020b

connect

Connect initial and terminal Frenet states

Syntax

```
frenetTrajectory = connect(connectorFrenet,initialState,terminalState,
timeSpan)
[____,globalTrajectory] = connect(____)
```

Description

frenetTrajectory = connect(connectorFrenet,initialState,terminalState,
timeSpan) connects the specified initial Frenet states to the specified terminal states over a span of
time in seconds. This object function supports 1-to-n, n-to-1, or n-to-n pairwise trajectory connections.

[____,globalTrajectory] = connect(____) returns the trajectories in global coordinates in addition to all arguments in the previous syntax.

Examples

Generate Alternative Trajectories for Reference Path

Generate alternative trajectories for a reference path using Frenet coordinates. Specify different initial and terminal states for your trajectories. Tune your states based on the generated trajectories.

Generate a reference path from a set of waypoints. Create a trajectoryGeneratorFrenet object from the reference path.

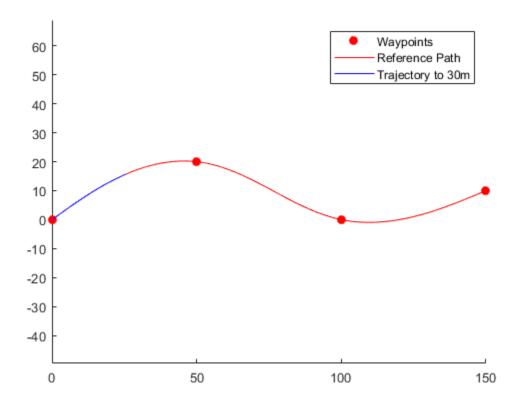
```
waypoints = [0 0; ...
50 20; ...
100 0; ...
150 10];
refPath = referencePathFrenet(waypoints);
connector = trajectoryGeneratorFrenet(refPath);
```

Generate a five-second trajectory between the path origin and a point 30 m down the path as Frenet states.

```
initState = [0 0 0 0 0 0]; % [S ds ddS L dL ddL]
termState = [30 0 0 0 0 0]; % [S ds ddS L dL ddL]
[~,trajGlobal] = connect(connector,initState,termState,5);
```

Display the trajectory in global coordinates.

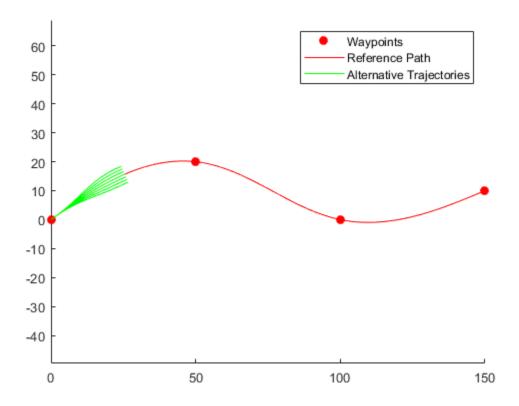
```
show(refPath);
hold on
axis equal
plot(trajGlobal.Trajectory(:,1),trajGlobal.Trajectory(:,2),'b')
legend(["Waypoints","Reference Path","Trajectory to 30m"])
```



Create a matrix of terminal states with lateral deviations between -3 m and 3 m. Generate trajectories that cover the same arc length in 10 seconds, but deviate laterally from the reference path. Display the new alternative paths.

```
termStateDeviated = termState + ([-3:3]' * [0 0 0 1 0 0]);
[~,trajGlobal] = connect(connector,initState,termStateDeviated,5);

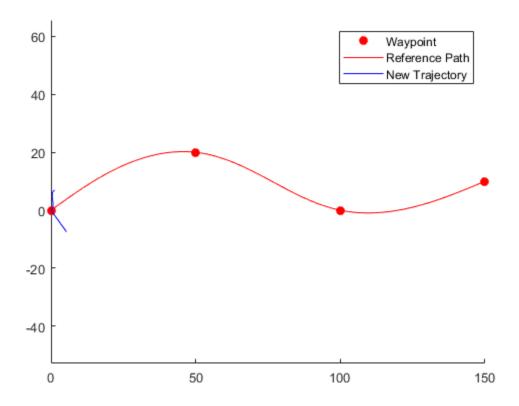
clf
show(refPath);
hold on
axis equal
for i = 1:length(trajGlobal)
    plot(trajGlobal(i).Trajectory(:,1),trajGlobal(i).Trajectory(:,2),'g')
end
legend(["Waypoints","Reference Path","Alternative Trajectories"])
hold off
```



Specify a new terminal state to generate a new trajectory. This trajectory is not desirable because it requires reverse motion to achieve a lateral velocity of 10 m/s.

```
newTermState = [5 10 0 5 0 0];
[~,newTrajGlobal] = connect(connector,initState,newTermState,3);

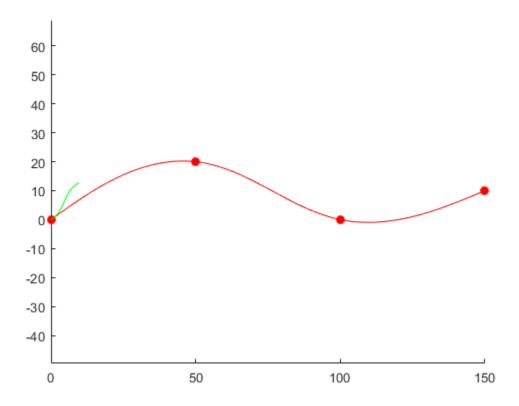
clf
show(refPath);
hold on
axis equal
plot(newTrajGlobal.Trajectory(:,1),newTrajGlobal.Trajectory(:,2),'b');
legend(["Waypoint","Reference Path","New Trajectory"])
hold off
```



Relax the restriction on the longitudinal state by specifying an arc length of NaN. Generate and display the trajectory again. The new position shows a good alternative trajectory that deviates off the reference path.

```
relaxedTermState = [NaN 10 0 5 0 0];
[~,trajGlobalRelaxed] = connect(connector,initState,relaxedTermState,3);

clf
show(refPath);
hold on
axis equal
plot(trajGlobalRelaxed.Trajectory(:,1),trajGlobalRelaxed.Trajectory(:,2),'g');
hold off
```



Input Arguments

connectorFrenet — Frenet trajectory generator

trajectoryGeneratorFrenet object

Frenet trajectory generator, specified as a trajectoryGeneratorFrenet object.

initialState — Initial Frenet states

n-by-6 numeric matrix

Initial Frenet states, specified as an n-by-6 numeric matrix. Each row of the matrix is a set of Frenet coordinates for the initial state of a trajectory in the form [S dS ddS L dL ddL]. The value of n must be equal to the number of rows in the terminalState argument or 1.

terminalState — Final Frenet states

n-by-6 numeric matrix

Final Frenet states, specified as an n-by-6 numeric matrix. Each row of the matrix is a set of Frenet coordinates for the initial state of a trajectory in the form [S dS ddS L dL ddL]. The value of n must be equal to the number of rows in the initialState argument or 1.

timeSpan — Time horizon for all trajectories

positive scalar in seconds

Time horizon for all trajectories, specified as a positive scalar in seconds. The generated trajectories are sampled evenly across this time span based on the TimeResolution property of the trajectoryGeneratorFrenet object specified in the connectorFrenet argument.

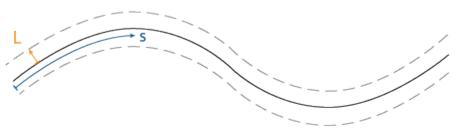
Output Arguments

frenetTrajectory — Frenet trajectories

structure | structure array

Frenet trajectories between all initial and final states, returned as a structure array with these fields:

- Trajectory n-by-6 numeric matrix. Each row of the matrix is a set of Frenet coordinates for the initial state of a trajectory in the form [S dS ddS L dL ddL].
- Time Vector of positive scalars from 0 to timeSpan in seconds.



Frenet States: [s $\delta s \delta^2 s L \delta L \delta^2 L$]

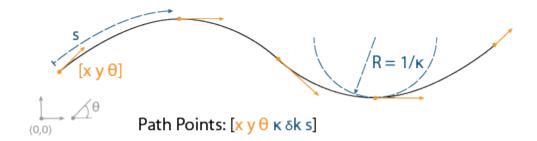
This function supports 1-to-*n*, *n*-to-1, or *n*-to-*n* pairwise trajectory connections based on the number of rows of initialState and terminalState.

globalTrajectory — Global trajectories

structure | structure array

Global trajectories between all initial and final states, returned as structure or structure array with fields:

- Trajectory *n*-by-6 numeric matrix. Each row of the matrix is a set of global sates of the form [x y theta kappa dkappa s].
- Time Vector of positive scalars from 0 to timeSpan in seconds.



This function supports 1-to-n, n-to-1, or n-to-n pairwise trajectory connections based on the number of rows of initialState and terminalState.

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

Objects

referencePathFrenet | trajectoryGeneratorFrenet

Functions

closestPoint | frenet2global | global2frenet | interpolate | show

Topics

"Highway Trajectory Planning Using Frenet Reference Path"

Introduced in R2020b

trajectoryOptimalFrenet

Find optimal trajectory along reference path

Description

The trajectoryOptimalFrenet object is a path planner which samples and evaluates local trajectories based on a reference path. The planner generates a set of terminal states based on the reference path and other parameters in the object. The planner then connects the state to each terminal state using 4^{th} or 5^{th} order polynomials. To choose an optimal path, sampled trajectories are evaluated for kinematic feasibility, collision, and cost.

Creation

Syntax

```
trajectoryOptimalFrenet(refPath,validator)
planner = trajectoryOptimalFrenet(____,Name,Value)
```

Description

trajectoryOptimalFrenet(refPath, validator) creates a trajectoryOptimalFrenet object with reference path, refPath, in the form of an n-by-2 array of $[x \ y]$ waypoints and a state validator, validator, specified as a validatorOccupancyMap object.

planner = trajectoryOptimalFrenet(____, Name, Value) sets additional properties using one
or more name-value pairs in any order.

Input Arguments

refPath - Reference path

n-by-2 matrix

Reference path, specified as an n-by-2 matrix of $[x \ y]$ pairs, where n is the number of waypoints.

Example: [100,100;400,400]

Data Types: double

validator — State validator object

validatorOccupancyMap object

State validator object, specified as a validator Occupancy Map object.

Properties

Note For the 'Weights' and 'FeasibilityParameters' properties, you cannot specify the entire structures at once. Instead, set their fields individually as name-value pairs. For example,

trajectoryOptimalFrenet(refPath, validator, 'Deviation',0) sets the 'Deviation' field
of the structure 'Weights'.

Weights — Weights for all trajectory costs

structure

The weights for all trajectory costs, specified as a structure containing scalars for the cost multipliers of the corresponding trajectory attributes. The total trajectory cost is a sum of all attributes multiplied by their weights. The structure has the these fields.

Time — Weight for time cost

0 (default) | positive scalar

The cost function multiplies the weight by the total time taken to reach the terminal state. Specify this value as the comma-separated pair of 'Time' and a positive scalar in seconds.

Data Types: double

ArcLength — Weight for arc length cost

0 (default) | positive scalar

The cost function multiplies the weight by the total length of the generated trajectories. Specify this value as the comma-separated pair of 'ArcLength' and a positive scalar in meters.

Data Types: double

LateralSmoothness — Weight for lateral jerk cost

0 (default) | positive scalar

The cost function multiplies the weight by the integral of lateral jerk squared. This value determines the aggressiveness of the trajectory in the lateral direction (perpendicular to the reference path). Specify this value as the comma-separated pair of 'LateralSmoothness' and a positive scalar. To penalize lateral jerk in the planned trajectory increase this cost value.

Data Types: double

LongitudinalSmoothness — Weight for longitudinal jerk cost

0 (default) | positive scalar

The cost function multiplies the weight by the integral of longitudinal jerk squared. This value determines the aggressiveness of the trajectories in the longitudinal direction (direction of the reference path). Specify this value as the comma-separated pair of 'LongitudinalSmoothness' and a positive scalar. To penalize large change in forward and backward acceleration increase this cost value.

Data Types: double

Deviation — Weight for deviation from reference path

1 (default) | positive scalar

The cost function multiplies the weight by the perpendicular distance from the reference path at the end of the trajectory in meters. Specify this value as the comma-separated pair of 'Deviation' and a positive scalar in meters.

Data Types: double

Data Types: struct

FeasibilityParameters — Structure containing feasibility parameters

structure

Feasibility parameters, specified as a structure containing scalar values to check the validity of a trajectory. The structure has the these fields.

MaxCurvature — Maximum curvature that vehicle can execute

0.1 (default) | positive real scalar

Maximum curvature that the vehicle can execute. Specify this value as the comma-separated pair of 'MaxCurvature' and a positive real scalar in m⁻¹. This value determines the kinematic feasibility of the trajectory.

Data Types: double

MaxAcceleration — Maximum acceleration in direction of motion of vehicle

2.5 (default) | positive real scalar

Maximum acceleration in the direction of motion of the vehicle. Specify this value as the commaseparated pair of 'MaxAcceleration' and a positive real scalar in m/s². To lower the limit on the acceleration of the vehicle in the forward or reverse direction decrease this value.

Data Types: double
Data Types: struct

TimeResolution — Trajectory discretization interval

0.1 (default) | positive real scalar

Time interval between discretized states of the trajectory. Specify this value as the comma-separated pair of 'TimeResolution' and a positive real scalar in seconds. These discretized states determine state validity and cost function.

Data Types: double

CostFunction — User-defined cost function

nullCost (default) | function handle

The user-defined cost function, specified as a function handle. The function must accept a matrix of *n*-by-7 states, TRAJSTATES, for each trajectory and return a cost value as a scalar. The plan function returns the path with the lowest cost.

For example, leftLaneChangeCost = @(states)((states(end,2) < refPath(end,2))*10) creates a cost function handle to prioritize left lane changes.

Data Types: function handle

TrajectoryList — List of all possible trajectories

structure array

This property is read-only.

The 'TrajectoryList' property, returned as a structure array of all the candidate trajectories and their corresponding parameters. Each structure has the these fields:

- Trajectory An n-by-7 matrix of [x, y, theta, kappa, speed, acceleration, time], where <math>n is the number of trajectory waypoints.
- Cost Cost of the trajectory.
- MaxAcceleration Maximum acceleration of the trajectory.
- MaxCurvature Maximum curvature of the trajectory.
- Feasible A four-element vector [velocity, acceleration, curvature, collision] indicating the validity of the trajectory.

The value of the elements can be either,

- 1 The trajectory is valid.
- 0 The trajectory is invalid.
- -1 The trajectory is not checked.

Data Types: struct

TerminalStates — Structure of all goal states

structure

A structure that contains a list of goal states relative to the reference path. These parameters define the sampling behavior for generating alternative trajectory segments between start and each goal state. The structure has the these fields.

Longitudinal — Lengths of the trajectory segment

30:15:90 (default) | vector

Lengths of the trajectory segment, specified as a vector in meters.

Data Types: double

Lateral — Array of deviations from reference path in perpendicular direction at goal state -2:1:2 (default) | vector

Array of deviations from reference path in perpendicular direction at goal state, specified as a vector in meters.

Data Types: double

Speed — Velocity at goal state in direction of motion

10 (default) | positive scalar

Velocity at the goal state in the direction of motion, specified as a positive scalar in m/s.

Data Types: double

Acceleration — Acceleration at goal state in direction of motion

0 (default) | positive scalar

Acceleration at the goal state in the direction of motion, specified as a positive scalar in m/s².

Data Types: double

Time — Array of end-times for executing trajectory segment

7 (default) | positive vector

Array of end-times for executing the trajectory segment, specified as a positive vector in seconds.

Data Types: double
Data Types: struct

Waypoints — Waypoints of reference path

[] (default) | *n*-by-2 matrix

Waypoints of reference path, specified as an n-by-2 matrix of $[x \ y]$ pairs, where n is the number of waypoints. Waypoints act as a reference for planning alternative trajectories optimized by this planner.

Data Types: double

NumSegments — Number of longitudinal segments for each trajectory

1 (default) | positive scalar

Number of longitudinal segments for each trajectory. Specify this value as the comma-separated pair of 'NumSegments' and a positive scalar. This property generates intermediate longitudinal terminal states to which all lateral terminal states are combined with for generating more motion primitives to each terminal state.

For example, 'NumSegments', 2 creates two partitions between each longitudinal terminal state. Trajectories are generated to reach the intermediate longitudinal states with all the available lateral terminal states.

Data Types: double

DeviationOffset — Deviation offset from reference path in lateral direction

0 (default) | scalar

Deviation offset from the reference path in the lateral direction. Specify this value as the comma-separated pair of 'DeviationOffset' and a scalar. A negative value offset the deviation to the right, and a positive value offset the deviation to the left of the reference path in the lateral direction. Set this property to bias your solution to a certain turn direction when avoiding obstacles in the reference path.

Data Types: double

Object Functions

cart2frenet Convert Cartesian states to Frenet states

copy Create deep copy of object

frenet2cart Convert Frenet states to Cartesian states

plan Plan optimal trajectory show Visualize trajectories

Examples

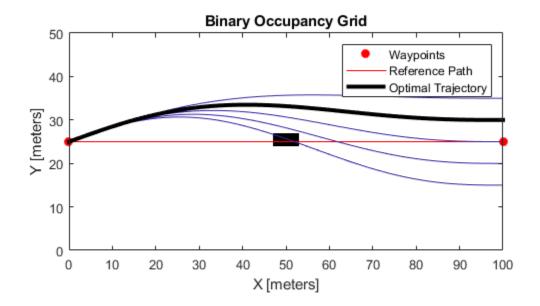
Optimal Trajectory Planning in Frenet Space

This example shows how to plan an optimal trajectory using a trajectoryOptimalFrenet object.

Create and Assign Map to State Validator

show(planner, 'Trajectory', 'all')

```
Create a state validator object for collision checking.
stateValidator = validatorOccupancyMap;
Create an obstacle grid map.
grid = zeros(50,100);
grid(24:26,48:53) = 1;
Create a binaryOccupancyMap with the grid map.
map = binaryOccupancyMap(grid);
Assign the map to the state validator.
stateValidator.Map = map;
Plan and Visualize Trajectory
Create a reference path for the planner to follow.
refPath = [0,25;100,25];
Initialize the planner object with the reference path, and the state validator.
planner = trajectoryOptimalFrenet(refPath,stateValidator);
Assign longitudinal terminal state, lateral deviation, and maximum acceleration values.
planner.TerminalStates.Longitudinal = 100;
planner.TerminalStates.Lateral = -10:5:10;
planner.FeasibilityParameters.MaxAcceleration = 10;
Specify the deviation offset value close to the left lateral terminal state to prioritize left lane changes.
planner.DeviationOffset = 5;
Trajectory Planning
Initial cartesian state of vehicle.
initCartState = [0 25 pi/9 0 0 0];
Convert cartesian state of vehicle to Frenet state.
initFrenetState = cart2frenet(planner,initCartState);
Plan a trajectory from initial Frenet state.
plan(planner,initFrenetState);
Trajectory Visualization
Visualize the map and the trajectories.
show(map)
hold on
```



Partitioning Longitudinal Terminal States in Trajectory Generation

This example shows how to partition the longitudinal terminal states in optimal trajectory planning using a trajectoryOptimalFrenet object.

Create and Assign Map to State Validator

Create a state validator object for collision checking.

```
statevalidator = validatorOccupancyMap;
```

Create an obstacle grid map.

```
grid = zeros(50,100);
grid(25:27,28:33) = 1;
grid(16:18,37:42) = 1;
grid(29:31,72:77) = 1;
```

Create a binaryOccupancyMap with the grid map.

```
map = binaryOccupancyMap(grid);
```

Assign the map to the state validator.

```
statevalidator.Map = map;
```

Plan and Visualize Trajectory

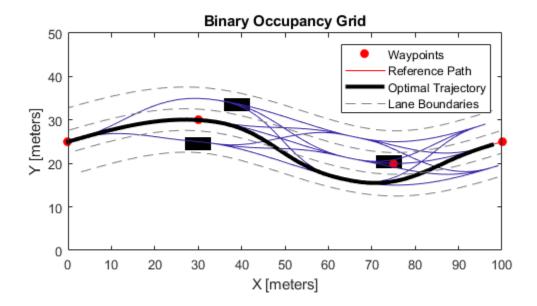
```
Create a reference path for the planner to follow.
refPath = [0,25;30,30;75,20;100,25];
Initialize the planner object with the reference path, and the state validator.
planner = trajectoryOptimalFrenet(refPath, statevalidator);
Assign longitudinal terminal state, lateral deviation, and maximum acceleration values.
planner.TerminalStates.Longitudinal = 100;
planner.TerminalStates.Lateral = -5:5:5;
planner.FeasibilityParameters.MaxAcceleration = 10;
Assign the number of partitions for the longitudinal terminal state.
planner.NumSeaments = 3:
Trajectory Planning
Initial Frenet state of vehicle.
initFrenetState = zeros(1,6);
Plan a trajectory from initial Frenet state.
plan(planner,initFrenetState);
Trajectory Visualization
Visualize the map and the trajectories.
show(map)
hold on
show(planner, 'Trajectory', 'all')
hold on
Generate Lane Boundaries
Calculate end of reference path as Frenet state.
refPathEnd = cart2frenet(planner,[planner.Waypoints(end,:) 0 0 0 0]);
Calculate lane offsets on both sides of the lateral terminal states with half lane width value.
laneOffsets = unique([planner.TerminalStates.Lateral+2.5 planner.TerminalStates.Lateral-2.5]);
Calculate positions of lanes in Cartesian state.
numLaneOffsets = numel(laneOffsets);
xRefPathEnd = ceil(refPathEnd(1));
laneXY = zeros((numLaneOffsets*xRefPathEnd)+numLaneOffsets,2);
xIndex = 0;
for laneID = 1:numLaneOffsets
    for x = 1:xRefPathEnd
```

laneCart = frenet2cart(planner,[x 0 0 laneOffsets(laneID) 0 0]);

```
xIndex = xIndex + 1;
laneXY(xIndex,:) = laneCart(1:2);
end
xIndex = xIndex + 1;
laneXY(xIndex,:) = NaN(1,2);
end
```

Plot lane boundaries.

```
plot(laneXY(:,1),laneXY(:,2),'LineWidth',0.5,'Color',[0.5 0.5 0.5],'DisplayName','Lane Boundarie
```



Limitations

- Self-intersections in the reference path can lead to unexpected behavior.
- The planner does not support reverse driving.
- Initial orientation for planning should be within -pi/2 and pi/2 to the reference path.
- Limit the number of TerminalStates for real-time applications since computational complexity grows with it.

References

[1] Werling, Moritz, Julius Ziegler, Sören Kammel, and Sebastian Thrun. "Optimal Trajectory Generation for Dynamic Street Scenarios in a Frenet Frame." 2010 IEEE International Conference on Robotics and Automation. 2010, pp. 987–993.

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

nav.StateValidator|plannerHybridAStar|validatorOccupancyMap

Introduced in R2019b

cart2frenet

Convert Cartesian states to Frenet states

Syntax

cart2frenet(planner,cartesianStates)

Description

cart2frenet(planner, cartesianStates) converts a six-element vector of cartesianStates [x, y, theta, kappa, speed, acceleration] to a six-element vector of Frenet states [s, ds/dt, d^2s/dt^2 , l, dl/ds, d^2l/ds^2], where s is arc length from the first point in reference path, and l is normal distance from the closest point at s on the reference path.

Examples

Optimal Trajectory Planning in Frenet Space

This example shows how to plan an optimal trajectory using a trajectoryOptimalFrenet object.

Create and Assign Map to State Validator

```
Create a state validator object for collision checking.
```

```
stateValidator = validatorOccupancyMap;
```

Create an obstacle grid map.

```
grid = zeros(50,100);

grid(24:26,48:53) = 1;
```

Create a binaryOccupancyMap with the grid map.

```
map = binaryOccupancyMap(grid);
```

Assign the map to the state validator.

```
stateValidator.Map = map;
```

Plan and Visualize Trajectory

Create a reference path for the planner to follow.

```
refPath = [0,25;100,25];
```

Initialize the planner object with the reference path, and the state validator.

```
planner = trajectoryOptimalFrenet(refPath, stateValidator);
```

Assign longitudinal terminal state, lateral deviation, and maximum acceleration values.

```
planner.TerminalStates.Longitudinal = 100;
planner.TerminalStates.Lateral = -10:5:10;
planner.FeasibilityParameters.MaxAcceleration = 10;

Specify the deviation offset value close to the left lateral terminal state to prioritize left lane changes.
planner.DeviationOffset = 5;

Trajectory Planning
Initial cartesian state of vehicle.
initCartState = [0 25 pi/9 0 0 0];

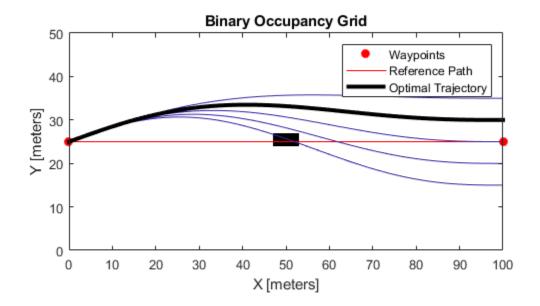
Convert cartesian state of vehicle to Frenet state.
initFrenetState = cart2frenet(planner,initCartState);
Plan a trajectory from initial Frenet state.
plan(planner,initFrenetState);

Trajectory Visualization

Visualize the map and the trajectories.
show(map)
```

hold on

show(planner, 'Trajectory', 'all')



Partitioning Longitudinal Terminal States in Trajectory Generation

This example shows how to partition the longitudinal terminal states in optimal trajectory planning using a trajectoryOptimalFrenet object.

Create and Assign Map to State Validator

Create a state validator object for collision checking.

```
statevalidator = validatorOccupancyMap;
```

Create an obstacle grid map.

```
grid = zeros(50,100);
grid(25:27,28:33) = 1;
grid(16:18,37:42) = 1;
grid(29:31,72:77) = 1;
```

Create a binaryOccupancyMap with the grid map.

```
map = binaryOccupancyMap(grid);
```

Assign the map to the state validator.

```
statevalidator.Map = map;
```

Plan and Visualize Trajectory

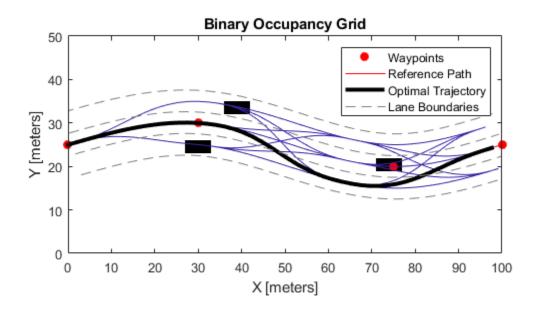
```
Create a reference path for the planner to follow.
refPath = [0,25;30,30;75,20;100,25];
Initialize the planner object with the reference path, and the state validator.
planner = trajectoryOptimalFrenet(refPath, statevalidator);
Assign longitudinal terminal state, lateral deviation, and maximum acceleration values.
planner.TerminalStates.Longitudinal = 100;
planner.TerminalStates.Lateral = -5:5:5;
planner.FeasibilityParameters.MaxAcceleration = 10;
Assign the number of partitions for the longitudinal terminal state.
planner.NumSeaments = 3:
Trajectory Planning
Initial Frenet state of vehicle.
initFrenetState = zeros(1,6);
Plan a trajectory from initial Frenet state.
plan(planner,initFrenetState);
Trajectory Visualization
Visualize the map and the trajectories.
show(map)
hold on
show(planner, 'Trajectory', 'all')
hold on
Generate Lane Boundaries
Calculate end of reference path as Frenet state.
refPathEnd = cart2frenet(planner,[planner.Waypoints(end,:) 0 0 0 0]);
Calculate lane offsets on both sides of the lateral terminal states with half lane width value.
laneOffsets = unique([planner.TerminalStates.Lateral+2.5 planner.TerminalStates.Lateral-2.5]);
Calculate positions of lanes in Cartesian state.
numLaneOffsets = numel(laneOffsets);
xRefPathEnd = ceil(refPathEnd(1));
laneXY = zeros((numLaneOffsets*xRefPathEnd)+numLaneOffsets,2);
xIndex = 0;
for laneID = 1:numLaneOffsets
    for x = 1:xRefPathEnd
```

laneCart = frenet2cart(planner,[x 0 0 laneOffsets(laneID) 0 0]);

```
xIndex = xIndex + 1;
laneXY(xIndex,:) = laneCart(1:2);
end
xIndex = xIndex + 1;
laneXY(xIndex,:) = NaN(1,2);
end
```

Plot lane boundaries.

```
plot(laneXY(:,1),laneXY(:,2),'LineWidth',0.5,'Color',[0.5 0.5 0.5],'DisplayName','Lane Boundarie
```



Input Arguments

planner — Optimal trajectory planner in Frenet space

trajectoryOptimalFrenet object

Optimal trajectory planner in Frenet space, specified as a trajectoryOptimalFrenet object.

cartesianStates — Vector of Cartesian states

six-element vector

Vector of Cartesian states, specified as a 1-by-6 vector [x, y, theta, kappa, speed, acceleration].

• *x* and *y* specify the position in meters.

- theta specifies the orientation angle in radians.
- *kappa* specifies the curvature in m⁻¹.
- *speed* specifies the velocity in m/s.
- acceleration specifies the acceleration in m/s^2 .

Example: [110 110 pi/4 0 0 0]

Data Types: double

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

frenet2cart | trajectoryOptimalFrenet

Introduced in R2019b

copy

Create deep copy of object

Syntax

plannerCopy = copy(planner)

Description

plannerCopy = copy(planner) creates a deep copy of the trajectoryOptimalFrenet object
with the same properties.

Input Arguments

planner — Trajectory optimal Frenet object

trajectoryOptimalFrenet object

Trajectory optimal Frenet object, specified as a trajectoryOptimalFrenet object.

Output Arguments

plannerCopy — Copy of trajectory optimal Frenet object

trajectoryOptimalFrenet object

Copy of trajectory optimal Frenet object, returned as a trajectoryOptimalFrenet object with the same properties.

See Also

trajectoryOptimalFrenet

Introduced in R2020b

frenet2cart

Convert Frenet states to Cartesian states

Syntax

```
frenet2cart(planner, frenetStates)
```

Description

```
frenet2cart(planner, frenetStates) converts a six-element vector of frenetStates [s, ds/dt, d^2s/dt^2, l, dl/ds, d^2l/ds^2] to a six-element vector of Cartesian states [x, y, theta, kappa, speed, acceleration].
```

Examples

Optimal Trajectory Planning in Frenet Space

This example shows how to plan an optimal trajectory using a trajectoryOptimalFrenet object.

Create and Assign Map to State Validator

```
Create a state validator object for collision checking.
```

```
stateValidator = validatorOccupancyMap;
```

Create an obstacle grid map.

```
grid = zeros(50,100);

grid(24:26,48:53) = 1;
```

Create a binaryOccupancyMap with the grid map.

```
map = binaryOccupancyMap(grid);
```

Assign the map to the state validator.

```
stateValidator.Map = map;
```

Plan and Visualize Trajectory

Create a reference path for the planner to follow.

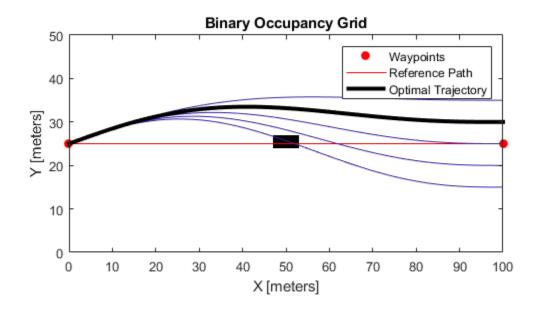
```
refPath = [0,25;100,25];
```

Initialize the planner object with the reference path, and the state validator.

```
planner = trajectoryOptimalFrenet(refPath,stateValidator);
```

Assign longitudinal terminal state, lateral deviation, and maximum acceleration values.

```
planner.TerminalStates.Longitudinal = 100;
planner.TerminalStates.Lateral = -10:5:10;
planner.FeasibilityParameters.MaxAcceleration = 10;
Specify the deviation offset value close to the left lateral terminal state to prioritize left lane changes.
planner.DeviationOffset = 5;
Trajectory Planning
Initial cartesian state of vehicle.
initCartState = [0 25 pi/9 0 0 0];
Convert cartesian state of vehicle to Frenet state.
initFrenetState = cart2frenet(planner,initCartState);
Plan a trajectory from initial Frenet state.
plan(planner,initFrenetState);
Trajectory Visualization
Visualize the map and the trajectories.
show(map)
hold on
show(planner, 'Trajectory', 'all')
```



Partitioning Longitudinal Terminal States in Trajectory Generation

This example shows how to partition the longitudinal terminal states in optimal trajectory planning using a trajectoryOptimalFrenet object.

Create and Assign Map to State Validator

Create a state validator object for collision checking.

```
statevalidator = validatorOccupancyMap;
```

Create an obstacle grid map.

```
grid = zeros(50,100);
grid(25:27,28:33) = 1;
grid(16:18,37:42) = 1;
grid(29:31,72:77) = 1;
```

Create a binaryOccupancyMap with the grid map.

```
map = binaryOccupancyMap(grid);
```

Assign the map to the state validator.

```
statevalidator.Map = map;
```

Plan and Visualize Trajectory

Create a reference path for the planner to follow.

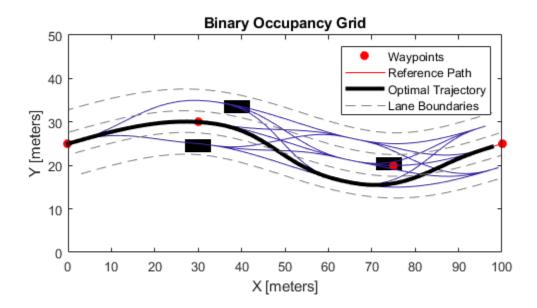
```
refPath = [0,25;30,30;75,20;100,25];
Initialize the planner object with the reference path, and the state validator.
planner = trajectoryOptimalFrenet(refPath, statevalidator);
Assign longitudinal terminal state, lateral deviation, and maximum acceleration values.
planner.TerminalStates.Longitudinal = 100;
planner.TerminalStates.Lateral = -5:5:5;
planner.FeasibilityParameters.MaxAcceleration = 10;
Assign the number of partitions for the longitudinal terminal state.
planner.NumSegments = 3;
Trajectory Planning
Initial Frenet state of vehicle.
initFrenetState = zeros(1,6);
Plan a trajectory from initial Frenet state.
plan(planner,initFrenetState);
Trajectory Visualization
Visualize the map and the trajectories.
show(map)
hold on
show(planner, 'Trajectory', 'all')
hold on
Generate Lane Boundaries
Calculate end of reference path as Frenet state.
refPathEnd = cart2frenet(planner,[planner.Waypoints(end,:) 0 0 0 0]);
Calculate lane offsets on both sides of the lateral terminal states with half lane width value.
laneOffsets = unique([planner.TerminalStates.Lateral+2.5 planner.TerminalStates.Lateral-2.5]);
Calculate positions of lanes in Cartesian state.
numLaneOffsets = numel(laneOffsets);
xRefPathEnd = ceil(refPathEnd(1));
laneXY = zeros((numLaneOffsets*xRefPathEnd)+numLaneOffsets,2);
xIndex = 0;
for laneID = 1:numLaneOffsets
    for x = 1:xRefPathEnd
```

laneCart = frenet2cart(planner,[x 0 0 laneOffsets(laneID) 0 0]);

```
xIndex = xIndex + 1;
laneXY(xIndex,:) = laneCart(1:2);
end
xIndex = xIndex + 1;
laneXY(xIndex,:) = NaN(1,2);
end
```

Plot lane boundaries.

```
plot(laneXY(:,1),laneXY(:,2),'LineWidth',0.5,'Color',[0.5 0.5 0.5],'DisplayName','Lane Boundarie
```



Input Arguments

planner — Optimal trajectory planner in Frenet space

trajectoryOptimalFrenet object

Optimal trajectory planner in Frenet space, specified as a trajectoryOptimalFrenet object.

frenetStates — Vector of Frenet states

six-element vector

Vector of Frenet states, specified as a 1-by-6 vector, $[s, ds/dt, d^2s/dt^2, l, dl/ds, d^2l/ds^2]$.

- *s* specifies the arc length from the first point in reference path in meters.
- *ds/dt* specifies the first derivative of arc length.

- d^2s/dt^2 specifies the second derivative of arc length.
- *l* specifies the normal distance from the closest point in the reference path in meters.
- dl/ds specifies the first derivative of normal distance.
- d^2l/ds^2 specifies the second derivative of normal distance.

Example: [10 1 0 3 0 0]

Data Types: double

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

cart2frenet|trajectoryOptimalFrenet

Introduced in R2019b

plan

Plan optimal trajectory

Syntax

```
[traj,index,cost,flag] = plan(planner,start)
```

Description

[traj,index,cost,flag] = plan(planner,start) computes a feasible trajectory, traj, from a list of candidate trajectories generated from the trajectoryOptimalFrenet object, planner. start is specified as a six-element vector [s, ds/dt, d^2s/dt^2 , l, dl/ds, d^2l/ds^2], where s is the arc length from the first point in the reference path, and l is normal distance from the closest point at s on the reference path.

The output trajectory, traj, also has an associated cost and index for the TrajectoryList property of the planner. flag is a numeric exit flag indicating status of the solution.

To improve the results of the planning output, modify the parameters on the planner object.

Examples

Optimal Trajectory Planning in Frenet Space

This example shows how to plan an optimal trajectory using a trajectoryOptimalFrenet object.

Create and Assign Map to State Validator

```
Create a state validator object for collision checking.
```

```
stateValidator = validatorOccupancyMap;
```

Create an obstacle grid map.

```
grid = zeros(50,100);

grid(24:26,48:53) = 1;
```

Create a binaryOccupancyMap with the grid map.

```
map = binaryOccupancyMap(grid);
```

Assign the map to the state validator.

```
stateValidator.Map = map;
```

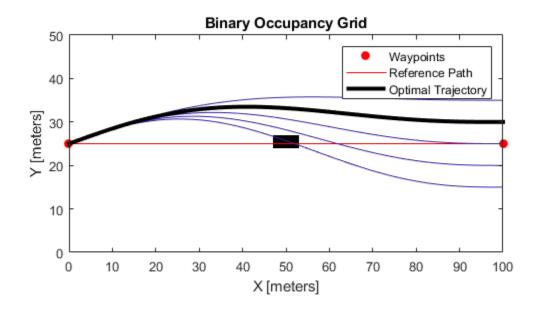
Plan and Visualize Trajectory

Create a reference path for the planner to follow.

```
refPath = [0,25;100,25];
```

Initialize the planner object with the reference path, and the state validator.

```
planner = trajectoryOptimalFrenet(refPath,stateValidator);
Assign longitudinal terminal state, lateral deviation, and maximum acceleration values.
planner.TerminalStates.Longitudinal = 100;
planner.TerminalStates.Lateral = -10:5:10;
planner.FeasibilityParameters.MaxAcceleration = 10;
Specify the deviation offset value close to the left lateral terminal state to prioritize left lane changes.
planner.DeviationOffset = 5;
Trajectory Planning
Initial cartesian state of vehicle.
initCartState = [0 25 pi/9 0 0 0];
Convert cartesian state of vehicle to Frenet state.
initFrenetState = cart2frenet(planner,initCartState);
Plan a trajectory from initial Frenet state.
plan(planner,initFrenetState);
Trajectory Visualization
Visualize the map and the trajectories.
show(map)
hold on
show(planner, 'Trajectory', 'all')
```



Partitioning Longitudinal Terminal States in Trajectory Generation

This example shows how to partition the longitudinal terminal states in optimal trajectory planning using a trajectoryOptimalFrenet object.

Create and Assign Map to State Validator

Create a state validator object for collision checking.

```
statevalidator = validatorOccupancyMap;
```

Create an obstacle grid map.

```
grid = zeros(50,100);
grid(25:27,28:33) = 1;
grid(16:18,37:42) = 1;
grid(29:31,72:77) = 1;
```

Create a binaryOccupancyMap with the grid map.

```
map = binaryOccupancyMap(grid);
```

Assign the map to the state validator.

```
statevalidator.Map = map;
```

Plan and Visualize Trajectory

Create a reference path for the planner to follow.

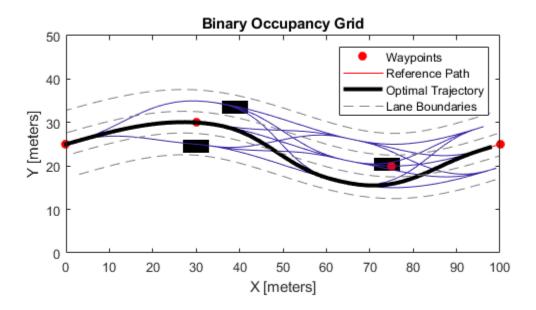
```
refPath = [0,25;30,30;75,20;100,25];
Initialize the planner object with the reference path, and the state validator.
planner = trajectoryOptimalFrenet(refPath, statevalidator);
Assign longitudinal terminal state, lateral deviation, and maximum acceleration values.
planner.TerminalStates.Longitudinal = 100;
planner.TerminalStates.Lateral = -5:5:5;
planner.FeasibilityParameters.MaxAcceleration = 10;
Assign the number of partitions for the longitudinal terminal state.
planner.NumSegments = 3;
Trajectory Planning
Initial Frenet state of vehicle.
initFrenetState = zeros(1,6);
Plan a trajectory from initial Frenet state.
plan(planner,initFrenetState);
Trajectory Visualization
Visualize the map and the trajectories.
show(map)
hold on
show(planner, 'Trajectory', 'all')
hold on
Generate Lane Boundaries
Calculate end of reference path as Frenet state.
refPathEnd = cart2frenet(planner,[planner.Waypoints(end,:) 0 0 0 0]);
Calculate lane offsets on both sides of the lateral terminal states with half lane width value.
laneOffsets = unique([planner.TerminalStates.Lateral+2.5 planner.TerminalStates.Lateral-2.5]);
Calculate positions of lanes in Cartesian state.
numLaneOffsets = numel(laneOffsets);
xRefPathEnd = ceil(refPathEnd(1));
laneXY = zeros((numLaneOffsets*xRefPathEnd)+numLaneOffsets,2);
xIndex = 0;
for laneID = 1:numLaneOffsets
    for x = 1:xRefPathEnd
```

laneCart = frenet2cart(planner,[x 0 0 laneOffsets(laneID) 0 0]);

```
xIndex = xIndex + 1;
laneXY(xIndex,:) = laneCart(1:2);
end
xIndex = xIndex + 1;
laneXY(xIndex,:) = NaN(1,2);
end
```

Plot lane boundaries.

```
plot(laneXY(:,1),laneXY(:,2),'LineWidth',0.5,'Color',[0.5 0.5 0.5],'DisplayName','Lane Boundarie
```



Input Arguments

planner — Optimal trajectory planner in Frenet space

trajectoryOptimalFrenet object

Optimal trajectory planner in Frenet space, specified as a trajectoryOptimalFrenet object.

start — Initial Frenet state

six-element vector

Initial Frenet state, specified as a 1-by-6 vector $[s, ds/dt, d^2s/dt^2, l, dl/ds, d^2l/ds^2]$.

- *s* specifies the arc length from the first point in reference path in meters.
- *ds/dt* specifies the first derivative of arc length.

- d^2s/dt^2 specifies the second derivative of arc length.
- *l* specifies the normal distance from the closest point in the reference path in meters.
- *dl/ds* specifies the first derivative of normal distance.
- d^2l/ds^2 specifies the second derivative of normal distance.

Output Arguments

traj — Feasible trajectory with minimum cost

n-by-7 matrix

Feasible trajectory with minimum cost, returned as an n-by-7 matrix of [x, y, theta, kappa, speed, acceleration, time], where n is the number of trajectory waypoints.

- *x* and *y* specify the position in meters.
- *theta* specifies the orientation angle in radians.
- *kappa* specifies the curvature in m⁻¹.
- speed specifies the velocity in m/s.
- acceleration specifies the acceleration in m/s².
- *time* specifies the time in s.

index — Index of feasible trajectory with minimum cost

positive integer scalar

Index of feasible trajectory with minimum cost, returned as a positive integer scalar.

cost — Least cost of feasible trajectory

positive scalar

Least cost of feasible trajectory, returned as a positive scalar.

flag — Exit flag indicating solution status

0 | 1

Exit flag indicating the solution status, returned either as 0 or 1.

- 0 Optimal trajectory was found.
- 1 No feasible trajectory exists.

When no feasible trajectory exists, the planner returns an empty trajectory.

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

show|trajectoryOptimalFrenet

Introduced in R2019b

show

Visualize trajectories

Syntax

```
show(planner)
show(planner,Name,Value)
axHandle = show(planner)
```

Description

show(planner) visualizes the reference path and trajectory from the candidates generated by the plan function. The trajectory is shown as a line plot. The plot also includes datatip mode, which can be used to visualize the feasibility vector and index of the trajectory from the TrajectoryList property.

show(planner, Name, Value) specifies additional options using one or more Name, Value pair arguments.

axHandle = show(planner) returns the axes handle of the figure used to plot the trajectory.

Examples

Optimal Trajectory Planning in Frenet Space

This example shows how to plan an optimal trajectory using a trajectoryOptimalFrenet object.

Create and Assign Map to State Validator

```
Create a state validator object for collision checking.
```

```
stateValidator = validatorOccupancyMap;
```

Create an obstacle grid map.

```
grid = zeros(50,100);

grid(24:26,48:53) = 1;
```

Create a binaryOccupancyMap with the grid map.

```
map = binaryOccupancyMap(grid);
```

Assign the map to the state validator.

```
stateValidator.Map = map;
```

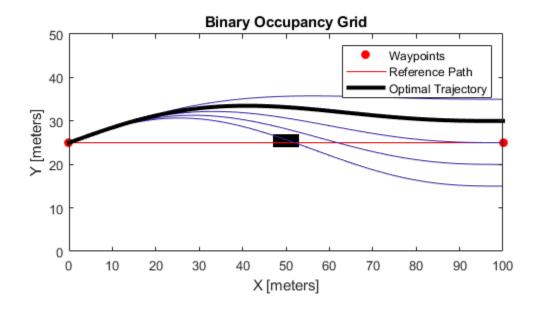
Plan and Visualize Trajectory

Create a reference path for the planner to follow.

```
refPath = [0,25;100,25];
```

Initialize the planner object with the reference path, and the state validator.

```
planner = trajectoryOptimalFrenet(refPath,stateValidator);
Assign longitudinal terminal state, lateral deviation, and maximum acceleration values.
planner.TerminalStates.Longitudinal = 100;
planner.TerminalStates.Lateral = -10:5:10;
planner.FeasibilityParameters.MaxAcceleration = 10;
Specify the deviation offset value close to the left lateral terminal state to prioritize left lane changes.
planner.DeviationOffset = 5;
Trajectory Planning
Initial cartesian state of vehicle.
initCartState = [0 25 pi/9 0 0 0];
Convert cartesian state of vehicle to Frenet state.
initFrenetState = cart2frenet(planner,initCartState);
Plan a trajectory from initial Frenet state.
plan(planner,initFrenetState);
Trajectory Visualization
Visualize the map and the trajectories.
show(map)
hold on
show(planner, 'Trajectory', 'all')
```



Partitioning Longitudinal Terminal States in Trajectory Generation

This example shows how to partition the longitudinal terminal states in optimal trajectory planning using a trajectoryOptimalFrenet object.

Create and Assign Map to State Validator

Create a state validator object for collision checking.

```
statevalidator = validatorOccupancyMap;
```

Create an obstacle grid map.

```
grid = zeros(50,100);
grid(25:27,28:33) = 1;
grid(16:18,37:42) = 1;
grid(29:31,72:77) = 1;
```

Create a binaryOccupancyMap with the grid map.

```
map = binaryOccupancyMap(grid);
```

Assign the map to the state validator.

```
statevalidator.Map = map;
```

Plan and Visualize Trajectory

Create a reference path for the planner to follow.

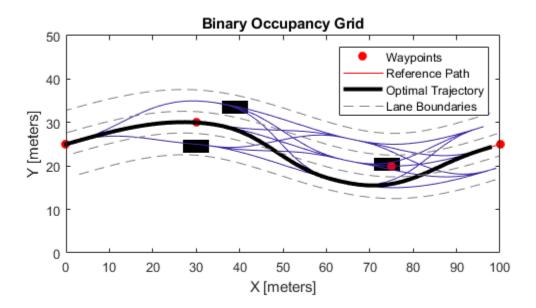
```
refPath = [0,25;30,30;75,20;100,25];
Initialize the planner object with the reference path, and the state validator.
planner = trajectoryOptimalFrenet(refPath, statevalidator);
Assign longitudinal terminal state, lateral deviation, and maximum acceleration values.
planner.TerminalStates.Longitudinal = 100;
planner.TerminalStates.Lateral = -5:5:5;
planner.FeasibilityParameters.MaxAcceleration = 10;
Assign the number of partitions for the longitudinal terminal state.
planner.NumSegments = 3;
Trajectory Planning
Initial Frenet state of vehicle.
initFrenetState = zeros(1,6);
Plan a trajectory from initial Frenet state.
plan(planner,initFrenetState);
Trajectory Visualization
Visualize the map and the trajectories.
show(map)
hold on
show(planner, 'Trajectory', 'all')
hold on
Generate Lane Boundaries
Calculate end of reference path as Frenet state.
refPathEnd = cart2frenet(planner,[planner.Waypoints(end,:) 0 0 0 0]);
Calculate lane offsets on both sides of the lateral terminal states with half lane width value.
laneOffsets = unique([planner.TerminalStates.Lateral+2.5 planner.TerminalStates.Lateral-2.5]);
Calculate positions of lanes in Cartesian state.
numLaneOffsets = numel(laneOffsets);
xRefPathEnd = ceil(refPathEnd(1));
laneXY = zeros((numLaneOffsets*xRefPathEnd)+numLaneOffsets,2);
xIndex = 0;
for laneID = 1:numLaneOffsets
    for x = 1:xRefPathEnd
```

laneCart = frenet2cart(planner,[x 0 0 laneOffsets(laneID) 0 0]);

```
xIndex = xIndex + 1;
laneXY(xIndex,:) = laneCart(1:2);
end
xIndex = xIndex + 1;
laneXY(xIndex,:) = NaN(1,2);
end
```

Plot lane boundaries.

```
plot(laneXY(:,1),laneXY(:,2),'LineWidth',0.5,'Color',[0.5 0.5 0.5],'DisplayName','Lane Boundarie
```



Input Arguments

planner — Optimal trajectory planner in Frenet space

trajectoryOptimalFrenet object

Optimal trajectory planner in Frenet space, specified as a trajectoryOptimalFrenet object.

Name-Value Pair Arguments

Specify optional comma-separated pairs of Name, Value arguments. Name is the argument name and Value is the corresponding value. Name must appear inside quotes. You can specify several name and value pair arguments in any order as Name1, Value1, . . . , NameN, ValueN.

```
Example: 'Trajectory', 'all'
```

Parent — Axes to plot trajectory

Axes object | UIAxes object

Axes to plot trajectory, specified as the comma-separated pair consisting of 'Parent' and either an Axes or UIAxes object. See axes or uiaxes.

Trajectory — Trajectory display option

```
'optimal' (default) | 'all'
```

Trajectory display option, specified as the comma-separated pair consisting of 'Trajectory' and either 'optimal' or 'all'.

ReferencePath — Reference path display option

```
'on' (default) | 'off'
```

Reference path display option, specified as the comma-separated pair consisting of 'ReferencePath' and either 'on' or 'off'.

TrajectoryColor — Trajectory color display option

```
'velocity' (default) | 'acceleration' | 'cost' | 'none'
```

Trajectory color display option, specified as the comma-separated pair consisting of 'TrajectoryColor' and one of the following:

- 'acceleration'
- 'cost'
- · 'velocity'
- 'none'

Set this property to display the specified trajectory as a color-gradient along the specified path.

Output Arguments

axHandle — Axes handle used to plot trajectory

Axes object | UIAxes object

Axes handle used to plot trajectory, returned as either an axes, or uiaxes object.

See Also

plan | trajectoryOptimalFrenet

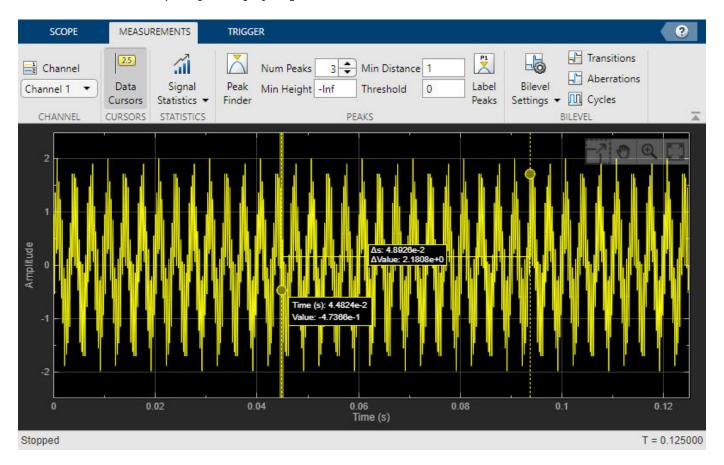
Introduced in R2019b

timescope

Display time-domain signals

Description

The timescope object displays signals in the time domain.



Scope features:

- "Data Cursors" Measure signal values using vertical and horizontal cursors.
- "Signal Statistics" Display the maximum, minimum, peak-to-peak difference, mean, median, and RMS values of a selected signal.
- "Peak Finder" Find maxima, showing the x-axis values at which they occur.
- "Bilevel Measurements" Measure transitions, overshoots, undershoots, and cycles.
- "Triggers" Set triggers to sync repeating signals and pause the display when events occur.

Use "Object Functions" on page 2-1192 to show, hide, and determine visibility of the scope window.

Creation

Syntax

```
scope = timescope
scope = timescope(Name, Value)
```

Description

scope = timescope returns a timescope object, scope. This object displays real- and complexvalued floating and fixed-point signals in the time domain.

scope = timescope(Name, Value) returns a timescope object with properties set to the
specified value. Specify properties and their values in quotes, separated by commas. You can specify
name-value pair arguments in any order.

Properties

Most properties can be changed from the timescope UI.

Frequently Used

SampleRate — Sample rate of inputs

1 (default) | finite numeric scalar | vector

Sampling rate of the input signal, in hertz, specified as a finite numeric scalar or vector of scalars.

The inverse of the sample rate determines the *x*-axis (time axis) spacing between points in the displayed signal. When the value of NumInputPorts is greater than 1 and the sample rate is scalar, the object uses the same sample rate for all inputs. To specify different sample rates for each input, use a vector.

You can only set this property when creating the object or after calling release.

UI Use

On the **Scope** tab, click **Settings**. Under **Data and Axes**, set **Sample Rate**.

Data Types: single | double | int8 | int16 | int32 | int64 | uint8 | uint16 | uint32 | uint64

TimeSpanSource — Source of time span

```
'auto' (default) | 'property'
```

Source of the time span for frame-based input signals, specified as one of the following:

- 'property' The object derives the x-axis limits from the TimeDisplayOffset and TimeSpan properties.
- 'auto' The x-axis limits are derived from the TimeDisplayOffset property, SampleRate property, and the number of rows in each input signal (FrameSize in the equations below). The limits are calculated as:
 - Minimum time-axis limit = TimeDisplayOffset
 - Maximum time-axis limit = TimeDisplayOffset + max(1/SampleRate.*FrameSize)

UI Use

On the **Scope** tab, click **Settings**. Under **Data and Axes**, set **Time Span**.

Data Types: char | string

TimeSpan — Time span

10 (default) | positive scalar

Time span, in seconds, specified as a positive, numeric scalar value. The time-axis limits are calculated as:

- Minimum time-axis limit = TimeDisplayOffset
- Maximum time-axis limit = TimeDisplayOffset + TimeSpan

Dependencies

To enable this property, set TimeSpanSource to 'property'.

UI Use

On the **Scope** tab, click **Settings**. Under **Data and Axes**, edit **Time Span**.

Data Types: single | double | int8 | int16 | int32 | int64 | uint8 | uint16 | uint32 | uint64

TimeSpanOverrunAction — Data overrun behavior

```
'scroll' (default) | 'wrap'
```

Specify how the scope displays new data beyond the visible time span as either:

- 'scroll' In this mode, the scope scrolls old data to the left to make room for new data on the right of the scope display. This mode is beneficial for debugging and monitoring time-varying signals.
- 'wrap' In this mode, the scope adds data to the left of the plot after overrunning the right of the plot.

UI Use

On the **Scope** tab, click **Settings**. Under **Data and Axes**, set **Overrun Action**.

Data Types: char | string

PlotType — Type of plot

```
'line' (default) | 'stairs'
```

Type of plot, specified as either:

- 'line' Line graph, similar to the line or plot function.
- 'stairs' Stair-step graph, similar to the stairs function. Stair-step graphs are useful for drawing time history graphs of digitally sampled data.

UI Use

On the **Scope** tab, click **Settings**. Under **Data and Axes**, set **Plot Type**.

Data Types: char | string

AxesScaling — Axes scaling mode

```
'onceatstop' (default) | 'auto' | 'manual' | 'updates'
```

When this property is set to:

- 'onceatstop' -- The limits are updated once at the end of the simulation (when release is called).
- 'auto' -- The scope attempts to always keep the data in the display while minimizing the number of updates to the axes limits.
- 'manual' -- The scope takes no action unless specified by the user.
- 'updates' -- The scope scales the axes once and only once after 100 updates to the visualization.

You can set this property only when creating the object.

Data Types: char | string

Advanced

Layout Dimensions — Display layout grid dimensions

```
[1,1] (default) | [numberOfRows, numberOfColumns]
```

Specify the layout grid dimensions as a two-element vector: [numberOfRows,numberOfColumns]. The grid can have a maximum of 4 rows and 4 columns.

If you create a grid of multiple axes, to modify the settings of individual axes, use the ActiveDisplay.

Example: scope.LayoutDimensions = [2,4]

UI Use

On the **Scope** tab, click **Display Grid** () and select a specific number of rows and columns from the grid.

Data Types: single | double | int8 | int16 | int32 | int64 | uint8 | uint16 | uint32 | uint64

TimeUnits — Units of x-axis

```
'seconds' (default) | 'none' | 'metric'
```

Specify the units used to describe the x-axis (time axis). You can select one of the following options:

- 'seconds' —The scope always displays the units on the x-axis as seconds. The scope shows the word Time(s) on the x-axis.
- 'none' The scope does not display any units on the x-axis. The scope only shows the word Time on the x-axis.
- 'metric' The scope displays the units on the x-axis as Time (s) changing the units to day, weeks, months, or years as you plot more data points.

UI Use

On the **Scope** tab, click **Settings**. Under **Data and Axes**, set **Time Units**.

Data Types: char | string

TimeDisplayOffset — Offset x-axis limits

0 (default) | scalar | vector

Specify, in seconds, how far to move the data on the x-axis. The signal value does not change, only the limits displayed on the x-axis change.

If you specify this property as a scalar, then that value is the time display offset for all channels. If you specify this property as a vector, each input channel can be a different time display offset

UI Use

On the **Scope** tab, click **Settings**. Under **Data and Axes**, set **Time Offset**.

TimeAxisLabels — Time-axis labels

'all' (default) | 'bottom | 'none'

Time-axis labels, specified as:

- 'all' Time-axis labels appear in all displays.
- 'bottom Time-axis labels appear in the bottom display of each column.
- 'none' No labels appear in any display.

UI Use

On the **Scope** tab, click **Settings**. Under **Data and Axes**, set **Time Labels**.

Data Types: char | string

MaximizeAxes — Maximize axes control

```
'auto' (default) | 'on' | 'off'
```

Specify whether to display the scope in the maximized-axes mode. In this mode, the axes are expanded to fit into the entire display. To conserve space, labels do not appear in each display. Instead, the tick-marks and their values appear on top of the plotted data. You can select one of the following options:

- 'auto' The axes appear maximized in all displays only if the Title and YLabel properties are
 empty for every display. If you enter any value in any display for either of these properties, the
 axes are not maximized.
- 'on' The axes appear maximized in all displays. Any values entered into the Title and YLabel properties are hidden.
- 'off' None of the axes appear maximized.

UI Use

On the scope window, click on to maximize axes, hiding all labels and insetting the axes values.

Data Types: char | string

BufferLength — Buffer length

50000 (default) | positive integer

Specify the length of the buffer used for each input signal as a positive integer.

You can set this property only when creating the object.

UI Use

On the **Scope** tab, click **Settings**. Under **Data and Axes**, set **Buffer Length**.

Data Types: single | double | int8 | int16 | int32 | int64 | uint8 | uint16 | uint32 | uint64

Visualization

Name — Window name

'Time Scope' (default) | character vector | string scalar

Specify the name of the scope as a character vector or string scalar. This name appears as the title of the scope's figure window. To specify a title of a scope plot, use the Title property.

Data Types: char | string

Position — Window position

screen center (default) | [left bottom width height]

Scope window position in pixels, specified by the size and location of the scope window as a fourelement vector of the form [left bottom width height]. You can place the scope window in a specific position on your screen by modifying the values of this property.

By default, the window appears in the center of your screen with a width of 800 pixels and height of 500 pixels. The exact values of the position depend on your screen resolution.

Channel Names — Channel names

{ ' ' } (default) | cell array of character vectors

Specify the input channel names as a cell array of character vectors. The channel names appear in the legend, and on the **Measurements** tab under **Select Channel**. If you do not specify names, the channels are labeled as Channel 1, Channel 2, etc.

Dependency

To enable this property, set ShowLegend to true.

Data Types: char

ActiveDisplay — Active display for setting properties

1 (default) | integer

Active display used to set properties, specified by the integer display number. The number of a display corresponds to the display's row-wise placement index. Setting this property controls which display is used for the following properties: YLimits, YLabel, ShowLegend, ShowGrid, Title, and PlotAsMagnitudePhase.

UI Use

On the **Scope** tab, click **Settings**. Under **Display and Labels**, set **Active Display**.

Title — Display title

' ' (default) | character vector | string scalar

Specify the display title as a character vector or a string scalar.

Dependency

When you set this property, ActiveDisplay controls the display that is updated.

UI Use

On the **Scope** tab, click **Settings**. Under **Display and Labels**, set **Title**.

Data Types: char | string

YLabel — y-axis label

'Amplitude' (default) | character vector | string scalar

Specify the text for the scope to display to the left of the y-axis.

Dependencies

This property applies only when PlotAsMagnitudePhase is false. When PlotAsMagnitudePhase is true, the two *y*-axis labels are read-only values "Magnitude" and "Phase", for the magnitude plot and the phase plot, respectively.

When you set this property, ActiveDisplay controls the display that is updated.

UI Use

On the **Scope** tab, click **Settings**. Under **Display and Labels**, set **YLabel**.

Data Types: char | string

YLimits — y-axis limits

[-10,10] (default) | [ymin, ymax]

Specify the y-axis limits as a two-element numeric vector, [ymin, ymax].

- If PlotAsMagnitudePhase is false, the default is [-10,10].
- If PlotAsMagnitudePhase is true, the default is [0,10]. This property specifies the y-axis limits of only the magnitude plot. The y-axis limits of the phase plot are always [-180,180]

Dependency

When you set this property, ActiveDisplay controls the display that is updated.

UI Use

On the **Scope** tab, click **Settings**. Under **Display and Labels**, set **Y-Axis Limits**.

ShowLegend — Show legend

false (default) | true

To show a legend with the input names, set this property to true.

From the legend, you can control which signals are visible. In the scope legend, click a signal name to hide the signal in the scope. To show the signal, click the signal name again.

UI Use

On the **Scope** tab, click **Settings**. Under **Display and Labels**, select **Show Legend**.

Data Types: logical

ShowGrid — Grid visibility

```
true (default) | false
```

Set this property to true to show grid lines on the plot.

UI Use

On the Scope tab, click Settings. Under Display and Labels, select Show Grid.

PlotAsMagnitudePhase — Plot signal as magnitude and phase

```
false (default) | true
```

Plot signal as magnitude and phased, specified as either:

- true The scope plots the magnitude and phase of the input signal on two separate axes within the same active display.
- false The scope plots the real and imaginary parts of the input signal on two separate axes within the same active display.

This property is useful for complex-valued input signals. Turning on this property affects the phase for real-valued input signals. When the amplitude of the input signal is nonnegative, the phase is 0 degrees. When the amplitude of the input signal is negative, the phase is 180 degrees.

UI Use

On the Scope tab, click Settings. Under Display and Labels, select Magnitude Phase Plot.

Object Functions

To use an object function, specify the object as the first input argument.

hide Hide scope window show Display scope window isVisible Determine visibility of scope

generateScript Generate MATLAB script to create scope with current settings

step Run System object algorithm

release Release resources and allow changes to System object property values and input

characteristics

reset Reset internal states of System object

Examples

View Sine Wave on Time Scope

Create a time-domain sinusoidal signal. Display the signal by calling the time scope object.

Create a sinusoidal signal with two tones, one at 0.3 kHz and the other at 3 kHz.

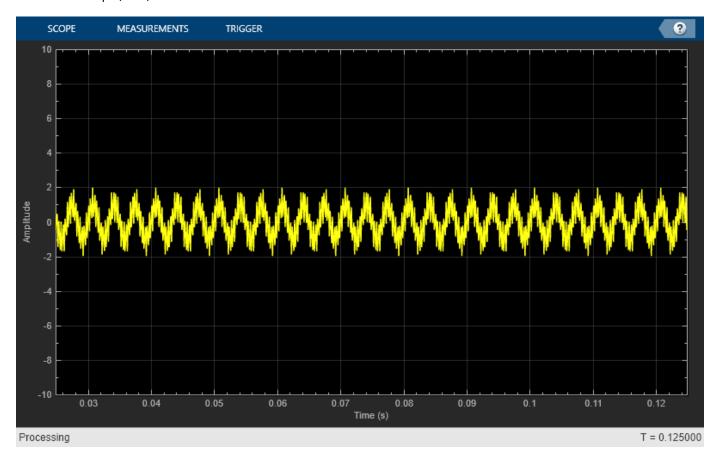
```
t = (0:1000)'/8e3;

xin = sin(2*pi*0.3e3*t) + sin(2*pi*3e3*t);
```

Create a timescope object and view the sinusoidal signal by calling the time scope object scope.

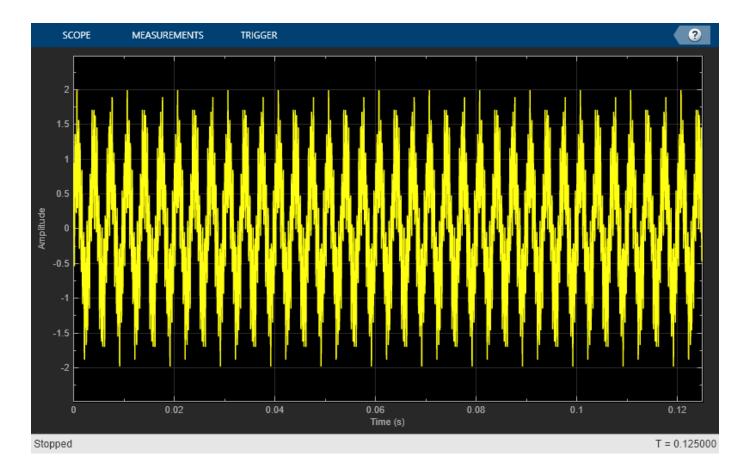
```
scope = timescope('SampleRate', 8e3,...
'TimeSpanSource', 'property', ...
```

'TimeSpan', 0.1); scope(xin)



Run $\tt release$ to allow changes to property values and input characteristics. The scope automatically scales the axes.

release(scope);

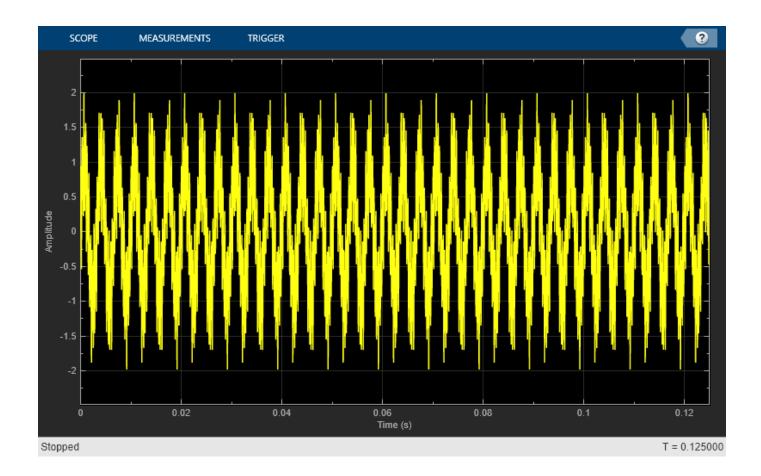


Hide the scope window.

```
if(isVisible(scope))
    hide(scope)
end
```

Show the scope window.

```
if(~isVisible(scope))
    show(scope)
end
```



Use Bilevel Measurements Panel with Clock Input Signal

Create and Display Clock Input Signal

Load the clock data, x and t. Find the sample time, ts.

```
load clockex
ts = t(2)-t(1);
```

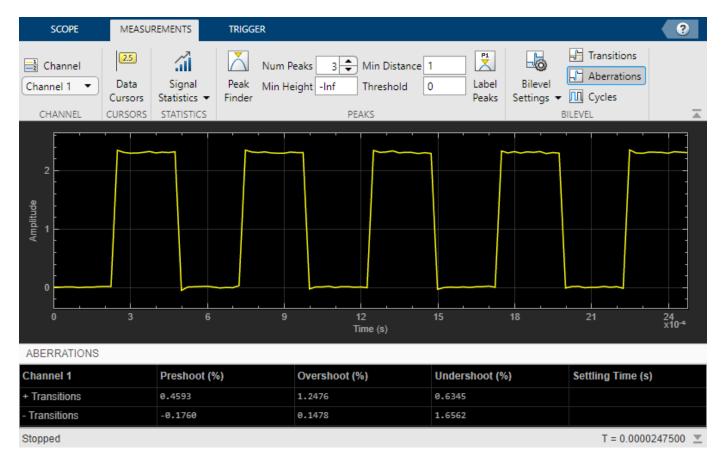
Create a timescope object and call the object to display the signal. To autoscale the axes and enable changes to property values and input characteristics, call release.

```
scope = timescope(1,1/ts,'TimeSpanSource','Auto');
scope(x);
release(scope);
```



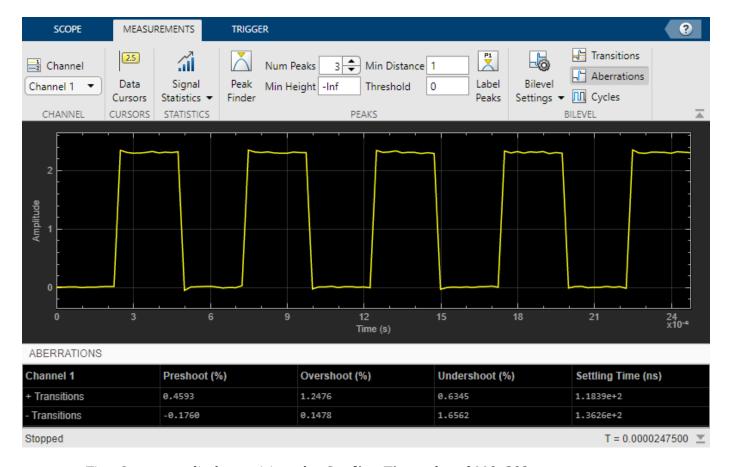
Use Bilevel Measurements Panel to Find Settling Time

1. From the **Measurements** tab, select **Aberrations**.



Initially, the Time Scope does not display the **Settling Time** measurement. This absence occurs because the default value of the **Settle Seek** parameter is longer than the entire simulation duration.

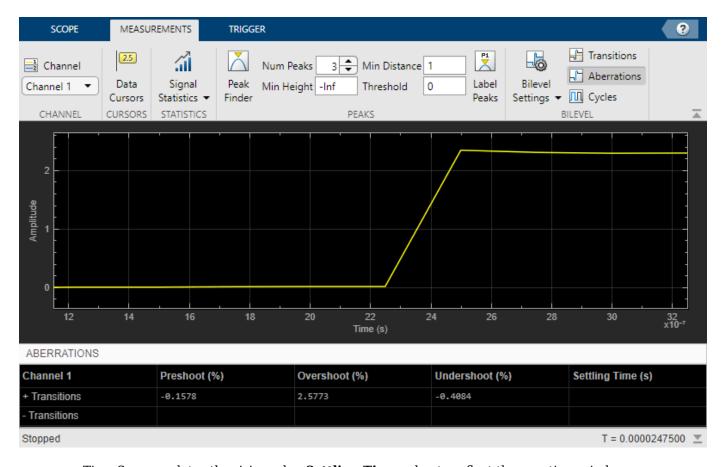
2. In the **Bilevel Settings > Settle Seek** box, enter 2e-6 and press **Enter**.



Time Scope now displays a rising edge **Settling Time** value of 118.392 ns.

This settling time value is actually the statistical average of the settling times for all five rising edges. To show the settling time for only one rising edge, you can zoom in on that transition.

- 3. Hover over the upper right corner of the scope axes, and click the zoom button.
- 4. Click and drag to zoom in on one of the transitions.



Time Scope updates the rising edge **Settling Time** value to reflect the new time window.

View Sine Wave Input Signals at Different Sample Rates and Offsets

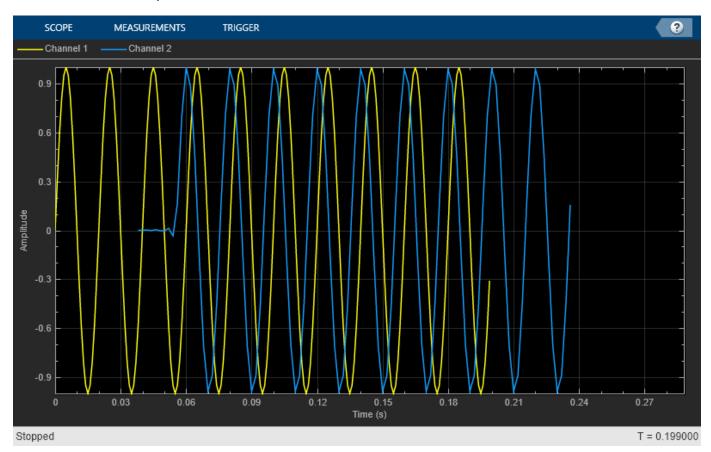
Create a dsp.SineWave with a 1000 Hz sampling frequency. Create a dsp.FIRDecimator object to decimate the sine wave by 2. Create a timescope object with two input ports.

```
Fs = 1000; % Sampling frequency
sine = dsp.SineWave('Frequency',50,...
    'SampleRate',Fs, ...
    'SamplesPerFrame',100);
decimate = dsp.FIRDecimator; % To decimate sine by 2
scope = timescope(2,[Fs Fs/2], ...
    'TimeDisplayOffset',[0 38/Fs], ...
    'TimeSpanSource','Property',...
    'TimeSpan',0.25, ...
    'YLimits',[-1 1], ...
    'ShowLegend', true);
```

Call the dsp.SineWave object to create a sine wave signal. Use the dsp.FIRDecimator object to create a second signal that equals the original signal, but decimated by a factor of 2. Display the signals by calling the timescope object.

```
for ii = 1:2
    xsine = sine();
```

```
xdec = decimate(xsine);
    scope(xsine,xdec)
end
release(scope)
```



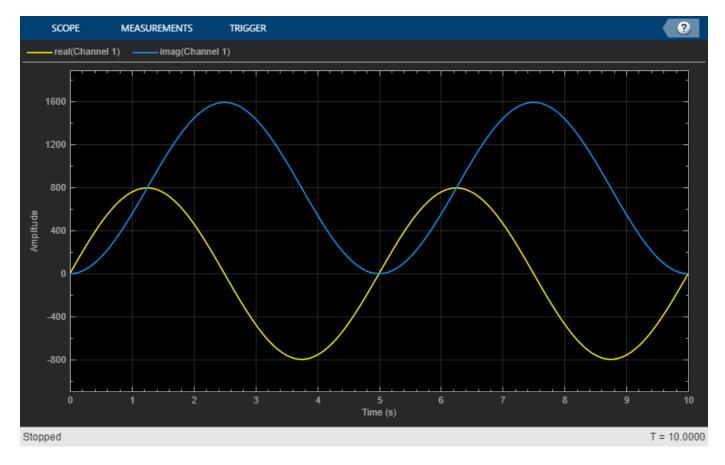
Close the Time Scope window and clear the variables.

clear scope Fs sine decimate ii xsine xdec

Display Complex-Valued Input Signal

Create a vector representing a complex-valued sinusoidal signal, and create a timescope object. Call the scope to display the signal.

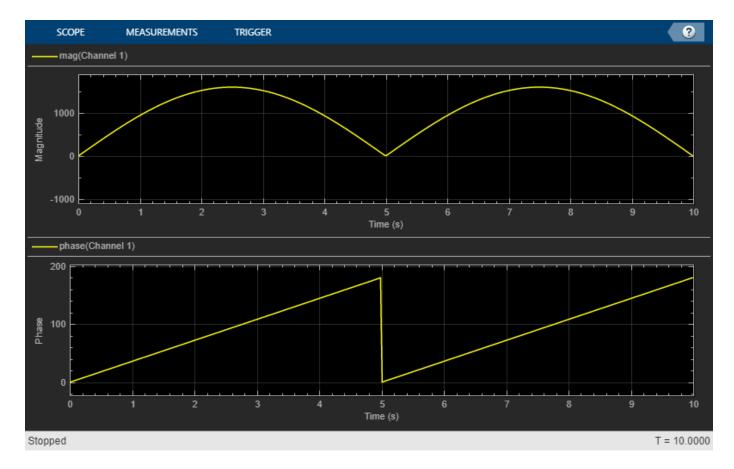
```
fs = 1000;
t = (0:1/fs:10)';
CxSine = cos(2*pi*0.2*t) + 1i*sin(2*pi*0.2*t);
CxSineSum = cumsum(CxSine);
scope = timescope(1,fs,'TimeSpanSource','Auto','ShowLegend',1);
scope(CxSineSum);
release(scope)
```



By default, when the input is a complex-valued signal, Time Scope plots the real and imaginary portions on the same axes. These real and imaginary portions appear as different-colored lines on the same axes within the same active display.

Change the PlotAsMagnitudePhase property to true and call release.

```
scope.PlotAsMagnitudePhase = true;
scope(CxSineSum);
release(scope)
```

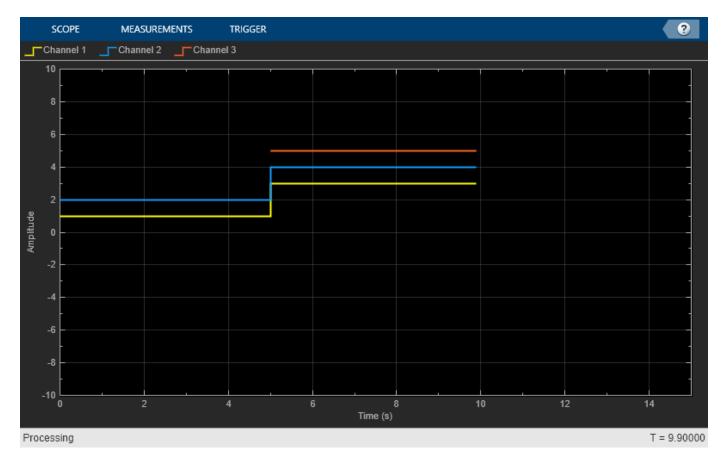


Time Scope now plots the magnitude and phase of the input signal on two separate axes within the same active display. The top axes display magnitude and the bottom axes display the phase, in degrees.

Display Input Signal of Changing Size

This example shows how the timescope object visualizes inputs that change dimensions halfway through.

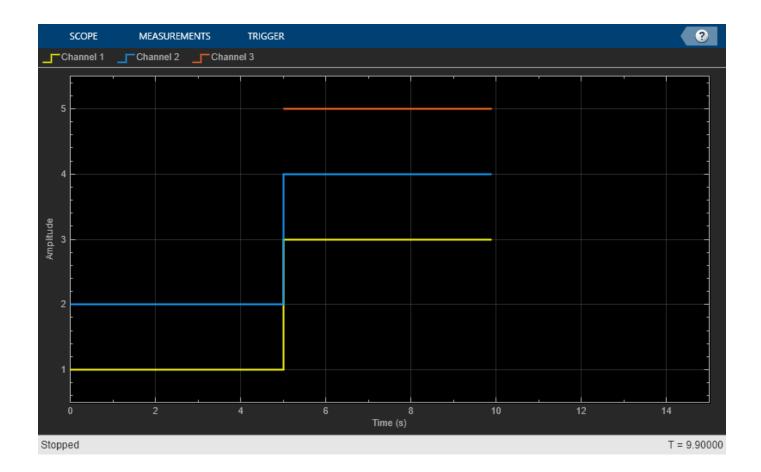
Create a vector that represents a two-channel constant signal. Create another vector that represents a three-channel constant signal. Create a timescope object. Call the scope with two inputs to display the signal.



In this example, the size of the input signal to the Time Scope changes as the simulation progresses. When the simulation time is less than 5 seconds, Time Scope plots only the two-channel signal, sigdim2. After 5 seconds, Time Scope also plots the three-channel signal, sigdim3.

Run the release method to enable changes to property values and input characteristics. The scope automatically scales the axes.

release(scope)



Find Heart Rate Using Peak Finder Panel with ECG Input Signal

Use Peak Finder panel of the Time Scope to measure a heart rate.

Create and Display ECG Signal

Create the electrocardiogram (ECG) signal. The custom $\operatorname{\mathsf{ecg}}$ function helps generate the heartbeat signal.

```
function x = ecg(L)
a0 = [0, 1, 40, 1, 0, -34, 118, -99, 0, 2, 21, 2, 0, 0, 0];
d0 = [0, 27, 59, 91, 131, 141, 163, 185, 195, 275, 307, 339, 357, 390, 440];
a = a0 / max(a0);
d = round(d0 * L / d0(15));
d(15) = L;
for i = 1:14
    m = d(i) : d(i+1) - 1;
    slope = (a(i+1) - a(i)) / (d(i+1) - d(i));
    x(m+1) = a(i) + slope * (m - d(i));
end

x1 = 3.5*ecg(2700).';
y1 = sgolayfilt(kron(ones(1,13),x1),0,21);
```

```
n = (1:30000)';
del = round(2700*rand(1));
mhb = y1(n + del);
ts = 0.00025;
```

Create a timescope object and call the object to display the signal. To autoscale the axes and enable changes to property values and input characteristics, call release.

```
scope = timescope(1,1/ts);
scope(mhb);
release(scope)
```

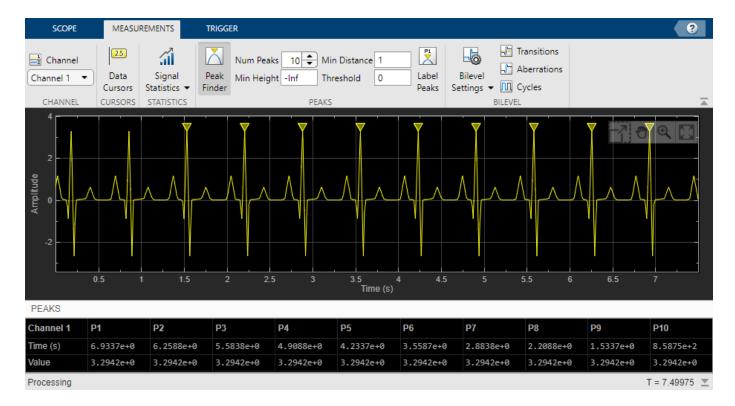


Find Heart Rate

Use the Peak Finder measurements to measure the time between heart beats.

- 1 On the **Measurements** tab, select **Peak Finder**.
- 2 For the **Num Peaks** property, enter 10.

In the **Peaks** pane at the bottom of the window, the Time Scope displays a list of ten peak amplitude values and the times at which they occur.



The list of peak values shows a constant time difference of 0.675 second between each heartbeat. Based on the following equation, the heart rate of this ECG signal is about 89 beats per minute.

$$\frac{60 \text{ s/min}}{0.675 \text{ s/beat}} = 88.89 \text{ bpm}$$

Close the Time Scope window and remove the variables you created from the workspace.

clear scope x1 y1 n del mhb ts

See Also

Topics

"Configure Time Scope MATLAB Object"

Introduced in R2020a

generateScript

Generate MATLAB script to create scope with current settings

Syntax

generateScript(scope)

Description

generateScript(scope) generates a MATLAB script that can re-create a timescope object with the current settings in the scope.

Examples

Generate Script from timescope

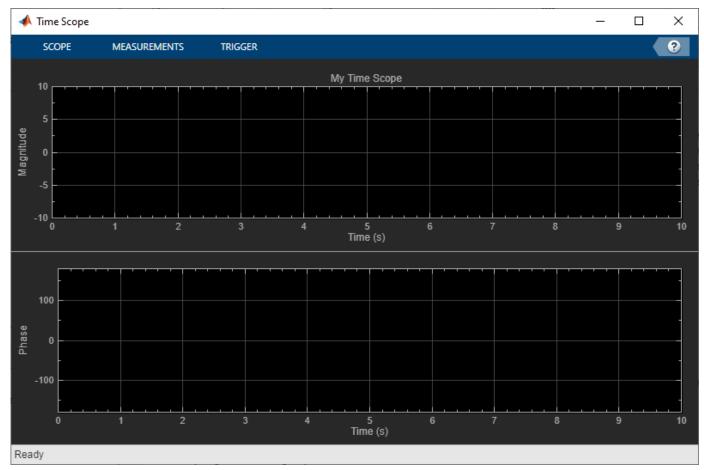
Generate MATLAB script after making changes to the timescope object in the scope window.

Note The script only generates commands for settings that are available from the command line, applicable to the current visualization, and changed from the default value.

1 Create a timescope object.

```
scope = timescope;
show(scope)
```

2 Set options in the Time Scope. For this example, on the **Scope** tab, click **Settings**. Under **Display and Labels**, select **Show Legend** and **Magnitude Phase Plot**. Set the **Title** as well.



3 Generate a script to recreate the timescope with the same modified settings. Either select **Generate Script** from the **Scope** tab, or enter:

```
generateScript(scope);
```

A new editor window opens with code to regenerate the same scope.

```
% Creation Code for 'timescope'.
% Generated by Time Scope on 8-Nov-2019 13:51:54 -0500.
timeScope = timescope('Position',[2286 355 800 500], ...
    'Title','My Time Scope', ...
    'ShowLegend',true, ...
    'PlotAsMagnitudePhase',true);
```

Input Arguments

scope — object

timescope object

Object whose settings you want to recreate with a script.

See Also

Functions

hide | isVisible | show

Objects timescope

Introduced in R2020a

hide

Hide scope window

Syntax

hide(scope)

Description

hide(scope) hides the scope window.

Examples

View Sine Wave on Time Scope

Create a time-domain sinusoidal signal. Display the signal by calling the time scope object.

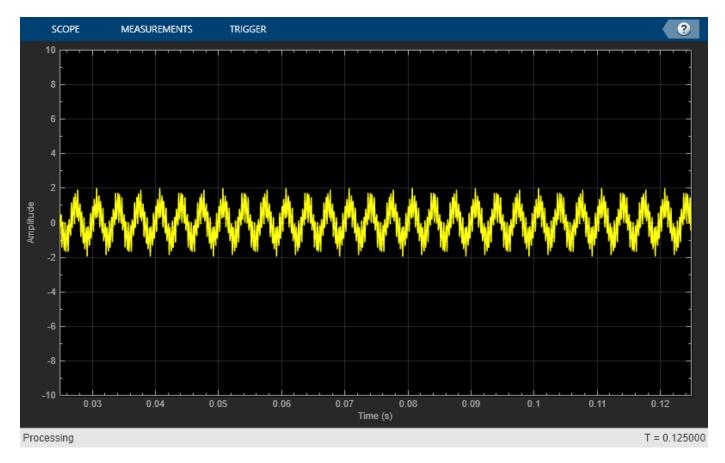
Create a sinusoidal signal with two tones, one at 0.3 kHz and the other at 3 kHz.

```
t = (0:1000)'/8e3;

xin = sin(2*pi*0.3e3*t)+sin(2*pi*3e3*t);
```

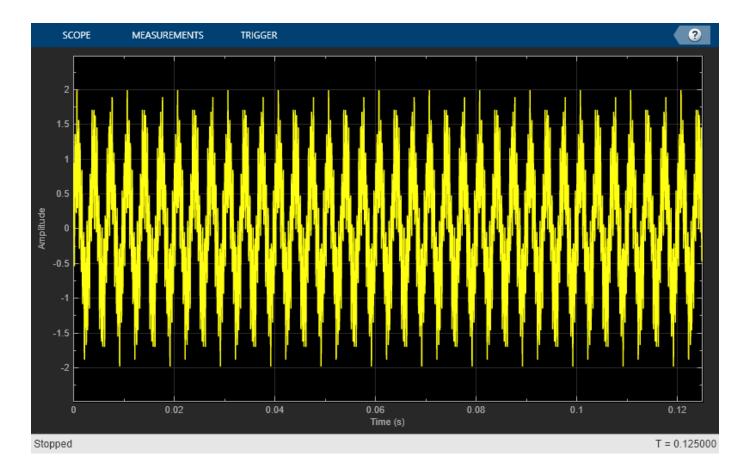
Create a timescope object and view the sinusoidal signal by calling the time scope object scope.

```
scope = timescope('SampleRate', 8e3,...
    'TimeSpanSource', 'property', ...
    'TimeSpan', 0.1);
scope(xin)
```



Run $\tt release$ to allow changes to property values and input characteristics. The scope automatically scales the axes.

release(scope);

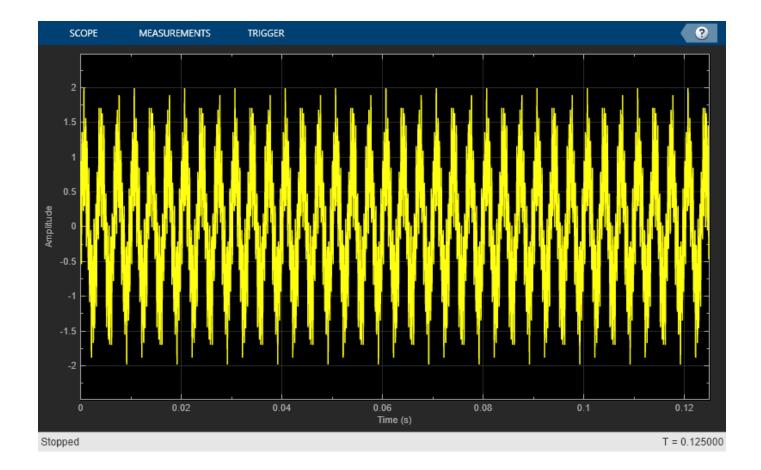


Hide the scope window.

```
if(isVisible(scope))
    hide(scope)
end
```

Show the scope window.

```
if(~isVisible(scope))
    show(scope)
end
```



Input Arguments

scope — Scope object

timescope object

Scope object whose window you want to hide, specified as a timescope object.

Example: myScope = timescope; hide(myScope)

See Also

Functions

generateScript|isVisible|show

Objects

timescope

Introduced in R2020a

isVisible

Determine visibility of scope

Syntax

```
visibility = isVisible(scope)
```

Description

visibility = isVisible(scope) returns the visibility of the scope as logical, with 1 (true) for visible.

Examples

View Sine Wave on Time Scope

Create a time-domain sinusoidal signal. Display the signal by calling the time scope object.

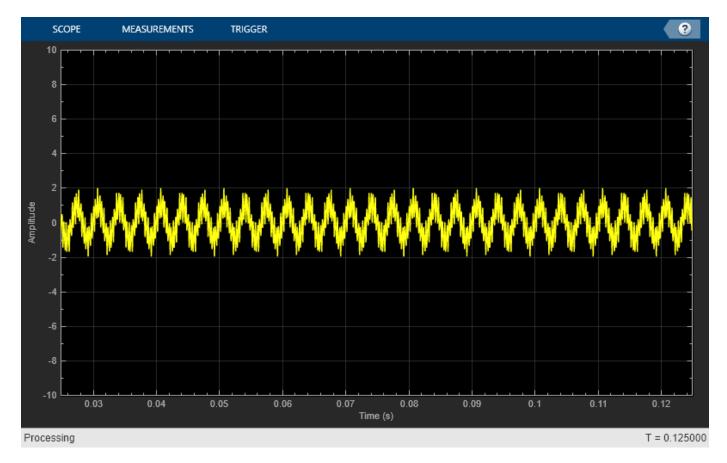
Create a sinusoidal signal with two tones, one at 0.3 kHz and the other at 3 kHz.

```
t = (0:1000)'/8e3;

xin = sin(2*pi*0.3e3*t)+sin(2*pi*3e3*t);
```

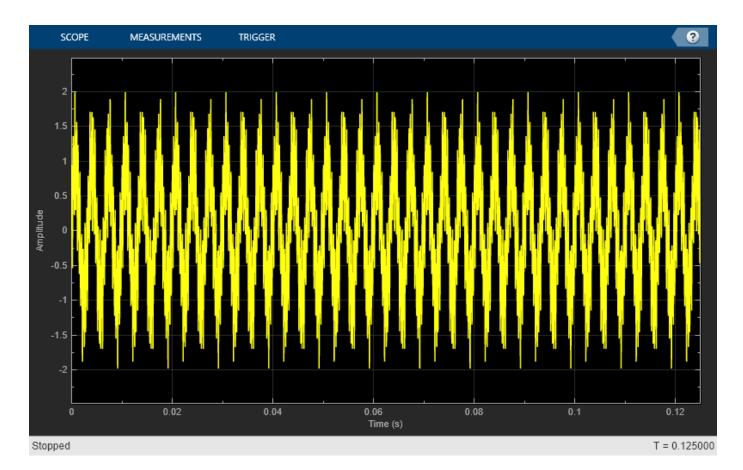
Create a timescope object and view the sinusoidal signal by calling the time scope object scope.

```
scope = timescope('SampleRate', 8e3,...
    'TimeSpanSource', 'property', ...
    'TimeSpan', 0.1);
scope(xin)
```



Run release to allow changes to property values and input characteristics. The scope automatically scales the axes.

release(scope);

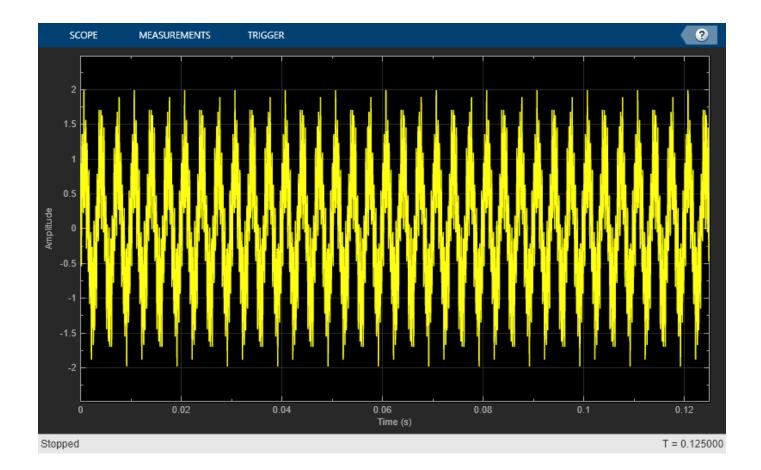


Hide the scope window.

```
if(isVisible(scope))
    hide(scope)
end
```

Show the scope window.

```
if(~isVisible(scope))
    show(scope)
end
```



Input Arguments

scope — Scope object

timescope object

Scope object whose visibility you want to query.

Example: myScope = timescope; visibility = isVisible(myScope)

Output Arguments

visibility — Scope visibility

1 | 0

If the scope window is open, the isVisible function returns 1 (true). Otherwise, the function returns 0 (false).

See Also

Functions

generateScript|hide|show

Objects timescope

Introduced in R2020a

show

Display scope window

Syntax

show(scope)

Description

show(scope) shows the scope window.

Examples

View Sine Wave on Time Scope

Create a time-domain sinusoidal signal. Display the signal by calling the time scope object.

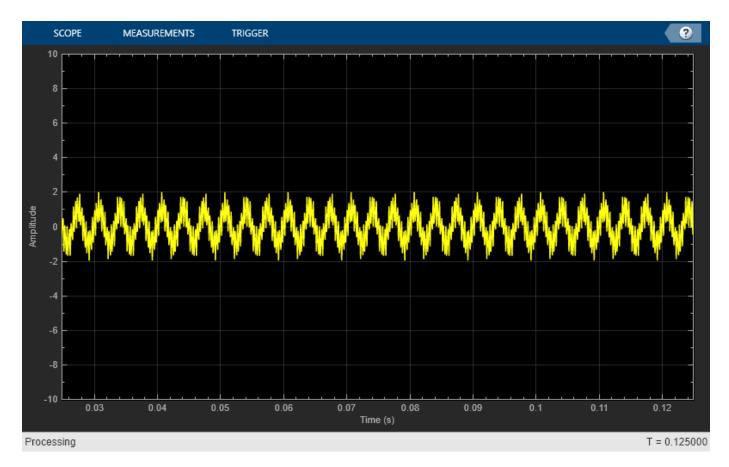
Create a sinusoidal signal with two tones, one at 0.3 kHz and the other at 3 kHz.

```
t = (0:1000)'/8e3;

xin = sin(2*pi*0.3e3*t)+sin(2*pi*3e3*t);
```

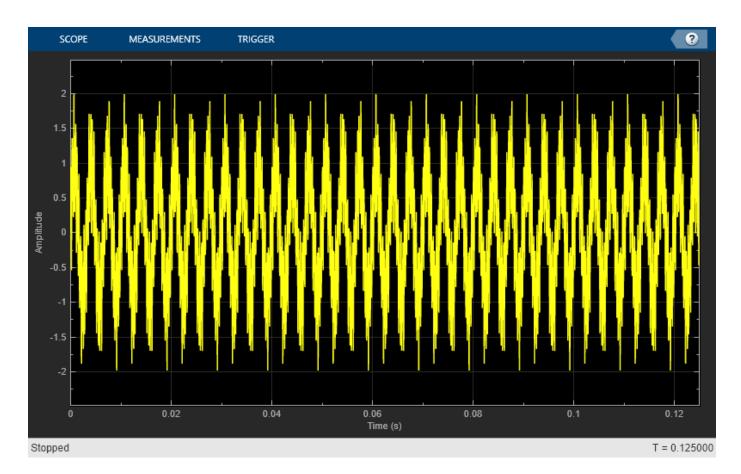
Create a timescope object and view the sinusoidal signal by calling the time scope object scope.

```
scope = timescope('SampleRate', 8e3,...
    'TimeSpanSource', 'property', ...
    'TimeSpan', 0.1);
scope(xin)
```



Run $\tt release$ to allow changes to property values and input characteristics. The scope automatically scales the axes.

release(scope);

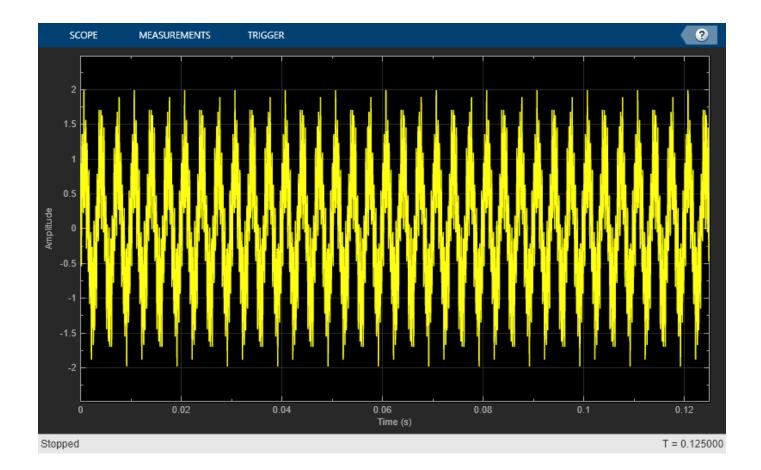


Hide the scope window.

if(isVisible(scope))
 hide(scope)
end

Show the scope window.

if(~isVisible(scope))
 show(scope)
end



Input Arguments

scope — Scope object

timescope object

Scope object whose window you want to show, specified as a timescope object.

Example: myScope = timescope; show(myScope)

See Also

Functions

generateScript|hide|isVisible

Objects

timescope

Introduced in R2020a

tunerconfig

Fusion filter tuner configuration options

Description

The tunerconfig object creates a tuner configuration for a fusion filter used to tune the filter for reduced estimation error.

Creation

Syntax

```
config = tunerconfig(filterName)
config = tunerconfig(filterName, Name, Value)
```

Description

config = tunerconfig(filterName) creates a tunerconfig object controlling the optimization
algorithm of the tune function of the fusion filter.

config = tunerconfig(filterName, Name, Value) configures the created tunerconfig object properties using one or more name-value pair arguments. Name is a property name and Value is the corresponding value. Name must appear inside quotes. You can specify several name-value pair arguments in any order as Name1, Value1, . . . , NameN, ValueN. Any unspecified properties take default values.

For example, tunerconfig('imufilter', 'MaxIterations', 3) create a tunerconfig object for the imufilter object with the a maximum of three allowed iterations.

Inputs Arguments

filterName — Fusion filter name

```
'imufilter'|'ahrsfilter'|'ahrs10filter'|'insfilterAsync'|'insfilterMARG'|
'insfitlerErrorState'|'insfilterNonholonomic'
```

Fusion filter name, specified as one of these options:

- 'imufilter'
- 'ahrsfilter'
- 'ahrs10filter'
- 'insfilterAsync'
- 'insfilterMARG'
- 'insfitlerErrorState'
- 'insfilterNonholonomic'

Properties

Filter — Class name of filter

string

This property is read-only.

Class name of filter, specified as a string. Its value is one of these strings:

- "imufilter"
- "ahrsfilter"
- "ahrs10filter"
- "insfilterAsync"
- "insfilterMARG"
- "insfitlerErrorState"
- "insfilterNonholonomic"

TunableParameters — **Tunable parameters**

array of string

Tunable parameters, specified as an array of strings. Each string is a tunable property name of the fusion filter. By default, the property contains all the tunable parameters of a fusion filter.

Example: ["AccelerometerNoise" "GyroscopeNoise"]

StepForward — Factor of forward step

1.1 (default) | scalar larger than 1

Factor of a forward step, specified as a scalar larger than 1. During the tuning process, the tuner increases or decreases the noise parameters to achieve smaller estimation errors. This property specifies the ratio of parameter increase during a parameter increase step.

StepBackward — Factor of backward step

0.5 (default) | scalar in range (0,1)

Factor of a backward step, specified as a scalar in the range of (0,1). During the tuning process, the tuner increases or decreases the noise parameters to achieve smaller estimation errors. This property specifies the factor of parameter decrease during a parameter decrease step.

MaxIterations — Maximum number of iterations

20 (default) | positive integer

Maximum number of iterations allowed by the tuning algorithm, specified as a positive integer.

ObjectiveLimit — Cost at which to stop tuning process

0.1 (default) | positive scalar

Cost at which to stop the tuning process, specified as a positive scalar.

FunctionTolerance — Minimum change in cost to continue tuning

0 (default) | nonnegative scalar

Minimum change in cost to continue tuning, specified as a nonnegative scalar. If the change in cost is smaller than the specified tolerance, the tuning process stops.

Display — Enable showing the iteration details

"iter" (default) | "none"

Enable showing the iteration details, specified as "iter" or "none". When specified as:

- "iter" The program shows the tuned parameter details in each iteration in the Command Window.
- "none" The program does not show any tuning information.

Cost — Metric for evaluating filter performance

"RMS" (default) | "Custom"

Metric for evaluating filter performance, specified as "RMS" or "Custom". When specified as:

- "RMS" The program optimizes the root-mean-squared (RMS) error between the estimate and the truth.
- "Custom" The program optimizes the filter performance by using a customized cost function specified by the CustomCostFcn property.

CustomCostFcn — Customized cost function

[] (default) | function handle

Customized cost function, specified as a function handle.

Dependencies

To enable this property, set the Cost property to 'Custom'.

OutputFcn — Output function called at each iteration

[] (default) | function handle

Output function called at each iteration, specified as a function handle. The function must use the following syntax:

stop = myOutputFcn(params,tunerValues)

params is a structure of the current best estimate of each parameter at the end of the current iteration. tunerValues is a structure containing information of the tuner configuration, sensor data, and truth data. It has these fields:

Field Name	Description
Iteration	Iteration count of the tuner, specified as a positive integer
SensorData	Sensor data input to the tune function
GroundTruth	Ground truth input to the tune function
Configuration	tunerconfig object used for tuning
Cost	Tuning cost at the end of the current iteration

Tip You can use the built-in function tunerPlotPose to visualize the truth data and the estimates for most of your tuning applications. See the "Visualize Tuning Results Using tunerPlotPose" on page 1-210 example for details.

Examples

Create Tunerconfig Object and Show Tunable Parameters

Create a tunerconfig object for the insfilterAsync object.

```
config = tunerconfig('insfilterAsync')
config =
  tunerconfig with properties:

   TunableParameters: [1×14 string]
        StepForward: 1.1000
        StepBackward: 0.5000
        MaxIterations: 20
   OptimalityTolerance: 0.1000
        Display: iter
        Cost: RMS
```

Display the default tunable parameters.

```
config. Tunable Parameters\\
```

```
ans = 1 \times 14 string "AccelerometerNoise" "GyroscopeNoise" "MagnetometerNoise" "GPSPositionNoise"
```

"GP

Tune insfilterAsync to Optimize Pose Estimate

Load the recorded sensor data and ground truth data.

```
load('insfilterAsyncTuneData.mat');
```

Create timetables for the sensor data and the truth data.

```
sensorData = timetable(Accelerometer, Gyroscope, ...
    Magnetometer, GPSPosition, GPSVelocity, 'SampleRate', 100);
groundTruth = timetable(Orientation, Position, ...
    'SampleRate', 100);
```

Create an insfilterAsync filter object that has a few noise properties.

```
filter = insfilterAsync('State', initialState, ...
    'StateCovariance', initialStateCovariance, ...
    'AccelerometerBiasNoise', le-7, ...
    'GyroscopeBiasNoise', le-7, ...
    'MagnetometerBiasNoise', le-7, ...
    'GeomagneticVectorNoise', le-7);
```

Create a tuner configuration object for the filter. Set the maximum iterations to two. Also, set the tunable parameters as the unspecified properties.

```
config = tunerconfig('insfilterAsync','MaxIterations',8);
config.TunableParameters = setdiff(config.TunableParameters, ...
```

```
{'GeomagneticVectorNoise', 'AccelerometerBiasNoise', ...
'GyroscopeBiasNoise', 'MagnetometerBiasNoise'});
config.TunableParameters

ans = 1×10 string
"AccelerationNoise" "AccelerometerNoise" "AngularVelocityNoise" "GPSPositionNoise"
```

Use the tuner noise function to obtain a set of initial sensor noises used in the filter.

```
measNoise = tunernoise('insfilterAsync')
measNoise = struct with fields:
    AccelerometerNoise: 1
        GyroscopeNoise: 1
        MagnetometerNoise: 1
        GPSPositionNoise: 1
        GPSVelocityNoise: 1
```

Tune the filter and obtain the tuned parameters.

tunedParams = tune(filter, measNoise, sensorData, groundTruth, config);

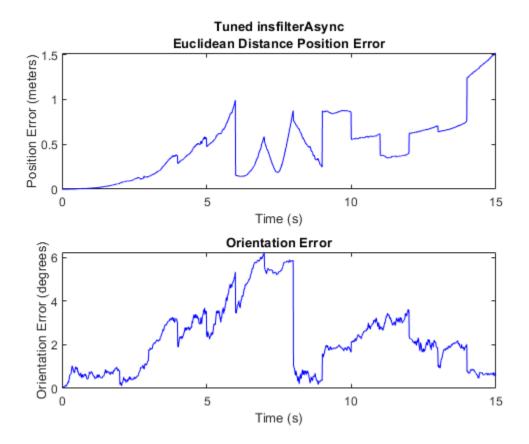
Iteration	Parameter	Metric
1	AccelerationNoise	2.1345
1	AccelerometerNoise	2.1264
1	AngularVelocityNoise	1.9659
1	GPSPositionNoise	1.9341
1	GPSVelocityNoise	1.8420
1	GyroscopeNoise	1.7589
1	MagnetometerNoise	1.7362
1	PositionNoise	1.7362
1	QuaternionNoise	1.7218
1	VelocityNoise	1.7218
2	AccelerationNoise	1.7190
2	AccelerometerNoise	1.7170
2	AngularVelocityNoise	1.6045
2	GPSPositionNoise	1.5948
2	GPSVelocityNoise	1.5323
2	GyroscopeNoise	1.4803
2	MagnetometerNoise	1.4703
2	PositionNoise	1.4703
2	QuaternionNoise	1.4632
2	VelocityNoise	1.4632
3	AccelerationNoise	1.4596
3	AccelerometerNoise	1.4548
3	AngularVelocityNoise	1.3923
3	GPSPositionNoise	1.3810
3	GPSVelocityNoise	1.3322
3	GyroscopeNoise	1.2998
3	MagnetometerNoise	1.2976
3	PositionNoise	1.2976
3	QuaternionNoise	1.2943
2 2 2 2 2 2 2 2 2 2 2 3 3 3 3 3 3 3 3 3	VelocityNoise	1.2943
	AccelerationNoise	1.2906
4	AccelerometerNoise	1.2836
4	AngularVelocityNoise	1.2491

```
GPSPositionNoise
                                      1.2258
4
             GPSVelocityNoise
                                      1.1880
4
                                      1.1701
             GyroscopeNoise
4
             MagnetometerNoise
                                      1.1698
4
             PositionNoise
                                      1.1698
4
             QuaternionNoise
                                      1.1688
4
             VelocityNoise
                                      1.1688
5
             AccelerationNoise
                                      1.1650
5
             AccelerometerNoise
                                      1.1569
5
             AngularVelocityNoise
                                      1.1454
5
             GPSPositionNoise
                                      1.1100
5
             GPSVelocityNoise
                                      1.0778
5
             GyroscopeNoise
                                      1.0709
5
             MagnetometerNoise
                                      1.0675
5
                                      1.0675
             PositionNoise
5
                                      1.0669
             QuaternionNoise
5
                                      1.0669
             VelocityNoise
6
             AccelerationNoise
                                      1.0634
6
             AccelerometerNoise
                                      1.0549
6
             AngularVelocityNoise
                                      1.0549
6
             GPSPositionNoise
                                      1.0180
6
             GPSVelocityNoise
                                      0.9866
6
             GyroscopeNoise
                                      0.9810
6
                                      0.9775
             MagnetometerNoise
6
                                      0.9775
             PositionNoise
6
                                      0.9768
             QuaternionNoise
6
             VelocityNoise
                                      0.9768
7
             AccelerationNoise
                                      0.9735
7
             AccelerometerNoise
                                      0.9652
7
             AngularVelocityNoise
                                      0.9652
7
             GPSPositionNoise
                                      0.9283
7
             GPSVelocityNoise
                                      0.8997
7
             GyroscopeNoise
                                      0.8947
7
             MagnetometerNoise
                                      0.8920
7
             PositionNoise
                                      0.8920
7
                                      0.8912
             QuaternionNoise
7
             VelocityNoise
                                      0.8912
8
             AccelerationNoise
                                      0.8885
8
             AccelerometerNoise
                                      0.8811
8
             AngularVelocityNoise
                                      0.8807
8
             GPSPositionNoise
                                      0.8479
8
             GPSVelocityNoise
                                      0.8238
             GyroscopeNoise
                                      0.8165
8
             MagnetometerNoise
                                      0.8165
8
             PositionNoise
                                      0.8165
8
             QuaternionNoise
                                      0.8159
8
             VelocityNoise
                                      0.8159
```

Fuse the sensor data using the tuned filter.

```
dt = seconds(diff(groundTruth.Time));
N = size(sensorData,1);
qEst = quaternion.zeros(N,1);
posEst = zeros(N,3);
% Iterate the filter for prediction and correction using sensor data.
for ii=1:N
    if ii ~= 1
        predict(filter, dt(ii-1));
```

```
end
    if all(~isnan(Accelerometer(ii,:)))
        fuseaccel(filter,Accelerometer(ii,:), ...
            tunedParams.AccelerometerNoise);
   end
    if all(~isnan(Gyroscope(ii,:)))
        fusegyro(filter, Gyroscope(ii,:), ...
            tunedParams.GyroscopeNoise);
    if all(~isnan(Magnetometer(ii,1)))
        fusemag(filter, Magnetometer(ii,:), ...
            tunedParams.MagnetometerNoise);
    end
    if all(~isnan(GPSPosition(ii,1)))
        fusegps(filter, GPSPosition(ii,:), ...
            tunedParams.GPSPositionNoise, GPSVelocity(ii,:), ...
            tunedParams.GPSVelocityNoise);
    end
    [posEst(ii,:), qEst(ii,:)] = pose(filter);
end
Compute the RMS errors.
orientationError = rad2deg(dist(qEst, Orientation));
rmsorientationError = sqrt(mean(orientationError.^2))
rmsorientationError = 2.7801
positionError = sqrt(sum((posEst - Position).^2, 2));
rmspositionError = sqrt(mean( positionError.^2))
rmspositionError = 0.5966
Visualize the results.
figure();
t = (0:N-1)./ groundTruth.Properties.SampleRate;
subplot(2,1,1)
plot(t, positionError, 'b');
title("Tuned insfilterAsync" + newline + "Euclidean Distance Position Error")
xlabel('Time (s)');
ylabel('Position Error (meters)')
subplot(2,1,2)
plot(t, orientationError, 'b');
title("Orientation Error")
xlabel('Time (s)');
ylabel('Orientation Error (degrees)');
```



Tune imufilter to Optimize Orientation Estimate

Load recorded sensor data and ground truth data.

```
ld = load('imufilterTuneData.mat');
qTrue = ld.groundTruth.Orientation; % true orientation
```

Create an imufilter object and fuse the filter with the sensor data.

```
fuse = imufilter;
qEstUntuned = fuse(ld.sensorData.Accelerometer, ...
    ld.sensorData.Gyroscope);
```

Create a tunerconfig object and tune the imufilter to improve the orientation estimate.

```
cfg = tunerconfig('imufilter');
tune(fuse, ld.sensorData, ld.groundTruth, cfg);
```

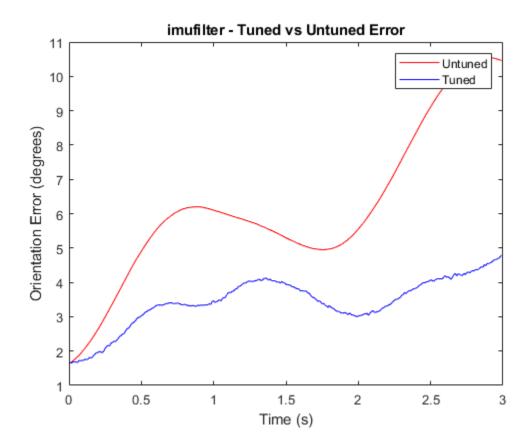
Iteration	Parameter	Metric
1	AccelerometerNoise	0.1149
1	GyroscopeNoise	0.1146
1	GyroscopeDriftNoise	0.1146
1	LinearAccelerationNoise	0.1122
1	LinearAccelerationDecayFactor	0.1103

2	A see The seems to subtract the	0 1100
2	AccelerometerNoise	0.1102
2	GyroscopeNoise	0.1098
2 2	GyroscopeDriftNoise	0.1098
2	LinearAccelerationNoise	0.1070
2	LinearAccelerationDecayFactor	0.1053
2		
3	AccelerometerNoise	0.1053
3	GyroscopeNoise	0.1048
3	GyroscopeDriftNoise	0.1048
2 3 3 3 3 3	LinearAccelerationNoise	0.1016
3	LinearAccelerationDecayFactor	0.1002
4		
	AccelerometerNoise	0.1001
4	GyroscopeNoise	0.0996
4	GyroscopeDriftNoise	0.0996
4	LinearAccelerationNoise	0.0962
4	LinearAccelerationDecayFactor	0.0950
	AccelerometerNoise	0.0950
5 5	GyroscopeNoise	0.0943
5		0.0943
2	GyroscopeDriftNoise	
5	LinearAccelerationNoise	0.0910
5	LinearAccelerationDecayFactor	0.0901
6	AccelerometerNoise	0.0900
6	GyroscopeNoise	0.0893
6	GyroscopeDriftNoise	0.0893
6	LinearAccelerationNoise	0.0862
6	LinearAccelerationDecayFactor	0.0855
7	AccelerometerNoise	0.0855
7	GyroscopeNoise	0.0848
7	GyroscopeDriftNoise	0.0848
7	LinearAccelerationNoise	0.0822
7	LinearAccelerationDecayFactor	0.0818
8	AccelerometerNoise	0.0817
8	GyroscopeNoise	0.0811
8		
	GyroscopeDriftNoise	0.0811
8	LinearAccelerationNoise	0.0791
8	LinearAccelerationDecayFactor	0.0789
9	AccelerometerNoise	0.0788
9	GyroscopeNoise	0.0782
9	GyroscopeDriftNoise	0.0782
9	LinearAccelerationNoise	0.0769
9	LinearAccelerationDecayFactor	0.0768
10		
	AccelerometerNoise	0.0768
10	GyroscopeNoise	0.0762
10	GyroscopeDriftNoise	0.0762
10	LinearAccelerationNoise	0.0754
10	LinearAccelerationDecayFactor	0.0753
11	AccelerometerNoise	0.0753
11	GyroscopeNoise	0.0747
11	GyroscopeDriftNoise	
		0.0747
11	LinearAccelerationNoise	0.0741
11	LinearAccelerationDecayFactor	0.0740
12	AccelerometerNoise	0.0740
12	GyroscopeNoise	0.0734
12	GyroscopeDriftNoise	0.0734
12	LinearAccelerationNoise	0.0728
12	LinearAccelerationDecayFactor	0.0728
13	AccelerometerNoise	0.0728
13	GyroscopeNoise	
		0.0721
13	GyroscopeDriftNoise	0.0721

```
13
                 LinearAccelerationNoise
                                                    0.0715
    13
                 LinearAccelerationDecayFactor
                                                    0.0715
    14
                 AccelerometerNoise
                                                    0.0715
    14
                 GyroscopeNoise
                                                    0.0706
    14
                 GyroscopeDriftNoise
                                                    0.0706
    14
                 LinearAccelerationNoise
                                                    0.0700
    14
                 LinearAccelerationDecayFactor
                                                    0.0700
    15
                 AccelerometerNoise
                                                    0.0700
    15
                 GyroscopeNoise
                                                    0.0690
    15
                 GyroscopeDriftNoise
                                                    0.0690
    15
                 LinearAccelerationNoise
                                                    0.0684
    15
                 LinearAccelerationDecayFactor
                                                    0.0684
    16
                 AccelerometerNoise
                                                    0.0684
    16
                                                    0.0672
                 GyroscopeNoise
    16
                                                    0.0672
                 GyroscopeDriftNoise
    16
                 LinearAccelerationNoise
                                                    0.0668
    16
                 LinearAccelerationDecayFactor
                                                    0.0667
    17
                 AccelerometerNoise
                                                    0.0667
    17
                 GyroscopeNoise
                                                    0.0655
    17
                 GyroscopeDriftNoise
                                                    0.0655
    17
                 LinearAccelerationNoise
                                                    0.0654
    17
                 LinearAccelerationDecayFactor
                                                    0.0654
    18
                 AccelerometerNoise
                                                    0.0654
    18
                                                    0.0641
                 GyroscopeNoise
    18
                 GyroscopeDriftNoise
                                                    0.0641
    18
                 LinearAccelerationNoise
                                                    0.0640
    18
                 LinearAccelerationDecayFactor
                                                    0.0639
    19
                 AccelerometerNoise
                                                    0.0639
    19
                 GyroscopeNoise
                                                    0.0627
    19
                 GyroscopeDriftNoise
                                                    0.0627
    19
                 LinearAccelerationNoise
                                                    0.0627
    19
                 LinearAccelerationDecayFactor
                                                    0.0624
    20
                 AccelerometerNoise
                                                    0.0624
    20
                 GyroscopeNoise
                                                    0.0614
    20
                 GyroscopeDriftNoise
                                                    0.0614
    20
                                                    0.0613
                 LinearAccelerationNoise
    20
                 LinearAccelerationDecayFactor
                                                    0.0613
Fuse the sensor data again using the tuned filter.
qEstTuned = fuse(ld.sensorData.Accelerometer, ...
    ld.sensorData.Gyroscope);
Compare the tuned and untuned filter RMS error performances.
```

```
dUntuned = rad2deg(dist(qEstUntuned, qTrue));
dTuned = rad2deg(dist(qEstTuned, qTrue));
rmsUntuned = sqrt(mean(dUntuned.^2))
rmsUntuned = 6.5864
rmsTuned = sqrt(mean(dTuned.^2))
rmsTuned = 3.5098
Visualize the results.
N = numel(dUntuned);
t = (0:N-1)./ fuse.SampleRate;
```

```
plot(t, dUntuned, 'r', t, dTuned, 'b');
legend('Untuned', 'Tuned');
title('imufilter - Tuned vs Untuned Error')
xlabel('Time (s)');
ylabel('Orientation Error (degrees)');
```



Save Tuned Parameters in MAT File Using Output Function

Load the recorded sensor data and ground truth data.

```
load('insfilterAsyncTuneData.mat');
```

Create timetables for the sensor data and the truth data.

```
sensorData = timetable(Accelerometer, Gyroscope, ...
    Magnetometer, GPSPosition, GPSVelocity, 'SampleRate', 100);
groundTruth = timetable(Orientation, Position, ...
    'SampleRate', 100);
```

Create an insfilterAsync filter object that has a few noise properties.

```
filter = insfilterAsync('State', initialState, ...
    'StateCovariance', initialStateCovariance, ...
    'AccelerometerBiasNoise', 1e-7, ...
    'GyroscopeBiasNoise', 1e-7, ...
```

```
'MagnetometerBiasNoise', le-7, ... 'GeomagneticVectorNoise', le-7);
```

Create a tuner configuration object for the filter. Define the OutputFcn property as a customized function, myOutputFcn, which saves the latest tuned parameters in a MAT file.

```
config = tunerconfig('insfilterAsync', ...
    'MaxIterations',5, ...
    'Display','none', ...
    'OutputFcn', @myOutputFcn);
config.TunableParameters = setdiff(config.TunableParameters, ...
    {'GeomagneticVectorNoise', 'AccelerometerBiasNoise', ...
    'GyroscopeBiasNoise', 'MagnetometerBiasNoise'});
config.TunableParameters
ans = 1x10 string
 Columns 1 through 3
    "AccelerationNoise"
                           "AccelerometerNoise"
                                                   "AngularVelocityN..."
 Columns 4 through 6
    "GPSPositionNoise"
                          "GPSVelocityNoise"
                                                "GyroscopeNoise"
 Columns 7 through 9
                                              "QuaternionNoise"
    "MagnetometerNoise"
                           "PositionNoise"
 Column 10
    "VelocityNoise"
```

Use the tuner noise function to obtain a set of initial sensor noises used in the filter.

```
measNoise = tunernoise('insfilterAsync')
measNoise = struct with fields:
    AccelerometerNoise: 1
        GyroscopeNoise: 1
        MagnetometerNoise: 1
        GPSPositionNoise: 1
        GPSVelocityNoise: 1
```

Tune the filter and obtain the tuned parameters.

```
tunedParams = tune(filter,measNoise,sensorData,groundTruth,config);
```

Display the save parameters using the saved file.

```
GPSPositionNoise: 1.1664
GPSVelocityNoise: 0.5210

GeomagneticVectorNoise: [1.0000e-07 1.0000e-07 1.0000e-07]
GyroscopeBiasNoise: [1.0000e-07 1.0000e-07 1.0000e-07]
GyroscopeNoise: 0.5210

MagnetometerBiasNoise: [1.0000e-07 1.0000e-07 1.0000e-07]
MagnetometerNoise: 1.0128
PositionNoise: [5.2100e-07 5.2100e-07 5.2100e-07]
QuaternionNoise: [1.3239e-06 1.3239e-06 1.3239e-06]
ReferenceLocation: [0 0 0]
State: [28x1 double]
StateCovariance: [28x28 double]
VelocityNoise: [6.3678e-07 6.3678e-07]
```

The output function

```
function stop = myOutputFcn(params, ~)
save('myfile.mat','params'); % overwrite the file with latest
stop = false;
end
```

See Also

ahrs10filter|ahrsfilter|imufilter|insfilterAsync|insfilterErrorState|
insfilterMARG|insfilterNonholonomic

Introduced in R2020b

validatorOccupancyMap

State validator based on 2-D grid map

Description

The validatorOccupancyMap object validates states and discretized motions based on the value in a 2-D occupancy map. An occupied map location is interpreted as an invalid state.

Creation

Syntax

Description

validator = validatorOccupancyMap creates a 2-D occupancy map validator associated with an SE2 state space with default settings.

validator = validatorOccupancyMap(stateSpace) creates a validator in the given state
space definition derived from nav.StateSpace.

validator = validatorOccupancyMap(stateSpace,Name,Value) specifies the Map or XYIndices properties using Name,Value pair arguments.

Properties

StateSpace — State space for validating states

stateSpaceSE2 (default) | subclass of nav.StateSpace

State space for validating states, specified as a subclass of nav.StateSpace. Provided state space objects include:

- stateSpaceSE2
- stateSpaceDubins
- stateSpaceReedsShepp

Map — Map used for validating states

binaryOccupancyMap(10,10) (default) | binaryOccupancyMap object | occupancyMap object

Map used for validating states, specified as a binaryOccupancyMap or occupancyMap object.

ValidationDistance — Interval for checking state validity

Inf (default) | positive numeric scalar

Interval for sampling between states and checking state validity, specified as a positive numeric scalar.

XYIndices — State variable mapping for xy-coordinates

[1 2] (default) | [xIdx yIdx]

State variable mapping for xy-coordinates in state vector, specified as a two-element vector, [xIdx yIdx]. For example, if a state vector is given as [r p y x y z], the xy-coordinates are [4 5].

Object Functions

copy Create deep copy of state validator object

isStateValid Check if state is valid

isMotionValid Check if path between states is valid

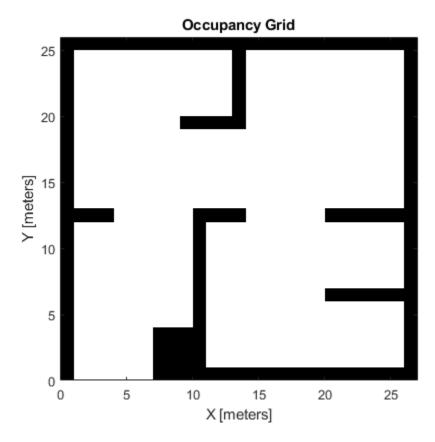
Examples

Validate Path Through Occupancy Map Environment

This example shows how to validate paths through an evironment.

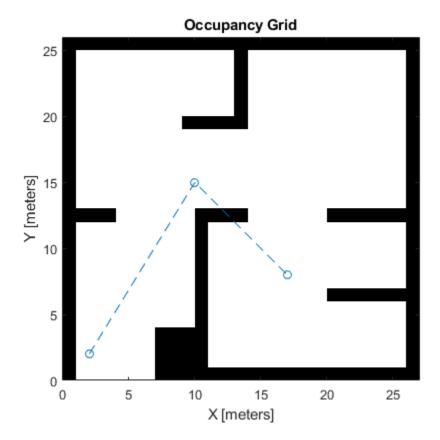
Load example maps. Use the simple map to create a binary occupancy map.

```
load exampleMaps.mat
map = occupancyMap(simpleMap);
show(map)
```



Specify a coarse path through the map.

```
path = [2 2 pi/2; 10 15 0; 17 8 -pi/2];
hold on
plot(path(:,1),path(:,2),"--o")
```



Create a state validator using the stateSpaceSE2 definition. Specify the map and the distance for interpolating and validating path segments.

```
validator = validatorOccupancyMap(stateSpaceSE2);
validator.Map = map;
validator.ValidationDistance = 0.1;
```

Check the points of the path are valid states. All three points are in free space, so are considered valid.

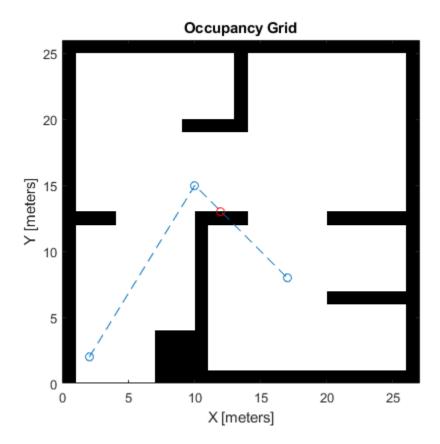
```
isValid = isStateValid(validator,path)
isValid = 3x1 logical array

1
1
1
```

Check the motion between each sequential path states. The isMotionValid function interpolates along the path between states. If a path segment is invalid, plot the last valid point along the path.

```
startStates = [path(1,:);path(2,:)];
endStates = [path(2,:);path(3,:)];
for i = 1:2
    [isPathValid, lastValid] = isMotionValid(validator,startStates(i,:),endStates(i,:));
    if ~isPathValid
        plot(lastValid(1),lastValid(2),'or')
```

end end hold off



Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

Specify the Map and XYIndices properties when your create the object. For example:

validator = validatorOccupancyMap('Map',occMap,'XYIndices',[4 5])

See Also

nav.StateSpace|nav.StateValidator|stateSpaceSE2

Introduced in R2019b

validatorOccupancyMap3D

State validator based on 3-D grid map

Description

The validatorOccupancyMap3D object validates states and discretized motions based on occupancy values in a 3-D occupancy map. The object interprets obstacle-free map locations as valid states. The object interprets occupied and unknown map locations as invalid states.

Creation

Syntax

```
validator = validatorOccupancyMap3D
validator = validatorOccupancyMap3D(stateSpace)
validator = validatorOccupancyMap3D(stateSpace,Name,Value)
```

Description

validator = validatorOccupancyMap3D creates a 3-D occupancy map validator associated with
an SE(3) state space with default settings.

validator = validatorOccupancyMap3D(stateSpace) creates a validator in the specified state space. The stateSpace input sets the value of the StateSpace property.

validator = validatorOccupancyMap3D(stateSpace,Name,Value) sets properties using one or more name-value pairs. Unspecified properties have default values. Enclose each property name in quotes.

For example, validatorOccupancyMap3D('ValidationDistance', 0.1) creates a 3-D occupancy map validator with a sampling interval of 0.1.

Properties

StateSpace — State space for validating states

stateSpaceSE3 object (default) | subclass of nav.StateSpace

This property is read-only.

State space for validating states, specified as a subclass of nav.StateSpace. These are the predefined state space objects:

- stateSpaceSE3
- stateSpaceSE2
- stateSpaceDubins
- stateSpaceReedsShepp

Example: validatorOccupancyMap3D(stateSpaceSE3)

Map — Map used for validating states

occupancyMap3D (default) | occupancyMap3D object

Map used for validating states, specified as an occupancyMap3D object.

Example: validator.Map = occupancyMap3D(10)

ValidationDistance — Interval for checking state validity

Inf (default) | positive numeric scalar

Interval for sampling between states and checking state validity, specified as a positive numeric scalar.

```
Example: validator.ValidationDistance = 0.1
Data Types: double
```

XYZIndices — State variable mapping for xyz-coordinates

[1 2 3] (default) | three-element vector

State variable mapping for xyz-coordinates in the state vector, specified as a three-element vector of form [xIdx yIdx zIdx].

Data Types: double

Object Functions

copy Create deep copy of state validator object isMotionValid Check if path between states is valid

isStateValid Check if state is valid

Examples

Validate Path Through 3-D Occupancy Map Environment

Create a 3-D occupancy map and associated state validator. Plan, validate, and visualize a path through the occupancy map.

Load and Assign Map to State Validator

Load a 3-D occupancy map of a city block into the workspace. Specify a threshold for which cells to consider as obstacle-free.

```
mapData = load('dMapCityBlock.mat');
omap = mapData.omap;
omap.FreeThreshold = 0.5;
```

Inflate the occupancy map to add a buffer zone for safe operation around the obstacles.

```
inflate(omap,5)
```

Create an SE(3) state space object with bounds for state variables.

```
-10 100;
inf inf;
inf inf;
inf inf;
inf inf]);
```

Create a 3-D occupancy map state validator using the created state space.

```
sv = validatorOccupancyMap3D(ss);
```

Assign the occupancy map to the state validator object. Specify the sampling distance interval.

```
sv.Map = omap;
sv.ValidationDistance = 0.1;
```

Plan and Visualize Path

Create a path planner with increased maximum connection distance. Reduce the maximum number of iterations.

```
planner = plannerRRT(ss,sv);
planner.MaxConnectionDistance = 50;
planner.MaxIterations = 1000;
```

Create a user-defined evaluation function for determining whether the path reaches the goal. Specify the probability of choosing the goal state during sampling.

```
planner.GoalReachedFcn = @(~,x,y)(norm(x(1:3)-y(1:3))<5);
planner.GoalBias = 0.1;

Set the start and goal states.

start = [40 180 25 0.7 0.2 0 0.1];
goal = [150 33 35 0.3 0 0.1 0.6];

Plan a path using the specified start, goal, and planner.

[pth0bj,solnInfo] = plan(planner,start,goal);

Check that the points of the path are valid states.

isValid = isStateValid(sv,pth0bj.States)

isValid = 6x1 logical array

1
1
1
1</pre>
```

Check that the motion between each sequential path state is valid.

```
isPathValid = zeros(size(pth0bj.States,1)-1,1,'logical');
for i = 1:size(pth0bj.States,1)-1
   [isPathValid(i),~] = isMotionValid(sv,pth0bj.States(i,:),...
        pth0bj.States(i+1,:));
```

1

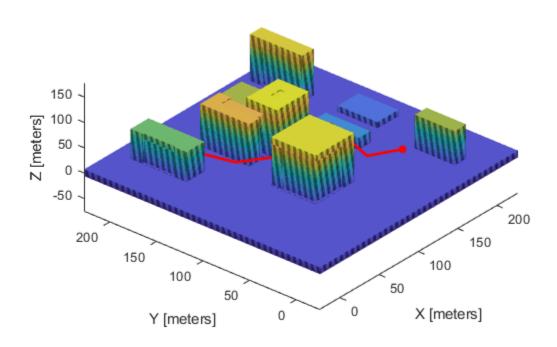
end isPathValid

isPathValid = 5x1 logical array

Visualize the results.

```
show(omap)
hold on
scatter3(start(1,1),start(1,2),start(1,3),'g','filled') % draw start state
scatter3(goal(1,1),goal(1,2),goal(1,3),'r','filled') % draw goal state
plot3(pth0bj.States(:,1),pth0bj.States(:,2),pth0bj.States(:,3),...
    'r-','LineWidth',2) % draw path
```

Occupancy Map



Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder $^{\text{\tiny TM}}$.

See Also

occupancyMap3D | stateSpaceSE3 | validatorOccupancyMap

Introduced in R2020b

validatorVehicleCostmap

State validator based on 2-D costmap

Description

The validatorOccupancyMap object validates states and discretized motions based on the value in a 2-D costmap. An occupied map location is interpreted as an invalid state.

Creation

Syntax

Description

validator = validatorVehicleCostmap creates a vehicle cost map validator associated with an SE2 state space with default settings.

validator = validatorVehicleCostmap(stateSpace) creates a validator in the given state
space definition derived from nav.StateSpace.

validator = validatorVehicleCostmap(stateSpace,xyIndices)sets the XYIndices
property to specify which variables in the state vector define the xy-coordinates.

validator = validatorVehicleCostmap(stateSpace,Name,Value) specifies the Map or XYIndices properties using Name,Value pair arguments.

Properties

StateSpace — State space for validating states

stateSpaceSE2 (default) | subclass of nav.StateSpace

State space for validating states, specified as a subclass of nav.StateSpace. Provided state space objects include:

- stateSpaceSE2
- stateSpaceDubins
- stateSpaceReedsShepp

Map — Map used for validating states

vehicleCostMap(10,10) (default) | vehicleCostMap object

Map used for validating states, specified as a vehicleCostMap object.

ValidationDistance — Interval for checking state validity

Inf (default) | positive numeric scalar

Interval for sampling between states and checking state validity, specified as a positive numeric scalar.

XYIndices — State variable mapping for xy-coordinates

```
[1 2] (default) | [xIdx yIdx]
```

State variable mapping for xy-coordinates in state vector, specified as a two-element vector, [xIdx yIdx]. For example, if a state vector is given as [r p y x y z], the xy-coordinates are [4 5].

ThetaIndex — State variable mapping for theta coordinate

NaN (default) | positive integer

State variable mapping for *theta* coordinate in state vector, specified as a positive integer. For example, if a state vector is given as [x y theta], the *theta* coordinate is 3.

Object Functions

copy Create deep copy of state validator object

isStateValid Check if state is valid

isMotionValid Check if path between states is valid

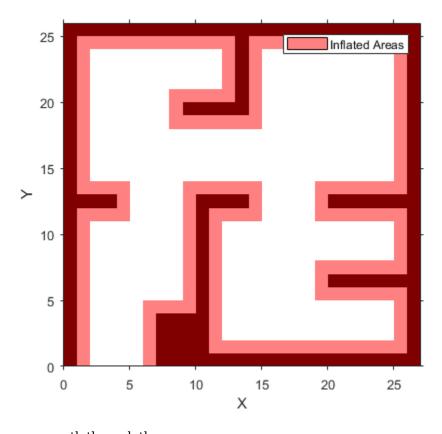
Examples

Validate Path Through Vehicle Costmap Environment

This example shows how to validate paths through an evironment.

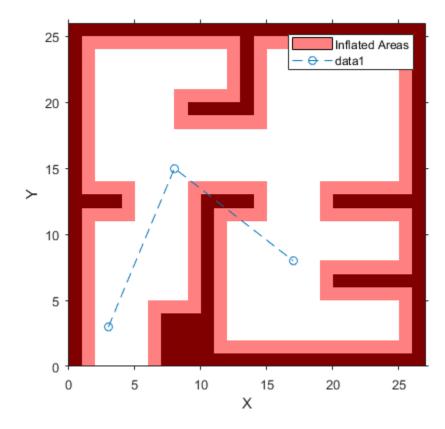
Load example maps. Use the simple map to create a vehicle cost map. Specify an inflation raidus of 1 meter.

```
load exampleMaps.mat
map = vehicleCostmap(double(simpleMap));
map.CollisionChecker = inflationCollisionChecker("InflationRadius",1);
plot(map)
```



Specify a coarse path through the map.

```
path = [3 3 pi/2; 8 15 0; 17 8 -pi/2];
hold on
plot(path(:,1),path(:,2),"--o")
```



Create a state validator using the stateSpaceSE2 definition. Specify the map and the distance for interpolating and validating path segments.

```
validator = validatorVehicleCostmap(stateSpaceSE2);
validator.Map = map;
validator.ValidationDistance = 0.1;
```

Check the points of the path are valid states. All three points are in free space, so are considered valid.

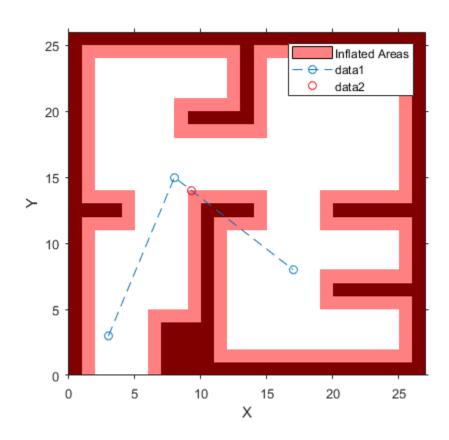
```
isValid = isStateValid(validator,path)
isValid = 3x1 logical array

1
1
1
```

Check the motion between each sequential path states. The isMotionValid function interpolates along the path between states. If a path segment is invalid, plot the last valid point along the path.

```
startStates = [path(1,:);path(2,:)];
endStates = [path(2,:);path(3,:)];
for i = 1:2
    [isPathValid, lastValid] = isMotionValid(validator, startStates(i,:), endStates(i,:));
    if ~isPathValid
        plot(lastValid(1), lastValid(2), 'or')
```

end end hold off



Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

For code generation, the map used inside the object must remain constant.

See Also

nav.StateSpace | nav.StateValidator | stateSpaceSE2 | validatorOccupancyMap

Introduced in R2019b

copy

Create deep copy of state validator object

Syntax

```
validator2 = copy(validator1)
```

Description

validator2 = copy(validator1) creates a deep copy of the specified state validator object.

Examples

Create Deep Copy of 3-D Occupancy Map State Validator Object

Create a validator object and set a custom validation distance.

Create a deep copy of the state validator object.

Verify that the ValidationDistance property values of the two state validator objects are equal.

isequal(validator.ValidationDistance,validator2.ValidationDistance)

```
ans = logical
```

Input Arguments

validator1 — State validator object

validatorOccupancyMap object | validatorOccupancyMap3D object |
validatorVehicleCostmap object

State validator object, specified as a validatorOccupancyMap, validatorOccupancyMap3D, or validatorVehicleCostmap object.

Output Arguments

validator2 — State validator object

validatorOccupancyMap object | validatorOccupancyMap3D object |
validatorVehicleCostmap object

State validator object, returned as a validator Occupancy Map, validator Occupancy Map 3D, or validator Vehicle Cost map object.

See Also

validatorOccupancyMap | validatorOccupancyMap3D | validatorVehicleCostmap

Introduced in R2020b

isMotionValid

Check if path between states is valid

Syntax

[isValid, lastValid] = isMotionValid(validator, state1, state2)

Description

[isValid,lastValid] = isMotionValid(validator,state1,state2) checks if the path between two states is valid by interpolating between states. The function also returns the last valid state along the path.

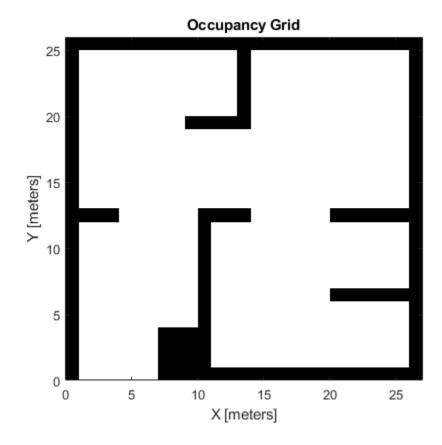
Examples

Validate Path Through Occupancy Map Environment

This example shows how to validate paths through an evironment.

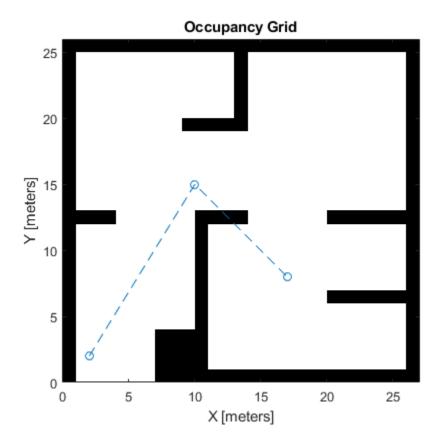
Load example maps. Use the simple map to create a binary occupancy map.

```
load exampleMaps.mat
map = occupancyMap(simpleMap);
show(map)
```



Specify a coarse path through the map.

```
path = [2 2 pi/2; 10 15 0; 17 8 -pi/2];
hold on
plot(path(:,1),path(:,2),"--o")
```



Create a state validator using the stateSpaceSE2 definition. Specify the map and the distance for interpolating and validating path segments.

```
validator = validatorOccupancyMap(stateSpaceSE2);
validator.Map = map;
validator.ValidationDistance = 0.1;
```

Check the points of the path are valid states. All three points are in free space, so are considered valid.

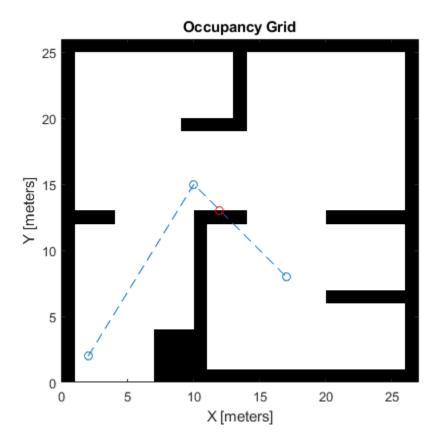
```
isValid = isStateValid(validator,path)
isValid = 3x1 logical array

1
1
1
```

Check the motion between each sequential path states. The isMotionValid function interpolates along the path between states. If a path segment is invalid, plot the last valid point along the path.

```
startStates = [path(1,:);path(2,:)];
endStates = [path(2,:);path(3,:)];
for i = 1:2
    [isPathValid, lastValid] = isMotionValid(validator, startStates(i,:), endStates(i,:));
    if ~isPathValid
        plot(lastValid(1), lastValid(2), 'or')
```

end end hold off

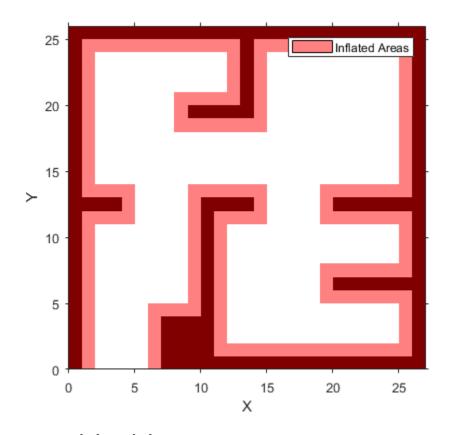


Validate Path Through Vehicle Costmap Environment

This example shows how to validate paths through an evironment.

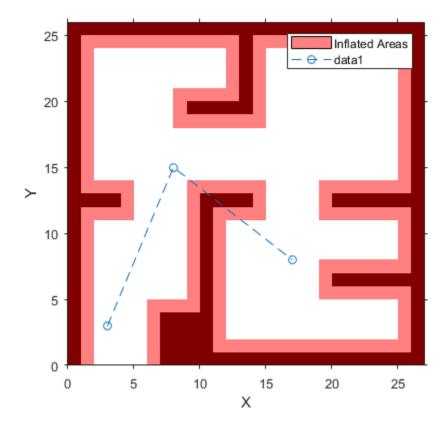
Load example maps. Use the simple map to create a vehicle cost map. Specify an inflation raidus of 1 meter.

```
load exampleMaps.mat
map = vehicleCostmap(double(simpleMap));
map.CollisionChecker = inflationCollisionChecker("InflationRadius",1);
plot(map)
```



Specify a coarse path through the map.

```
path = [3 3 pi/2; 8 15 0; 17 8 -pi/2];
hold on
plot(path(:,1),path(:,2),"--o")
```



Create a state validator using the stateSpaceSE2 definition. Specify the map and the distance for interpolating and validating path segments.

```
validator = validatorVehicleCostmap(stateSpaceSE2);
validator.Map = map;
validator.ValidationDistance = 0.1;
```

Check the points of the path are valid states. All three points are in free space, so are considered valid.

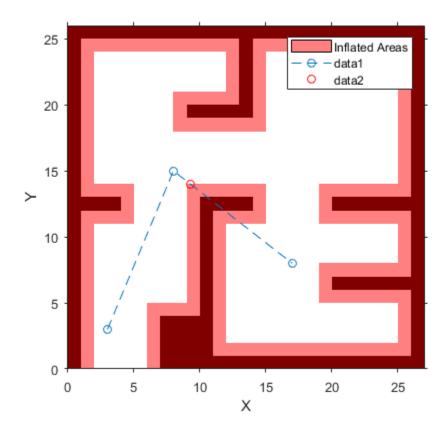
```
isValid = isStateValid(validator,path)
isValid = 3x1 logical array

1
1
1
```

Check the motion between each sequential path states. The isMotionValid function interpolates along the path between states. If a path segment is invalid, plot the last valid point along the path.

```
startStates = [path(1,:);path(2,:)];
endStates = [path(2,:);path(3,:)];
for i = 1:2
    [isPathValid, lastValid] = isMotionValid(validator, startStates(i,:), endStates(i,:));
    if ~isPathValid
        plot(lastValid(1), lastValid(2), 'or')
```

```
end
end
hold off
```



Validate Path Through 3-D Occupancy Map Environment

Create a 3-D occupancy map and associated state validator. Plan, validate, and visualize a path through the occupancy map.

Load and Assign Map to State Validator

Load a 3-D occupancy map of a city block into the workspace. Specify a threshold for which cells to consider as obstacle-free.

```
mapData = load('dMapCityBlock.mat');
omap = mapData.omap;
omap.FreeThreshold = 0.5;
```

Inflate the occupancy map to add a buffer zone for safe operation around the obstacles.

inflate(omap,5)

Create an SE(3) state space object with bounds for state variables.

```
-10 100;
inf inf;
inf inf;
inf inf;
inf inf]);
```

Create a 3-D occupancy map state validator using the created state space.

```
sv = validatorOccupancyMap3D(ss);
```

Assign the occupancy map to the state validator object. Specify the sampling distance interval.

```
sv.Map = omap;
sv.ValidationDistance = 0.1;
```

Plan and Visualize Path

Create a path planner with increased maximum connection distance. Reduce the maximum number of iterations.

```
planner = plannerRRT(ss,sv);
planner.MaxConnectionDistance = 50;
planner.MaxIterations = 1000;
```

Create a user-defined evaluation function for determining whether the path reaches the goal. Specify the probability of choosing the goal state during sampling.

```
planner.GoalReachedFcn = @(~,x,y)(norm(x(1:3)-y(1:3))<5);
planner.GoalBias = 0.1;

Set the start and goal states.

start = [40 180 25 0.7 0.2 0 0.1];
goal = [150 33 35 0.3 0 0.1 0.6];

Plan a path using the specified start, goal, and planner.

[pth0bj,solnInfo] = plan(planner,start,goal);

Check that the points of the path are valid states.

isValid = isStateValid(sv,pth0bj.States)

isValid = 6x1 logical array</pre>
```

```
isValid = 6x1 logical array

1
1
1
1
1
```

Check that the motion between each sequential path state is valid.

```
isPathValid = zeros(size(pth0bj.States,1)-1,1,'logical');
for i = 1:size(pth0bj.States,1)-1
   [isPathValid(i),~] = isMotionValid(sv,pth0bj.States(i,:),...
        pth0bj.States(i+1,:));
```

end isPathValid

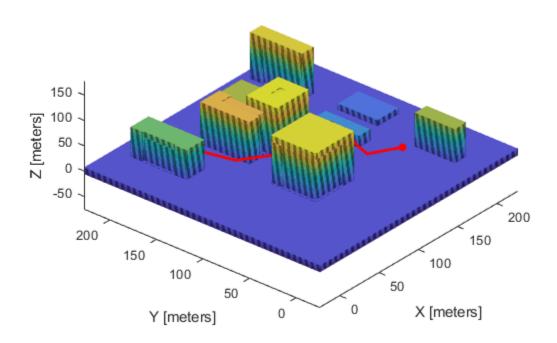
isPathValid = 5x1 logical array
1

1 1 1

Visualize the results.

```
show(omap)
hold on
scatter3(start(1,1),start(1,2),start(1,3),'g','filled') % draw start state
scatter3(goal(1,1),goal(1,2),goal(1,3),'r','filled') % draw goal state
plot3(pth0bj.States(:,1),pth0bj.States(:,2),pth0bj.States(:,3),...
    'r-','LineWidth',2) % draw path
```

Occupancy Map



Input Arguments

validator — State validator object

object of subclass of nav.StateValidator

State validator object, specified as an object of subclass of nav.StateValidator. These are the predefined state validator objects:

- validatorOccupancyMap
- validatorVehicleCostmap
- validatorOccupancyMap3D

state1 — Initial state positions

n-element row vector | *m*-by-*n* matrix

Initial state positions, specified as an n-element row vector or m-by-n matrix. n is the dimension of the state space specified in validator. m is the number of states to validate.

Data Types: single | double

state2 — Final state positions

n-element row vector | *m*-by-*n* matrix

Final state positions, specified as an n-element row vector or m-by-n matrix. n is the dimension of the state space specified in validator. m is the number of states to validate.

Data Types: single | double

Output Arguments

isValid — Valid states

m-element logical column vector

Valid states, returned as an *m*-element logical column vector.

Data Types: logical

lastValid — Final valid state along each path

n-element row vector | *m*-by-*n* matrix

Final valid state along each path, returned as an n-element row vector or m-by-n matrix. n is the dimension of the state space specified in the state space property in validator. m is the number of paths validated. Each row contains the final valid state along the associated path.

Data Types: single | double

See Also

isStateValid | nav.StateSpace | nav.StateValidator | stateSpaceSE2

Introduced in R2019b

isStateValid

Check if state is valid

Syntax

isValid = isStateValid(validator,states)

Description

isValid = isStateValid(validator, states) checks if a set of given states are valid.

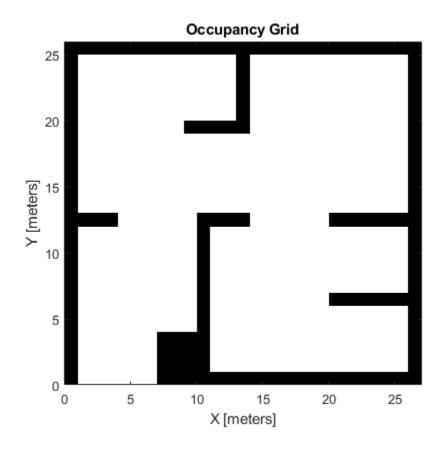
Examples

Validate Path Through Occupancy Map Environment

This example shows how to validate paths through an evironment.

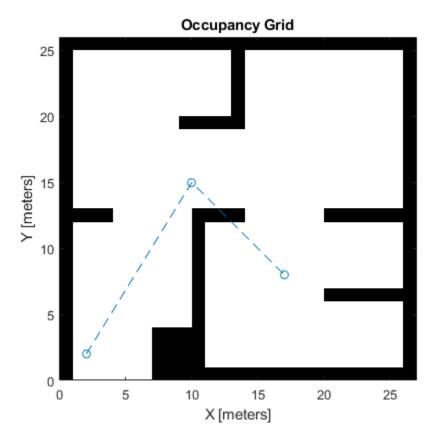
Load example maps. Use the simple map to create a binary occupancy map.

```
load exampleMaps.mat
map = occupancyMap(simpleMap);
show(map)
```



Specify a coarse path through the map.

```
path = [2 2 pi/2; 10 15 0; 17 8 -pi/2];
hold on
plot(path(:,1),path(:,2),"--o")
```



Create a state validator using the stateSpaceSE2 definition. Specify the map and the distance for interpolating and validating path segments.

```
validator = validatorOccupancyMap(stateSpaceSE2);
validator.Map = map;
validator.ValidationDistance = 0.1;
```

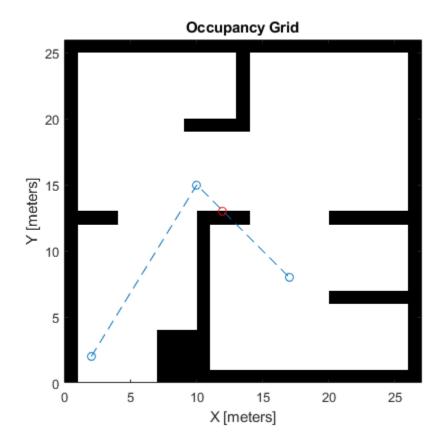
Check the points of the path are valid states. All three points are in free space, so are considered valid.

```
isValid = isStateValid(validator,path)
isValid = 3x1 logical array

1
1
1
```

Check the motion between each sequential path states. The <code>isMotionValid</code> function interpolates along the path between states. If a path segment is invalid, plot the last valid point along the path.

```
startStates = [path(1,:);path(2,:)];
endStates = [path(2,:);path(3,:)];
  for i = 1:2
      [isPathValid, lastValid] = isMotionValid(validator,startStates(i,:),endStates(i,:));
      if ~isPathValid
            plot(lastValid(1),lastValid(2),'or')
      end
  end
hold off
```

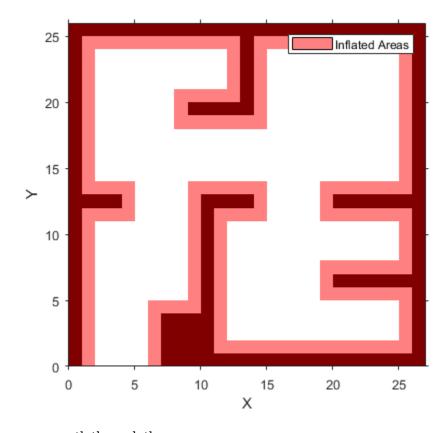


Validate Path Through Vehicle Costmap Environment

This example shows how to validate paths through an evironment.

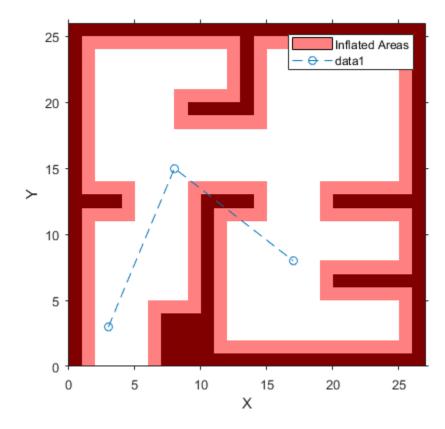
Load example maps. Use the simple map to create a vehicle cost map. Specify an inflation raidus of 1 meter.

```
load exampleMaps.mat
map = vehicleCostmap(double(simpleMap));
map.CollisionChecker = inflationCollisionChecker("InflationRadius",1);
plot(map)
```



Specify a coarse path through the map.

```
path = [3 3 pi/2; 8 15 0; 17 8 -pi/2];
hold on
plot(path(:,1),path(:,2),"--o")
```



Create a state validator using the stateSpaceSE2 definition. Specify the map and the distance for interpolating and validating path segments.

```
validator = validatorVehicleCostmap(stateSpaceSE2);
validator.Map = map;
validator.ValidationDistance = 0.1;
```

Check the points of the path are valid states. All three points are in free space, so are considered valid.

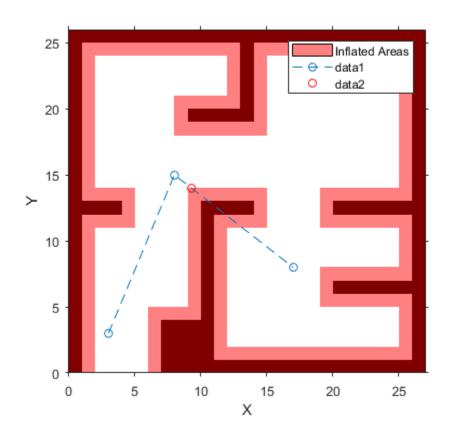
```
isValid = isStateValid(validator,path)
isValid = 3x1 logical array

1
1
1
```

Check the motion between each sequential path states. The isMotionValid function interpolates along the path between states. If a path segment is invalid, plot the last valid point along the path.

```
startStates = [path(1,:);path(2,:)];
endStates = [path(2,:);path(3,:)];
for i = 1:2
    [isPathValid, lastValid] = isMotionValid(validator, startStates(i,:), endStates(i,:));
    if ~isPathValid
        plot(lastValid(1), lastValid(2), 'or')
```

```
end
end
hold off
```



Validate Path Through 3-D Occupancy Map Environment

Create a 3-D occupancy map and associated state validator. Plan, validate, and visualize a path through the occupancy map.

Load and Assign Map to State Validator

Load a 3-D occupancy map of a city block into the workspace. Specify a threshold for which cells to consider as obstacle-free.

```
mapData = load('dMapCityBlock.mat');
omap = mapData.omap;
omap.FreeThreshold = 0.5;
```

Inflate the occupancy map to add a buffer zone for safe operation around the obstacles.

inflate(omap,5)

Create an SE(3) state space object with bounds for state variables.

```
-10 100;
inf inf;
inf inf;
inf inf;
inf inf]);
```

Create a 3-D occupancy map state validator using the created state space.

```
sv = validatorOccupancyMap3D(ss);
```

Assign the occupancy map to the state validator object. Specify the sampling distance interval.

```
sv.Map = omap;
sv.ValidationDistance = 0.1;
```

Plan and Visualize Path

Create a path planner with increased maximum connection distance. Reduce the maximum number of iterations.

```
planner = plannerRRT(ss,sv);
planner.MaxConnectionDistance = 50;
planner.MaxIterations = 1000;
```

Create a user-defined evaluation function for determining whether the path reaches the goal. Specify the probability of choosing the goal state during sampling.

```
the probability of choosing the goal state during sampling.

planner.GoalReachedFcn = @(~,x,y)(norm(x(1:3)-y(1:3))<5);
planner.GoalBias = 0.1;

Set the start and goal states.

start = [40 180 25 0.7 0.2 0 0.1];
goal = [150 33 35 0.3 0 0.1 0.6];

Plan a path using the specified start, goal, and planner.

[pth0bj,solnInfo] = plan(planner,start,goal);

Check that the points of the path are valid states.

isValid = isStateValid(sv,pth0bj.States)

isValid = 6x1 logical array

1
1
1
1
1
```

Check that the motion between each sequential path state is valid.

```
isPathValid = zeros(size(pth0bj.States,1)-1,1,'logical');
for i = 1:size(pth0bj.States,1)-1
   [isPathValid(i),~] = isMotionValid(sv,pth0bj.States(i,:),...
        pth0bj.States(i+1,:));
```

1

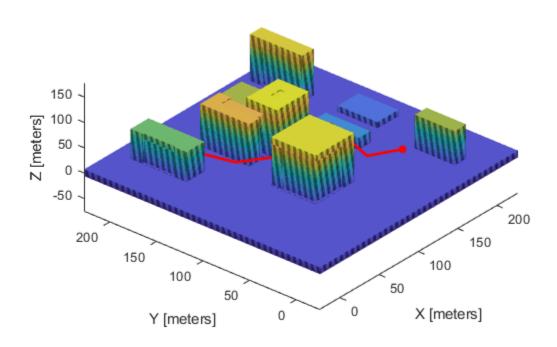
end isPathValid

isPathValid = 5x1 logical array

Visualize the results.

```
show(omap)
hold on
scatter3(start(1,1),start(1,2),start(1,3),'g','filled') % draw start state
scatter3(goal(1,1),goal(1,2),goal(1,3),'r','filled') % draw goal state
plot3(pth0bj.States(:,1),pth0bj.States(:,2),pth0bj.States(:,3),...
    'r-','LineWidth',2) % draw path
```

Occupancy Map



Input Arguments

validator — State validator object

object of subclass of nav.StateValidator

State validator object, specified as an object of subclass of nav.StateValidator. These are the predefined state validator objects:

- validatorOccupancyMap
- validatorVehicleCostmap
- validatorOccupancyMap3D

states — State positions

n-element row vector | *m*-by-*n* matrix

State positions, specified as an n-element row vector or m-by-n matrix. n is the dimension of the state space specified in validator. m is the number of states to validate.

Data Types: single | double

Output Arguments

isValid — Valid states

m-element logical column vector

Valid states, returned as an *m*-element logical column vector.

Data Types: logical

See Also

isMotionValid | nav.StateSpace | nav.StateValidator | stateSpaceSE2

Introduced in R2019b

waypointTrajectory

Waypoint trajectory generator

Description

The waypointTrajectory System object generates trajectories using specified waypoints. When you create the System object, you can optionally specify the time of arrival, velocity, and orientation at each waypoint. See "Algorithms" on page 2-1298 for more details.

To generate a trajectory from waypoints:

- 1 Create the waypointTrajectory object and set its properties.
- **2** Call the object as if it were a function.

To learn more about how System objects work, see What Are System Objects?.

Creation

Syntax

```
trajectory = waypointTrajectory
trajectory = waypointTrajectory(Waypoints, TimeOfArrival)
trajectory = waypointTrajectory(Waypoints, TimeOfArrival, Name, Value)
```

Description

trajectory = waypointTrajectory returns a System object, trajectory, that generates a trajectory based on default stationary waypoints.

trajectory = waypointTrajectory(Waypoints, TimeOfArrival) specifies the Waypoints that the generated trajectory passes through and the TimeOfArrival at each waypoint.

trajectory = waypointTrajectory(Waypoints, TimeOfArrival, Name, Value) sets each creation argument or property Name to the specified Value. Unspecified properties and creation arguments have default or inferred values.

Example: trajectory = waypointTrajectory([10,10,0;20,20,0;20,20,10],[0,0.5,10]) creates a waypoint trajectory System object, trajectory, that starts at waypoint [10,10,0], and then passes through [20,20,0] after 0.5 seconds and [20,20,10] after 10 seconds.

Creation Arguments

Creation arguments are properties which are set during creation of the System object and cannot be modified later. If you do not explicitly set a creation argument value, the property value is inferred.

If you specify any creation argument, then you must specify both the Waypoints and TimeOfArrival creation arguments. You can specify Waypoints and TimeOfArrival as value-only arguments or name-value pairs.

Properties

Unless otherwise indicated, properties are *nontunable*, which means you cannot change their values after calling the object. Objects lock when you call them, and the release function unlocks them.

If a property is tunable, you can change its value at any time.

For more information on changing property values, see System Design in MATLAB Using System Objects.

SampleRate — Sample rate of trajectory (Hz)

100 (default) | positive scalar

Sample rate of trajectory in Hz, specified as a positive scalar.

Tunable: Yes

Data Types: double

SamplesPerFrame — Number of samples per output frame

1 (default) | positive scalar integer

Number of samples per output frame, specified as a positive scalar integer.

Tunable: Yes

Data Types: double

Waypoints — Positions in the navigation coordinate system (m)

N-by-3 matrix

Positions in the navigation coordinate system in meters, specified as an N-by-3 matrix. The columns of the matrix correspond to the first, second, and third axes, respectively. The rows of the matrix, N, correspond to individual waypoints.

Dependencies

To set this property, you must also set valid values for the TimeOfArrival property.

Data Types: double

TimeOfArrival — Time at each waypoint (s)

N-element column vector of nonnegative increasing numbers

Time corresponding to arrival at each waypoint in seconds, specified as an N-element column vector. The first element of TimeOfArrival must be 0. The number of samples, N, must be the same as the number of samples (rows) defined by Waypoints.

Dependencies

To set this property, you must also set valid values for the Waypoints property.

Data Types: double

Velocities — Velocity in navigation coordinate system at each waypoint (m/s)

N-by-3 matrix

Velocity in the navigation coordinate system at each way point in meters per second, specified as an N-by-3 matrix. The columns of the matrix correspond to the first, second, and third axes, respectively.

The number of samples, N, must be the same as the number of samples (rows) defined by Waypoints.

If the velocity is specified as a non-zero value, the object automatically calculates the course of the trajectory. If the velocity is specified as zero, the object infers the course of the trajectory from adjacent waypoints.

Dependencies

To set this property, you must also set valid values for the Waypoints and TimeOfArrival properties.

Data Types: double

Course — Horizontal direction of travel (degree)

N-element real vector

Horizontal direction of travel, specified as an *N*-element real vector in degrees. The number of samples, *N*, must be the same as the number of samples (rows) defined by Waypoints. If neither Velocities nor Course is specified, course is inferred from the waypoints.

Dependencies

To set this property, the Velocities property must not be specified in object creation.

Data Types: double

GroundSpeed — Groundspeed at each waypoint (m/s)

N-element real vector

Groundspeed at each waypoint, specified as an N-element real vector in m/s. If the property is not specified, it is inferred from the waypoints. The number of samples, N, must be the same as the number of samples (rows) defined by Waypoints.

Dependencies

To set this property, the Velocities property must not be specified at object creation.

Data Types: double

ClimbRate — Climb rate at each waypoint (m/s)

N-element real vector

Climb Rate at each waypoint, specified as an *N*-element real vector in degrees. The number of samples, *N*, must be the same as the number of samples (rows) defined by Waypoints. If neither Velocities nor Course is specified, climbrate is inferred from the waypoints.

Dependencies

To set this property, the Velocities property must not be specified at object creation.

Data Types: double

Orientation — **Orientation** at each waypoint

N-element quaternion column vector | 3-by-3-by-*N* array of real numbers

Orientation at each waypoint, specified as an N-element quaternion column vector or 3-by-3-by-N array of real numbers. The number of quaternions or rotation matrices, N, must be the same as the number of samples (rows) defined by Waypoints.

If Orientation is specified by quaternions, the underlying class must be double.

Dependencies

To set this property, you must also set valid values for the Waypoints and TimeOfArrival properties.

Data Types: quaternion | double

AutoPitch — Align pitch angle with direction of motion

false (default) | true

Align pitch angle with the direction of motion, specified as true or false. When specified as true, the pitch angle automatically aligns with the direction of motion. If specified as false, the pitch angle is set to zero (level orientation).

Dependencies

To set this property, the Orientation property must not be specified at object creation.

AutoBank — Align roll angle to counteract centripetal force

false (default) | true

Align roll angle to counteract the centripetal force, specified as true or false. When specified as true, the roll angle automatically counteract the centripetal force. If specified as false, the roll angle is set to zero (flat orientation).

Dependencies

To set this property, the Orientation property must not be specified at object creation.

ReferenceFrame — Reference frame of trajectory

'NED' (default) | 'ENU'

Reference frame of the trajectory, specified as 'NED' (North-East-Down) or 'ENU' (East-North-Up).

Usage

Syntax

[position,orientation,velocity,acceleration,angularVelocity] = trajectory()

Description

[position, orientation, velocity, acceleration, angular Velocity] = trajectory() outputs a frame of trajectory data based on specified creation arguments and properties.

Output Arguments

position — Position in local navigation coordinate system (m)

M-by-3 matrix

Position in the local navigation coordinate system in meters, returned as an M-by-3 matrix.

M is specified by the SamplesPerFrame property.

Data Types: double

orientation — Orientation in local navigation coordinate system

M-element quaternion column vector | 3-by-3-by-*M* real array

Orientation in the local navigation coordinate system, returned as an M-by-1 quaternion column vector or a 3-by-3-by-M real array.

Each quaternion or 3-by-3 rotation matrix is a frame rotation from the local navigation coordinate system to the current body coordinate system.

M is specified by the SamplesPerFrame property.

Data Types: double

velocity — Velocity in local navigation coordinate system (m/s)

M-by-3 matrix

Velocity in the local navigation coordinate system in meters per second, returned as an M-by-3 matrix.

M is specified by the SamplesPerFrame property.

Data Types: double

acceleration — Acceleration in local navigation coordinate system (m/s²)

M-by-3 matrix

Acceleration in the local navigation coordinate system in meters per second squared, returned as an M-by-3 matrix.

M is specified by the SamplesPerFrame property.

Data Types: double

angular Velocity — Angular velocity in local navigation coordinate system (rad/s)

M-by-3 matrix

Angular velocity in the local navigation coordinate system in radians per second, returned as an M-by-3 matrix.

M is specified by the SamplesPerFrame property.

Data Types: double

Object Functions

To use an object function, specify the System object as the first input argument. For example, to release system resources of a System object named obj, use this syntax:

release(obj)

Specific to waypointTrajectory

waypointInfo Get waypoint information table

lookupPose Obtain pose information for certain time

perturbations Perturbation defined on object perturb Apply perturbations to object

Common to All System Objects

clone Create duplicate System object step Run System object algorithm

release Release resources and allow changes to System object property values and input

characteristics

reset Reset internal states of System object

isDone End-of-data status

Examples

Create Default waypointTrajectory

```
trajectory = waypointTrajectory
```

```
trajectory =
  waypointTrajectory with properties:

    SampleRate: 100
  SamplesPerFrame: 1
     Waypoints: [2x3 double]
    TimeOfArrival: [2x1 double]
     Velocities: [2x3 double]
          Course: [2x1 double]
          GroundSpeed: [2x1 double]
          ClimbRate: [2x1 double]
          Orientation: [2x1 quaternion]
          AutoBank: 0
          ReferenceFrame: 'NED'
```

Inspect the default waypoints and times of arrival by calling waypointInfo. By default, the waypoints indicate a stationary position for one second.

waypointInfo(trajectory)

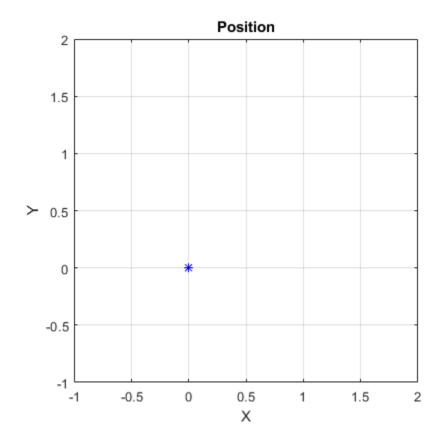
```
ans=2×2 table
TimeOfArrival Waypoints
------
0 0 0 0 0 1 0 0 0
```

Create Square Trajectory

Create a square trajectory and examine the relationship between waypoint constraints, sample rate, and the generated trajectory.

Create a square trajectory by defining the vertices of the square. Define the orientation at each waypoint as pointing in the direction of motion. Specify a 1 Hz sample rate and use the default SamplesPerFrame of 1.

```
waypoints = [0,0,0; ... % Initial position
              0,1,0; ...
              1,1,0; ...
              1,0,0; ...
0,0,0]; % Final position
toa = 0:4; % time of arrival
orientation = quaternion([0,0,0; ...
                            45,0,0; ...
135,0,0; ...
                             225,0,0; ...
                            0,0,0], ...
'eulerd','ZYX','frame');
trajectory = waypointTrajectory(waypoints, ...
     'TimeOfArrival',toa, ...
    'Orientation', orientation, ...
    'SampleRate',1);
Create a figure and plot the initial position of the platform.
figure(1)
plot(waypoints(1,1),waypoints(1,2),'b*')
title('Position')
axis([-1,2,-1,2])
axis square
xlabel('X')
ylabel('Y')
grid on
hold on
```

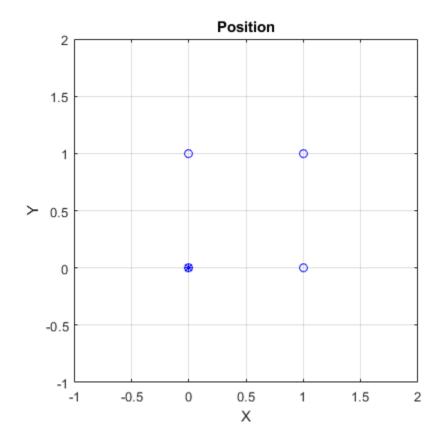


In a loop, step through the trajectory to output the current position and current orientation. Plot the current position and log the orientation. Use pause to mimic real-time processing.

```
orientationLog = zeros(toa(end)*trajectory.SampleRate,1,'quaternion');
count = 1;
while ~isDone(trajectory)
    [currentPosition,orientationLog(count)] = trajectory();

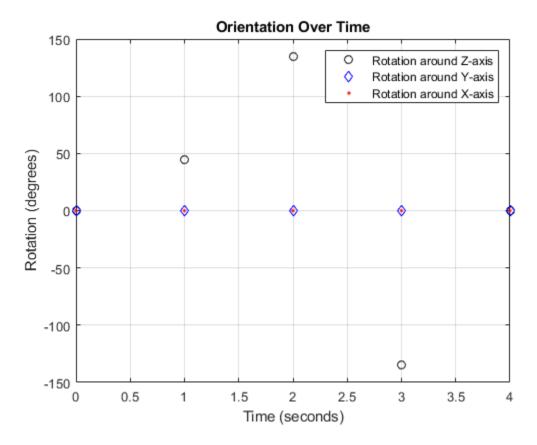
plot(currentPosition(1),currentPosition(2),'bo')

pause(trajectory.SamplesPerFrame/trajectory.SampleRate)
    count = count + 1;
end
hold off
```



Convert the orientation quaternions to Euler angles for easy interpretation, and then plot orientation over time.

```
figure(2)
eulerAngles = eulerd([orientation(1);orientationLog],'ZYX','frame');
plot(toa,eulerAngles(:,1),'ko', ...
        toa,eulerAngles(:,2),'bd', ...
        toa,eulerAngles(:,3),'r.');
title('Orientation Over Time')
legend('Rotation around Z-axis','Rotation around Y-axis','Rotation around X-axis')
xlabel('Time (seconds)')
ylabel('Rotation (degrees)')
grid on
```



So far, the trajectory object has only output the waypoints that were specified during construction. To interpolate between waypoints, increase the sample rate to a rate faster than the time of arrivals of the waypoints. Set the trajectory sample rate to 100 Hz and call reset.

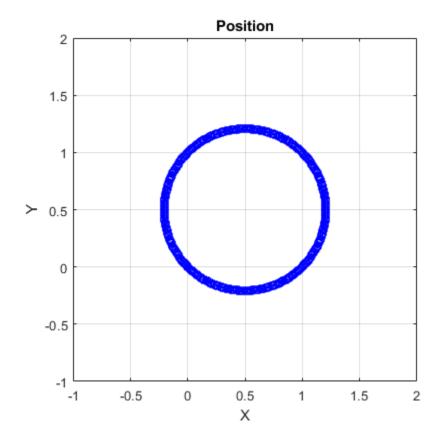
```
trajectory.SampleRate = 100;
reset(trajectory)
```

Create a figure and plot the initial position of the platform. In a loop, step through the trajectory to output the current position and current orientation. Plot the current position and log the orientation. Use pause to mimic real-time processing.

```
figure(1)
plot(waypoints(1,1),waypoints(1,2),'b*')
title('Position')
axis([-1,2,-1,2])
axis square
xlabel('X')
ylabel('Y')
grid on
hold on

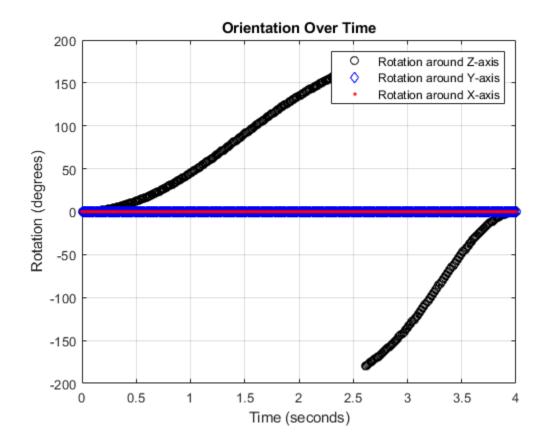
orientationLog = zeros(toa(end)*trajectory.SampleRate,1,'quaternion');
count = 1;
while ~isDone(trajectory)
    [currentPosition,orientationLog(count)] = trajectory();
    plot(currentPosition(1),currentPosition(2),'bo')
```

```
pause(trajectory.SamplesPerFrame/trajectory.SampleRate)
  count = count + 1;
end
hold off
```



The trajectory output now appears circular. This is because the waypointTrajectory System object™ minimizes the acceleration and angular velocity when interpolating, which results in smoother, more realistic motions in most scenarios.

Convert the orientation quaternions to Euler angles for easy interpretation, and then plot orientation over time. The orientation is also interpolated.

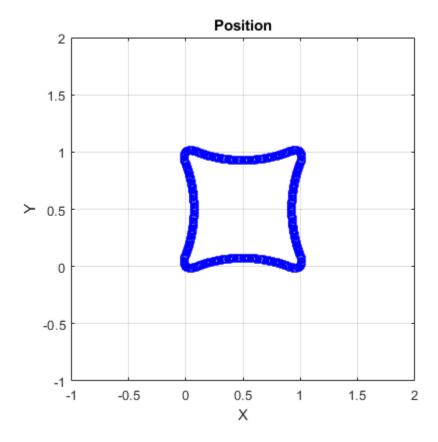


The waypointTrajectory algorithm interpolates the waypoints to create a smooth trajectory. To return to the square trajectory, provide more waypoints, especially around sharp changes. To track corresponding times, waypoints, and orientation, specify all the trajectory info in a single matrix.

```
% Time, Waypoint, Orientation
trajectoryInfo = [0,
                       0,0,0,
                                 0,0,0; ... % Initial position
                  0.1, 0,0.1,0,
                                 0,0,0; ...
                  0.9, 0,0.9,0,
                                 0,0,0; ...
                  1, 0,1,0,
                                  45,0,0; ...
                  1.1, 0.1,1,0,
                                 90,0,0; ...
                  1.9, 0.9, 1, 0,
                                 90,0,0; ...
                  2,
                       1,1,0,
                                  135,0,0; ...
                  2.1, 1,0.9,0,
                                 180,0,0; ...
                  2.9, 1,0.1,0,
                                  180,0,0; ...
                  3, 1,0,0,
                                  225,0,0; ...
                  3.1, 0.9,0,0,
                                 270,0,0; ...
                  3.9, 0.1,0,0,
                                 270,0,0; ...
                       0,0,0,
                                  270,0,0];
                                               % Final position
trajectory = waypointTrajectory(trajectoryInfo(:,2:4), ...
    'TimeOfArrival',trajectoryInfo(:,1), ...
    'Orientation',quaternion(trajectoryInfo(:,5:end),'eulerd','ZYX','frame'), ...
    'SampleRate',100);
```

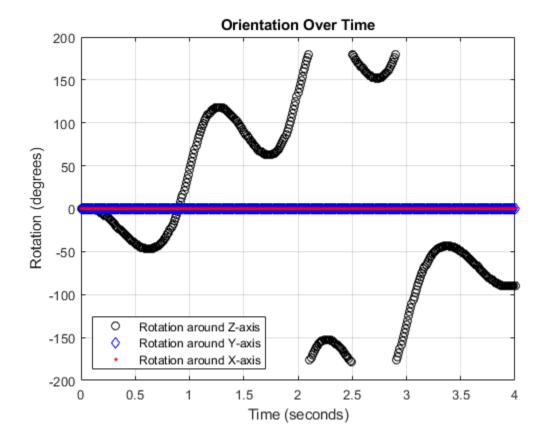
Create a figure and plot the initial position of the platform. In a loop, step through the trajectory to output the current position and current orientation. Plot the current position and log the orientation. Use pause to mimic real-time processing.

```
figure(1)
plot(waypoints(1,1),waypoints(1,2),'b*')
title('Position')
axis([-1,2,-1,2])
axis square
xlabel('X')
ylabel('Y')
grid on
hold on
orientationLog = zeros(toa(end)*trajectory.SampleRate,1,'quaternion');
count = 1;
while ~isDone(trajectory)
   [currentPosition,orientationLog(count)] = trajectory();
   plot(currentPosition(1), currentPosition(2), 'bo')
   pause(trajectory.SamplesPerFrame/trajectory.SampleRate)
   count = count+1;
end
hold off
```



The trajectory output now appears more square-like, especially around the vertices with waypoints.

Convert the orientation quaternions to Euler angles for easy interpretation, and then plot orientation over time.



Create Arc Trajectory

This example shows how to create an arc trajectory using the waypointTrajectory System object™. waypointTrajectory creates a path through specified waypoints that minimizes acceleration and angular velocity. After creating an arc trajectory, you restrict the trajectory to be within preset bounds.

Create an Arc Trajectory

Define a constraints matrix consisting of waypoints, times of arrival, and orientation for an arc trajectory. The generated trajectory passes through the waypoints at the specified times with the specified orientation. The waypointTrajectory System object requires orientation to be specified using quaternions or rotation matrices. Convert the Euler angles saved in the constrains matrix to quaternions when specifying the Orientation property.

Call waypointInfo on trajectory to return a table of your specified constraints. The creation properties Waypoints, TimeOfArrival, and Orientation are variables of the table. The table is convenient for indexing while plotting.

```
tInfo = waypointInfo(trajectory)
```

```
tInfo = 4x3 table
```

TimeOfArrival	Waypoints			Orientation
0	20	20 20	0	{1x1 quaternion} {1x1 quaternion}
4 5.5	58 59.5	15.5 0	⊙ ⊙	{1x1 quaternion} {1x1 quaternion}

The trajectory object outputs the current position, velocity, acceleration, and angular velocity at each call. Call trajectory in a loop and plot the position over time. Cache the other outputs.

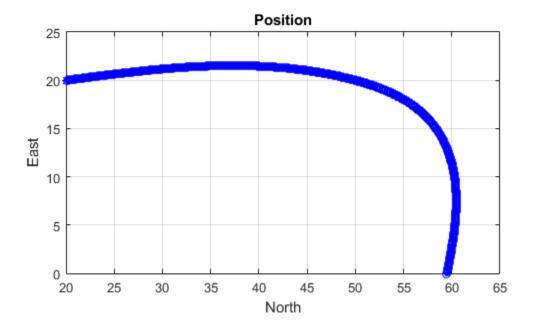
```
figure(1)
plot(tInfo.Waypoints(1,1),tInfo.Waypoints(1,2),'b*')
title('Position')
axis([20,65,0,25])
xlabel('North')
ylabel('East')
grid on
daspect([1 1 1])
hold on

orient = zeros(tInfo.TimeOfArrival(end)*trajectory.SampleRate,1,'quaternion');
vel = zeros(tInfo.TimeOfArrival(end)*trajectory.SampleRate,3);
acc = vel;
angVel = vel;

count = 1;
while ~isDone(trajectory)
```

```
[pos,orient(count),vel(count,:),acc(count,:),angVel(count,:)] = trajectory();
plot(pos(1),pos(2),'bo')

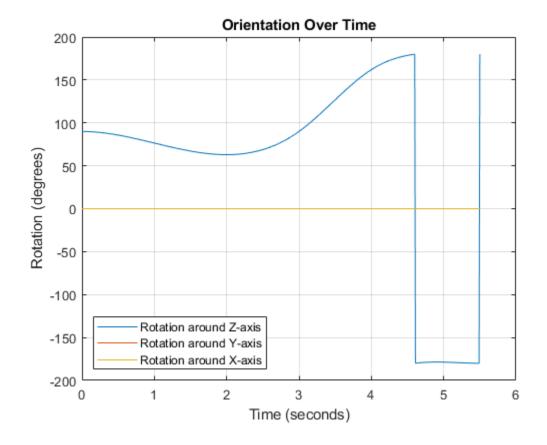
pause(trajectory.SamplesPerFrame/trajectory.SampleRate)
    count = count + 1;
end
```

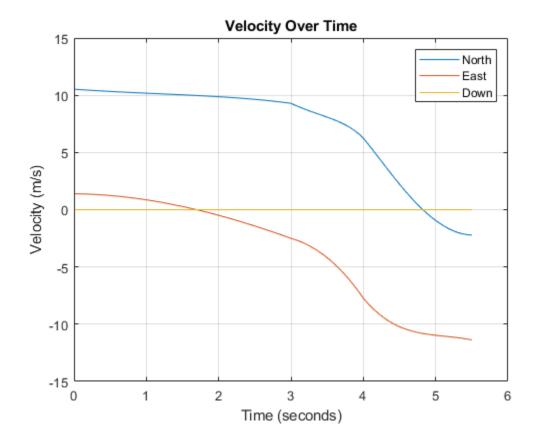


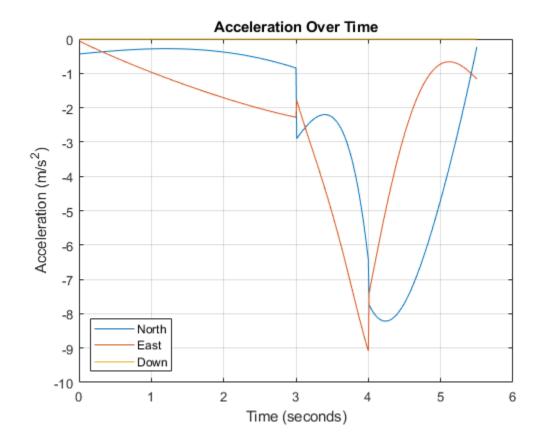
Inspect the orientation, velocity, acceleration, and angular velocity over time. The waypointTrajectory System objectTM creates a path through the specified constraints that minimized acceleration and angular velocity.

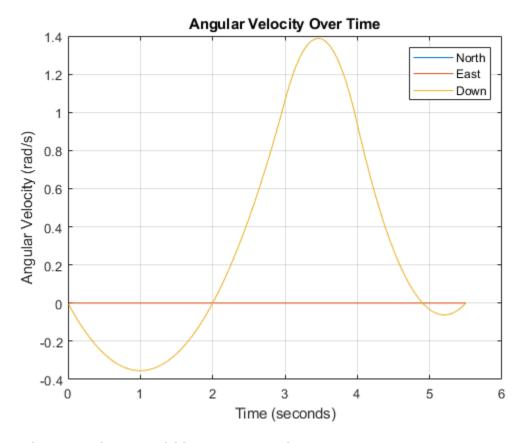
```
figure(2)
timeVector = 0:(1/trajectory.SampleRate):tInfo.TimeOfArrival(end);
eulerAngles = eulerd([tInfo.Orientation{1};orient],'ZYX','frame');
plot(timeVector,eulerAngles(:,1), ...
    timeVector,eulerAngles(:,2), ...
    timeVector,eulerAngles(:,3));
title('Orientation Over Time')
legend('Rotation around Z-axis', ...
    'Rotation around Y-axis', ...
    'Rotation around X-axis', ...
    'Location','southwest')
xlabel('Time (seconds)')
ylabel('Rotation (degrees)')
grid on
```

```
figure(3)
plot(timeVector(2:end), vel(:,1), ...
      timeVector(2:end),vel(:,2), ...
      timeVector(2:end),vel(:,3));
title('Velocity Over Time')
legend('North','East','Down')
xlabel('Time (seconds)')
ylabel('Velocity (m/s)')
grid on
figure(4)
plot(timeVector(2:end),acc(:,1), ...
      timeVector(2:end),acc(:,2), ...
      timeVector(2:end),acc(:,3));
title('Acceleration Over Time')
legend('North','East','Down','Location','southwest')
xlabel('Time (seconds)')
ylabel('Acceleration (m/s^2)')
grid on
figure(5)
plot(timeVector(2:end),angVel(:,1), ...
      timeVector(2:end),angVel(:,2), ...
      timeVector(2:end),angVel(:,3));
title('Angular Velocity Over Time')
legend('North','East','Down')
xlabel('Time (seconds)')
ylabel('Angular Velocity (rad/s)')
grid on
```





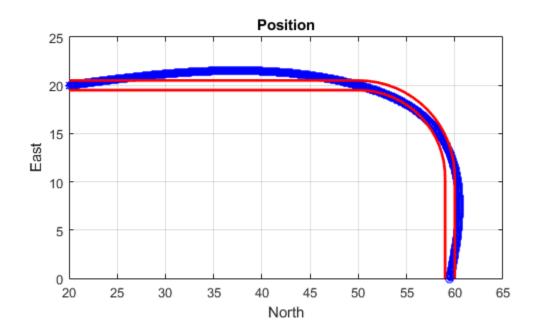




Restrict Arc Trajectory Within Preset Bounds

You can specify additional waypoints to create trajectories within given bounds. Create upper and lower bounds for the arc trajectory.

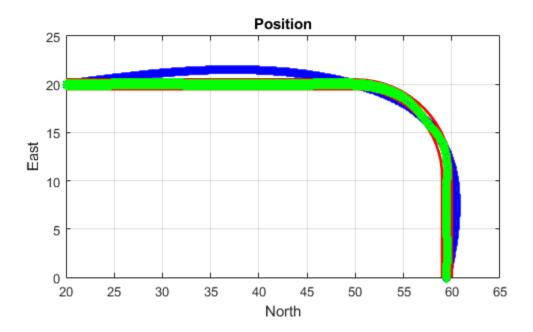
```
figure(1)
xUpperBound = [(20:50)';50+10*sin(0:0.1:pi/2)';60*ones(11,1)];
yUpperBound = [20.5.*ones(31,1);10.5+10*cos(0:0.1:pi/2)';(10:-1:0)'];
xLowerBound = [(20:49)';50+9*sin(0:0.1:pi/2)';59*ones(11,1)];
yLowerBound = [19.5.*ones(30,1);10.5+9*cos(0:0.1:pi/2)';(10:-1:0)'];
plot(xUpperBound,yUpperBound,'r','LineWidth',2);
plot(xLowerBound,yLowerBound,'r','LineWidth',2)
```



To create a trajectory within the bounds, add additional waypoints. Create a new waypointTrajectory System object™, and then call it in a loop to plot the generated trajectory. Cache the orientation, velocity, acceleration, and angular velocity output from the trajectory object.

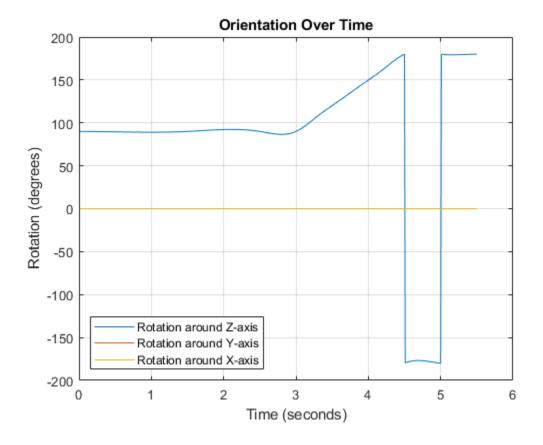
```
% Time,
                     Waypoint,
                                    Orientation
constraints = [0,
                     20,20,0,
                                    90,0,0;
               1.5,
                                    90,0,0;
                     35,20,0,
               2.5
                                    90,0,0;
                      45,20,0,
               3,
                      50,20,0,
                                    90,0,0;
               3.3,
                     53, 19.5, 0,
                                    108,0,0;
                     55.5,18.25,0, 126,0,0;
               3.6,
               3.9,
                     57.5,16,0,
                                    144,0,0;
               4.2,
                     59,14,0,
                                    162,0,0;
               4.5,
                     59.5,10,0
                                    180,0,0;
               5,
                      59.5,5,0
                                    180,0,0;
               5.5,
                    59.5,0,0
                                    180,0,0];
trajectory = waypointTrajectory(constraints(:,2:4), ...
    'TimeOfArrival',constraints(:,1), ...
    'Orientation',quaternion(constraints(:,5:7),'eulerd','ZYX','frame'));
tInfo = waypointInfo(trajectory);
figure(1)
plot(tInfo.Waypoints(1,1),tInfo.Waypoints(1,2),'b*')
count = 1;
```

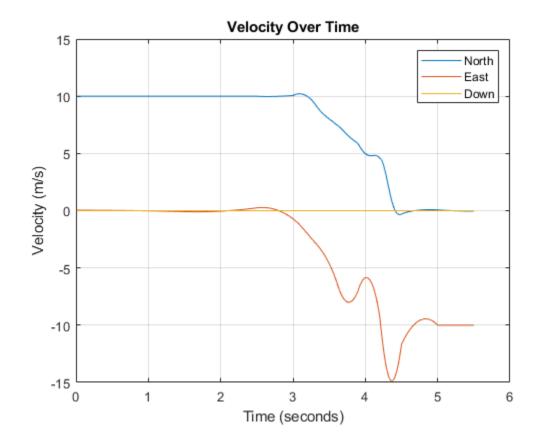
```
while ~isDone(trajectory)
  [pos,orient(count),vel(count,:),acc(count,:),angVel(count,:)] = trajectory();
  plot(pos(1),pos(2),'gd')
  pause(trajectory.SamplesPerFrame/trajectory.SampleRate)
  count = count + 1;
end
```

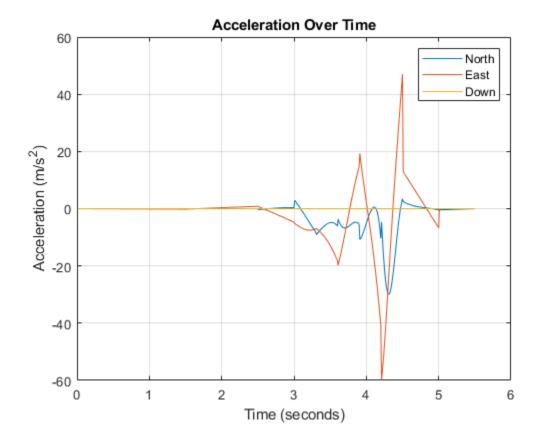


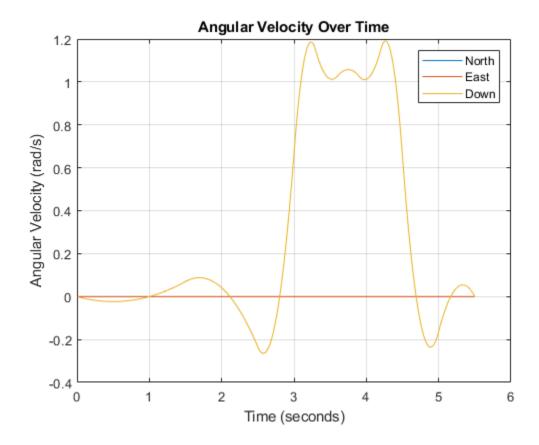
The generated trajectory now fits within the specified boundaries. Visualize the orientation, velocity, acceleration, and angular velocity of the generated trajectory.

```
plot(timeVector(2:end),vel(:,1), ...
     timeVector(2:end),vel(:,2), ...
     timeVector(2:end), vel(:,3));
title('Velocity Over Time')
legend('North', 'East', 'Down')
xlabel('Time (seconds)')
ylabel('Velocity (m/s)')
grid on
figure(4)
plot(timeVector(2:end),acc(:,1), ...
     timeVector(2:end),acc(:,2), ...
     timeVector(2:end),acc(:,3));
title('Acceleration Over Time')
legend('North','East','Down')
xlabel('Time (seconds)')
ylabel('Acceleration (m/s^2)')
grid on
figure(5)
plot(timeVector(2:end),angVel(:,1), ...
     timeVector(2:end),angVel(:,2), ...
     timeVector(2:end),angVel(:,3));
title('Angular Velocity Over Time')
legend('North', 'East', 'Down')
xlabel('Time (seconds)')
ylabel('Angular Velocity (rad/s)')
grid on
```









Note that while the generated trajectory now fits within the spatial boundaries, the acceleration and angular velocity of the trajectory are somewhat erratic. This is due to over-specifying waypoints.

Algorithms

The waypointTrajectory System object defines a trajectory that smoothly passes through waypoints. The trajectory connects the waypoints through an interpolation that assumes the gravity direction expressed in the trajectory reference frame is constant. Generally, you can use waypointTrajectory to model platform or vehicle trajectories within a hundreds of kilometers distance span.

The planar path of the trajectory (the x-y plane projection) consists of piecewise, clothoid curves. The curvature of the curve between two consecutive waypoints varies linearly with the curve length between them. The tangent direction of the path at each waypoint is chosen to minimize discontinuities in the curvature, unless the course is specified explicitly via the Course property or implicitly via the Velocities property. Once the path is established, the object uses cubic Hermite interpolation to compute the location of the vehicle throughout the path as a function of time and the planar distance travelled.

The normal component (z-component) of the trajectory is subsequently chosen to satisfy a shape-preserving piecewise spline (PCHIP) unless the climb rate is specified explicitly via the ClimbRate property or the third column of the Velocities property. Choose the sign of the climb rate based on the selected ReferenceFrame:

- When an 'ENU' reference frame is selected, specifying a positive climb rate results in an increasing value of *z*.
- When an 'NED' reference frame is selected, specifying a positive climb rate results in a decreasing value of *z*.

You can define the orientation of the vehicle through the path in two primary ways:

- If the Orientation property is specified, then the object uses a piecewise-cubic, quaternion spline to compute the orientation along the path as a function of time.
- If the Orientation property is not specified, then the yaw of the vehicle is always aligned with the path. The roll and pitch are then governed by the AutoBank and AutoPitch property values, respectively.

AutoBank	AutoPitch	Description	
false	false	The vehicle is always level (zero pitch and roll). This is typically used for large marine vessels.	
false	true	The vehicle pitch is aligned with the path, and its roll is always zero. This is typically used for ground vehicles.	
true	false	The vehicle pitch and roll are chosen so that its local <i>z</i> -axis is aligned with the net acceleration (including gravity). This is typically used for rotary-wing craft.	
true	true	The vehicle roll is chosen so that its local transverse plane aligns with the net acceleration (including gravity). The vehicle pitch is aligned with the path. This is typically used for two-wheeled vehicles and fixed-wing aircraft.	

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

The object function, waypointInfo, does not support code generation.

Usage notes and limitations:

See "System Objects in MATLAB Code Generation" (MATLAB Coder).

See Also

kinematic Trajectory

Introduced in R2019b

lookupPose

Obtain pose information for certain time

Syntax

[position,orientation,velocity,acceleration,angularVelocity] = lookupPose(
traj,sampleTimes)

Description

[position,orientation,velocity,acceleration,angularVelocity] = lookupPose(traj,sampleTimes) returns the pose information of the waypoint trajectory at the specified sample times. If any sample time is beyond the duration of the trajectory, the corresponding pose information is returned as NaN.

Input Arguments

traj — Waypoint trajectory

waypointTrajectory object

Waypoint trajectory, specified as a waypointTrajectory object.

sampleTimes — Sample times

M-element vector of nonnegative scalar

Sample times in seconds, specified as an *M*-element vector of nonnegative scalars.

Output Arguments

position — Position in local navigation coordinate system (m)

M-by-3 matrix

Position in the local navigation coordinate system in meters, returned as an M-by-3 matrix.

M is specified by the sampleTimes input.

Data Types: double

orientation — Orientation in local navigation coordinate system

M-element quaternion column vector | 3-by-3-by-*M* real array

Orientation in the local navigation coordinate system, returned as an M-by-1 quaternion column vector or a 3-by-3-by-M real array.

Each quaternion or 3-by-3 rotation matrix is a frame rotation from the local navigation coordinate system to the current body coordinate system.

M is specified by the sampleTimes input.

Data Types: double

velocity — Velocity in local navigation coordinate system (m/s)

M-by-3 matrix

Velocity in the local navigation coordinate system in meters per second, returned as an M-by-3 matrix.

M is specified by the sampleTimes input.

Data Types: double

acceleration — Acceleration in local navigation coordinate system (m/s²)

M-by-3 matrix

Acceleration in the local navigation coordinate system in meters per second squared, returned as an M-by-3 matrix.

M is specified by the sampleTimes input.

Data Types: double

angular Velocity — Angular velocity in local navigation coordinate system (rad/s)

M-by-3 matrix

Angular velocity in the local navigation coordinate system in radians per second, returned as an *M*-by-3 matrix.

M is specified by the sampleTimes input.

Data Types: double

See Also

waypointTrajectory

Introduced in R2019b

waypointInfo

Get waypoint information table

Syntax

trajectoryInfo = waypointInfo(trajectory)

Description

trajectoryInfo = waypointInfo(trajectory) returns a table of waypoints, times of arrival,
velocities, and orientation for the trajectory System object

Input Arguments

${\tt trajectory} - {\tt Object} \ {\tt of} \ {\tt waypointTrajectory}$

object

Object of the waypointTrajectory System object.

Output Arguments

trajectoryInfo — Trajectory information

table

Trajectory information, returned as a table with variables corresponding to set creation properties: Waypoints, TimeOfArrival, Velocities, and Orientation.

The trajectory information table always has variables Waypoints and TimeOfArrival. If the Velocities property is set during construction, the trajectory information table additionally returns velocities. If the Orientation property is set during construction, the trajectory information table additionally returns orientation.

See Also

waypointTrajectory

Introduced in R2019b

perturb

Apply perturbations to object

Syntax

```
offsets = perturb(obj)
```

Description

offsets = perturb(obj) applies the perturbations defined on the object, obj and returns the offset values. You can define perturbations on the object by using the perturbations function.

Examples

Perturb Waypoint Trajectory

Define a waypoint trajectory. By default, this trajectory contains two waypoints.

```
traj = waypointTrajectory

traj =
    waypointTrajectory with properties:

        SampleRate: 100
    SamplesPerFrame: 1
        Waypoints: [2x3 double]
        TimeOfArrival: [2x1 double]
        Velocities: [2x3 double]
        Course: [2x1 double]
        GroundSpeed: [2x1 double]
        ClimbRate: [2x1 double]
        Orientation: [2x1 quaternion]
        AutoPitch: 0
        AutoBank: 0
        ReferenceFrame: 'NED'
```

Define perturbations on the Waypoints property and the TimeOfArrival property.

```
      Property
      Type
      Value

      "Waypoints"
      "Normal"
      {[ 1]}
      {[ 1]}

      "TimeOfArrival"
      "Selection"
      {1x2 cell}
      {[0.5000 0.5000]}
```

Perturb the trajectory.

```
offsets = perturb(traj)
```

```
offsets=2×1 struct array with fields:
    Property
    Offset
    PerturbedValue
```

The Waypoints property and the TimeOfArrival property have changed.

traj.Waypoints

```
ans = 2×3

1.8674   1.0203   0.7032

2.3154   -0.3207   0.0999
```

traj.TimeOfArrival

ans = 2×1 0
2

Perturb Accuracy of insSensor

Create an insSensor object.

sensor = insSensor

```
RollAccuracy: 0.2 deg
PitchAccuracy: 0.2 deg
YawAccuracy: 1 deg
PositionAccuracy: [1 1 1] m
VelocityAccuracy: 0.05 m/s
AccelerationAccuracy: 0 m/s²
AngularVelocityAccuracy: 0 deg/s
TimeInput: 0
```

RandomStream: 'Global stream'

Define the perturbation on the RollAccuracy property as three values with an equal possibility each.

```
values = \{0.1 \ 0.2 \ 0.3\}
values=1×3 cell array
    {[0.1000]} {[0.2000]}
                                 {[0.3000]}
probabilities = [1/3 1/3 1/3]
probabilities = 1 \times 3
    0.3333 0.3333
                        0.3333
perturbations(sensor, 'RollAccuracy', 'Selection', values, probabilities)
ans=7×3 table
                                                                  Value
            Property
                                     Type
    "RollAccuracy"
                                  "Selection"
                                                 {1x3 cell}
                                                                {[0.3333 0.3333 0.3333]}
    "PitchAccuracy"
                                  "None"
                                                 {[ NaN]}
                                                                [ ]
                                                                                    NaN1}
    "YawAccuracy"
                                  "None"
                                                      NaN]}
                                                                                    NaN]}
                                                 {[
                                                                {[
    "PositionAccuracy"
                                  "None"
                                                      NaN1}
                                                                {[
                                                                                    NaN1}
                                                 {[
```

NaN]}

NaN]}

NaN1}

{[

{[

{[

[]

] }

[

NaN]}

NaN]}

NaN1}

"None"

"None"

"None"

Perturb the sensor object using the perturb function.

"VelocityAccuracy"

"AccelerationAccuracy"

"AngularVelocityAccuracy"

```
rng(2020)
perturb(sensor);
sensor
sensor =
 insSensor with properties:
           MountingLocation: [0 0 0]
               RollAccuracy: 0.5
                                                 deg
              PitchAccuracy: 0.2
                                                 deg
                YawAccuracy: 1
                                                 deg
           PositionAccuracy: [1 1 1]
           VelocityAccuracy: 0.05
                                                 m/s
      AccelerationAccuracy: 0
                                                 m/s^2
   AngularVelocityAccuracy: 0
                                                 deg/s
                  TimeInput: 0
               RandomStream: 'Global stream'
```

The RollAccuracy is perturbed to 0.5 deg.

Input Arguments

obj — Object for perturbation

objects

Object for perturbation, specified as an object. The objects that you can perturb include:

- waypointTrajectory
- kinematicTrajectory
- insSensor

Output Arguments

offsets — Property offsets

array of structure

Property offsets, returned as an array of structures. Each structure contains these fields:

Field Name	Description	
Property	Name of perturbed property	
Offset	Offset values applied in the perturbation	
PerturbedValue	Property values after the perturbation	

See Also

perturbations

Introduced in R2020b

perturbations

Perturbation defined on object

Syntax

```
perturbs = perturbations(obj)
perturbs = perturbations(obj,property)
perturbs = perturbations(obj,property,'None')
perturbs = perturbations(obj,property,'Selection',values,probabilities)
perturbs = perturbations(obj,property,'Normal',mean,deviation)
perturbs = perturbations(obj,property,'Uniform',minVal,maxVal)
perturbs = perturbations(obj,property,'Custom',perturbFcn)
```

Description

perturbs = perturbations(obj) returns the list of property perturbations, perturbs, defined
on the object, obj. The returned perturbs lists all the perturbable properties. If any property is not
perturbed, then its corresponding Type is returned as "Null" and its corresponding Value is
returned as {Null, Null}.

perturbs = perturbations(obj,property) returns the current perturbation applied to the specified property.

perturbs = perturbations(obj,property,'None') defines a property that must not be perturbed.

perturbs = perturbations(obj,property,'Selection',values,probabilities) defines the property perturbation offset drawn from a set of values that have corresponding probabilities.

perturbs = perturbations(obj,property,'Normal',mean,deviation) defines the property perturbation offset drawn from a normal distribution with specified mean and standard deviation.

perturbs = perturbations(obj,property,'Uniform',minVal,maxVal) defines the
property perturbation offset drawn from a uniform distribution on an interval [minVal, maxValue].

perturbs = perturbations(obj,property,'Custom',perturbFcn) enables you to define a custom function, perturbFcn, that draws the perturbation offset value.

Examples

Default Perturbation Properties of waypointTrajectory

Create a waypointTrajectory object.

```
traj = waypointTrajectory;
```

Show the default perturbation properties using the perturbations method.

perturbs = perturbations(traj)

Perturb Accuracy of insSensor

Create an insSensor object.

```
sensor = insSensor
sensor =
 \verb"insSensor with properties:
           MountingLocation: [0 0 0]
               RollAccuracy: 0.2
                                                  deg
              PitchAccuracy: 0.2
                                                  deg
                YawAccuracy: 1
                                                  deg
           PositionAccuracy: [1 1 1]
                                                 m/s
           VelocityAccuracy: 0.05
      AccelerationAccuracy: 0
                                                 m/s^2
   AngularVelocityAccuracy: 0
                                                 deg/s
                  TimeInput: 0
               RandomStream: 'Global stream'
```

Define the perturbation on the RollAccuracy property as three values with an equal possibility each.

perturbations(sensor, 'RollAccuracy', 'Selection', values, probabilities)

Notinecuracy	JC CCC CIOII	(TV) C		[[0:3333 0:3333	0.0000]]
"PitchAccuracy"	"None"	{ [Na	laN]}]}	NaN]}
"YawAccuracy"	"None"	{[N	laN]}]}	NaN]}

```
"PositionAccuracy"
                             "None"
                                            ] }
                                                 NaN]}
                                                          ] }
                                                                             NaN]}
"VelocityAccuracy"
                             "None"
                                           ] }
                                                 NaN]}
                                                          ] }
                                                                             NaN]}
"AccelerationAccuracy"
                             "None"
                                            ] }
                                                 NaN]}
                                                          ] }
                                                                             NaN]}
"AngularVelocityAccuracy"
                             "None"
                                            ]}
                                                 NaN]}
                                                          ] }
                                                                             NaN]}
```

Perturb the sensor object using the perturb function.

```
rng(2020)
perturb(sensor);
sensor
sensor =
  insSensor with properties:
           MountingLocation: [0 0 0]
               RollAccuracy: 0.5
                                                  deg
              PitchAccuracy: 0.2
                                                  deg
                YawAccuracy: 1
                                                  deg
           PositionAccuracy: [1 1 1]
           VelocityAccuracy: 0.05
                                                 m/s
                                                 \rm m/s^2
       AccelerationAccuracy: 0
    AngularVelocityAccuracy: 0
                                                 deg/s
                  TimeInput: 0
               RandomStream: 'Global stream'
```

The RollAccuracy is perturbed to 0.5 deg.

Perturb Waypoint Trajectory

Define a waypoint trajectory. By default, this trajectory contains two waypoints.

```
traj = waypointTrajectory

traj =
  waypointTrajectory with properties:

    SampleRate: 100
  SamplesPerFrame: 1
        Waypoints: [2x3 double]
        TimeOfArrival: [2x1 double]
        Velocities: [2x3 double]
        Course: [2x1 double]
        GroundSpeed: [2x1 double]
        ClimbRate: [2x1 double]
        Orientation: [2x1 quaternion]
        AutoPitch: 0
        AutoBank: 0
        ReferenceFrame: 'NED'
```

Define perturbations on the Waypoints property and the TimeOfArrival property.

```
rng(2020);
perturbs1 = perturbations(traj,'Waypoints','Normal',1,1)
```

```
perturbs1=2×3 table
       Property
                         Туре
                                          Value
                       "Normal"
    "Waypoints"
                                    {[ 1]}
                                               {[ 1]}
    "TimeOfArrival"
                       "None"
                                    {[NaN]}
                                               {[NaN]}
perturbs2 = perturbations(traj,'TimeOfArrival','Selection',{[0;1],[0;2]})
perturbs2=2×3 table
       Property
                          Туре
                                                    Value
    "Waypoints"
                       "Normal"
                                              1]}
    "TimeOfArrival"
                                       {1x2 cell}
                                                     {[0.5000 0.5000]}
                       "Selection"
```

Perturb the trajectory.

```
offsets = perturb(traj)
```

```
offsets=2×1 struct array with fields:
    Property
    Offset
    PerturbedValue
```

The Waypoints property and the TimeOfArrival property have changed.

traj.Waypoints

```
ans = 2×3

1.8674    1.0203    0.7032

2.3154    -0.3207    0.0999
```

traj.TimeOfArrival

ans = 2×1 0
2

Input Arguments

obj - Object to be perturbed

objects

Object to be perturbed, specified as an object. The objects that you can perturb include:

- waypointTrajectory
- kinematicTrajectory
- insSensor

property — Perturbable property

property name

Perturbable property, specified as a property name. Use perturbations to obtain a full list of perturbable properties for the specified obj.

values — Perturbation offset values

n-element cell array of property values

Perturbation offset values, specified as an *n*-element cell array of property values. The function randomly draws the perturbation value for the property from the cell array based on the values' corresponding probabilities specified in the probabilities input.

probabilities — Drawing probabilities for each perturbation value

n-element array of nonnegative scalar

Drawing probabilities for each perturbation value, specified as an n-element array of nonnegative scalars, where n is the number of perturbation values provided in the values input. The sum of all elements must be equal to one.

For example, you can specify a series of perturbation value-probability pair as $\{x1,x2,...,xn\}$ and $\{p1,p2,...,pn\}$, where the probability of drawing xi is pi (i = 1, 2, ...,n).

mean — Mean of normal distribution

scalar | vector | matrix

Mean of normal distribution, specified as a scalar, vector, or matrix. The dimension of mean must be compatible with the corresponding property that you perturb.

deviation — Standard deviation of normal distribution

nonnegative scalar | vector of nonnegative scalar | matrix of nonnegative scalar

Standard deviation of normal distribution, specified as a nonnegative scalar, vector of nonnegative scalars, or matrix of nonnegative scalars. The dimension of deviation must be compatible with the corresponding property that you perturb.

minVal — Minimum value of uniform distribution interval

scalar | vector | matrix

Minimum value of the uniform distribution interval, specified as a scalar, vector, or matrix. The dimension of minVal must be compatible with the corresponding property that you perturb.

maxVal — Maximum value of uniform distribution interval

scalar | vector | matrix

Maximum value of the uniform distribution interval, specified as a scalar, vector, or matrix. The dimension of maxVal must be compatible with the corresponding property that you perturb.

perturbFcn — Perturbation function

function handle

Perturbation function, specified as a function handle. The function must have this syntax:

offset = myfun(propVal)

where propVal is the value of the property and offset is the perturbation offset for the property.

Output Arguments

perturbs — Perturbations defined on object

table of perturbation property

Perturbations defined on the object, returned as a table of perturbation properties. The table has three columns:

- Property Property names.
- Type Type of perturbations, returned as "None", "Selection", "Normal", "Uniform", or "Custom".
- Value Perturbation values, returned as a cell array.

See Also

perturb

Introduced in R2020b

wheelEncoderAckermann

Simulate wheel encoder sensor readings for Ackermann vehicle

Description

The wheelEncoderAckermann System object computes wheel encoder tick readings based on the pose input of an Ackermann vehicle.

To obtain the encoder tick readings:

- 1 Create the wheelEncoderAckermann object and set its properties.
- **2** Call the object with arguments, as if it were a function.

To learn more about how System objects work, see What Are System Objects?.

Creation

Syntax

```
encoder = wheelEncoderAckermann
encoder= wheelEncoderAckermann(Name, Value)
```

Description

encoder = wheelEncoderAckermann creates a wheelEncoderAckermann System object, encoder.

encoder= wheelEncoderAckermann(Name, Value) sets properties for the encoder using one or more name-value pairs. For example, wheelAckermann('SampleRate', 120) sets the sample rate of the encoder to 120 Hz. Unspecified properties have default values. Enclose each property name in quotes.

Properties

Unless otherwise indicated, properties are *nontunable*, which means you cannot change their values after calling the object. Objects lock when you call them, and the release function unlocks them.

If a property is *tunable*, you can change its value at any time.

For more information on changing property values, see System Design in MATLAB Using System Objects.

SampleRate — Sample rate of encoder

100 (default) | positive scalar

Sample rate of the encoder, specified as a positive scalar in Hz.

Example: 'SampleRate',100

Data Types: double

TicksPerRevolution — Number of encoder ticks per wheel revolution

[2048 2048 2048 2048] (default) | four-element vector of positive integers

Number of encoder ticks per wheel revolution, specified as a four-element vector of positive integers. The first, second, third, and fourth elements are for the back-left, back-right, front-left, and front-right wheels, respectively.

Data Types: double

WheelRadius — Wheel radius

[0.35 0.35 0.35] (default) | four-element vector of positive scalars

Wheel radius, specified as a four-element vector of positive scalars in meters. The first, second, third, and fourth elements are for the back-left, back-right, front-left, and front-right wheels, respectively.

Data Types: double

WheelRadiusBias — Bias of wheel radius

[0 0 0 0] (default) | four-element vector of scalars

Bias of the wheel radius, specified as a four-element vector of scalars in meters. The first, second, third, and fourth elements are for the back-left, back-right, front-left, and front-right wheels, respectively.

Data Types: double

WheelPositionAccuracy — Standard deviation of wheel position error

[0 0 0 0] (default) | four-element vector of nonnegative scalars

Standard deviation of wheel position error, specified as a four-element vector of nonnegative scalars in radians. The first, second, third, and fourth elements are for the back-left, back-right, front-left, and front-right wheels, respectively.

Data Types: double

SlipRatio — Slip or skid ratio of wheel

[0 0 0 0] (default) | four-element vector of scalars

Slip or skid ratio of the wheel, specified as a four-element vector of scalars in which each scalar is larger than or equal to -1. The first, second, third, and fourth elements are for the back-left, backright, front-left, and front-right wheels, respectively.

- For a wheel that slips (over rotation), specify it as a positive value. A higher value denotes more slipping.
- For a wheel that skids (under rotation), specify it as a negative value larger than or equal to -1. A lower value denotes more skidding. For a wheel that does not rotate, specify it as -1.

Data Types: double

TrackWidth — **Distance between wheel axles**

[1.572 1.572] (default) | two-element vector of positive scalars

Distance between the wheel axles, specified as a two-element vector of positive scalars in meters. The first element is for the back track, and the second element is for the front track.

Data Types: double

TrackWidthBias — Bias of track width

0 (default) | two-element vector of scalars

Bias of track width, specified as a two-element vector of scalars in meters. The first element is for the back track, and the second element is for the front track.

Data Types: double

WheelBase — Distance between front and rear axles

2.818 (default) | positive scalar

Distance between the front and the rear axles, specified as a positive scalar in meters.

Data Types: double

RandomStream — Random number source

'Global stream' (default) | 'mt19937ar with seed'

Random number source, specified as a character vector or string:

- 'Global stream' -- Random numbers are generated using the current global random number stream.
- 'mt19937ar with seed' -- Random numbers are generated using the mt19937ar algorithm with the seed specified by the Seed property.

Data Types: char | string

Seed — Initial seed

67 (default) | nonnegative integer

Initial seed of an mt19937ar random number generator algorithm, specified as a nonnegative integer.

Dependencies

To enable this property, set RandomStream to 'mt19937ar with seed'.

Usage

Syntax

ticks = encoder(velocity, angular Velocity, orientation)

Description

ticks = encoder(velocity, angular Velocity, orientation) return the wheel tick readings, ticks, form velocity, angular velocity, and orientation information.

Input Arguments

velocity — Velocity of vehicle

N-by-3 matrix of scalars

Velocity of the vehicle in the local navigation frame, specified as an N-by-3 matrix of scalars in m/s. N is the number of samples.

angular Velocity — Angular velocity of vehicle

N-by-3 matrix of scalars

Angular velocity of the vehicle in the local navigation frame, specified as an N-by-3 matrix of scalars in rad/s. N is the number of samples.

orientation — orientation of vehicle

N-element vector of quaternion | 3-by-3-by-N array of rotation matrices

Orientation of the vehicle in the local navigation frame, specified as an N-element vector of quaternion or a 3-by-3-by-N array of rotation matrices. N is the number of samples. Each quaternion or rotation matrix is a frame rotation from the local navigation coordinate system to the current vehicle body coordinate system.

Output Arguments

ticks — Number of wheel ticks per time step

N-by-4 matrix of nonnegative integers

Number of wheel ticks the vehicle moved per time step, returned as an *N*-by-4 matrix of nonnegative integers. *N* is the number of samples. The first, second, third, and fourth columns are for the backleft, back-right, front-left, and front-right wheels, respectively.

Object Functions

To use an object function, specify the System object as the first input argument. For example, to release system resources of a System object named obj, use this syntax:

release(obj)

Common to All System Objects

clone Create duplicate System object step Run System object algorithm

release Release resources and allow changes to System object property values and input

characteristics

reset Reset internal states of System object isLocked Determine if System object is in use

Examples

Generate Wheel Ticks from Ackermann Vehicle Pose

Create the wheel encoder sensor.

```
encoder = wheelEncoderAckermann;
```

Define poses of the vehicle.

```
orient = [quaternion([60 0 0],'eulerd','ZYX','frame'); quaternion([45 0 0], 'eulerd', 'ZYX', 'frame'); quaternion([45 0 0], 'eulerd', 'ZYX', 'frame'); angvel = [0 0 0.2; 0 0 0.1];
```

Generate wheel ticks from the poses.

ticks = encoder(vel,angvel,orient)

ticks = 2×4

3 6 6 8 6 7 6 7

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder $^{\text{\tiny TM}}$.

Usage notes and limitations:

See "System Objects in MATLAB Code Generation" (MATLAB Coder).

See Also

Introduced in R2020b

wheelEncoderBicycle

Simulate wheel encoder sensor readings for bicycle vehicle

Description

The wheelEncoderBicycle System object computes wheel encoder tick readings based on the pose input for a bicycle vehicle.

To obtain the encoder tick readings:

- 1 Create the wheelEncoderBicycle object and set its properties.
- **2** Call the object with arguments, as if it were a function.

To learn more about how System objects work, see What Are System Objects?.

Creation

Syntax

encoder = wheelEncoderBicycle
encoder= wheelEncoderBicycle(Name, Value)

Description

encoder = wheelEncoderBicycle creates a wheelEncoderBicycle System object, encoder.

encoder= wheelEncoderBicycle(Name, Value) sets properties for the encoder using one or more name-value pairs. For example, wheelEncoderBicycle('SampleRate', 120) sets the sample rate of the encoder to 120 Hz. Unspecified properties have default values. Enclose each property name in quotes.

Properties

Unless otherwise indicated, properties are *nontunable*, which means you cannot change their values after calling the object. Objects lock when you call them, and the release function unlocks them.

If a property is *tunable*, you can change its value at any time.

For more information on changing property values, see System Design in MATLAB Using System Objects.

SampleRate — Sample rate of encoder

100 (default) | positive scalar

Sample rate of the encoder, specified as a positive scalar in Hz.

Data Types: double

TicksPerRevolution — Number of encoder ticks per wheel revolution

[2048 2048] (default) | two-element vector of positive integers

Number of encoder ticks per wheel revolution, specified as a two-element vector of positive integers. The first element is for the back wheel, and the second element is for the front wheel.

Data Types: double

WheelRadius — Wheel radius

[0.35 0.35] (default) | two-element vector of positive scalars

Wheel radius, specified as a two-element vector of positive scalars in meters. The first element is for the back wheel, and the second element is for the front wheel.

Data Types: double

WheelRadiusBias — Bias of wheel radius

[0 0] (default) | two-element vector of scalars

Bias of the wheel radius, specified as a two-element vector of scalars in meters. The first element is for the back wheel, and the second element is for the front wheel.

Data Types: double

WheelPositionAccuracy — Standard deviation of wheel position error

[0 0] (default) | two-element vector of nonnegative scalars

Standard deviation of wheel position error, specified as a two-element vector of nonnegative scalars in radians. The first element is for the back wheel, and the second element is for the front wheel.

Data Types: double

SlipRatio — Slip or skid ratio of wheel

[0 0] (default) | two-element vector of scalar

Slip or skid ratio of the wheel, specified as a two-element vector of scalars in which each scalar is larger than or equal to -1. The first element is for the back wheel, and the second element is for the front wheel.

- For a wheel that slips (over rotation), specify it as a positive value. A higher value denotes more slipping.
- For a wheel that skids (under rotation), specify it as a negative value larger than or equal to -1. A lower value denotes more skidding. For a wheel that does not rotate, specify it as -1.

Data Types: double

WheelBase — Distance between front and rear wheels

2.818 (default) | positive scalar

Distance between the front and the rear wheels, specified as a positive scalar in meters.

Data Types: double

RandomStream — Random number source

'Global stream' (default) | 'mt19937ar with seed'

Random number source, specified as a character vector or string:

- 'Global stream' -- Random numbers are generated using the current global random number stream.
- 'mt19937ar with seed' -- Random numbers are generated using the mt19937ar algorithm with the seed specified by the Seed property.

Data Types: char | string

Seed — Initial seed of mt19937ar random number generator

67 (default) | nonnegative integer

Initial seed of an mt19937ar random number generator algorithm, specified as a nonnegative integer.

Dependencies

To enable this property, set RandomStream to 'mt19937ar with seed'.

Usage

Syntax

ticks = encoder(velocity,angularVelocity,orientation)

Description

ticks = encoder(velocity, angular Velocity, orientation) return the wheel tick readings, ticks, form velocity, angular velocity, and orientation information.

Input Arguments

velocity — Velocity of vehicle

N-by-3 matrix of scalars

Velocity of the vehicle in the local navigation frame, specified as an N-by-3 matrix of scalars in m/s. N is the number of samples.

angularVelocity — Angular velocity of vehicle

N-by-3 matrix of scalars

Angular velocity of the vehicle in the local navigation frame, specified as an N-by-3 matrix of scalars in rad/s. N is the number of samples.

orientation — orientation of vehicle

N-element vector of quaternion | 3-by-3-by-*N* array of rotation matrices

Orientation of the vehicle in the local navigation frame, specified as an N-element vector of quaternion or a 3-by-3-by-N array of rotation matrices. N is the number of samples. Each quaternion or rotation matrix is a frame rotation from the local navigation coordinate system to the current vehicle body coordinate system.

Output Arguments

ticks — Number of wheel ticks per time step

N-by-2 matrix of integer

Number of wheel ticks the vehicle moved per time step, returned as an N-by-2 matrix of integers. N is the number of samples. The first column is for the back wheel, and the second column is for the front wheel.

Object Functions

To use an object function, specify the System object as the first input argument. For example, to release system resources of a System object named obj, use this syntax:

release(obj)

Common to All System Objects

clone Create duplicate System object step Run System object algorithm

release Release resources and allow changes to System object property values and input

characteristics

reset Reset internal states of System object isLocked Determine if System object is in use

Examples

Generate Wheel Ticks from Bicycle Vehicle Pose

```
Create the wheel encoder sensor.
```

```
encoder = wheelEncoderBicycle;
```

Define poses of the vehicle.

```
orient = [quaternion([90 0 0], 'eulerd', 'ZYX', 'frame'); quaternion([45 0 0], 'eulerd', 'ZYX', 'frame', 'ZYX', 'frame', 'ZYX', 'frame', 'ZYX', 'frame', 'ZYX', 'frame', 'ZYX'
```

Generate wheel ticks from the poses.

```
ticks = encoder(vel,angvel,orient)
```

```
ticks = 2 \times 2
0 \qquad 5
6 \qquad 7
```

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

Usage notes and limitations:

See "System Objects in MATLAB Code Generation" (MATLAB Coder).

See Also

Introduced in R2020b

wheelEncoderDifferentialDrive

Simulate wheel encoder sensor readings for differential drive vehicle

Description

The wheelEncoderDifferentialDrive System object computes wheel encoder tick readings based on the pose input of a differential drive vehicle.

To obtain the encoder tick readings:

- 1 Create the wheelEncoderDifferentialDrive object and set its properties.
- **2** Call the object with arguments, as if it were a function.

To learn more about how System objects work, see What Are System Objects?.

Creation

Syntax

encoder = wheelEncoderDifferentialDrive
encoder= wheelEncoderDifferentialDrive(Name, Value)

Description

encoder = wheelEncoderDifferentialDrive creates a wheelEncoderDifferentialDrive
System object, encoder.

encoder= wheelEncoderDifferentialDrive(Name, Value) sets properties for the encoder using one or more name-value pairs. For example,

wheelEncoderDifferentialDrive('SampleRate', 120) sets the sample rate of the encoder to 120 Hz. Unspecified properties have default values. Enclose each property name in quotes.

Properties

Unless otherwise indicated, properties are *nontunable*, which means you cannot change their values after calling the object. Objects lock when you call them, and the release function unlocks them.

If a property is tunable, you can change its value at any time.

For more information on changing property values, see System Design in MATLAB Using System Objects.

SampleRate — Sample rate of encoder

100 (default) | positive scalar

Sample rate of the encoder, specified as a positive scalar in Hz.

Data Types: double

TicksPerRevolution — Number of encoder ticks per wheel revolution

[2048 2048] (default) | two-element vector of positive integers

Number of encoder ticks per wheel revolution, specified as a two-element vector of positive integers. The first element is for the left wheel, and the second element is for the right wheel.

Data Types: double

WheelRadius — Wheel radius

[0.35 0.35] (default) | two-element vector of positive scalars

Wheel radius, specified as a two-element vector of positive scalars in meters. The first element is for the left wheel, and the second element is for the right wheel.

Data Types: double

WheelRadiusBias — Bias of wheel radius

[0 0] (default) | two-element vector of scalars

Bias of the wheel radius, specified as a two-element vector of scalars in meters. The first element is for the left wheel, and the second element is for the right wheel.

Data Types: double

WheelPositionAccuracy — Standard deviation of wheel position error

[0 0] (default) | two-element vector of nonnegative scalar

Standard deviation of wheel position error, specified as a two-element vector of nonnegative scalars in radians. The first element is for the left wheel, and the second element is for the right wheel.

Data Types: double

SlipRatio — Slip or skid ratio of wheel

[0 0] (default) | two-element vector of scalar

Slip or skid ratio of the wheel, specified as a two-element vector of scalars in which each scalar is larger than or equal to -1. The first element is for the left wheel, and the second element is for the right wheel.

- For a wheel that slips (over rotation), specify it as a positive value. A higher value denotes more slipping.
- For a wheel that skids (under rotation), specify it as a negative value larger than or equal to -1. A lower value denotes more skidding. For a wheel that does not rotate, specify it as -1.

Data Types: double

TrackWidth — Distance between wheel axles

1.572 (default) | positive scalar

Distance between the wheel axles, specified as a positive scalar in meters.

Data Types: double

TrackWidthBias — Bias of track width

0 (default) | scalar

Bias of track width, specified as a scalar in meters.

Data Types: double

RandomStream — Random number source

'Global stream' (default) | 'mt19937ar with seed'

Random number source, specified as a character vector or string:

- 'Global stream' -- Random numbers are generated using the current global random number stream.
- 'mt19937ar with seed' -- Random numbers are generated using the mt19937ar algorithm with the seed specified by the Seed property.

Data Types: char | string

Seed — Initial seed

67 (default) | nonnegative integer

Initial seed of an mt19937ar random number generator algorithm, specified as a nonnegative integer.

Dependencies

To enable this property, set RandomStream to 'mt19937ar with seed'.

Usage

Syntax

ticks = encoder(velocity,angularVelocity,orientation)

Description

ticks = encoder(velocity, angular Velocity, orientation) return the wheel tick readings, ticks, form velocity, angular velocity, and orientation information.

Input Arguments

velocity — Velocity of vehicle

N-by-3 matrix of scalars

Velocity of the vehicle in the local navigation frame, specified as an N-by-3 matrix of scalars in m/s. N is the number of samples.

angularVelocity — Angular velocity of vehicle

N-by-3 matrix of scalars

Angular velocity of the vehicle in the local navigation frame, specified as an N-by-3 matrix of scalars in rad/s. N is the number of samples.

orientation — orientation of vehicle

N-element vector of quaternion | 3-by-3-by-*N* array of rotation matrices

Orientation of the vehicle in the local navigation frame, specified as an N-element vector of quaternion or a 3-by-3-by-N array of rotation matrices. N is the number of samples. Each quaternion or rotation matrix is a frame rotation from the local navigation coordinate system to the current vehicle body coordinate system.

Output Arguments

ticks - Number of wheel ticks per time step

N-by-2 matrix of nonnegative integers

Number of wheel ticks the vehicle moved per time step, returned as an N-by-2 matrix of integers. N is the number of samples. The first column is for the left wheel, and the second column is for the right wheel.

Object Functions

To use an object function, specify the System object as the first input argument. For example, to release system resources of a System object named obj, use this syntax:

release(obj)

Common to All System Objects

clone Create duplicate System object step Run System object algorithm

release Release resources and allow changes to System object property values and input

characteristics

reset Reset internal states of System object isLocked Determine if System object is in use

Examples

Generate Wheel Ticks from Differential Drive Vehicle Pose

```
Create the wheel encoder sensor.
```

```
encoder = wheelEncoderDifferentialDrive;
```

Define poses of the vehicle.

```
orient = [quaternion([60 0 0], 'eulerd', 'ZYX', 'frame'); quaternion([45 0], 'eulerd', 'ZYX', 'frame', 'ZYX', 'frame', 'ZYX', 'frame', 'ZYX', 'frame', 'ZYX', 'frame', 'ZYX', 'frame', 'ZYX'
```

Generate wheel ticks from the poses.

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

Usage notes and limitations:

See "System Objects in MATLAB Code Generation" (MATLAB Coder).

See Also

Introduced in R2020b

wheelEncoderUnicycle

Simulate wheel encoder sensor readings for unicycle vehicle

Description

The wheelEncoderUnicycle System object computes wheel encoder tick readings based on the pose input of a unicycle vehicle.

To obtain the encoder tick readings:

- 1 Create the wheelEncoderUnicycle object and set its properties.
- **2** Call the object with arguments, as if it were a function.

To learn more about how System objects work, see What Are System Objects?.

Creation

Syntax

```
encoder = wheelEncoderUnicycle
encoder = wheelEncoderUnicycle(Name, Value)
```

Description

encoder = wheelEncoderUnicycle creates a wheelEncoderUnicycle System object encoder.

encoder = wheelEncoderUnicycle(Name, Value) sets properties for the encoder using one or more name-value pairs. For example, wheelEncoderUnicycle('SampleRate', 120) sets the sample rate of the encoder to 120 Hz. Unspecified properties have default values. Enclose each property name in quotes.

Properties

Unless otherwise indicated, properties are *nontunable*, which means you cannot change their values after calling the object. Objects lock when you call them, and the release function unlocks them.

If a property is *tunable*, you can change its value at any time.

For more information on changing property values, see System Design in MATLAB Using System Objects.

SampleRate — Sample rate of encoder

100 (default) | positive scalar

Sample rate of the encoder, specified as a positive scalar in Hz.

Data Types: double

TicksPerRevolution — Number of encoder ticks per wheel revolution

2048 (default) | positive integer

Number of encoder ticks per wheel revolution, specified as a positive integer.

Data Types: double

WheelRadius — Wheel radius

0.35 (default) | positive scalar

Wheel radius, specified as a positive scalar in meters.

Data Types: double

WheelRadiusBias — Bias of wheel radius

0 (default) | scalar

Bias of the wheel radius, specified as a scalar in meters.

Data Types: double

WheelPositionAccuracy — Standard deviation of wheel position error

0 (default) | nonnegative scalar

Standard deviation of wheel position error, specified as a nonnegative scalar in radians.

Data Types: double

SlipRatio — Slip or skid ratio of wheel

0 (default) | scalar

Slip or skid ratio of the wheel, specified as a scalar larger than or equal to -1.

- For a wheel that slips (over rotation), specify it as a positive value. A higher value denotes more slipping.
- For a wheel that skids (under rotation), specify it as a negative value larger than or equal to -1. A lower value denotes more skidding. For a wheel that does not rotate, specify it as -1.

Data Types: double

RandomStream — Random number source

'Global stream' (default) | 'mt19937ar with seed'

Random number source, specified as a character vector or string:

- 'Global stream' -- Random numbers are generated using the current global random number stream.
- 'mt19937ar with seed' -- Random numbers are generated using the mt19937ar algorithm with the seed specified by the Seed property.

Data Types: char | string

Seed — Initial seed of mt19937ar random number generator algorithm

67 (default) | nonnegative integer

Initial seed of an mt19937ar random number generator algorithm, specified as a nonnegative integer.

Dependencies

To enable this property, set RandomStream to 'mt19937ar with seed'.

Usage

Syntax

ticks = encoder(velocity,angularVelocity,orientation)

Description

ticks = encoder(velocity, angularVelocity, orientation) return the wheel tick readings ticks from the specified velocity, angular velocity, and orientation information.

Input Arguments

velocity — Velocity of vehicle

N-by-3 matrix of scalars

Velocity of the vehicle in the local navigation frame, specified as an N-by-3 matrix of scalars in m/s. N is the number of samples.

angular Velocity — Angular velocity of vehicle

N-by-3 matrix of scalars

Angular velocity of the vehicle in the local navigation frame, specified as an N-by-3 matrix of scalars in rad/s. N is the number of samples.

orientation — orientation of vehicle

N-element vector of quaternion | 3-by-3-by-*N* array of rotation matrices

Orientation of the vehicle in the local navigation frame, specified as an N-element vector of quaternion or a 3-by-3-by-N array of rotation matrices. N is the number of samples. Each quaternion or rotation matrix is a frame rotation from the local navigation coordinate system to the current vehicle body coordinate system.

Output Arguments

ticks — Number of wheel ticks per time step

N-element vector of nonnegative integers

Number of wheel ticks the vehicle moved per time step, returned as an N-element vector of nonnegative integers. N is the number of samples.

Object Functions

To use an object function, specify the System object as the first input argument. For example, to release system resources of a System object named obj, use this syntax:

release(obj)

Common to All System Objects

clone Create duplicate System object step Run System object algorithm

release Release resources and allow changes to System object property values and input

characteristics

reset Reset internal states of System object isLocked Determine if System object is in use

Examples

Generate Wheel Ticks from Unicycle Vehicle Pose

```
Create the wheel encoder sensor.
```

```
encoder = wheelEncoderUnicycle;
```

Define poses of the vehicle.

```
orient = [quaternion([90 0 0],'eulerd','ZYX','frame'); quaternion([45 0 0], 'eulerd', 'ZYX', 'frame');
vel = [1 0 0; 0 1 0];
angvel = [0 0 0.2; 0 0 0.1];
```

Generate wheel ticks from the poses.

```
ticks = encoder(vel,angvel,orient)
ticks = 2 \times 1
```

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder $^{\text{\tiny TM}}$.

Usage notes and limitations:

See "System Objects in MATLAB Code Generation" (MATLAB Coder).

See Also

6

Introduced in R2020b

wheelEncoderOdometryAckermann

Compute Ackermann vehicle odometry using wheel encoder ticks and steering angle

Description

The wheelEncoderOdometryAckermann System object computes Ackermann vehicle odometry using the wheel encoder ticks and steering angle of the vehicle.

To compute Ackermann vehicle odometry:

- 1 Create the wheelEncoderOdometryAckermann object and set its properties.
- **2** Call the object with arguments, as if it were a function.

To learn more about how System objects work, see What Are System Objects?.

Creation

Syntax

```
whlEncOdom = wheelEncoderOdometryAckermann
whlEncOdom = wheelEncoderOdometryAckermann(encoder)
whlEncOdom = wheelEncoderOdometryAckermann(Name, Value)
```

Description

whlEncOdom = wheelEncoderOdometryAckermann creates a
wheelEncoderOdometryAckermann System object with default property values.

whlEncOdom = wheelEncoderOdometryAckermann(encoder) creates a wheelEncoderOdometryAckermann System object using the specified wheelEncoderAckermann System object, encoder, to set properties.

whlEncOdom = wheelEncoderOdometryAckermann(Name, Value) sets properties using one or more name-value pairs. Unspecified properties have default values. Enclose each property name in quotes.

For example, whlEncOdom = wheelEncoderOdometryAckermann('SampleRate',100) sets the sample rate of the sensor to 100 Hz.

Properties

Unless otherwise indicated, properties are *nontunable*, which means you cannot change their values after calling the object. Objects lock when you call them, and the release function unlocks them.

If a property is *tunable*, you can change its value at any time.

For more information on changing property values, see System Design in MATLAB Using System Objects.

SampleRate — Sample rate of sensor

100 (default) | positive scalar

Sample rate of sensor, specified as a positive scalar in hertz.

Example: 'SampleRate', 100

Data Types: double

TicksPerRevolution — Number of encoder ticks per wheel revolution

[2048 2048] (default) | positive integer | two-element vector of positive integers

Number of encoder ticks per wheel revolution, specified as a positive integer or two-element vector of positive integers.

When specifying this value as a two-element vector, the first element corresponds to the back left wheel and the second to the back right wheel.

Example: 'TicksPerRevolution', [2048 2048]

Data Types: double

WheelRadius — Wheel radius

[0.35 0.35] (default) | positive scalar | two-element vector of positive numbers

Wheel radius, specified as a positive scalar or two-element vector of positive numbers in meters.

When specifying this value as a two-element vector, the first element corresponds to the back left wheel and the second to the back right wheel.

Example: 'WheelRadius', [0.35 0.35]

Data Types: double

TrackWidth — Distance between wheels on axle

1.572 (default) | positive scalar

Distance between the wheels on the axle, specified as a positive scalar in meters.

Example: 'TrackWidth',1.572

Data Types: double

WheelBase — Distance between front and rear axle

2.818 (default) | positive scalar

Distance between the front and rear axle, specified as a positive scalar in meters.

Example: 'WheelBase',2.818

Data Types: double

InitialPose — Initial pose of vehicle

[0 0 0] (default) | three-element vector

Initial pose of the vehicle, specified as three-element vector of the form $[X \ Y \ Yaw]$. X and Y specify the vehicle position in meters. Yaw specifies the vehicle orientation in radians. All values are in the local navigation coordinate system.

Example: 'InitialPose', [0 0 0]

Data Types: double

Usage

Syntax

```
pose = whlEncOdom(ticks, steer)
[pose, velocity] = whlEncOdom(ticks, steer)
```

Description

pose = whlEncOdom(ticks, steer) computes the odometry of an Ackermann vehicle using the
specified wheel encoder ticks ticks and steering angle steer, and returns the position and
orientation of the vehicle in the local navigation coordinate system.

[pose, velocity] = whlEncOdom(ticks, steer) additionally returns the linear and angular velocity of the vehicle in the local navigation coordinate system.

Input Arguments

ticks - Number of wheel encoder ticks

n-by-2 matrix

Number of wheel encoder ticks, specified as an n-by-2 matrix. n is the number of samples in the current frame.

Each row of the matrix specifies wheel encoder ticks in the form [ticksBackLeft ticksBackRight], where ticksBackLeft and ticksBackRight specify the number of ticks for the back left and back right wheels, respectively.

```
Example: [5 5; 2 2]
Data Types: single | double
```

steer — Steering angle of vehicle

n-element column vector

Steering angle of the vehicle, specified as an n-element column vector in radians. n is the number of samples in the current frame.

```
Example: [0.2; 0.2]
Data Types: single | double
```

Output Arguments

pose — Position and orientation of vehicle

n-by-3 matrix

Position and orientation of the vehicle, returned as an *n*-by-3 matrix. *n* is the number of samples in the current frame. Each row of the matrix specifies the position and orientation of a sample in the form [X Y Yaw]. X and Y specify the vehicle position in meters. Yaw specifies the vehicle orientation in radians. All values are in the local navigation coordinate system.

```
Data Types: single | double
```

velocity — Linear and angular velocity of vehicle

n-by-3 matrix

Linear and angular velocity of the vehicle, returned as an *n*-by-3 matrix. *n* is the number of samples in the current frame. Each row of the matrix specifies the linear and angular velocity of a sample in the form [*velX velY yawRate*]. *velX* and *velY* specify the linear velocity of the vehicle in meters per second. *yawRate* specifies the angular velocity of the vehicle in radians per second. All values are in the local navigation coordinate system.

Data Types: single | double

Object Functions

To use an object function, specify the System object as the first input argument. For example, to release system resources of a System object named obj, use this syntax:

release(obj)

Common to All System Objects

clone Create duplicate System object step Run System object algorithm

release Release resources and allow changes to System object property values and input

characteristics

reset Reset internal states of System object isLocked Determine if System object is in use

Examples

Compute Ackermann Vehicle Odometry Using Wheel Encoder Ticks and Steering Angle

Create a wheelEncoderOdometryAckermann System object.

```
whlEncOdom = wheelEncoderOdometryAckermann;
```

Specify the number of wheel encoder ticks and the steering angle.

```
ticks = [5 5; 2 2];
steer = [0.2; 0.2];
```

Compute the Ackermann vehicle odometry.

```
[pose,vel] = whlEncOdom(ticks,steer)
pose = 2×3
      0.0053689     1.0368e-06     0.00038621
      0.0075165     2.0321e-06     0.00054069

vel = 2×3
      0.53689     0.00020735     0.038621
      0.21476     0.00011612     0.015448
```

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

wheelEncoderAckermann | wheelEncoderOdometryBicycle |
wheelEncoderOdometryDifferentialDrive | wheelEncoderOdometryUnicycle

Introduced in R2020b

wheelEncoderOdometryBicycle

Compute bicycle odometry using wheel encoder ticks and steering angle

Description

The wheelEncoderOdometryBicycle System object computes bicycle odometry using the wheel encoder ticks and steering angle of the vehicle.

To compute bicycle odometry:

- 1 Create the wheelEncoderOdometryBicycle object and set its properties.
- **2** Call the object with arguments, as if it were a function.

To learn more about how System objects work, see What Are System Objects?.

Creation

Syntax

```
whlEncOdom = wheelEncoderOdometryBicycle
whlEncOdom = wheelEncoderOdometryBicycle(encoder)
whlEncOdom = wheelEncoderOdometryBicycle(Name, Value)
```

Description

whlEncOdom = wheelEncoderOdometryBicycle creates a wheelEncoderOdometryBicycle System object with default property values.

whlEncOdom = wheelEncoderOdometryBicycle(encoder) creates a wheelEncoderOdometryBicycle System object using the specified wheelEncoderBicycle System object, encoder, to set properties.

whlEncOdom = wheelEncoderOdometryBicycle(Name, Value) sets properties using one or more name-value pairs. Unspecified properties have default values. Enclose each property name in quotes.

For example, whlEncOdom = wheelEncoderOdometryBicycle('SampleRate',100) sets the sample rate of the sensor to 100 Hz.

Properties

Unless otherwise indicated, properties are *nontunable*, which means you cannot change their values after calling the object. Objects lock when you call them, and the release function unlocks them.

If a property is *tunable*, you can change its value at any time.

For more information on changing property values, see System Design in MATLAB Using System Objects.

SampleRate — **Sample rate of sensor**

100 (default) | positive scalar

Sample rate of sensor, specified as a positive scalar in hertz.

Example: 'SampleRate', 100

Data Types: double

TicksPerRevolution — Number of encoder ticks per wheel revolution

2048 (default) | positive integer

Number of encoder ticks per wheel revolution, specified as a positive integer. This value corresponds to the rear wheel of the bicycle.

Example: 'TicksPerRevolution',2048

Data Types: double

WheelRadius — Wheel radius

0.35 (default) | positive scalar

Wheel radius, specified as a positive scalar in meters.

Example: 'WheelRadius',0.35

Data Types: double

WheelBase — Distance between front and rear axle

2.818 (default) | positive scalar

Distance between front and rear axle, specified as a positive scalar in meters.

Example: 'WheelBase',2.818

Data Types: double

InitialPose — Initial pose of vehicle

[0 0 0] (default) | three-element vector

Initial pose of the vehicle, specified as three-element vector of the form [X Y Yaw]. X and Y specify the vehicle position in meters. Yaw specifies the vehicle orientation in radians. All values are in the local navigation coordinate system.

Example: 'InitialPose',[0 0 0]

Tunable: No

Data Types: double

Usage

Syntax

```
pose = whlEncOdom(ticks,steer)
[pose,velocity] = whlEncOdom(ticks,steer)
```

Description

pose = whlEncOdom(ticks, steer) computes the odometry of a bicycle using the specified wheel
encoder ticks ticks and steering angle steer, and returns the position and orientation of the
vehicle in the local navigation coordinate system.

[pose, velocity] = whlEncOdom(ticks, steer) additionally returns the linear and angular velocity of the vehicle in the local navigation coordinate system.

Input Arguments

ticks - Number of wheel encoder ticks

n-element column vector

Number of wheel encoder ticks, specified as an n-element column vector. n is the number of samples in the current frame. Each element is the number of ticks for the rear wheel of the bicycle in the corresponding sample.

Example: [5; 2]

Data Types: single | double

steer — Steering angle of vehicle

n-element column vector

Steering angle of the vehicle, specified as an n-element column vector in radians. n is the number of samples in the current frame.

Example: [0.2; 0.2]

Data Types: single | double

Output Arguments

pose — Position and orientation of vehicle

n-by-3 matrix

Position and orientation of the vehicle, returned as an n-by-3 matrix. n is the number of samples in the current frame. Each row of the matrix specifies the position and orientation of a sample in the form $[X\ Y\ Yaw]$. X and Y specify the vehicle position in meters. Yaw specifies the vehicle orientation in radians. All values are in the local navigation coordinate system.

Data Types: single | double

velocity — Linear and angular velocity of vehicle

n-by-3 matrix

Linear and angular velocity of the vehicle, returned as an *n*-by-3 matrix. *n* is the number of samples in the current frame. Each row of the matrix specifies the linear and angular velocity of a sample in the form [*velX velY yawRate*]. *velX* and *velY* specify the linear velocity of the vehicle in meters per second. *yawRate* specifies the angular velocity of the vehicle in radians per second. All values are in the local navigation coordinate system.

Data Types: single | double

Object Functions

To use an object function, specify the System object as the first input argument. For example, to release system resources of a System object named obj, use this syntax:

```
release(obj)
```

Common to All System Objects

clone Create duplicate System object step Run System object algorithm

release Release resources and allow changes to System object property values and input

characteristics

reset Reset internal states of System object isLocked Determine if System object is in use

Examples

Compute Bicycle Odometry Using Wheel Encoder Ticks and Steering Angle

Create a wheelEncoderOdometryBicycle System object.

```
whlEncOdom = wheelEncoderOdometryBicycle;
```

Specify the number of wheel encoder ticks and the steering angle.

```
ticks = [5; 2];
steer = [0.2; 0.2];
```

Compute the bicycle odometry.

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

wheelEncoderBicycle | wheelEncoderOdometryAckermann |
wheelEncoderOdometryDifferentialDrive | wheelEncoderOdometryUnicycle

Introduced in R2020b

wheelEncoderOdometryDifferentialDrive

Compute differential-drive vehicle odometry using wheel encoder ticks

Description

The wheelEncoderOdometryDifferentialDrive System object computes differential-drive vehicle odometry using the wheel encoder ticks.

To compute differential-drive vehicle odometry:

- 1 Create the wheelEncoderOdometryDifferentialDrive object and set its properties.
- **2** Call the object with arguments, as if it were a function.

To learn more about how System objects work, see What Are System Objects?.

Creation

Syntax

```
whlEncOdom = wheelEncoderOdometryDifferentialDrive
whlEncOdom = wheelEncoderOdometryDifferentialDrive(encoder)
whlEncOdom = wheelEncoderOdometryDifferentialDrive(Name, Value)
```

Description

whlEncOdom = wheelEncoderOdometryDifferentialDrive creates a
wheelEncoderOdometryDifferentialDrive System object with default property values.

whlEncOdom = wheelEncoderOdometryDifferentialDrive(encoder) creates a wheelEncoderOdometryDifferentialDrive System object using the specified wheelEncoderDifferentialDrive System object, encoder, to set properties.

whlEncOdom = wheelEncoderOdometryDifferentialDrive(Name, Value) sets properties using one or more name-value pairs. Unspecified properties have default values. Enclose each property name in quotes.

For example, whlEncOdom = wheelEncoderOdometryDifferentialDrive('SampleRate', 100) sets the sample rate of the sensor to 100 Hz.

Properties

Unless otherwise indicated, properties are *nontunable*, which means you cannot change their values after calling the object. Objects lock when you call them, and the release function unlocks them.

If a property is *tunable*, you can change its value at any time.

For more information on changing property values, see System Design in MATLAB Using System Objects.

SampleRate — Sample rate of sensor

100 (default) | positive scalar

Sample rate of sensor, specified as a positive scalar in hertz.

Example: 'SampleRate', 100

Data Types: double

TicksPerRevolution — Number of encoder ticks per wheel revolution

[2048 2048] (default) | positive integer | two-element vector of positive integers

Number of encoder ticks per wheel revolution, specified as a positive integer or two-element vector of positive integers.

When specifying this value as a two-element vector, the first element corresponds to the left wheel and the second to the right wheel.

Example: 'TicksPerRevolution',[2048 2048]

Data Types: double

WheelRadius — Wheel radius

[0.35 0.35] (default) | positive scalar | two-element vector of positive numbers

Wheel radius, specified as a positive scalar or two-element vector of positive numbers in meters.

When specifying this value as a two-element vector, the first element corresponds to the left wheel and the second to the right wheel.

Example: 'WheelRadius', [0.35 0.35]

Data Types: double

TrackWidth — Distance between wheels on axle

1.572 (default) | positive scalar

Distance between the wheels on the axle, specified as a positive scalar in meters.

Example: 'TrackWidth', 1.572

Data Types: double

InitialPose — Initial pose of vehicle

[0 0 0] (default) | three-element vector

Initial pose of the vehicle, specified as three-element vector of the form [X Y Yaw]. X and Y specify the vehicle position in meters. Yaw specifies the vehicle orientation in radians. All values are in the local navigation coordinate system.

Example: 'InitialPose', [0 0 0]

Data Types: double

Usage

Syntax

```
pose = whlEncOdom(ticks)
[pose,velocity] = whlEncOdom(ticks)
```

Description

pose = whlEncOdom(ticks) computes the odometry of a differential-drive vehicle using the specified wheel encoder ticks ticks, and returns the position and orientation of the vehicle in the local navigation coordinate system.

[pose, velocity] = whlEncOdom(ticks) additionally returns the linear and angular velocity of the vehicle in the local navigation coordinate system.

Input Arguments

ticks — Number of wheel encoder ticks

n-by-2 matrix

Number of wheel encoder ticks, specified as an n-by-2 matrix. n is the number of samples in the current frame.

Each row of the matrix specifies wheel encoder ticks in the form [ticksLeft ticksRight], where ticksLeft and ticksRight specify the number of ticks for the left and right wheels, respectively.

Example: [5 5; 2 2]

Data Types: single | double

Output Arguments

pose — Position and orientation of vehicle

n-by-3 matrix

Position and orientation of the vehicle, returned as an n-by-3 matrix. n is the number of samples in the current frame. Each row of the matrix specifies the position and orientation of a sample in the form $[X \ Y \ Yaw]$. X and Y specify the vehicle position in meters. Yaw specifies the vehicle orientation in radians. All values are in the local navigation coordinate system.

Data Types: single | double

velocity — Linear and angular velocity of vehicle

n-by-3 matrix

Linear and angular velocity of the vehicle, returned as an *n*-by-3 matrix. *n* is the number of samples in the current frame. Each row of the matrix specifies the linear and angular velocity of a sample in the form [*velX velY yawRate*]. *velX* and *velY* specify the linear velocity of the vehicle in meters per second. *yawRate* specifies the angular velocity of the vehicle in radians per second. All values are in the local navigation coordinate system.

Data Types: single | double

Object Functions

To use an object function, specify the System object as the first input argument. For example, to release system resources of a System object named obj, use this syntax:

release(obj)

Common to All System Objects

clone Create duplicate System object step Run System object algorithm

release Release resources and allow changes to System object property values and input

characteristics

reset Reset internal states of System object isLocked Determine if System object is in use

Examples

Compute Differential-Drive Vehicle Odometry Using Wheel Encoder Ticks

Create a wheelEncoderOdometryDifferentialDrive System object.

whlEncOdom = wheelEncoderOdometryDifferentialDrive;

Specify the number of wheel encoder ticks.

ticks = [5 5; 2 2];

Compute the differential-drive vehicle odometry.

[pose,vel] = whlEncOdom(ticks)

pose = 2×3 0.0054 0 0

0.0075 0 0

vel = 2×3 0.5369 0 0

0.2148 0 0

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder[™].

See Also

wheelEncoderDifferentialDrive|wheelEncoderOdometryAckermann|
wheelEncoderOdometryBicycle|wheelEncoderOdometryUnicycle

Introduced in R2020b

wheelEncoderOdometryUnicycle

Compute unicycle odometry using wheel encoder ticks and angular velocity

Description

The wheelEncoderOdometryUnicycle System object computes unicycle odometry using the wheel encoder ticks and angular velocity.

To compute unicycle odometry:

- 1 Create the wheelEncoderOdometryUnicycle object and set its properties.
- **2** Call the object with arguments, as if it were a function.

To learn more about how System objects work, see What Are System Objects?.

Creation

Syntax

```
whlEncOdom = wheelEncoderOdometryUnicycle
whlEncOdom = wheelEncoderOdometryUnicycle(encoder)
whlEncOdom = wheelEncoderOdometryUnicycle(Name, Value)
```

Description

whlEncOdom = wheelEncoderOdometryUnicycle creates a wheelEncoderOdometryUnicycle System object with default property values.

whlEncOdom = wheelEncoderOdometryUnicycle(encoder) creates a wheelEncoderOdometryUnicycle System object using the specified wheelEncoderUnicycle System object, encoder, to set properties.

whlEncOdom = wheelEncoderOdometryUnicycle(Name, Value) sets properties using one or more name-value pairs. Unspecified properties have default values. Enclose each property name in quotes.

For example, whlEncOdom = wheelEncoderOdometryUnicycle('SampleRate',100) sets the sample rate of the sensor to 100 Hz.

Properties

Unless otherwise indicated, properties are *nontunable*, which means you cannot change their values after calling the object. Objects lock when you call them, and the release function unlocks them.

If a property is tunable, you can change its value at any time.

For more information on changing property values, see System Design in MATLAB Using System Objects.

SampleRate — Sample rate of sensor

100 (default) | positive scalar

Sample rate of sensor, specified as a positive scalar in hertz.

Example: 'SampleRate', 100

Data Types: double

TicksPerRevolution — Number of encoder ticks per wheel revolution

2048 (default) | positive integer

Number of encoder ticks per wheel revolution, specified as a positive integer.

Example: 'TicksPerRevolution',2048

Data Types: double

WheelRadius — Wheel radius

0.35 (default) | positive scalar

Wheel radius, specified as a positive scalar in meters.

Example: 'WheelRadius', 0.35

Data Types: double

InitialPose — Initial pose of vehicle

[0 0 0] (default) | three-element vector

Initial pose of the vehicle, specified as three-element vector of the form $[X \ Y \ Yaw]$. X and Y specify the vehicle position in meters. Yaw specifies the vehicle orientation in radians. All values are in the local navigation coordinate system.

Example: 'InitialPose', [0 0 0]

Tunable: No

Data Types: double

Usage

Syntax

```
pose = whlEncOdom(ticks,angVel)
[pose,velocity] = whlEncOdom(ticks,angVel)
```

Description

pose = whlEncOdom(ticks,angVel) computes the odometry of a unicycle using the specified
wheel encoder ticks ticks and angular velocity angVel, and returns the position and orientation of
the vehicle in the local navigation coordinate system.

[pose, velocity] = whlEncOdom(ticks, angVel) additionally returns the linear and angular velocity of the vehicle in the local navigation coordinate system.

Input Arguments

ticks — Number of wheel encoder ticks

n-element column vector

Number of wheel encoder ticks, specified as an n-element column vector. n is the number of samples in the current frame.

Example: [5; 2]

Data Types: single | double

angVel — Angular velocity of vehicle in vehicle body coordinate system

n-element column vector

Angular velocity of the vehicle in the vehicle body coordinate system, specified as an n-element column vector in radians per second. n is the number of samples in the current frame.

Example: [0.2; 0.2]

Data Types: single | double

Output Arguments

pose — Position and orientation of vehicle

n-by-3 matrix

Position and orientation of the vehicle, returned as an n-by-3 matrix. n is the number of samples in the current frame. Each row of the matrix specifies the position and orientation of a sample in the form $[X \ Y \ Yaw]$. X and Y specify the vehicle position in meters. Yaw specifies the vehicle orientation in radians. All values are in the local navigation coordinate system.

Data Types: single | double

velocity — Linear and angular velocity of vehicle

n-by-3 matrix

Linear and angular velocity of the vehicle, returned as an *n*-by-3 matrix. *n* is the number of samples in the current frame. Each row of the matrix specifies the linear and angular velocity of a sample in the form [*velX velY yawRate*]. *velX* and *velY* specify the linear velocity of the vehicle in meters per second. *yawRate* specifies the angular velocity of the vehicle in radians per second. All values are in the local navigation coordinate system.

Data Types: single | double

Object Functions

To use an object function, specify the System object as the first input argument. For example, to release system resources of a System object named obj, use this syntax:

release(obj)

Common to All System Objects

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release Release resources and allow changes to System object property values and input

characteristics

reset Reset internal states of System object isLocked Determine if System object is in use

Examples

Compute Unicycle Odometry Using Wheel Encoder Ticks and Angular Velocity

Create a wheelEncoderOdometryUnicycle System object.

```
whlEncOdom = wheelEncoderOdometryUnicycle;
```

Specify the number of wheel encoder ticks and angular velocity.

```
ticks = [5; 2];
angVel = [0.2; 0.2];
```

Compute the unicycle odometry.

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder™.

See Also

wheelEncoderOdometryAckermann | wheelEncoderOdometryBicycle | wheelEncoderOdometryDifferentialDrive | wheelEncoderUnicycle

Introduced in R2020b

Methods

Blocks

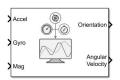
AHRS

Orientation from accelerometer, gyroscope, and magnetometer readings **Library:** Navigation Toolbox Toolbox / Multisensor Positioning /

Navigation Filters

Sensor Fusion and Tracking Toolbox / Multisensor

Positioning / Navigation Filters



Description

The AHRS Simulink® block fuses accelerometer, magnetometer, and gyroscope sensor data to estimate device orientation.

Ports

Input

Accel — Accelerometer readings in sensor body coordinate system (m/s²)

N-by-3 matrix of real scalar

Accelerometer readings in the sensor body coordinate system in m/s^2 , specified as an N-by-3 matrix of real scalars. N is the number of samples, and the three columns of Accel represent the $[x\ y\ z]$ measurements, respectively.

Data Types: single | double

Gyro — Gyroscope readings in sensor body coordinate system (rad/s)

N-by-3 matrix of real scalar

Gyroscope readings in the sensor body coordinate system in rad/s, specified as an N-by-3 matrix of real scalars. N is the number of samples, and the three columns of Gyro represent the $[x\ y\ z]$ measurements, respectively.

Data Types: single | double

Mag — Magnetometer readings in sensor body coordinate system (μT)

N-by-3 matrix of real scalar

Magnetometer readings in the sensor body coordinate system in μT , specified as an N-by-3 matrix of real scalars. N is the number of samples, and the three columns of magReadings represent the $[x\ y\ z]$ measurements, respectively.

Data Types: single | double

Output

Orientation — Orientation of sensor body frame relative to navigation frame

M-by-4 array of scalar | 3-by-3-by-*M*-element rotation matrix

Orientation of the sensor body frame relative to the navigation frame, return as an M-by-4 array of scalars or a 3-by-3-by-M array of rotation matrices. Each row the of the N-by-4 array is assumed to be the four elements of a quaternion. The number of input samples, N, and the **Decimation Factor** parameter determine the output size M.

Data Types: single | double

Angular Velocity — Angular velocity in sensor body coordinate system (rad/s)

M-by-3 array of real scalar (default)

Angular velocity with gyroscope bias removed in the sensor body coordinate system in rad/s, returned as an M-by-3 array of real scalars. The number of input samples, N, and the **Decimation Factor** parameter determine the output size M.

Data Types: single | double

Parameters

Main

Reference frame — Navigation reference frame

NED (default) | ENU

Navigation reference frame, specified as NED (North-East-Down) or ENU (East-North-Up).

Decimation factor — Decimation factor

1 (default) | positive integer

Decimation factor by which to reduce the input sensor data rate, specified as a positive integer.

The number of rows of the inputs -- **Accel**, **Gyro** , and **Mag** -- must be a multiple of the decimation factor.

Data Types: single | double

Initial process noise — Initial process noise

ahrsfilter.defaultProcessNoise (default) | 12-by-12 matrix of real scalar

Initial process noise, specified as a 12-by-12 matrix of real scalars. The default value, ahrsfilter.defaultProcessNoise, is a 12-by-12 diagonal matrix as:



Columns 7 through 12

	0	0	0	0
	0	0	0	0
	0	0	0	0
	0	0	0	0
	0	0	0	0
	0	0	0	0
	0	0	0	0.009623610000000
	0	0	0.009623610000000	0
	0	0.009623610000000	0	0
	0.6000000000000000	0	0	0
0.600000000000	0	0	0	0
	0	0	0	0

Data Types: single | double

Orientation format — Orientation output format

'quaternion' (default) | 'Rotation matrix'

Output orientation format, specified as 'quaternion' or 'Rotation matrix':

- 'quaternion' -- Output is an *M*-by-4 array of real scalars. Each row of the array represents the four components of a quaternion.
- 'Rotation matrix' -- Output is a 3-by-3-by-*M* rotation matrix.

The output size M depends on the input dimension N and the **Decimation Factor** parameter.

Data Types: char | string

Simulate using — Type of simulation to run

Interpreted Execution (default) | Code Generation

- Interpreted execution Simulate the model using the MATLAB interpreter. This option shortens startup time. In Interpreted execution mode, you can debug the source code of the block.
- Code generation Simulate the model using generated C code. The first time you run a simulation, Simulink generates C code for the block. The C code is reused for subsequent simulations as long as the model does not change. This option requires additional startup time.

Measurement Noise

Accelerometer noise $((m/s^2)^2)$ — Variance of accelerometer signal noise $((m/s^2)^2)$ 0.00019247 (default) | positive real scalar

Variance of accelerometer signal noise in $(m/s^2)^2$, specified as a positive real scalar.

Data Types: single | double

Gyroscope noise $((rad/s)^2)$ — Variance of gyroscope signal noise $((rad/s)^2)$

9.1385e-5 (default) | positive real scalar

Variance of gyroscope signal noise in (rad/s)², specified as a positive real scalar.

Data Types: single | double

Magnetometer noise (μT^2) — Variance of magnetometer signal noise (μT^2)

0.1 (default) | positive real scalar

Variance of magnetometer signal noise in μT^2 , specified as a positive real scalar.

Data Types: single | double

Gyroscope drift noise (rad/s) — Variance of gyroscope offset drift $((rad/s)^2)$

3.0462e-13 (default) | positive real scalar

Variance of gyroscope offset drift in (rad/s)², specified as a positive real scalar.

Data Types: single | double

Environmental Noise

Linear acceleration noise $((m/s^2)^2)$ — Variance of linear acceleration noise $(m/s^2)^2$ 0.0096236 (default) | positive real scalar

Variance of linear acceleration noise in $(m/s^2)^2$, specified as a positive real scalar. Linear acceleration is modeled as a lowpass-filtered white noise process.

Data Types: single | double

Magnetic disturbance noise (μT^2) — Variance of magnetic disturbance noise (μT^2)

0.5 (default) | real finite positive scalar

Variance of magnetic disturbance noise in μT^2 , specified as a real finite positive scalar.

Data Types: single | double

Linear acceleration decay factor — Decay factor for linear acceleration drift 0.5 (default) | scalar in the range [0,1)

Decay factor for linear acceleration drift, specified as a scalar in the range [0,1). If linear acceleration changes quickly, set this parameter to a lower value. If linear acceleration changes slowly, set this parameter to a higher value. Linear acceleration drift is modeled as a lowpass-filtered white noise process.

Data Types: single | double

${\bf Magnetic\ disturbance\ decay\ factor-Decay\ factor\ for\ magnetic\ disturbance}$

0.5 (default) | positive scalar in the range [0,1]

Decay factor for magnetic disturbance, specified as a positive scalar in the range [0,1]. Magnetic disturbance is modeled as a first order Markov process.

Data Types: single | double

Magnetic field strength (μ T) — Magnetic field strength (μ T)

50 (default) | real positive scalar

Magnetic field strength in μT , specified as a real positive scalar. The magnetic field strength is an estimate of the magnetic field strength of the Earth at the current location.

Data Types: single | double

Algorithms

Note: The following algorithm only applies to an NED reference frame.

The AHRS block uses the nine-axis Kalman filter structure described in [1] (Sensor Fusion and Tracking Toolbox). The algorithm attempts to track the errors in orientation, gyroscope offset, linear acceleration, and magnetic disturbance to output the final orientation and angular velocity. Instead of tracking the orientation directly, the indirect Kalman filter models the error process, x, with a recursive update:

$$x_k = \begin{bmatrix} \theta_k \\ b_k \\ a_k \\ d_k \end{bmatrix} = F_k \begin{bmatrix} \theta_{k-1} \\ b_{k-1} \\ a_{k-1} \\ d_{k-1} \end{bmatrix} + w_k$$

where x_k is a 12-by-1 vector consisting of:

- θ_k -- 3-by-1 orientation error vector, in degrees, at time k
- b_k -- 3-by-1 gyroscope zero angular rate bias vector, in deg/s, at time k
- a_k -- 3-by-1 acceleration error vector measured in the sensor frame, in g, at time k
- d_k -- 3-by-1 magnetic disturbance error vector measured in the sensor frame, in μ T, at time k

and where w_k is a 12-by-1 additive noise vector, and F_k is the state transition model.

Because x_k is defined as the error process, the *a priori* estimate is always zero, and therefore the state transition model, F_k , is zero. This insight results in the following reduction of the standard Kalman equations:

Standard Kalman equations:

$$x_{k}^{-} = F_{k}x_{k-1}^{+}$$

$$P_{k}^{-} = F_{k}P_{k-1}^{+}F_{k}^{T} + Q_{k}$$

$$y_{k} = z_{k} - H_{k}x_{k}^{-}$$

$$S_{k} = R_{k} + H_{k}P_{k}^{-}H_{k}T$$

$$K_{k} = P_{k}^{-}H_{k}^{T}(S_{k})^{-1}$$

$$x_{k}^{+} = x_{k}^{-} + K_{k}y_{k}$$

$$P_{k}^{+} = P_{k} - K_{k}H_{k}P_{k}^{-}$$

Kalman equations used in this algorithm:

$$x_k^- = 0$$

$$P_k^- = Q_k$$

$$y_k = z_k$$

$$S_k = R_k + H_k P_k^- H_k T$$

$$K_k = P_k^- H_k^T (S_k)^{-1}$$

$$x_k^+ = K_k y_k$$

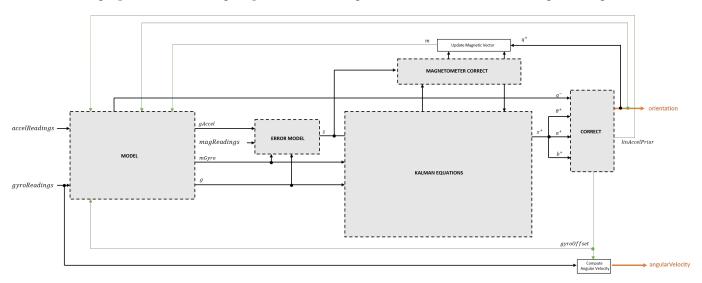
$$P_k^+ = P_k - K_k H_k P_k^-$$

where:

- x_k^- -- predicted (*a priori*) state estimate; the error process
- P_k^- -- predicted (a priori) estimate covariance
- y_k -- innovation
- S_k -- innovation covariance
- K_k -- Kalman gain
- x_k^+ -- updated (*a posteriori*) state estimate
- P_k^+ -- updated (a posteriori) estimate covariance

k represents the iteration, the superscript $^+$ represents an a posteriori estimate, and the superscript $^-$ represents an a priori estimate.

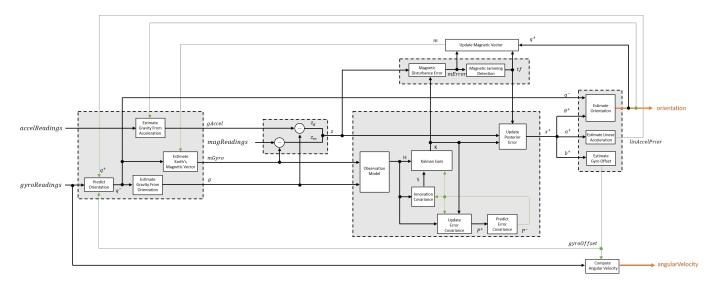
The graphic and following steps describe a single frame-based iteration through the algorithm.



Before the first iteration, the accelReadings, gyroReadings, and magReadings inputs are chunked into DecimationFactor-by-3 frames. For each chunk, the algorithm uses the most current accelerometer and magnetometer readings corresponding to the chunk of gyroscope readings.

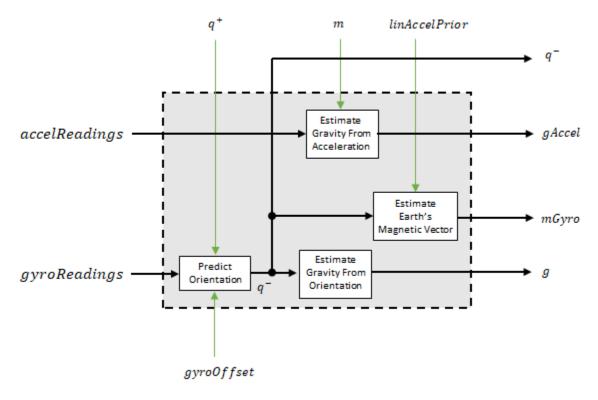
Detailed Overview

Walk through the algorithm for an explanation of each stage of the detailed overview.



Model

The algorithm models acceleration and angular change as linear processes.



Predict Orientation

The orientation for the current frame is predicted by first estimating the angular change from the previous frame:

$$\Delta \varphi_{N \times 3} = \frac{(gyroReadings_{N \times 3} - gyroOffset_{1 \times 3})}{fs}$$

where N is the decimation factor specified by the Decimation factor and fs is the sample rate.

The angular change is converted into quaternions using the rotvec quaternion construction syntax:

$$\Delta Q_{N \times 1} = \text{quaternion}(\Delta \varphi_{N \times 3}, 'rotvec')$$

The previous orientation estimate is updated by rotating it by ΔQ :

$$q_{1\times 1}^{-} = \left(q_{1\times 1}^{+}\right) \left(\prod_{n=1}^{N} \Delta Q_{n}\right)$$

During the first iteration, the orientation estimate, q^- , is initialized by **ecompass**.

Estimate Gravity from Orientation

The gravity vector is interpreted as the third column of the quaternion, q^- , in rotation matrix form:

$$g_{1\times 3} = (rPrior(:,3))^T$$

Estimate Gravity from Acceleration

A second gravity vector estimation is made by subtracting the decayed linear acceleration estimate of the previous iteration from the accelerometer readings:

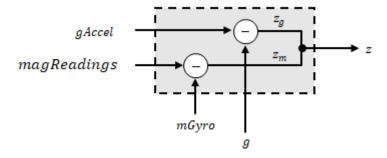
$$gAccel_{1 \times 3} = accelReadings_{1 \times 3} - linAccelprior_{1 \times 3}$$

Estimate Earth's Magnetic Vector

Earth's magnetic vector is estimated by rotating the magnetic vector estimate from the previous iteration by the *a priori* orientation estimate, in rotation matrix form:

$$mGyro_{1 \times 3} = ((rPrior)(m^T))^T$$

Error Model

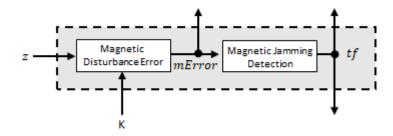


The error model combines two differences:

- The difference between the gravity estimate from the accelerometer readings and the gravity estimate from the gyroscope readings: $z_q = g gAccel$
- The difference between the magnetic vector estimate from the gyroscope readings and the magnetic vector estimate from the magnetometer: $z_m = mGyro magReadings$

Magnetometer Correct

The magnetometer correct estimates the error in the magnetic vector estimate and detects magnetic jamming.



Magnetometer Disturbance Error

The magnetic disturbance error is calculated by matrix multiplication of the Kalman gain associated with the magnetic vector with the error signal:

$$mError_{3 \times 1} = ((K(10:12,:)_{3 \times 6})(z_{1 \times 6})^T)^T$$

The Kalman gain, *K*, is the Kalman gain calculated in the current iteration.

Magnetic Jamming Detection

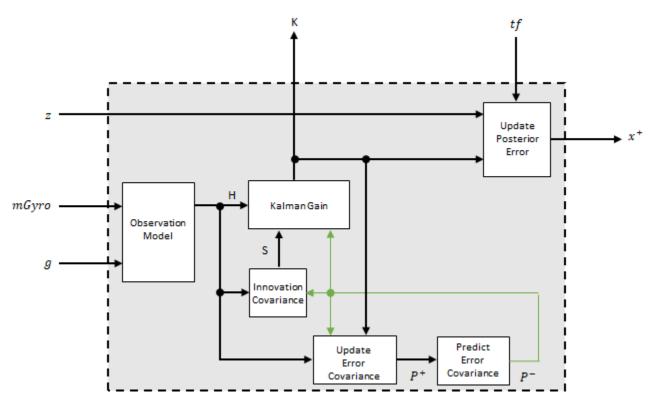
Magnetic jamming is determined by verifying that the power of the detected magnetic disturbance is less than or equal to four times the power of the expected magnetic field strength:

$$tf = \begin{cases} \text{true if } \sum |mError|^2 > (4)(\text{ExpectedMagneticFieldStrength})^2 \end{cases}$$

ExpectedMagneticFieldStrength is a property of ahrsfilter.

Kalman Equations

The Kalman equations use the gravity estimate derived from the gyroscope readings, g, the magnetic vector estimate derived from the gyroscope readings, mGyro, and the observation of the error process, z, to update the Kalman gain and intermediary covariance matrices. The Kalman gain is applied to the error signal, z, to output an a posteriori error estimate, x^+ .



Observation Model

The observation model maps the 1-by-3 observed states, g and mGyro, into the 6-by-12 true state, H.

The observation model is constructed as:

$$H_{3 \times 9} = \begin{bmatrix} 0 & g_z & -g_y & 0 & -\kappa g_z & \kappa g_y & 1 & 0 & 0 & 0 & 0 \\ -g_z & 0 & g_x & \kappa g_z & 0 & -\kappa g_x & 0 & 1 & 0 & 0 & 0 & 0 \\ g_y & -g_x & 0 & -\kappa g_y & \kappa g_x & 0 & 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & m_z & -m_y & 0 & -\kappa m_z & -\kappa m_y & 0 & 0 & 0 & -1 & 0 & 0 \\ -m_z & 0 & m_x & \kappa m_z & 0 & -\kappa m_x & 0 & 0 & 0 & 0 & -1 & 0 \\ m_y & -m_x & 0 & -\kappa m_y & \kappa m_x & 0 & 0 & 0 & 0 & 0 & -1 \end{bmatrix}$$

where g_x , g_y , and g_z are the x-, y-, and z-elements of the gravity vector estimated from the a priori orientation, respectively. m_x , m_y , and m_z are the x-, y-, and z-elements of the magnetic vector estimated from the a priori orientation, respectively. κ is a constant determined by the Sample rate and Decimation factor properties: $\kappa = \text{Decimation factor}/\text{Sample rate}$.

Innovation Covariance

The innovation covariance is a 6-by-6 matrix used to track the variability in the measurements. The innovation covariance matrix is calculated as:

$$S_{6x6} = R_{6x6} + (H_{6x12})(P_{12x12}^{-})(H_{6x12})^{T}$$

where

- *H* is the observation model matrix
- P^- is the predicted (a priori) estimate of the covariance of the observation model calculated in the previous iteration
- *R* is the covariance of the observation model noise, calculated as:

$$R_{6 \times 6} = \begin{bmatrix} accel_{\text{noise}} & 0 & 0 & 0 & 0 & 0 \\ 0 & accel_{\text{noise}} & 0 & 0 & 0 & 0 \\ 0 & 0 & accel_{\text{noise}} & 0 & 0 & 0 \\ 0 & 0 & 0 & mag_{\text{noise}} & 0 & 0 \\ 0 & 0 & 0 & 0 & mag_{\text{noise}} & 0 \\ 0 & 0 & 0 & 0 & 0 & mag_{\text{noise}} \end{bmatrix}$$

where

 $accel_{noise}$ = AccelerometerNoise + LinearAccelerationNoise + κ^2 (GyroscopeDriftNoise + GyroscopeNoise)

and

 $mag_{\text{noise}} = \text{MagnetometerNoise} + \text{MagneticDisturbanceNoise} + \kappa^2$ (GyroscopeDriftNoise + GyroscopeNoise)

Update Error Estimate Covariance

The error estimate covariance is a 12-by-12 matrix used to track the variability in the state.

The error estimate covariance matrix is updated as:

$$P_{12 \times 12}^+ = P_{12 \times 12}^- - (K_{12 \times 6})(H_{6 \times 12})(P_{12 \times 12}^-)$$

where K is the Kalman gain, H is the measurement matrix, and P^- is the error estimate covariance calculated during the previous iteration.

Predict Error Estimate Covariance

The error estimate covariance is a 12-by-12 matrix used to track the variability in the state. The *a priori* error estimate covariance, P^- , is set to the process noise covariance, Q, determined during the previous iteration. Q is calculated as a function of the *a posteriori* error estimate covariance, P^+ . When calculating Q, it is assumed that the cross-correlation terms are negligible compared to the autocorrelation terms, and are set to zero:

Q =

$P^{+}(1) + \kappa^{2}P^{+}(40) + \beta + \eta$	0	0	$-\kappa(P^{+}(40)+\beta)$	0
0	$P^{+}(14) + \kappa^{2}P^{+}(53) + \beta + \eta$	0	0	$-\kappa (P^{+}(53) +$
0	0	$P^{+}(27) + \kappa^{2}P^{+}(66) + \beta + \eta$	0	0
$-\kappa \left(P^+(40)+\beta\right)$	0	0	$P^+(40) + \beta$	0
0	$-\kappa \left(P^+(53) + \beta\right)$	0	0	$P^+(53) + \beta$
0	0	$-\kappa \left(P^+(66) + \beta\right)$	0	0
0	0	0	0	0
0	0	0	0	0
0	0	0	0	0
0	0	0	0	0
0	0	0	0	0
0	0	0	0	0
I				

where

- P+ -- is the updated (a posteriori) error estimate covariance
- κ -- Decimation factor divided by sample rate.
- β -- Gyroscope drift noise.
- η -- Gyroscope noise.
- ν -- Linear acceleration decay factor.
- ξ -- Linear acceleration noise.
- σ --- Magnetic disturbance decay factor.
- *y* -- Magnetic disturbance noise.

Kalman Gain

The Kalman gain matrix is a 12-by-6 matrix used to weight the innovation. In this algorithm, the innovation is interpreted as the error process, z.

The Kalman gain matrix is constructed as:

$$K_{12 \times 6} = (P_{12 \times 12}^{-})(H_{6 \times 12})^{T}((S_{6 \times 6})^{T})^{-1}$$

where

- *P*⁻ -- predicted error covariance
- *H* -- observation model
- S -- innovation covariance

Update a Posteriori Error

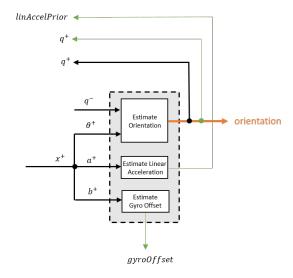
The *a posterior* error estimate is determined by combining the Kalman gain matrix with the error in the gravity vector and magnetic vector estimations:

$$x_{12 \times 1} = (K_{12 \times 6})(z_{1 \times 6})^T$$

If magnetic jamming is detected in the current iteration, the magnetic vector error signal is ignored, and the *a posterior* error estimate is calculated as:

$$x_{9 \times 1} = (K(1:9, 1:3)(z_q)^T)$$

Correct



Estimate Orientation

The orientation estimate is updated by multiplying the previous estimation by the error:

$$q^+ = (q^-)(\theta^+)$$

Estimate Linear Acceleration

The linear acceleration estimation is updated by decaying the linear acceleration estimation from the previous iteration and subtracting the error:

$$linAccelPrior = (linAccelPrior_{k-1})\nu - b^+$$

where

• ν -- Linear acceleration decay factor

Estimate Gyroscope Offset

The gyroscope offset estimation is updated by subtracting the gyroscope offset error from the gyroscope offset from the previous iteration:

$$gyroOffset = gyroOffset_{k-1} - a^+$$

Compute Angular Velocity

To estimate angular velocity, the frame of <code>gyroReadings</code> are averaged and the gyroscope offset computed in the previous iteration is subtracted:

$$angular Velocity_{1\times 3} = \frac{\sum gyroReadings_{N\times 3}}{N} - gyroOffset_{1\times 3}$$

where N is the decimation factor specified by the **DecimationFactor** property.

The gyroscope offset estimation is initialized to zeros for the first iteration.

Update Magnetic Vector

If magnetic jamming was not detected in the current iteration, the magnetic vector estimate, m, is updated using the a posteriori magnetic disturbance error and the a posteriori orientation.

The magnetic disturbance error is converted to the navigation frame:

$$mErrorNED_{1 \times 3} = ((rPost_{3 \times 3})^T (mError_{1 \times 3})^T)^T$$

The magnetic disturbance error in the navigation frame is subtracted from the previous magnetic vector estimate and then interpreted as inclination:

```
M = m - mErrorNED

inclination = atan2(M(3), M(1))
```

The inclination is converted to a constrained magnetic vector estimate for the next iteration:

- m(1) = (ExpectedMagneticFieldStrength)(cos(inclination))
- m(2) = 0
- m(3) = (ExpectedMagneticFieldStrength)(sin(inclination))

References

- [1] Open Source Sensor Fusion. https://github.com/memsindustrygroup/Open-Source-Sensor-Fusion/tree/master/docs
- [2] Roetenberg, D., H.J. Luinge, C.T.M. Baten, and P.H. Veltink. "Compensation of Magnetic Disturbances Improves Inertial and Magnetic Sensing of Human Body Segment Orientation." *IEEE Transactions on Neural Systems and Rehabilitation Engineering*. Vol. 13. Issue 3, 2005, pp. 395-405.

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using Simulink® Coder™.

See Also

ahrsfilter | ecompass | gpsSensor | imuSensor | imufilter

Introduced in R2020a

Coordinate Transformation Conversion

Convert to a specified coordinate transformation representation

Library: Robotics System Toolbox / Utilities

Navigation Toolbox / Utilities ROS Toolbox / Utilities UAV Toolbox / Utilities



Description

The Coordinate Transformation Conversion block converts a coordinate transformation from the input representation to a specified output representation. The input and output representations use the following forms:

- Axis-Angle (AxAng) [x y z theta]
- Euler Angles (Eul) [z y x], [z y z], or [x y z]
- Homogeneous Transformation (TForm) 4-by-4 matrix
- Quaternion (Quat) [w x y z]
- Rotation Matrix (RotM) 3-by-3 matrix
- Translation Vector (TrVec) [x y z]

All vectors must be **column vectors**.

To accommodate representations that only contain position or orientation information (TrVec or Eul, for example), you can specify two inputs or outputs to handle all transformation information. When you select the Homogeneous Transformation as an input or output, an optional Show TrVec input/output port parameter can be selected on the block mask to toggle the multiple ports.

Ports

Input

Input transformation — Coordinate transformation

column vector | 3-by-3 matrix | 4-by-4 matrix

Input transformation, specified as a coordinate transformation. The following representations are supported:

- Axis-Angle (AxAng) [x y z theta]
- Euler Angles (Eul) [z y x], [z y z], or [x y z]
- Homogeneous Transformation (TForm) 4-by-4 matrix
- Quaternion (Quat) [w x y z]
- Rotation Matrix (RotM) 3-by-3 matrix

• Translation Vector (TrVec) - [x y z]

All vectors must be **column vectors**.

To accommodate representations that only contain position or orientation information (TrVec or Eul, for example), you can specify two inputs or outputs to handle all transformation information. When you select the Homogeneous Transformation as an input or output, an optional Show TrVec input/output port parameter can be selected on the block mask to toggle the multiple ports.

TrVec — Translation vector

3-element column vector

Translation vector, specified as a 3-element column vector, $[x \ y \ z]$, which corresponds to a translation in the x, y, and z axes respectively. This port can be used to input or output the translation information separately from the rotation vector.

Dependencies

You must select Homogeneous Transformation (TForm) for the opposite transformation port to get the option to show the additional TrVec port. Enable the port by clicking Show TrVec input/output port.

Output Arguments

Output transformation — Coordinate transformation

column vector | 3-by-3 matrix | 4-by-4 matrix

Output transformation, specified as a coordinate transformation with the specified representation. The following representations are supported:

- Axis-Angle (AxAng) [x y z theta]
- Euler Angles (Eul) [z y x], [z y z], or [x y z]
- Homogeneous Transformation (TForm) 4-by-4 matrix
- Quaternion (Quat) [w x y z]
- Rotation Matrix (RotM) 3-by-3 matrix
- Translation Vector (TrVec) [x y z]

To accommodate representations that only contain position or orientation information (TrVec or Eul, for example), you can specify two inputs or outputs to handle all transformation information. When you select the Homogeneous Transformation as an input or output, an optional Show TrVec input/output port parameter can be selected on the block mask to toggle the multiple ports.

TrVec — Translation vector

three-element column vector

Translation vector, specified as a three-element column vector, $[x \ y \ z]$, which corresponds to a translation in the x, y, and z axes respectively. This port can be used to input or output the translation information separately from the rotation vector.

Dependencies

You must select Homogeneous Transformation (TForm) for the opposite transformation port to get the option to show the additional TrVec port. Enable the port by clicking Show TrVec input/output port.

Parameters

Representation — Input or output representation

Axis-Angle | Euler Angles | Homogeneous Transformation | Rotation Matrix | Translation Vector | Quaternion

Select the representation for both the input and output port for the block. If you are using a transformation with only orientation information, you can also select the Show TrVec input/output port when converting to or from a homogeneous transformation.

Axis rotation sequence — Order of Euler angle axis rotations

ZYX (default) | ZYZ | XYZ

Order of the Euler angle axis rotations, specified as ZYX, ZYZ, or XYZ. The order of the angles in the input or output port Eul must match this rotation sequence. The default order ZYX specifies an orientation by:

- Rotating about the initial *z*-axis
- Rotating about the intermediate *y*-axis
- Rotating about the second intermediate *x*-axis

Dependencies

You must select Euler Angles for the Representation input or output parameter. The axis rotation sequence only applies to Euler angle rotations.

Show TrVec input/output port — Toggle TrVec port

off (default) | on

Toggle the TrVec input or output port when you want to specify or receive a separate translation vector for position information along with an orientation representation.

Dependencies

You must select Homogeneous Transformation (TForm) for the opposite transformation port to get the option to show the additional TrVec port.

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using Simulink® Coder™.

See Also

axang2quat | eul2tform | trvec2tform

Introduced in R2017b

IMU

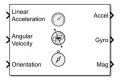
IMU simulation model

Library: Sensor Fusion and Tracking Toolbox / Multisensor

Positioning / Sensor Models

Navigation Toolbox / Multisensor Positioning / Sensor

Models



Description

The IMU Simulink block models receiving data from an inertial measurement unit (IMU) composed of accelerometer, gyroscope, and magnetometer sensors.

Ports

Input

Linear Acceleration — Acceleration of IMU in local navigation coordinate system (m/s 2) N-by-3 matrix of real scalar

Acceleration of the IMU in the local navigation coordinate system, specified as an N-by-3 matrix of real scalars in meters per second squared. N is the number of samples in the current frame.

Data Types: single | double

Angular Velocity — Angular velocity of IMU in local navigation coordinate system (rad/s) N-bv-3 matrix of real scalar

Angular velocity of the IMU sensor body frame in the local navigation coordinate system, specified as an N-by-3 matrix of scalars in radians per second. N is the number of samples in the current frame.

Data Types: single | double

Orientation — Orientation of IMU in local navigation coordinate system

N-by-4 array of real scalar | 3-by-3-by-N-element rotation matrix

Orientation of the IMU sensor body frame with respect to the local navigation coordinate system, specified as an N-by-4 array of real scalars or a 3-by-3-by-N rotation matrix. Each row the of the N-by-4 array is assumed to be the four elements of a quaternion. N is the number of samples in the current frame.

Data Types: single | double

Output

Accel — Accelerometer measurement of IMU in sensor body coordinate system (m/s 2) N-bv-3 matrix of real scalar

Accelerometer measurement of the IMU in the sensor body coordinate system, returned as an N-by-3 matrix of real scalars in meters per second squared. N is the number of samples in the current frame.

Data Types: single | double

Gyro — Gyroscope measurement of IMU in sensor body coordinate system (rad/s)

N-by-3 matrix of real scalar

Gyroscope measurement of the IMU in the sensor body coordinate system, returned as an N-by-3 matrix of real scalars in radians per second. N is the number of samples in the current frame.

Data Types: single | double

Mag — Magnetometer measurement of IMU in sensor body coordinate system (μT)

N-by-3 matrix of real scalar

Magnetometer measurement of the IMU in the sensor body coordinate system, returned as an N-by-3 matrix of real scalars in microtesla. N is the number of samples in the current frame.

Data Types: single | double

Parameters

Parameters

Reference frame — Navigation reference frame

NED (default) | ENU

Navigation reference frame, specified as NED (North-East-Down) or ENU (East-North-Up).

Temperature (°C) — Operating temperature of IMU (°C)

25 (default) | real scalar

Operating temperature of the IMU in degrees Celsius, specified as a real scalar.

When the block calculates temperature scale factors and environmental drift noises, $25~^{\circ}\text{C}$ is used as the nominal temperature.

Data Types: single | double

Magnetic field (NED) — Magnetic field vector expressed in NED navigation frame (μT) [27.5550, -2.4169, -16.0849] (default) | 1-by-3 vector of scalar

Magnetic field vector expressed in the NED navigation frame, specified as a 1-by-3 vector of scalars.

The default magnetic field corresponds to the magnetic field at latitude zero, longitude zero, and altitude zero.

Dependencies

To enable this parameter, set **Reference frame** to NED.

Data Types: single | double

MagneticField (ENU) — Magnetic field vector expressed in ENU navigation frame (μT) [-2.4169, 27.5550, 16.0849] (default) | 1-by-3 vector of scalar

Magnetic field vector expressed in the ENU navigation frame, specified as a 1-by-3 vector of scalars.

The default magnetic field corresponds to the magnetic field at latitude zero, longitude zero, and altitude zero.

Dependencies

To enable this parameter, set **Reference frame** to ENU.

Data Types: single | double

Seed — Initial seed for randomization

67 (default) | nonnegative integer

Initial seed of a random number generator algorithm, specified as a nonnegative integer.

Data Types: single | double

Simulate using — Type of simulation to run

Interpreted Execution (default) | Code Generation

- Interpreted execution Simulate the model using the MATLAB interpreter. This option shortens startup time. In Interpreted execution mode, you can debug the source code of the block.
- Code generation Simulate the model using generated C code. The first time that you run a simulation, Simulink generates C code for the block. The C code is reused for subsequent simulations if the model does not change. This option requires additional startup time.

Accelerometer

Maximum readings (m/s^2) — Maximum sensor reading (m/s^2)

inf (default) | real positive scalar

Maximum sensor reading in m/s², specified as a real positive scalar.

Data Types: single | double

Resolution $((m/s^2)/LSB)$ — Resolution of sensor measurements $((m/s^2)/LSB)$

0 (default) | real nonnegative scalar

Resolution of sensor measurements in (m/s²)/LSB, specified as a real nonnegative scalar.

Data Types: single | double

Constant offset bias (m/s^2) — Constant sensor offset bias (m/s^2)

[0 0 0] (default) | real scalar | real 3-element row vector

Constant sensor offset bias in m/s², specified as a real scalar or 3-element row vector. Any scalar input is converted into a real 3-element row vector where each element has the input scalar value.

Data Types: single | double

Axis skew (%) — Sensor axes skew (%)

[0 0 0] (default) | real scalar in the range [0,100] | real 3-element row vector in the range [0,100]

Sensor axes skew in a percentage, specified as a real scalar or 3-element row vector with values ranging from 0 to 100. Any scalar input is converted into a real 3-element row vector where each element has the input scalar value.

Data Types: single | double

Velocity random walk $(m/s^2/\sqrt{Hz})$ — Velocity random walk $(m/s^2/\sqrt{Hz})$

[0 0 0] (default) | real scalar | real 3-element row vector

Velocity random walk in $(m/s^2/\sqrt{Hz})$, specified as a real scalar or 3-element row vector. This property corresponds to the power spectral density of sensor noise. Any scalar input is converted into a real 3-element row vector where each element has the input scalar value.

Data Types: single | double

Bias Instability (m/s^2) — Instability of the bias offset (m/s^2)

[0 0 0] (default) | real scalar | real 3-element row vector

Instability of the bias offset in m/s^2 , specified as a real scalar or 3-element row vector. Any scalar input is converted into a real 3-element row vector where each element has the input scalar value.

Data Types: single | double

Acceleration random walk $((m/s^2)(\sqrt{Hz}))$ — Acceleration random walk $((m/s^2)(\sqrt{Hz}))$ [0 0 0] (default) | real scalar | real 3-element row vector

Acceleration random walk of sensor in $(m/s^2)(\sqrt{Hz})$, specified as a real scalar or 3-element row vector. Any scalar input is converted into a real 3-element row vector where each element has the input scalar value.

Data Types: single | double

Bias from temperature ((m/s 2)/ $^{\circ}$ C) — Sensor bias from temperature ((m/s 2)/ $^{\circ}$ C) [0 0 0] (default) | real scalar | real 3-element row vector

Sensor bias from temperature in (m/s^2) /°C, specified as a real scalar or 3-element row vector. Any scalar input is converted into a real 3-element row vector where each element has the input scalar value.

Data Types: single | double

Temperature scale factor (%/°C) — Scale factor error from temperature (%/°C)

[0 0 0] (default) | real scalar in the range [0,100] | real 3-element row vector in the range [0,100]

Scale factor error from temperature in %°C, specified as a real scalar or real 3-element row vector with values ranging from 0 to 100. Any scalar input is converted into a real 3-element row vector where each element has the input scalar value.

Data Types: single | double

Gyroscope

Maximum readings (rad/s) — Maximum sensor reading (rad/s)

inf (default) | real positive scalar

Maximum sensor reading in rad/s, specified as a real positive scalar.

Data Types: single | double

Resolution ((rad/s)/LSB) — Resolution of sensor measurements ((rad/s)/LSB)

0 (default) | real nonnegative scalar

Resolution of sensor measurements in (rad/s)/LSB, specified as a real nonnegative scalar.

Data Types: single | double

Constant offset bias (rad/s) — Constant sensor offset bias (rad/s)

[0 0 0] (default) | real scalar | real 3-element row vector

Constant sensor offset bias in rad/s, specified as a real scalar or 3-element row vector. Any scalar input is converted into a real 3-element row vector where each element has the input scalar value.

Data Types: single | double

Axis skew (%) — Sensor axes skew (%)

[0 0 0] (default) | real scalar in the range [0,100] | real 3-element row vector in the range [0,100]

Sensor axes skew in a percentage, specified as a real scalar or 3-element row vector with values ranging from 0 to 100. Any scalar input is converted into a real 3-element row vector where each element has the input scalar value.

Data Types: single | double

Bias from acceleration $((rad/s)/(m/s^2) - Sensor bias from linear acceleration$ $(rad/s)/(m/s^2)$

[0 0 0] (default) | real scalar | real 3-element row vector

Sensor bias from linear acceleration in (rad/s)/(m/s²), specified as a real scalar or 3-element row vector. Any scalar input is converted into a real 3-element row vector where each element has the input scalar value.

Data Types: single | double

Angle random walk $((rad/s)/(\sqrt{Hz}))$ — Acceleration random walk $((rad/s)/(\sqrt{Hz}))$

[0 0 0] (default) | real scalar | real 3-element row vector

Acceleration random walk of sensor in $(rad/s)/(\sqrt{Hz})$, specified as a real scalar or 3-element row vector. Any scalar input is converted into a real 3-element row vector where each element has the input scalar value.

Data Types: single | double

Bias Instability (rad/s) — Instability of the bias offset (rad/s)

[0 0 0] (default) | real scalar | real 3-element row vector

Instability of the bias offset in rad/s, specified as a real scalar or 3-element row vector. Any scalar input is converted into a real 3-element row vector where each element has the input scalar value.

Data Types: single | double

Rate random walk ((rad/s)(√Hz)) — Integrated white noise of sensor ((rad/s)(√Hz))

[0 0 0] (default) | real scalar | real 3-element row vector

Integrated white noise of sensor in $(rad/s)(\sqrt{Hz})$, specified as a real scalar or 3-element row vector. Any scalar input is converted into a real 3-element row vector where each element has the input scalar value.

Data Types: single | double

Bias from temperature $((rad/s))^{\circ}C)$ — Sensor bias from temperature $((rad/s))^{\circ}C)$

[0 0 0] (default) | real scalar | real 3-element row vector

Sensor bias from temperature in (rad/s)/°C, specified as a real scalar or 3-element row vector. Any scalar input is converted into a real 3-element row vector where each element has the input scalar value.

Data Types: single | double

Temperature scale factor (%/°C) — Scale factor error from temperature (%/°C)

[0 0 0] (default) | real scalar in the range [0,100] | real 3-element row vector in the range [0,100]

Scale factor error from temperature in %/°C, specified as a real scalar or real 3-element row vector with values ranging from 0 to 100. Any scalar input is converted into a real 3-element row vector where each element has the input scalar value.

Data Types: single | double

Magnetometer

Maximum readings (μT) — Maximum sensor reading (μT)

inf (default) | real positive scalar

Maximum sensor reading in µT, specified as a real positive scalar.

Data Types: single | double

Resolution $((\mu T)/LSB)$ — Resolution of sensor measurements $((\mu T)/LSB)$

0 (default) | real nonnegative scalar

Resolution of sensor measurements in $(\mu T)/LSB$, specified as a real nonnegative scalar.

Data Types: single | double

Constant offset bias (μT) — Constant sensor offset bias (μT)

[0 0 0] (default) | real scalar | real 3-element row vector

Constant sensor offset bias in μT , specified as a real scalar or 3-element row vector. Any scalar input is converted into a real 3-element row vector where each element has the input scalar value.

Data Types: single | double

Axis skew (%) — Sensor axes skew (%)

[0 0 0] (default) | real scalar in the range [0,100] | real 3-element row vector in the range [0,100]

Sensor axes skew in a percentage, specified as a real scalar or 3-element row vector with values ranging from 0 to 100. Any scalar input is converted into a real 3-element row vector where each element has the input scalar value.

Data Types: single | double

White noise PSD $(\mu T/\sqrt{Hz})$ — Power spectral density of sensor noise $(\mu T/\sqrt{Hz})$

[0 0 0] (default) | real scalar | real 3-element row vector

Power spectral density of sensor noise in $\mu T/\sqrt{Hz}$, specified as a real scalar or 3-element row vector. Any scalar input is converted into a real 3-element row vector where each element has the input scalar value.

Data Types: single | double

Bias Instability (μT) — Instability of the bias offset (μT)

[0 0 0] (default) | real scalar | real 3-element row vector

Instability of the bias offset in μ T, specified as a real scalar or 3-element row vector. Any scalar input is converted into a real 3-element row vector where each element has the input scalar value.

Data Types: single | double

Random walk $((\mu T)*\sqrt{Hz})$ — Integrated white noise of sensor $((\mu T)*\sqrt{Hz})$

[0 0 0] (default) | real scalar | real 3-element row vector

Integrated white noise of sensor in $(\mu T)^*\sqrt{Hz}$, specified as a real scalar or 3-element row vector. Any scalar input is converted into a real 3-element row vector where each element has the input scalar value.

Data Types: single | double

Bias from temperature ($\mu T/^{\circ}C$) — Sensor bias from temperature ($\mu T/^{\circ}C$)

[0 0 0] (default) | real scalar | real 3-element row vector

Sensor bias from temperature in μ T/°C, specified as a real scalar or 3-element row vector. Any scalar input is converted into a real 3-element row vector where each element has the input scalar value.

Data Types: single | double

Temperature scale factor (%/°C) — Scale factor error from temperature (%/°C)

[0 0 0] (default) | real scalar in the range [0,100] | real 3-element row vector in the range [0,100]

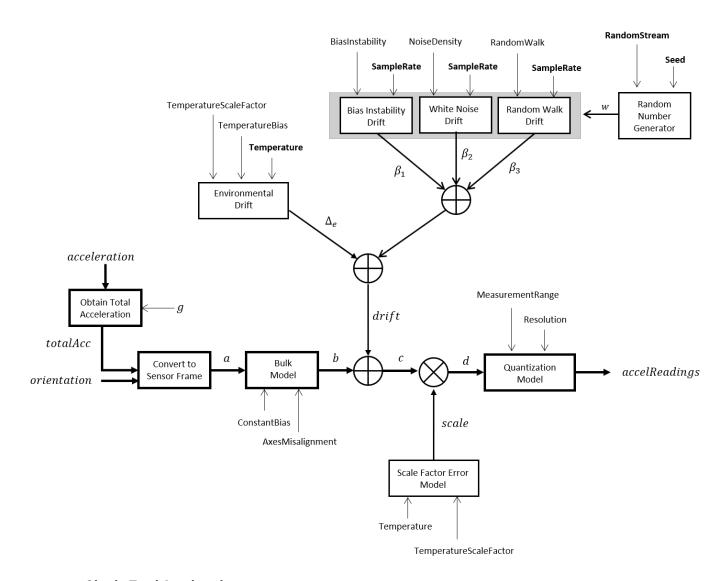
Scale factor error from temperature in %C, specified as a real scalar or real 3-element row vector with values ranging from 0 to 100. Any scalar input is converted into a real 3-element row vector where each element has the input scalar value.

Data Types: single | double

Algorithms

Accelerometer

The accelerometer model uses the ground-truth orientation and acceleration inputs and the imuSensor and accelerams properties to model accelerometer readings.



Obtain Total Acceleration

To obtain the total acceleration (totalAcc), the acceleration is preprocessed by negating and adding the gravity constant vector ($g = [0; 0; 9.8] \text{ m/s}^2$) as:

$$totalAcc = -acceleration + g$$

Convert to Sensor Frame

Then the total acceleration is converted from the local navigation frame to the sensor frame using:

$$a = (orientation)(totalAcc)^T$$

If the orientation is input in quaternion form, it is converted to a rotation matrix before processing.

Bulk Model

The ground-truth acceleration in the sensor frame, *a*, passes through the bulk model, which adds axes misalignment and bias:

$$b = \begin{pmatrix} 1 & \frac{\alpha_2}{100} & \frac{\alpha_3}{100} \\ \frac{\alpha_1}{100} & 1 & \frac{\alpha_3}{100} \\ \frac{\alpha_1}{100} & \frac{\alpha_2}{100} & 1 \end{pmatrix} + \text{ConstantBias}$$

where ConstantBias is a property of accelparams, and α_1 , α_2 , and α_3 are given by the first, second, and third elements of the AxesMisalignment property of accelparams.

Bias Instability Drift

The bias instability drift is modeled as white noise biased and then filtered:

$$\beta_1 = h_1 * (w)$$
(BiasInstability)

where BiasInstability is a property of accelparams, and h_1 is a filter defined by the SampleRate property:

$$H_1(z) = \frac{1}{1 - \frac{1}{2}z^{-1}}$$

White Noise Drift

White noise drift is modeled by multiplying elements of the white noise random stream by the standard deviation:

$$\beta_2 = (w) \left(\sqrt{\frac{\text{SampleRate}}{2}} \right) (\text{NoiseDensity})$$

where SampleRate is an imuSensor property, and NoiseDensity is an accelparams property. Elements of *w* are random numbers given by settings of the imuSensor random stream.

Random Walk Drift

The random walk drift is modeled by biasing elements of the white noise random stream and then filtering:

$$\beta_3 = h_2 * (w) \left(\frac{\text{RandomWalk}}{\sqrt{\frac{\text{SampleRate}}{2}}} \right)$$

where RandomWalk is a property of accelparams, SampleRate is a property of imuSensor, and h_2 is a filter defined as:

$$H_2(z) = \frac{1}{1 - z^{-1}}$$

Environmental Drift Noise

The environmental drift noise is modeled by multiplying the temperature difference from a standard with the temperature bias:

$$\Delta_e$$
 = (Temperature – 25)(TemperatureBias)

where Temperature is a property of imuSensor, and TemperatureBias is a property of accelparams. The constant 25 corresponds to a standard temperature.

Scale Factor Error Model

The temperature scale factor error is modeled as:

$$scaleFactorError = 1 + \left(\frac{\text{Temperature} - 25}{100}\right) (\text{TemperatureScaleFactor})$$

where Temperature is a property of imuSensor, and TemperatureScaleFactor is a property of accelparams. The constant 25 corresponds to a standard temperature.

Quantization Model

The quantization is modeled by first saturating the continuous signal model:

$$e = \begin{cases} \text{MeasurementRange} & \text{if} & d > \text{MeasurementRange} \\ -\text{MeasurementRange} & \text{if} & -d > \text{MeasurementRange} \\ d & \text{else} \end{cases}$$

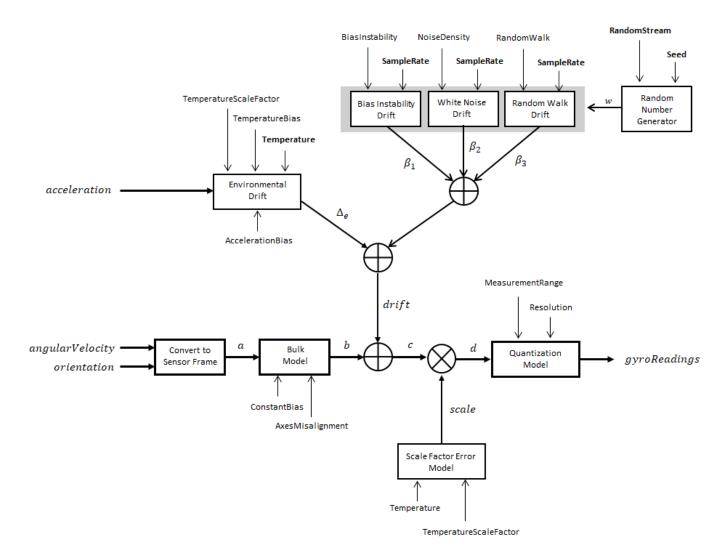
and then setting the resolution:

$$accelReadings = (Resolution) \left(round \left(\frac{e}{Resolution} \right) \right)$$

where MeasurementRange is a property of accelparams.

Gyroscope

The gyroscope model uses the ground-truth orientation, acceleration, and angular velocity inputs, and the imuSensor and gyroparams properties to model accelerometer readings.



Convert to Sensor Frame

The ground-truth angular velocity is converted from the local frame to the sensor frame using the ground-truth orientation:

 $a = (orientation)(angular Velocity)^T$

If the orientation is input in quaternion form, it is converted to a rotation matrix before processing.

Bulk Model

The ground-truth angular velocity in the sensor frame, a, passes through the bulk model, which adds axes misalignment and bias:

$$b = \begin{pmatrix} 1 & \frac{\alpha_2}{100} & \frac{\alpha_3}{100} \\ \frac{\alpha_1}{100} & 1 & \frac{\alpha_3}{100} \\ \frac{\alpha_1}{100} & \frac{\alpha_2}{100} & 1 \end{pmatrix} + \text{ConstantBias}$$

where ConstantBias is a property of gyroparams, and α_1 , α_2 , and α_3 are given by the first, second, and third elements of the AxesMisalignment property of gyroparams.

Bias Instability Drift

The bias instability drift is modeled as white noise biased and then filtered:

$$\beta_1 = h_1 * (w)$$
(BiasInstability)

where BiasInstability is a property of gyroparams and h_1 is a filter defined by the SampleRate property:

$$H_1(z) = \frac{1}{1 - \frac{1}{2}z^{-1}}$$

White Noise Drift

White noise drift is modeled by multiplying elements of the white noise random stream by the standard deviation:

$$\beta_2 = (w) \left(\sqrt{\frac{\text{SampleRate}}{2}} \right) (\text{NoiseDensity})$$

where SampleRate is an imuSensor property, and NoiseDensity is an gyroparams property. The elements of w are random numbers given by settings of the imuSensor random stream.

Random Walk Drift

The random walk drift is modeled by biasing elements of the white noise random stream and then filtering:

$$\beta_3 = h_2 * (w) \left(\frac{\text{RandomWalk}}{\sqrt{\frac{\text{SampleRate}}{2}}} \right)$$

where RandomWalk is a property of gyroparams, SampleRate is a property of imuSensor, and h_2 is a filter defined as:

$$H_2(z) = \frac{1}{1 - z^{-1}}$$

Environmental Drift Noise

The environmental drift noise is modeled by multiplying the temperature difference from a standard with the temperature bias:

$$\Delta_e$$
 = (Temperature – 25)(TemperatureBias)

where Temperature is a property of imuSensor, and TemperatureBias is a property of gyroparams. The constant 25 corresponds to a standard temperature.

Scale Factor Error Model

The temperature scale factor error is modeled as:

$$scaleFactorError = 1 + \left(\frac{\text{Temperature} - 25}{100}\right) (\text{TemperatureScaleFactor})$$

where Temperature is a property of imuSensor, and TemperatureScaleFactor is a property of gyroparams. The constant 25 corresponds to a standard temperature.

Quantization Model

The quantization is modeled by first saturating the continuous signal model:

$$e = \begin{cases} \text{MeasurementRange} & \text{if} & d > \text{MeasurementRange} \\ -\text{MeasurementRange} & \text{if} & -d > \text{MeasurementRange} \\ d & \text{else} \end{cases}$$

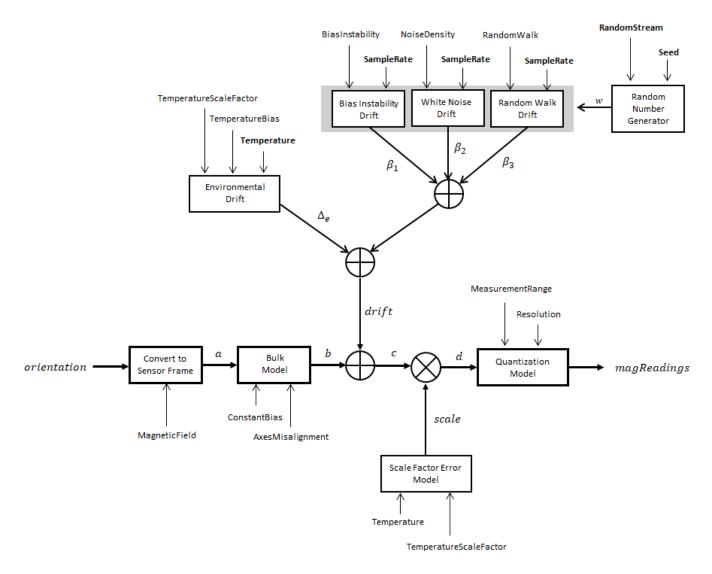
and then setting the resolution:

$$gyroReadings = (Resolution) \left(round \left(\frac{e}{Resolution} \right) \right)$$

where MeasurementRange is a property of gyroparams.

Magnetometer

The magnetometer model uses the ground-truth orientation and acceleration inputs, and the imuSensor and magparams properties to model magnetometer readings.



Convert to Sensor Frame

The ground-truth acceleration is converted from the local frame to the sensor frame using the ground-truth orientation:

$$a = (orientation)(totalAcc)^{T}$$

If the orientation is input in quaternion form, it is converted to a rotation matrix before processing.

Bulk Model

The ground-truth acceleration in the sensor frame, *a*, passes through the bulk model, which adds axes misalignment and bias:

$$b = \begin{pmatrix} 1 & \frac{\alpha_2}{100} & \frac{\alpha_3}{100} \\ \frac{\alpha_1}{100} & 1 & \frac{\alpha_3}{100} \\ \frac{\alpha_1}{100} & \frac{\alpha_2}{100} & 1 \end{pmatrix} + \text{ConstantBias}$$

where ConstantBias is a property of magparams, and α_1 , α_2 , and α_3 are given by the first, second, and third elements of the AxesMisalignment property of magparams.

Bias Instability Drift

The bias instability drift is modeled as white noise biased and then filtered:

$$\beta_1 = h_1 * (w)$$
(BiasInstability)

where BiasInstability is a property of magparams and h_1 is a filter defined by the SampleRate property:

$$H_1(z) = \frac{1}{1 - \frac{1}{2}z^{-1}}$$

White Noise Drift

White noise drift is modeled by multiplying elements of the white noise random stream by the standard deviation:

$$\beta_2 = (w) \left(\sqrt{\frac{\text{SampleRate}}{2}} \right) (\text{NoiseDensity})$$

where SampleRate is an imuSensor property, and NoiseDensity is an magparams property. The elements of *w* are random numbers given by settings of the imuSensor random stream.

Random Walk Drift

The random walk drift is modeled by biasing elements of the white noise random stream and then filtering:

$$\beta_3 = h_2 * (w) \left(\frac{\text{RandomWalk}}{\sqrt{\frac{\text{SampleRate}}{2}}} \right)$$

where RandomWalk is a property of magparams, SampleRate is a property of imuSensor, and h_2 is a filter defined as:

$$H_2(z) = \frac{1}{1 - z^{-1}}$$

Environmental Drift Noise

The environmental drift noise is modeled by multiplying the temperature difference from a standard with the temperature bias:

$$\Delta_e$$
 = (Temperature – 25)(TemperatureBias)

where Temperature is a property of imuSensor, and TemperatureBias is a property of magparams. The constant 25 corresponds to a standard temperature.

Scale Factor Error Model

The temperature scale factor error is modeled as:

$$scaleFactorError = 1 + \left(\frac{\text{Temperature} - 25}{100}\right) (\text{TemperatureScaleFactor})$$

where Temperature is a property of imuSensor, and TemperatureScaleFactor is a property of magparams. The constant 25 corresponds to a standard temperature.

Quantization Model

The quantization is modeled by first saturating the continuous signal model:

$$e = \begin{cases} \text{MeasurementRange} & \text{if} & d > \text{MeasurementRange} \\ -\text{MeasurementRange} & \text{if} & -d > \text{MeasurementRange} \\ d & \text{else} \end{cases}$$

and then setting the resolution:

$$magReadings = (Resolution) \left(round \left(\frac{e}{Resolution} \right) \right)$$

where MeasurementRange is a property of magparams.

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using Simulink® Coder™.

See Also

Classes

accelparams | gyroparams | magparams

Objects

gpsSensor|imuSensor

Introduced in R2020a

INS

Simulate INS sensor

Library: Navigation Toolbox / Multisensor Positioning / Sensor

Models

Sensor Fusion and Tracking Toolbox / Multisensor

Positioning / Sensor Models



Description

The block simulates an INS sensor, which outputs noise-corrupted position, velocity, and orientation based on the corresponding inputs. To change the level of noise present in the output, you can vary the roll, pitch, yaw, position, and velocity accuracies . The accuracy is defined as the standard deviation of the noise.

Ports

Input

Position — Position of INS sensor

N-by-3 matrix of scalar

Position of the INS sensor relative to the navigation frame, specified as an N-by-3 matrix of scalars. N is the number of samples.

Data Types: single | double

Velocity — Velocity of INS sensor

N-by-3 matrix of scalar

Velocity of the INS sensor relative to the navigation frame, specified as an N-by-3 matrix of scalars. N is the number of samples.

Data Types: single | double

Orientation — **Orientation of INS sensor**

3-by-3-by-*N* array of scalar | *N*-by-4 matrix of scalar

Orientation of the INS sensor relative to the navigation frame, specified as either a 3-by-3-by-N array of scalars, where each page of the array (3-by-3 matrix) is a rotation matrix or as an N-by-4 matrix of scalars, where each row of the matrix is the four elements of a quaternion. N is the number of samples.

Data Types: single | double

Output

Position — Position of INS sensor

N-by-3 matrix of scalar

Position of the INS sensor relative to the navigation frame, returned as an N-by-3 matrix of scalars. N is the number of samples in the input.

Data Types: single | double

Velocity — Velocity of INS sensor

N-by-3 matrix of scalar

Velocity of the INS sensor relative to the navigation frame, returned as an N-by-3 matrix of scalars. N is the number of samples in the inputs.

Data Types: single | double

Orientation — **Orientation of INS sensor**

3-by-3-by-*N* array of scalar | *N*-by-4 matrix of scalar

Orientation of the INS sensor relative to the navigation frame, returned either as a 3-by-3-by-N array of scalars, where each page of the array (3-by-3 matrix) is a rotation matrix, or an N-by-4 matrix of scalars, where each row of the matrix is the four elements of a quaternion. The exact type of orientation output follows the type of orientation input. N is the number of samples in the input.

Data Types: single | double

Parameters

Roll (X-axis) Accuracy (deg) — Accuracy of roll measurement (deg)

0.2 (default) | nonnegative real scalar

Accuracy of the roll measurement of the sensor body in degrees, specified as a nonnegative real scalar.

Roll is defined as rotation around the *x*-axis of the sensor body. Roll noise is modeled as white process noise with standard deviation equal to the specified **Roll accuracy** in degrees.

Data Types: single | double

Pitch (Y-axis) Accuracy (deg) — Accuracy of pitch measurement (deg)

0.2 (default) | nonnegative real scalar

Accuracy of the pitch measurement of the sensor body in degrees, specified as a nonnegative real scalar.

Pitch is defined as rotation around the *y*-axis of the sensor body. Pitch noise is modeled as white process noise with standard deviation equal to the specified **Pitch Accuracy** in degrees.

Data Types: single | double

Yaw (Z-axis) Accuracy (deg) — Accuracy of yaw measurement (deg)

1 (default) | nonnegative real scalar

Accuracy of the yaw measurement of the sensor body in degrees, specified as a nonnegative real scalar.

Yaw is defined as rotation around the z-axis of the sensor body. Yaw noise is modeled as white process noise with standard deviation equal to the specified **Yaw Accuracy** in degrees.

Data Types: single | double

Position Accuracy (m) — Accuracy of position measurement (deg)

1 (default) | nonnegative real scalar

Accuracy of the position measurement of the sensor body in meters, specified as a nonnegative real scalar.

Position noise is modeled as white process noise with a standard deviation equal to the specified **Position Accuracy** in degrees.

Data Types: single | double

Velocity Accuracy (m/s) — Accuracy of velocity measurement (deg)

1 (default) | nonnegative real scalar

Accuracy of the velocity measurement of the sensor body in meters per second, specified as a nonnegative real scalar.

Velocity noise is modeled as white process noise with a standard deviation equal to the specified **Velocity Accuracy** in degrees.

Data Types: single | double

Intial Seed — Initial seed for randomization

67 (default) | nonnegative integer

Initial seed of a random number generator algorithm, specified as a nonnegative integer.

Data Types: single | double

Simulate using — Type of simulation to run

Interpreted Execution (default) | Code Generation

- Interpreted execution Simulate the model using the MATLAB interpreter. This option shortens startup time. In Interpreted execution mode, you can debug the source code of the block.
- Code generation Simulate the model using generated C code. The first time that you run a simulation, Simulink generates C code for the block. The C code is reused for subsequent simulations if the model does not change. This option requires additional startup time.

See Also

IMU | insSensor

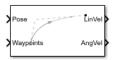
Introduced in R2020b

Pure Pursuit

Linear and angular velocity control commands

Library:

Robotics System Toolbox / Mobile Robot Algorithms Navigation Toolbox / Control Algorithms



Description

The Pure Pursuit block computes linear and angular velocity commands for following a path using a set of waypoints and the current pose of a differential drive vehicle. The block takes updated poses to update velocity commands for the vehicle to follow a path along a desired set of waypoints. Use the **Max angular velocity** and **Desired linear velocity** parameters to update the velocities based on the performance of the vehicle.

The **Lookahead distance** parameter computes a look-ahead point on the path, which is an instantaneous local goal for the vehicle. The angular velocity command is computed based on this point. Changing **Lookahead distance** has a significant impact on the performance of the algorithm. A higher look-ahead distance results in a smoother trajectory for the vehicle, but can cause the vehicle to cut corners along the path. Too low of a look-ahead distance can result in oscillations in tracking the path, causing unstable behavior. For more information on the pure pursuit algorithm, see "Pure Pursuit Controller".

Input/Output Ports

Input

Pose — Current vehicle pose

[x y theta] vector

Current vehicle pose, specified as an [x y theta] vector, which corresponds to the x-y position and orientation angle, *theta*. Positive angles are measured counterclockwise from the positive x-axis.

Waypoints — Waypoints

[] (default) | n-by-2 array

Waypoints, specified as an n-by-2 array of [x y] pairs, where n is the number of waypoints. You can generate the waypoints using path planners like mobileRobotPRM or specify them as an array in Simulink.

Output

LinVel — Linear velocity

scalar in meters per second

Linear velocity, specified as a scalar in meters per second.

Data Types: double

AngVel — **Angular velocity**

scalar in radians per second

Angular velocity, specified as a scalar in radians per second.

Data Types: double

TargetDir — Target direction for vehicle

scalar in radians

Target direction for the vehicle, specified as a scalar in radians. The forward direction of the vehicle is considered zero radians, with positive angles measured counterclockwise. This output can be used as the input to the **TargetDir** port for the Vector Field Histogram block.

Dependencies

To enable this port, select the **Show TargetDir output port** parameter.

Parameters

Desired linear velocity (m/s) — Linear velocity

0.1 (default) | scalar

Desired linear velocity, specified as a scalar in meters per second. The controller assumes that the vehicle drives at a constant linear velocity and that the computed angular velocity is independent of the linear velocity.

Maximum angular velocity (rad/s) — Angular velocity

1.0 (default) | scalar

Maximum angular velocity, specified as a scalar in radians per second. The controller saturates the absolute angular velocity output at the given value.

Lookahead distance (m) — Look-ahead distance

1.0 (default) | scalar

Look-ahead distance, specified as a scalar in meters. The look-ahead distance changes the response of the controller. A vehicle with a higher look-ahead distance produces smooth paths but takes larger turns at corners. A vehicle with a smaller look-ahead distance follows the path closely and takes sharp turns, but oscillate along the path. For more information on the effects of look-ahead distance, see "Pure Pursuit Controller".

Show TargetDir output port — Target direction indicator

off (default) | on

Select this parameter to enable the **TargetDir** out port. This port gives the target direction as an angle in radians from the forward position, with positive angles measured counterclockwise.

Extended Capabilities

C/C++ Code Generation

Generate C and C++ code using Simulink® Coder™.

See Also

Blocks

Vector Field Histogram

Classes

binaryOccupancyMap|binaryOccupancyMap|controllerVFH|occupancyMap| occupancyMap

Topics

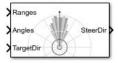
"Plan Path for a Differential Drive Robot in Simulink" (Robotics System Toolbox)
"Path Following with Obstacle Avoidance in Simulink®"
"Pure Pursuit Controller"

Introduced in R2019b

Vector Field Histogram

Avoid obstacles using vector field histogram

Library: Navigation Toolbox / Control Algorithms



Description

The Vector Field Histogram (VFH) block enables your vehicle to avoid obstacles based on range sensor data. Given a range sensor reading in terms of ranges and angles, and a target direction to drive toward, the VFH controller computes an obstacle-free steering direction.

For more information on the algorithm details, see "Vector Field Histogram" on page 4-44 under Algorithms.

Limitations

• The Ranges and Angles inputs are limited to 4000 elements when generating code for models that use this block.

Input/Output Ports

Input

Ranges — Range values from scan data

vector of scalars

Range values from scan data, specified as a vector of scalars in meters. These range values are distances from a sensor at specified angles. The vector must be the same length as the corresponding **Angles** vector.

Angles — Angle values from scan data

vector of scalars

Angle values from scan data, specified as a vector of scalars in radians. These angle values are the specific angles of the specified ranges. The vector must be the same length as the corresponding **Ranges** vector.

TargetDir — Target direction for vehicle

scalar

Target direction for the vehicle, specified as a scalar in radians. The forward direction of the vehicle is considered zero radians, with positive angles measured counterclockwise. You can use the **TargetDir** output from the Pure Pursuit block when generating controls from a set of waypoints.

Output

steeringDir — Steering direction for vehicle

scalar

Steering direction for the vehicle, specified as a scalar in radians. This obstacle-free direction is calculated based on the VFH+ algorithm. The forward direction of the vehicle is considered zero radians, with positive angles measured counterclockwise.

Parameters

Main

Number of angular sectors — Number of bins used to create the histograms 180 (default) | scalar

Number of bins used to create the histograms, specified as a scalar. This parameter is nontunable. You can set this parameter only when the object is initialized.

Range distance limits (m) — Limits for range readings

[0.05 2] (default) | two-element vector of scalars

Limits for range readings in meters, specified as a two-element vector of scalars. The range readings input are only considered if they fall within the distance limits. Use the lower distance limit to ignore false positives from poor sensor performance at lower ranges. Use the upper limit to ignore obstacles that are too far away from the vehicle.

Histogram thresholds — Thresholds for computing binary histogram

[3 10] (default) | two-element vector of scalars

Thresholds for computing binary histogram, specified as a two-element vector of scalars. The algorithm uses these thresholds to compute the binary histogram from the polar obstacle density. Polar obstacle density values higher than the upper threshold are represented as occupied space (1) in the binary histogram. Values smaller than the lower threshold are represented as free space (0). Values that fall between the limits are set to the values of a previous computed binary histogram if one exists from previous iterations. If a previous histogram does not exist, the value is set as free space (0).

vehicle radius (m) - Radius of the vehicle

0.1 (default) | scalar

Radius of the vehicle, specified as a scalar in meters. This dimension defines the smallest circle that can circumscribe your vehicle. The vehicle radius is used to account for vehicle size when computing the obstacle-free direction.

Safety distance (m) — Safety distance around the vehicle

0.1 (default) | scalar

Safety distance left around the vehicle position in addiction to **vehicle radius**, specified as a scalar in meters. The vehicle radius and safety distance are used to compute the obstacle-free direction.

Minimum turning radius (m) — Minimum turning radius at current speed

0.1 (default) | scalar

Minimum turning radius for the vehicle moving at its current speed, specified as a scalar in meters.

Simulate using — Specify type of simulation to run

Code generation (default) | Interpreted execution

- Code generation Simulate model using generated C code. The first time you run a simulation, Simulink generates C code for the block. The C code is reused for subsequent simulations, as long as the model does not change. This option requires additional startup time but the speed of the subsequent simulations is comparable to Interpreted execution.
- Interpreted execution Simulate model using the MATLAB interpreter. This option shortens startup time but has a slower simulation speed than Code generation. In this mode, you can debug the source code of the block.

Tunable: No

Cost Function Weights

Target direction weight — Cost function weight for target direction

5 (default) | scalar

Cost function weight for moving toward the target direction, specified as a scalar. To follow a target direction, set this weight to be higher than the sum of **Current direction weight** and **Previous direction weight**. To ignore the target direction cost, set this weight to 0.

Current direction weight — Cost function weight for current direction

2 (default) | scalar

Cost function weight for moving the vehicle in the current heading direction, specified as a scalar. Higher values of this weight produce efficient paths. To ignore the current direction cost, set this weight to θ .

Previous direction weight — Cost function weight for previous direction

2 (default) | scalar

Cost function weight for moving in the previously selected steering direction, specified as a scalar. Higher values of this weight produce smoother paths. To ignore the previous direction cost, set this weight to θ .

Algorithms

Vector Field Histogram

The block uses the VFH+ algorithm to compute the obstacle-free direction. First, the algorithm takes the ranges and angles from range sensor data and builds a polar histogram for obstacle locations. Then, it uses the input histogram thresholds to calculate a binary histogram that indicates occupied and free directions. Finally, the algorithm computes a masked histogram, which is computed from the binary histogram based on the minimum turning radius of the vehicle.

The algorithm selects multiple steering directions based on the open space and possible driving directions. A cost function, with weights corresponding to the previous, current, and target directions, calculates the cost of different possible directions. The algorithm then returns an obstacle-free direction with minimal cost. Using the obstacle-free direction, you can input commands to move your vehicle in that direction.

To use this block for your own application and environment, you must tune the algorithm parameters. Parameter values depend on the type of vehicle, the range sensor, and the hardware you use. For more information on the VFH algorithm, see controllerVFH.

See Also

Blocks

Publish | Pure Pursuit | Subscribe

Classes

controllerVFH

Topics

"Vector Field Histogram"

Introduced in R2019b

Apps

SLAM Map Builder

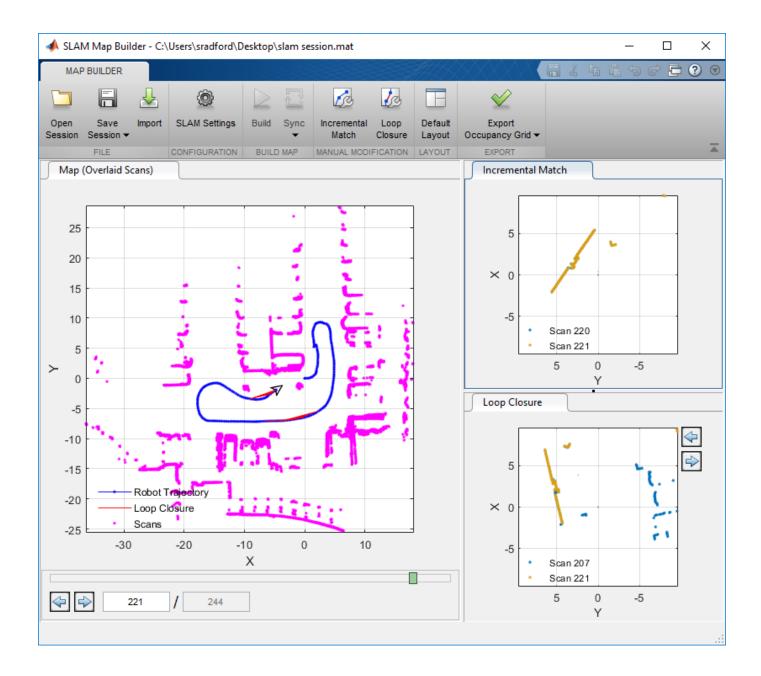
Build 2-D grid maps using lidar-based SLAM

Description

The **SLAM Map Builder** app loads recorded lidar scans and odometry sensor data to build a 2-D occupancy grid using simultaneous localization and mapping (SLAM) algorithms. Incremental scan matching aligns and overlays scans to build the map. Loop closure detection adjusts for drift of the vehicle odometry by detecting previously visited locations and adjusting the overall map. Sometimes, the scan matching algorithm and loop closure detection require manual adjustment. Use the app to manually align scans and modify loop closures to improve the overall map accuracy. You can also tune the SLAM algorithm settings to improve the automatic map building.

To use the app:

Import	To load rosbag log files, select Import > Import from rosbag . Select the rosbag file and click Open . This opens the Import tab. For more information, see Import and Filter a rosbag on page 5-13. To load data from the workspace, Import > Import from workspace . Select your Scans and Poses variables using the drop downs provided. You can also specify the variables in the slamMapBuilder function. See Programmatic Use on page 5-12.
SLAM Settings	Use SLAM Settings to adjust the SLAM algorithm settings. Default values are provided, but your specific sensors and data may require tuning of these settings. The most important value to tune is the Loop Closure Threshold . For more information, see Tune SLAM Settings on page 5-13.
Build	Click Build to begin the SLAM map building process. The building process aligns scans in the map using incremental scan matching, identifies loop closures when visiting previous locations, and adjusts poses. Click Pause at any time during the map building process to manually align incremental scans or modify loop closures.
Incremental Loop Match Closure	Click Incremental Match to modify the relative pose of the currently selected frame and align the scan with the previous scan. Click Loop Closure to modify or ignore the detected loop closure for the current frame. Use the slider on the bottom to scroll back to areas where scan matching or loop closures are not accurate. You can modify any number of scans or loop closures. For more information, see Modify Increment Scans and Loop Closures on page 5-14.
Sync	After modifying your map, click Sync to update all the poses in the scan map. The two options under Sync are Sync , which searches for new loop closures, or Sync Fast , which skips loop closure searching and just updates the scan map. For more information, see Sync the Map on page 5-15.
Export Occupancy Grid ▼	When you are satisfied with how the map looks, click Export to OccupancyGrid to either export the map to an m-file or save the map in the workspace. The map is output as a 2-D probabilistic occupancy grid in an occupancyMap object.
Open Save Session Session ▼	You can open existing app sessions you have saved using Open Session . When you are in the Map Builder tab, you can save your progress to an m-file using Save Session .



Open the SLAM Map Builder App

- MATLAB Toolstrip: On the Apps tab, under Control System Design and Analysis, click **SLAM Map Builder**.
- MATLAB Command Window: Enter slamMapBuilder

Examples

Build and Tune a Map Using Lidar Scans with SLAM

The **SLAM Map Builder** app helps you build an occupancy grid from lidar scans using simultaneous localization and mapping (SLAM) algorithms. The map is built by estimating poses through scan matching and using loop closures for pose graph optimization. This example shows you the workflow for loading a rosbag of lidar scan data, filtering the data, and building the map. Tune the scan map by adjusting incremental scan matches and modifying loop closures.

Load Lidar Scan Data

Load the example .mat file into the workspace, which contains a variable, scans, as a cell array of lidarScan objects.

load slamLidarScans.mat

Open the App

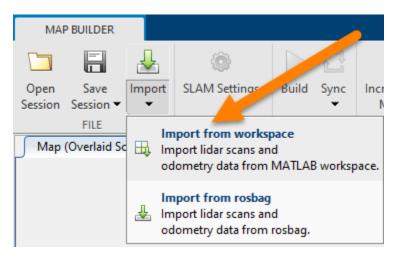
In the Apps tab, under Control System Design and Analysis, click SLAM Map Builder.

Also, you can call the slamMapBuilder function:

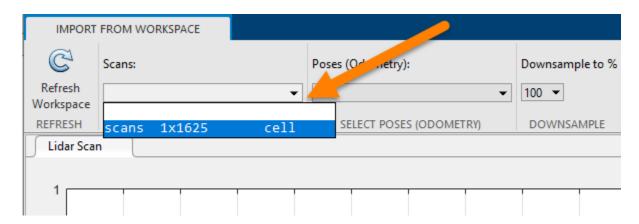
slamMapBuilder

Import Lidar Scans

Click **Import > Import from workspace** to load the scans. Data stored as a rosbag can be loaded with a ROS Toolbox license.



Select the scans variable in the Scans drop down.



In the tool bar, set **Downsample to (%)** to 10. Downsampling evenly samples from the data to reduce computation time for the SLAM algorithm. For this example, 10% is every 5th scan. Click **Apply**.

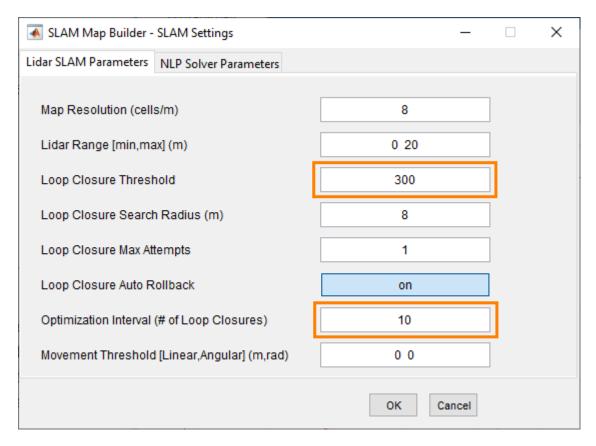
Use the slider or arrow keys at the bottom to preview the scans.



Once you are done importing, click Close.

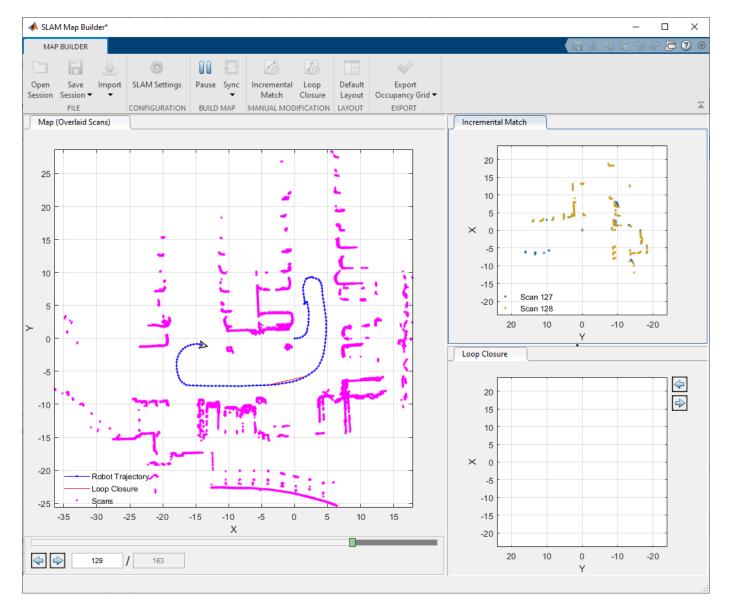
Tune SLAM Settings

The SLAM algorithm can be tuned using the **SLAM Settings** dialog. The parameters should be adjusted based on your sensor specifications, the environment, and your application. For this example, increase **Loop Closure Threshold** from 200 to 300. This increased threshold decreases the likelihood of accepting and using a detected loop closure. Set the **Optimization Interval** to 10. With every 10th loop closure accepted, the pose graph is optimized to account for drift.



Build the Map

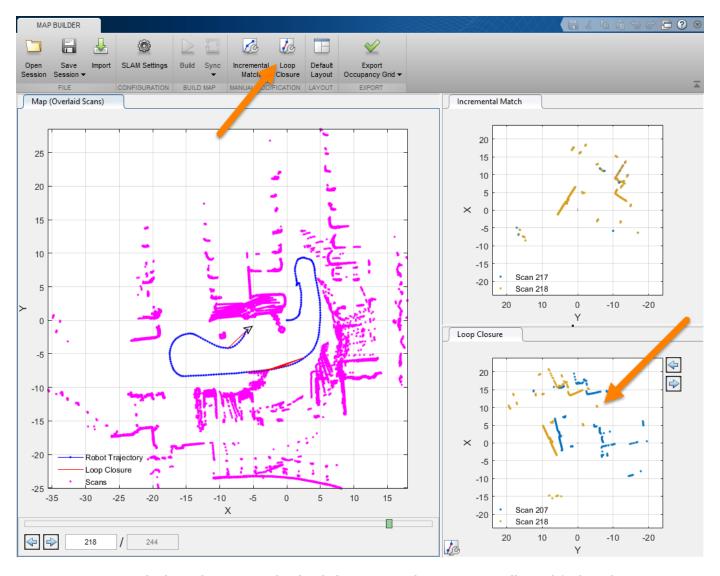
After filtering your data and setting the SLAM algorithm settings, click **Build**. The app begins processing scans to build the map. You should see the slider progressing and scans being overlaid in the map. The estimated robot trajectory is plotted on the same scan map. Incremental scan matches are shown in the **Incremental Match** pane. Whenever a loop closure is detected, the **Loop Closure** pane shows the two scans overlaid on each other.



Adjust Scan Matches or Loop Closures

At any time during the build process, if you notice the map is distorted or an incremental match or loop closure looks off, click **Pause** to select scans for adjustment. You can modify scans at the end of the build process as well. Navigate using the arrow keys or slider to the point in the file where the distortion first occurs. Click the **Incremental Match** or **Loop Closure** buttons to adjust the currently displayed scan poses. In this section, the bad loop closure is artificial and only for illustration purposes.

Click the **Loop Closure** button. This opens a tab for modifying the loop closure relative pose.

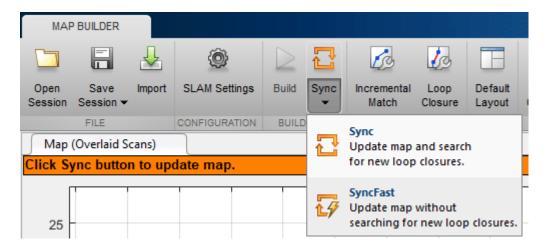


To ignore the loop closure completely, click **Ignore**. Otherwise, manually modify the relative scan pose until the scans line up.

Click **Pan Scan** or **Rotate Scan**, then click and drag in the figure to align the two scans. Click **Accept** when you are done. You can do this for multiple scans.

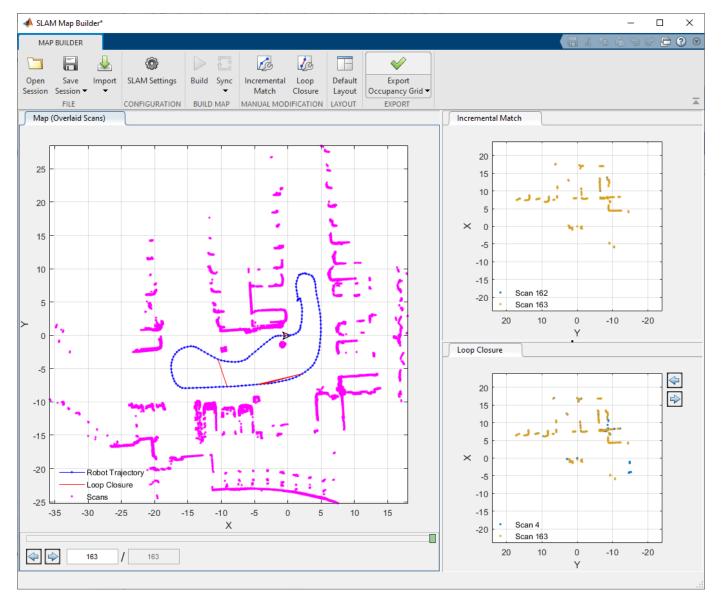


After you modify your scan poses for incremental matches and loop closures, click **Sync** to apply changes. **SyncFast** updates the map without searching for new loop closures and reduces computation time if you have already processed all the scans.



Export Occupancy Grid

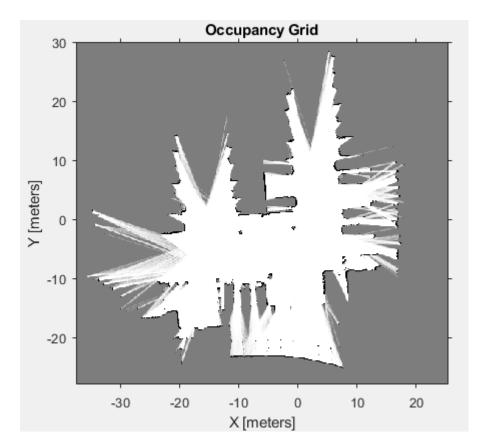
Once you have synced your changes and finished building the map, you should see a fully overlaid scan map with a robot trajectory.



Click **Export Occupancy Grid** to get a final occupancy map of your environment as a occupancyMap object. Specify the variable name to export the map to the workspace. You can create a map from a subset of scans by scrolling back to the desired frame before exporting and selecting **Up to currently selected scan**.

Call show on the stored map to visualize the occupancy map.

show(my0ccMap)



You can also save a SLAM Map Builder app session using the **Save Session** button. The app writes the current state of the app to a .mat file that can be loaded later using **Open Session**.

- "Implement Simultaneous Localization And Mapping (SLAM) with Lidar Scans"
- "Implement Online Simultaneous Localization And Mapping (SLAM) with Lidar Scans"

Programmatic Use

slamMapBuilder(bag) opens the **SLAM Map Builder** app and imports the rosbag log file specified in bag, a BagSelection object created using the rosbag function. The app opens to the **Import** tab to filter the sensor data in your rosbag.

slamMapBuilder(sessionFile) opens the **SLAM Map Builder** app from a saved session file name, sessionFile. An app session file is created through the **Save Session** button in the app toolstrip.

slamMapBuilder(scans) opens the **SLAM Map Builder** app and imports the scans specified in scans, a cell array of lidarScan objects. The app assumes you have prefiltered your scans and skips the import process. Click **Build** to start building the map.

slamMapBuilder(scans, poses) opens the **SLAM Map Builder** app and imports the scans and poses. scans is specified as a cell array of lidarScan objects. poses is a matrix of [x y theta] vectors that correspond to the poses of scans. The app assumes you have prefiltered your scans and skips the import process. Click **Build** to start building the map.

More About

Import and Filter a rosbag

When you click the **Import** button, specify the parameters for your rosbag and how you want to filter the data in the toolstrip. You must **Apply** your settings to see the scans updated in the figures.

- Select the ROS topic for the lidar scans and odometry (if available).
- In **Odom Topic**, if you select **Use TF**, specify the frame of the lidar scan sensor, **Lidar Frame**, and the base fixed frame of the vehicle, **Fixed Frame**. The items in the drop down menu are generated based on the available frames in the tf transformation tree of the rosbag.
- Specify the **Start Time** and **End Time** if you want to trim data from rosbag. You can use the sliders or manually type in your time values.
- Select the desired downsample percentage of scans in **Downsample Scans**. This evenly
 downsamples the scans based on the percentage. For example, a value of 25% would only select
 every fourth scan.
- Click **Apply** to see the new filtered scans and apply all settings. **Close** the tab when you are done.

If you'd like more control over filtering scans in the rosbag, import your rosbag into MATLAB using rosbag. Filter the rosbag using select. To open the app using your custom filtered rosbag, see Programmatic Use on page 5-12.

Tune SLAM Settings

To improve the automatic map building process, the SLAM algorithm has tunable parameters. Click **SLAM Settings** to tune the parameters. Use **Lidar SLAM Parameters** to affect different aspects of the scan alignment and loop closure detection processes. Also, tune the **NLP Solver Parameters** to change how the map optimization algorithm improves the overall map based on loop closures.

Lidar SLAM Parameters:

- **Map Resolution (cells/m)** Resolution of the map. The resolution affects the location accuracy of the scan alignment and defines the output size of the occupancy grid.
- **Lidar Range [min,max] (m)** -- Range of lidar sensor readings. When processing the lidar scans, readings outside of the lidar range are ignored.
- **Loop Closure Threshold** Unitless threshold for accepting loop closures. Depending on your lidar scans, the average loop closure score varies. If the build process does not find loop closures and the vehicle revisits locations in the map, consider lowering this threshold.
- Loop Closure Search Radius (m) -- Radius to search for loop closures. Based on the odometry
 pose, the algorithm searches for loop closures in the existing map within the given radius in
 meters.
- Loop Closure Max Attempts -- Number of attempts at finding loop closures. When this number increases, the algorithm makes more attempts to find loop closures in the map but increases computation time.
- **Loop Closure Auto Rollback** Allow automatic rejection of loop closures. The algorithm tracks the residual error from the map optimization. If it detects a sudden change in the error and this parameter is set to on, the loop closure is rejected.
- **Optimization Interval (# of Loop Closures)** Number of detected loop closures accepted to trigger optimization. By default, the map is optimized with every loop closure found.

• Movement Threshold [Linear, Angular] (m, rad) -- Minimum change in pose required to accept a new scan. If the pose of the vehicle does not exceed this threshold, the next scan is discarded from the map building process.

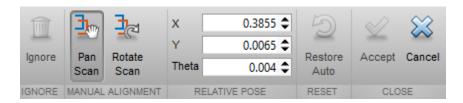
NLP Solver Parameters:

- Max Iterations -- Maximum number of iterations for map optimization. Increasing this value may improve map accuracy but increases computation time.
- Max Time (s) -- Maximum time allowed for map optimization specified in seconds. Increasing this value may improve map accuracy but increases computation time.
- **Gradient Tolerance** -- Lower bound on the norm of the gradient of the cost function for optimization. Lowering this value causes the optimization to run longer to search for a local minimum but increases the computation time.
- **Function Tolerance** -- Lower bound on the change in the cost function for optimization. Lowering this value causes the optimization to run longer to search for a local minimum but increases the computation time.
- Step Tolerance -- Lower bound on the step size for optimization. Lowering this value causes the optimization to run longer to search for a local minimum but increases the computation time.
- First Node Pose [x,y,theta] (m,rad) -- Pose of the first node in the graph. If you need to offset the position of the scans in the map, specify the position, [x y], in meters and orientation, theta. in radians.

After changing any of these settings, the map building process must be restarted to rebuild the map with the new parameters.

Modify Incremental Matches and Loop Closures

This app allows you to manually modify incremental scans and adjust detected loop closures. If you notice scans are not properly aligned after you build the map, use the Incremental Match and Loop **Closure** buttons to open their modification tabs. Use the modification toolstrip buttons to adjust the relative pose between scans.



- **Ignore** -- When modifying loop closures, you can simply ignore loop closures if they are inaccurate. The algorithm always discards ignored loop closure if detected in the same app session. You cannot ignore incremental scan matches.
- Pan Scan -- Click this button to manually shift the pose. After selecting, click and drag inside the map to shift the scans and overlay them properly. Align all the points of the scans until you are satisfied. You can manually specify the X, Y location in the Relative Pose section as well.
- Rotate Scan -- Click this button to manually rotate the pose. After selecting, click and drag inside the map to rotate the scans and overlay them properly. Align all the points of the scans until you are satisfied. You can manually specify the **Theta** location in the **Relative Pose** section as well.

Sync the Map

After making modifications to the map building process using **Incremental Scans** and **Loop Closures**, you must sync the map to apply the changes. Based on the changes you make to properly align scans, the overall map shifts and alignments change for every scan after your modification. You have two options after making your modifications, **Sync** or **Sync Fast**. If you click **Sync Fast**, the changes to the poses are automatically applied and no other changes to the map occur. **Sync** restarts the entire map building and loop closure detection processes starting at the first modification. The specified modifications are applied, but the algorithm attempts to realign other scans and search for new loop closures as well.

See Also

Functions

buildMap | matchScans | matchScansGrid | optimizePoseGraph | rosbag

Objects

lidarSLAM | lidarScan | occupancyMap | poseGraph

Topics

"Implement Simultaneous Localization And Mapping (SLAM) with Lidar Scans"

"Implement Online Simultaneous Localization And Mapping (SLAM) with Lidar Scans"

Introduced in R2019b